

# **Effect of Positron Polarization on $P_{\text{eff}}$ , $\delta(P_{\text{eff}})$ and W-pair Background Suppression**

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## **4. $P_{\text{eff}}$**

When both beams are polarized, an effective polarization can be defined for  $A_{LR}$  measurements relevant for s-channel vector exchange,

$$P_{\text{eff}} = \frac{P_- + P_+}{1 + P_- P_+},$$

where  $P_-$  and  $P_+$  are absolute values of the electron and positron polarization respectively.

The benefit of positron polarization can be seen in Table 1. If we define a Figure-of-Merit, FOM, to be  $(P_{\text{eff}}/P_-)^2$ , then 30% positron polarization increases the FOM by 23% (10%) for  $P_-$ =80%(90%).

**Table 1:  $P_{\text{eff}}$**

$P_-$	$P_+$	$P_{\text{eff}}$	FOM
0.8	0.3	0.887	1.23
0.8	0.6	0.946	1.40
0.9	0.3	0.945	1.10
0.9	0.6	0.974	1.17

## 5. $\delta(P_{\text{eff}})$

The uncertainty in  $P_{\text{eff}}$  is reduced compared to the uncertainty in  $P_-$  and  $P_+$  given from the polarimeters. This is summarized in Table 2, where I assume 0.25% polarimetry uncertainties on both the electron and positron polarimeters. Substantial improvements in the precision on  $A_{LR}$  measurements is achieved with 30% positron polarization.

$$\frac{\partial P_{\text{eff}}}{\partial P_-} = \frac{1 - P_+^2}{(1 + P_- P_+)^2}, \quad \frac{\partial P_{\text{eff}}}{\partial P_+} = \frac{1 - P_-^2}{(1 + P_- P_+)^2}$$

**Table 2:  $\delta(P_{\text{eff}})$**

$P_-$	$P_+$	$\delta(P_{\text{eff}})/P_{\text{eff}}$
0.8	0.3	0.16%
0.8	0.6	0.08%
0.9	0.3	0.14%
0.9	0.6	0.07%

## 6. W-pair Background suppression

The production cross section for W-pairs for

- i. Left-polarized electrons and right-polarized positrons, is  
 $\sigma_1 \approx (1 + P_-)(1 + P_+) \sigma_{LR}$
- ii. Right-polarized electrons and left-polarized positrons, is  
 $\sigma_2 \approx (1 - P_-)(1 - P_+) \sigma_{LR}$

A FOM for background suppression studies can be defined as

FOM =  $\sigma_1/\sigma_2$ . Table 3 summarizes these FOM. A substantial improvement is achieved with 30% positron polarization.

**Table 3: FOM W-pair background suppression**

$P_-$	$P_+$	FOM
0.8	0	9
0.8	0.3	17
0.8	0.6	36
0.9	0	19
0.9	0.3	35
0.9	0.6	76