

Total hadronic cross-sections: from LHC to ILC

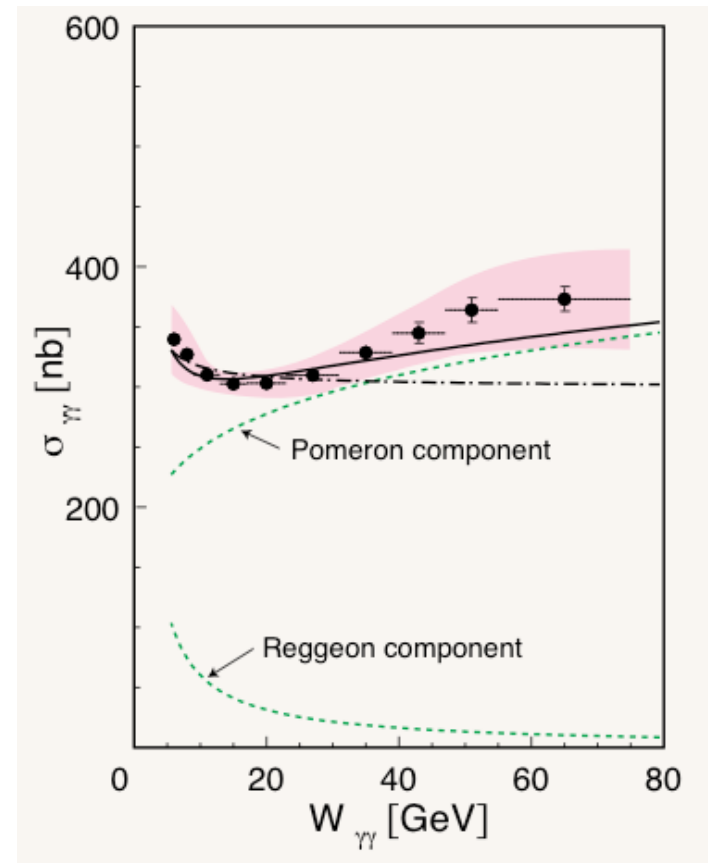
[Giulia Pancheri - INFN-Frascati]

Presented by M. Krawczyk



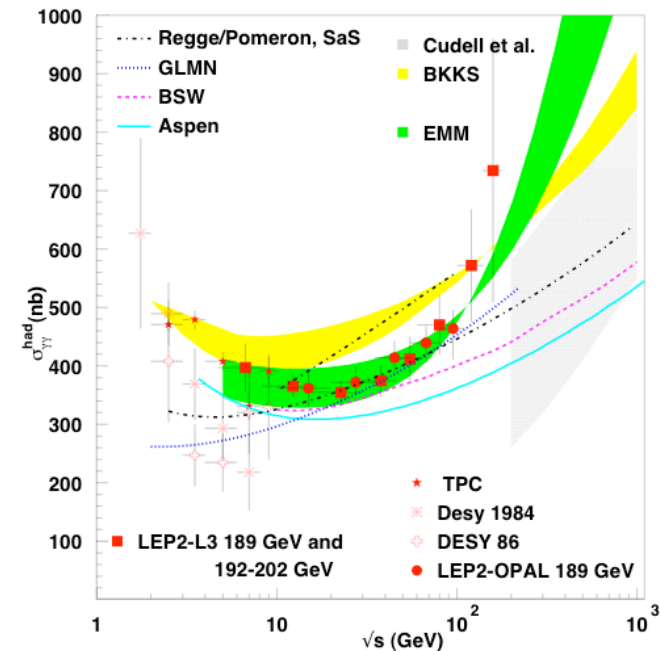
QCD tests

- Models for total cross-section



Models for total cross-section

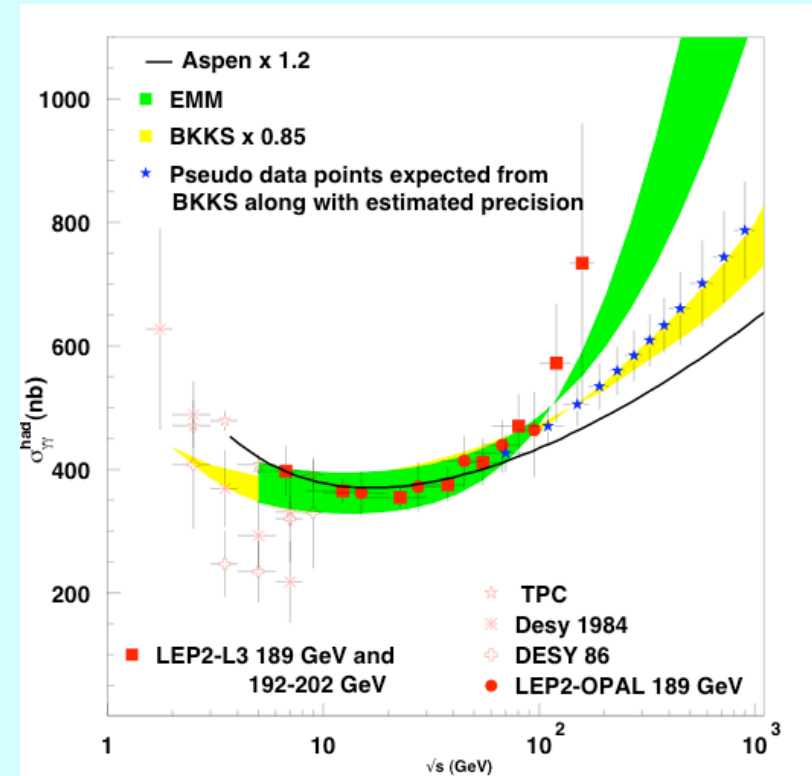
- The interest lies in QCD role
- What is the Pomeron?
The Reggeon?
- Are these concepts universal?
- Or do they just phenomenologically describe our ignorance?
- How can ILC help ?



A.de Roeck, R. Godbole, A. Grau, G.Pancheri,
JHEP 2003

S^ε : Should ε be the same for all hadronic cross-sections?

- **Yes if the model**
 - is based on Regge poles and a universal Pomeron pole exchange
$$\sigma = Bs^{-\eta} + As^\varepsilon$$
- **Not necessarily if**
 - The model has some connection with QCD and parton densities play a role



A fit to LEP data shows that ε is not the same for proton and photon cross-sections

$$\sigma = B s^{-\eta} + A s^{\varepsilon} + C s^{\varepsilon_1}$$

- Fit3

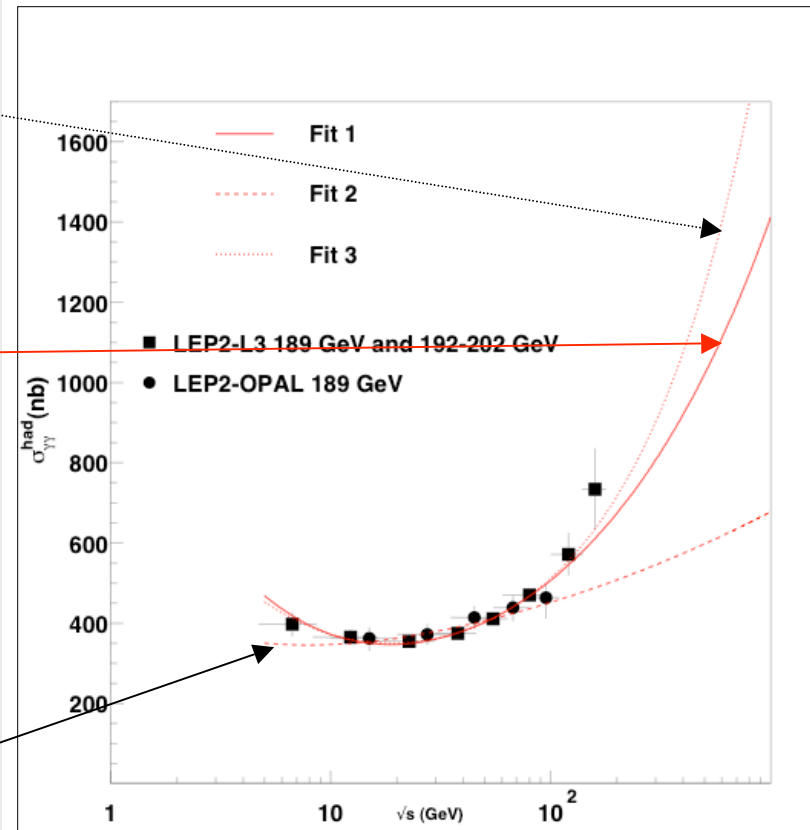
$C \neq 0$ $\varepsilon = 0.093$
 $\varepsilon_1 = 0.418$

- **Fit 1**

$C = 0$ $\varepsilon = 0.250$

- Fit2

$C = 0$ $\varepsilon = 0.093$ as in pp



A realistic QCD model should relate the fit to QCD phenomenological inputs quantities like densities etc.


The Bloch-Nordsieck Eikonal Minijet model includes k_+ resummation

R.Godbole, A. Grau, G.Pancheri, Y.Srivastava PRD 2005
A. Corsetti, A. Grau, G.Pancheri, Y. Srivastava PLB 1996

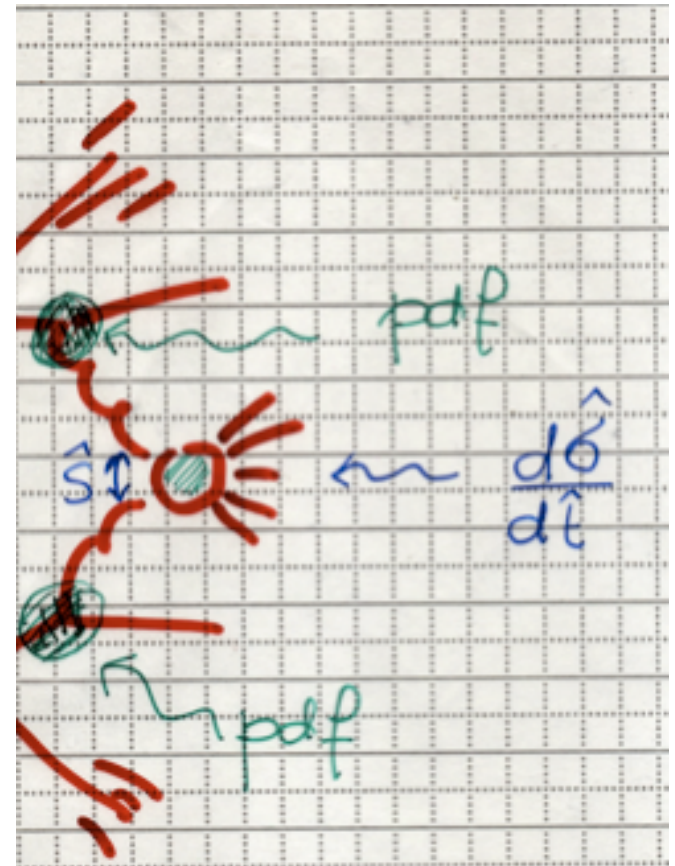
1. Multiple parton interactions : optical theorem and **eikonal** representation for $T_{el}(s,t)$
2. Hard scattering to drive the **rise due to $1/x$**
3. **Soft gluons** down to zero momentum to **tame** the rise

The hard cross-section

- Mini-jet cross-section



$\Sigma \int$ densities $\int dp_t \frac{d\hat{\sigma}}{dp_t}$



In all mini-jet models densities make all the difference between photon and proton processes

Proton-proton and proton-antiproton

Most commonly used densities

- GRV
- CTEQ
- MRST

γ -proton and $\gamma\gamma$

Most commonly used densities

- GRV
- GRS
- CJKL

Soft resummation

Probability of total K_T from infinite # of soft gluons

$$\int d^2b e^{iK_T b} \exp\{-\int d^3n(k)[1-e^{-ik_t b}]\}$$

depends upon single gluon energy

- maximum : use Kinematics
- **minimum : 0** from Bloch-Nordsieck theorem

Role of resummation

An **infinite** number of soft quanta

- down to **zero momentum** but how?
next slides
- Up to an energy dependent limit q_{\max}
 - Higher hadron energy \Rightarrow possibility
of more small x partons with “high energy”
($\approx 1-2$ GeV) \Rightarrow higher q_{\max}

Maximum soft gluon energy

- q_1 and q_2 : any two partons
- X : the 2-jet final state
- $Q^2 \geq 4 p_{tmin}^2$
- q_{max} depends on X_1, X_2
- We average over densities

$$q_1 + q_2 \rightarrow g + X$$

$$q_{max} = \max\{R_t\} = \frac{\sqrt{\hat{S}}}{2} \left(1 - \frac{Q^2}{\hat{S}}\right)$$

$$\hat{S} = (q_1 + q_2)^2$$

$$Q^2 = X^2$$

*Chiappetta, Greco
1981*

Zero momentum quanta

- **Soft** gluons need to be resummed if they are indeed soft $\approx 1/k$
- **Resummation** implies **integration** over dk_t
- What matters will be $\int \alpha_s(k_t) dk_t f(k_t)$ and not $\alpha_s(0)$

Models for infrared behaviour

$$\alpha_s^{\text{FROZEN}}(R_t) = \frac{\text{constant}}{\ln\left(a^2 + \frac{R_t^2}{\Lambda^2}\right)} \xrightarrow{R_t \rightarrow 0} \frac{\text{const}}{\ln a^2}$$

$$\alpha_s^{\text{sing}}(R_t) = \frac{c}{\ln\left(1 + \left(\frac{R_t}{\Lambda}\right)^{2p}\right)} \sim \frac{1}{R_t^{2p}}$$

↑
integrable

Soft gluons give b-distributions

In eikonal representation

$$\sigma_{\text{tot}} \approx 2 \int d^2b [1 - e^{-n(b,s)/2}]$$

- $n(b,s)$ = average # of collisions at distance b , at energy \sqrt{s}
- b-distribution is needed

Our ansatz:

b-distribution =
Fourier transform of soft gluon K_t distribution

Resummation of soft gluons down to $k_{\perp}=0$

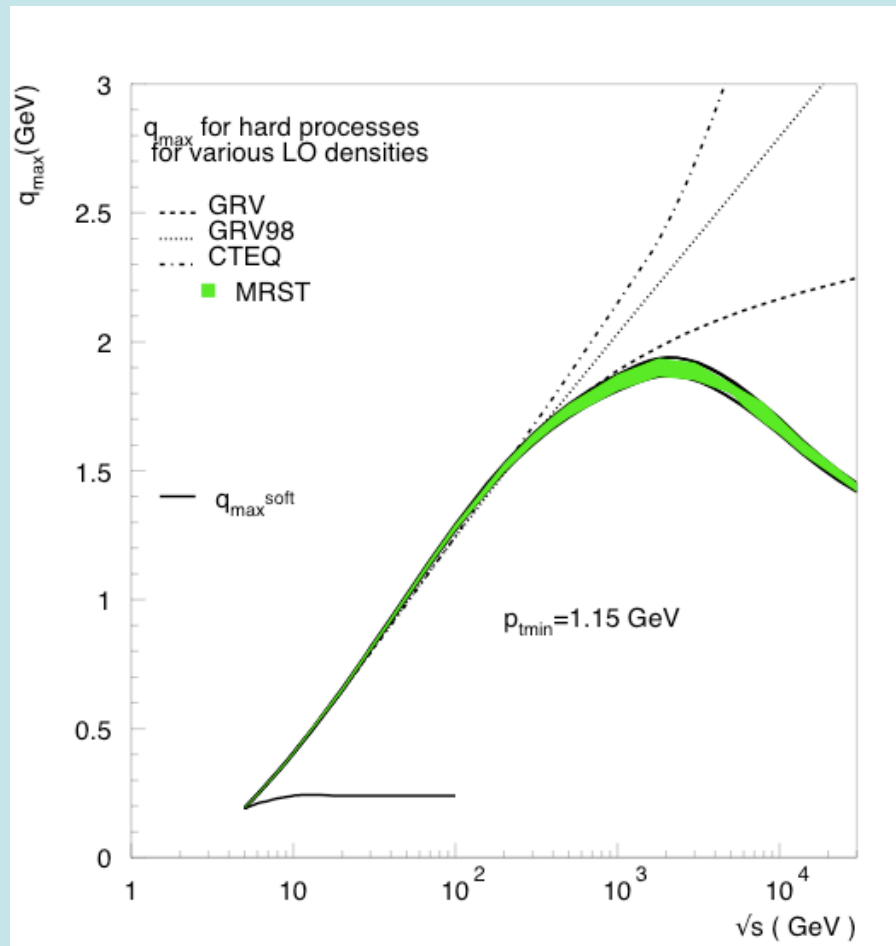
- **Gluon emission in k_{\perp}** changes the collinearity of initial partons
- And for same energy and p_{tmin} , **acollinearity** of initial partons will bring loss of luminosity of the parton beams and parton-parton cross-sections will decrease
- As the energy available for soft gluon emission increases, so does the acollinearity of the parton-parton collision
- The rate of rise of total cross-sections due to **rising minijet cross-section** is **reduced** (softened by) by soft gluon emissions.
- Softening effect more important the more singular α_s

We shall illustrate how the model works
for the proton-proton case and then
show its application to $\gamma\gamma$

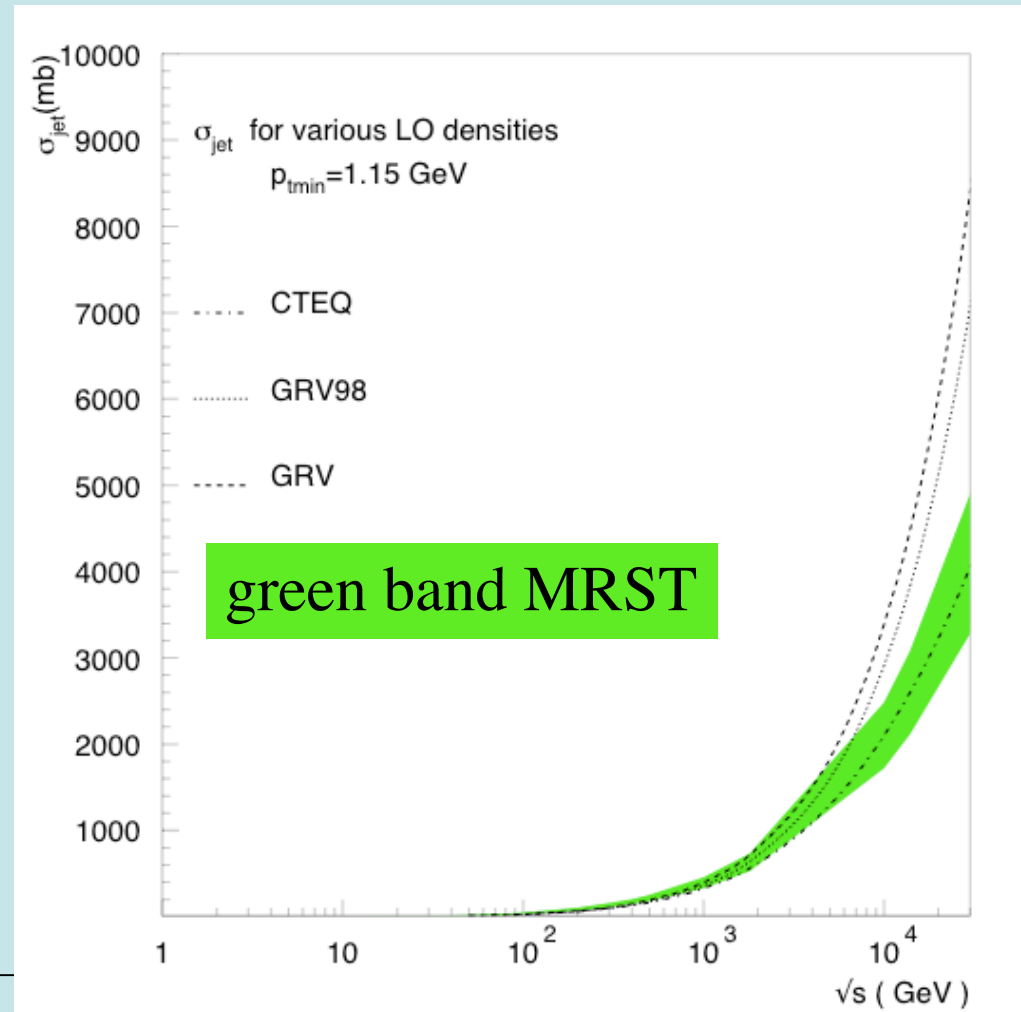
How the model works

- Choose $p_{\text{tmin}} = 1\div 2$ GeV for mini-jets
- Choose parton densities
- Calculate minijet x-section
- Calculate q_{max} for soft gluons
- Calculate $A(b,s)$ for given q_{max}
- Calculate $n_{\text{hard}}(b,s) = A(b,s) \sigma_{\text{jet}}(p_{\text{tmin}}, s)$
- Parametrize n_{soft}
- Evaluate $n(b,s) = n_{\text{soft}} + n_{\text{hard}}$
- Eikonalize $\sigma_{\text{tot}} \approx 2 \int d^2b [1 - e^{-n(b,s)/2}]$

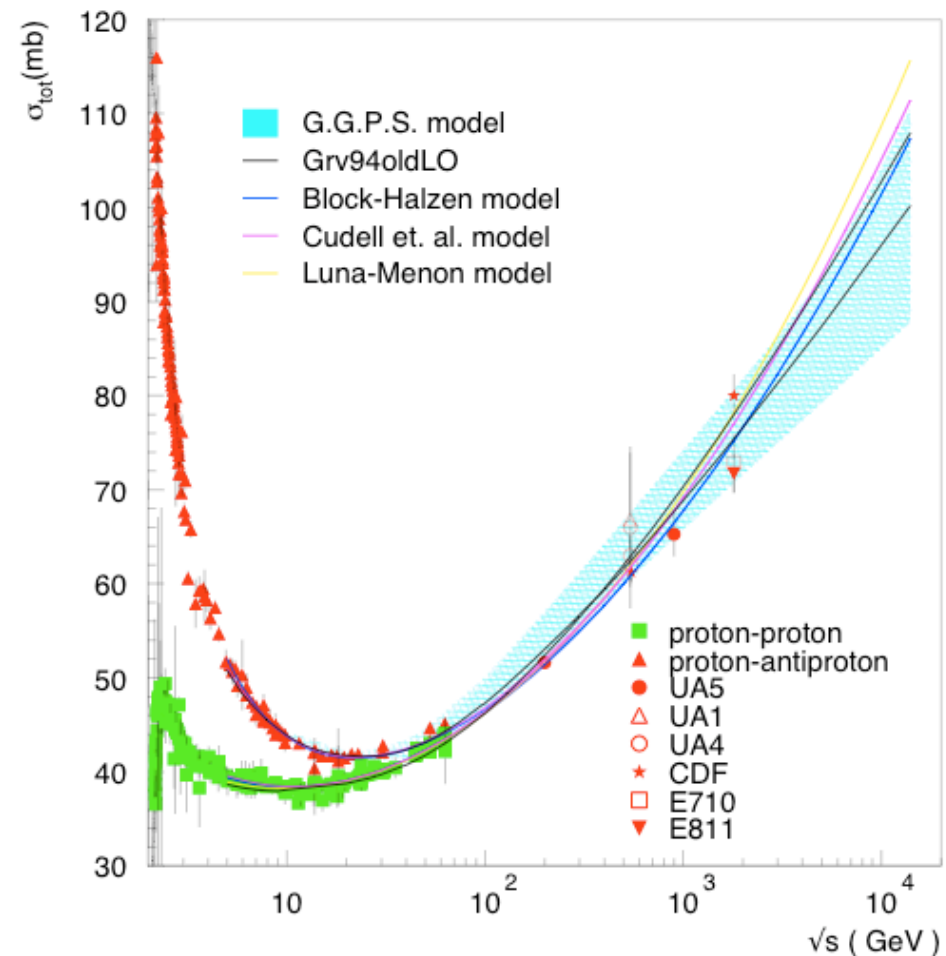
q_{\max} for $p_{t\min}=1.15$ GeV



σ_{jet} for $p_{t\text{min}}=1.15 \text{ GeV}$



Comparison with proton data



R. Godbole,
A. Grau
R. Hedge
G. Pancheri
Y. Srivastava
Les Houches 2005
Pramana **67** (2006)

GGPS PRD **2005**

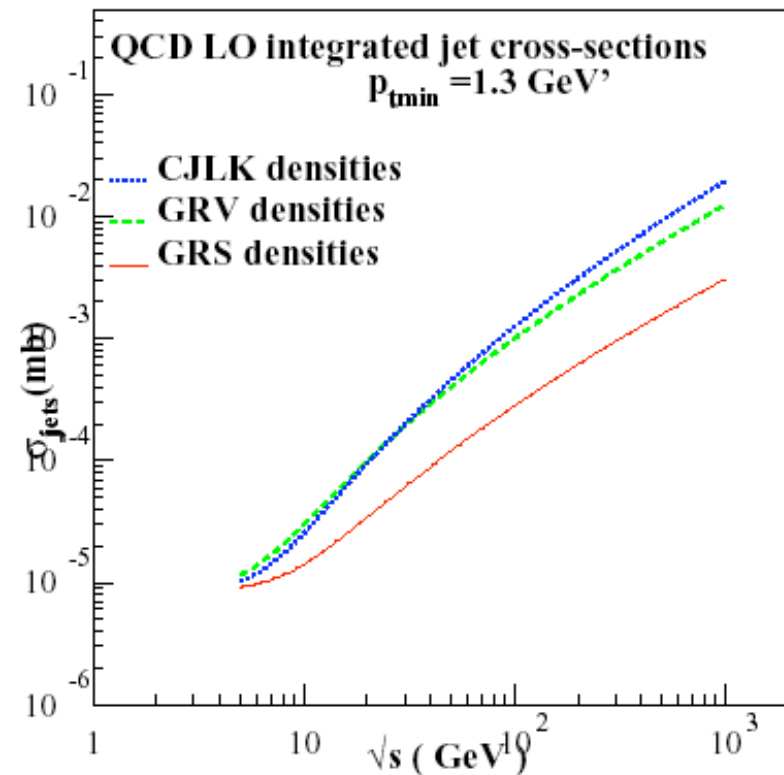
Now apply the model to $\gamma\gamma$

Choose $p_{t\min} = 1 \div 2 \text{ GeV}$ for mini-jets
and parton densities

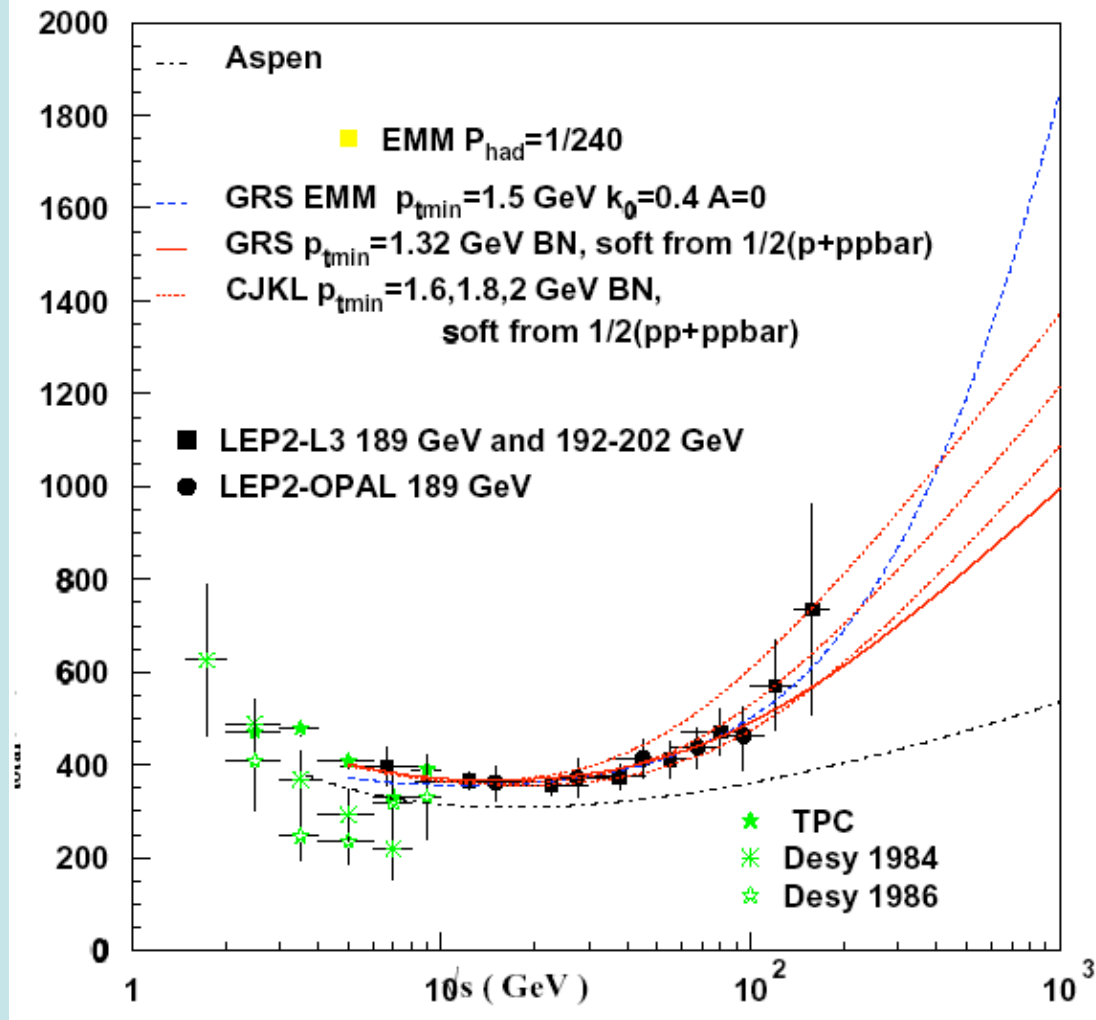
For photons, LEP data
suggest

$p_{t\min} \sim 1.3 \div 1.8 \text{ GeV}$

- Gluck Reya Vogt
- Gluck Reya Shielbein
- Cornet Jankowski Lorca
Krawczyk



Eikonalize $\sigma_{\text{tot}} \approx 2P_{\text{had}} \int d^2b [1 - e^{-n(b,s)/2}]$
and compare with data



P_{had} is a
Phenomenological
input describing
the hadronic
content of the
photon in eikonal
models

R.Fletcher, T.Gaisser, F.Halzen, 1993

Conclusions

- Predictions at ILC vary according to which densities better describe the behaviour at low x
- Total cross-sections measurements in Collider mode would allow clean information on $\gamma\gamma$ cross-sections, reducing the errors due to modelling of diffractive components
- Even in regular mode, difference in the model predictions are measurable and can give insights into the soft or non perturbative region of QCD.