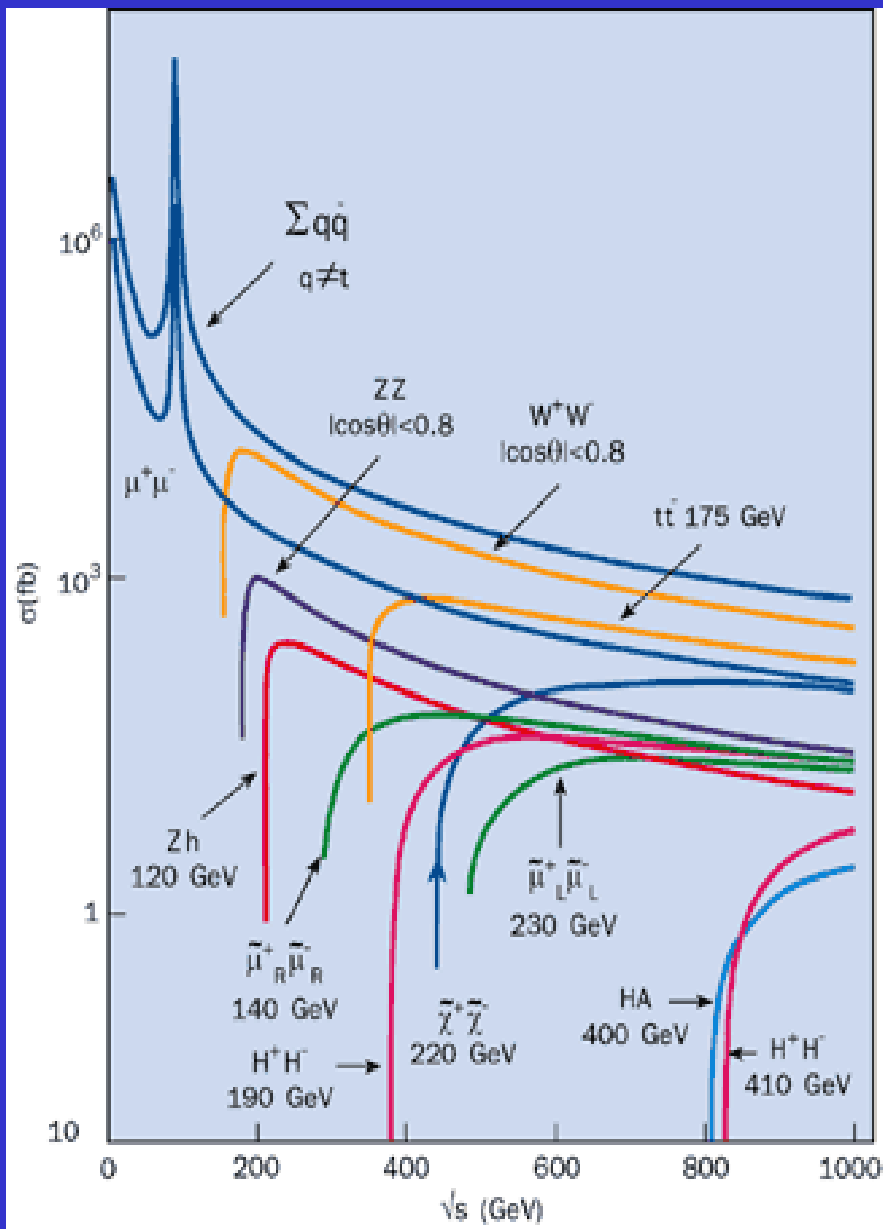




# A qualitative perspective on what is needed for top physics at the ILC

Juan A. Fuster Verdú IFIC-València  
ILC-ECFA & GDE meeting  
València, 6-10 November 2006

In cooperation with M. Vos and E. Ros



Standard Production of top in  $e^+e^-$ :

$\mathcal{L} \sim 500 \text{ fb}^{-1}$

Events  $\sim 5 \times 10^5$

Statistics Low (compared to LHC)

Excellent signal/background ratio  
(accurate measurements possible)

# Our present knowledge of top

✓ The top quark completes the three family structure of the SM

✓ It's massive, "very heavy"  $\Delta m_t \sim 2,1 \text{ GeV}$  (CDF+D0)

✓ Spin=1/2 Not directly

✓ Charge=+2/3 -4/3 excluded @ 94% C.L.(D0)

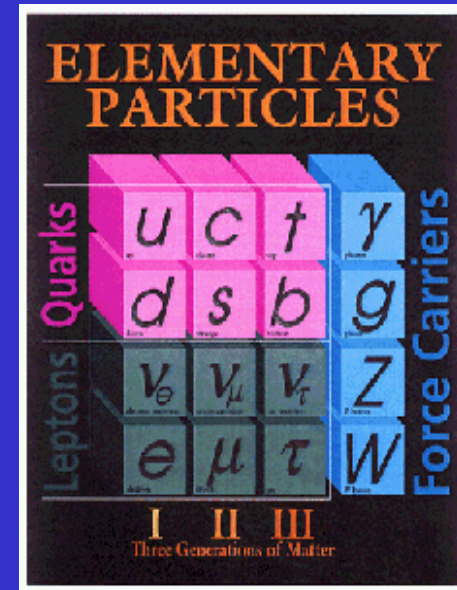
✓ Isospin=+1/2 Not directly

✓  $t \rightarrow bW$  ~100%

✓ Large  $\Gamma=1.42 \text{ GeV}$  ( $m_b, M_W, \alpha_s, \text{EW corr.}$ )

✓ Short lifetime  $c\tau < 53 \mu\text{m}$  @ 95% C.L.(CDF)

✓ Couplings:  $\alpha_t, v_t, V_{td}, V_{ts}, V_{tb}, g_{ttH}$  not yet measured,  $\Delta V_{tb} \sim 11\%$



$$\tau_{\text{had}} = L_{\text{QCD}}^{-1} > \tau_{\text{decay}}$$

→ "t-quarks are produced and decay as free particles"

**NO top hadrons**

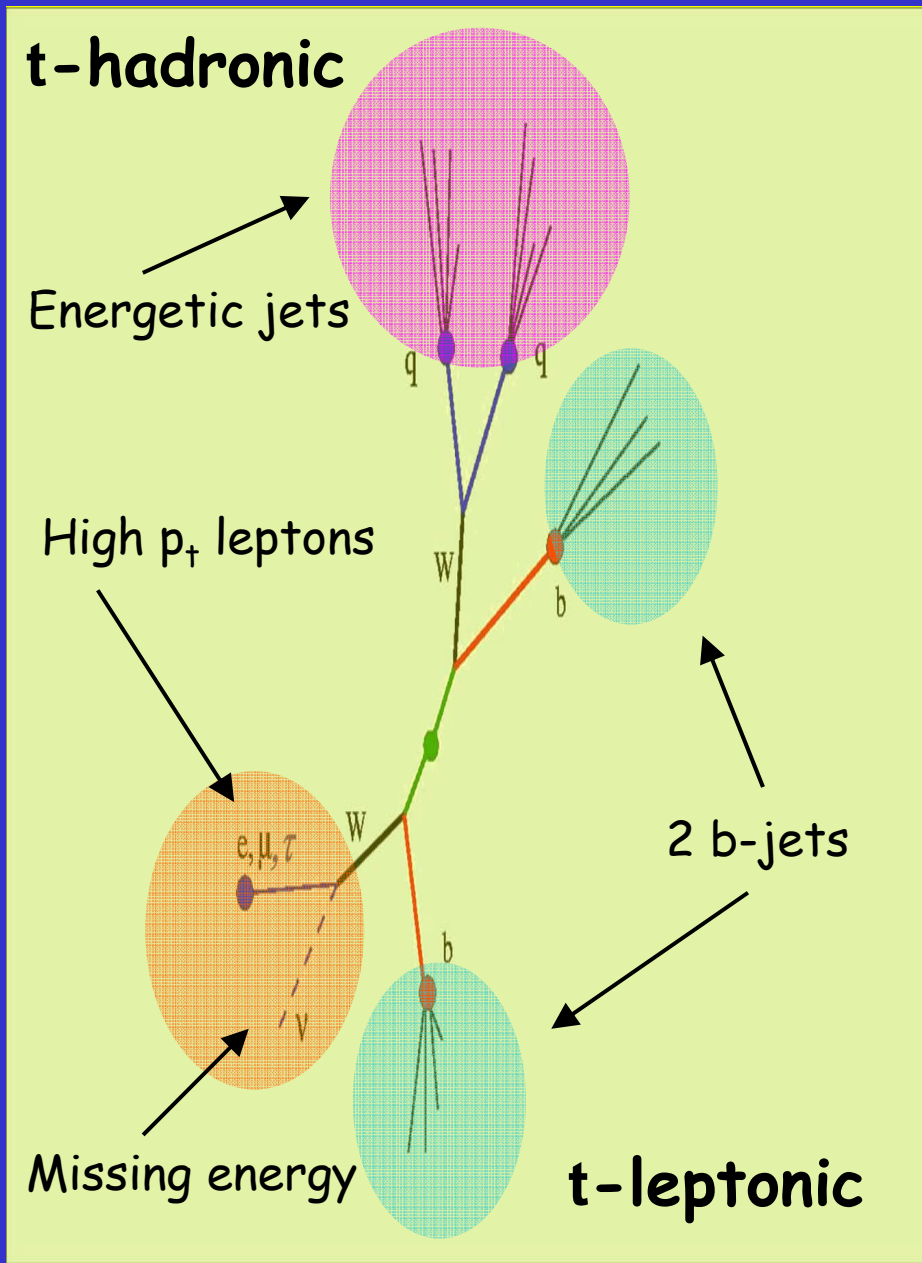
**t-hadronic**

Energetic jets

High  $p_{\perp}$  leptons

Missing energy

**t-leptonic**



$$t \rightarrow Wb \begin{cases} qq'b (68\%) \\ \ell\nu b (32\%) \end{cases}$$



$t\bar{t}$  final states (standard model):

~46% 6 jets (2b)

~44% 4jets (2b) + lepton + neutrino

~10% 2jets (2b) + leptons + neutrinos  
(complicated topologies !!)

Detector capabilities required (very much demanding):

b,c, $\tau$ -tagging in energetic b,c, $\tau$ -jets

High energetic jet reconstruction

W mass reconstruction (jets, leptons)

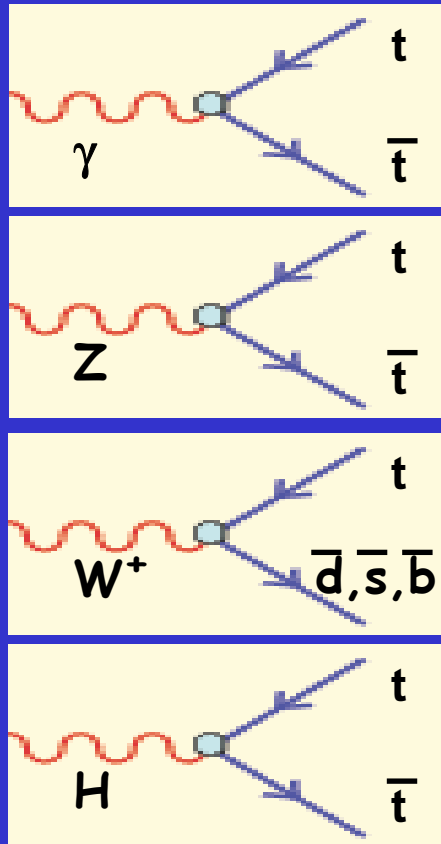
Missing energy, ie, hermiticity

Reconstruction of lepton direction

Precise lepton identification ( $\tau$  also)

# ILC: Accurate measurements of SM-top parameters:

## Top couplings



$$q_t = +2/3 |e|$$

Natural in  $e^+e^-$

$$a_t, v_t$$

$$V_{td}, V_{ts}, V_{tb}$$

$$g_{ttH},$$

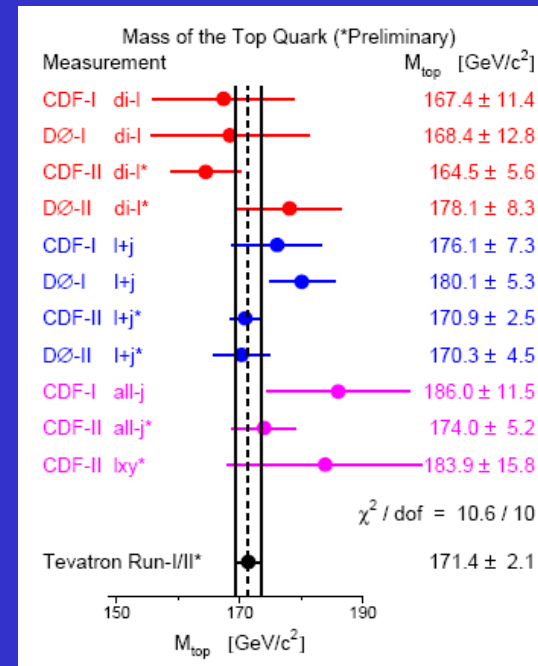
top Yukawa Coupling

$$\sigma_{tt} (e^+e^- \rightarrow tt)$$

$$\Gamma_{tt}$$

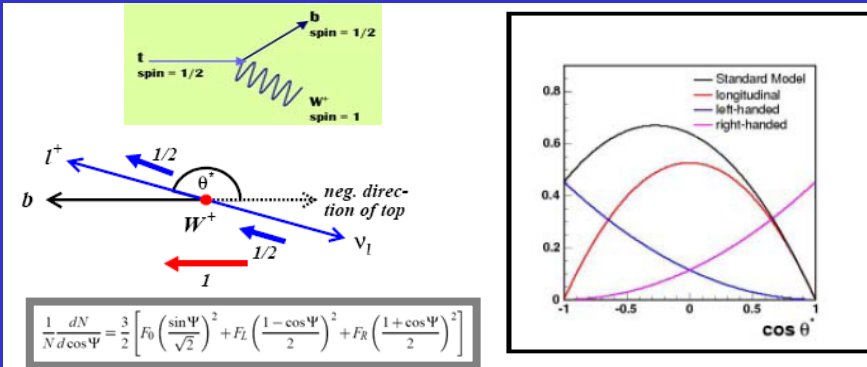
$$m_t (1\text{‰})$$

(at threshold and above)



# ILC: Accurate measurements of SM-top parameters: Polarizations and Asymmetries

Darien Wood, ICHEP'06, "Electroweak Physics"

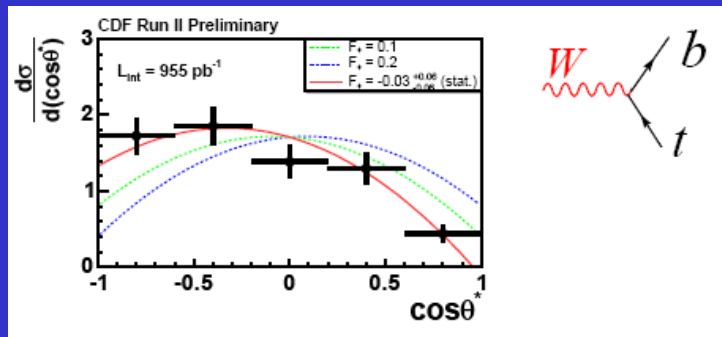


SM prediction of helicity fractions (assuming  $M_t=175\text{GeV}$ ):

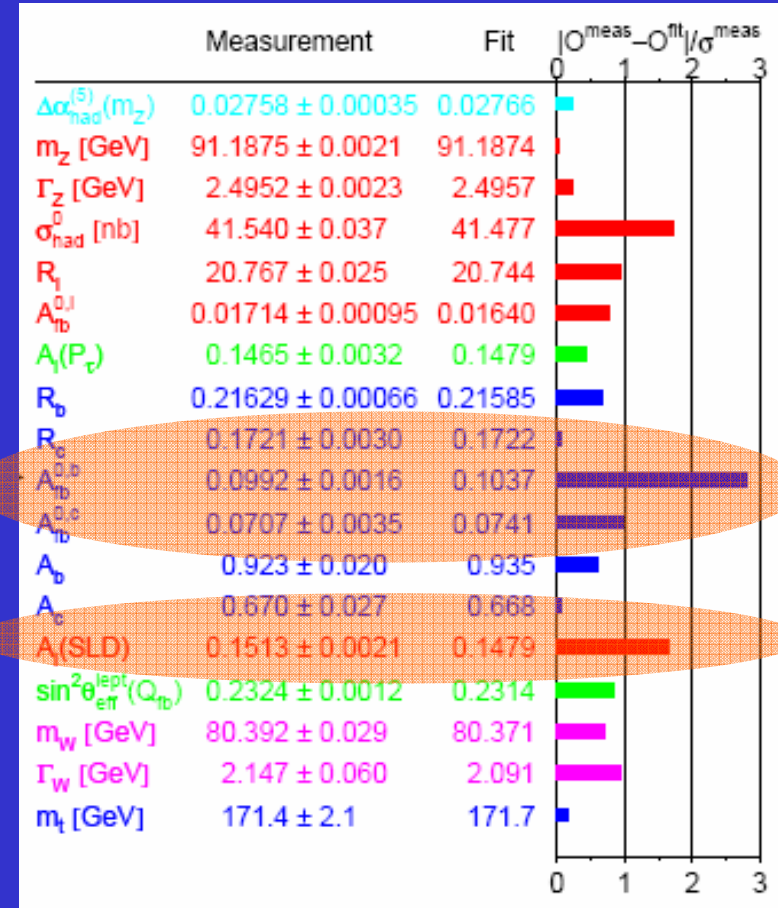


SM(LO):  $F_0=0.703$ ,  $F_L=0.297$ ,  $F_R=3.6 \times 10^{-4}$

(NLO):  $F_0=0.695$ ,  $F_L=0.304$ ,  $F_R=0.001$



|   | $F_0$   | $F_R$  |
|---|---|--|
| CDF ( $\sim 700 \text{ pb}^{-1}$ ) [prelim] |   | $-0.02 \pm 0.07$   |
| CDF ( $955 \text{ pb}^{-1}$ ) [prelim]      | $0.61 \pm 0.12(\text{stat}) \pm 0.04(\text{syst})$          | $-0.06 \pm 0.06(\text{stat}) \pm 0.03(\text{syst})$          |
| CDF ( $955 \text{ pb}^{-1}$ ) [prelim]      | $0.59 \pm 0.12(\text{stat}) \pm_{0.06}^{0.07}(\text{syst})$ | $-0.03 \pm 0.06(\text{stat}) \pm_{0.03}^{0.04}(\text{syst})$ |
| DØ ( $370 \text{ pb}^{-1}$ ) [prelim]       |   | $0.08 \pm 0.08(\text{stat}) \pm 0.05(\text{syst})$           |



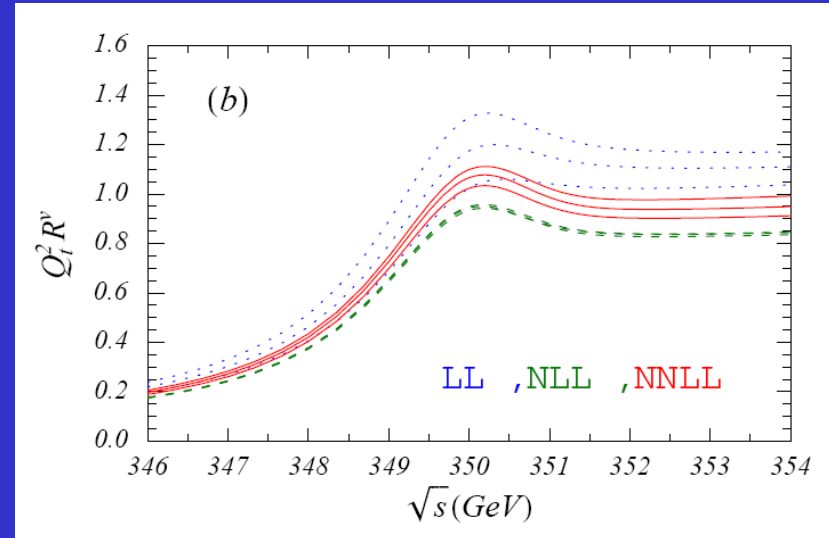
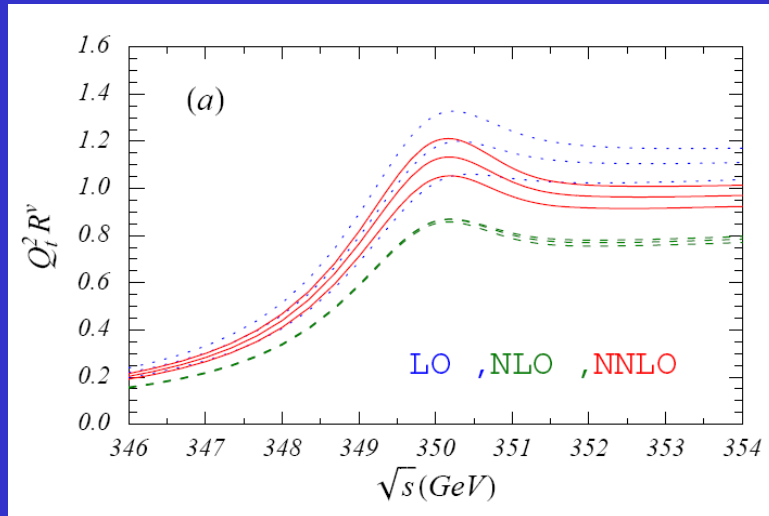
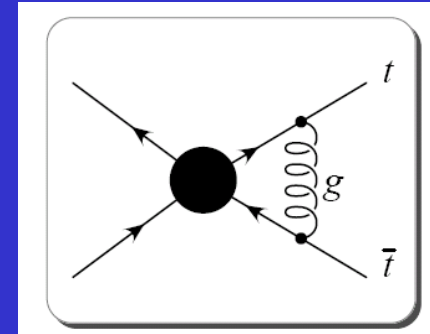
Asymmetries of heavy fermions are the most problematic

What will happen with top ?



# ILC: Top cross section at threshold, theoretical issues:

- ✓ Theoretical issues for top-at-threshold:
- ✓ Coulomb potential, toponium bound state
- ✓ Theoretical interpretation of threshold scan mass
- ✓ NNLO, NNLL calculations available.

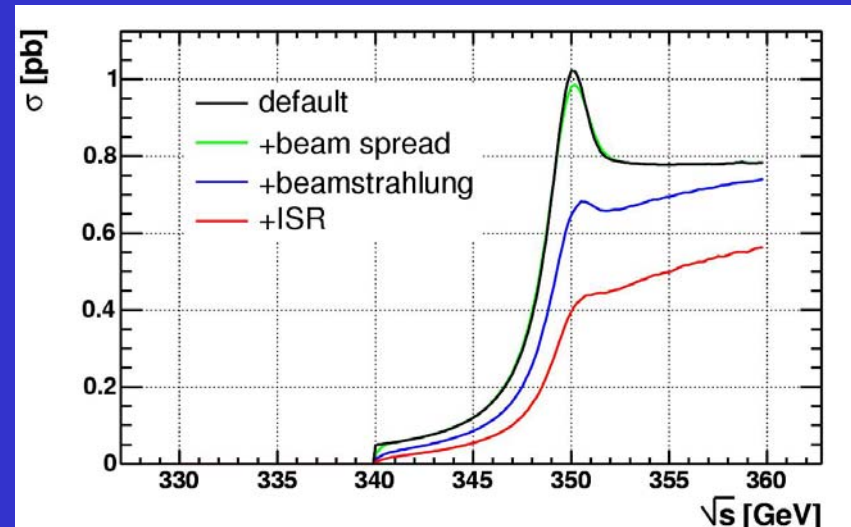
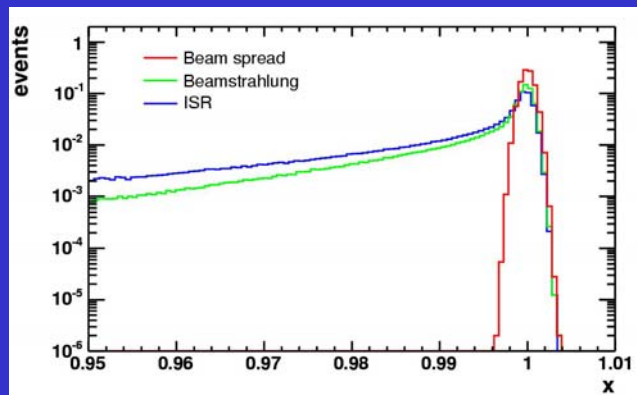
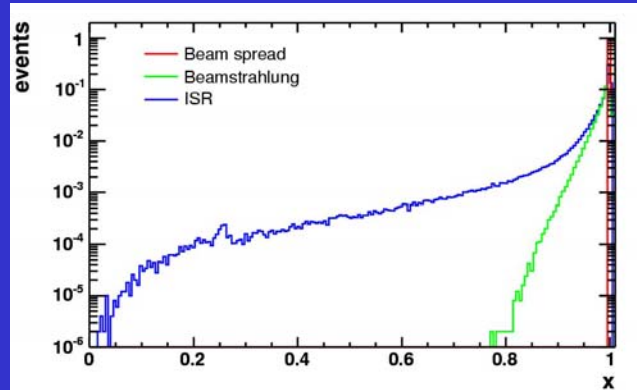


Vector current induced cross section with fixed  $M_t^{1S}$

(a) fixed order, (b) Renormalization Group improved ([A.H. Hoang, A.V. Manohar, I.W. Stewart, T. Teubner](#))

# ILC: Top cross section, experimental issues:

Figures from S. Boogert, experimental top threshold scan, Snowmass 08/2005



- Effect on top cross section:

$$\sigma^{\text{obs}}(\sqrt{s}) = \frac{1}{L_0} \int_0^1 L(x) \sigma(x\sqrt{s}) dx$$

Top threshold is the benchmark for high precision analysis. Impressive progress but many details remain to be clarified to make error estimates (th+Exp) more reliable.

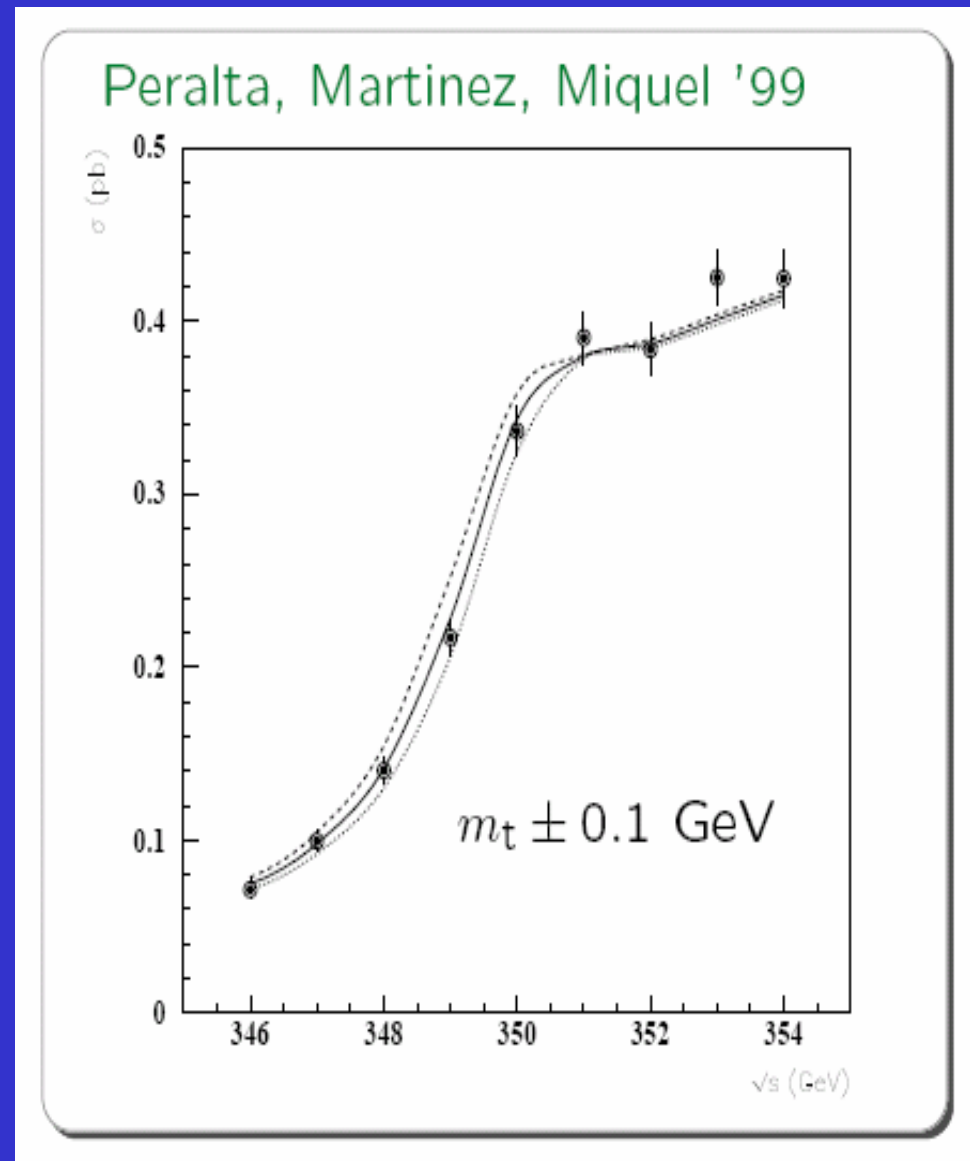
Accurate simulations including beam effects are needed for threshold scan

(T. Teubner, Ambleside Linear Collider Physics Summer School)



## ILC: Top cross section:

- ✓ Measurement of  $t\bar{t}$  cross section at various points around the production threshold. Fit top mass (and width).
- ✓ Total error top mass expected  $< 100$  MeV or better.
- ✓ Complementary kinematic reconstruction of top anti-top events above threshold expected to yield good statistical uncertainty



# ILC: CKM matrix elements from t decays

As an experimental requirement:

Clean isolation of the decay (ok at ILC)

Excellent quark flavour identification (b,c, uds)

Parton charge (efficient track reconstruction, track-to-vertex association, down to low  $p_T$ )

CKM from top decays,  
Letts, Mattig '01  
( $\mathcal{L} \sim 300 \text{ fb}^{-1}$ )

|  |          | now                 | ILC         |
|--|----------|---------------------|-------------|
|  | $V_{td}$ | $0.0074 \pm 0.0008$ | $\pm 0.026$ |
|  | $V_{ts}$ | $0.0406 \pm 0.0027$ | $\pm 0.006$ |
|  | $V_{tb}$ | $1.0 \pm 0.11$      | $\pm 0.005$ |

## ILC: Top couplings to Z and $\gamma$

- General t-t- $\gamma$  and t-t-Z vertices:

$$\mathcal{M}^{\mu(\gamma,Z)} = e\gamma^\mu \left[ Q_V^{\gamma,Z} F_{1V}^{\gamma,Z} + Q_A^{\gamma,Z} F_{1A}^{\gamma,Z} \gamma^5 \right] + \frac{ie}{2m_t} \sigma^{\mu\nu} k_\nu \left[ Q_V^{\gamma,Z} F_{2V}^{\gamma,Z} + Q_A^{\gamma,Z} F_{2A}^{\gamma,Z} \gamma^5 \right]$$

Within the SM:  $F_{1V}^\gamma = F_{1V}^Z = F_{1A}^Z = 1$  with the rest equal to 0.

$\uparrow$  CP-conserving       $\uparrow$  CP-violating

Strong EWSB models (e.g. technicolor):  $F_{2V} \sim 5\text{-}10\%$

SUSY/MHDM models:  $F_{2A} \sim 0.1\text{-}1\%$

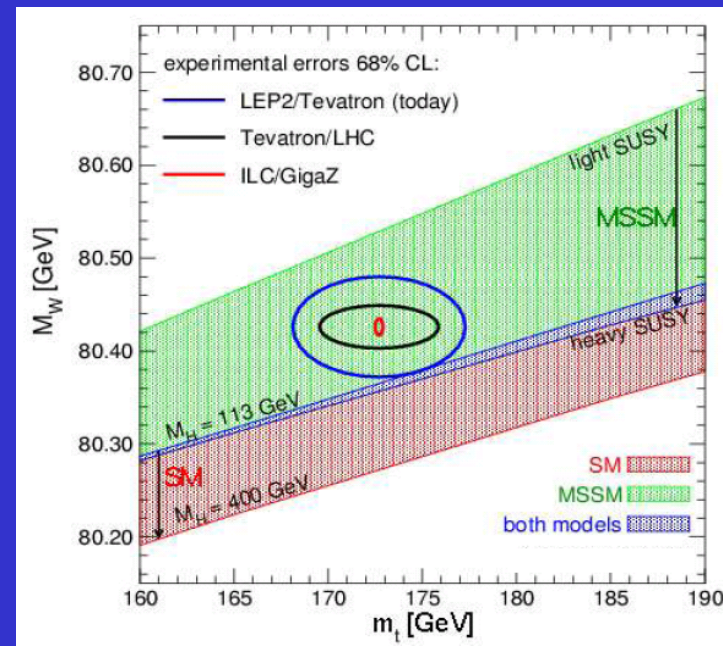
See Aurelio Juste talk at Vancouver: for  $Zt\bar{t}$  ILC better than LHC

for  $\gamma t\bar{t}$  ILC comparable to LHC

# ILC: top and SUSY

No need to stress the importance of precision measurements of Standard Model parameters to constrain theory.

The top mass may reveal to be one of the most important ones.



Top decay  $t \rightarrow Wb$  ( $\sim 100\%$  in SM),  $W \rightarrow e, \mu, \tau$  (Branching ratios 10% per lepton)

For 2 doublet Higgs sector, with light charged Higgs boson  $H^+$ , top decay  $t \rightarrow H^+b$  becomes competitor.  $H^+ \rightarrow \tau \nu$  (branching ratio  $\sim 1$  for  $\tan \beta > 10$  and  $m_{H^+} < m_t - m_b$ )

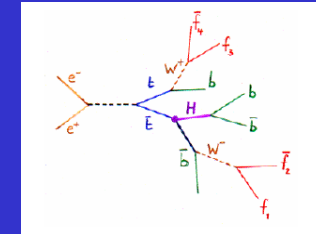
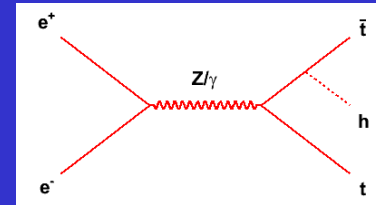
Measure Br.R. ( $t \rightarrow \mu \nu b$ ) / Br. R. ( $t \rightarrow \tau \nu b$ ), calibrate with W production.

Experimental requirement: precisely reconstruct missing energy and  $t$  - decays (including hadronically decaying  $\tau$ -jets)

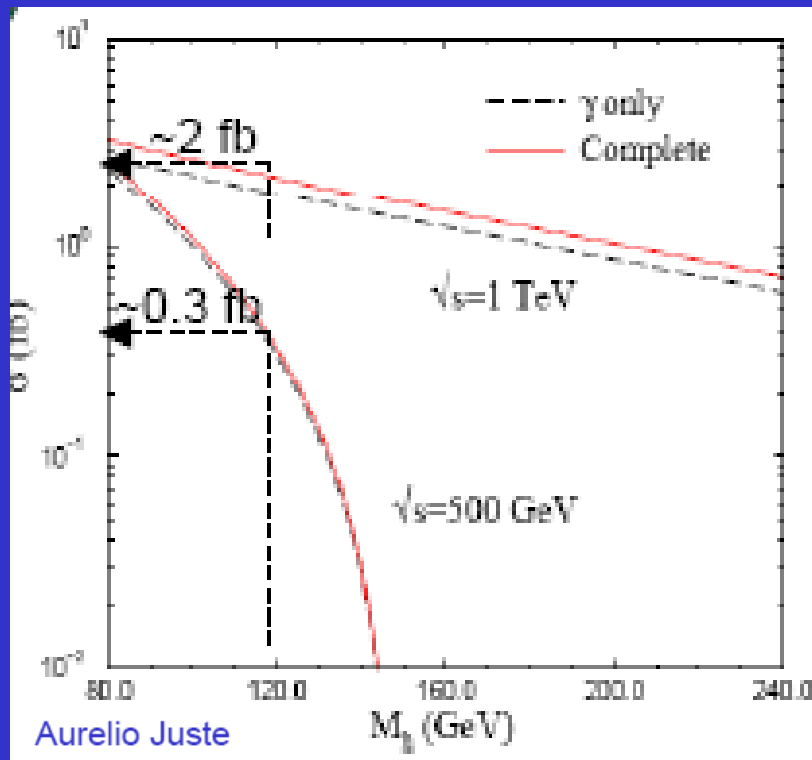
# ILC: top Yukawa coupling to Higgs

$t\bar{t}$  production cross-section at threshold is sensitive to  $t\bar{t}h$  Yukawa coupling.

For  $m_h = 115 \text{ GeV}$ , a variation of 14% in SM Yukawa coupling leads to a 2% change in normalization of the cross section near the 1S peak.



Very complicated topology



6 jets + 2bjets + leptons + missing energy

4 jets + 2bjets

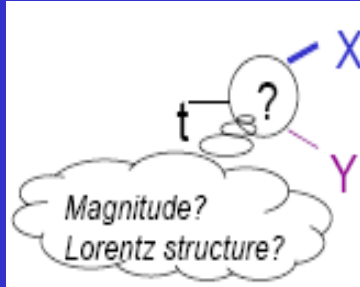
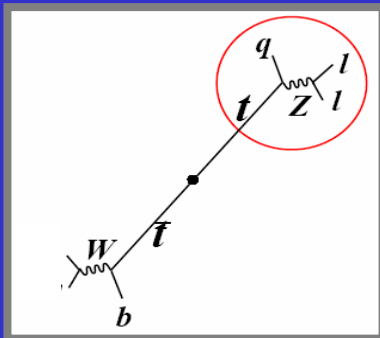
2 jets + 4bjets + leptons + neutrinos

$$\frac{\Delta g_{t\bar{t}H}}{g_{t\bar{t}H}} \sim 15\%, m_h \sim 120 \text{ GeV}$$

(  $E_{\text{beam}} \sim 250 \text{ GeV}$ ,  $\mathcal{L} \sim 1000 \text{ fb}^{-1}$  )

(with polariztion 60%e+, -80%e-)

# ILC: t and exotic physics, rare decays, FCNC

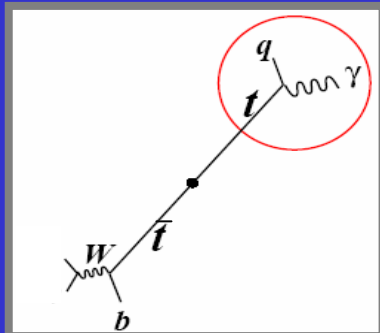


In the SM:  $X=W$  100% of the time,  $Y=b$  ~100% of the time ( $|V_{tb}| \sim 1$ )

$$\Gamma_{tbW}^\mu = -\frac{g}{\sqrt{2}} V_{tb} \left\{ \gamma^\mu [f_1^L P_L + f_1^R P_R] - \frac{i \sigma^{\mu\nu} (p_t - p_b)_\nu}{M_W} [f_2^L P_L + f_2^R P_R] \right\}$$

$f_1^L = \bar{f}_1^L = 1$  with the rest equal to 0 (pure V-A interaction)

If  $f_1^{LR} - \bar{f}_1^{LR} \neq 0$  or  $f_2^{LR} - \bar{f}_2^{LR} \neq 0 \Rightarrow$  CP-violation



ILC: both anomalous production ( $e^+e^- \rightarrow tq$ ) and decay ( $e^+e^- \rightarrow tt; t \rightarrow Vq$ ) can be explored.

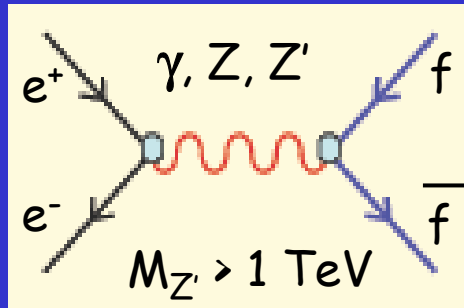
hep-ph/0102197

|  | $(P(e^-), P(e^+)) = (0,0)$ |                      | $(P(e^-), P(e^+)) = (-0.8,0)$ |                      | $(P(e^-), P(e^+)) = (-0.8,+0.45)$ |                      |       |
|--|----------------------------|----------------------|-------------------------------|----------------------|-----------------------------------|----------------------|-------|
|  | No pol.                    |                      | Pol. $e^-$                    |                      | Pol. $e^- e^+$                    |                      |       |
|  | 95%                        | $3\sigma$            | 95%                           | $3\sigma$            | 95%                               | $3\sigma$            |       |
| $Br(t \rightarrow \gamma q)$             | $3.9 \times 10^{-5}$       | $5.9 \times 10^{-5}$ | $3.2 \times 10^{-5}$          | $3.3 \times 10^{-5}$ | $1.9 \times 10^{-5}$              | $1.8 \times 10^{-5}$ | tq    |
|  | $3.3 \times 10^{-4}$       | $3.2 \times 10^{-4}$ | $5.0 \times 10^{-4}$          | $3.2 \times 10^{-4}$ | $4.0 \times 10^{-4}$              | $2.6 \times 10^{-4}$ | decay |
| $Br(t \rightarrow Zq) (\gamma_\mu)$      | $7.9 \times 10^{-4}$       | $1.2 \times 10^{-3}$ | $7.1 \times 10^{-4}$          | $7.5 \times 10^{-4}$ | $4.4 \times 10^{-4}$              | $4.2 \times 10^{-4}$ | tq    |
|  | $5.4 \times 10^{-3}$       | $3.5 \times 10^{-3}$ | $8.0 \times 10^{-3}$          | $2.6 \times 10^{-3}$ | $6.3 \times 10^{-3}$              | $2.0 \times 10^{-3}$ | decay |
| $Br(t \rightarrow Zq) (\sigma_{\mu\nu})$ | $6.3 \times 10^{-5}$       | $9.4 \times 10^{-5}$ | $5.7 \times 10^{-5}$          | $6.0 \times 10^{-5}$ | $3.5 \times 10^{-5}$              | $3.4 \times 10^{-5}$ | tq    |
|  | $5.7 \times 10^{-3}$       | $3.7 \times 10^{-3}$ | $8.3 \times 10^{-3}$          | $2.7 \times 10^{-3}$ | $6.5 \times 10^{-3}$              | $2.1 \times 10^{-3}$ | decay |

- Sensitivity better from production than from decay since, despite the lower S/B,  $\sigma$  is larger.
- Beam polarization very useful to improve limits from production.
- $\gamma\gamma \rightarrow tc$  would allow to study FCNC with higher  $\sigma$  (~x100) and lower SM bckg.

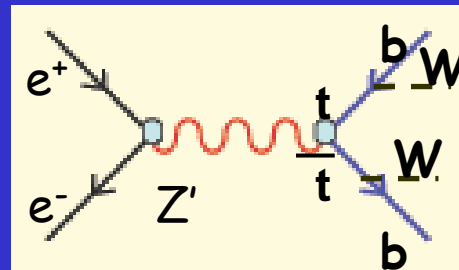
# ILC: t and exotic physics, Z' resonances

Even, if Z' discovered at LHC in leptonic decays



$$\bar{f} \gamma^\mu (v_f' - a_f' \gamma^5) f$$

↓  
f=t



Very important to make accurate measurements of the couplings to discriminate between Z' models (very difficult at LHC):

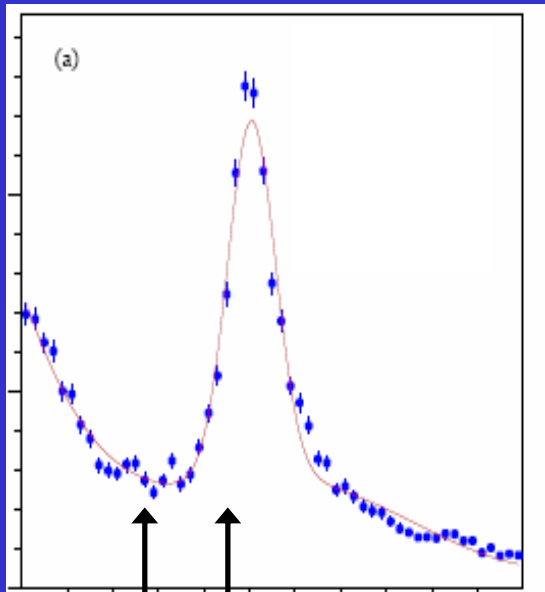
SM Z'

LR symmetric models

Little Higgs

Extra dimensions

Effective symmetries



Depending on the beam energy it will be more or less difficult to extract couplings! Energy crucial!!

## Key Observables

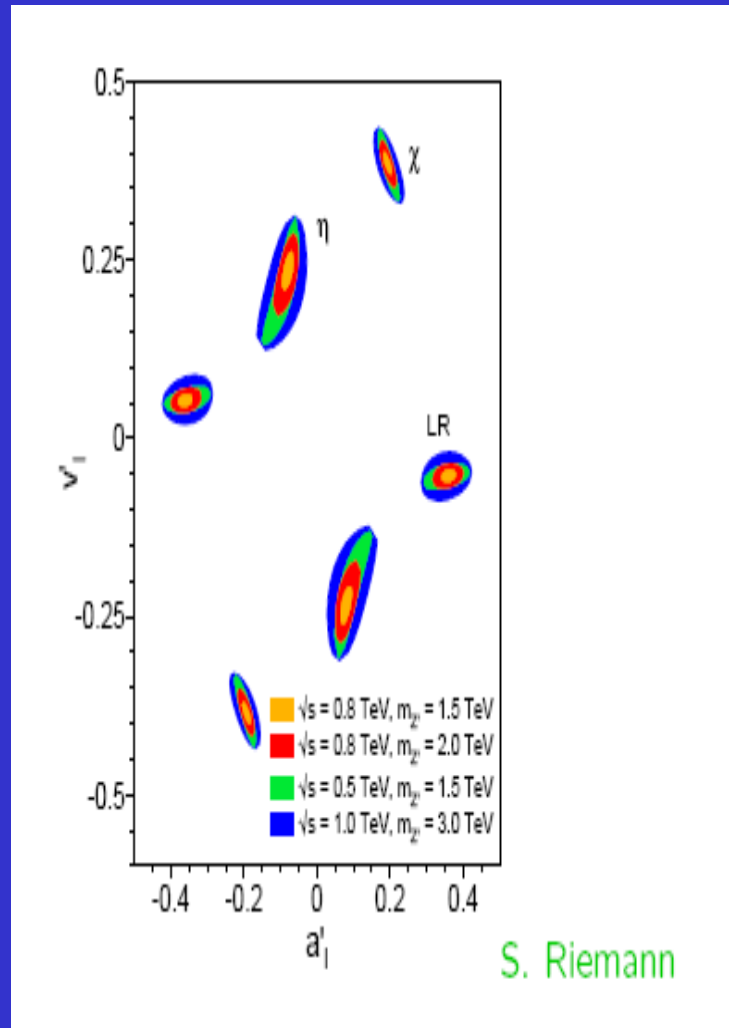
$$\sigma_t \sim (v_t')^2 + (a_t')^2 \quad A_f^{\text{FB}} \sim \frac{2v_f' a_f'}{(v_f')^2 + (a_f')^2}$$

Polarization studies also possible (like  $\tau$  at LEP)  
(if all decay products reconstructed)

Polarized beams very beneficial!



# ILC: t and exotic physics, Z' resonances, possibilities



| Energy    | Observables | $\Delta(\%)$ | Deviation From SM |
|-----------|-------------|--------------|-------------------|
| 500 (GeV) | $R_t$       | 0.2          | +24               |
| 500 (GeV) | $A_t^{LR}$  | 0.1          | +200              |

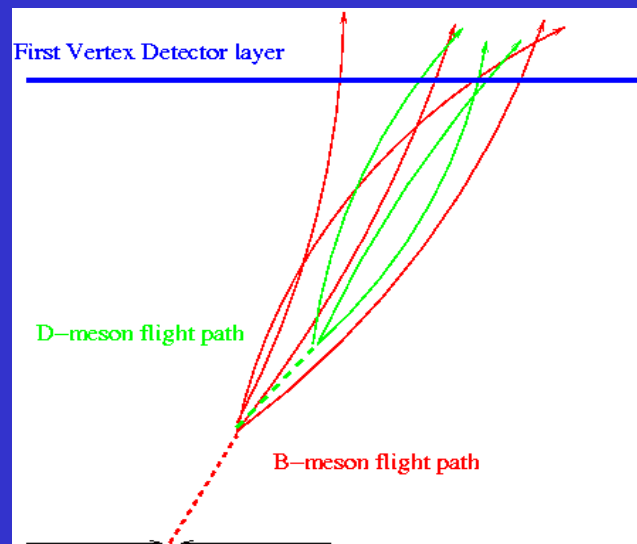
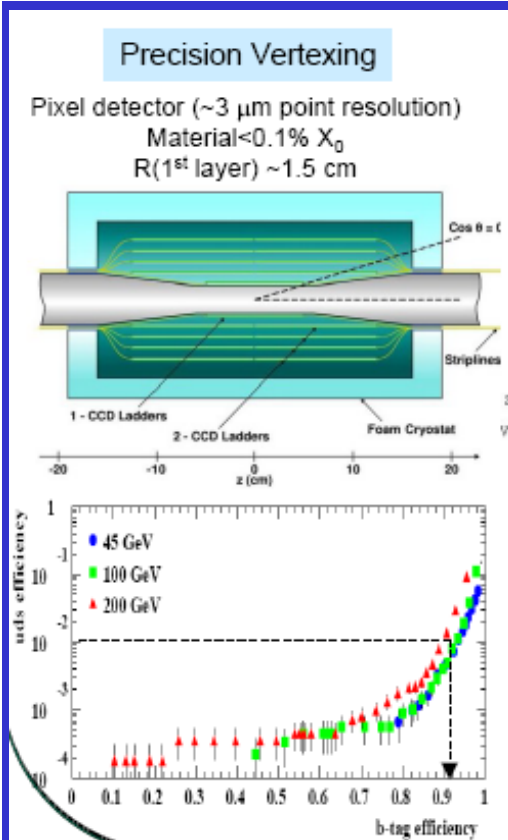
Resolving the  $A_B^{FB}$  puzzle in an extra dimensional model

(A. Djouadi, G. Moreau, F. Richard)

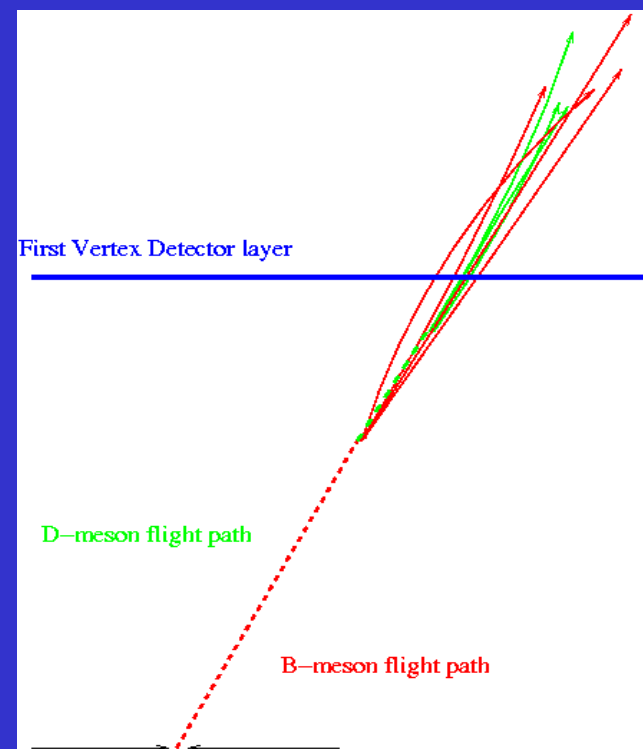
( $E_{\text{beam}} \sim 250 \text{ GeV}$ ,  $\mathcal{L} \sim 500 \text{ fb}^{-1}$ )

Main background being ZWW events, accurate reconstruction of Z mass needed (particle flow)

# Flavour tagging at ILC



"soft b-jet"

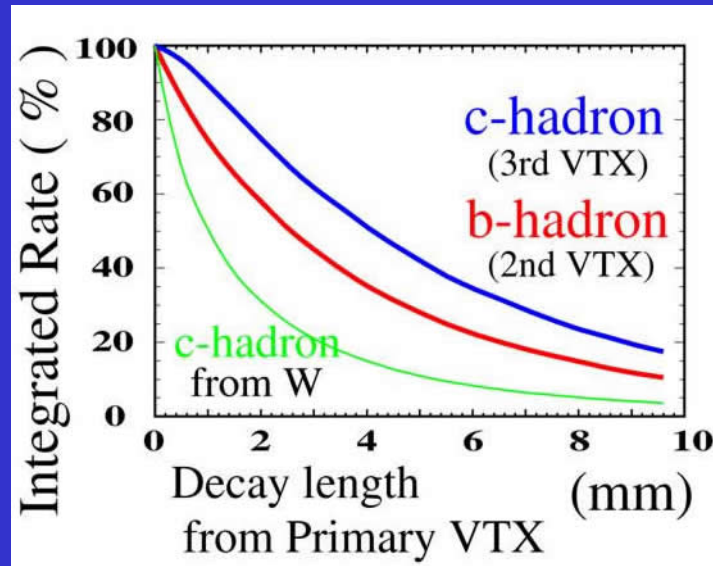


"hard b-jet"

- ✓ Typically b-tagging becomes "easier" for larger jet energy (more and stiffer tracks, boost leads to greater displacement of the vertex for the same lifetime)
- ✓ True only up to the point where a negative effect kicks in: the dense environment in collimated jet, with B/D decay vertex very close to first layer, leads to problems in hit-to-track assignment, merging of hits etc.

# Flavour tagging at ILC

How close do our secondary vertices get?

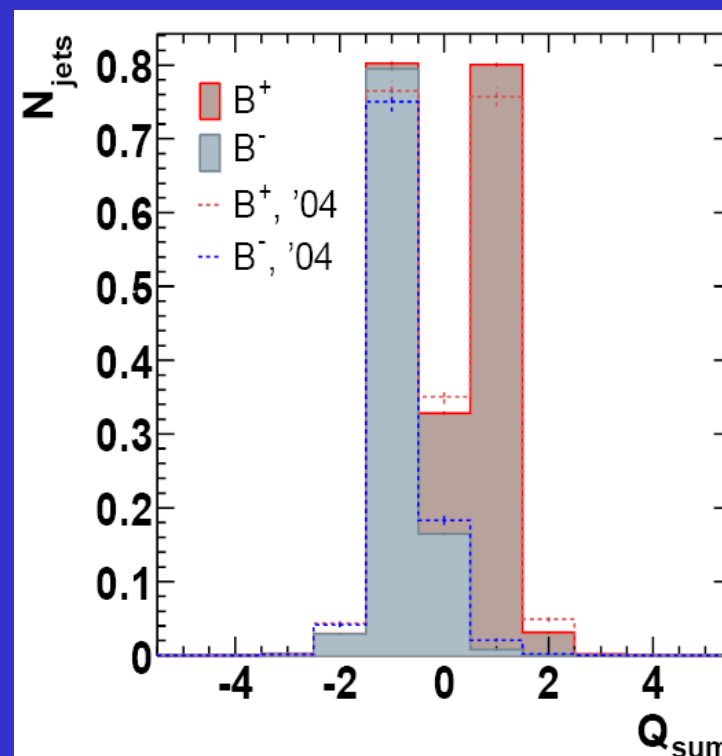
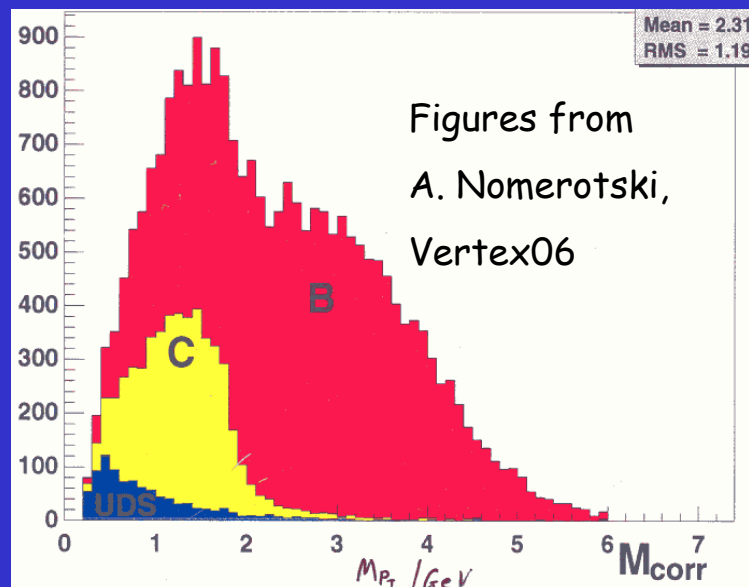
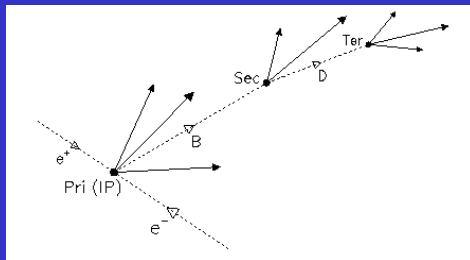


- ✓ Illustration: decay length of B-hadrons with 40-50 GeV (ACFA report)
- ✓ Typical values for top (produced at rest) decay products: jet energy  $\sim m_t/2$
- ✓ decay length (distance PV-SV) =  $\beta \gamma c \tau$
- ✓ (b-jets:  $\langle c\tau \rangle \sim 450 \mu\text{m}$ ,  $\langle \beta\gamma \rangle \sim 20$ )
- ✓ ( $\tau$ -jets:  $\langle c\tau \rangle \sim 80 \mu\text{m}$ ,  $\langle \beta\gamma \rangle \sim 50$ )

A good fraction of B-hadrons from top decay at rest (and charmed hadrons formed in the B-decay) come very close to the first vertex layer. For large  $M_{tt}$  events....

$\tau$ -leptons travel much less before decay, and the (charged) decay products are typically few. However, high energy  $\tau$ -jets are extremely collimated.

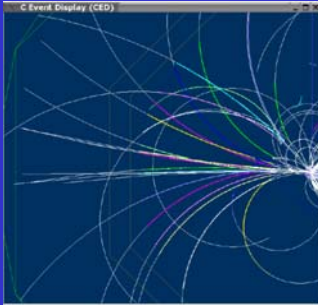
# Flavour tagging at ILC II



✓ Impact parameter is not the end of it: secondary (and tertiary) vertex reconstruction allows to determine decay vertex properties. Vertex sign determination allows to distinguish jets containing  $B^+$  and  $B^-$ , of utmost importance for asymmetries.

✓ One lost track (or one fake) ruins it all. Tracking efficiency (and fake control) is crucial! Reconstruction needs to be tested on realistic Monte Carlo (including pattern recognition).

# Particle Flow - Jet Energy reconstruction ILC

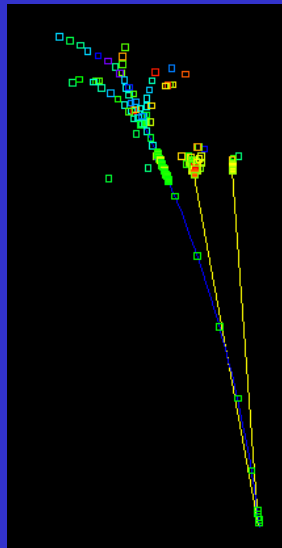
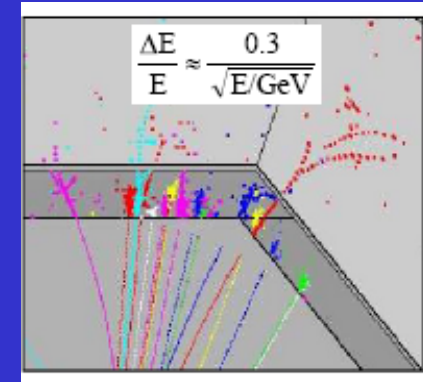


Jet Reconstuction:

Track momentum resolution important but not only

Two track separation essential

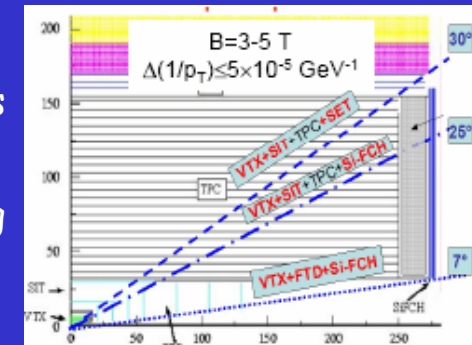
Track association to calorimeters and vertex



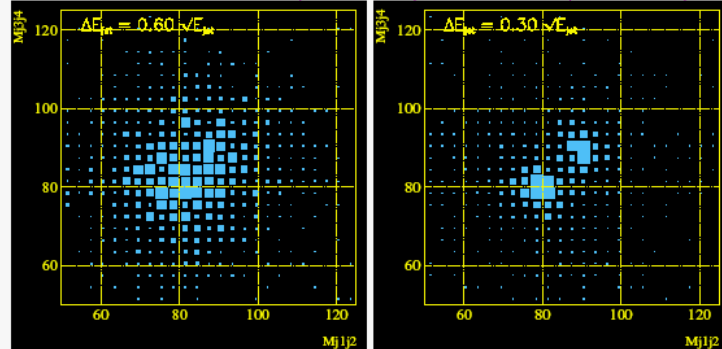
Jets in top topologies:

Essential to have very good jet-jet invariant mass resolution (W-Z separation, etc..)

Energetic jets imply high collimation requiring granularity



WW-ZZ separation for  $\Delta E/E = 60\%/\sqrt{E}$  and  $\Delta E/E = 30\%/\sqrt{E}$



|   |                            |
|---|----------------------------|
| Resolution on the jets $\delta E_{jet}$     | <b>2-3</b> better than LHC |
| Granularity/segmentation of the calorimeter | <b>&gt;250</b> × LHC       |

# Reconstructing multi-jet final states (from LEP knowledge)

" we know that they are not fully understood in generators, specially when heavy quarks are involved"

Double rates ( $R_n^{bl} = R_n^b / R_n^l$ )

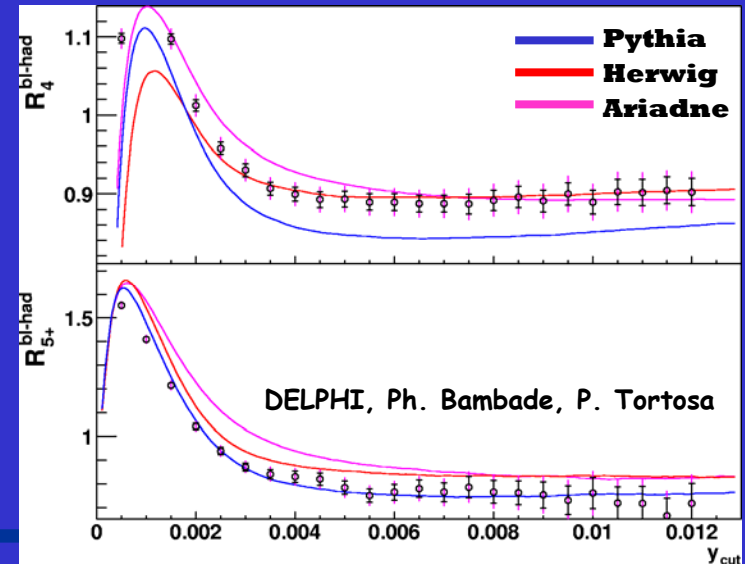
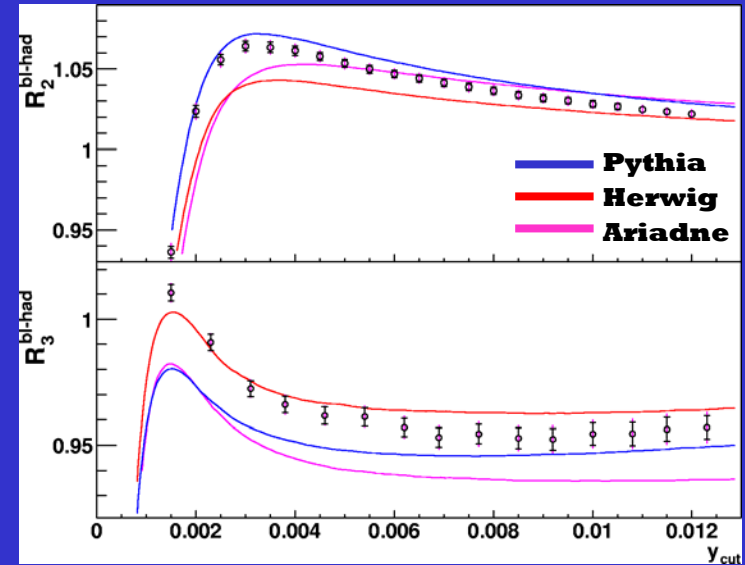
$$R_n^{bl}(y_c) = \frac{\sigma_{nj}^{Z^0 \rightarrow b\bar{b}(n-2)g}(y_c) / \sigma_{tot}^{Z^0 \rightarrow b\bar{b}}}{\sigma_{nj}^{Z^0 \rightarrow l\bar{l}(n-2)g}(y_c) / \sigma_{tot}^{Z^0 \rightarrow l\bar{l}}}$$

Cancel systematics. Small hadronisation corrections, partial cancellation of higher order terms

Cancel EW effects.

- No generator describes all rates at the same time
- In general there are more heavy quark jets than predicted

Understanding top/background final states will need improved generator descriptions for heavy quark initiated jets





# Conclusions

Top physics are very rich and its exploitation is very detector performance demanding (vertexing, tracking, calorimetry and flavour identification)

Due, mainly, to its large mass studying its phenomenology is not only interesting for Standard Model measurements but also to evaluate the existence of many new physics scenarios

ILC complements with LHC also for top

A lot of work though extremely challenging waiting for us ...