CP violation in SUSY particle production and decay



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based on

Bartl, Fraas, SH, Hohenwarter-Sodek, Moortgat-Pick, JHEP **0408** (2004) 038 [hep-ph/0406190] Bartl, Fraas, SH, Hohenwarter-Sodek, Kernreiter, Moortgat-Pick, JHEP **0601** (2006) 170 [hep-ph/0510029] Bartl, Fraas, SH, Hohenwarter-Sodek, Kernreiter, Moortgat-Pick, EPJC **51** (2007) 149 [hep-ph/0608065]

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Outline

- Introduction
 - Supersymmetry with complex parameters
 - Complex parameters in chargino/neutralino sectors
- Aim: determination of the phases \leftrightarrow analysis of CP structure of theory
- CP-even observables (σ , BR, ...) ↔ ambiguities ⇒ CP-odd observables needed
- Here: CP-odd asymmetries in chargino/neutralino sectors
 - \rightarrow defined via triple products and transverse beam polarization
 - \rightarrow estimation of measurability
- Outlook: CP violation in Higgs sector
- Summary

Introduction MSSM with complex parameters

General MSSM:

Many parameters can be complex

- New sources of CP violation
 - May help to explain baryon asymmetry of universe
 - Constraints from electric dipole moments (EDMs) of e, n, Hg, Tl
 [Ibrahim, Nath, '99; Barger, Falk, Han, Jiang, Li, Plehn, '01; Abel, Khalil, Lebedev, '01]
 [Oshima, Nihei, Fujita, '05; Pospelov, Ritz, '05; Olive, Pospelov, Ritz, Santoso, '05]
 [Abel, Lebedev, '05; Yaser Ayazi, Farzan, '06, '07]
- Physical phases of the parameters
 - μ : Higgs-higgsino mass parameter
 - M_1 : U(1) gaugino mass parameter
 - A_f : trilinear couplings of sfermions
 - M_3 : SU(3) gaugino mass parameter (gluino mass)

Introduction Complex parameters in $ilde{\chi}^{\pm}$, $ilde{\chi}^{0}$ sectors

• Chargino (
$$\tilde{\chi}^{\pm}$$
) mass matrix: $X = \begin{pmatrix} M_2 & \sqrt{2} m_W s_\beta \\ \sqrt{2} m_W c_\beta & |\mu| e^{i\varphi_\mu} \end{pmatrix}$

Neutralino ($\tilde{\chi}^0$) mass matrix:

$$Y = \begin{pmatrix} |M_1|e^{i\varphi_{M_1}} & 0 & -m_Z s_W c_\beta & m_Z s_W s_\beta \\ 0 & M_2 & m_Z c_W c_\beta & -m_Z c_W s_\beta \\ -m_Z s_W c_\beta & m_Z c_W c_\beta & 0 & -|\mu|e^{i\varphi_\mu} \\ m_Z c_W c_\beta & -m_Z c_W s_\beta & -|\mu|e^{i\varphi_\mu} & 0 \end{pmatrix}$$

 $s_{\beta} \equiv \sin \beta$, $c_{\beta} \equiv \cos \beta$

- μ : Higgs-higgsino mass parameter (M₂ : SU(2) gaugino mass parameter) M₁ : U(1) gaugino mass parameter (tan β = ^{v₂}/_{v₁} : ratio of Higgs VEVs)
 Diagonalization ⇒ complex mixing matrices → enter ^x/_ℓ, ^x ⁰ couplings → φ_{M₁}, φ_μ dependence of σ, Γ, BR
 - → CP asymmetries

Introduction Parameter determination

- Aim: determination of parameters with phases in $\tilde{\chi}^{\pm}$, $\tilde{\chi}^{0}$ sectors
- CP-even observables: cross sections, masses, ...

[Choi, Djouadi, Song, Zerwas, '98; Kneur, Moultaka, '99; Barger, Han, Li, Plehn, '99] [Choi, Guchait, Kalinowski, Zerwas, '00; Choi, Djouadi, Guchait, Kalinowski, Song, Zerwas, '00] [Choi, Kalinowski, Moortgat-Pick, Zerwas, '01, '02; Gounaris, Mouël, '02] [Choi, Drees, Gaissmaier, '04]

→ Determination of $|\mu|$, φ_{μ} , $|M_1|$, φ_{M_1} , M_2 , tan β in principle possible However: ambiguities for phases remain

CP-odd/T-odd observables needed

recent studies e.g. [Choi, Kim, '03; Choi, '03, '04; Aguilar-Saavedra, '04] [Eberl, Gajdosik, Majerotto, Schraußer, '05; Choi, Chung, Kalinowski, Kim, Rolbiecki, '05] [Frank, Turan, de la Cruz do Oña, '05; Bartl, Christova, Hohenwarter-Sodek, Kernreiter, '06] [Bartl, Fraas, Hohenwarter-Sodek, Kernreiter, Moortgat-Pick, Wagner, '06] [Langacker, Paz, Wang, Yavin, '07; Osland, Vereshagin, '07]

▶ Here: T-odd/CP-odd asymmetries in $\tilde{\chi}^{\pm}$, $\tilde{\chi}^{0}$ production and decay

Triple product asymmetries

\$\tilde{\chi}^{\pm}\$, \$\tilde{\chi}^{0}\$ production with subsequent 2-body decays
 Leptonic decays

 [Bartl, Fraas, Kittel, Majerotto,'03]
 [Bartl, Fraas, Kernreiter, Kittel, Majerotto, '03]
 [Bartl, Fraas, Kittel, Majerotto, '04]

[Bartl, Fraas, Kittel, Majerotto, '04] [Kittel, Bartl, Fraas, Majerotto, '04]

• CP asymmetries using tau polarization for $\ell = \tau$

Decays into W and Z

[Bartl, Kernreiter, Kittel, '03] [Choi, Drees, Gaissmaier, Song, '03]

Monte Carlo study for neutralino production and decay

[Aguilar-Saavedra, '04]

Here: $\tilde{\chi}^{\pm}$, $\tilde{\chi}^{0}$ production with subsequent 3-body decays

Triple product asymmetries

Chargino/neutralino production with subsequent three-body decays

$$e^+e^- \longrightarrow \tilde{\chi}_i + \tilde{\chi}_j \longrightarrow \tilde{\chi}_i + \tilde{\chi}_1^0 f \bar{f}^{(\prime)}$$

Full spin correlation between production and decay [Moortgat-Pick, Fraas, '97; Moortgat-Pick, Fraas, Bartl, Majerotto, '98, '99; Choi, Song, Song, '99]

• Amplitude squared
$$|T|^2 = PD + \sum_{a=1}^{3} \Sigma_P^a \Sigma_D^a$$

• In Σ_P^a and Σ_D^a : products like $i \epsilon_{\mu\nu\rho\sigma} p_i^{\mu} p_j^{\nu} p_k^{\rho} p_l^{\sigma}$

 \Rightarrow with complex couplings: real contributions to observables

 \Rightarrow CP violation at tree level

Triple product asymmetries

Triple products:
$$\begin{aligned} \mathcal{T} = \vec{p}_{e^-} \cdot (\vec{p}_f \times \vec{p}_{\bar{f}^{(\prime)}}) \text{ or } \mathcal{T} = \vec{p}_{e^-} \cdot (\vec{p}_{\bar{\chi}_j} \times \vec{p}_f) \end{aligned}$$

$$\rightarrow \text{T-odd asymmetry:} \quad A_T = \frac{\sigma(T > 0) - \sigma(T < 0)}{\sigma(T > 0) + \sigma(T < 0)} = \frac{\int \text{sign}(\mathcal{T}) |T|^2 d\text{Lips}}{\int |T|^2 d\text{Lips}}$$

 \rightarrow CP-odd, if final state interactions, finite-widths effects negligible \rightarrow for $\tilde{\chi}^{\pm}$ possible: define CP-odd asymmetry $A_{CP} = \frac{1}{2}(A_T - \bar{A}_T)$

 \bar{A}_T : A_T for charge-conjugated process

T-odd asymmetry in $ilde{\chi}^0$ sector

Asymmetry A_T for $e^+e^- \rightarrow \tilde{\chi}_1^0 \tilde{\chi}_2^0 \rightarrow \tilde{\chi}_1^0 \tilde{\chi}_1^0 \ell^+ \ell^-$, $\mathcal{T} = \vec{p}_{e^-} \cdot (\vec{p}_{\ell^+} \times \vec{p}_{\ell^-})$ [Bartl, Fraas, SH, Hohenwarter-Sodek, Moortgat-Pick, hep-ph/0406190]

 $\tan \beta = 10, M_2 = 300 \text{ GeV}, |M_1| = 150 \text{ GeV}, |\mu| = 200 \text{ GeV}, \varphi_{\mu} = 0$ $m_{\tilde{e}_L} = 267.6 \text{ GeV}, m_{\tilde{e}_R} = 224.4 \text{ GeV}, P_{e^-} = -0.8, P_{e^+} = +0.6$



 $\rightarrow A_T$ larger closer to threshold (spin correlations)

T-odd asymmetry in $ilde{\chi}^0$ sector



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Asymmetry A_{CP} for $e^+e^- \rightarrow \tilde{\chi}_2^- \tilde{\chi}_1^+ \rightarrow \tilde{\chi}_2^- \tilde{\chi}_1^0 c\bar{s}$, $\mathcal{T} = \vec{p}_{e^-} \cdot (\vec{p}_{\bar{s}} \times \vec{p}_c)$ [Bartl, Fraas, SH, Hohenwarter-Sodek, Kernreiter, Moortgat-Pick, hep-ph/0608065] \rightarrow tagging of c jet important

 $\tan \beta = 5, M_2 = 150 \text{ GeV}, |M_1| = M_2 5/3 \tan^2 \theta_W, |\mu| = 320 \text{ GeV}, m_{\tilde{\nu}} = 250 \text{ GeV}, m_{\tilde{u}_L} = 500 \text{ GeV}, \sqrt{s} = 500 \text{ GeV}, P_{e^-} = -0.8, P_{e^+} = +0.6, P_{e^-} = +0.8, P_{e^+} = -0.6$



Contours of A_{CP} [in %] and $\mathcal{N}_{\sigma} = \sqrt{2A_{CP}^2 \sigma \mathcal{L}_{int}}$ for $e^+e^- \rightarrow \tilde{\chi}_2^- \tilde{\chi}_1^+ \rightarrow \tilde{\chi}_2^- \tilde{\chi}_1^0 c\bar{s}$ $\tan \beta = 5$, $|M_1| = M_2 5/3 \tan^2 \theta_W$, $m_{\tilde{\nu}} = 250 \text{ GeV}$, $m_{\tilde{u}_L} = 500 \text{ GeV}$, $\varphi_{M_1} = 0.5\pi$, $\varphi_{\mu} = 0$ $\sqrt{s} = 500 \text{ GeV}$, $P_{e^-} = -0.8$, $P_{e^+} = +0.6$, $\mathcal{L}_{int} = 500 \text{ fb}^{-1}$



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Contours of A_{CP} [in %] and \mathcal{N}_{σ} for $e^+e^- \to \tilde{\chi}_1^- \tilde{\chi}_1^+ \to \tilde{\chi}_1^- \tilde{\chi}_1^0 c\bar{s}$ $\tan \beta = 5$, $|M_1| = M_2 5/3 \tan^2 \theta_W$, $m_{\tilde{\nu}} = 250$ GeV, $m_{\tilde{u}_L} = 500$ GeV, $\varphi_{M_1} = 0.5\pi$, $\varphi_{\mu} = 0$ $\sqrt{s} = 500$ GeV, $P_{e^-} = -0.8$, $P_{e^+} = +0.6$, $\mathcal{L}_{int} = 500$ fb⁻¹



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Chargino/neutralino production

$$e^+e^- \longrightarrow \tilde{\chi}_i + \tilde{\chi}_j$$

with transverse beam polarization (4-vector t^{μ}_{\pm} , polarization degree $\mathcal{P}^{T}_{e^{\pm}}$)

• Terms in amplitude squared $|T|^2 = P$ depending on $\mathcal{P}_{e^{\pm}}^T$: $P_T \sim \mathcal{P}_{e^{-}}^T \mathcal{P}_{e^{\pm}}^T [f_1 \Delta_1 r_1 + f_2 \Delta_2 r_2]$

 f_i : couplings; Δ_i : propagators; r_i : products of t_{\pm} and momenta

 \Rightarrow both beams have to be polarized (in limit $m_e = 0$!) [POWER report, hep-ph/0507011]

- r_1 is real; r_2 is imaginary, consisting of products like $i\epsilon_{\mu\nu\rho\sigma}t^{\mu}_{\pm}p^{\nu}_{i}p^{\rho}_{j}p^{\sigma}_{k}$ \Rightarrow with complex couplings f_2 : real contributions to observables
 - \Rightarrow CP-odd terms $\sim \text{Im}(f_2\Delta_2)\text{Im}(r_2)$ at tree level

Chargino production:

Dirac particles: couplings $f_2\Delta_2$ have to be real (CPT invariance)

- \Rightarrow CP-odd terms $f_2\Delta_2r_2$ vanish [Bartl, Hohenwarter-Sodek, Kernreiter, Rud, '04]
- \rightarrow CP-even asymmetries can be defined with help of $f_1 \Delta_1 r_1$
- Neutralino production:

Majorana particles: t and u channels contribute

- \Rightarrow CP-odd terms $f_2 \Delta_2 r_2 \neq 0$ allowed
- \Rightarrow CP-odd observables can be defined

Analysis for subsequent 2-body decays

[Choi, Drees, Song, '06]

 $f_2 \Delta_2 r_2 \sim \sin(\eta - 2\phi)$

with ϕ : azimuthal angle of scattering plane; η : orientation of transverse polarizations

- CP-odd asymmetry
 - ϕ integration:

$$A_{\rm CP}(\theta) = \frac{1}{\sigma} \left[\int_{\frac{\eta}{2}}^{\frac{\pi}{2} + \frac{\eta}{2}} - \int_{\frac{\pi}{2} + \frac{\eta}{2}}^{\pi + \frac{\eta}{2}} + \int_{\pi + \frac{\eta}{2}}^{\frac{3\pi}{2} + \frac{\eta}{2}} - \int_{\frac{3\pi}{2} + \frac{\eta}{2}}^{2\pi + \frac{\eta}{2}} \right] \frac{d^2\sigma}{d\phi \, d\theta} d\phi$$

• θ integration:

$$A_{\mathsf{CP}} = \left[\int_0^{\pi/2} - \int_{\pi/2}^{\pi}\right] A_{CP}(\theta) \,\mathrm{d}\theta$$

 \rightarrow 8 sectors with alternating sign

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Contours of A_{CP} [in %] and $\mathcal{L}_{int} = \mathcal{N}_{\sigma}^2/(A_{CP}^2\sigma)$ for $e^+e^- \rightarrow \tilde{\chi}_1^0 \tilde{\chi}_2^0$ $\tan \beta = 5$, $|M_1| = M_2 5/3 \tan^2 \theta_W$, $m_{\tilde{e}_L} = 400$ GeV, $m_{\tilde{e}_R} = 150$ GeV $\phi_{M_1} = 0.5\pi$, $\phi_{\mu} = 0$ $\sqrt{s} = 500$ GeV, $\mathcal{N}_{\sigma} = 5$



Asymmetries including neutralino decay

$$e^+e^- \to \tilde{\chi}^0_i + \tilde{\chi}^0_j \to \tilde{\chi}^0_i + \tilde{\ell}^\pm_{L,R} \ell^\mp_1 \to \tilde{\chi}^0_i + \tilde{\chi}^0_1 \ell^\mp_1 \ell^\pm_2$$

•
$$A_{1}^{\mp} = \frac{1}{\sigma_{1}} \left[\int_{\frac{\eta}{2}}^{\frac{\pi}{2} + \frac{\eta}{2}} - \int_{\frac{\pi}{2} + \frac{\eta}{2}}^{\pi + \frac{\eta}{2}} + \int_{\pi + \frac{\eta}{2}}^{\frac{3\pi}{2} + \frac{\eta}{2}} - \int_{\frac{3\pi}{2} + \frac{\eta}{2}}^{2\pi + \frac{\eta}{2}} \right] \frac{\mathrm{d}\sigma_{1}}{\mathrm{d}\phi_{\ell_{1}^{\mp}}} \mathrm{d}\phi_{\ell_{1}^{\mp}}$$

with $\sigma_{1} = \sigma(e^{+}e^{-} \to \tilde{\chi}_{i}^{0}\tilde{\chi}_{j}^{0}) \times BR(\tilde{\chi}_{j}^{0} \to \tilde{\ell}\ell_{1})$

•
$$A_{2}^{\pm} = \frac{1}{\sigma_{2}} \left[\int_{\frac{\eta}{2}}^{\frac{\pi}{2} + \frac{\eta}{2}} - \int_{\frac{\pi}{2} + \frac{\eta}{2}}^{\pi + \frac{\eta}{2}} + \int_{\pi + \frac{\eta}{2}}^{\frac{3\pi}{2} + \frac{\eta}{2}} - \int_{\frac{3\pi}{2} + \frac{\eta}{2}}^{2\pi + \frac{\eta}{2}} \right] \frac{d\sigma_{2}}{d\phi_{\ell_{2}^{\pm}}} d\phi_{\ell_{2}^{\pm}}$$

with $\sigma_{2} = \sigma(e^{+}e^{-} \to \tilde{\chi}_{i}^{0}\tilde{\chi}_{j}^{0}) \times BR(\tilde{\chi}_{j}^{0} \to \tilde{\ell}\ell_{1}) \times BR(\tilde{\ell} \to \tilde{\chi}_{1}^{0}\ell_{2})$

→ Distinguishing of ℓ_1 and ℓ_2 necessary (energy/angular distributions) → $A_i^- = -A_i^+$

Asymmetries including neutralino decay

•
$$A'^{-} = \frac{(\int^{+} - \int^{-})(\frac{d\sigma_{1}}{d\phi_{\ell_{1}}}d\phi_{\ell_{1}} + \frac{d\sigma_{2}}{d\phi_{\ell_{2}}}d\phi_{\ell_{2}})}{\int_{0}^{2\pi}(\frac{d\sigma_{1}}{d\phi_{\ell_{1}}}d\phi_{\ell_{1}} + \frac{d\sigma_{2}}{d\phi_{\ell_{2}}}d\phi_{\ell_{2}})} = \frac{A_{1}^{-} + A_{2}^{-} BR(\tilde{\ell} \to \ell \tilde{\chi}_{1}^{0})}{1 + BR(\tilde{\ell} \to \ell \tilde{\chi}_{1}^{0})}$$

 \int^{\pm} : integration over regions where $\sin(\eta - 2\phi_{\ell_{1,2}})$ is positive/negative

 \rightarrow Only measurement of charges of ℓ_1 and ℓ_2 necessary (no distinguishing of ℓ_1 and ℓ_2 required)



Outlook: SUSY phases in Higgs sector

- Possibly strong impact on Higgs search
- Projects within NExT Institute

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(Southampton University \leftrightarrow PPD, RAL)
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http://www.hep.phys.soton.ac.uk/next/NEXT_web/NEXT_web.htm

- SUSY phase dependence of $BR(H_1 \rightarrow \gamma \gamma)$
 - [Moretti, Munir, Poulose, '07; SH, Moretti, Munir, Poulose, in preparation]
 - → strong phase dependence possible
- Analysis of CPV in MSSM for LHC Higgs search

 \rightarrow Implications of light Higgs ($m_{H_1} \sim 50 \text{ GeV}$) \leftrightarrow NMSSM

Analysis of explicit CP violation in NMSSM

NEx1

Summary

- Aim: revealing the CP structure of the underlying model
 - CP-even observables \rightarrow ambiguities remain
 - CP-odd observables needed
 - \rightarrow here: T-odd/CP-odd asymmetries in $\tilde{\chi}^{\pm}$, $\tilde{\chi}^{0}$ production + decay
- Triple product asymmetries
 - Neutralinos: leptonic decays: $\mathcal{T} = \vec{p}_{e^-} \cdot (\vec{p}_{\ell^+} \times \vec{p}_{\ell^-})$ hadronic decays: discrimination of $c \leftrightarrow \bar{c}$ or $b \leftrightarrow \bar{b}$
 - Charginos: leptonic decays: reconstruction of $p(\tilde{\chi}^+)$ hadronic decays: discrimination of $c \leftrightarrow s$ jets
- CP-odd asymmetries with transverse beam polarization
 both beams have to be polarized
- ▲ Asymmetries of $\mathcal{O}(10\%-20\%)$ possible
 ⇒ important tool for → search for CP violation in SUSY
 → unambiguous determination of SUSY phases

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