# Precision Measurement of the Stop Mass at the Linear Collider <br> LCWS2007 \& ILC2007-SUSY- June 2-2007 <br> Desy- Hamburg 

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## Introduction

- We have previously studied the light stop, with a small mass difference to the neutralino, in an attempt to understand EW baryogenesis the asymmetry matter anti-matter and its role in dark matter annihilation.
Phys. rev. D 72,115008(2005)
M. Carena, A. Finch, A. Freitas, C. Milstene, H. Nowak, A. Sopczak

The mass precision measurement reached was $\delta m \sim 1.2 \mathrm{GeV}$.
This analysis aims at the minimization of the systematics while using more realistic data, stop hadronization/fragmentation included.

- The precision is improved in two ways:
a/ The systematic uncertainties are minimized by measuring the production cross-section at two energies $\rightarrow$ cancellations .
b/ The $2^{\text {nd }}$ energy point chosen at or close to the production energy threshold
$\rightarrow$ increased sensitivity to mass changes.
- The stop hadronization is included at production $\rightarrow$ the c quark energy is spread out in the process of hadronization.
the final number jets increases- the c-tagging is now a necessity to identify the charm jets (bench-marking for the vertex detector)
- Two approaches are used, a cut based analysis, a multi-parameters optimization analysis IDA
- The polarization improves further the.sidystaheto background ratio


## Cross-Section Precision In Production



Cross-sections [fb] calculated using NLO In MC software by Freitas et al EPJ
C21(2001)361,
EPJ C34(2004)487

## The Method

$$
\begin{aligned}
& \sigma=\frac{N-B}{\varepsilon L} \\
& Y\left(M_{x} \sqrt{s_{t h}}\right)=\frac{N_{t h}-B_{t h}}{N_{p k}-B_{p k}}=\frac{\sigma\left(\sqrt{s_{t h}}\right)}{\sigma\left(\sqrt{s_{p k}}\right)}
\end{aligned}
$$

$\sigma$ the cross-section [fb]
N the number of selected data events
$B$ number of estimated background events
s Square of the energy in center of Mass
$\mathrm{N}_{\mathrm{th}}, \mathrm{B}_{\mathrm{th}}, \mathrm{s}_{\mathrm{th}}$ at or close to production threshold
$\mathrm{N}_{\mathrm{pk}}, \mathrm{B}_{\mathrm{pk}}, \mathrm{S}_{\mathrm{pk}}$, at peak value
$\varepsilon$ total efficiency \& acceptance
L Integrated luminosity
$M_{x}$ : Mass to be determined with high precision.
$Y$ ratio of cross-section $\sigma_{\mathrm{th}}$ and $\sigma_{\mathrm{pk}} \rightarrow$ Allows Reduction of systematic uncertainty as well as uncertainties from $L$ measurement.
Remark: yield close to threshold is very sensitive to $M_{x} \rightarrow$ choice of $N_{t h}$ and $B_{\text {th .. }}$
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## Determination of the Stop Mass


$Y=f\left(M_{x}\right)$ from the theoretical cross-section is be drawn in Red
$Y$ from the data the blue line.
As an example, Assume 2\% precision for Y , The blue hashed region $\rightarrow$ one obtains $\rightarrow$ Precision $\Delta M_{x}= \pm 1 \%$, the 2 vertical arrows

The Scenario depicted:
$\mathrm{E}_{\mathrm{CM}}=260 \mathrm{GeV}$ with $\sigma=9.2 \mathrm{fb}$ and $\sigma=77 \mathrm{fb}$ at peak

Remark: Assumed luminosities
$\mathrm{L}_{\mathrm{th}}=50 \mathrm{fb}^{-1}(260 \mathrm{GeV}), \mathrm{L}_{\mathrm{pk}}=500 \mathrm{fb}^{-1}(500 \mathrm{GeV})$

$$
e^{+} e^{-} \rightarrow \widetilde{t_{1} t_{1}} \rightarrow c \tilde{\chi}_{0}^{-} \bar{c} \tilde{\chi}_{0}^{1}
$$

-Analysis uses N -tuple tool incorporating jet finding algorithm (T. Kuhl)
-Soft Multi-jets in the final state
-Stop Hadronization $\rightarrow$ the final state jets smeared :
due to gluon radiation + fragmentation
-At ECM=260 GeV mostly 2 jets, carry the charm.
-At ECM $=500 \mathrm{GeV}$ 2jets $\rightarrow 2,3,4$ jets (more energy available in the CM )
$\rightarrow$ the Charm tagging a necessary tool to identify the charm jets (Vertex bench-marking)

## Simulation Characteristics

- Signal and Background generated with: Pythia (6.129) Simdet (4-0-3)- Circe(1.0)
- Hadronisation of the c quark and the $\tilde{t}$ from the Lund string fragmentation Pythia uses Peterson fragmentation
(Peterson et al PR D27:105)
- The t fragmentation is simulated using Torbjorn code
/http://wwwthep.lu.se/torborn/pythia/main73 f
The $\check{t}_{1}$ quark is set stable until after fragmentation where it is
Allowed to decay again as described in (Kraan, EPJ C37:91)
- Signal and Background are generated in each channel for the given luminosity in conjunction to the cross-sections


## Jet Multiplicity - Without/With Fragmentation



- Stop fragmentation simulated using Torbjorn code //http://www.thep.Iu.seftorbiorn/pythia/mai n73.f
-The stop fragmentation parameter is set relative to the bottom fragmentation parameter
$\tilde{\varepsilon}=\varepsilon_{-} b^{*} m_{b}{ }^{2 / / / \tilde{t}^{2}}$
And $\varepsilon \_b=-0.0050+1-0.0015$ following (OPAL,EPJ C6:225)
-The jet Multiplicity without Fragmentation
Upper figure
~ 70\% 2 jets
-The jet Multiplicity with t Fragmentation
Lower Figure
~ 50\% 3 jets
\& bigger admixture of 4jets


## Background- Channels @500 GeV



Z Phys. C 76 (1997) 549- A.Bartl, H. Eberl,S. Kraml, W.Majerotto,W.Porod,A. Sopczak

## The cross-sections

| Process | $\sigma[\mathrm{pb}]$ at ECM=260GeV |  |  | $\sigma[\mathrm{pb}]$ at ECM=500GeV |  |  |
| :--- | :---: | :---: | :---: | :--- | :---: | :---: |
| $\mathrm{P}(\mathrm{e}-) / \mathrm{P}(\mathrm{e}+)$ | $0 / 0$ | $-80 \% /+60 \%$ | $+80 \% /-60 \%$ | $0 / 0$ | $-80 \% /+60 \%$ | $+80 \% /-60 \%$ |
| $\tilde{\mathrm{t}}_{1} \tilde{\mathrm{t}}_{1}{ }^{*}$ | 0.032 | 0.017 | 0.077 | 0.118 | 0.072 | 0.276 |
| W W | 16.9 | 48.6 | 1.77 | 8.6 | 24.5 | 0.77 |
| Z Z | 1.12 | 2.28 | 0.99 | 0.49 | 1.02 | 0.44 |
| Wenu | 1.73 | 3.04 | 0.50 | 6.14 | 10.6 | 1.82 |
| eeZ | 5.1 | 6.0 | 4.3 | 7.5 | 8.5 | 6.2 |
| qq, qq $\neq \mathrm{tt}$ | 49.5 | 92.7 | 53.1 | 13.1 | 25.4 | 14.9 |
| tt | 0.0 | 0.0 | 0.0 | 0.55 | 1.13 | 0.50 |
| $2 \mathrm{y}\left(\mathrm{p}_{\mathrm{t}}>5 \mathrm{GeV}\right)$ | 786 |  |  | 936 |  |  |
|  |  |  |  |  |  |  |

Table 1
A. Freitas et al EPJ C21(2001)361, EPJ C34(2004)487 and GRACE and COMPHEP -Next to leading order, assuming a stop mixing angle (0.01)
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## Selection Cuts at $\mathrm{E}_{\mathrm{Cm}}=260,500 \mathrm{GeV}$

| Variable | $\begin{gathered} \mathrm{ECM} \\ 260 \mathrm{GeV} \end{gathered}$ | $\begin{gathered} \mathrm{ECM} \\ 500 \mathrm{GeV} \end{gathered}$ |
| :---: | :---: | :---: |
| Number of jets | $\mathrm{N}_{\text {jets }}=2$ | $\begin{gathered} \mathrm{N}_{\text {jets }} \geq 2 \& \mathrm{E}_{\mathrm{n}}<25 \mathrm{GeV} \\ \mathrm{n}=3,4, . . \end{gathered}$ |
| Transverse Momentum $\mathrm{p}_{\mathrm{t}}$ Thrust T $\cos \theta_{\text {Thrust }}$ Visible Energy $\mathrm{E}_{\text {vis }}$ Acoplanarity $\Phi_{\text {acop }}$ Invariant mass of jet pair $\mathrm{m}_{\mathrm{j}}$ Charm tagging likelihood $P_{c}$ | $\begin{aligned} & \mathrm{p}_{\mathrm{t}}>10 \mathrm{GeV} \\ & - \\ & \left\|\cos \theta_{\text {Thrust }}\right\|<0.7 \\ & \mathrm{E}_{\text {vis }}<0.175 \text { *ECM } \\ & \left\|\Phi_{\text {acop }}\right\|<0.9 \\ & 25.5 \mathrm{GeV}<\mathrm{m}_{\mathrm{jj}}<90 \mathrm{GeV} \\ & \mathrm{P}_{\mathrm{c}}>40 \% \end{aligned}$ | $\begin{aligned} & \mathrm{p}_{\mathrm{t}}>12 \mathrm{GeV} \\ & \mathrm{~T}>0.8 \\ & \left\|\cos \theta_{\text {Thrust }}\right\|<0.7 \\ & \mathrm{E}_{\text {vis }}<0.4 \text { *ECM } \\ & \left\|\Phi_{\text {acop }}\right\|<0.9 \\ & 60 \mathrm{GeV}<\mathrm{m}_{\mathrm{jj}}<90 \mathrm{GeV} \\ & \mathrm{P}_{\mathrm{c}}>40 \% \end{aligned}$ |

Table 2
In order to optimize the cancellation of the systematics we aim to have a selection as similar as possible at the two energies. (cancellation in Y )
The two-photons background did require a 5 GeV pt cut.

## Events Generated and After Sequential cuts

|  | $\mathrm{L}=50 \mathrm{fb}^{-1}$ at ECM=260GeV |  |  | $\mathrm{L}=500 \mathrm{fb}^{-1}$ at $\mathrm{ECM}=500 \mathrm{GeV}$ |  |  |
| :--- | :---: | :---: | :---: | :--- | :--- | :---: |
| $\mathrm{P}(\mathrm{e}-) / \mathrm{P}(\mathrm{e}+)$ | Generated | $0 / 0$ | $+80 \% /-60 \%$ | Generated | $0 / 0$ | $+80 \% /-60 \%$ |
| $\tilde{\mathrm{t}}_{1} \tilde{\mathrm{t}}_{1}{ }^{*}$ | 50000 | 382 | 921 (24\%eff.) | 50000 | 11300 | 26430 (19\%eff.) |
| WW | 180000 | $<5$ | $<1$ | 210000 | 102 | 9 |
| ZZ | 30000 | $<2$ | $<2$ | 30000 | 250 | 224 |
| Wenu | 210000 | 36 | 4 | 210000 | 10102 | 2994 |
| eeZ | 210000 | $<1$ | $<1$ | 210000 | $<18$ | $<15$ |
| qq, qұt | 350000 | $<7$ | $<8$ | 350000 | 19 | 22 |
| tt | - | 0 | 0 | 180000 | 21 | 19 |
| 2-Photons | $1.610^{6}$ | 12 | 12 | $8.5 \times 10^{6}$ | 120 | 120 |

Table 3
0/0 polarization beam $\rightarrow$ Unambiguous discovery $+80 \% /-60 \%$ polarization $\rightarrow$ Precision Measurement
Remark: $\tilde{\mathrm{t}}_{1}$ fragmentation $\rightarrow$ the separation from the Wenu more difficult

## Iterative Discriminant Analysis (IDA)

- Improves even more the precision in the $\tilde{\mathrm{t}}_{1}$ mass measurement an Iterative Discriminant Analysis (IDA) is used. (modified Fisher Disc. Analysis) - IDA combines the kinematic variables in parallel. The same variables and simulated events are used than in the cut based analysis. A non linear discriminant function followed by iterations are enhancing the separation between signal and background.
- Both the signal and background have been divided in two equally sized samples, one sample is used for training, the other as data.
- Two IDA steps have been performed, with a cut after the $1^{\text {st }}$ IDA iteration keeping $99 \%$ of the signal efficiency.
- The performance is shown in the two next figures at 260 and 500 GeV .


## Invariant Mass Di-Jets Before Final IDA



## IDA Performance


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## Events Generated and After IDA Selection

|  | $\mathrm{L}=50 \mathrm{fb}^{-1}$ at $\mathrm{ECM}=260 \mathrm{GeV}$ |  |  | $\mathrm{L}=500 \mathrm{fb}^{-1}$ at $\mathrm{ECM}=500 \mathrm{GeV}$ |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{P}(\mathrm{e}-) / \mathrm{P}(\mathrm{e}+$ ) |  | +80\%/-6 |  | 0/0 | +80\%/-60\% |  |
| $\tilde{\mathrm{t}}_{1} \tilde{\mathrm{t}}_{1}{ }^{\text {r }}$ | 610 | 1470 | (38\%eff.) | 21240 | 49700 | (36\%eff.) |
| WW | 19 | 2 |  | <41 | <4 |  |
| zZ | 7 | 7 |  | 67 | 60 |  |
| Wenu | 68 | 39 |  | 10640 | 3155 |  |
| eeZ | 10 | 8 |  | <36 | <30 |  |
| qq, q\#\# | 30 | 32 |  | <38 | <43 |  |
| tt | 0 | 0 |  | <3 | <3 |  |
| 2-Photons | <25 | <25 |  | 840 | 840 |  |

Table 4
The efficiencies improves from $24 \%, 19 \%$ cut based $\rightarrow 38 \%, 36 \%$ IDA, while the background is of the same order of magnitude.

## Systematic Uncertainty in Kinematics Cuts Variables

| Variable | Error on <br> variable | Error on Y |
| :--- | :--- | :--- |
| $\mathrm{p}_{\mathrm{t}}$ | $2 \%$ | $0.28 \%$ |
| $\cos \theta_{\text {Thrust }}$ | $1.8 \%$ | $0.18 \%$ |
| $\mathrm{E}_{\text {vis }}$ | $2 \%$ | 0 |
| $\Phi_{\text {acop }}$ | $1 \%$ | $0.08 \%$ |
| $\mathrm{~m}_{\mathrm{jj}}$ | $4 \%$ | $0.61 \%$ |

Table 5
-All cuts are applied to hadronic and jet observables $\rightarrow$ Calibration quantities are jet energy scale \& jet angle.
-Based on LEP, we assume $2 \%$ calibration error for jets, 1 deg for jet angle -Effect on signal efficiency: Partial cancellation between 260 and 500 GeV -We assume cancellation in total luminosity in Y between $260 \& 500 \mathrm{GeV}$

## Effect of Stop and Charm Fragmentation

Comparison of the signal generated with and without gluon radiation
$\rightarrow$ The signal efficiency changes due to jet number cut is $2.5 \%$
$\rightarrow$ We assume an error of $1 \%$ for the number of jets
Charm fragmentation parameters assumed as precise as for LEP/OPAL
$\rightarrow \varepsilon_{\mathrm{c}}=-0.0031 \pm 0.011$

$\varepsilon_{\mathfrak{t} 1}=-0.0050 \pm 0.015$
They don't cancel between the 2 energies but are small
Including the effects of the fragmentation at both energy points
$\delta \varepsilon_{c}= \pm 35 \% \rightarrow$ Error $\delta Y=+1.2 \%-0.2 \%$
$\delta \varepsilon_{\mathfrak{t} 1}= \pm 30 \% \rightarrow$ Error $\delta Y=+0.4 \%+2.4 \%$
$\rightarrow$ contribute an error O(few\%)

## Theoretical Uncertainties

- Precise cross-section calculations are needed
- Stop production receive large corrections from QCD gluon exchange Between the final state stops (bigger @Threshold) $\rightarrow$ Coulomb corr.
- NLO- QCD corrections ~100\% @threshold down to $10 \%$ at high energies are included here
- NNLO-QCD corrections are expected to be same order than NLO based on the results for the top quark. The missing higher order correction ~7\% @260GeV, 2.5\% @500 GeV
- It is expected that theoretical uncertainties can be brought down by a factor 2
- Here we assume an uncertainty of $3.5 \%$ @ 260 GeV and $1 \%$ @ 500 GeV
- The EW corrections : NLO ~several \%, the NNLO ~1\%
- Combined $\rightarrow$ ~4\% @260 GeV and 1.5\% @500GeV $\rightarrow \delta Y=5.5 \%$


## Combined Statistic and systematic Errors

| Error source for Y | Cut-based Analysis |
| :--- | :--- |
| Statistical | $4.1 \%$ |
| Detector Effects | $1.15 \%$ |
| Jet number | $1 \%$ |
| Charm Fragmentation | $1.2 \%$ |
| Stop Fragmentation | $2.4 \%$ |
| Charm tagging algorithm | $<0.5 \%$ |
| Sum of Experimental | $5.2 \%$ |
| Errors |  |
| Theory for signal $\sigma$ | $5.5 \%$ |
| Theory for background $\sigma$ | $0.5 \%$ |
| Total error $\delta Y$ | $7.2 \%$ |

For IDA the determination of systematic uncertainties in progress.

Table 6

## Results

Combining the statistical and systematic errors Table 6(*)
$\delta Y=7.2 \% \rightarrow \delta m_{\mathfrak{t} 1} \sim 0.3 \mathrm{GeV}-$ a factor 4 better (Phys. rev. D 72,115008(2005) (dominated by the theory, expected to improve for signal and background ) $\delta Y=5.2 \% \rightarrow \delta m_{\mathfrak{t} 1} \sim 0.2 \mathrm{GeV}$ (cut based experimental errors alone) $\delta \mathrm{Y}=4.2 \% \rightarrow \delta \mathrm{~m}_{\mathfrak{t} 1} \sim 0.15 \mathrm{GeV}$ (experimental errors \& IDA) (expected)
$\rightarrow$ Improvements in dark matter relic density due to improvement in $\delta m_{\mathfrak{t} 1}$ is shown in the next figure.
Other limiting factors start to interplay, e.g. the precision on the neutralino mass $\delta \mathrm{m}_{\mathrm{x} 0}{ }^{1} \sim 0.3 \mathrm{GeV}$,(hep-ph/0608255, M.Carena, A.Freitas)

## Dark Matter Relic Abundance $=\mathrm{f}\left(\mathrm{m}_{\text {stop }}\right)$



Dark Matter relic density accounting The estimated experimental errors For stop, Chargino, neutralino and Higgs sector -( scan over 1 $\sigma$ ) versus $\mathrm{m}_{\mathrm{st}}{ }^{1}$ for $\delta m_{\mathfrak{t} 1}=1.2 \mathrm{GeV}$ light gray dot Previous study $\delta m_{\mathfrak{t} 1}=0.3 \mathrm{GeV}$ dark gray dot Now this study $\delta m_{\mathfrak{t} 1}=0.15 \mathrm{GeV}$ black dots Expected this study with IDA

$$
\begin{aligned}
& \delta \mathrm{m}_{\mathrm{st}}{ }^{1}=0.3 \mathrm{GeV} \rightarrow \Omega_{\mathrm{CDM}} \mathrm{~h}^{2}=0.109+0.0013-0.010 \\
& \delta \mathrm{~m}_{\mathrm{st}}=0.2 \mathrm{GeV} \rightarrow \Omega_{\mathrm{CDM}} \mathrm{~h}^{2}=0.109+0.0012-0.009 \\
& \delta \mathrm{~m}_{\mathrm{st}}=0.15 \mathrm{GeV} \rightarrow \Omega_{\mathrm{CDM}} \mathrm{~h}^{2}=0.109+0.0011-0.009
\end{aligned}
$$

## Relic Abundance as Function of $\mathrm{m}_{\mathrm{x} 0}{ }^{1}$



Dark Matter relic density as a function of the neutralino mass accounting for the estimated experimental errors as before but as function of the
Lightest neutralino mass $\mathrm{m}_{\mathrm{xo}}{ }^{1}$ Gray dots for $\delta m_{\mathfrak{t} 1}=0.3$ This study Errors from Experiment+theory Black dots for $\delta m_{\mathfrak{t} 1}=0.15$ This Study Experiment. Err. and IDA
$\delta m s t 1=0.3 \mathrm{GeV} \rightarrow \Omega_{\mathrm{CDM}} \mathrm{h}^{2}=0.109+0.0013-0.010$
$\delta m s t 1=0.15 \mathrm{GeV} \rightarrow \Omega_{\mathrm{CDM}} \mathrm{h}^{2}=0.109+0.0011-0.009$
WMAP: $\Omega_{\mathrm{CDM}} \mathrm{h}^{2}=0.1106+0.0056-0.0075$

## Conclusion

- More realistic data were produced including hadronization/fragmentation
- The precision, however, improved by a factor three on our previous analysis with $\delta m_{\mathrm{st}}{ }^{1}=0.3 \mathrm{GeV}$.
- This method could be applied to other particles e.g. to measure the Higgs mass
- The method improves the precision to the mass determination in two ways $\mathrm{a} /$ by reducing the systematics in Y -cancellation between the two energy points. $\mathrm{b} /$ by choosing the energy at threshold, Y extremely sensitive to the mass
- The polarization separates the right-handed signal $\tilde{\mathfrak{t}}_{1}$ from background.
- Due to hadronization and fragmentation the c-tagging was a necessary tool to identify the charm jets at $\mathrm{E}_{\mathrm{CM}}=500 \mathrm{GeV}$ (benchmark for the vertex detector)
- Systematics in progress for the IDA a multi-parameters analysis, expected improvement to $\delta \mathrm{m}_{\mathrm{st}}{ }^{1}=0.15 \mathrm{GeV}$
- Progress in the theoretical calculations is expected and partly accounted for
- With that precision we become limited by other factors.
- With this mass precision, the calculated relic density is in accordance with WMAP and SLOAN ,
$\delta \mathrm{mst} 1=0.15 \mathrm{GeV} \rightarrow \Omega \mathrm{CDM} \mathrm{h} 2=0.109+0.0011-0.009$
WMAP: $\Omega$ CDM h $2=0.1106+0.0056-0.0075$
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## Backup slides

## A Sample Parameter Point

- $\mathrm{m}_{\mathrm{U3}^{2}}{ }^{2}=-99^{2} \mathrm{GeV}^{2}$
- $A_{t}=-1050 \mathrm{GeV}$
- $\mathrm{M}_{1}=112.6 \mathrm{GeV}$
- $M_{2}=225 \mathrm{GeV}$
- $|\mu|=320 \mathrm{GeV}$
- $\Phi \mu=0.2$
- $\tan \beta=5$

Which gives:
$\tilde{m i}_{1}=122.5 \mathrm{GeV} ; \tilde{\mathrm{mt}}_{2}=4203 \mathrm{GeV}$;
$m \tilde{x}_{1}^{0}=107.2 \mathrm{GeV} ; \mathrm{m} \tilde{\mathrm{x}}_{1}{ }^{+}=194.3 \mathrm{GeV} ; m \tilde{x}_{2}{ }^{0}=196.1 \mathrm{GeV}$
$m \tilde{x}_{3}{ }^{0}=325.0 \mathrm{GeV} ; \quad \mathrm{m} \tilde{x}_{2}{ }^{+}=359.3 \mathrm{GeV}$
$\cos \theta \tilde{t}=0.0105 \sim \tilde{t}$ right handed
$\rightarrow \Delta \mathrm{m}=15.2 \mathrm{GeV}$

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