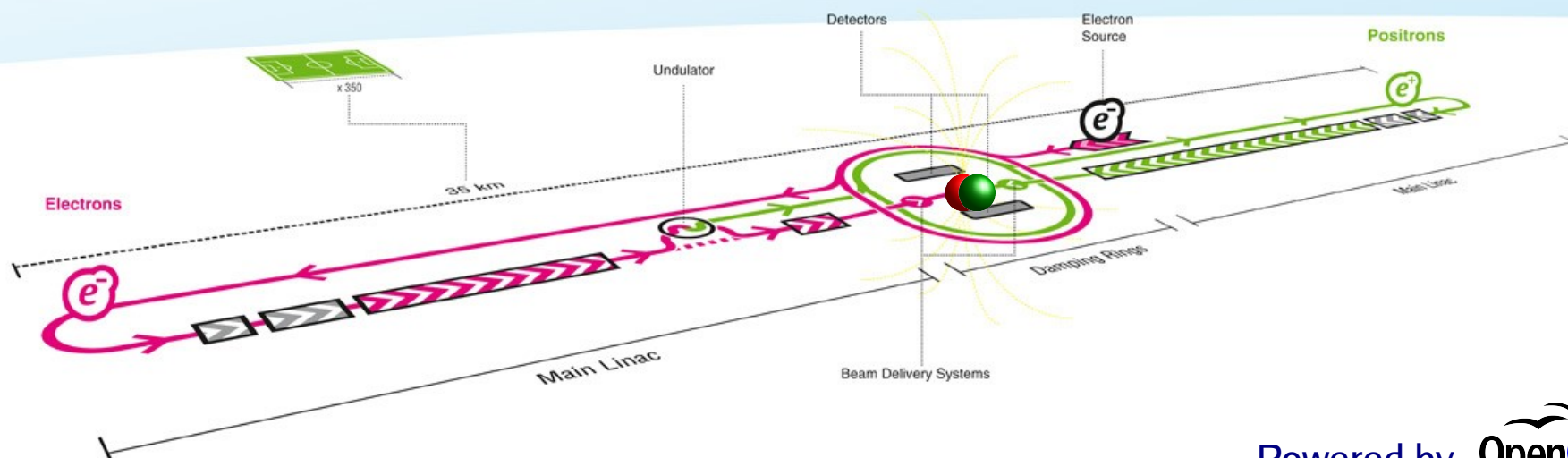
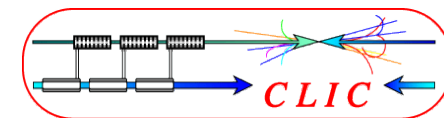


Positron Source for Linear Colliders

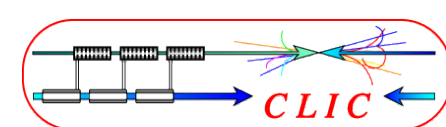
KURIKI Masao (Hiroshima/KEK)





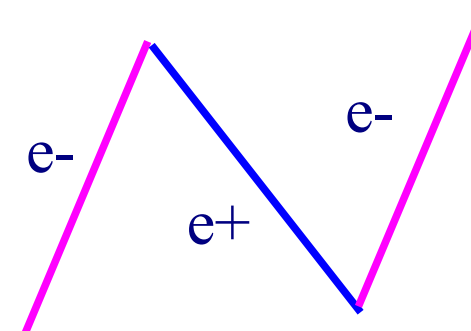
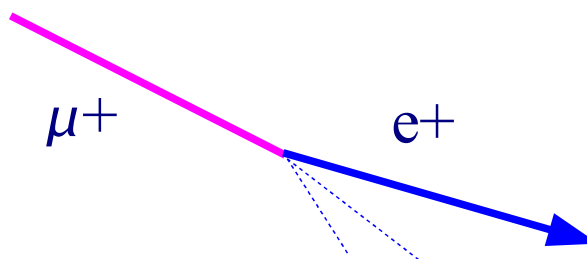
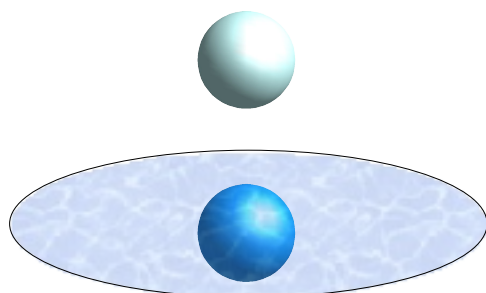
Positron Generation
Positron Capture
Positron Source
ILC Positron Source
Summary

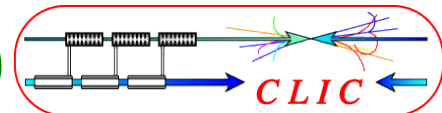
- ▶ Positron Generation
- ▶ Positron Capture
- ▶ Positron Source
- ▶ ILC Positron Sources
- ▶ Summary



Positron Generation
Positron Capture
Positron Source
ILC Positron Source
Summary

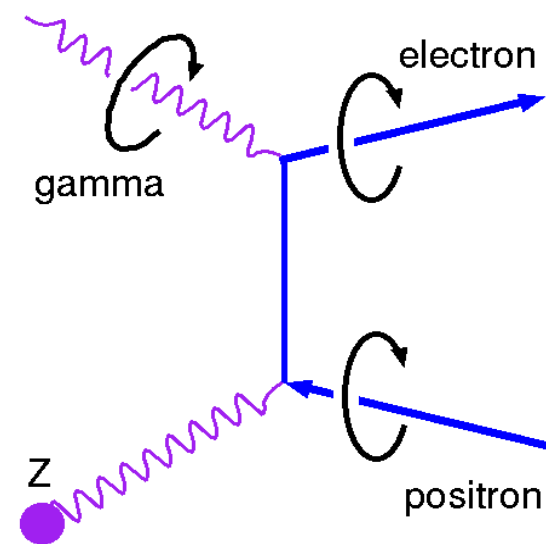
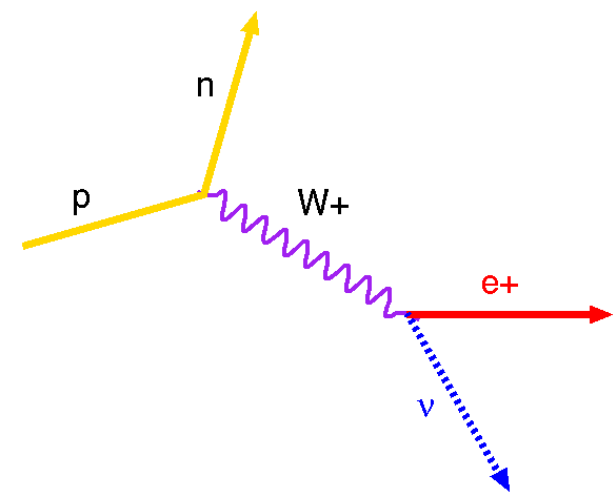
- ▶ 1928: Dirac equation suggested electrons with negative energy. Hole hypothesis: "vacuum" is filled with this negative energy electrons to prohibit Klein's paradox. "hole" in the sea of these electrons, acts as positrons.
- ▶ 1932: Anderson discovered positrons in cosmic rays with cloud chamber.
- ▶ In the modern field theory, positrons are considered to be electrons, which propagate inversely.

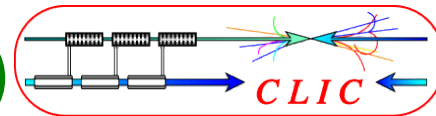




Positron Generation
Positron Capture
Positron Source
ILC Positron Source
Summary

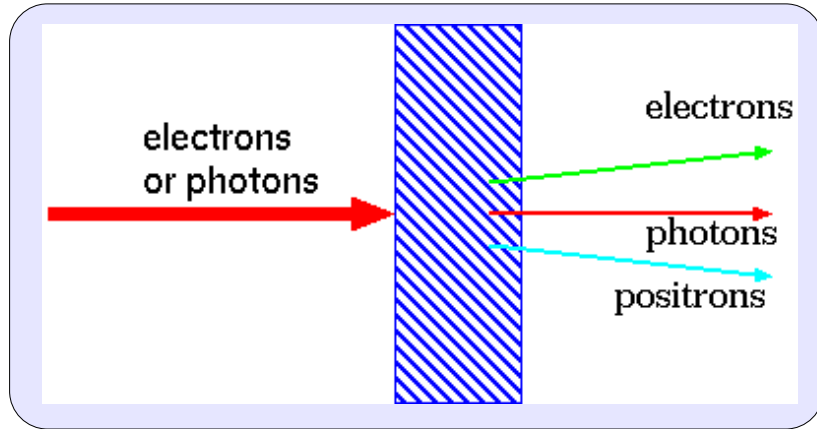
- ▶ There is only few positrons in nature.
- ▶ Two ways to produce positrons :
 - Create radio-active elements, which beta + decays;
 $p \rightarrow n e^+ \text{ neutrino}$.
 - Pair-creation ; $\text{gamma} \rightarrow e^+ e^-$
- ▶ All of the positron beam sources, employ the pair-creation process, which overcomes Compton scattering above 10 MeV region. Photon energy must be more than 10 MeV.

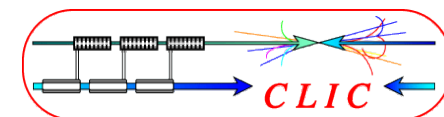




Positron Generation
Positron Capture
Positron Source
ILC Positron Source
Summary

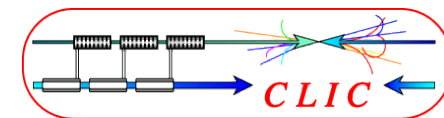
- ▶ Pair-Creation is the only process, which generates positron with a time structure.
- ▶ More than 10MeV gamma ray is required for this process.
 - ▶ EM shower induced by injecting electron beam into a heavy material. (Electron Driven scheme)
 - ▶ High energy gamma is directly produced by
 - ▶ Undulator
 - ▶ Compton back scattering.





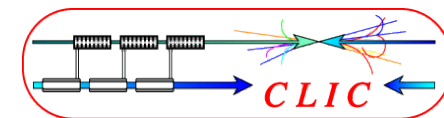
Positron Generation
Positron Capture
Positron Source
ILC Positron Source
Summary

- ▶ Electron energy becomes $1/e$ by passing one radiation length, X_0 . The lost energy is shared by the shower particles.
- ▶ EM shower is mixture of e^- , e^+ and gamma.
- ▶ # of particles is increased by developing the EM shower and decreased by absorption with the target. # of particle is peaked at the shower max. The shower max is a function of the initial energy; $3 - 5 X_0$ for several GeV.
- ▶ Positron beam is obtained by extracting it from the mixed flux.



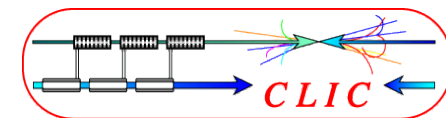
Positron Generation
Positron Capture
Positron Source
ILC Positron Source
Summary

- ▶ Principally, high energy photon can be a replacement of the high energy electron, but such high-energy photon is hard to obtain from undulator or Compton scattering (10 - 60 MeV).
- ▶ In such energy region, EM shower is not grown and photons directly generate positrons through pair creation process.
- ▶ Due to this simplicity, if the photons are polarized, the positrons are also polarized. (Polarized Positron)



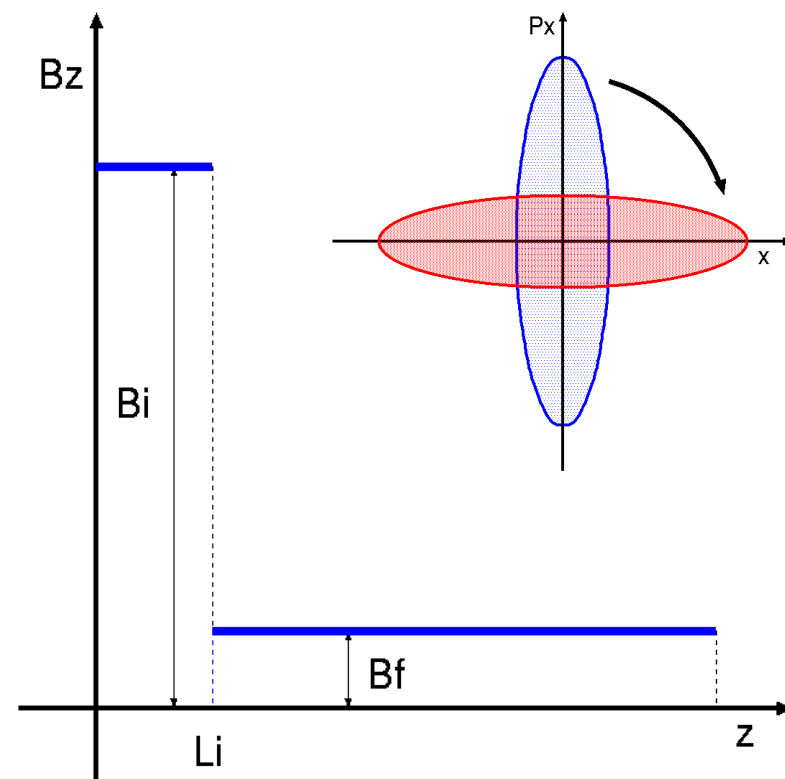
Positron Generation
Positron Capture
Positron Source
ILC Positron Source
Summary

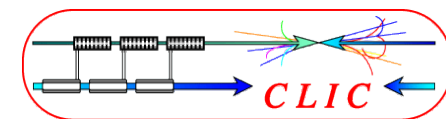
- ▶ Positrons are generated as a mixture of positrons, electrons, and gammas in a large area of phase space.
- ▶ To form the positron beam, we have to
 - **Select only positrons from the flux.**
 - **Capture the positron in a RF bucket.**
- ▶ The generated positrons are distributed in a small spot size and in a large momentum space.
- ▶ This divergent beam has to be converted into a parallel beam to fit the accelerator acceptance.
- ▶ There are two devices:
 - **QWT (Quarter Wave Transformer)**
 - **AMD (Adiabatic Matching Device)**



Positron Generation
Positron Capture
Positron Source
ILC Positron Source
Summary

- ▶ QWT consists from initial strong solenoid field, B_i , and weak solenoid field, B_f , along z direction.
- ▶ It has a good acceptance for a specific energy (longitudinal momentum, p_z), which is determined with $B_i L_i$.
- ▶ It transforms 90° in the phase space, that is why it is called as Quarter Wave Transformer.





Positron Generation
Positron Capture
Positron Source
ILC Positron Source
Summary

- ▶ Positrons at $(r,z)=(0,0)$ circulates with radius $\rho = \frac{p_t}{eB_i}$ in $r-\phi$ plane.

- ▶ If a positron travels L_i in z and $\pi\rho$ (180°) in $r-\phi$, the momentum satisfy,

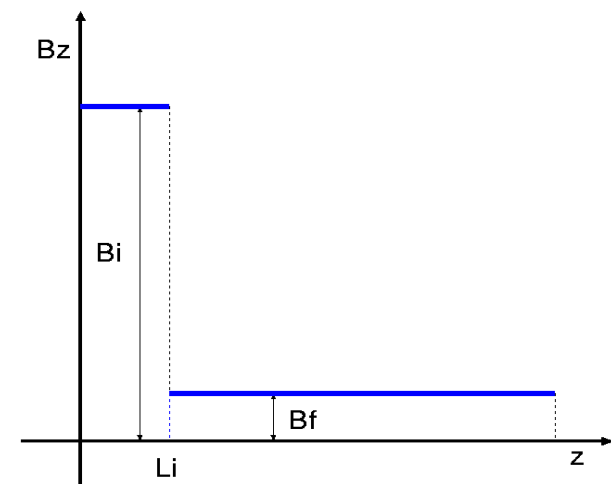
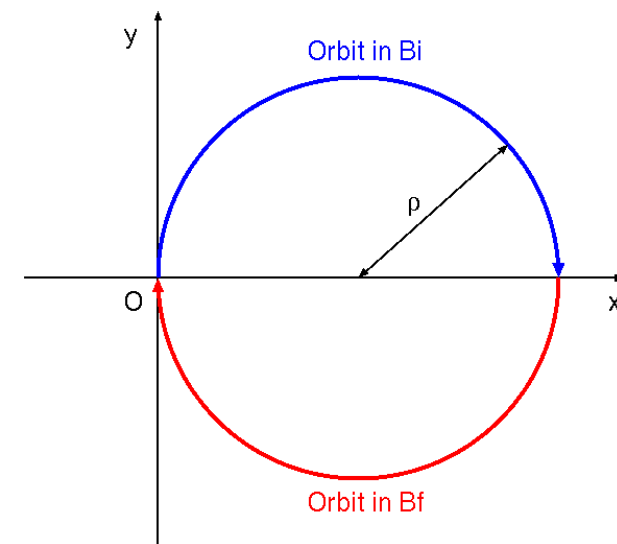
$$p_z = \frac{eB_i L_i}{\pi} \quad \frac{L_i}{\pi\rho} = \frac{p_z}{p_t}$$

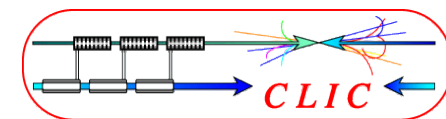
- ▶ The positron is kicked at the boundary of B_i and B_f and the transverse momentum becomes,

$$p_t \rightarrow p_t \frac{B_f}{B_i}$$

- ▶ The orbit radius in B_f area is

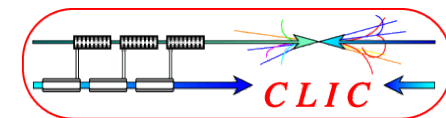
$$\rho_f = \frac{p_t}{eB_f} \frac{B_f}{B_i} = \frac{p_t}{eB_i}, \text{ which is same as } \rho.$$





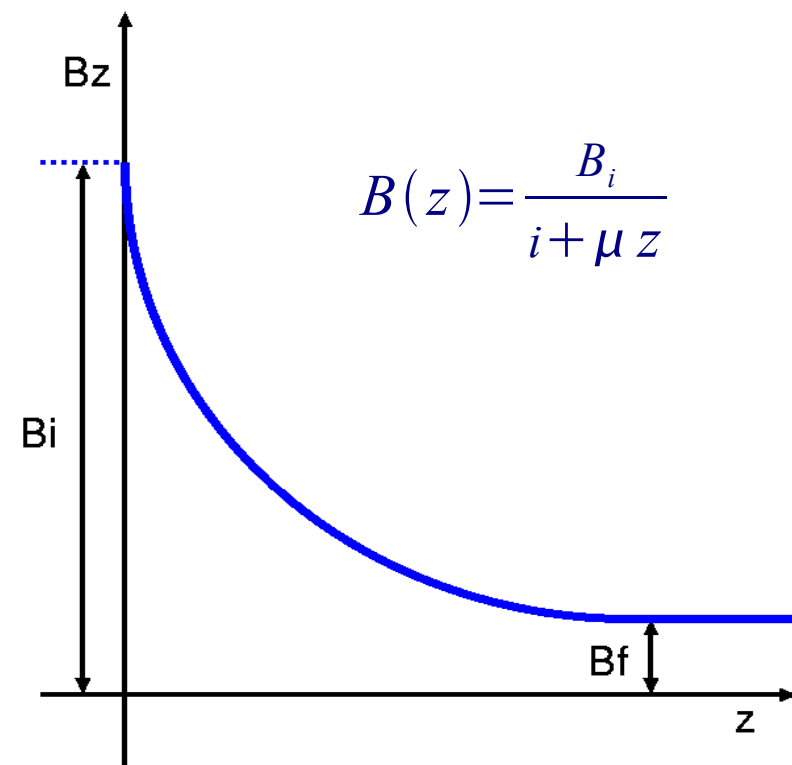
Positron Generation
Positron Capture
Positron Source
ILC Positron Source
Summary

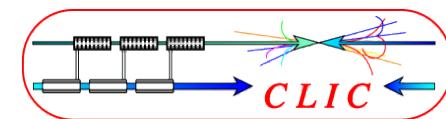
- ▶ The only positrons, which satisfy $p_z = eB_i L_i / \pi$, continue the circulation with a common radius, ρ in QWT.
- ▶ Those positrons are captured by the accelerating field, which is placed in Bf area.
- ▶ Orbit of off momentum positron is not a circle. They will be lost by hitting the wall.
- ▶ Acceptance
 - Energy : $\frac{\delta E}{E} \sim \frac{B_f}{B_i}$
 - Transverse momentum: $p_t < \frac{eB_i a}{2}$, where a is iris radius.



Positron Generation
Positron Capture
Positron Source
ILC Positron Source
Summary

- ▶ AMD consists from the initial strong solenoid field along z direction, B_i , which is decreased down to B_f continuously.
- ▶ AMD has relatively large energy acceptance.
- ▶ Positrons, which start at $r=0$ with $pt(0)$, perform helical motion with radius increasing along z.





Positron Generation
Positron Capture
Positron Source
ILC Positron Source
Summary

- ▶ The positron motion is varied adiabatically with an invariant of

$$\int p dq = \frac{\pi p_t^2}{eB}$$

- ▶ Then $p_t(z)$ is expressed as

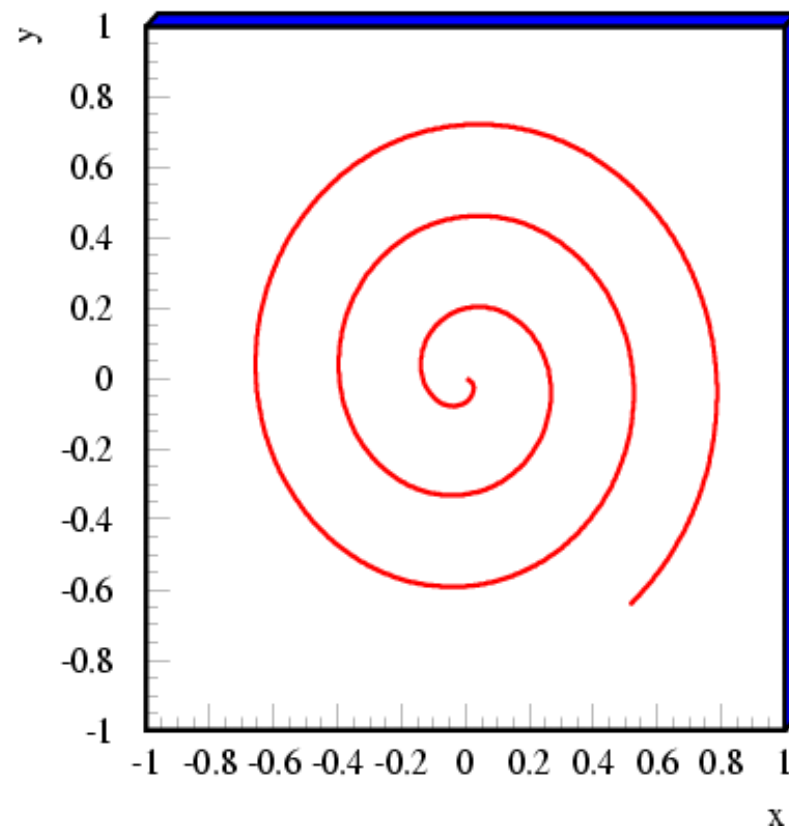
$$p_t(z) = \sqrt{\frac{B(z)}{B_i}} p_t(0)$$

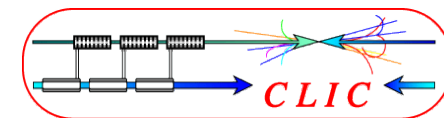
- ▶ The radius of the circular motion is

$$\rho(z) = \frac{p_t(z)}{eB(z)} = \frac{1}{e\sqrt{B(z)B_i}} p_t(0)$$

- ▶ The radius is increased up to

$$\rho_f = \frac{1}{e\sqrt{B_f B_i}} p_t(0)$$





Positron Generation
Positron Capture
Positron Source
ILC Positron Source
Summary

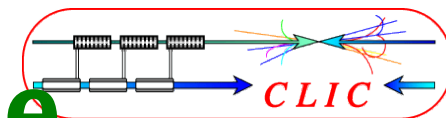
- ▶ $2\rho_f$ has to be within aperture, a . Then, the transverse momentum has to be

$$p_t < \frac{a}{2} e \sqrt{B_f B_i}$$

- ▶ If the longitudinal momentum is too large, the variation of the solenoid field, $B(z)$, becomes too fast to break the adiabatic condition.

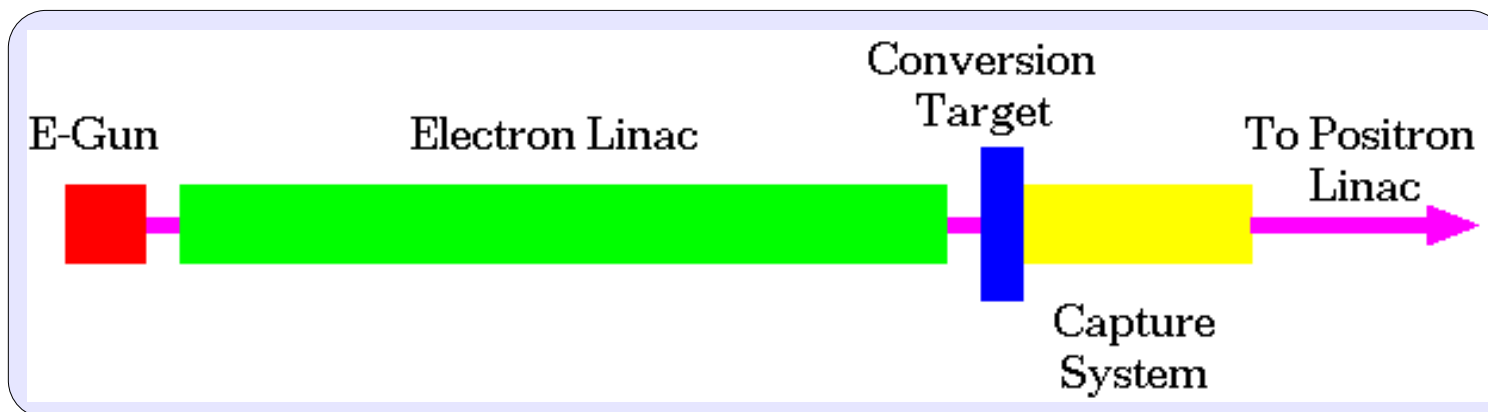
$$p_z < 0.5 \frac{eB_i}{\mu}$$

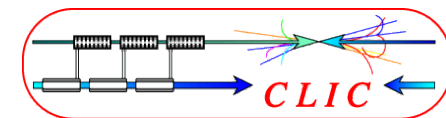
- ▶ These conditions give p_{tmax} and p_{zmax} .



Positron Generation
Positron Capture
Positron Source
ILC Positron Source
Summary

- ▶ Several GeVs driver electron beam.
- ▶ High Density Material for EM shower evolution.
- ▶ Positron capture by QWT or AMD + NC accelerator tube with solenoid focusing.
- ▶ 6 GeV drive electron with 4X₀ target yields one e⁺/e⁻.





Positron Generation
Positron Capture
Positron Source
ILC Positron Source
Summary

► An empirical expression for X_0 ;

- A, Z : mass number and atomic number

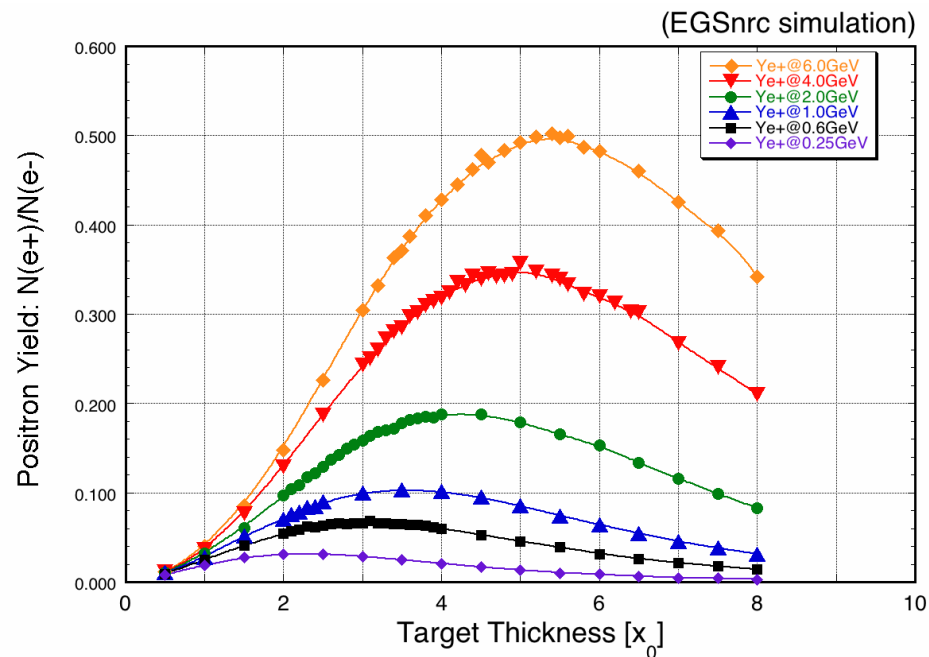
$$X_0 = \frac{716.4 [g.cm^{-2}] A}{Z(Z+1) \ln(287/\sqrt{Z})}$$

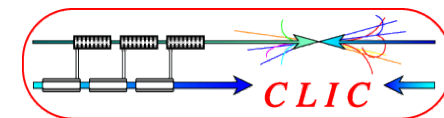
► Approximated expression for the shower max length in X_0 ;

$$T_{max} = 1.01 \left[\ln \left(\frac{E_0}{\epsilon_0} \right) - 1 \right]$$

- E_0 : Injected electron energy
- ϵ_0 : critical energy

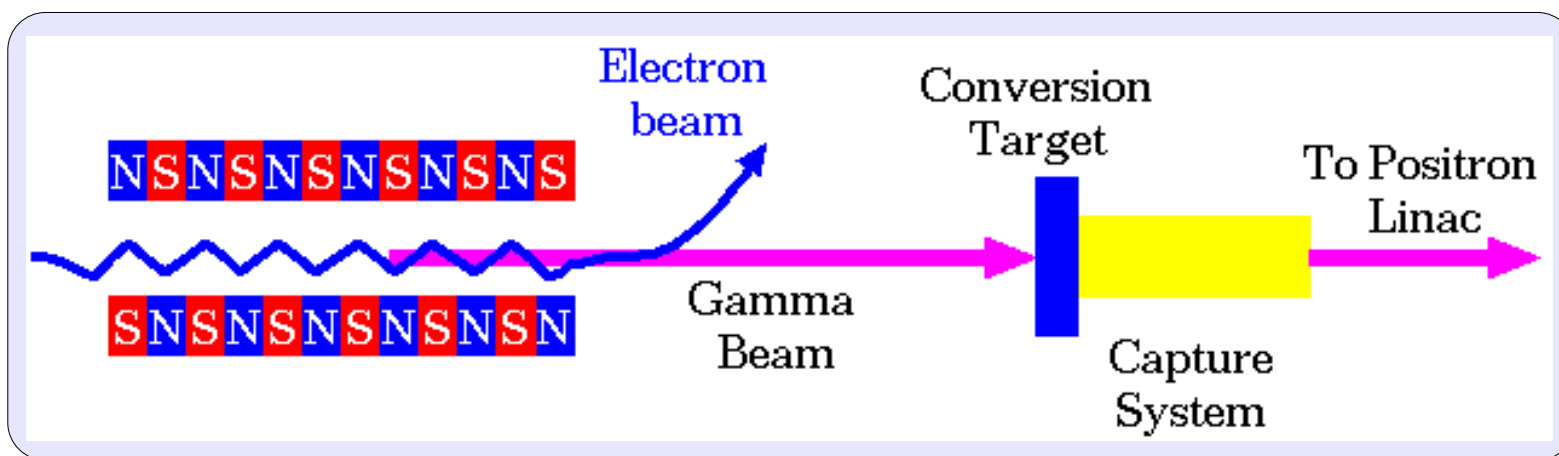
Courtesy of T.Kamitani

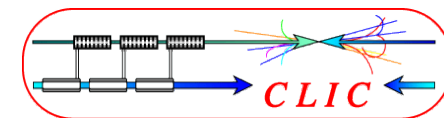




Positron Generation
Positron Capture
Positron Source
ILC Positron Source
Summary

- ▶ By passing more than 100 GeV energy electrons through a short period undulator, more than ~10MeV energy gamma rays are generated.
- ▶ This gamma ray is converted to positrons in a heavy material.
- ▶ Same capture system.



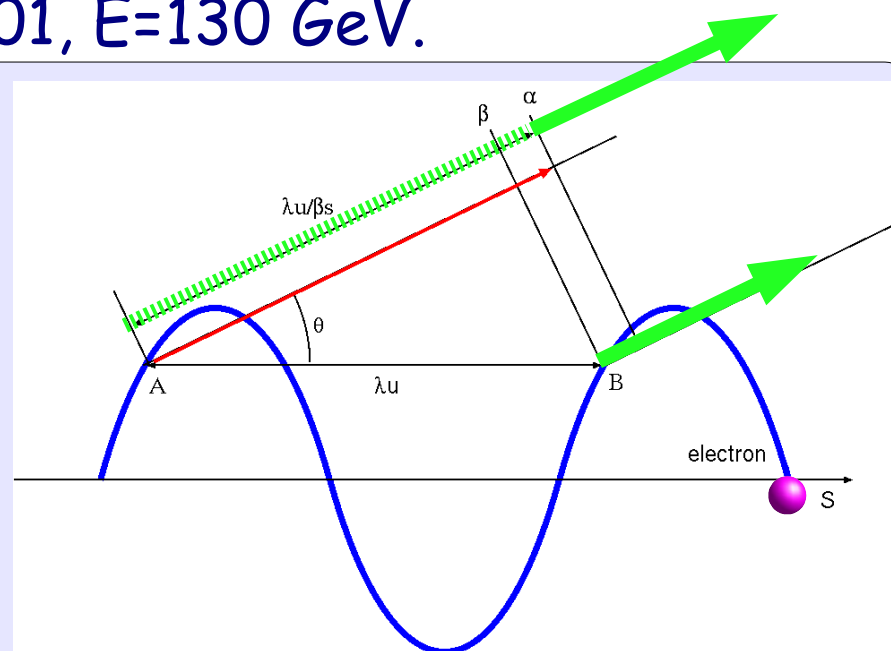


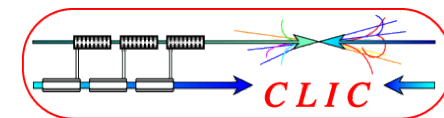
Positron Generation
Positron Capture
Positron Source
ILC Positron Source
Summary

- ▶ Electron speed in undulator along the longitudinal axis is less than speed of light due to zig-zag motion.
- ▶ Photons are emitted if the wave-plane path-length difference between undulator periods is quantized with the photon wave length.
- ▶ $E_{ph} = 10 \text{ MeV}$ photons (1st harmonic cut off) are obtained with $K=1.0$, $\lambda_u=0.01$, $E=130 \text{ GeV}$.

$$\lambda = \frac{\lambda_u}{2n\gamma^2} \left(1 + \frac{K^2}{2} \theta^2 \gamma^2 \right)$$

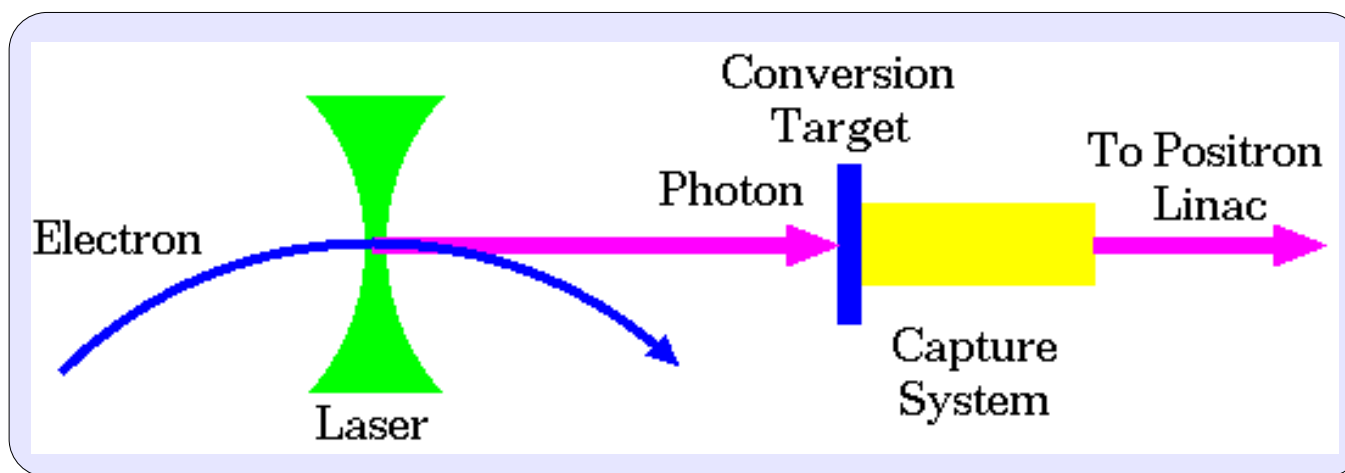
$$E_{ph} [eV] = 9.50 \frac{nE^2 [GeV]}{\lambda_u [m] \left(1 + \frac{K}{2} + \theta^2 \gamma^2 \right)}$$

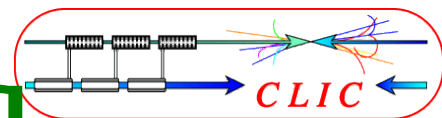




Positron Generation
Positron Capture
Positron Source
ILC Positron Source
Summary

- ▶ Compton back scattering between several GeVs electron and laser photons generates ~ 30 MeV gamma rays.
- ▶ These gamma rays are converted to positrons.
- ▶ If the laser is circularly polarized, positron can be polarized.



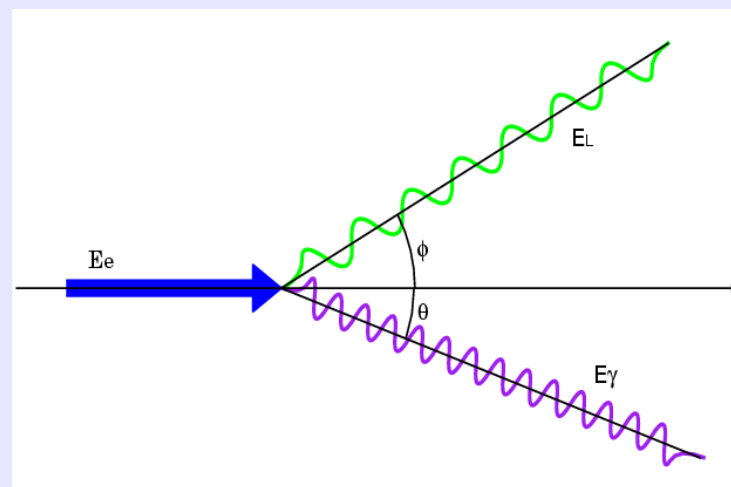


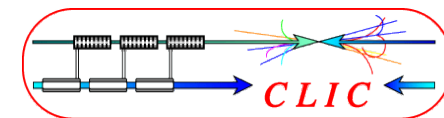
Positron Generation
Positron Capture
Positron Source
ILC Positron Source
Summary

- ▶ Inverse Compton scattering between laser photon and electron beam.
- ▶ Laser acts as a quite short period undulator; high energy gamma (several 10s MeV) is obtained with few GeV electron beam.

$$E_{\gamma} \sim \frac{4 \gamma^2 mc^2 E_L}{mc^2 + 4 \gamma E_L}$$

- ▶ E_L : Laser energy 1eV @ 1 μ m.
- ▶ Electron beam 1GeV, $\gamma=2000$.
- ▶ $E_{\gamma} \sim 16$ MeV

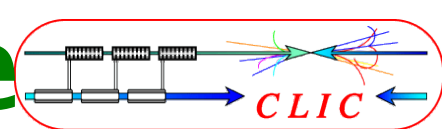




Positron Generation
Positron Capture
Positron Source
ILC Positron Source
Summary

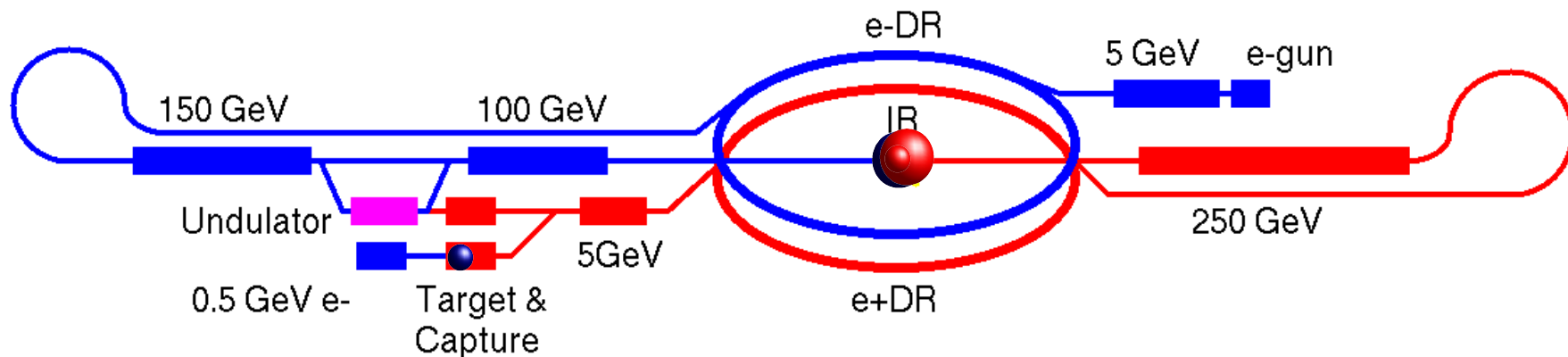
Parameter	Value	Unit
Bunch charge	3.2(1.6)	nC
Bunch length (rms)	4.3	ps
Norm. emittance ($\epsilon_x + \epsilon_y$)	0.09	m.rad
Bunch separation	369 (189)	ns
Bunch number in macro pulse	2625(5120)	number
Macro pulse length	0.9	ms

- ▶ Undulator scheme+ low intensity electron driven scheme (10%) is a baseline configuration.
- ▶ Compton scheme is an advanced alternative.
- ▶ Electron driven scheme is a back up option (when any unexpected serious difficulties were appeared for the baseline).

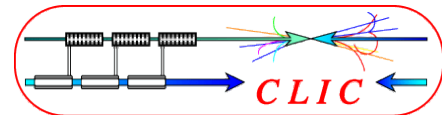


- A System-wide Sub-system -

Positron Generation
Positron Capture
Positron Source
ILC Positron Source
Summary



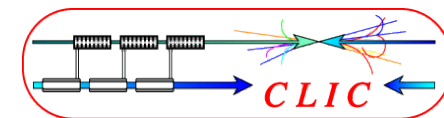
- ▶ Gamma rays for positron generation is produced by passing 150 GeV electron through undulator.
- ▶ Gamma rays are converted to positron.
- ▶ A positron source driven by 0.5 GeV electron is a back up for high availability.
- ▶ A common 5 GeV positron booster.



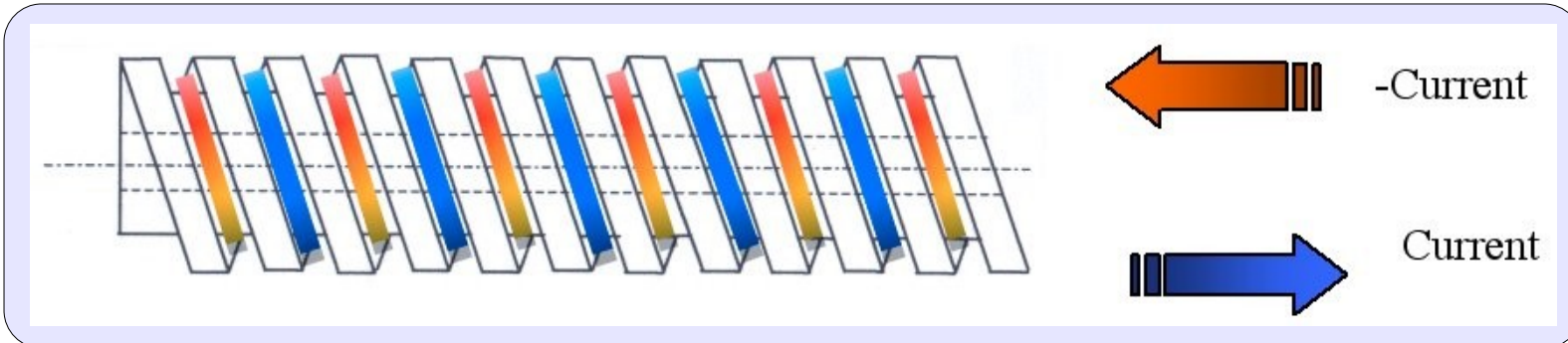
Positron Generation
Positron Capture
Positron Source
ILC Positron Source
Summary

Parameter	Value	Unit
Gamma/bunch	1.20E+13	Number
Positrons/bunch	2.0E+10(1.0E+10)	Number
Positron yield	1.5	e+/e-
Electron drive energy	150 GeV	GeV
Drive beam energy loss	4.8 (9.6)	GeV
Undulator length	147 (300)	m
Polarization (upgrade with 300m und.)	60	%

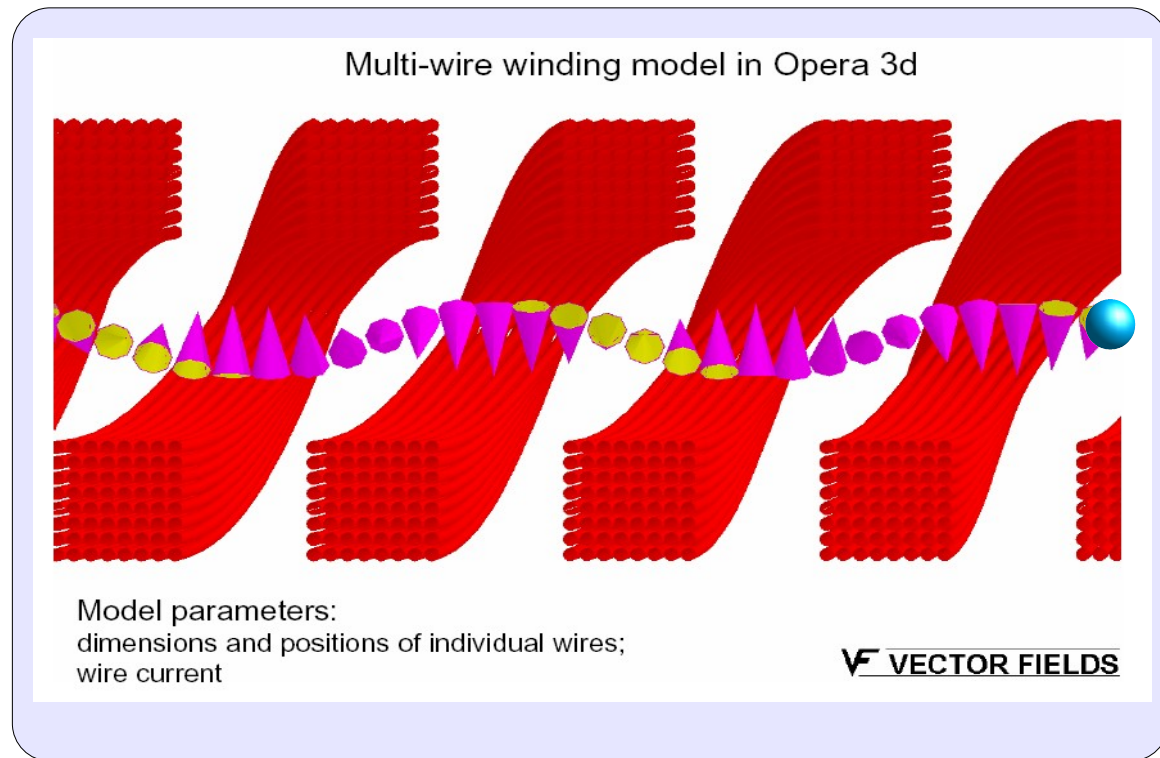
Helical Undulator



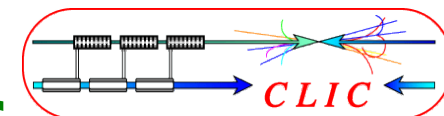
Positron Generation
Positron Capture
Positron Source
ILC Positron Source
Summary



- ▶ Two helical coils powered by opposite currents.
- ▶ Longitudinal field are cancelled and spiral transverse fields is appeared.

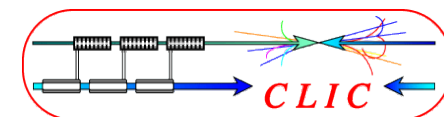


By Yury Ivanyushenkov



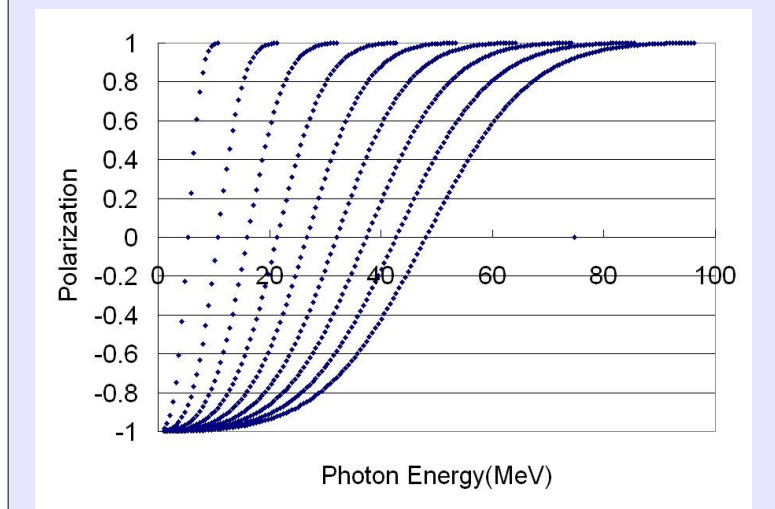
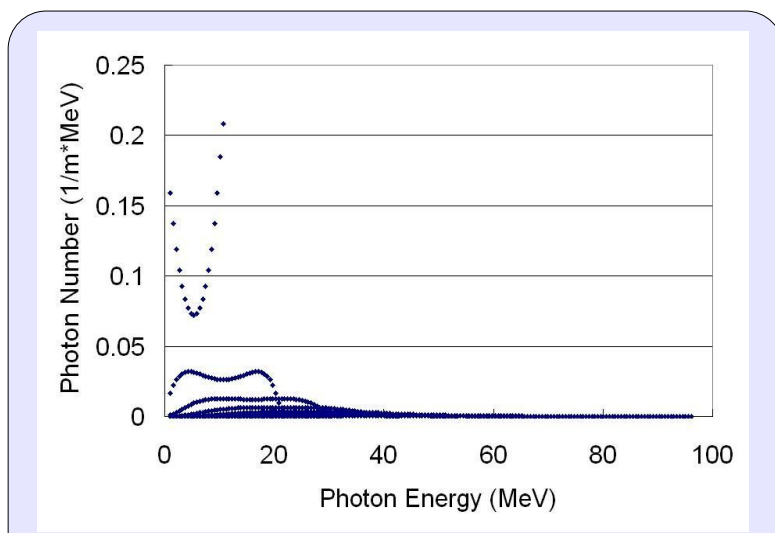
Positron Generation
Positron Capture
Positron Source
ILC Positron Source
Summary

Undulator Type	SC Helical	-
Undulator period	11.5	mm
Undulator Strength (K)	0.92	-
Magnet Current	205 (86% of critical)	A
Magnetic field (on axis)	0.86	T
Undulator Length (unpolarize)	147	m
Beam Aperture	5.85	mm
Photon Energy (1st hrm)	10.07	MeV
Max. photon power	131	kW



Positron Generation
Positron Capture
Positron Source
ILC Positron Source
Summary

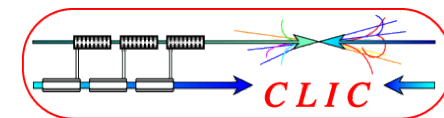
- ▶ Energy, angle, and helicity from undulator radiation are correlated.
- ▶ By taking gammas in super-forward direction, gamma rays and positrons are polarized.
- ▶ Number of particle is decreased by the collimation; need longer undulator.



$$\frac{dN_n}{dE} \left[\frac{1}{\text{MeV}} \right] = \frac{10^6 e^{2L}}{4\pi \epsilon c^2 h^2} \frac{K^2}{\gamma^2} \left[J_n'(x)^2 + \left(\frac{\alpha_n}{K} - \frac{n}{x} \right)^2 J_n(x)^2 \right]$$

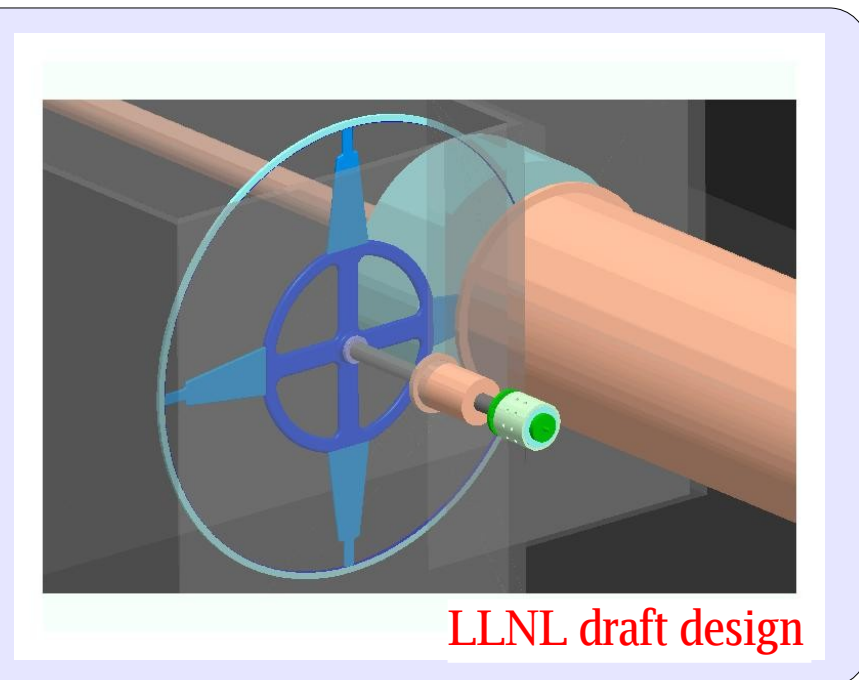
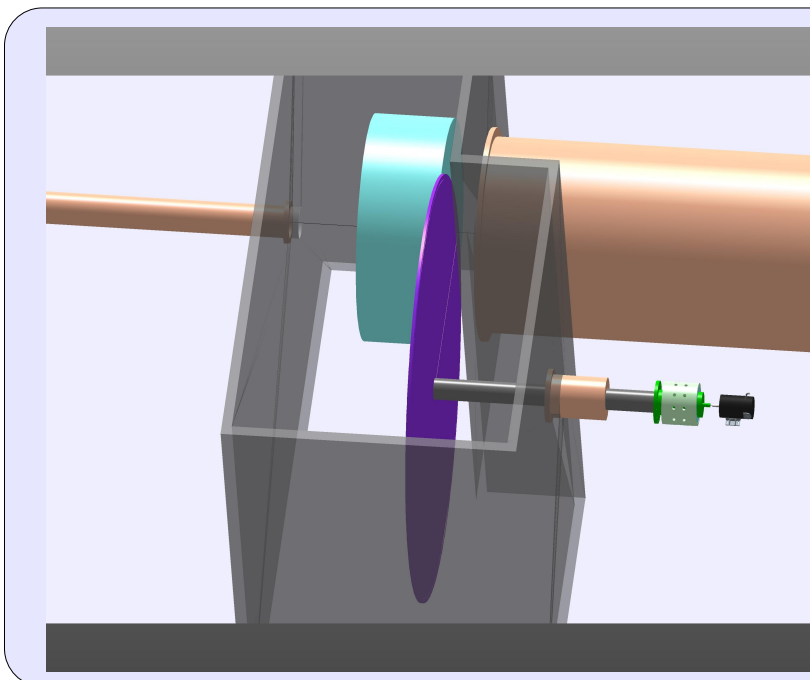
$$\theta = \frac{1}{\gamma} \sqrt{n \frac{\omega_n (1 + K^2)}{\omega} - 1 - K^2}$$

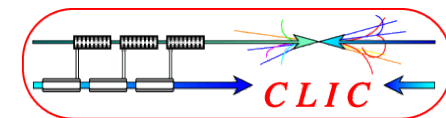
By W. Gai



Positron Generation
Positron Capture
Positron Source
ILC Positron Source
Summary

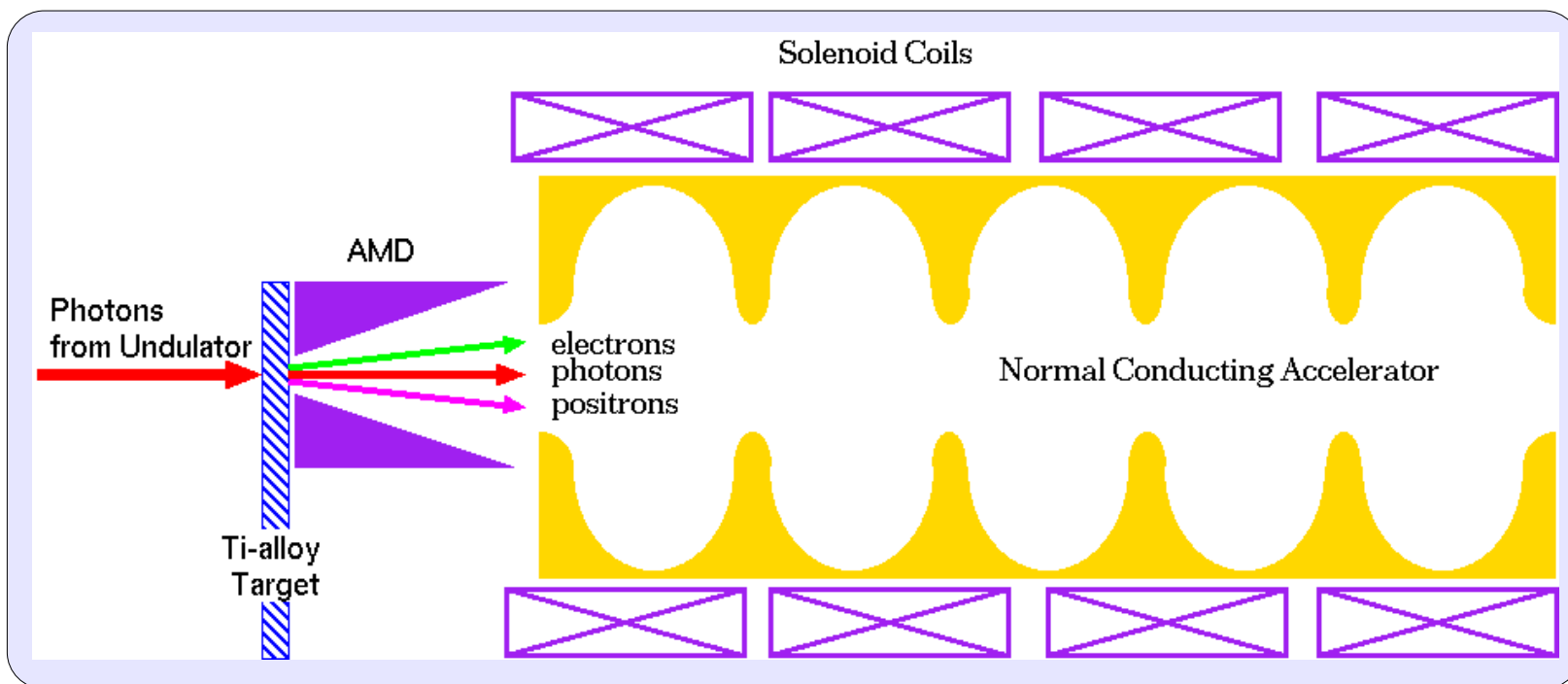
- ▶ Target : Ti-6% Al-4% V with $0.4 X_0$, rotating with tangential speed 100 m/s .
- ▶ Beam spot : 1.5 mm
- ▶ Heat load by gamma : 18 kW
- ▶ Heat load by Eddy current : 2MW (solid plate), 20kW (rim).





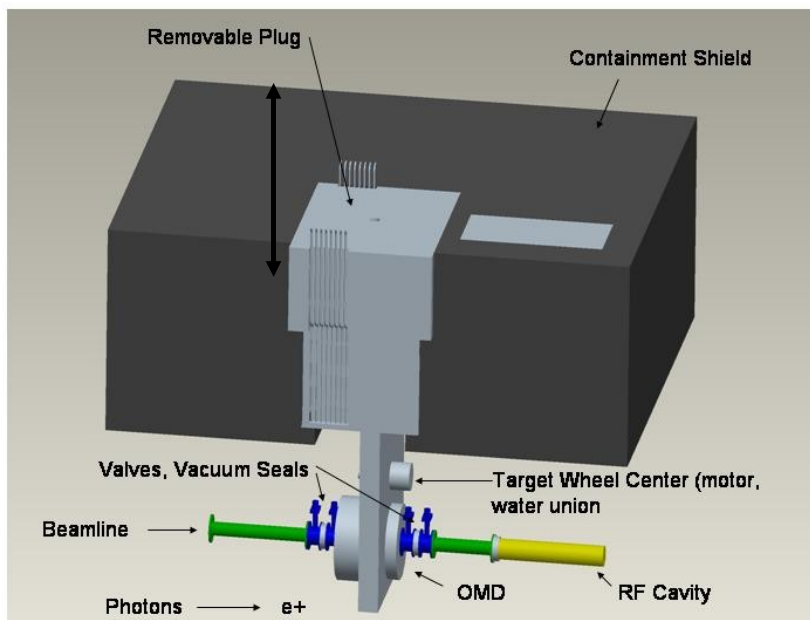
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- ▶ AMD ($B_i \sim 5T$, $B_f \sim 0.5T$ in 20cm): pulsed coil with bucking coil to shield any magnetic field in the target to avoid Eddy current problem.
- ▶ L-Band NC accelerator tube with 12 ~ 15 MV/m.



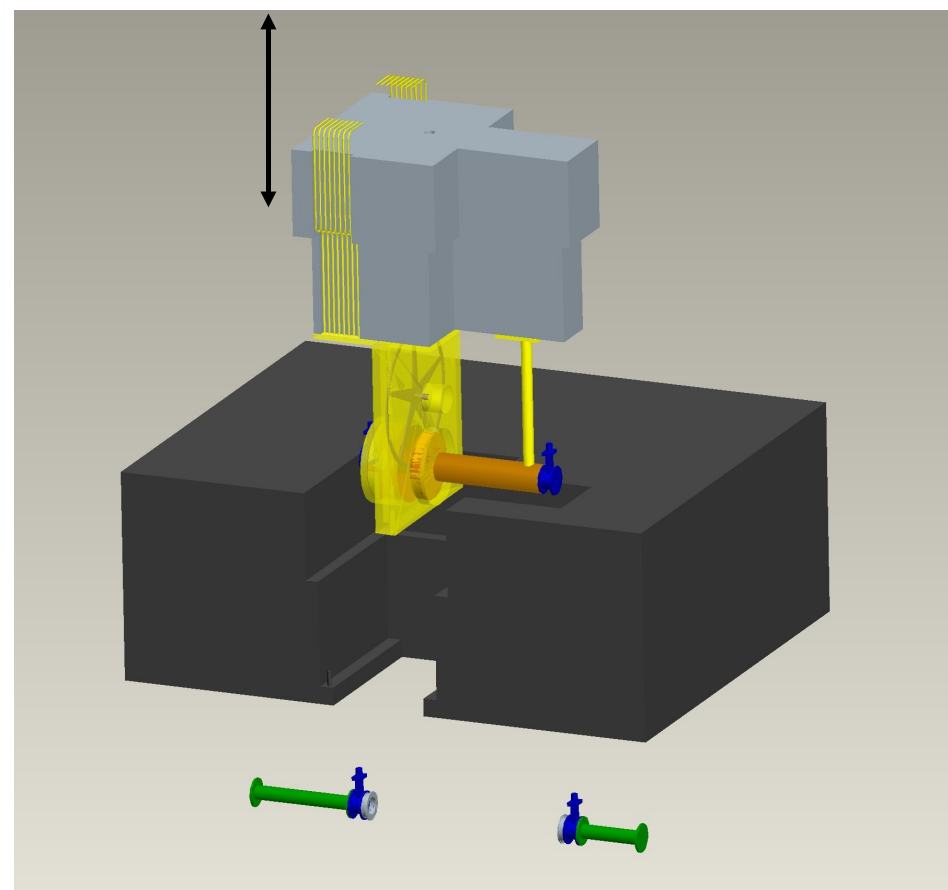
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Target Assembly In Place

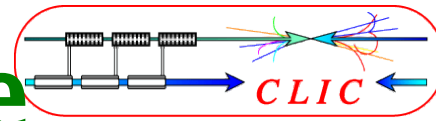


1.25 m

Target Assembly Lifting Out

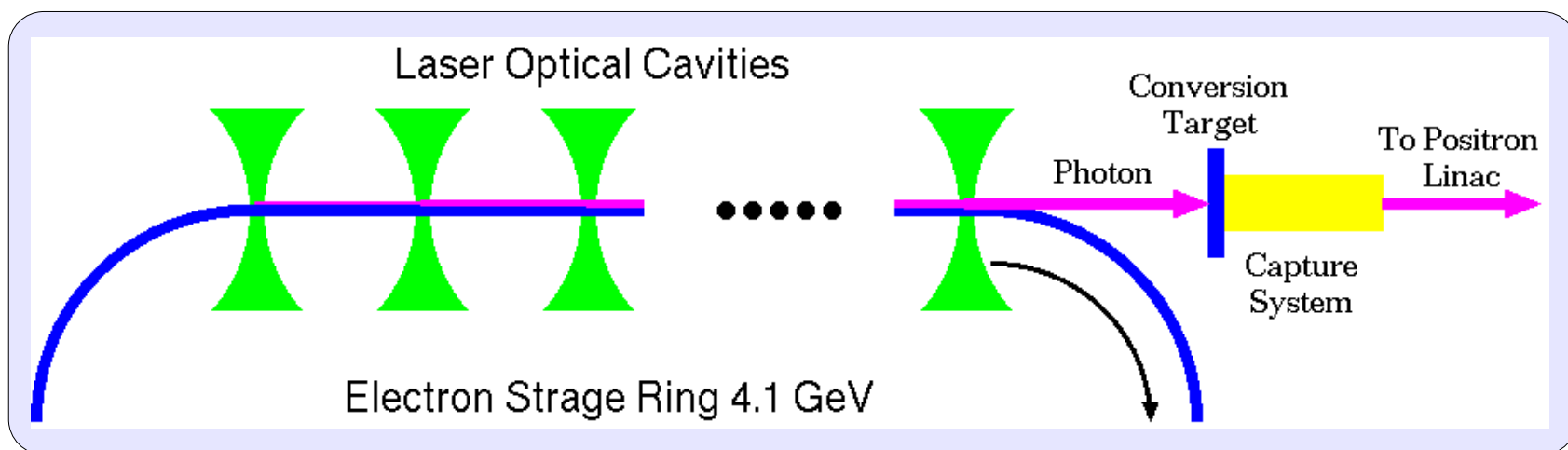


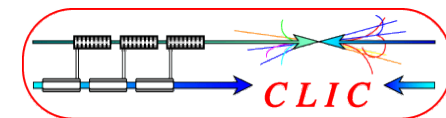
Laser Compton Scheme



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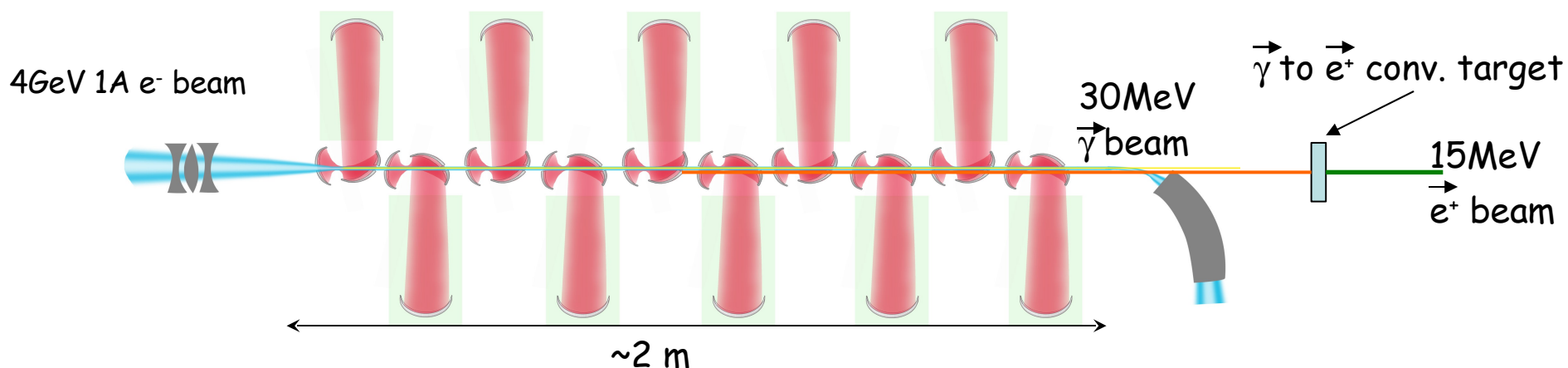
- ▶ Compton Ring : 1/10 of DR circumference storing 280 6.2(3.1)nC 1.3 GeV bunches with 6.16 (3.08) ns spacing.
- ▶ 10 optical cavities, which store 600mJ mode lock YAG laser (600μJ/pulse) by pulse-stacking technology.
- ▶ $1.7E+10 \gamma$ in 23-29 MeV energy range are generated every 6.2 ns; $2.4E+8$ positron per bunch are obtained.
- ▶ 28000 bunch train with 10ms interval are repeated 10 times; 100 bunches are filled to each bucket in DR.

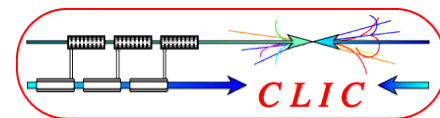




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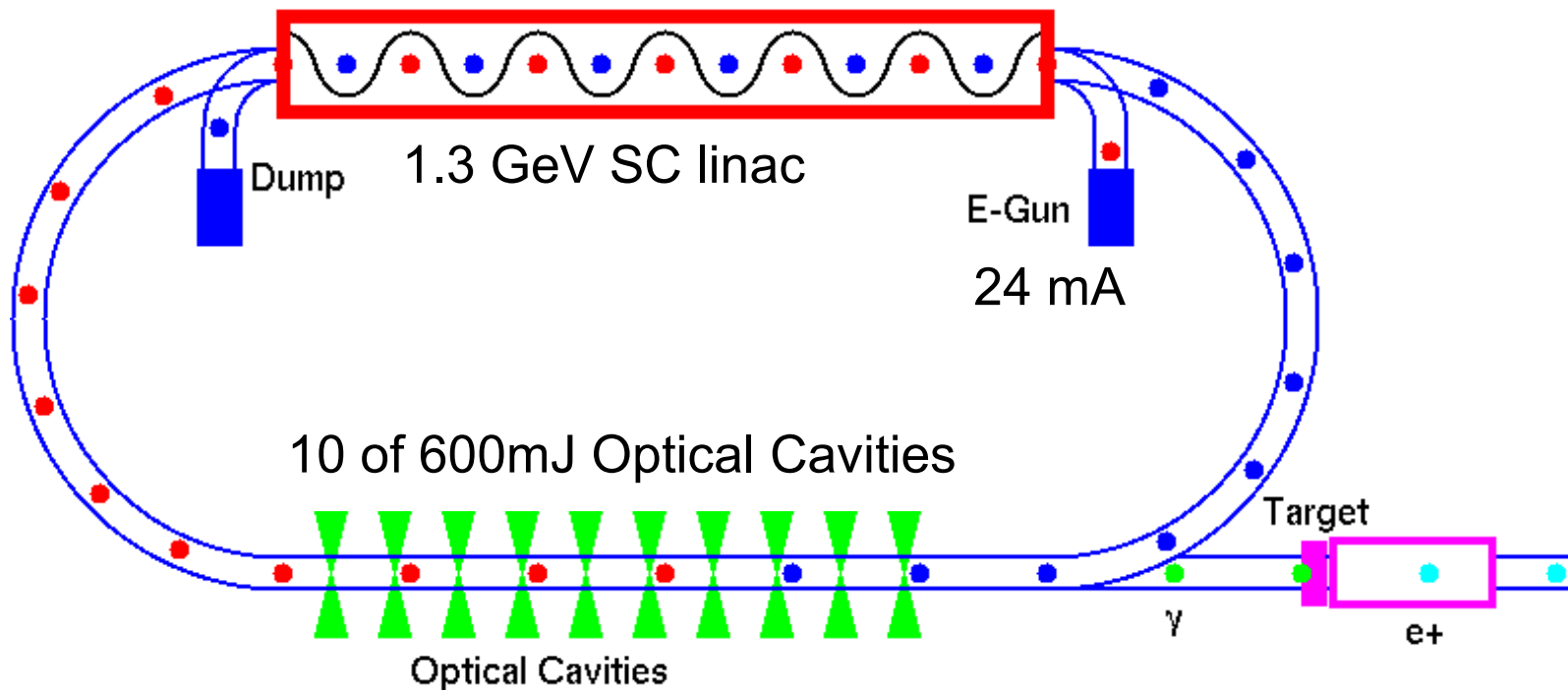
- ▶ Polarized gamma-ray beam is generated in the Compton back scattering inside optical cavity of CO_2 laser beam and 4 GeV e^- beam produced by linac.
- ▶ Laser system relies on the commercially available lasers but need R&D for high repetition operation.
- ▶ Ring cavity with laser amplifier realizes the CO_2 laser pulse train.

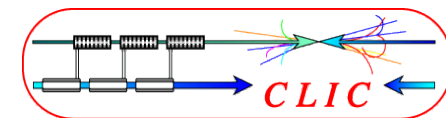




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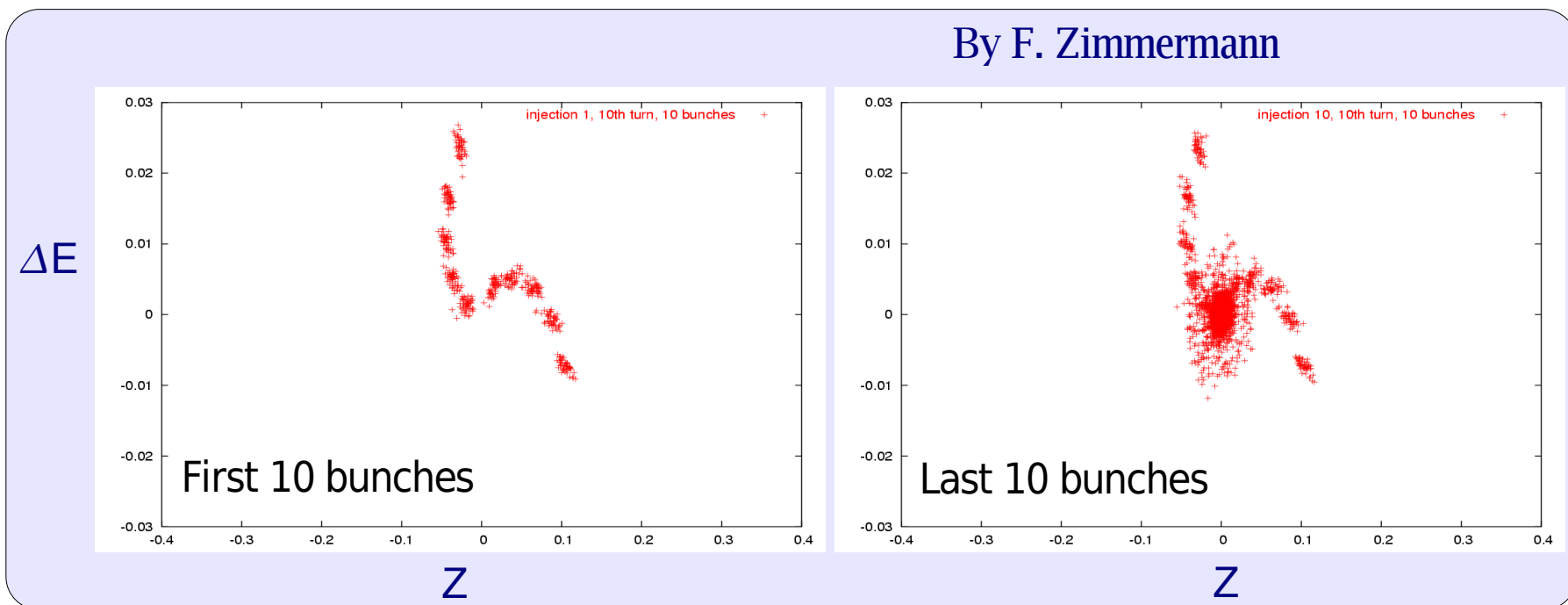
- ▶ Short bunch (<1ps) makes gamma yield higher.
- ▶ 1.5nC electrons with 62ns (24mA) → $8.2e+10 \gamma$.
- ▶ $7.5e+7 e+$ /bunch is obtained.
- ▶ Top-up injection up to 400 bunches in a same bucket make $3.0e+10 e+$ /bunch.
- ▶ Another 100ms is for damping.

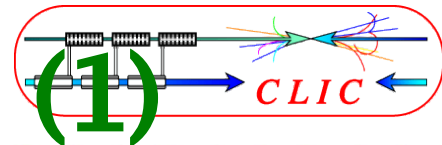




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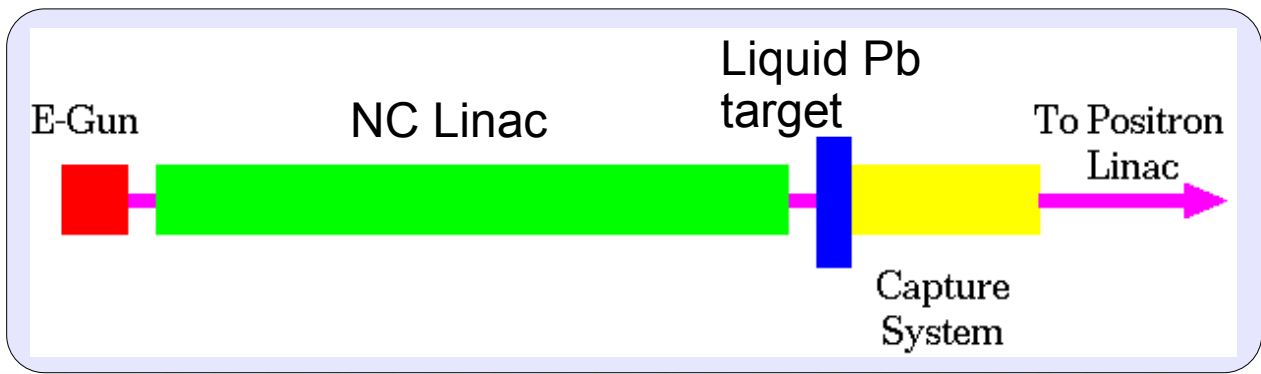
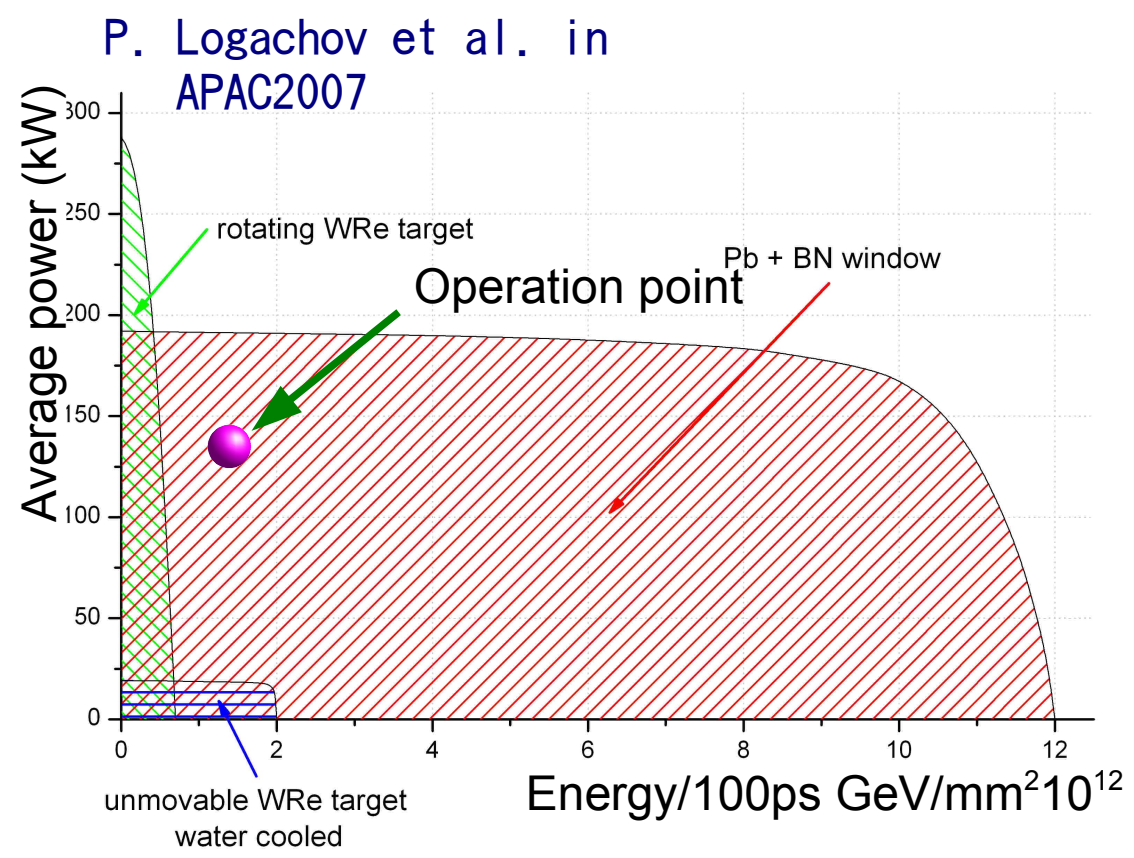
- ▶ Except the linac based Laser Compton scheme, number of positron generated by one collision is not sufficient.
- ▶ Many positron bunches are stacked in a same bucket in DR.
- ▶ Stacking scheme with less beam loss is under study.

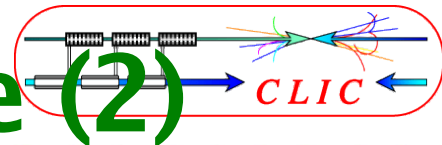




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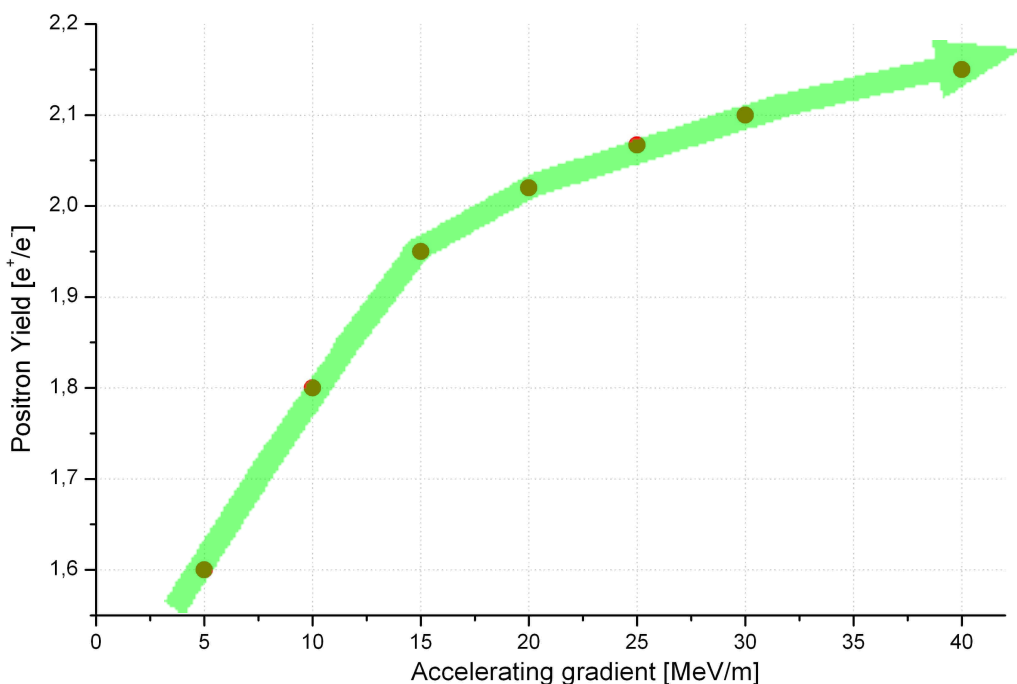
- ▶ Liquid Pb target + BN window is very strong against high peak power.
- ▶ Short bunch spacing mode (2625 6.2GeV 10^{10} bunches 6.2ns spacing) in 1mm^2 spot makes $1.0 \text{ GeV}/\text{mm}^2 10^{12}$.
- ▶ The load to the target is tolerable.

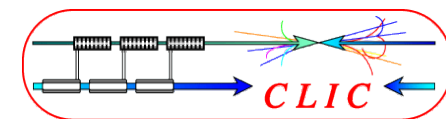




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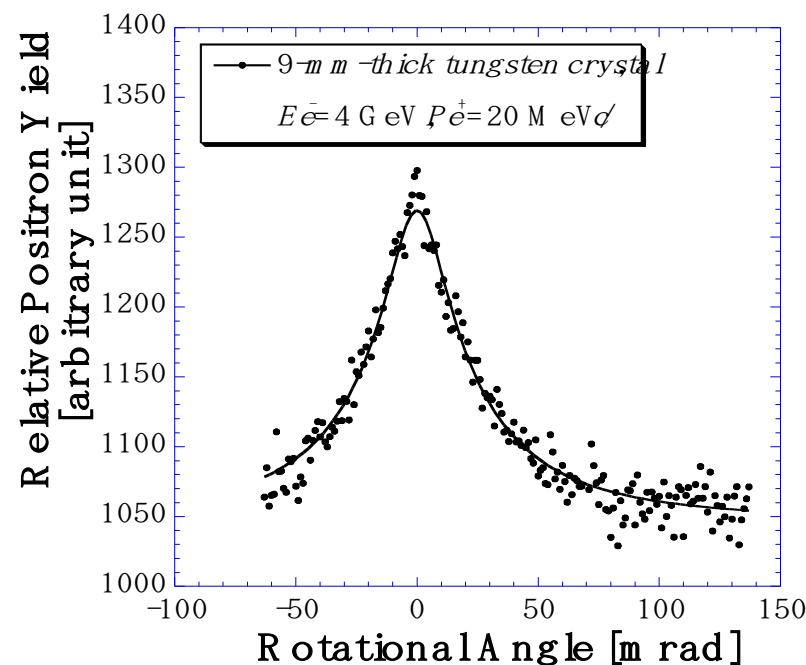
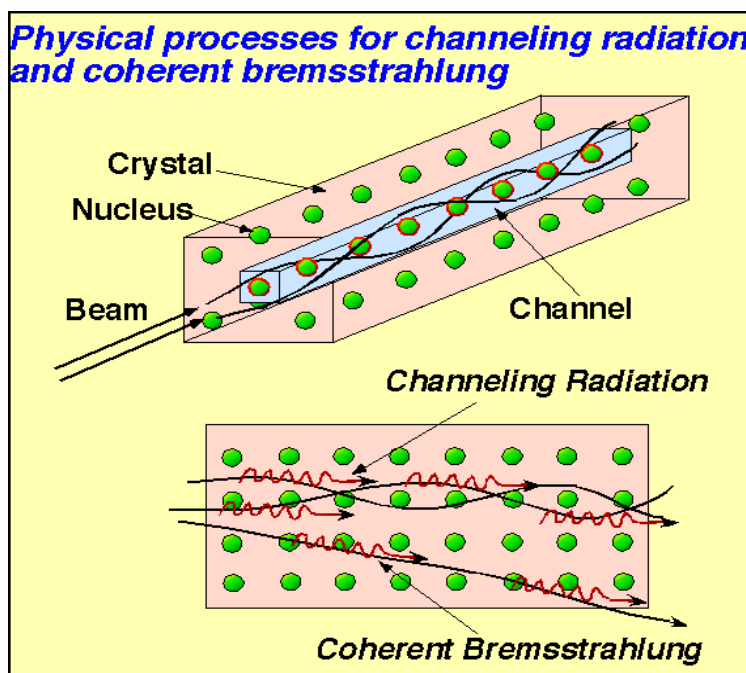
- ▶ Short pulse operation ($16\mu s$) allows higher gradient, eg. 25 MeV/m with positron yield $2.1 e^+/e^-$.
- ▶ Positron per bunch is 2.1×10^{10} .
- ▶ 10T Flux concentrator increases the capture and relaxes the condition.
- ▶ NC accelerator for e-driver and e+ booster.

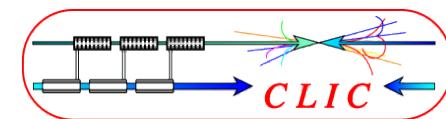




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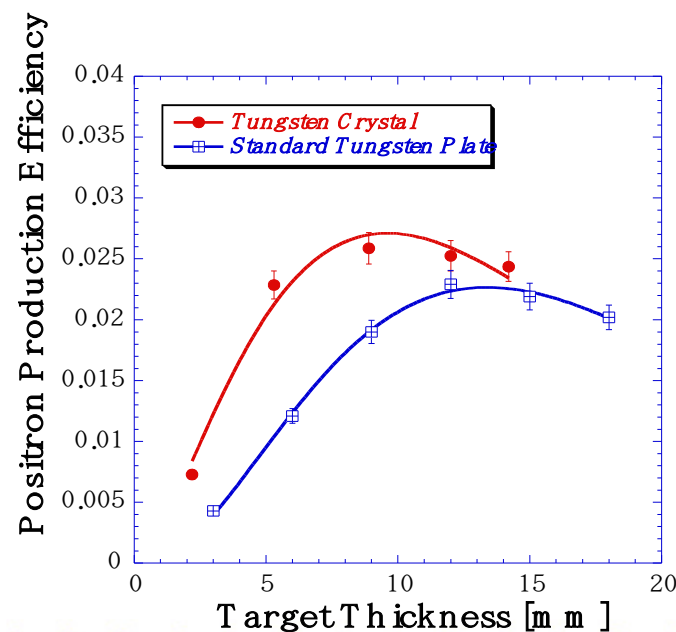
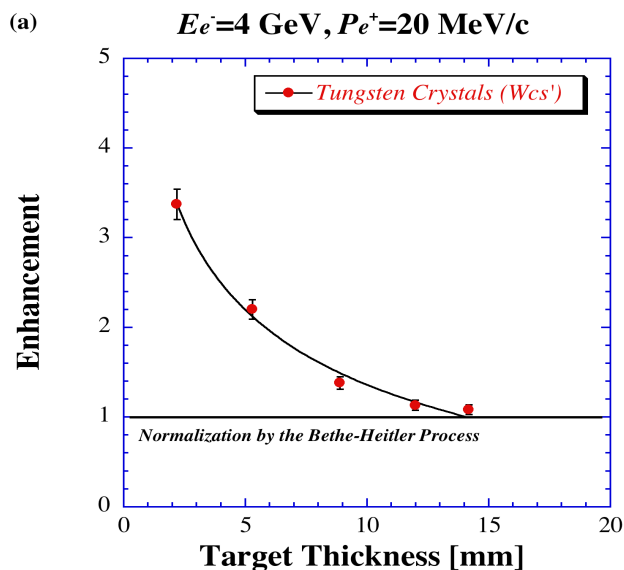
- ▶ Gamma radiation by e- beam in a crystalline W target along the crystal axis is enhanced by channeling and coherent bremsstrahlung.
- ▶ A clear enhancement on the positron generation with the crystalline W target is experimentally confirmed at KEKB injector.

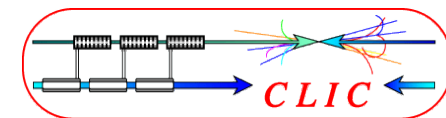




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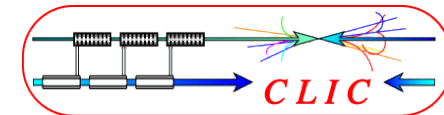
- ▶ Positron yield by the crystalline target is enhanced by ~30% with thinner (~9mm) target thickness.
- ▶ The heat load becomes almost half compare to the amorphous target.
- ▶ The heat load normalized to the generated positron flux is 40% of that by amorphous target. It relaxes the technical limitation very much.





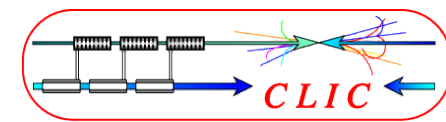
Positron Generation
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Summary

- ▶ Fundamentals of positron generation and its capture system are explained .
- ▶ ILC Positron Source is based on Undulator Scheme with auxiliary source based on electron driven scheme.
- ▶ Laser Compton scheme is advanced alternative.
- ▶ Electron driven is still a vital option.
- ▶ Need a lot of interesting works to implement the positron source.



Positron Generation
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- ▶ "Positron Sources" by R. Chehab, in proceedings of CERN Accelerator School, CERN 94-01, 1994
- ▶ "Positron Source" by T. Kamitani, Text book for high energy accelerator seminar OHO2002, 2002 (in Japanese)
- ▶ "Handbook of Accelerator Physics and Engineering" edited by A. Chao and M. Tigner, World Scientific, 1998
- ▶ "Conversion system for obtaining highly polarized electrons and positrons", by V.E. Balakin and A.A. Mikhailichenko, INP 79-85.
- ▶ "Conceptual Design of a Polarised Positron Source Based on Laser Compton Scattering", by S. Araki et al, KEK Preprint 2005-60, 2005.
- ▶ WEB site of PosiPol WS 2007 (LAL, May, 2007)
<http://events.lal.in2p3.fr/conferences/Posipol07/>



2-1) How much beam energy, E , is necessary to obtain 10 MeV photons from undulator? Undulator strength parameter, K , is given as

$$K = 93.4 B_0 [T] \lambda_p [m]$$

- λ_p : undulator period length; $\lambda_p = 0.01\text{m}$
- n : harmonic number = 1
- B_0 : Peak magnetic field, 1T

2-2) How much beam energy, E , is necessary to obtain 10 MeV photons from Laser Compton? Assume $1\mu\text{m}$ wave length for laser.

- Planck constant : $6.63\text{E-}34$ Js
- Speed of light : $3.00\text{E}+8$ m/s