Orthogonal Bumps in ILC Main Linac

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Previous works

Proposed by P. Eliasson and D.Schulte at "CLIC Tuning Bump Strategies", Daresbury LET face-toface meeting, Jan. 2007

Daniel Schulte and Andrea Latina are working on similar BUMPS for ILC linac (this meeting)

Our first look for ILC Main Linac

Bumps

For a given seed the final beam after BBA can be represented by a vector

$$s_i = (y_i^1, \dots, y_i^n, \beta y_i'^1, \dots, \beta y_i''), \quad i = 1 \dots nseed$$

where n - number of particles (11x11x9 in our case)

- The effect of knobs (correctors) can be represented by matrix (*mx2n*) $K = \begin{pmatrix} k_1 \\ \vdots \\ k_m \end{pmatrix} \text{ where: } k_j = (\Delta y^1, \dots, \Delta y^n, \beta \Delta y'^1, \dots, \beta \Delta y'^n)_j, \quad j = 1...ncorr$
- s_i contains the particle positions and angles at the end of the linac
- k_j contains *changes* in particle positions and angles for a unit change of knob j
- Matrix K is defined by lattice (independent of misalignment)

SVD

To minimize final emittance for each seed s one should find a vector x of amplitudes of correctors, which minimize:

$$s - x \cdot K \Longrightarrow \min$$

Singular value decomposition (SVD) on K represents it as a product of orthogonal matrices U and V and diagonal matrix K_{svd}:

$$K = U \cdot K_{svd} \cdot V^{T} = \begin{pmatrix} U_{1} & \cdots & U_{n} \end{pmatrix} \begin{pmatrix} \alpha_{1} & & \\ & \ddots & \\ & & \alpha_{n} \end{pmatrix} \begin{pmatrix} V_{1} \\ \vdots \\ V_{n} \end{pmatrix}$$

Then

$$s - \sum_{j=1}^{n} x_j \cdot \alpha_j \cdot (U_j \cdot V_j) \Longrightarrow \min$$

Column U_i is the weights of all correctors in j - th orthogonal bump.

- V_i corresponding changes of particle coordinates and angle
- x_i amplitude of j th orthogonal bump

Example: Straight ML Lattice

- Regular straight FODO lattice, 114 cells
- X/Y phase advance per cell = 75/60
- 8 cavities per cryomodule (CM)
- 4 CM per quadrupole (TESLA-like)
- Quadrupole package = BPM, quadrupole, Xcorr, Ycorr.





Singular value of matrix K



Weights of real correctors in orthogonal bumps.

















With wakefields turned off



With wakefields turned off (2)



No Wakes, No coupling (Quad roll)















Summary and Plans

- Orthogonal bumps was implemented in Lucretia
- It works good in straight linac. Coupling and wakes cann't be corrected.
- Future work: Perform the same study for irregular curved ILC ML lattice as for straight linac
 - The same study in presence of ground motion