The University of Manchester

MANCHESTER

Wake-fields and Beam Electrodynamics

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- Wake-fields and HOM beam dynamics for the ILC:
- 1. Main linac e.m. field and beam electrodynamics simulations for ACD high gradient cavities
- 2. Globalised matrix technique of cascading
 - > 3. Review of x-y transverse coupling
- 4. Crab cavity wire simulations and measurements
- > 5. HOM measurements at FLASH (FP7)











Personel

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Collaborators: <u>Nicoleta Baboi (DESY), Steve Molloy</u> (SLAC), Toshiyasu Higo, Kenji Saito, (KEK), Hasan Padamsee (Cornell Univ.), Amos Dexter, Richard Carter (Univ. Lancaster), Roger Barlow (Univ. Manchester)

A Few Points Lifted From BCD Document

- "Modifications/ variants of re-entrant:
- smaller aperture re-entrant
- half-re-entrant.
- Required R&D
- Considerable R&D will be required and different check points:
- Wake fields:
- The allowed iris diameter must be specified from theoretical analysis. This is a trade off between allowable emittance growth (luminosity) and cost.
- Complete wake field analysis must be carried out computationally and checked with measurements.
- Cold tests of wake fields must be carried out on two or more adjacent cavities.
- Wake fields must be checked in modules with beam [trapped modes and influence of fabrication errors must be checked].
- Gradient and Q:
- o Gradient and Q expectations up to at least 35MV/m must be achieved first in 9-cell cavity tests then in modules with beam.
- Instrumenting the HOM readouts to provide a measure of the average beam position in the cryomodules. To better center the beam, the cryomodules would either be moved manually during down periods or equipped with remote-controllable movers to allow corrections during machine operation...."



Simulations of Trapped Modes in RE Cavities



 Solid line correspond to single-cell infinite periodic structure
 Circles correspond to simulations made with 9 cell cavity (4.5 cells with E-wall and H-wall simulated separately)



Multi-Cell Kick Factors



Wake-field Along Bunch Train

For details see Jones et al, Linac 2006

Brillouin Diagram For RE Cavity



A small change in the bunch spacing (corresponding to a systematic error in the cels freqs) results in disturbingly large emittance dilution.

Emittance Dilution Vs Percentage Change In Bunch Spacing 300.



Eigenfrequency error sample at Q~10⁶



Eigenfrequency error sample at Q~10⁵







Amplitude of wake at bunch and corresponding sum wakefield for a Q of 10⁶



Amplitude of wake at bunch and corresponding sum wakefield for a Q of 10⁶

1. Beam Dynamics in Re-Entrant Cavity



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Y-Y' phase space at end of linac



Emittance dilution due to long-range wake-fields damped with a Q of 10^6 in Re-entrant cavity. The beam is offset with $1\sigma_y$ (~12.4 µm). The mean dilution is 17.25 % (with a standard error of .25 %). 200 machines are indicated together with the mean and the 95% confidence level.

1. Beam Dynamics in Re-Entrant Cavity



Emittance dilution due to long-range wake-fields damped with a Q of 10⁵



Emittance dilution due to long-range wake-fields damped with a Q of 10⁶

Emittance dilution due to longrange wake-fields damped with a Q of 10⁶ and a targeted damping of 10⁵ for Re-entrant cavity



1. HOMs in Ichiro Cavity



Simulations of E-field of the 3rd band modes in Ichiro cavities

(V/pC)

sefactor

0.2



Dispersion curves of first 8 dipole and 5 sextupole bands <u>See Glasman, Jones et al.</u>

SRF2007 pubs.

Comparison of Loss factors calculated with GdfidL (red) and MAFIA 2D (blue) Detailed studies conducted on HOMS in Ichiro cavity. Sensitivity to systematic changes in frequency investigated. Detailed comparison of codes –MAFIA,HFSS, GdfidL, Analyst.

Ichiro Cavity fabricated at KEK





Envelope of long-range wake-field



Sensitivity of RMS wake to small changes in bunch spacing

1. HOMs in Ichiro Cavity



Eigenfrequency error sample at Q~10⁶



Modal Kick Factor vs frequency



Eigenfrequency error sample at Q~10⁵

1. HOMs in Ichiro Cavity



Amplitude of wake at bunch and corresponding sum wakefield for a Q of 10⁶



Amplitude of wake at bunch and corresponding sum wakefield for a Q of 10⁵

1. Beam Dynamics in Ichiro Cavity





Emittance dilution due to long-range wake-fields damped with a Q of 10^6 in Ichiro cavity. The beam is offset with $1\sigma_y$ (~12.4 µm). The mean dilution is 17.25 % (with a standard error of .25 %). 200 machines are indicated together with the mean and the 95% confidence level.

1. Beam Dynamics in Ichiro Cavity





Phase Space: y-y'

•500 particles in all simulations
•Initial vertical and horizontal offset 12 μm (~ σ_y) and 0 (~ σ_x), respectively.
•Long range wakes included in simulations

Limited Q damping

-1

-2

-2

$\begin{array}{c} 20 \\ \hline 20 \\ \hline -20 \\ \hline -20 \\ \hline -40 \\ \hline 0 \\ 100 \\ \hline 200 \\ \hline 300 \\ \hline 400 \\ \hline 500 \\ \hline Bunch \# \end{array}$

Transverse Displacement

Phase Space: y-y'

0

Y

1

2

•500 particles in all simulations
•Initial vertical and horizontal offset 12 μm (~ σ_y) and 0 (~ σ_x), respectively.
•Long range wakes included in simulations

-1

1. Beam Dynamics in Ichiro Cavity





Emittance dilution due to long-range wake-fields damped with a Q of 10^6 in Ichiro cavity. The beam is offset with $1\sigma_y$ (~12.4 µm). The mean dilution is ~3% (with a standard error of .25 %). 50 machines are indicated together with the mean and the 95% confidence level.

1. Beam Dynamics in Ichiro Cavity



Mean emittance dilution due to long-range wake-fields damped with a Q of 10⁵ in Ichiro cavity. 200 machines considered.

> Emittance dilution due to longrange wake-fields damped with a Q of 10⁶ and a targeted damping of 10⁵ for Ichiro cavity



Emittance dilution due to longrange wake-fields damped with a Q of 10⁶ in Ichiro cavity



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2. EM Field in High Gradient Cavities

- Simulation of Higher Order Modes (HOMs) in high gradient cavities
- Utilise 3D codes: GdfidL, HFSS, Analyst
- Use 2D codes, ABCI, Echo2D for bulk of cavity structures.
- Develop interface that cascades given sections to make more efficient calculations of overall fields.
- **Focus on:**
- 1. Re-entrant -Cornell Univ. design
- 2. Low-loss (Ichiro variant) –KEK design.

2. Cascaded Computation of HOMs



2. Cascaded Computation of HOMs -Fabrication Sensitivity Studies





^{frequency: Ghz} S₂₁ due to random distribution of dents in TESLA cavity compared with ideal structure. Dent ranges from 1 to 3 mm. <u>See Shinton and Jones,</u>

SRF2007 pubs.



S₂₁ for an unperturbed structure and a perturbed structure with a 1mm slice. TE₁₁ mode scattered into the third mode (sextupole)

 $V_y = iV_x(0) \sin 2\theta \exp(i < \omega > t) \sin(\Delta \omega t/2)$

Thus for $\theta = 0$ or $\pi/2 V_v(0) = 0$ as expected!

The additional kick to the beam is of the form:

 $V(t) = \Sigma K_n \sin(\omega_p t) \exp(-\omega_{pt}/2Q_p) U(t) y + \Sigma K_n \cos(\langle \omega_p \rangle t) \sin(\Delta \omega_p t/2) \exp(-\langle \omega_{p} \rangle t/2Q_p) U(t) x$

Where the sum is taken over all modes of interest and U(t) is the unit step function

=> Recent TTF experiments (Ross, Napoly & Baboi) suggest that this frequency splitting varies by ~ 400 kHz to 800 kHz. In all simulations presented here we use 600 kHz frequency splitting for all modes.



TESLA 9-Cell Cavity

Make several injection offset simulations to investigate this issue. 1. Force the angle of all couplers relative to the dipole field to be static. 2. Allow complete azimuthal randomization of couplers (0 to 2π).

3. Limit the azimuthal spread of the couplers.

For detailed simulations consider a single machine for the above cases.
 For general emittance dilution consider 200 separate machines.

TYPICAL SIMULTATION PARAMETERS

•Injected emittance: $\varepsilon_{x,y} = 8e-6$, 2e-8 m.rads •Injection beam energy 5 GeV => O/P 500 GeV c.m. energy • $\gamma_{i,f} \sim 9782$, and 489,000 •All simulations made with LIAR. •500 bunches in all simulations. •Initial vertical and horizontal offset ~10 µm and 400µm. •c.f. initial beam $\sigma_{y,x}$ (= [$\beta \varepsilon_n / \gamma$]^{1/2}) ~ 10.1 µm, 270 µm. • $\sigma_{x',y'}$ (= [(1+ α^2)/ $\beta \varepsilon_n / \gamma$]^{1/2}) ~ 5.1, 0.26 µrads •Initial $\beta_{x,y} \sim 89.3$, 50.7 m

Does the Cross-Coupling of X-Y Motion Significantly Dilute the Beam Emittance?



Increase the damping of the HOM modes? At present the damping is $\sim 10^4 - 10^5$. It may be difficult to reduce the damping even further?

 The dipole frequency degeneracy's are already split -by ~ 400 kHz to 800 kHz. Increasing the splitting (which can be achieved by making markedly asymmetrical cavities) to say 10 MHz may allow the influence of mode coupling to be minimal over the length of the linac.

•Splitting the tune of the linac. Present design is 60/60 - horizontal/vertical. This may be the most straightforward to implement.

Re-entrant cavity shape is shown. Taken from Rong-

Li Geng SRF 2005

Amelioration of Large Emittance Dilution?





•Present lattice has phase advance per cell of 60 degrees per cell.

Each lattice cell consists of two groups of: quadupoles + 2 cryo-modules + quadrupole+ 2 cryo-modules.
There are 12 cavities per cryo-module.
If we split the tune then the coupling should be out of resonance.

•We look at 61/60 through 90/60.

•Single FODO array shown.

•We split the tune by raising the F functions for the focusing quadrupole with respect to the D quadrupole.



•The D quadrupole is then readjusted in order to achieve 60 in the vertical plane.

Split Tune of Lattice





•500 particles in all simulations
•Initial vertical and horizontal offset 0 μm and 270μm (~ σ_x), respectively.
•(c.f. initial beam σ_{y,x} ~ 10.1 μm, 270 μm)
•Fixed azimuthal orientation of couplers.
•Long range wakes included in simulations
Cross-Coupled Motion At Fixed Azimuthal
Phase Distribution (Yoff=0). Split Tune



These have been rescaled relative to the previous ones •Final mean dilution ~ 35% (95% CI 33, 37%)



•500 particles in all simulations and 200 machines are illustrated The dashed line marks the injection offset of all bunches Initial vertical and horizontal offset 0 μm and 270 μ m (~ σ_x), respectively. •(c.f. initial beam $\sigma_{y,x} \sim 10.1 \ \mu m$, 270 μm) •Fixed azimuthal phase. Long range wakes included in simulations **Cross-Coupled Motion At Fixed Azimuthal** Phase Distribution (Yoff=0). Split Tune 70/60

Mode Coupling Summary

>Mode-coupling is a significant source of emittance dilution.

>Emittance dilution may be ameliorated by splitting the tune of the lattice.

>Further experimental data is needed on the actual splitting of the dipole degeneracies in frequencies that is likely to occur in the fabrication of several thousand ILC cavities (experiments at DESY, TTF already in progress will be helpful in this respect –Ross, Napoly, Baboi et al). In addition, simulations are in progress on the splitting of the tune encountered due to the HOM couplers.

>Analysis of the influence of higher order bands on enRtf: Rapers dilbrain dy inntices formeds enlitting by Ancelet de outpaces EBAC06 required. The effect of purposely distorting the shapes of the cavities in order to increase the frequency degeneracy splitting requires further study.

- The feedback system, FONT currently under study will need interfacing with the beam wake fields that result from realistic fabrication errors.
- GDE (Adolphsen/Ross/Hayano/Napoly) have pointed out that mode characterisation studies and mode splitting under the influence of realistic fabrication errors are important issues.
- KEK (Hitoshi Hayano san) has started some preliminary mode measurements. UK collaboration has been initiated.
- These are issues which will be encountered in the baseline and in the alternative, high-gradient designs. In particular, the re-distribution of fields in the new cavity structure will require simulations of both the fields in the main body of the structure and within the vicinity of the

4. HOMs, Beam Dynamics in Crab Cavity

Personel

COCKCROFT INSTITUTE

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Cockcroft Institute



FNAL Leo Bellantoni Mike Church Timergali Khabiboulline Brian Chase

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 $\frac{\text{CKM Cavity design parameters}}{3.9 \text{ GHz}}$ 13 cells length = 0.5 m $B_{max} = 80 \text{ mT}$ $E_{max} = 18.6 \text{ MV/m}$ $L_{eff} = 0.5 \text{ m}$ $P_{\perp} = 5 \text{ M V/m}$



Courtesy: FNAL



The ILC crab cavity is based on the FNAL deflecting mode cavity.

To minimise wakefields for the short time structure of the ILC bunches, the number of cells must be optimised against overall length and new couplers designed.

A 3.9 GHz cavity was favoured it is compact longitudinally and transversely.



The crab cavity has to be close to the IP for phase synchronisation issues. This means that only the final focussing doublet is between the cavity and the IP. The positioning of the crab cavity at a region with a large beta function means that wakefield kicks are not focussed effectively.





A long range wakefield is a superposition of the fields created by each bunch.



If the bunches all arrive at regular intervals and the same offset then the wakefield will tend to a finite constant value known as the sum wake



 $\Delta \omega/2\pi$ (MHz) It is useful to find the frequency dependence of the sum wake. As we sweep through the frequency errors we see that we see resonances with the bunch. Calculating the damping tolerances using this method is slow. However each resonance is due to a single mode hence a single-mode analysis of the damping requirements is valid.



4. ILC 3.9 GHz Crab Cavity 20.0 15.0 щ 10.0 InfiniteBunchesImagQ=3x10^5 5.0 100 Bunches Imag Q=3x10^5 2800 bunches Imag Q=3x10^5 0.0 0.00 0.02 0.04 0.06 80.0 0.10 $\Delta\omega/2\pi$ (MHz)

Depending on the Q factor, the sum wake can be reached very quickly, for the ILC we are likely to reach the sum wake within a few hundred bunches. **Finite Bunch trains**

We can rearrange the single-mode wakefield equation for the sum wake as a quadratic equation.

$$F_{I\max}^{\infty} x^{2} - \left[2F_{I\max}^{\infty} \cos\delta + \sin\delta\right] x + F_{I\max}^{\infty} = 0$$

Where

$$x = \exp\left(-d\right) \equiv \exp\left(-T_b / T_d\right)$$

And F_{Imax} is the maximum allowable wakefield normalised by R/Q The solution of this equation is

$$c = \frac{\left[2F_{I_{max}}^{\infty}\cos\delta + \sin\delta\right] - \sqrt{\left[2F_{I_{max}}^{\infty}\cos\delta + \sin\delta\right]^{2} - 4(F_{I_{max}}^{\infty})^{2}}}{2F_{I_{max}}}$$

Giving a Q requirement of

$$Q = \frac{\omega T_b}{2\ln(1/x)}$$
Solving for Q

• As we are summing the contribution to the wake from all previous bunches, resonances can appear. For longitudinal wakes we sum

$$\sum_{n} \cos(n\omega\tau) \exp(-n\frac{\omega\tau}{2Q}) \qquad \omega = \frac{2\pi}{n^2}$$

hence resonances appear when

• It is more complex for transverse wakes as the sum is

$$\sum_{n} \sin(n\omega\tau) \exp(-n\frac{\omega\tau}{2Q})$$

• However we can find the resonances from the single-mode wake equation

$$F_I^{\infty} = \frac{\sin \delta}{2(\cosh d - \cos \delta)}$$

Using $\frac{dF_I^{\infty}}{d\omega} = 0$

The solution of which is

$$\Delta \omega_{\max} = \frac{1}{T_b} \cos^{-1} \left[\operatorname{sech} \left(T_b / T_d \right) \right]$$

Resonances



If we return to the single-mode sum wake we can see the two resonances at the frequencies either side of the longitudinal resonance

Single-Mode Sum Wake

Damping Requirements



Inserting the frequencies of the resonances into the single damping solution already derived gives

$$x = \frac{-1 + \sqrt{1 + (2F_{I\max}^{\infty})^{2}}}{2|F_{I\max}^{\infty}|}$$

$$x = \exp\left(-d\right) \equiv \exp\left(-T_b / T_d\right)$$

And hence

 $Q = \frac{-\omega T_{b}}{2 \ln \left[\frac{-1 + \sqrt{1 + (2F_{I_{\max}}^{\infty})^{2}}}{2 |F_{I_{\max}}^{\infty}|} \right]}$

This is the damping required to keep the wakefields below the level F_{Imax} , for the worst case wakefields.



The PLACET results show when the damping tolerances are met with a maximum Q of 1x10⁵ the maximum vertical offset is 1.5 nm.

The results give good agreement with the previous analytical results.









5. High Precision SC Cavity Alignment/Diagnostics/BPM with HOM Measurements

Nicoleta Baboi, Olivier Napoly, Ursula van Rienen <u>Roger M. Jones</u> DESY, CEA Saclay, Univ. of Rostock, Univ. of Manchester/ Cockcroft Inst.



Invited talk at EGARD-OMIA,CERN. Spokesperson on behalf of Accelerator and Beam Studies and HOM FP7 <u>collaboration</u>





5. Aspects of HOMs in SC Accelerator Cavities

<u>1. HOM based Beam Position Monitors (HOMBPM)</u>

•Initial electronics have been developed for single bunch and installed at FLASH allowing the beam to be centered to within 5 μ m.

Method needs to be verified with additional modes

Multi-bunch issues need to be understood.

•The 3.9 GHz bunch shaping cavities being installed in FLASH and XFEL can readily dilute the beam emittance –important to instrument with electronics modules to diagnose the beam position and improve the emittance.

2. HOM based phase monitors (HOMPM)

•Measure phase of RF injected into the cavities with respect to the phase of beam.

Proof of principle tests revealed the potential of a HOM-based method.

Additional LLRF development at FLASH needed.

3. HOM Cavity Diagnostics and ERLP (HOMCD)

•HOM spectrum allows one to ascertain the cavity alignment and cell geometry.

•Will investigate:

- mechanical deviations of individual cells from the ideal geometry,
- cell-to-cell misalignment,
- deformation of fields by couplers.

•This part of the project requires beam-based measurements at FLASH, DESY and ERLP, Daresbury, and RF-based measurements using the wire test facility at the Cockcroft Institute.

4. HOM Distributions and Geometrical Dependences (HOMDG)

•Combining finite element and S-matrix cascading techniques allows the eigenmodes in multiple accelerating cells and cavities to efficiently modeled. The University of Rostock and the University of Manchester have developed a suite of codes.

•Will apply these powerful computing methods in order to specify allowable tolerances on fabrication and alignment of the TESLA cells and cavities for future colliders and light sources.

5. HOM studies for Proton Injectors (HOMPI)

HOMS also impact the beam emittance and cause heating of the cavity in proton machines
Has the potential to benefit from similar HOM measurement diagnostics



5. Analysis of Narrowband Signals – Beam Position



5. HOM-BPMs

- Calibration based on SVD
- Resolution achieved:
 - ~5/10µm rms (Y/X) single bunch, limited by LO
- **Issues:**
 - improve resolution
 - multi-bunch:
 - individual bunches measurable with lower resolution (f_{rep} ≤ 1MHz at FLASH)
 - speed issues
 - suitability of various HOMs
 - alternative electronics
 - <u>electronics for 3.9GHz cavities</u> <u>needed</u>



