

# Higgs mass measurement through $\mu$ channel of Higgs strahlungs process ( $e^+e^- \rightarrow HZ \rightarrow \mu\mu H$ )

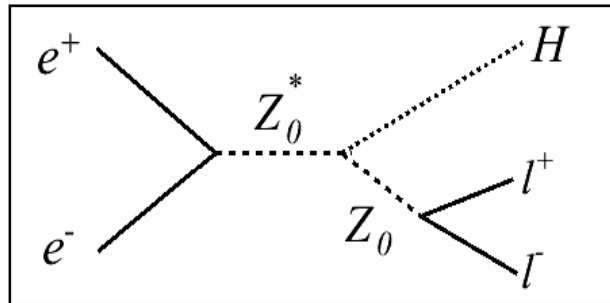
Manqi Ruan

Discussing & Support: Francois, Roman, Phillip Vincent,  
Advisor: Z. ZHANG (LAL) & Y. GAO (Tsinghua))

# Outline

- Motivation & Software introduction
- Higgs Mass & cross section determination
  - Model independent Measurement
  - Model dependent event selection: treat Higgs SM/invisible decay separately
    - Result for SM Higgs
    - Result if Higgs can decay invisibly
- Test of Higgs mass measurement with different beam parameters
- Summary

# Motivation: Higgs strahlung @ $\sqrt{s} = 230\text{GeV}$



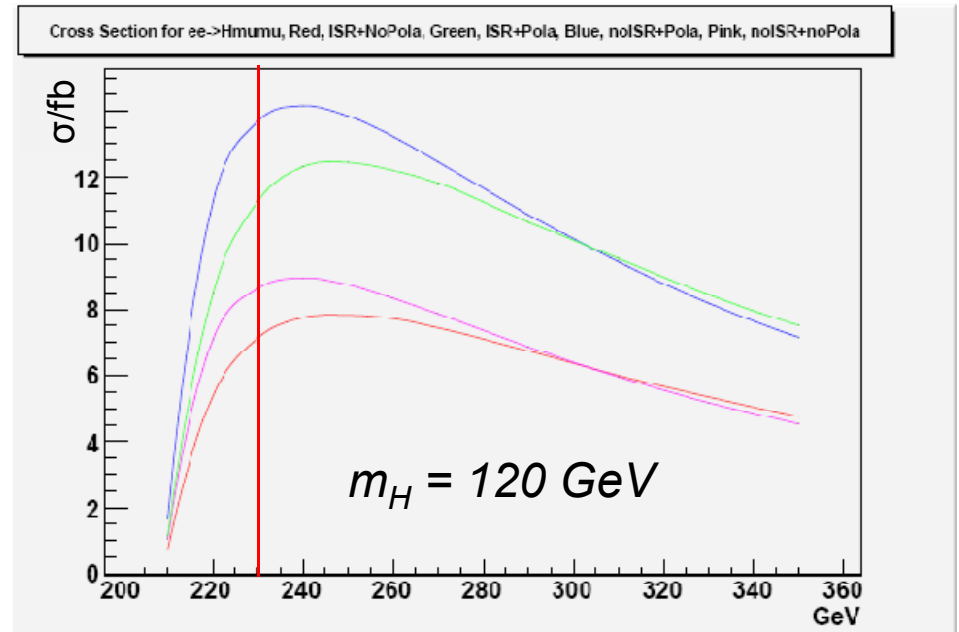
Golden Channel for measure Higgs Mass & Cross Section

$$m_h^2 = s + m_Z^2 - 2E_Z \sqrt{s}$$

$$g^2 \propto \sigma = N / L\mathcal{E}$$

Only muon momentum information is needed

A **model independent** analysis can be applied. We will avoid using any model dependent cuts (like separation angle, etc)



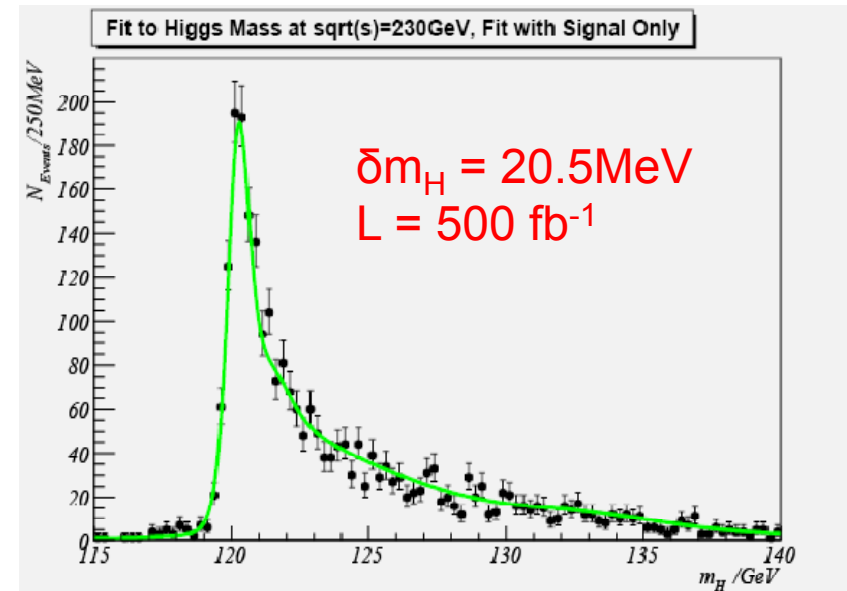
$$\delta m_h^2 \sim p^2 ;$$

Small  $\sqrt{s}$  means better Higgs mass resolution!

*Beam polarization will increase the signal cross section by 58%. (electron 80%, positron, 40%)  
ISR effect will reduce the cross section with  $\sqrt{s} < 300\text{GeV}$  (threshold effect) while increase it a little at higher energy*

# Software chain

- Generator: whizard-1.50 (for Signal), pythia 6.4.13 (for backgrounds) ( with Guinea-Pig to simulate BS effect);
- Full Simulation: Mokka-v06-04. with LDC01\_sc detector conception (184 TPC layer), *the accuracy of tracking system to  $5e-5$  at  $\delta(1/P)$  on average*
- Reconstruction & Analysis: MarlinReco/Marlin, ROOT;
- Fit: Using likelihood method provides by RooFit:  
 $\delta m_H = 20.5\text{MeV}$  for pure signal



# X section of main BG

Sqrt(s)	230GeV	250GeV	350GeV
ZH(fb)	6.62 (3310 evt)	7.78 (3890)	4.87 (2435)
ee→ZZ (fb)	1.34k (672k)	1.27k (635k)	0.856k (428k)
ee→WW (fb)	15.86k (7.93M)	15.61k (7.81M)	1.155k (5.77M)
ee→qq (fb)	57.6k (28.8M)	52.2k (26.1M)	22.63k (11.3M)
ee→μμγ (fb)	5.38k (2.69M)	4.34k (2.17M)	2.20k (1.1M)

- *Huge SM Background: Pre Cuts is needed!*
  - Energetic pion/muon ( $E1 > 15\text{GeV}$ ) (pions are included here for the PID has a chance  $\sim 1\%$  to misidentify the a pion as a muon)
  - Exist another pion/muon (with energy  $E2$ ), together with the most energetic pion/muon to form an invariant mass  $> 70\text{ GeV}$
  - $\Phi_{mumu} < 177.6\text{Degree}$
  - Kinetic cut:  $2E1 + E2 < 180$  &  $2E1 + 3E2 > 200$

Non-Polarized beam at  $500\text{ fb}^{-1}$ ; ISR, FSR, BS actived

# Precut Chain at Generator level

	ZH	ZZ	WW	QQ	$\mu\mu\gamma$
<i>No Precut</i>	3310	672k	7.93M	28.8M	2.69M
<i><math>E_1 &gt; 15</math></i>	3310	347k	5.22M	15.8M	2.69M
<i><math>m_Z &gt; 70</math></i>	3147	43.7k	310k	169k	920k
<i><math>\Delta\phi &lt; 3.10</math> (177.6°)</i>	3042	42.1k	299k	62.6k	242k
<i>Kinetic</i>	3000 90.6%	17.7k 2.6%	81.9k 1.0%	33.8k 0.12%	23.1k 0.86%

Replace **pre cuts** with more strict cuts after reconstruction:

$$E_1 > 15$$

$$2E_1 + E_2 < 180 \ \&\& \ 2E_1 + 3E_2 > 200$$

$$\Delta\phi < 177.6^\circ$$

$$m_Z > 70$$



$$E_{mu} > 20$$

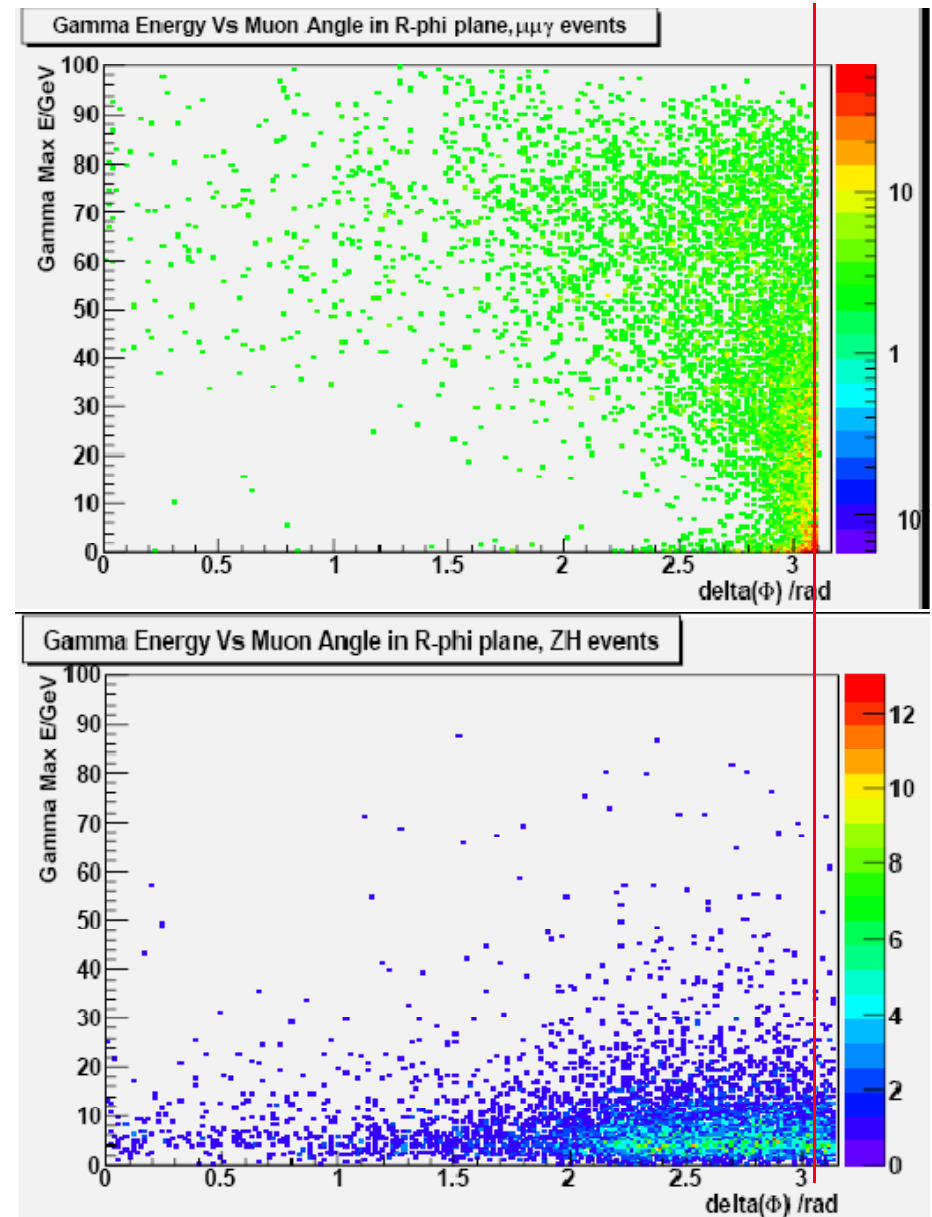
$$2E_1 + E_2 < 178 \ \&\& \ 2E_1 + 3E_2 > 202$$

$$\Delta\phi < 176.4^\circ$$

$$76.2 < m_Z < 100$$

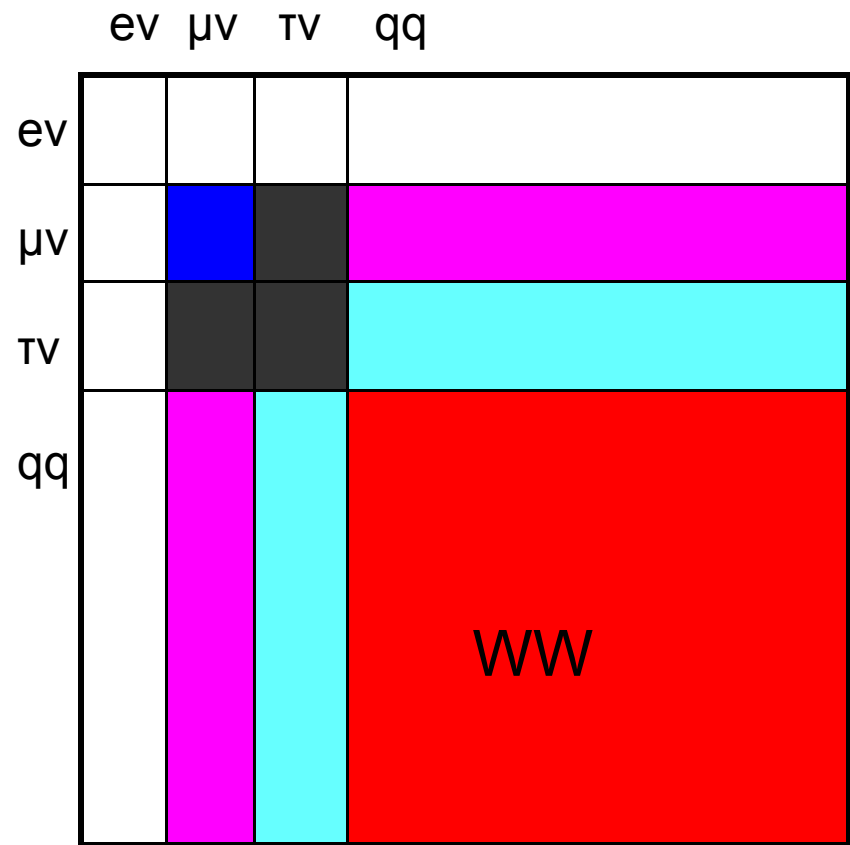
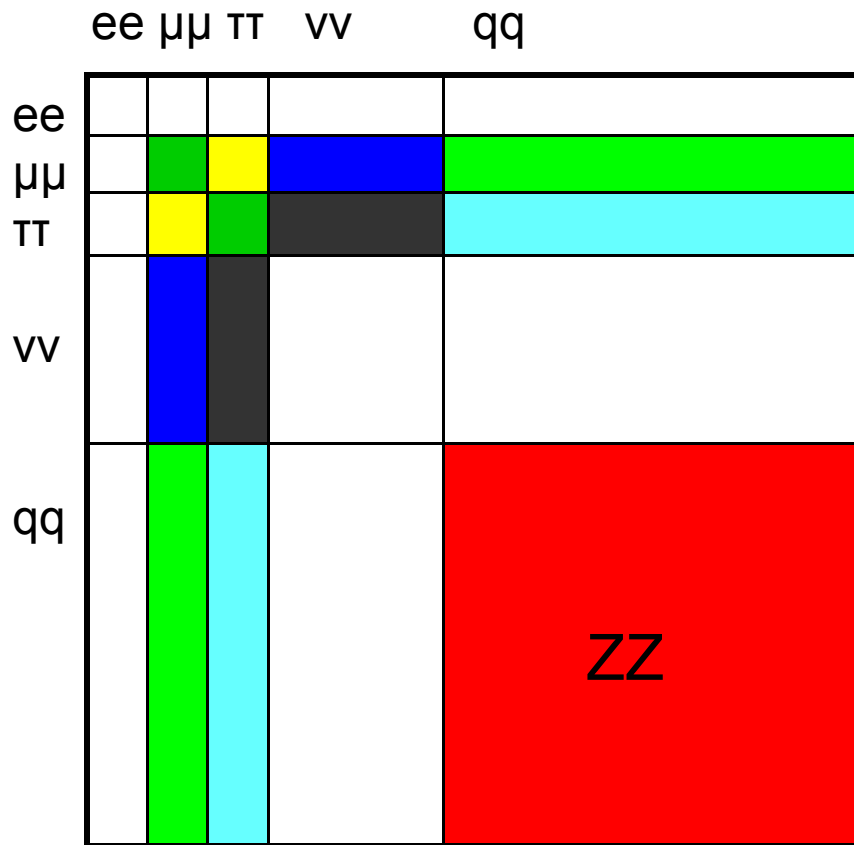
# qq & $\mu\mu\gamma$ BG

- QQ background vanishes after pre cut selection +  $\mu$  id (*the majority of QQ BG passed the precut have pion, not muons*)
- $\mu\mu\gamma$  BG: Veto events with no miss  $P_T$  ( $\Delta\phi \sim \pi$ ) or have reconstructed energetic photon;



# ZZ & WW background

Z decay ratio: ~3% to lepton pairs (each),  
 ~20% to neutrino pairs, ~70% to qq  
 W decay ratio: ~10% to lepton pairs (each), ~70% to qq



Blue: background for Higgs invisible decay

Gray: background for Higgs invisible decay through tau leptonic decay

Light green: background for Higgs SM decay

Red, pink and light blue: possible background for Higgs SM decay (pion be misidentified as muon & muon from bb, cc)

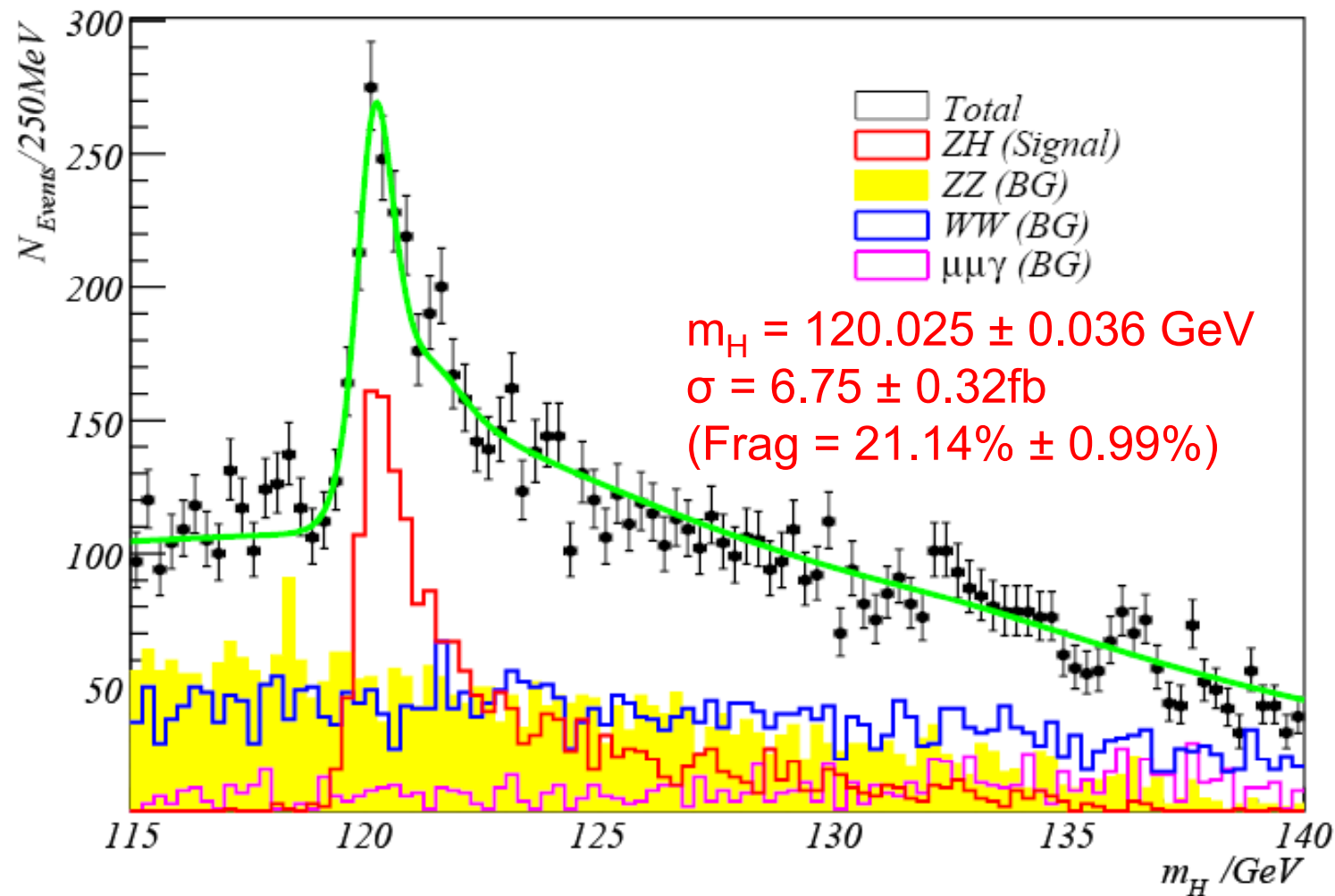
Yellow and Dark Green: background for Higgs SM decay:  $H \rightarrow \tau\tau$



# Cut Chain for model independent analysis

Minimal Version	ZH	ZZ	WW	$\mu\mu\gamma$
<i>Total event num at 500 fb<sup>-1</sup></i>	3310	672k	7.93M	2.69M
<i>Expected event num after preCuts</i>	3k	17.7k	81.9k	23.1k
Both muon identified	2824	15.3k	13.9k	20.3k
<i>recover precuts +Geometry</i>	2439	12.1k	8.6k	14.5k
<i><math>E_2 &gt; 20 \ \&amp;\&amp; \ E_2 &lt; 53</math> <math>\&amp;\&amp; 2E_1 + E_2 &lt; 178 \ \&amp;\&amp; \ 2E_1 + 3E_2 &gt; 202</math> <math>\&amp;\&amp; 2E_1 + 3E_2 &lt; 264</math></i>	2437	7.3k	7.5k	11.9k
<i><math>-0.995 &lt; \text{Cos}(\theta_{\mu\mu}) &lt; -0.3</math></i>	2426	7.0k	7.1k	11.1k
<i><math>\mu\mu\gamma</math> events veto</i>	2210	5.4k	4.8k	1401
<i><math>115\text{GeV} &lt; H_{\text{mass}} &lt; 140\text{GeV}</math></i>	2192	3531	3745	1138

# Model independent measurement: $\delta(m_H) = 36.3\text{MeV}$

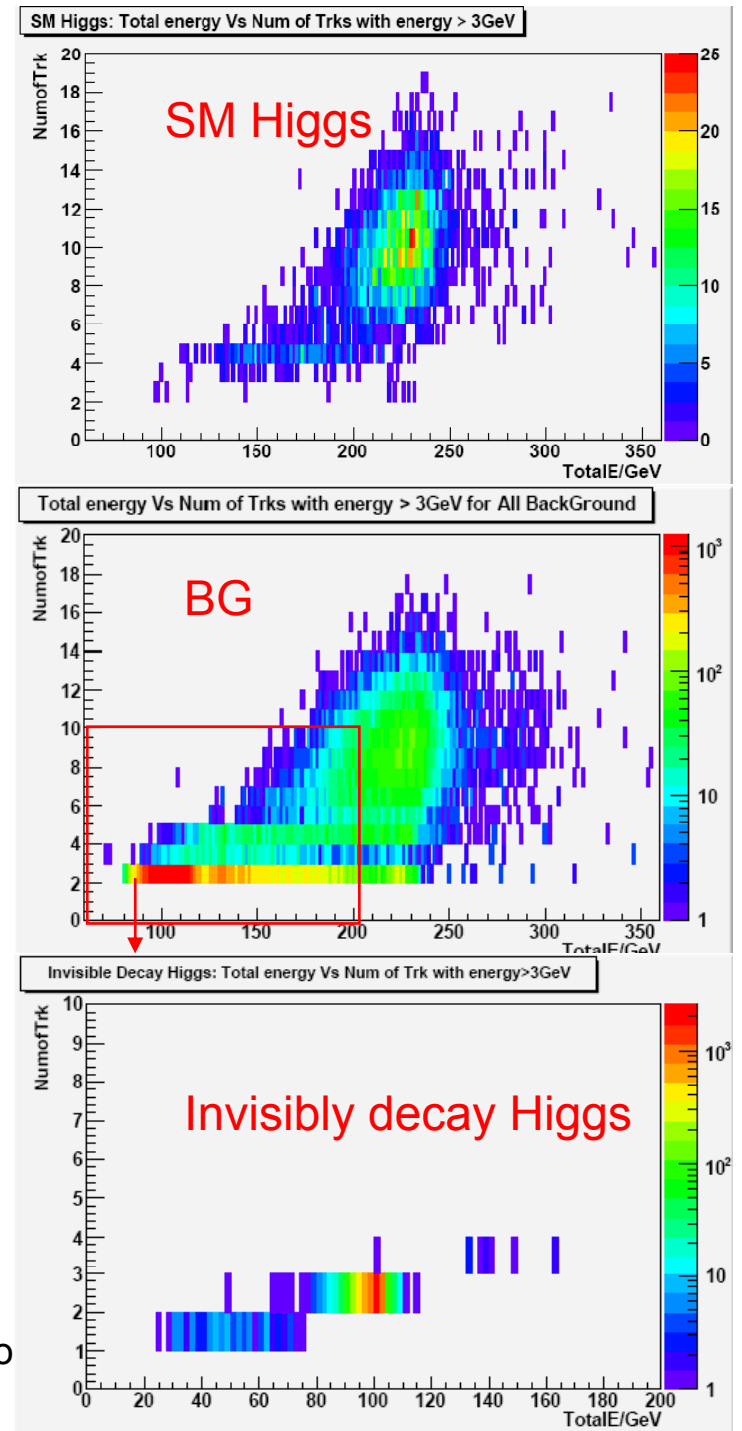


# Further (model dependent) analysis using information on H decay final states

- We can separate the Higgs SM/invisible decay events with 2 obvious benefits
  - Larger S/N ratio and thus better measurement
  - Freedom to tune cuts for different decay models
- Use the variable: Num of tracks with energy > 3 GeV & Total measured energy
- Count the If  $N_{\text{track}} < 4$  && Total energy < 110 GeV, Higgs invisible decay
- If  $N_{\text{track}} > 2$  && Total energy > 150 GeV, SM Higgs decay events

16/01/2008

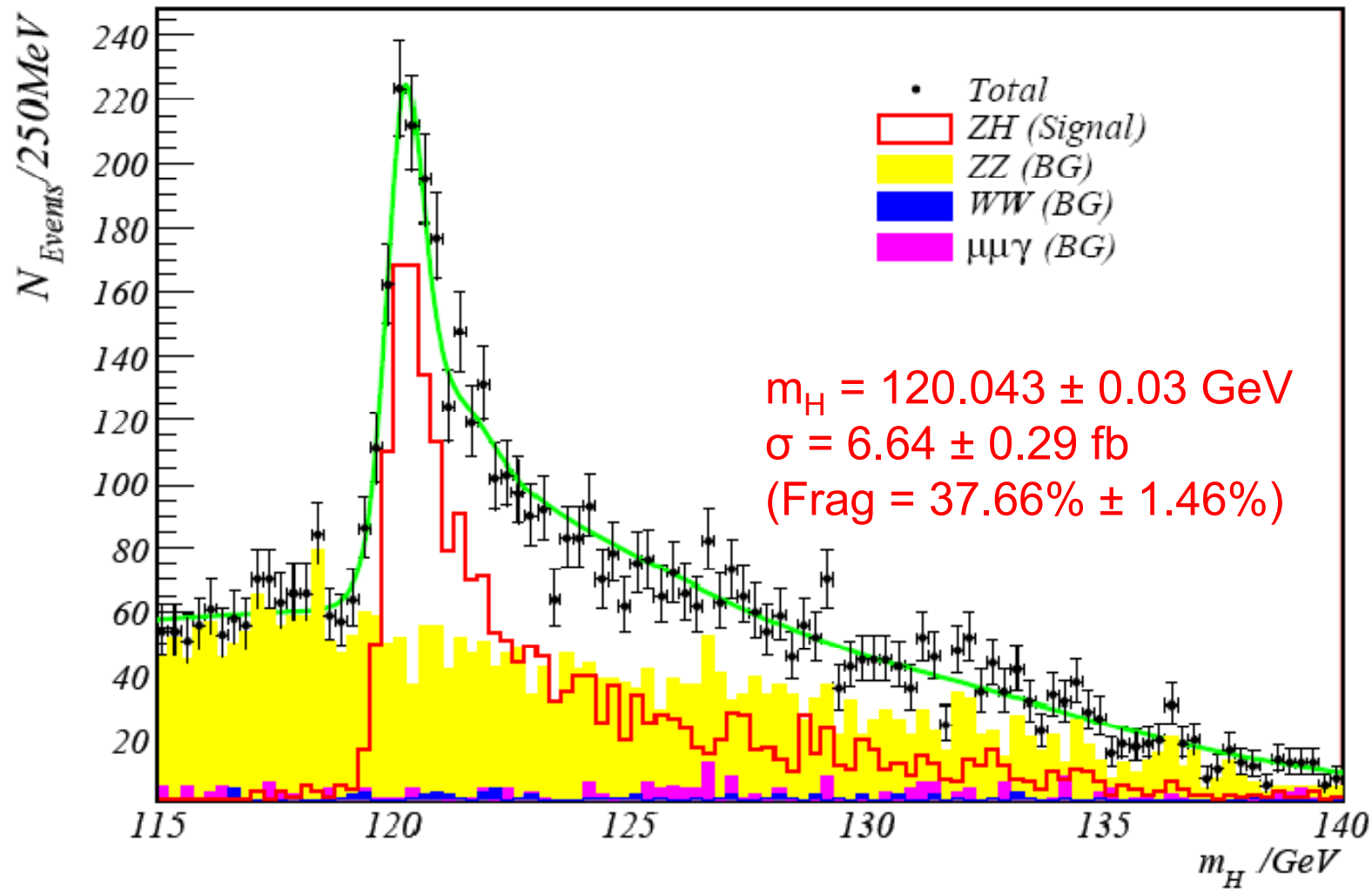
DESY\_Zeuthen@ILD worksho



# Cuts Chain for SM Higgs analysis

	ZH	ZZ	WW	$\mu\mu\gamma$
<i>Total event num at 500 fb<sup>-1</sup></i>	3310	672k	7.93M	2.69M
<i>Expected event num after preCuts</i>	3k	17.7k	81.9k	23.1k
Both muon identified	2824	15.3k	13.9k	20.3k
<i>recover precuts +Geometry</i>	2439	12.1k	8.6k	14.5k
<i>Same Kinetic Cut as model independent analysis</i>	2426	7.0k	7.1k	11.1k
<i>TrkNum&gt;2 &amp;&amp; TotalEn&gt;150</i>	2338	5.4k	526	146
<i>115GeV &lt; Hmass &lt; 140GeV</i>	2319	3.5k	128	389
<i>Loose Veto on <math>\gamma</math> Energy (30GeV)</i>	2280 68.9%	3.4k	124	269

# SM measurement: $\delta(m_H) = 29.95\text{MeV}$



# Higgs Invisible decay

Main background

$$e^+e^- \rightarrow WW, ZZ \rightarrow \mu\mu\nu\nu$$

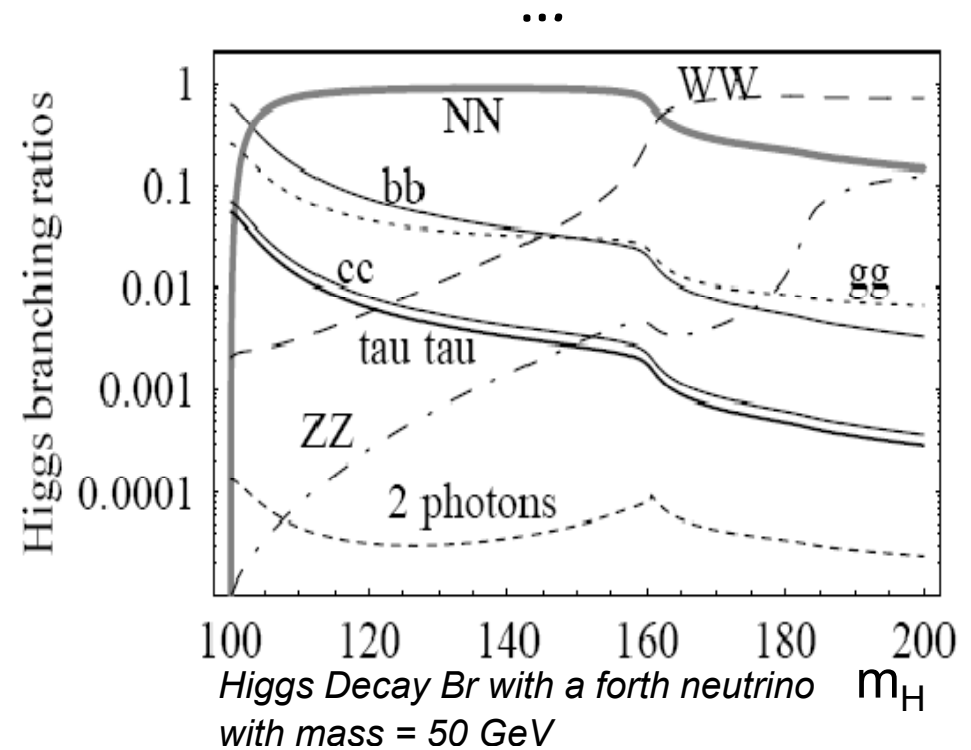
$$e^+e^- \rightarrow \mu\mu(\gamma)$$

Exotic Model beyond SM:

SUSY ?

Extra dimension ?

Heavy neutrino ?

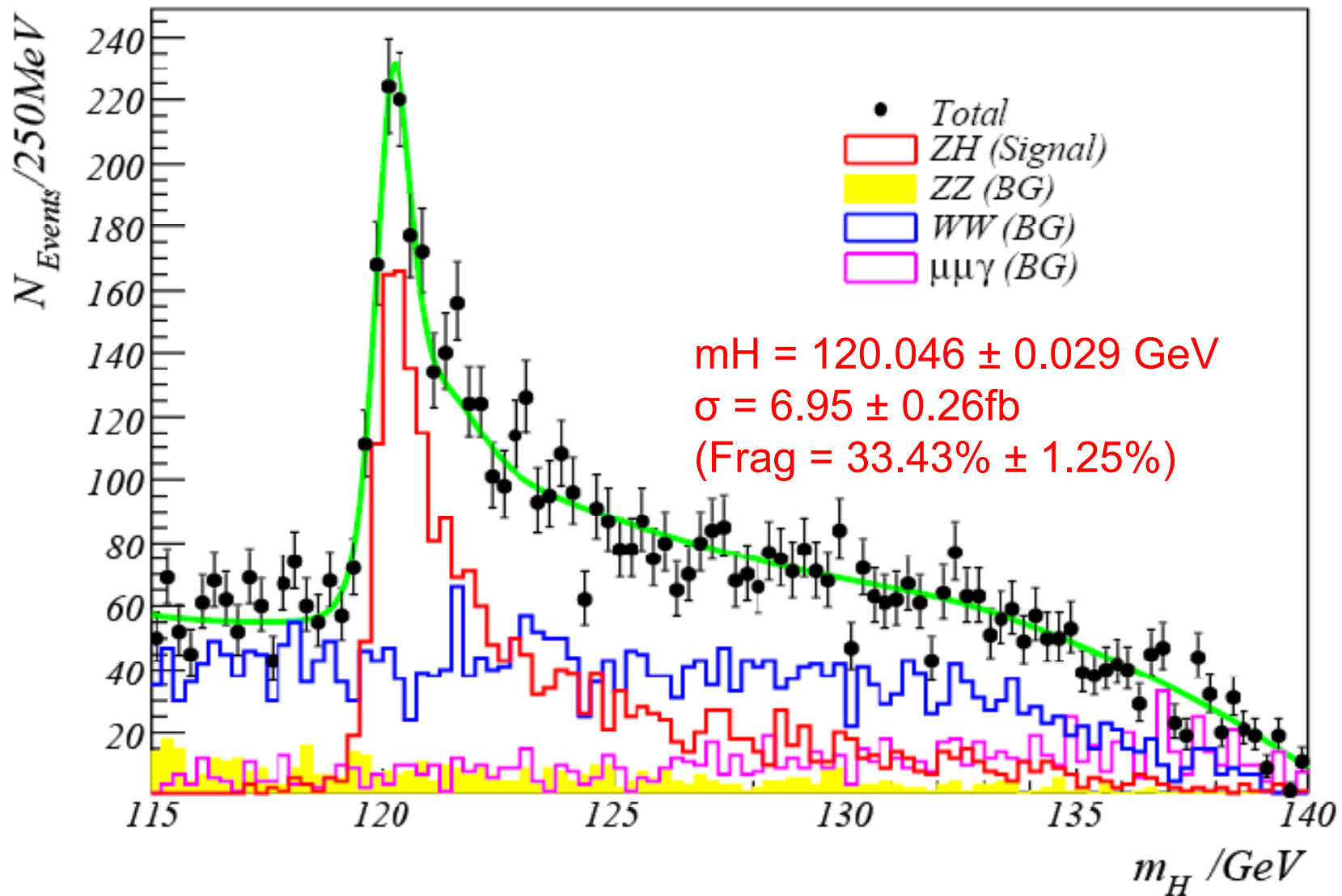


K.Belotsky hep-ph/0210153 (2002)

# Cuts Chain for Invisible Higgs analysis

	ZH	ZZ	WW	$\mu\mu\gamma$
<i>Total event num at 500 fb<sup>-1</sup></i>	3310	672k	7.93M	2.69M
<i>Expected event num after preCuts</i>	3k	17.7k	81.9k	23.1k
<i>recover precuts +Geometry</i>	2439	12.1k	8.6k	14.5k
<i>Same Kinetic Cut as model independent analysis</i>	2426	7.0k	7.1k	11.1k
<i>TrkNum&lt;4 &amp;&amp; 90&lt;TotalEn&lt;110</i>	2326	1.1k	5.2k	2090
<i><math>\mu\mu\gamma</math> events veto</i>	2285	863	4.1k	1164
<i>115GeV &lt; Hmass &lt; 140GeV</i>	2267	554	3316	1016

# Invisible Higgs measurement: $\delta(m_H) = 29.2\text{MeV}$





# Changing beam parameters

- For Linear collider, we can
  - Change beam parameters (eg, changing  $\sigma_z \beta_x \beta_y$  as  $\sim E_{cm}$ ) to maintain the same luminosity (and also same Beamstrahlung), which is the current strategy we applied on our Full simulation analysis. *But this is technologically hard to achieve*
  - Keep beam parameter constant, we have  $L \sim E_{cm}$ ;  $BS \sim E_{cm}^2$ ; while for small  $E_{cm}$ , we suffer more from the weak field reduction, and thus have less than  $230 \text{ fb}^{-1}$  the integration luminosity if scale the machine time to achieve  $500 \text{ fb}^{-1}$  luminosity for 500GeV nominal beam, but also much smaller Beamstrahlung.
  - Some strategy in between above 2
- Use toy MC (*Generator + hand made fast simulation*) to test accuracy of Higgs mass measurement for **signal only** with different **tentative** beam parameter provided by BDS group

# Points on beam parameter space yet scanned

Sqrt(s) /GeV	230	230	250	250	350	350	350	350
L* /m	3.5	4.5	3.5	4.5	3.5	4.5	3.5	4.5
$\beta_x$ /nm	22.7	29.2	20.9	26.9	15.0	19.2	20.3	20.5
ColliX	6	6	6	6	6	6	7.0	6.2
$\eta_L$ /percent	80.7	77.0	83.0	79.5	90.1	87.8	90.1	87.8
L / $10^{37}m^{-2}s^{-1}$	6.70	5.55	7.93	6.54	14.7	12.4	12.4	12.1
L /fb <sup>-1</sup>	181	150	214	177	397	335	335	327
$\sigma$ /fb	7.03	7.06	7.81	7.83	4.80	4.80	4.78	4.80
Exp event num	1272	1059	1671	1386	1906	1608	1601	1570
$\delta$ (mH) /MeV	22.4	24.7	32.8	31.9	107.2	109.1	115.2	117.5

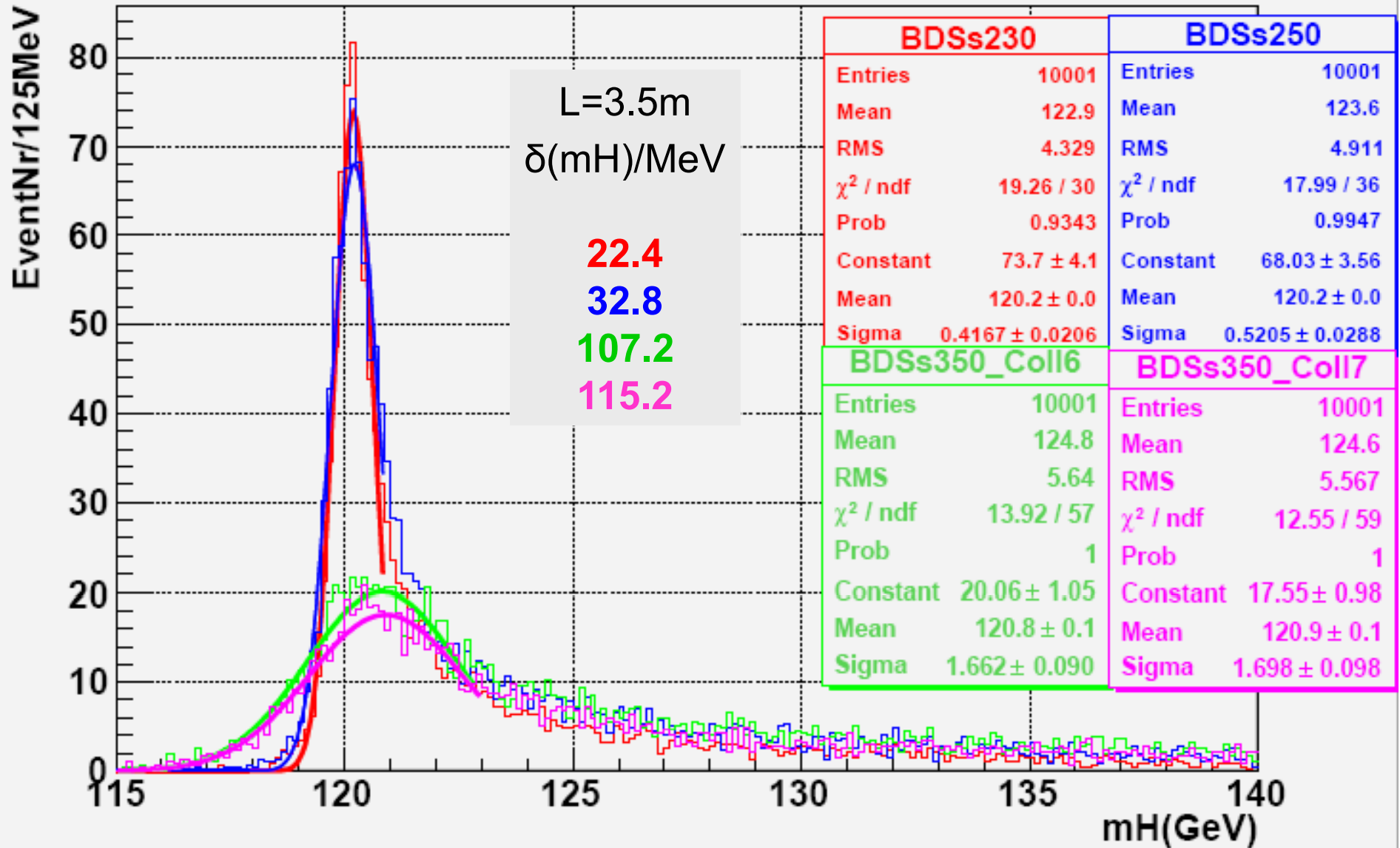
Machine time had been set to make Nominal beam (500GeV) reach an integrated Luminosity be 500 fb<sup>-1</sup>

$\eta_L$ : weak field reduce factor on Luminosity.  $L_{true} = L_{geo} * H_D * \eta_L$

ColliX: Collimator depth X, always bigger than 6

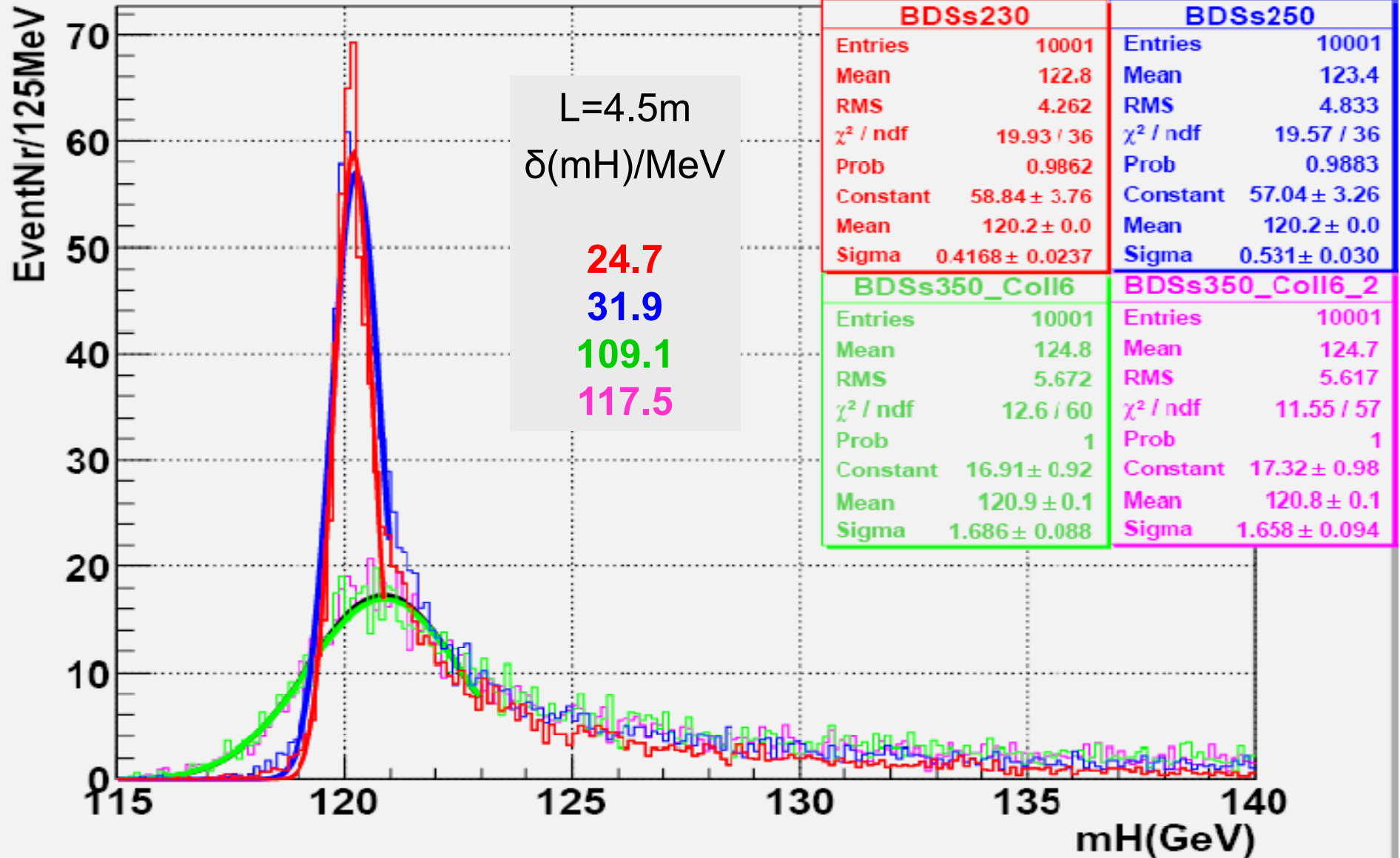
# Sample Gaussian fit to the core; $L^* = 3.5\text{m}$

Higgs Recoil Mass Spectrum Vary with different Beam Parameter



# Sample Gaussian fit to the core; $L^* = 4.5\text{m}$

Higgs Recoil Mass Spectrum Vary with different Beam Parameter with  $L=4.5\text{m}$



# Summary

- Accuracy of Higgs mass and cross section measurement through  $ee \rightarrow HZ \rightarrow H\mu\mu$  with Higgs SM decay and Higgs invisible decay assumption have been studied.
- Condition: 120GeV Higgs. Non polarized beam (with ISR, FSR & BS) with an integration luminosity of  $500 \text{ fb}^{-1}$
- Two strategies had been applied:
  - Model independent Higgs mass measurement:  $\delta(mH) = 36\text{MeV}$
  - Treat SM/Invisible decay Higgs separately:  $\delta(mH)$  could be measured better than 30MeV.
  - Cross section can be measured to an accuracy of 0.3 fb
- It is foreseen to improve a lot with beam polarization for it will not only reduce the WW background but also increase  $\sim 58\%$  the cross section of Higgs strahlung channel (electron, 80%, positron, 40%).
- To do: likelihood methods for events identification; for SM Higgs, use jet energy information to reduce the ZZ Background
- With beam parameter suggested by BDS group, best higgs mass measurement achieved at  $\sqrt{s} = 230\text{GeV}$



Thank you!

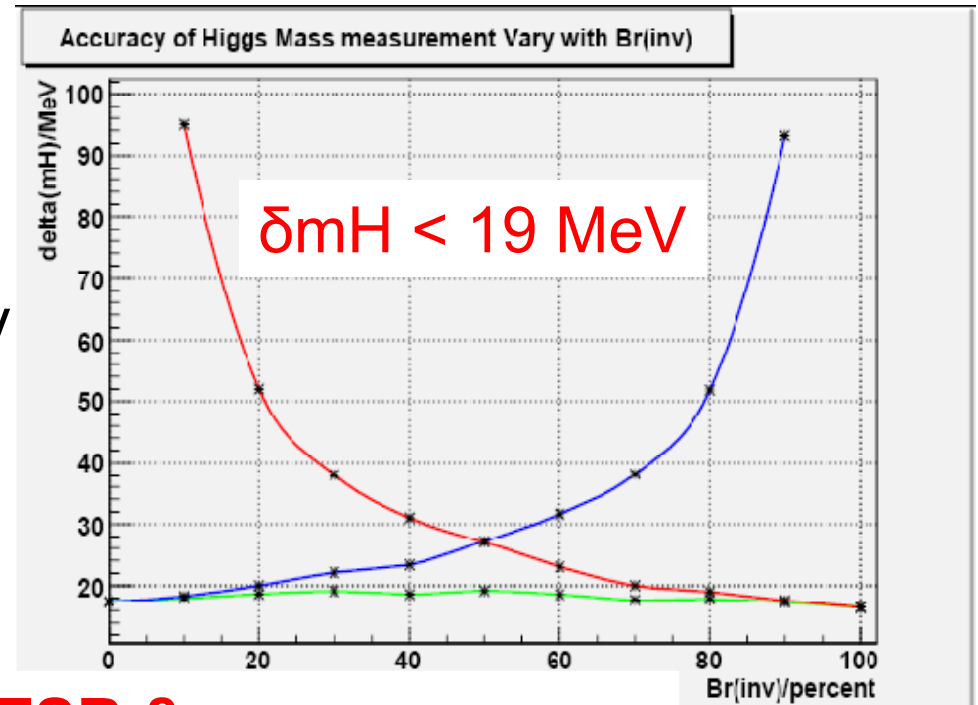
# For arbitrary Br(inv)

Combination the result from Higgs invisible and visible decay  
( Br(inv) + Br(visible) = 100% )

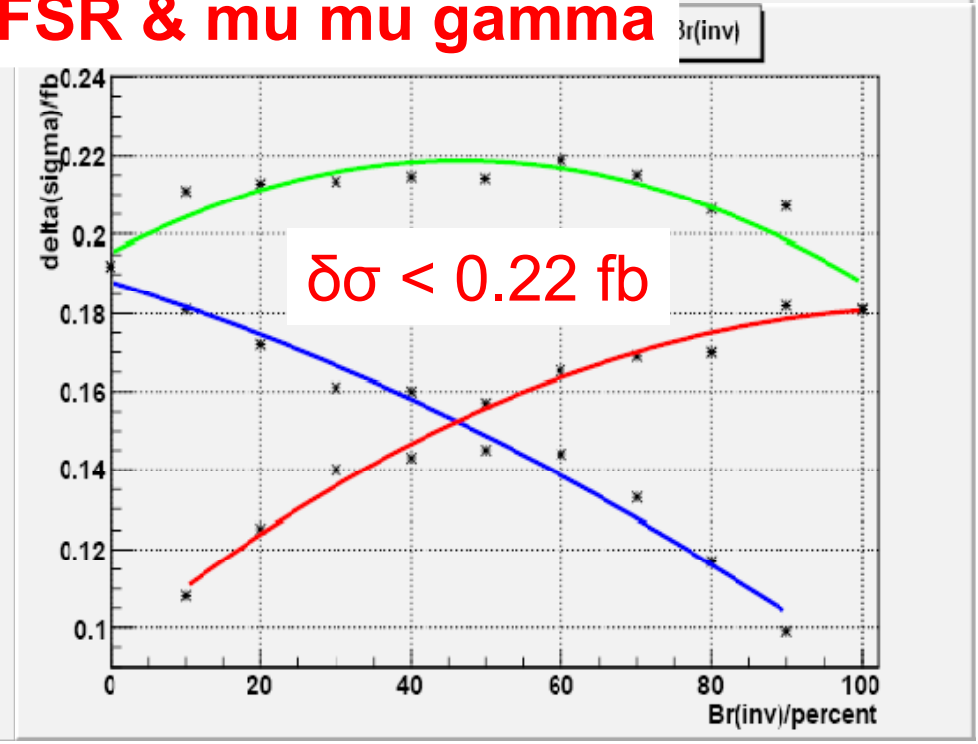
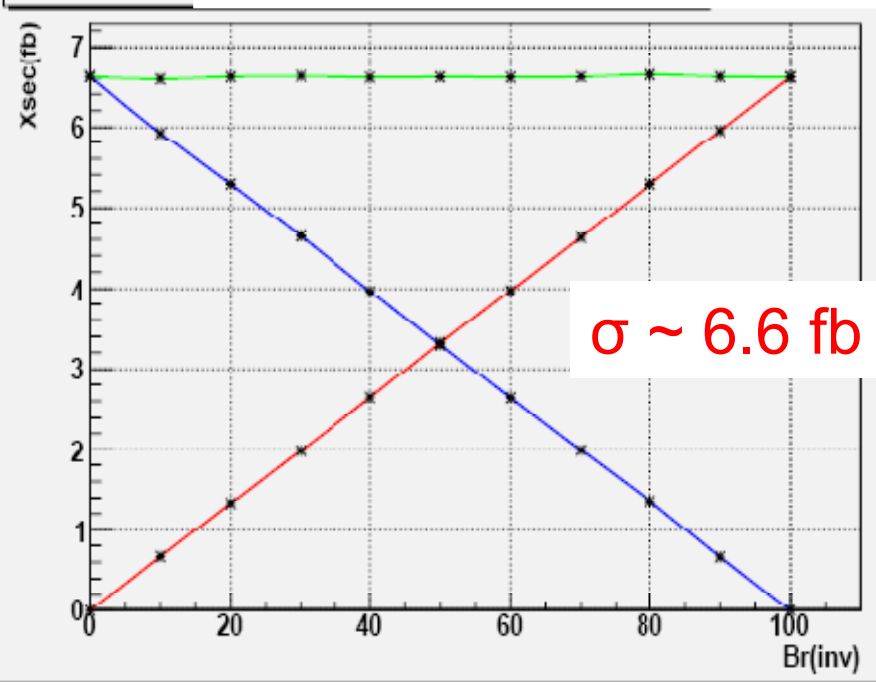
Red, invisible part contribution

Blue, visible part contribution

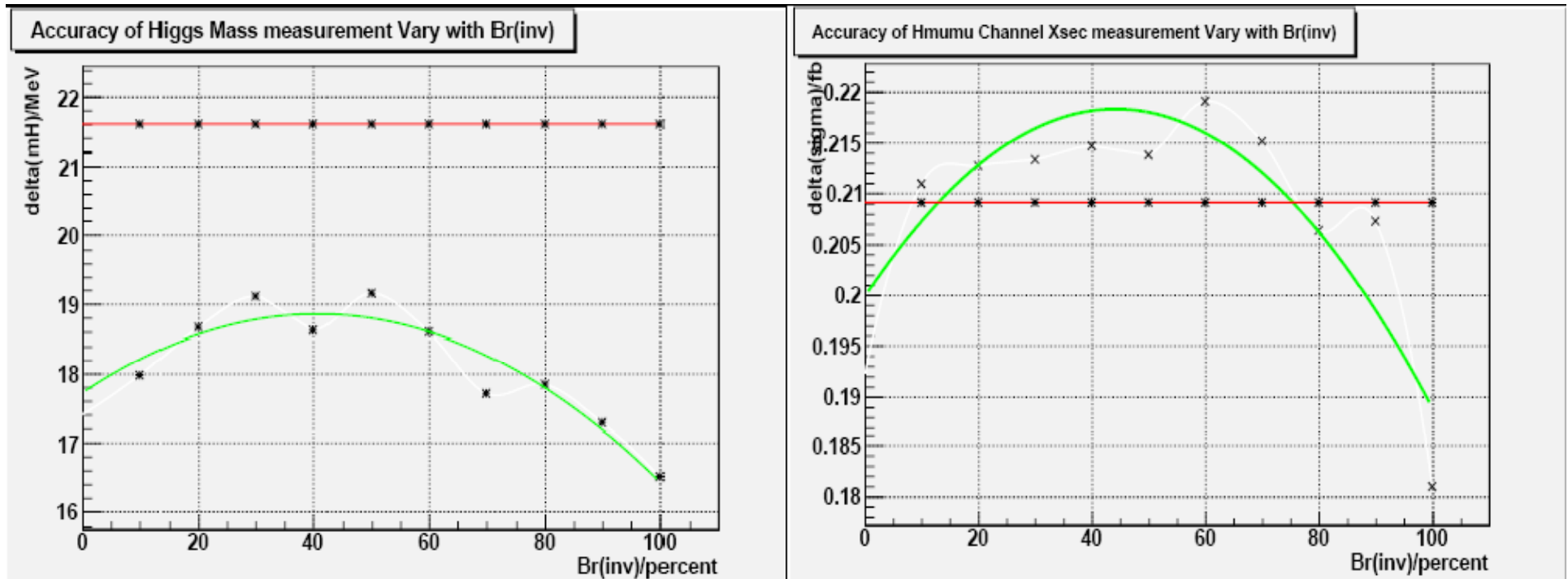
Green, overall result



## Total Cross Section Previous result with no FSR & mu mu gamma



# Comparison on effect of different analysis strategy

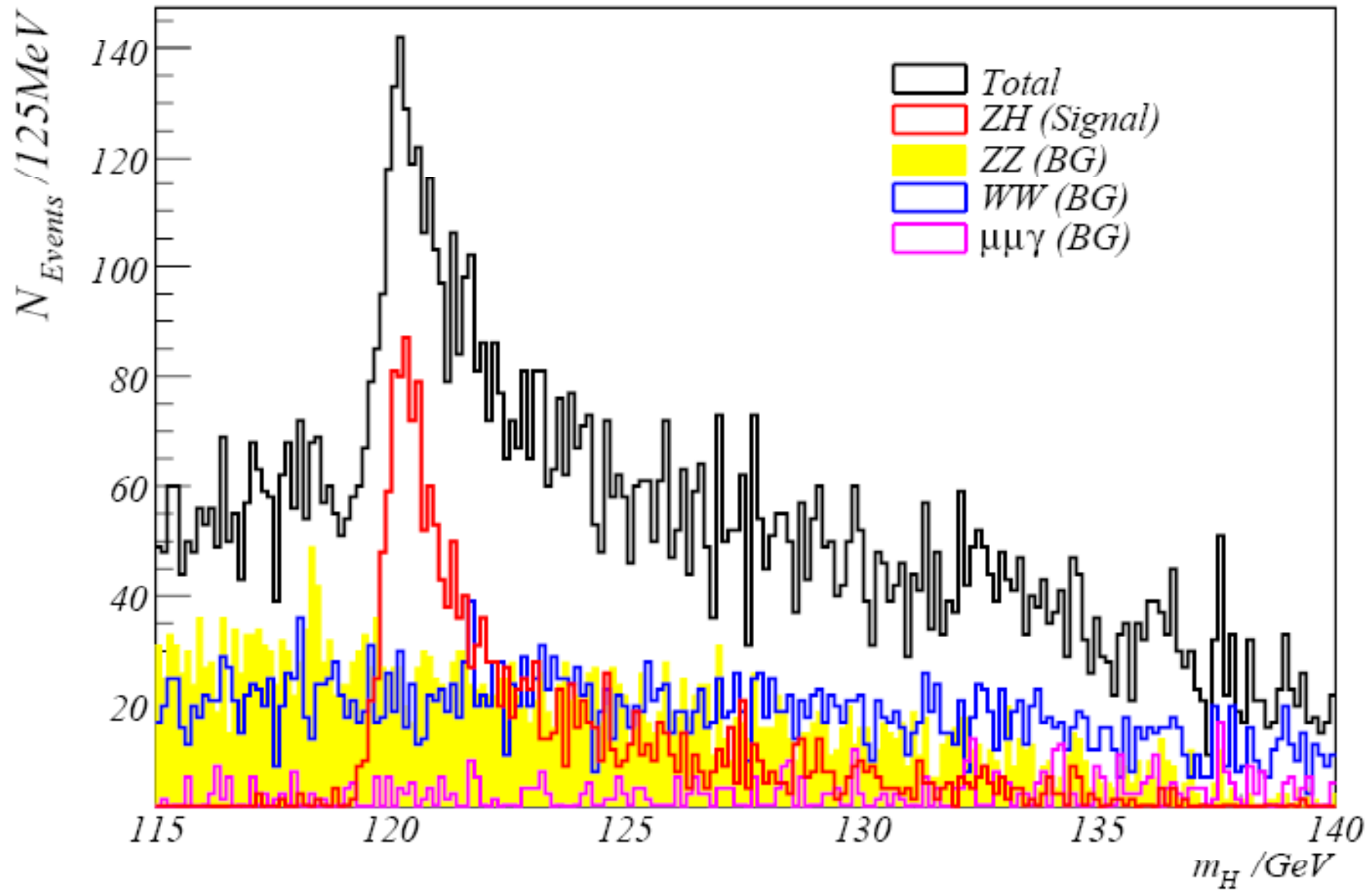


For Higgs Mass Measurement, the accuracy is improved by ~15% with using the Separate strategy; while for the cross section measurement, no obvious improve

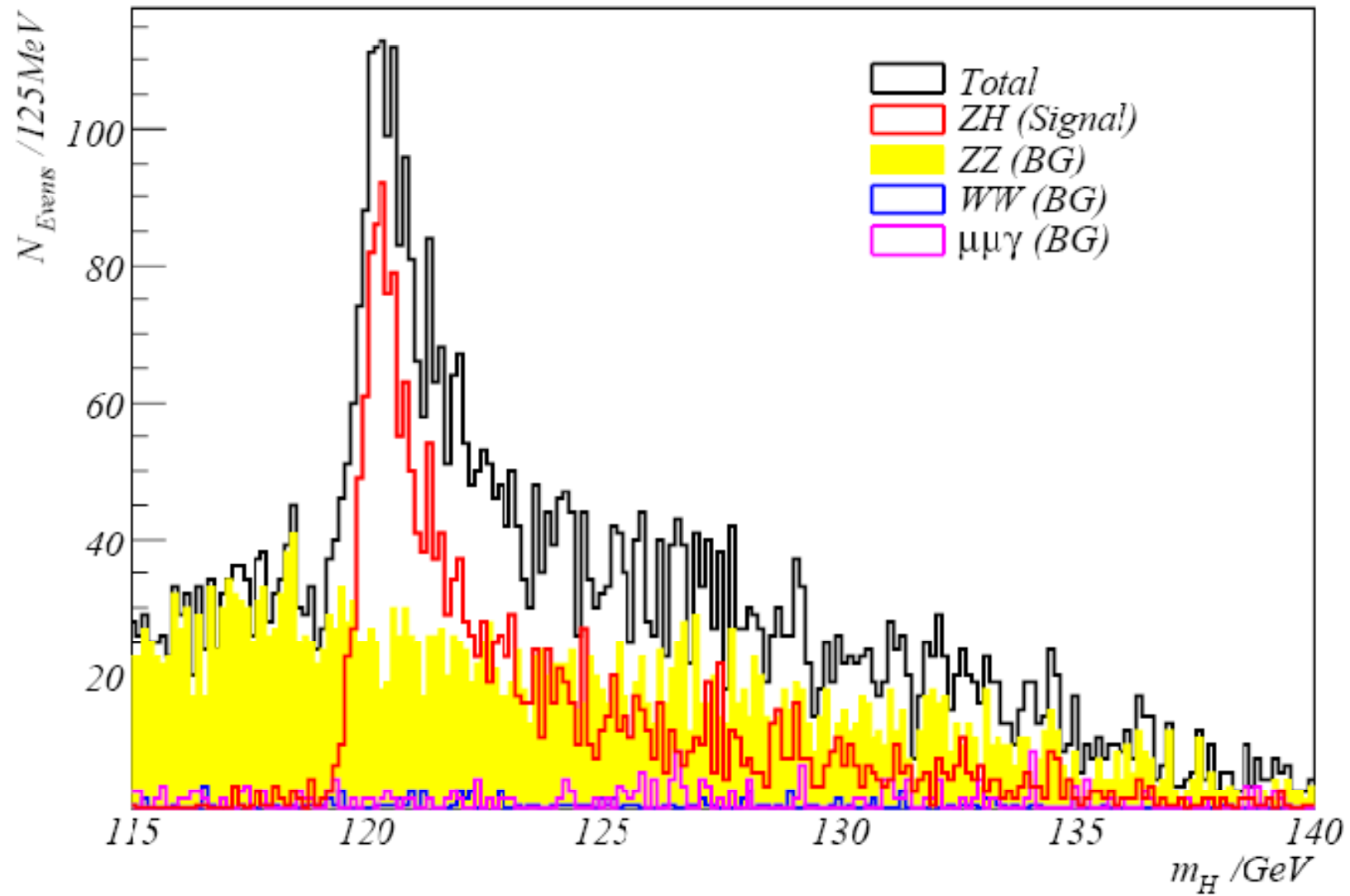
The separate strategy achieves best resolution while 100% Higgs decay invisibly (High reconstruction efficiency)



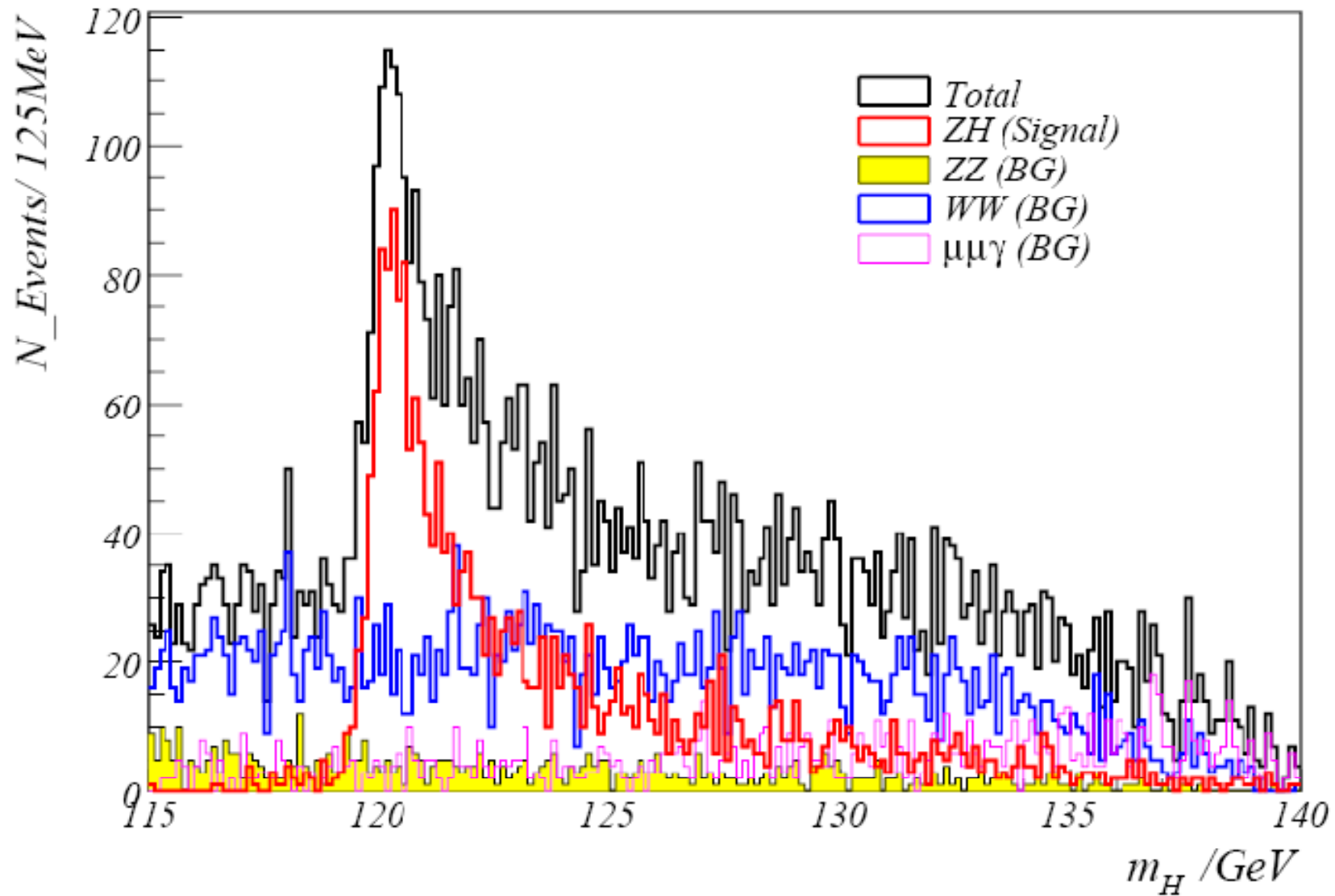
# Higgs Recoil Mass Spectrum after Cuts, Model independent analysis



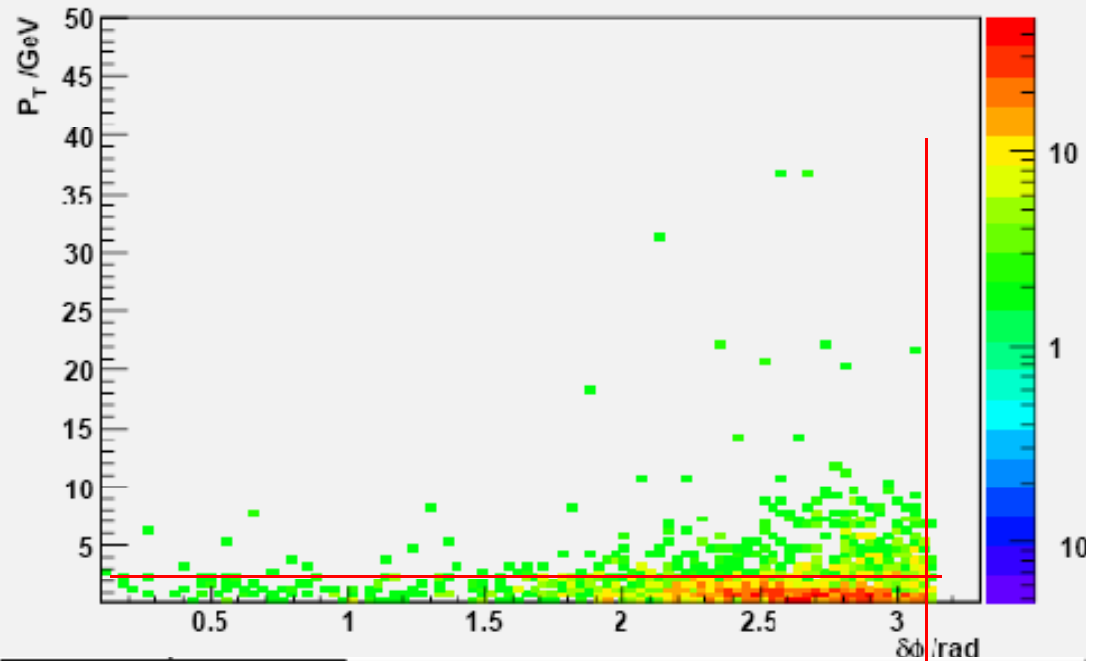
## Higgs Recoil Mass Spectrum after Cuts, SM Higgs



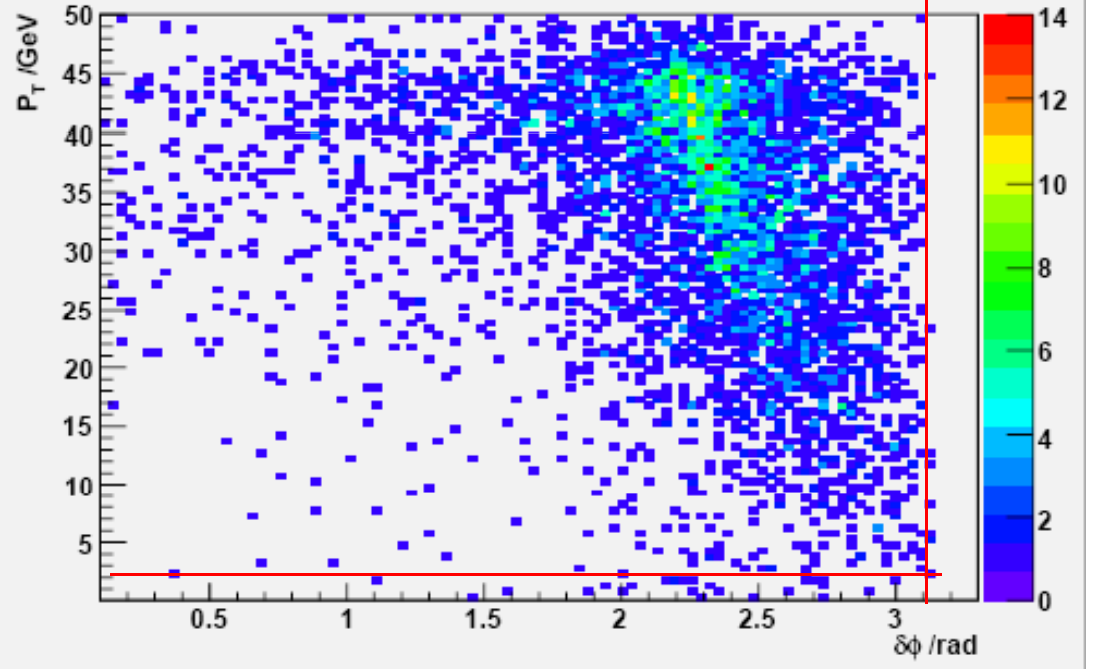
Higgs Recoil Mass Spectrum after Cuts, Invisibly Decaying Higgs



**$P_T$  Vs  $\delta\phi$ ,  $\mu\mu\gamma$  events**



**$P_T$  Vs  $\delta\phi$ , ZH events**



16/01/2008

DESY