

Pinning down the invisible sneutrino at the ILC

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Outline

- Motivation
- The setup
 - Signal and background processes
 - Imposing cuts
- Results
- Summary and outlook

In collaboration with W. Kilian, J. Reuter, T. Robens, K. Rolbiecki, JHEP10(2008)090

Motivation

Standard way of determining sneutrino mass

Martyn '03

- select $e_L^- e_R^+ \rightarrow \tilde{\nu}_e \tilde{\nu}_e \rightarrow e^- \tilde{\chi}_1^+ e^+ \tilde{\chi}_1^-$ with subsequent $\tilde{\chi}_1^\pm \rightarrow q\bar{q}' \tilde{\chi}_1^0$
- primary lepton energy spectra => sneutrino and chargino mass
- di-jet invariant mass spectrum => $\tilde{\chi}_1^\pm - \tilde{\chi}_1^0$ mass difference
- for tau-sneutrino more problematic due to ♦ decay

In some scenarios, e.g. SPS1a' $m_{\tilde{\chi}^\pm} > m_{\tilde{\nu}}$

- dominant decay $\tilde{\nu} \rightarrow \tilde{\chi}^0 \nu$
- invisible decay products
- can nevertheless 'see' sneutrino in the inverse process

$$\tilde{\chi}^\pm \rightarrow \ell^\pm \tilde{\nu}_\ell$$

already exploited by Freitas, Porod Zerwas '05

Setup

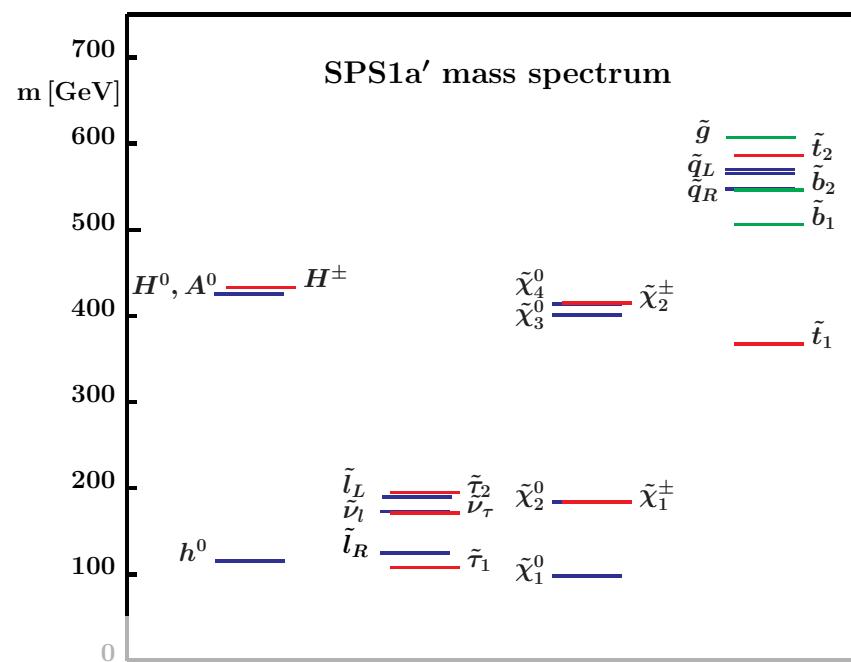
What's new???

- ❑ Revisit the analysis using full matrix element for both signal and background
 - ✓ include all interference and off-shell effects
 - ✓ get a handle on multi-particle final states (up to 10 particles)
 - ✓ include all SUSY and SM reducible and irreducible background
- ❑ Tools:
 - ✓ Monte Carlo event generator WHIZARD (Kilian, Ohl, Reuter)
 - ✓ matrix element generator O'Mega (Moretti, Ohl, Reuter)
 - ✓ so far LO MC for production+ decay implemented
- ❑ Environment
 - ✓ e+e- at $E_{CM} = 500$ GeV
 - ✓ brems- and beamstrahlung automatically included

Working scenario: SPS1a'

mSUGRA point:

m_0	70 GeV
$m_{1/2}$	250 GeV
A_0	-300 GeV
$\tan \beta$	10
sign μ	+



Parameter	Value	Decay	BR
m_h	116.0 GeV	$\tilde{\chi}_1^+ \rightarrow \tilde{\tau}_1^+ \nu_\tau$	53.6 %
m_A	424.9 GeV	$\tilde{\chi}_1^+ \rightarrow \tilde{\nu}_\ell \ell^+$	13.3 %
$m_{\tilde{\chi}_1^0}$	97.7 GeV	$\tilde{\chi}_1^+ \rightarrow \tilde{\nu}_\tau \tau^+$	18.5 %
$m_{\tilde{\chi}_2^0}$	183.9 GeV	$\tilde{\chi}_1^+ \rightarrow \tilde{\chi}_1^0 W^+$	1.3 %
$m_{\tilde{\chi}_1^\pm}$	183.7 GeV	$\tilde{\ell}_R^- \rightarrow \tilde{\chi}_1^0 \ell^-$	100.0 %
$m_{\tilde{\chi}_2^\pm}$	415.4 GeV	$\tilde{\ell}_L^- \rightarrow \tilde{\chi}_1^0 \ell^-$	92.5 %
$m_{\tilde{\ell}_R}$	125.3 GeV	$\tilde{\ell}_L^- \rightarrow \tilde{\chi}_1^- \nu_\ell$	4.9 %
$m_{\tilde{\ell}_L}$	189.9 GeV	$\tilde{\ell}_L^- \rightarrow \tilde{\chi}_2^- \ell^-$	2.6 %
$m_{\tilde{\nu}_\ell}$	172.5 GeV	$\tilde{\chi}_2^0 \rightarrow \tilde{\tau}_1^\pm \tau^\mp$	57.8 %
$m_{\tilde{\tau}_1}$	107.9 GeV	$\tilde{\chi}_2^0 \rightarrow \tilde{\nu}_\tau \bar{\nu}_\tau + \text{cc.}$	15.2 %
$m_{\tilde{\tau}_2}$	194.9 GeV	$\tilde{\chi}_2^0 \rightarrow \tilde{\nu}_\ell \bar{\nu}_\ell + \text{cc.}$	11.1 %
$m_{\tilde{\nu}_\tau}$	170.5 GeV	$\tilde{\chi}_2^0 \rightarrow \tilde{\ell}^\pm \ell^\mp$	2.4 %
$\Gamma(\tilde{\chi}_1^\pm)$	77.3 MeV	$\tilde{\tau}_2^- \rightarrow \tilde{\chi}_1^0 \tau^-$	86.8%
$\Gamma(\tilde{\nu}_\ell)$	121.5 MeV	$\tilde{\tau}_2^- \rightarrow \tilde{\chi}_2^0 \tau^-$	4.6%
$\Gamma(\tilde{\nu}_\tau)$	117.4 MeV	$\tilde{\tau}_2^- \rightarrow \tilde{\chi}_1^- \nu_\tau$	8.6%

Signal

Chargino pair production with subsequent leptonic decay

$$e^+ e^- \rightarrow \tilde{\chi}_1^+ \tilde{\chi}_1^-$$
$$\tilde{\chi}_1^+ \tilde{\chi}_1^- \rightarrow \tilde{\nu}_{\ell} \ell^+ \quad \tilde{\nu}_{\ell}^* \ell^-$$

- o $\sigma(\tilde{\chi}_1^+ \tilde{\chi}_1^-) = 173.6 \text{ fb}$ $\tilde{\chi}_1^+ \rightarrow \tilde{\nu}_{\ell} \ell^+ \mathcal{R}($
)= 13%
- o sneutrino decays invisibly
- o final state: two opposite-charge leptons + missing energy

Proper signal

$$e^+ e^- \rightarrow \tilde{\chi}_1^+ \tilde{\chi}_1^- \rightarrow \tilde{\nu}_e^* e^- \tilde{\nu}_{\mu} \mu^+ \rightarrow e^- \mu^+ \bar{\nu}_e \nu_{\mu} \tilde{\chi}_1^0 \tilde{\chi}_1^0$$

Signature: $e^- \mu^+ + E_{miss}$

Irreducible SUSY processes

$$e^+ e^- \rightarrow X \rightarrow e^- \mu^+ \bar{\nu}_e \nu_\mu \tilde{\chi}_1^0 \tilde{\chi}_1^0$$

like

- chargino decays to W+neutralino
- single-resonant diagrams
- non-resonant diagrams
- slepton-pair production
- SM decaying to SUSY,

Proper: 3.06 fb (2.50 fb with -strahlung)

6-fermion: 4.69 fb (3.94 fb with -strahlung)

Signal: proper + irreducible SUSY

SUSY background

- SUSY: different sources - here according to # ♦'s

Process	500 GeV	σ [fb], presel.
SUSY τ Bkgd.	$ee \rightarrow \tau\tau \tilde{\chi}_1^0 \tilde{\chi}_1^0 \rightarrow e\mu \tilde{\chi}_1^0 \tilde{\chi}_1^0 4\nu$	4.107(7)
SUSY $\tau\nu$ Bkgd.	$ee \rightarrow \tau\tau \tilde{\chi}_1^0 \tilde{\chi}_1^0 2\nu \rightarrow e\mu \tilde{\chi}_1^0 \tilde{\chi}_1^0 6\nu$	3.245(10)
SUSY τe Bkgd.	$ee \rightarrow e\tau \bar{\nu}_e \nu_\tau \tilde{\chi}_1^0 \tilde{\chi}_1^0 \rightarrow e\mu \tilde{\chi}_1^0 \tilde{\chi}_1^0 4\nu$	3.691(9)
SUSY $\tau\mu$ Bkgd.	$ee \rightarrow \mu\tau \nu_\mu \bar{\nu}_\tau \tilde{\chi}_1^0 \tilde{\chi}_1^0 \rightarrow e\mu \tilde{\chi}_1^0 \tilde{\chi}_1^0 4\nu$	2.617(10)

Compare to

Signal	$ee \rightarrow e\mu \bar{\nu}_e \nu_\mu \tilde{\chi}_1^0 \tilde{\chi}_1^0$	3.940(8)
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Signal / SUSY Bkgd ~ 1 / 3

Preselection:

5° cut for the final electron

1° cut for particles vanishing in the beam pipe

SM background

- WW, single W, tau pairs

Process	500 GeV	σ [fb], presel.
SM WW Bkgd.	$ee \rightarrow e\mu 2\nu$	152.42(25)
SM $e\tau$ Bkgd.	$ee \rightarrow e\tau 2\nu \rightarrow e\mu 4\nu$	26.522(12)
SM $\mu\tau$ Bkgd.	$ee \rightarrow \mu\tau 2\nu \rightarrow e\mu 4\nu$	15.569(54)
SM ν Bkgd.	$ee \rightarrow e\mu 4\nu$	0.145(1)
SM τ Bkgd.	$ee \rightarrow \tau\tau \rightarrow e\mu 4\nu$	32.679(98)
SM $\tau\nu$ Bkgd.	$ee \rightarrow \tau\tau 2\nu \rightarrow e\mu 6\nu$	3.852(10)

- Photon induced: tau pairs, charm pairs, ...

SM $\gamma \rightarrow \tau$ Bkgd.	$\gamma^* \gamma^* \rightarrow \tau\tau \rightarrow e\mu 2\nu$	21392(70)
SM $\gamma \rightarrow c$ Bkgd.	$\gamma^* \gamma^* \rightarrow c\bar{c} \rightarrow e\mu jj 2\nu$	1089(4)
SM $\gamma \rightarrow W$ Bkgd.	$\gamma^* \gamma^* \rightarrow WW \rightarrow e\mu 2\nu$	1.094(6)
SM $\gamma \rightarrow \tau\nu_\tau$ Bkgd.	$\gamma^* \gamma^* \rightarrow \tau\tau 2\nu \rightarrow e\mu 8\nu$	0.077(1)
SM $\gamma \rightarrow \ell\tau$ Bkgd.	$\gamma^* \gamma^* \rightarrow (e, \mu)\tau 2\nu \rightarrow e\mu 4\nu$	0.404(2)

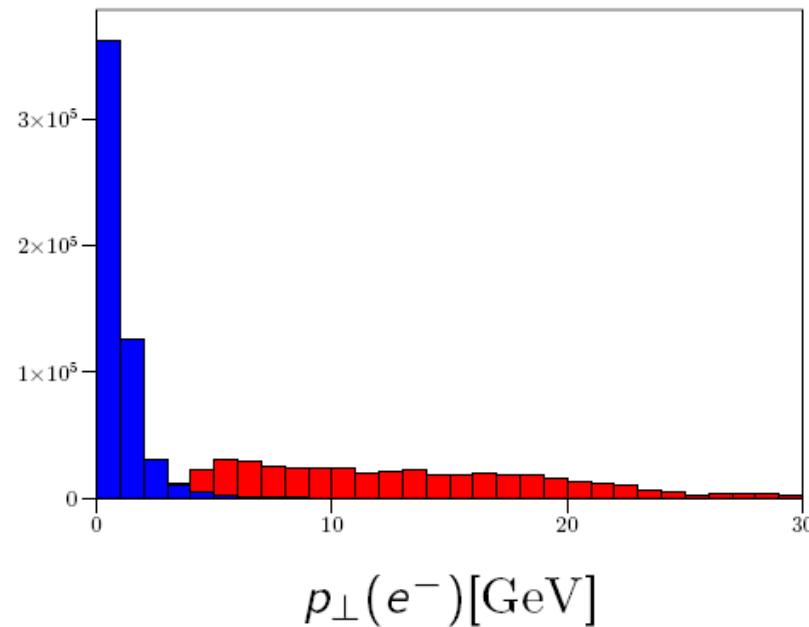


Signal / Bkgd $\sim 1 / 10^5$

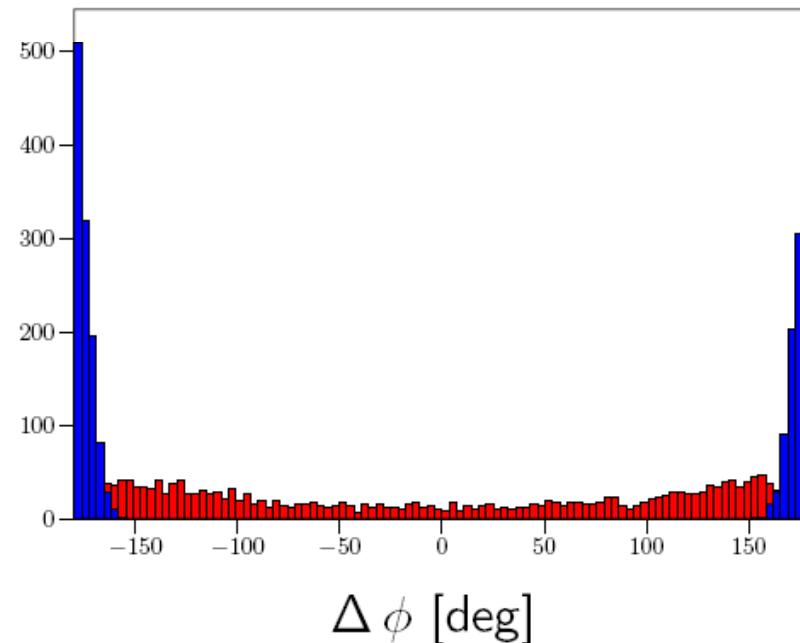
Event selection

- Many different background processes with different kinematics
- Dominant: photon-induced tau-pair: low p_T , back-to-back

Example: p_T and $\Delta\phi$ of signal and background



cut on p_T cuts out 99.58 % of
background, 11 % of signal



renormalized after p_T cuts
cut on $\Delta\phi$ cuts out 99.68 % of
background, 25 % of signal

Suppressing the background

Set of cuts:

$$2\text{GeV} \leq p_{\perp}(e, \mu) \quad 4\text{GeV} \leq p_{\perp}(e) + p_{\perp}(\mu)$$
$$1\text{GeV} \leq E(e, \mu) \leq 40\text{GeV}, -150^\circ \leq \Delta\phi \leq 150^\circ,$$
$$15^\circ \leq \theta(e) \leq 155^\circ, 25^\circ \leq \theta(\mu) \leq 165^\circ$$

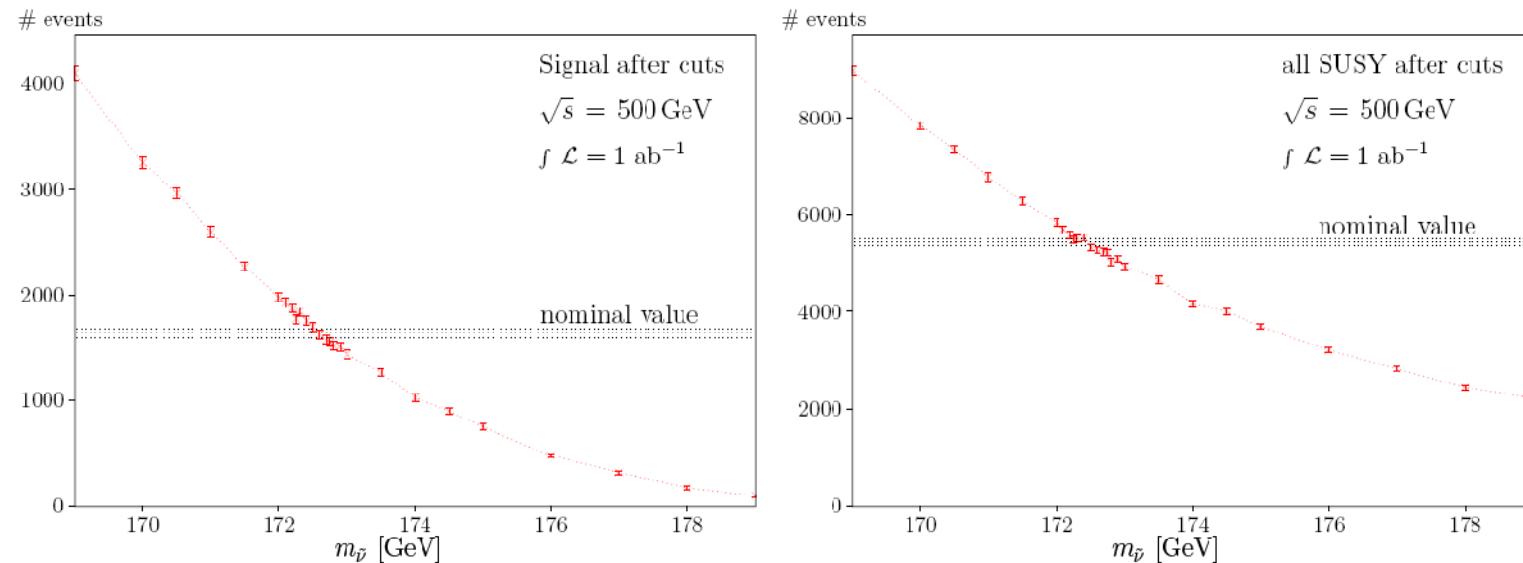
After the cuts:

Process	σ [fb], presel.	σ^{cut} [fb]
Signal	3.940(8)	1.639(3)
SUSY τ Bkgd.	4.107(7)	0.978(2)
SUSY $\tau\nu$ Bkgd.	3.245(10)	0.818(3)
SUSY τe Bkgd.	3.691(9)	1.102(8)
SUSY $\tau\mu$ Bkgd.	2.617(10)	0.966(8)
SM WW Bkgd.	152.42(25)	0.736(2)
SM $e\tau$ Bkgd.	26.522(12)	0.317(1)
SM τ Bkgd.	32.679(98)	< 0.001
SM $\gamma \rightarrow \tau$ Bkgd.	21392(70)	0.273(2)
SM $\gamma \rightarrow c$ Bkgd.	1089(4)	< 0.001

Determining the sneutrino mass: 1

- The dependence on the sneutrino mass enters
 - in the production (t-channel exchange)
 - in the decay $\tilde{\chi}_1^+ \rightarrow \tilde{\nu}_\ell \ell^+$

For the SPS1a' point strong dependence since $\tilde{\chi}_1^\pm, \tilde{\nu}$ close in mass



$$\Rightarrow m_{\tilde{\nu}} \sim 172.50 \pm 0.75 \text{ GeV}$$

Determining the sneutrino mass: 2

Assuming

- a) no beam- and bremsstrahlung
- b) on-shell kinematics

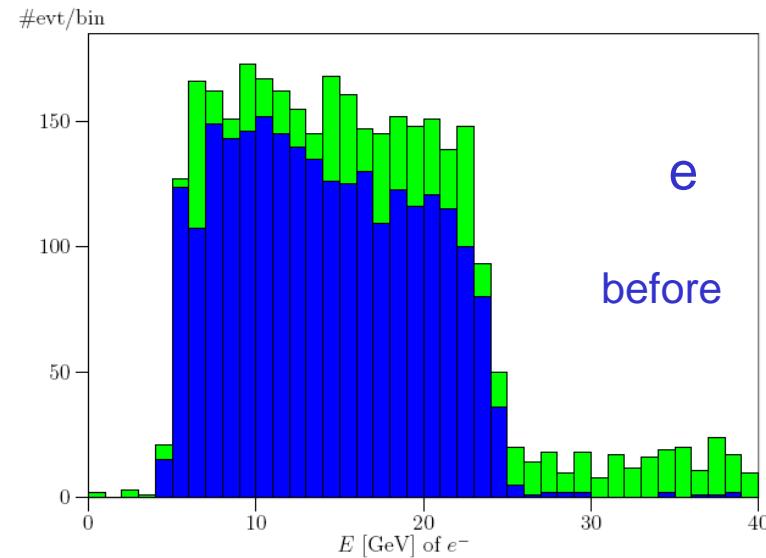
the lepton energy spectrum flat between endpoints E_{\min}, E_{\max}

$$m_{\tilde{\chi}_1^\pm} = \sqrt{s} \frac{\sqrt{E_{\min} E_{\max}}}{E_{\min} + E_{\max}}, \quad m_{\tilde{\nu}_\ell} = m_{\tilde{\chi}_1^\pm} \sqrt{1 - \frac{2(E_{\min} + E_{\max})}{\sqrt{s}}}$$

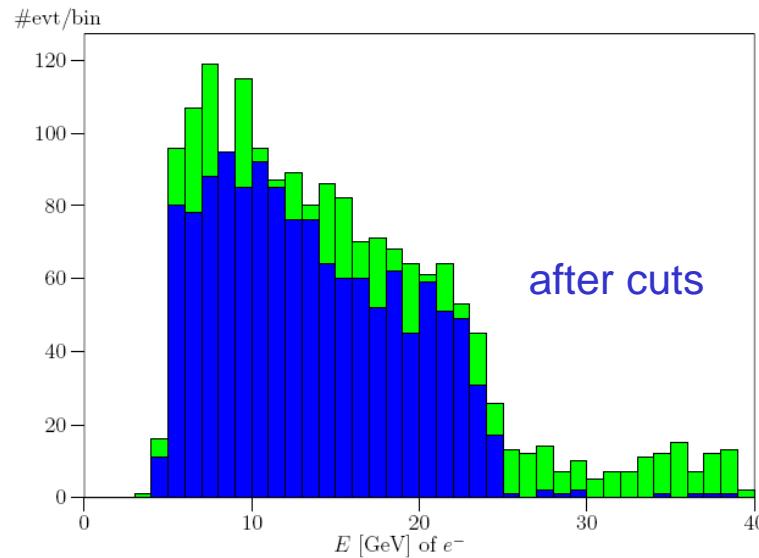
However, spectrum distorted because of

- ❖ chargino polarization effects
- ❖ beam- and bremsstrahlung
- ❖ off-shell and interference effects
- ❖ SUSY background, in particular ♦
- ❖ SM background
- ❖ response of signal to selection cuts

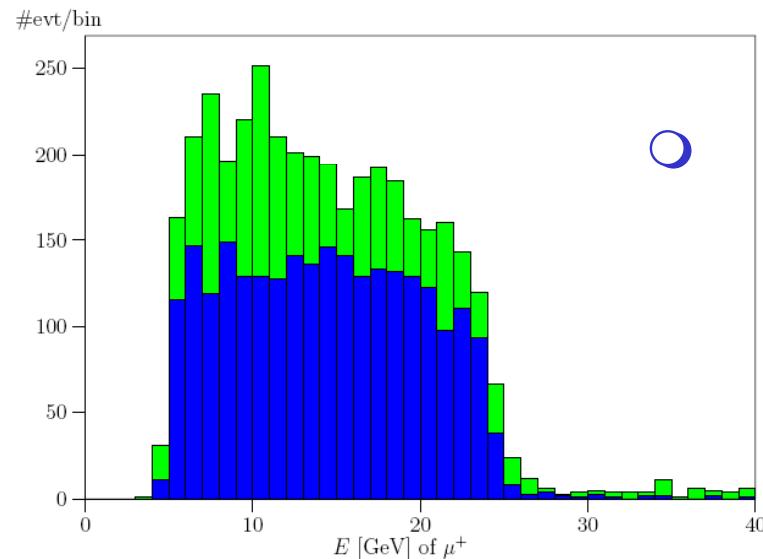
Effect of cuts



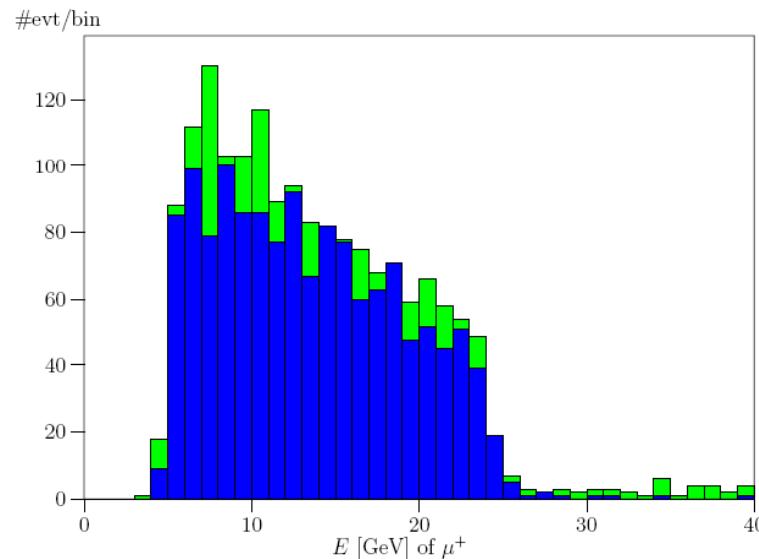
e^-
before



after cuts

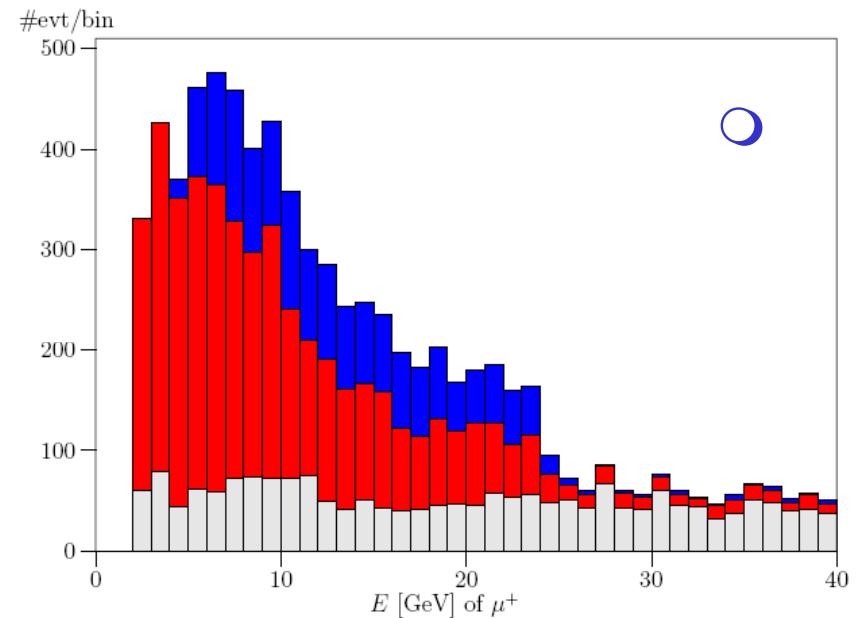
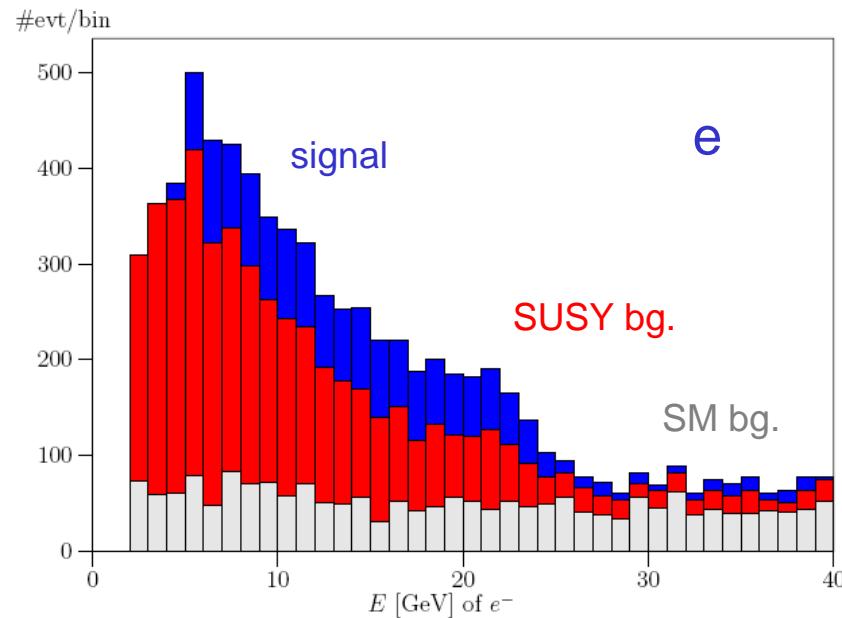


μ^+



blue – proper signal
green – irredu. SUSY

Determining the sneutrino mass: 2



Lower edge difficult to identify

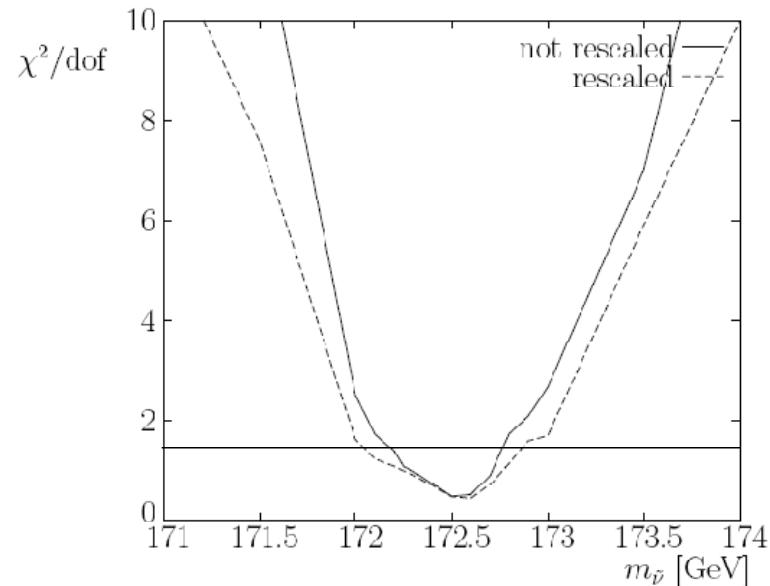
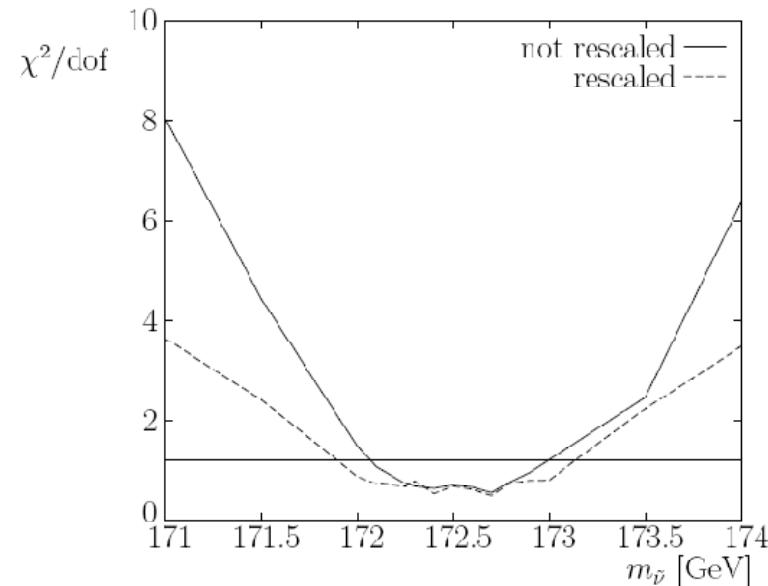
Assuming chargino mass known

$$m_{\tilde{\nu}_\ell}^2 = m_{\tilde{\chi}_1^\pm}^2 \left(1 - \frac{4E_{\max}}{\sqrt{s}} \frac{1}{1+\beta} \right) \quad \rightarrow \quad m_{\tilde{\nu}} = 173.1 \pm 1.3 \text{ GeV}$$

Determining the sneutrino mass: 3

Binned ch² fit: generate MC control samples for varying sneutrino mass

$$\chi^2(m_{\tilde{\nu}}) = \sum_i \frac{(N_i^{\text{tr}} - N_i^{\text{con}}(m_{\tilde{\nu}}))^2}{N_i^{\text{tr}} + N_i^{\text{con}}(m_{\tilde{\nu}})}$$



method →	full range rescaled	full range not rescaled	edge rescaled	edge not rescaled
limit ↓				
lower	171.9	172.1	172.1	172.2
upper	173.1	173.0	172.9	172.8

nominal

$$m_{\tilde{\nu}} = 172.52 \text{ GeV}$$

Summary

- ❖ "Invisible" sneutrino becomes visible in leptonic decays of charginos
- ❖ our analysis included
 - full matrix element for $2 \rightarrow n$ processes ($n \leq 10$)
 - off-shell and interference
 - all SUSY and SM background, including gamma-induced
- ❖ mass measurement possible but not easy
- ❖ three methods for sneutrino mass from leptonic decays of charginos
 - production cross section – good control of normalisation necessary
 - lepton energy spectra – strong effect of kinematic cuts
 - chi2 fit to templates with varying sneutrino mass

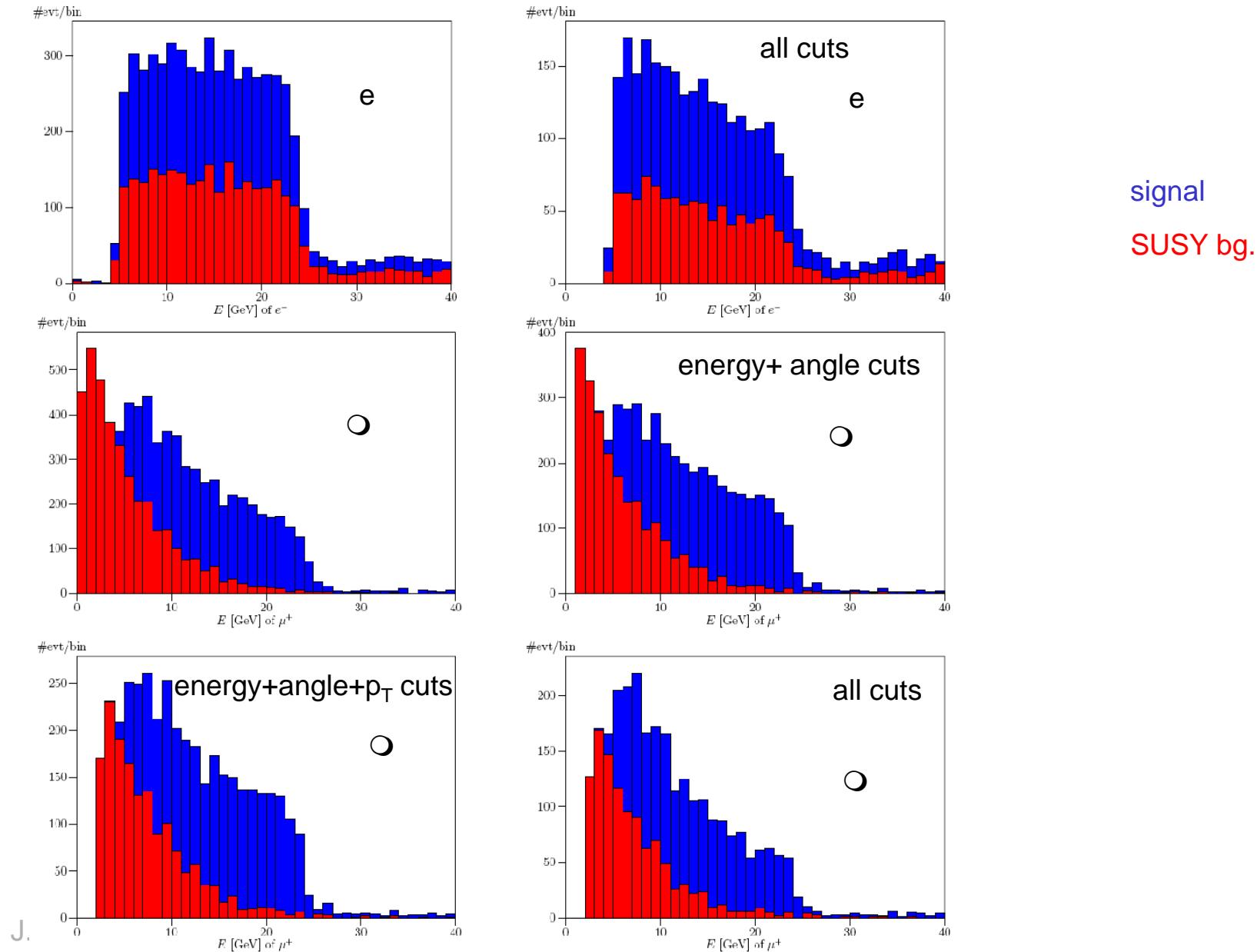
Outlook: NLO production implemented into WHIZARD (Kilian, Reuter, Robens)
NLO decays calculated (Roliecki, Fujimoto ea)



Full NLO MC analysis feasible in future



Proper vs irred. SUSY, 800 GeV



Ecm=800 GeV

