

Trilinear couplings in the 2HDM

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based on work with P.N. Pandita and L. Selbuz
arXiv0802.0060 (PRD)

Scenario/Summary

- Assume rich Higgs sector is revealed at the LHC
- It may be possible to measure some trilinear couplings at the linear collider (“whoever she may be”)
- The 2HDM has a rich menu of trilinear couplings
- They are considerably modified by CP violating and loop effects

Define model: 2HDM (II)

Potential:

$$V = \frac{\lambda_1}{2}(\Phi_1^\dagger\Phi_1)^2 + \frac{\lambda_2}{2}(\Phi_2^\dagger\Phi_2)^2 + \lambda_3(\Phi_1^\dagger\Phi_1)(\Phi_2^\dagger\Phi_2) + \lambda_4(\Phi_1^\dagger\Phi_2)(\Phi_2^\dagger\Phi_1) \\ + \frac{1}{2} \left[\lambda_5(\Phi_1^\dagger\Phi_2)^2 + \text{h.c.} \right] + \left\{ \left[\lambda_6(\Phi_1^\dagger\Phi_1) + \lambda_7(\Phi_2^\dagger\Phi_2) \right] (\Phi_1^\dagger\Phi_2) + \text{h.c.} \right\} \\ - \frac{1}{2} \left\{ m_{11}^2(\Phi_1^\dagger\Phi_1) + \left[m_{12}^2(\Phi_1^\dagger\Phi_2) + \text{h.c.} \right] + m_{22}^2(\Phi_2^\dagger\Phi_2) \right\}$$

Allow CP violation:

$\lambda_5, \lambda_6, \lambda_7, m_{12}^2$ may be **complex**

Neutral sector: 3×3 mixing matrix $\alpha = (\alpha_1, \alpha_2, \alpha_3)$

$$-\frac{\pi}{2} < \alpha_i \leq \frac{\pi}{2}, \quad i = 1, 2, 3$$

Often, take: $\lambda_6 = \lambda_7 = 0.$

Parameters:

$$\lambda_1, \lambda_2, \lambda_3, \lambda_4, \lambda_5, \mu^2, \tan \beta$$

or:

$$M_1 \leq M_2 \leq M_3, M_{H^\pm}, \tan \beta, \mu^2, \alpha_1, \alpha_2, \alpha_3$$

complex

Input parameters:

$$M_1 \leq M_2, M_{H^\pm}, \tan \beta, \mu^2, (\alpha_1, \alpha_2, \alpha_3)$$

Calculate:

$$M_3, \lambda_1, \lambda_2, \lambda_3, \lambda_4, \lambda_5$$

Conditions:

$$M_2 \leq M_3$$

$$V(\Phi_1, \Phi_2) > 0 \quad \text{asymptotically}$$

$$\Phi_i = \begin{pmatrix} \varphi_i^+ \\ \frac{1}{\sqrt{2}}(v_i + \eta_i + i\chi_i) \end{pmatrix}, \quad i = 1, 2.$$

Weak basis: η_1, η_2, η_3

$$\eta_3 = -\sin \beta \chi_1 + \cos \beta \chi_2. \quad \text{CP odd}$$

Mass basis:

$$H_i = R_{ij} \eta_j$$

$$\begin{aligned} R = R_3 R_2 R_1 &= \begin{pmatrix} 1 & 0 & 0 \\ 0 & \cos \alpha_3 & \sin \alpha_3 \\ 0 & -\sin \alpha_3 & \cos \alpha_3 \end{pmatrix} \begin{pmatrix} \cos \alpha_2 & 0 & \sin \alpha_2 \\ 0 & 1 & 0 \\ -\sin \alpha_2 & 0 & \cos \alpha_2 \end{pmatrix} \begin{pmatrix} \cos \alpha_1 & \sin \alpha_1 & 0 \\ -\sin \alpha_1 & \cos \alpha_1 & 0 \\ 0 & 0 & 1 \end{pmatrix} \\ &= \begin{pmatrix} c_1 c_2 & s_1 c_2 & s_2 \\ -(c_1 s_2 s_3 + s_1 c_3) & c_1 c_3 - s_1 s_2 s_3 & c_2 s_3 \\ -c_1 s_2 c_3 + s_1 s_3 & -(c_1 s_3 + s_1 s_2 c_3) & c_2 c_3 \end{pmatrix}, \end{aligned}$$

Approach A

$$\lambda_6 = \lambda_7 = 0$$

Input:

$$M_1 \leq M_2, M_{H^\pm}, \tan \beta, \mu^2, (\alpha_1, \alpha_2, \alpha_3)$$

Calculate:

$$M_3, \lambda_1, \lambda_2, \lambda_3, \lambda_4, \lambda_5$$

Approach B

Input: As above, plus:

$$M_3, \text{Im } \lambda_5, \text{Re } \lambda_6, \text{Re } \lambda_7$$

Calculate: As above, minus: $M_3, \text{Im } \lambda_5$

plus: $\text{Im } \lambda_6, \text{Im } \lambda_7$

Yukawa couplings

$$H_j b \bar{b} : \quad \frac{1}{\cos \beta} [R_{j1} - i \gamma_5 \sin \beta R_{j3}]$$

$$H_j t \bar{t} : \quad \frac{1}{\sin \beta} [R_{j2} - i \gamma_5 \cos \beta R_{j3}]$$

$$H^+ b \bar{t} : \quad \frac{ig}{2\sqrt{2}m_W} [m_b(1 + \gamma_5) \tan \beta + m_t(1 - \gamma_5) \cot \beta]$$

$$H^- t \bar{b} : \quad \frac{ig}{2\sqrt{2}m_W} [m_b(1 - \gamma_5) \tan \beta + m_t(1 + \gamma_5) \cot \beta]$$



Important at low $\tan \beta$

Constraints:

- Positivity
- Perturbative unitarity (Higgs sector)
- Experimental constraints

Experimental constraints:

Independent
of neutral sector

- $B \rightarrow X_s \Upsilon$

excludes low M_{H^\pm}

- $B \rightarrow \bar{B}$ oscillations

excludes low $\tan\beta$

- $B \rightarrow TV$

excludes high $\tan\beta$, low M_{H^\pm}

Depend on
neutral sector

- $\Gamma_Z \rightarrow b\bar{b}$

excludes low $\tan\beta$

- LEP2 non-discovery

light H decouples

- $\Delta\rho$

spectrum compact

- $(g-2)_\mu$

no simple characteristics

Trilinear couplings

$$\lambda_{ijk} = \frac{-i \partial^3 V}{\partial H_i \partial H_j \partial H_k}$$

Differentiate via weak fields

$$\lambda_{ijk} = \sum_{m \leq n \leq o=1,2,3}^* R_{i'm} R_{j'n} R_{k'o} \frac{-i \partial^3 V}{\partial \eta_m \partial \eta_n \partial \eta_o}$$

$\{i', j', k'\} = \text{permutation}\{i, j, k\}$

Reference, SM:

$$\lambda_{HHH}^{\text{SM}} = \frac{3M_H^2}{v}$$

CP conserving limit:

6 couplings involving neutral Higgs bosons:

$$\lambda_{hhh}, \lambda_{hhH}, \lambda_{hHH}, \lambda_{HHH}, \lambda_{hAA}, \lambda_{HAA}$$

CP non-conservation: 10 couplings

111, 112, 113, 122, 123, 133, 222, 223, 233, 333

Focus on two involving the lightest one, H_1



Study ratios wrt SM

$$\xi_1 \equiv \frac{\lambda_{111}}{\lambda_{HHH}^{\text{SM}}}$$

$H_1 H_1 H_1$

$$\xi_2 \equiv \frac{\lambda_{112}}{\lambda_{HHH}^{\text{SM}}}$$

$H_1 H_1 H_2$

average over some parameters $\alpha = (\alpha_1, \alpha_2, \alpha_3)$

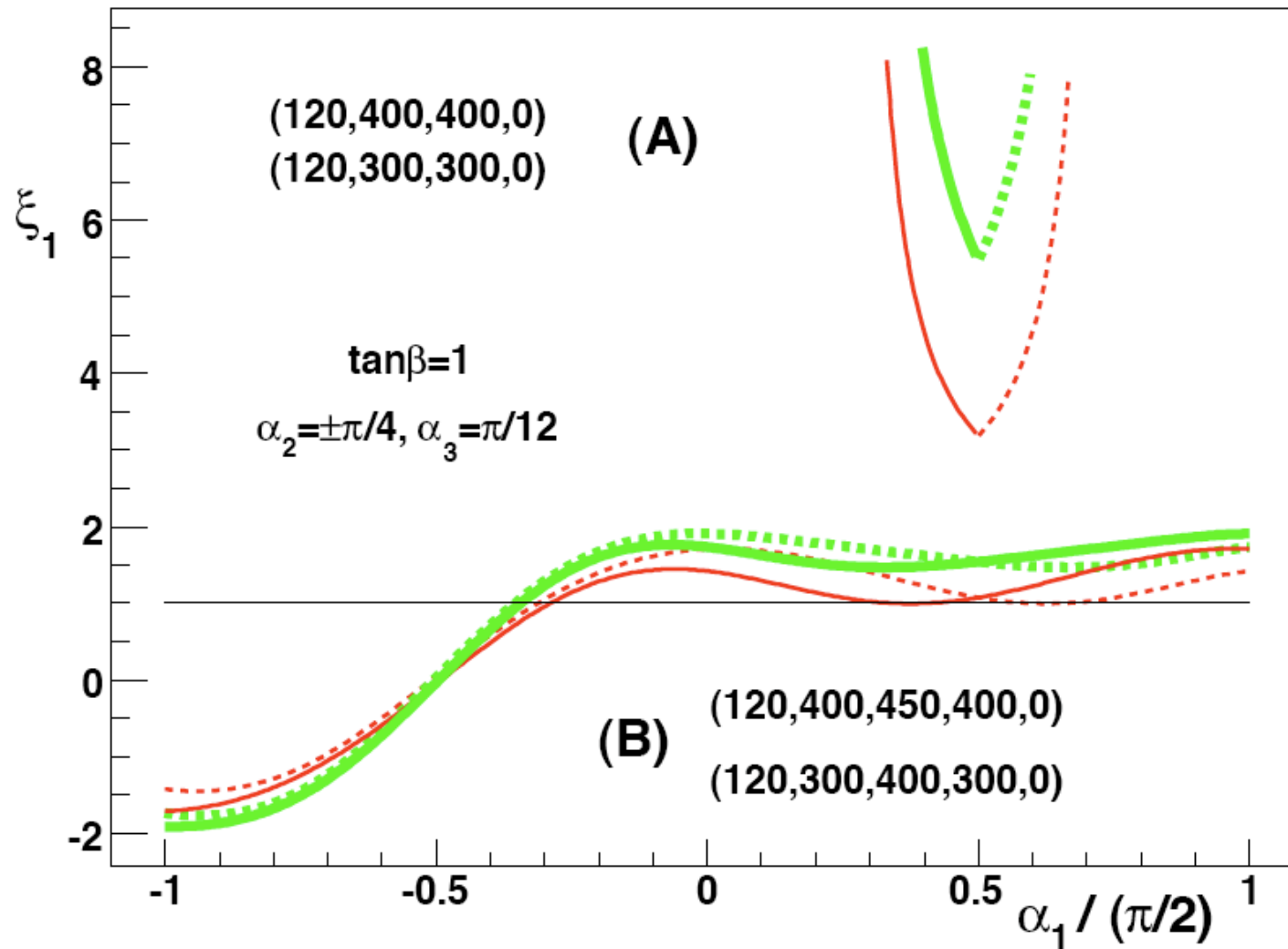
$$\langle \xi_1 \rangle = \frac{\langle \lambda_{111} \rangle}{\lambda_{HHH}^{\text{SM}}}$$

$$\langle \xi_2 \rangle = \frac{\langle \lambda_{112} \rangle}{\lambda_{HHH}^{\text{SM}}}$$

Reference mass: M_1

$\mu=0$

TREE LEVEL



Note: coupling may pass through zero

Limits of no CP violation

$$H_1 \text{ is odd: } \alpha_2 = \pm\pi/2,$$

$$H_2 \text{ is odd: } \alpha_3 = \pm\pi/2,$$

→ $H_3 \text{ is odd: } \alpha_2 = 0, \quad \alpha_3 = 0.$

Limit of “little” CP violation:

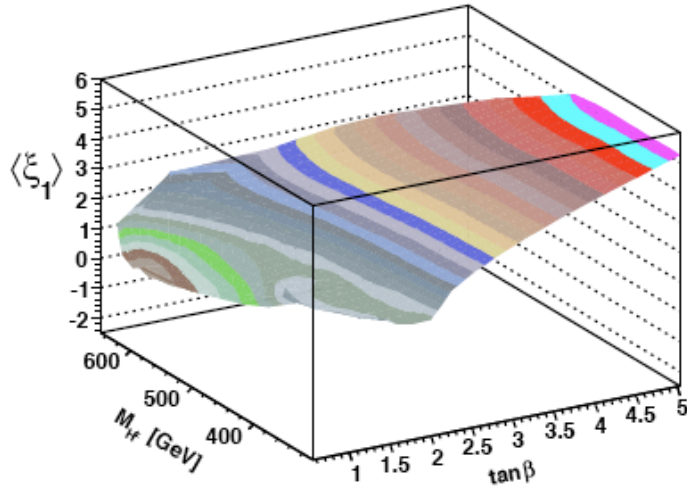
$$|\alpha_2| \leq \alpha_0, \quad |\alpha_3| \leq \alpha_0, \quad \alpha_0 = 0.05 \times \pi/2$$

$$M_1 = 120 \text{ GeV},$$

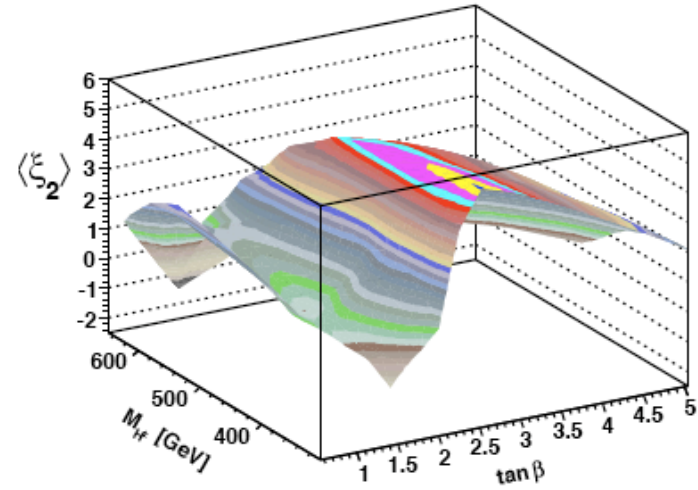
$$M_2 = 300 \text{ GeV}$$

“Little” CP violation

Tree level, $\mu=0$

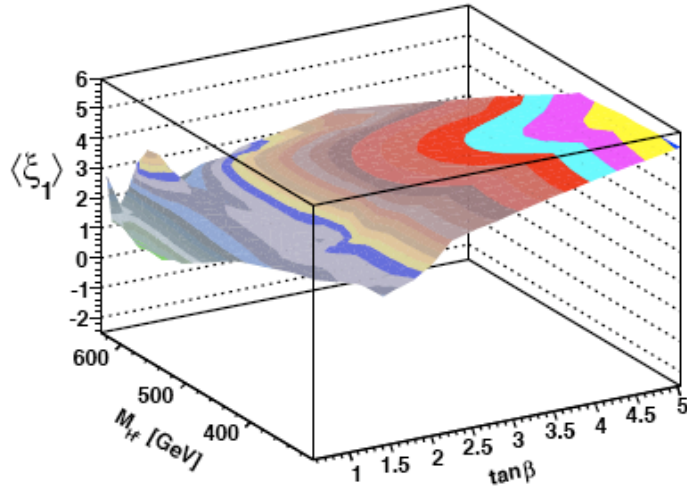


Tree level, $\mu=0$

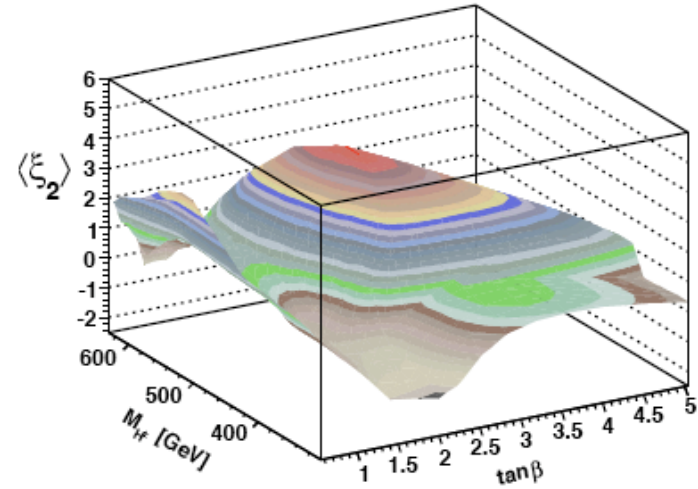


CP violation

Tree level, $\mu=0$

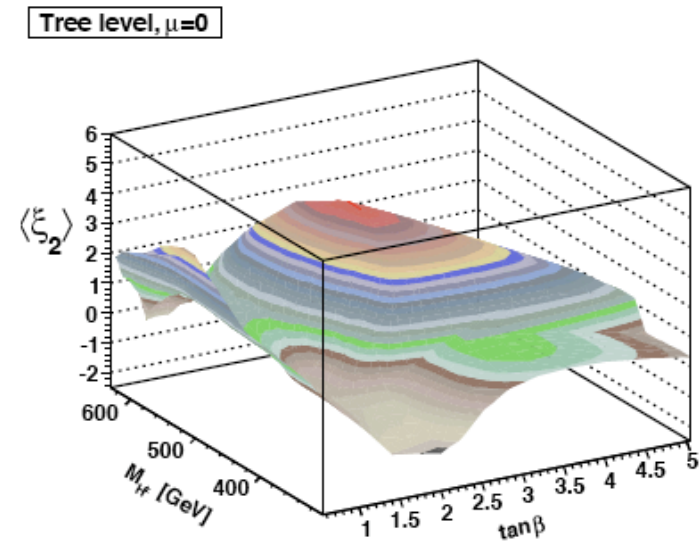
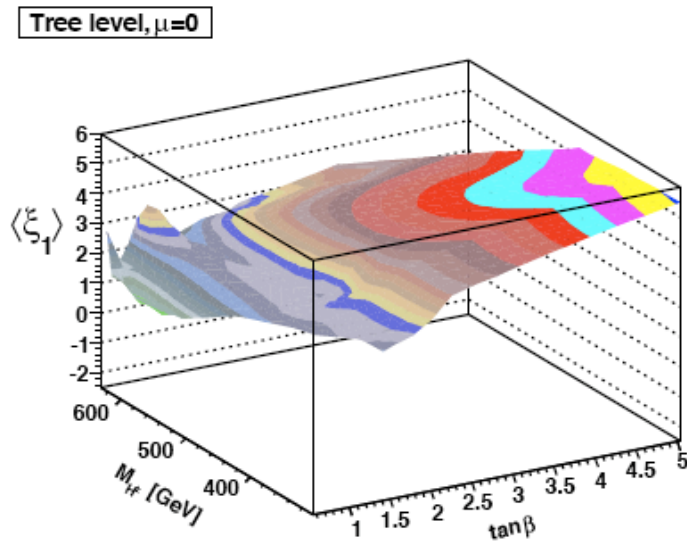


Tree level, $\mu=0$

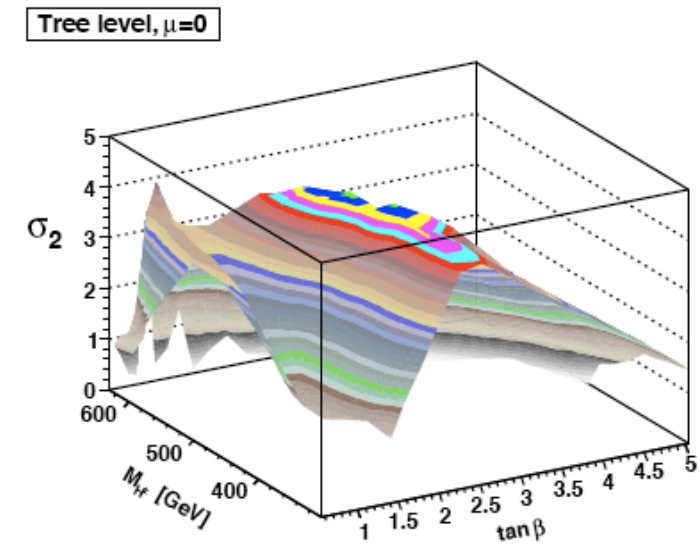
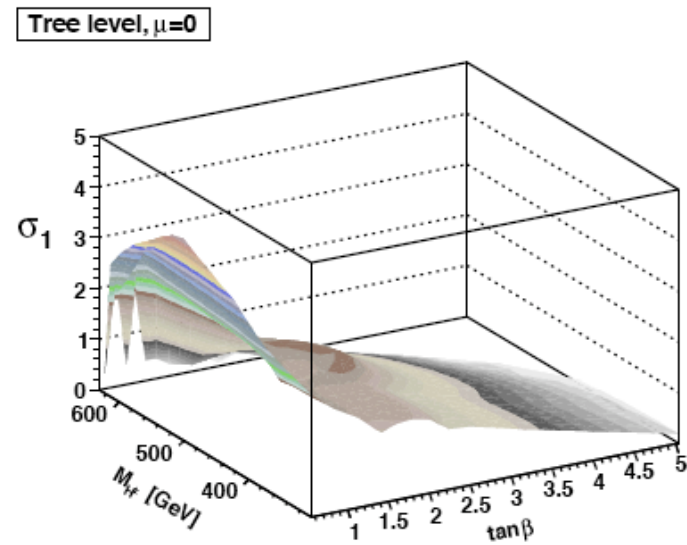


$$M_1 = 120 \text{ GeV}, \quad M_2 = 300 \text{ GeV}$$

Averages

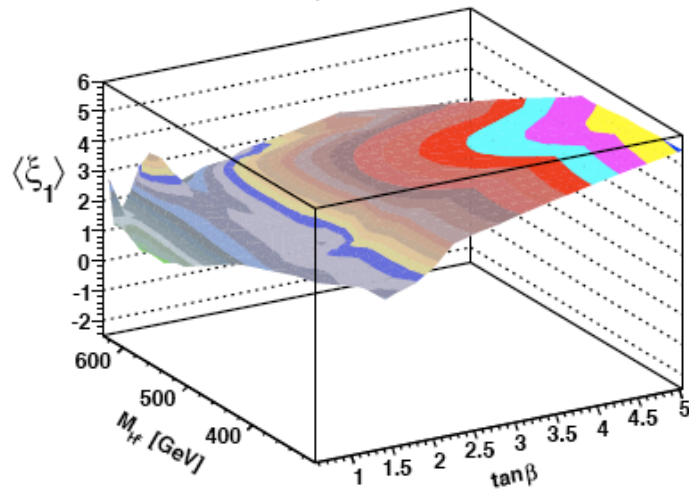


Variation

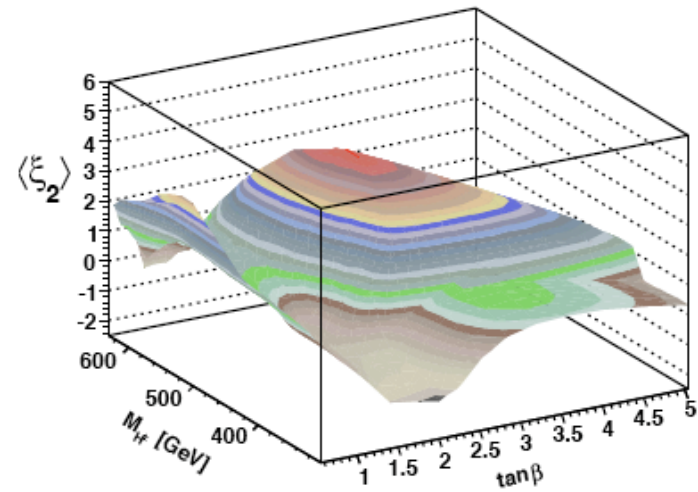


Approach A

$$M_1 = 120 \text{ GeV}, \quad M_2 = 300 \text{ GeV}$$

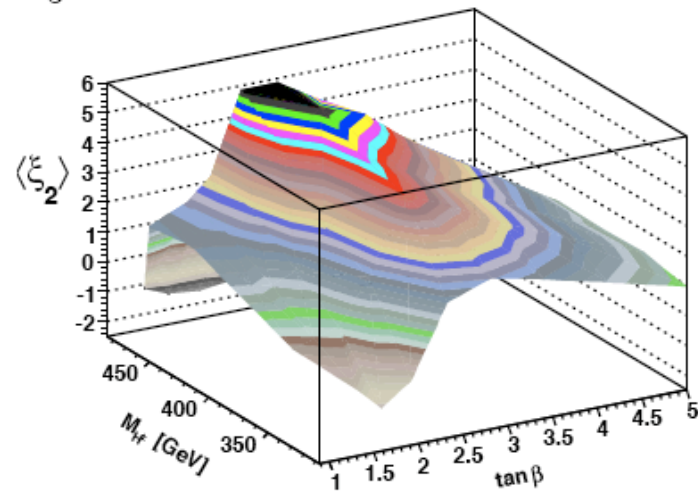
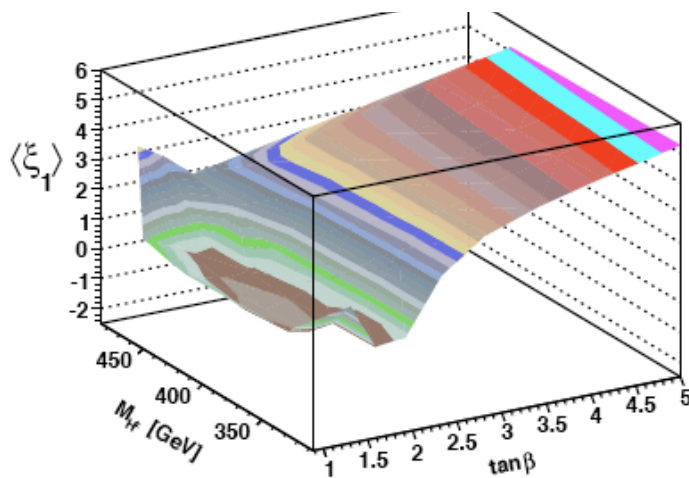


Tree level, $\mu=0$



Approach B

$$M_1 = 120 \text{ GeV}, \quad M_2 = 300 \text{ GeV}, \quad M_3 = 400 \text{ GeV}$$

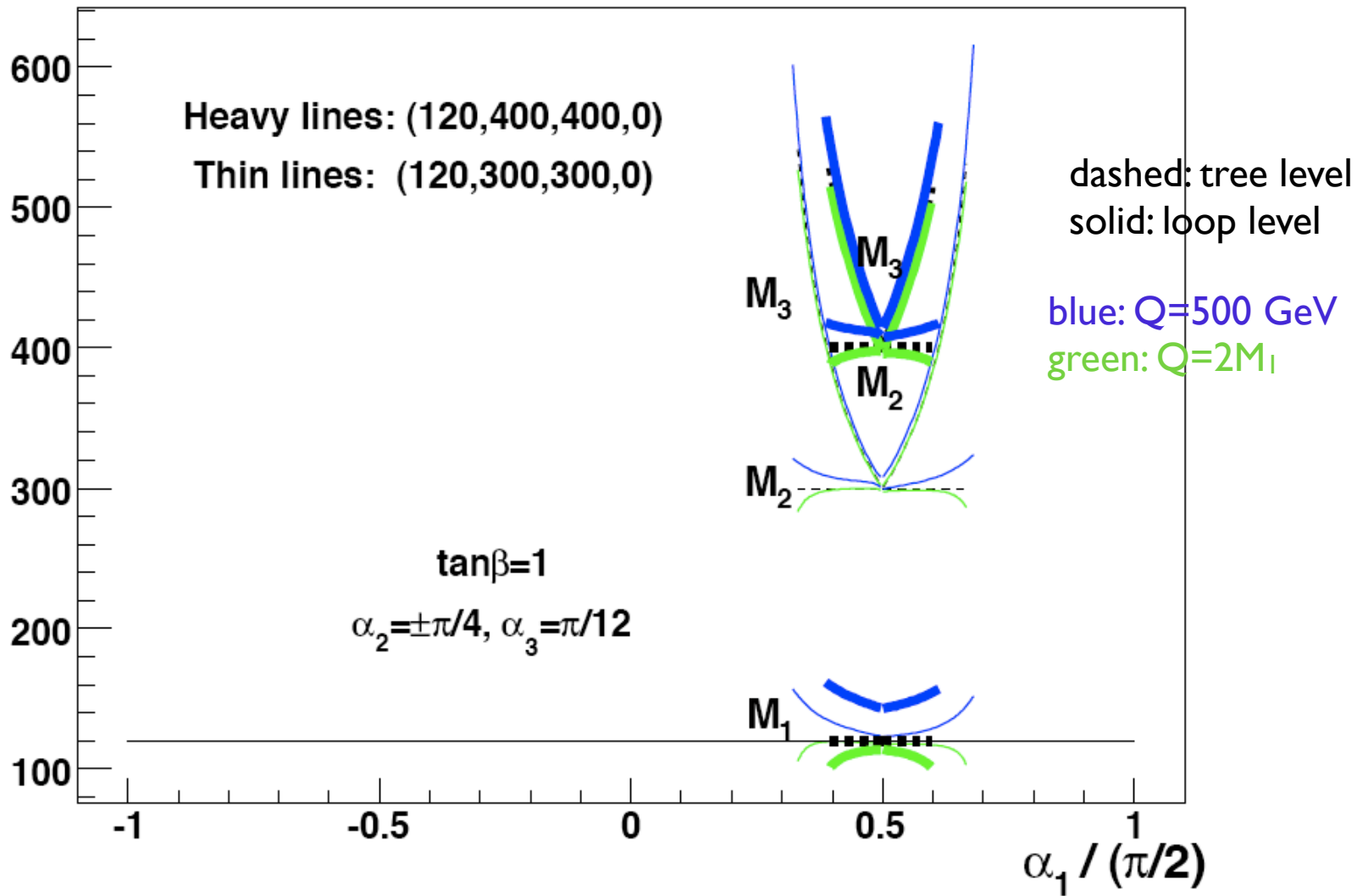


Loop corrections, Coleman-Weinberg:

$$\Delta V = \frac{1}{64\pi^2} \left[\sum_{\text{bosons}} M^4 \left(\log \frac{M^2}{Q^2} - \frac{3}{2} \right) - \sum_{\text{fermions}} M^4 \left(\log \frac{M^2}{Q^2} - \frac{3}{2} \right) \right],$$

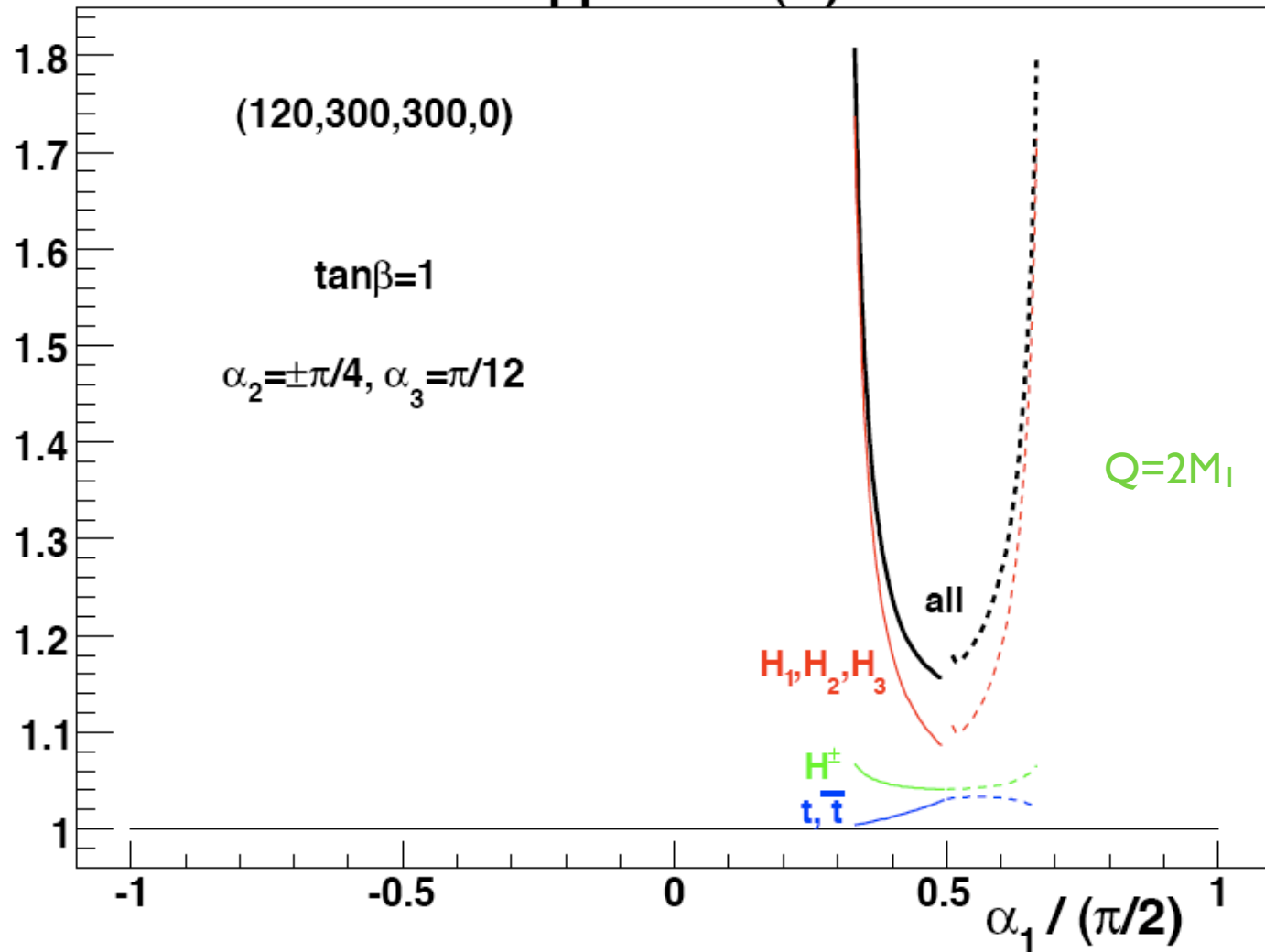
First, quick look at mass corrections...

Approach (A)

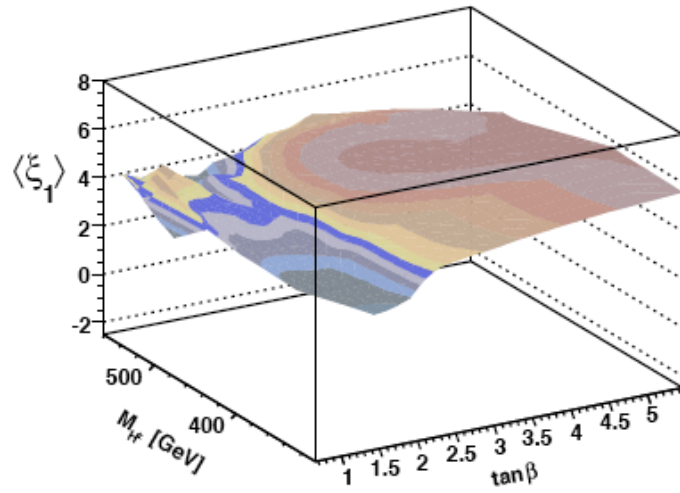


Ratio: loop/tree

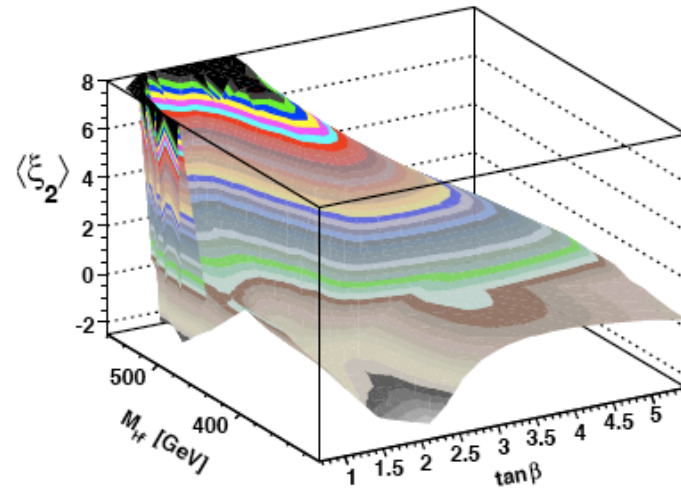
Approach (A)



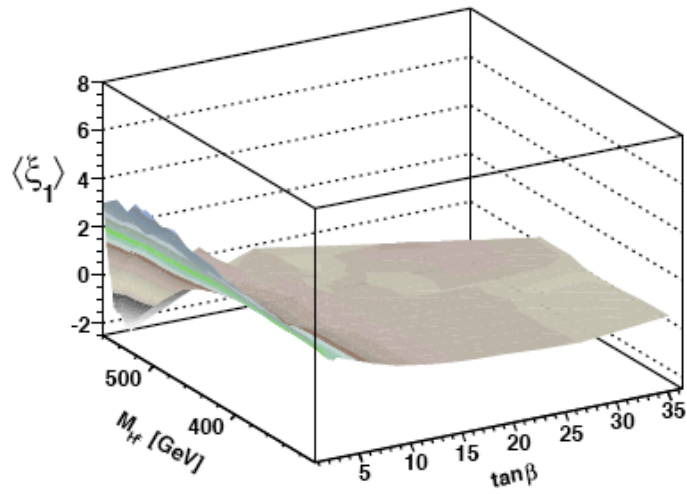
Loop level, $\mu=0$



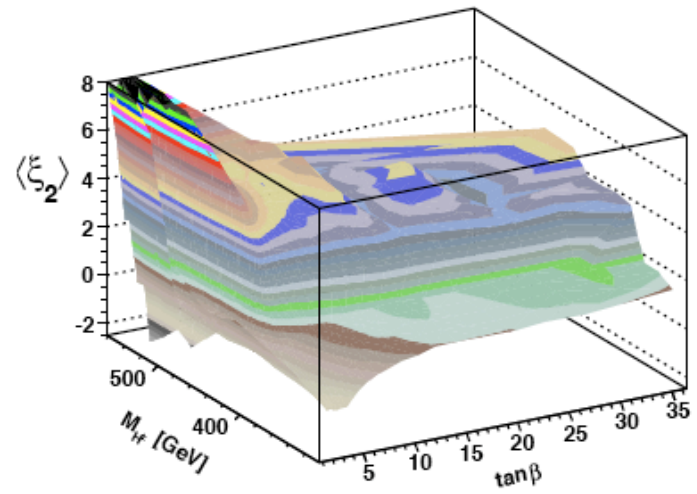
Loop level, $\mu=0$



Loop level, $\mu=200$ GeV



Loop level, $\mu=200$ GeV



Decoupling?

Definition from (CP-conserving) MSSM:

- W. Hollik and S. Penaranda, EPJC 23 (2002) 163
- A. Dobado, M.J. Herrero + above, PRD 66 (2002) 095016

Trilinear coupling can be expressed **in terms of masses**, as in the SM at tree level, but masses are loop corrected

Study:

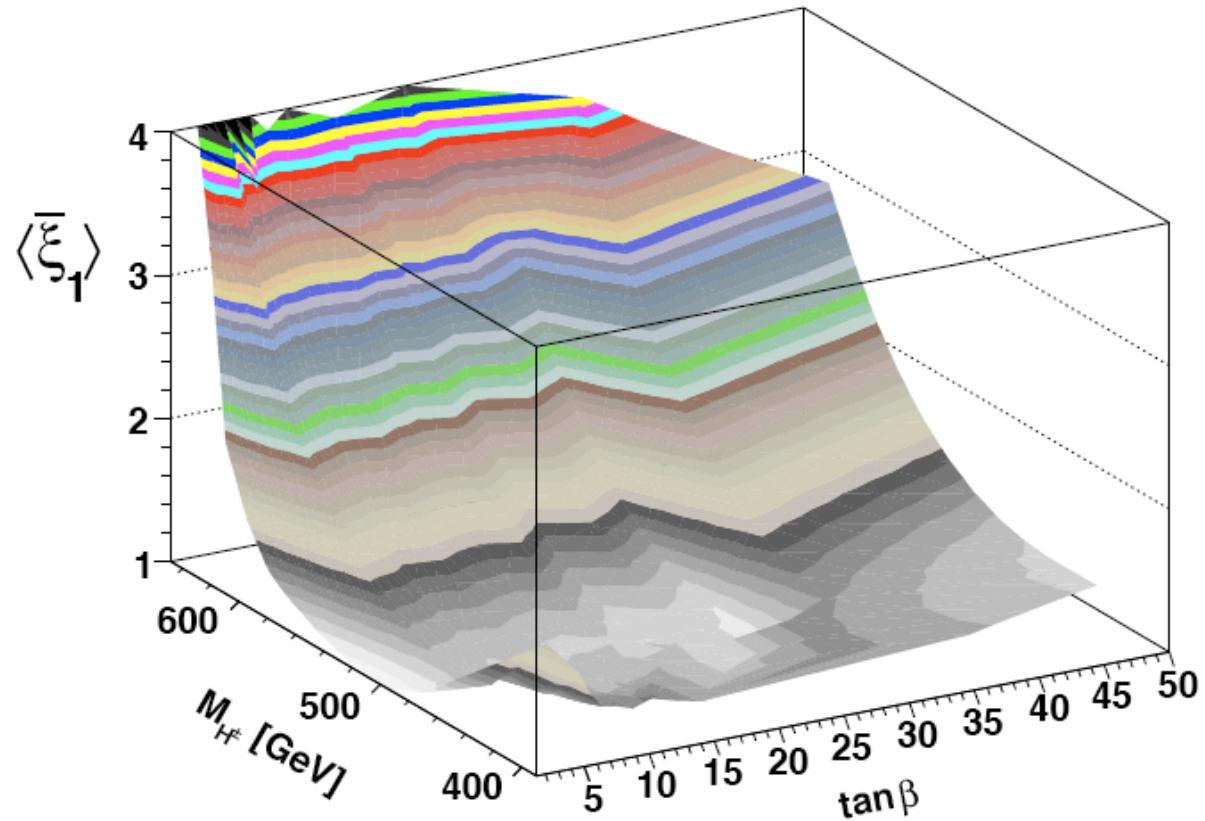
$$\langle \bar{\xi}_1 \rangle = \frac{\langle \lambda_{111}^{\text{full}} \rangle}{\langle \lambda_{111}^{\text{SM}} \rangle}$$

SM-like limit

SM-like limit:

- $\lambda_6 = \lambda_7 = 0$
- $|\alpha_2| \leq \alpha_0, \quad |\alpha_3| \leq \alpha_0, \quad \alpha_0 = 0.025 \times \pi/2$
“minimal CP violation”
- $\lambda_{111}^{\text{SM}}$ includes only loop corrections due to $t\bar{t}$ and H_1 , as would be the case in the SM.
- $\lambda_{111}^{\text{full}}$ includes all one-loop corrections to the Higgs coupling in the two Higgs doublet model, i.e., also those due to H_2, H_3 and H^\pm .

SM limit. Loop level, $\mu=500$ GeV



$$\langle \bar{\xi}_1 \rangle \simeq 1$$

Decoupling breaks down for high values of M_{H^\pm}

Summary

- Trilinear couplings are in the 2HDM typically larger than in the SM
- They vary a lot as one scans across parameter space, even for fixed masses M_1 and M_2
- Decoupling in limited region of parameter space