

Dark Matter in the $U(1)$ -extended MSSM

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Based on work with Jan Kalinowski and Steve King

- 1 What's wrong with the MSSM
 - μ - the black sheep of the MSSM
- 2 Solving the μ problem
- 3 Phenomenology of the USSM
- 4 Conclusions

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But all is not well

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We need a rationale for μ to be of the SUSY breaking scale.

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$\langle S \rangle$ is set by the running of soft SUSY breaking parameters

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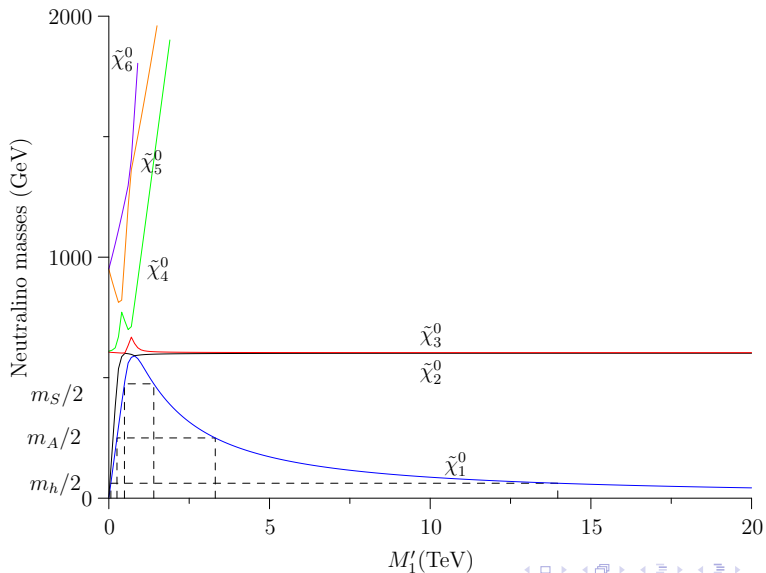
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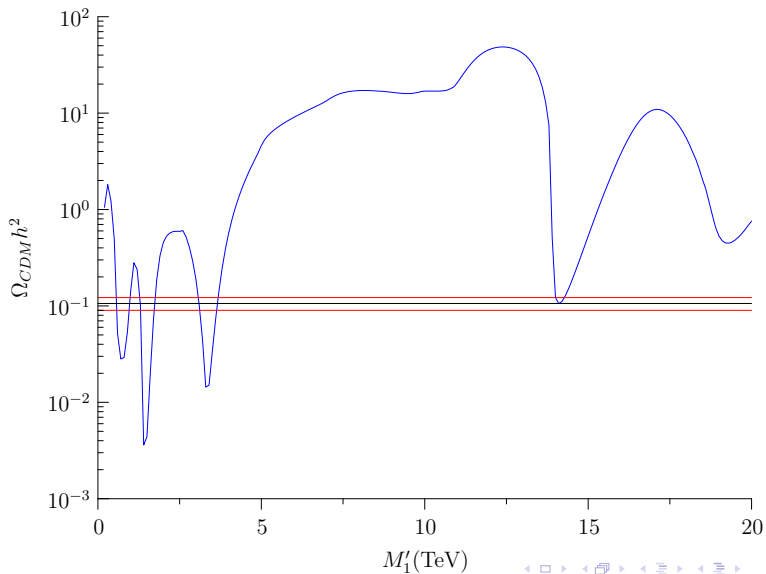
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 - Never have a dominantly bino' LSP

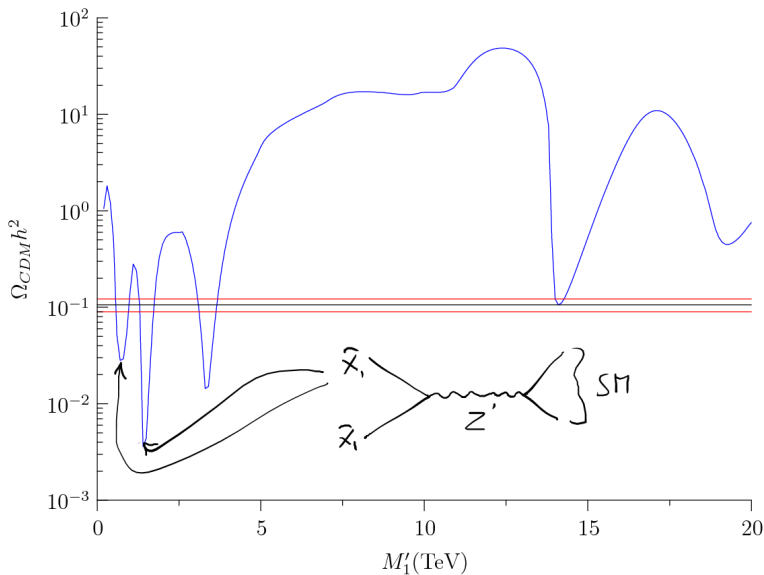
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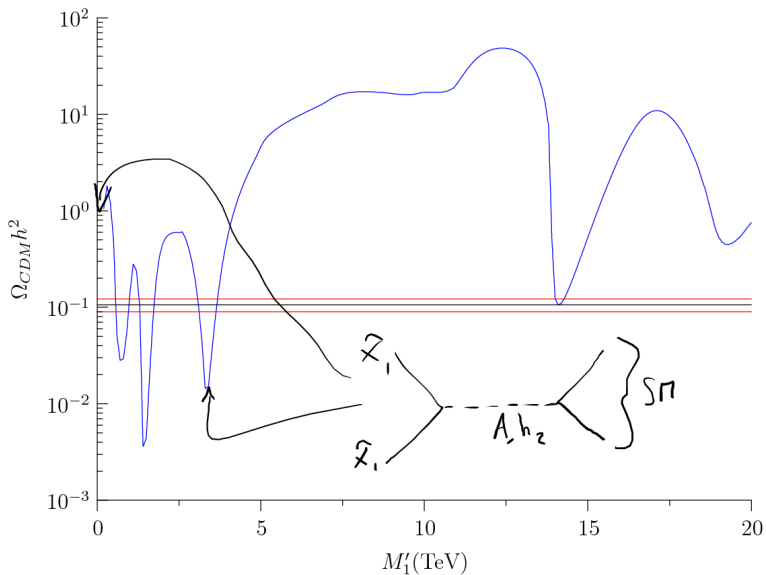
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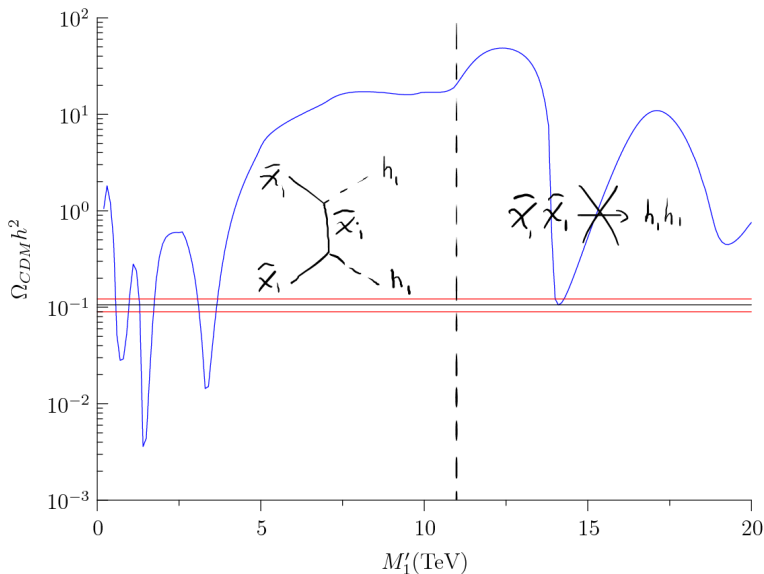
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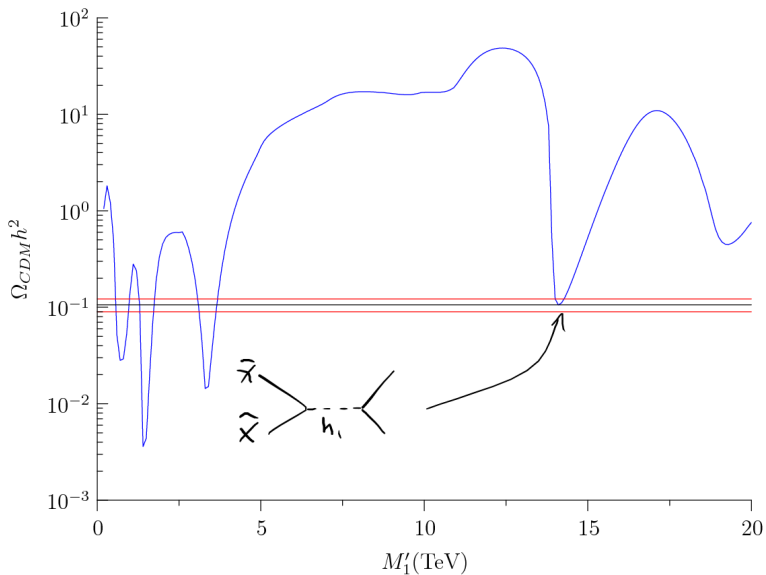
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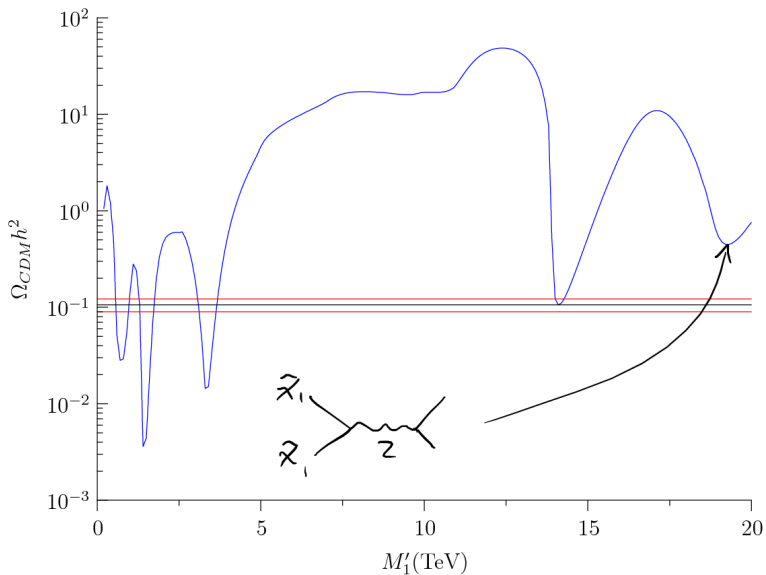
$M_1 = M'_1$: Relic Density

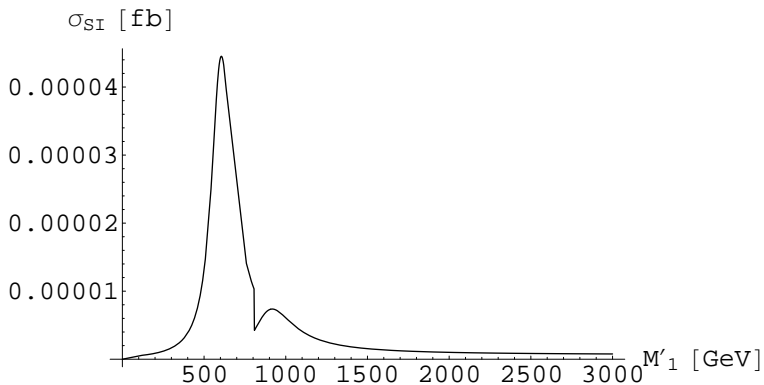


$M_1 = M'_1$: Relic Density



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$M_1 = M'_1$: Direct Detection

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- This, along with direct detection results, will also allow us to differentiate them on the basis of their prediction of the relic density.