

Generators & LoopVerein (w/a little NNLO top)

Thorsten Ohl

Institute for Theoretical Physics and Astrophysics, University of Würzburg

ILC/ECFA Workshop 2008
Warsaw, June 9-12, 2008

CARLOMAT, a program for automatic computation of multiparticle cross sections

- ▶ Plan: provide a more efficient alternative for generating event samples for arbitrary $2 \rightarrow 8, \dots, 12$ processes in the SM (incl. QCD)



carlomat

- a program written in Fortran 90/95
- generates the matrix element for a user specified process
- generates phase space parametrizations, which are later used for the multichannel Monte Carlo integration of the lowest order cross sections and event generation
- takes into account both the electroweak and QCD lowest order contributions
- fermion masses are not neglected
- the maximum number of external particles is 12
- only the Standard Model is implemented at the moment

- ▶ has been tested successfully against older programs for various 2 → 6 processes:



Top quark pair production in e^+e^- annihilation

Final state	\sqrt{s}	carlomat	AMAGIC++	HELAC
$b\bar{b}u\bar{u}d\bar{d}$	360	32.98(11)	32.90(15)	33.05(14)
	500	50.31(19)	49.74(21)	50.20(13)
$b\bar{b}u\bar{d}e^-\bar{\nu}_e$	360	11.448(26)	11.460(36)	11.488(15)
	500	17.424(56)	17.486(66)	17.492(41)
$b\bar{b}e^+\nu_e\mu^-\bar{\nu}_\mu$	360	3.843(5)	3.847(15)	3.848(7)
	500	5.856(11)	5.865(24)	5.868(10)
$b\bar{b}\mu^+\nu_\mu\mu^-\bar{\nu}_\mu$	360	3.837(5)	3.808(16)	3.861(19)
	500	5.834(10)	5.840(30)	5.839(12)

\sqrt{s} in GeV, cross sections in fb.

[T. Gleisberg, et al.]
carlomat - p. 18

PHANTOM: a Monte Carlo event generator for six parton final states at high energy colliders

- ▶ a **dedicated** event generator for **2** → **6** processes (SM and QCD) at **both** ILC and LHC, building on the PHACT expertise at Torino:

PHANTOM 1.0



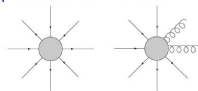
Ballestrero, Belhouari, G.B., Kashkan, Maina

arXiv:0801.3359 [hep-ph]

Event generator dedicated to six-parton physics at pp , $p\bar{p}$ and e^+e^- colliders

- Exact tree-level matrix elements at $\mathcal{O}(\alpha_{EM}^6) + \mathcal{O}(\alpha_{EM}^4 \alpha_S^2)$
- Full coverage of Standard Model processes at fixed order

$$\begin{array}{l} pp \\ p\bar{p} \\ e^+e^- \end{array} \longrightarrow \begin{cases} 6f \\ 5f + g \\ 4f + 2g \end{cases}$$



Holds the **signal** of

- Higgs production via Vector Boson Fusion $ffH \rightarrow ffVV \dots$
- Vector Boson Scattering $WW \rightarrow WW, WZ \rightarrow WZ \dots$
- triple gauge boson production
- $t\bar{t}$ production
- triple/quadruple-vertex EW interactions

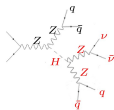
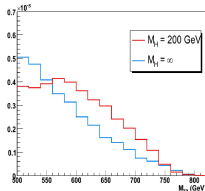
together with all **EW+QCD irreducible background** at fixed order

- e.g.: testing cuts that enhance the **VV scattering signal** over Higgsstrahlung for EWSB studies requires inclusion of all **irreducible backgrounds**:

Early on-set of EWSB effects is partially masked in the ZZ channel by residual non-scattering contributions. What's going on?

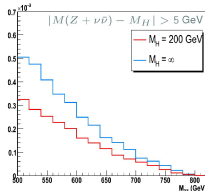
ISR and beamstrahlung limit the validity of the kinematical cut $M_{recoil} > 200$ GeV in suppressing Higgs-strahlung contributions

ZZ-resonant final states



No Higgs-strahlung

ZZ-resonant final states



Genuine $e^+e^- \rightarrow ZH \rightarrow jj + \nu\bar{\nu}jj$ events enter the analysis

News from Herwig++

- ▶ Lots of activity in the last two years

News from Herwig++

- ▶ Lots of activity in the last two years
- ▶ Herwig++ “*ready for prime time*”
- ▶ needs to be tuned and used

4. Summary

- Herwig++ group made a lot of progress in the last year
- The generator is now fully ready for hadron collisions
- A comprehensive manual is now available
- Support of experiments: herwig@projects.hepforge.org
- Further improvements will follow. News on wiki!

- e.g.: native description of τ -decays challenges TAUOLA (maybe not as flexible yet, but getting stronger):

Herwig++ (15/34)

└ Recent improvements/Tuning

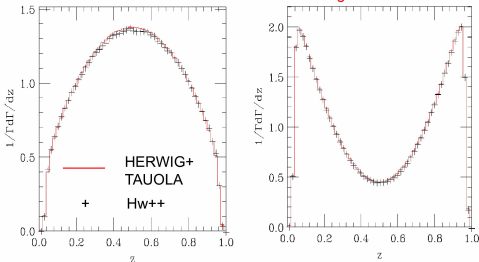
Hadronic Decays

Example: Tau Decays

$$\tilde{\tau}^{\pm} \rightarrow \tilde{\chi}_1^0 \tau^{\pm} \rightarrow \tilde{\chi}_1^0 \rho^{\pm} \nu_{\tau} \rightarrow \tilde{\chi}_1^0 \pi^0 \pi^{\pm} \nu_{\tau}$$

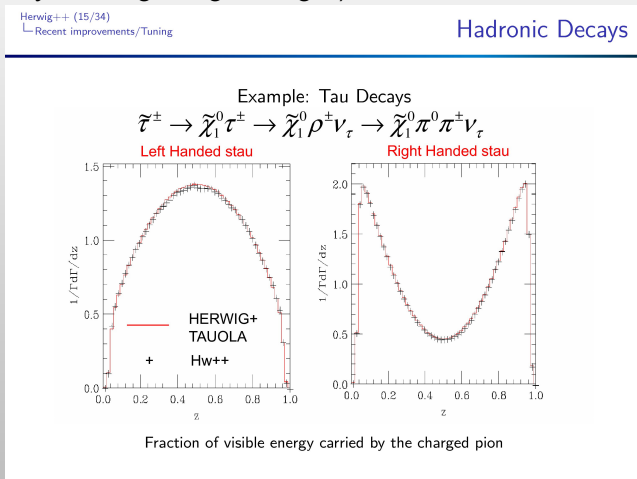
Left Handed stau

Right Handed stau



Fraction of visible energy carried by the charged pion

- e.g.: native description of τ -decays challenges TAUOLA (maybe not as flexible yet, but getting stronger):

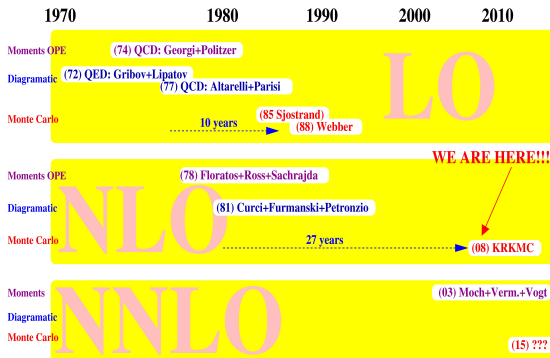


- also: underlying event, p_T distribution, hard matrix elements, hadronic decay database, BSM, ...

Unintegrated NLO evolution kernel for Monte Carlo modelling of the QCD/QED initial state radiation

- ▶ long roads from inclusive renormalization group evolution to exclusive event generation for the PDFs

Time evolution of the Collinear QCD Evolution



Unintegrated NLO evolution kernel for Monte Carlo modelling of the QCD/QED initial state radiation/KRKMC Project – p. 6/20

- ▶ operational proof of concept for **NLO** parton shower:

Discussion, Conclusions

- Unintegrated NLO kernel within full 2-particle LIPS in the MC can be constructed.
- Dimensional regularization can be removed.
- The integrand of the NLO kernel features nice IR cancellations, such that only **short range correlation** remain for large y_i and α_i . No long tails! No cancellations between distant regions in the LIPS!
- Re-insertion of the NLO unintegrated kernel into LO MC model representing LO+NLO (DGLAP) evolution done for $n = 2$ and is perfectly feasible for $n > 2$.
- Monte Carlo weight looks regular/positive.
- **A decisive/critical milestone towards NLO parton shower MC has been reached.**

Unintegrated NLO evolution kernel for Monte Carlo modelling of the QCD/QED initial state radiation KRMVC Project – p.20/20

Finite lifetime effects in top quark pair production at threshold

- ▶ physics at the $t\bar{t}$ threshold is governed by different scales: **energy**, **momentum**, **width (lifetime)**

Finite lifetime effects in top quark pair production at threshold

- ▶ physics at the $t\bar{t}$ threshold is governed by different scales: **energy, momentum, width (lifetime)**
- ▶ needs **effective field theory** for correct **power counting** and **running** between scales

Unstable quarks in vNRQCD

Power counting: $D^0 \sim m_t v^2$, $p^2 \sim m_t^2 v^2$, $\Gamma_t \sim m_t \alpha \sim m_t \alpha_s^2$

Full theory:

$$i\Sigma_t = \text{diagram with } W \text{ loop}$$

Effective theory:

$$\mathcal{L}_{\text{bil}} = \psi_{\mathbf{p}}^\dagger(\mathbf{x}) \left[iD^0 - \frac{p^2}{2m_t} + \frac{p^4}{8m_t^3} \right] \psi_{\mathbf{p}}(\mathbf{x}), \quad \delta\mathcal{L}_{\text{bil}} = \psi_{\mathbf{p}}^\dagger \left[\delta m_t + i\frac{\Gamma_t}{2} - i\frac{\Gamma_t}{2} \frac{p^2}{2m_t^2} \right] \psi_{\mathbf{p}}$$

$\sim m_t v^2$ $v \sim \alpha_s$ $\sim m_t \alpha_s^2$ $\sim m_t \alpha_s^4$

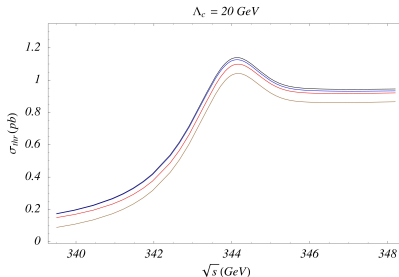
stable propagator: $\frac{i}{p^0 - \frac{p^2}{2m_t}}$

unstable propagator: $\frac{i}{p^0 - \frac{p^2}{2m_t} + i\frac{\Gamma_t}{2}}$

NNLL time dilatation correction

- ▶ sizable NNLO effects:

Numerical results



- Standard vNRQCD cross section
- plus usual electroweak corrections \Rightarrow change of normalization: $\approx -2\%$
- plus absorptive electroweak effects \Rightarrow top mass shift: $\approx 50 \text{ MeV}$
- plus phase space effects at NLO and NNLO \Rightarrow change of σ_{thr} : $\approx -60 \text{ fb}$



Dominant NNLO corrections to W-pair production near threshold

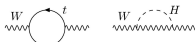
- ▶ ILC with $\sqrt{s} \approx 2M_W$ will improve ΔM_W , needs **reliable** theoretical predictions: avoid **gauge invariance** issues or **unitarity** violations

Motivation

Process of *W*-pair production near threshold has phenomenological relevance for accurate determination of the *W* boson mass at ILC

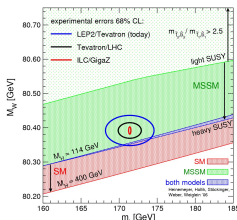
$$M_W$$

- Key observable for SM precision tests
- Combined with independent measurements of m_t and M_H constrains New Physics effects through virtual-particle exchange



$$\Delta M_W^2 \propto m_t^2 \qquad \Delta M_W^2 \propto \ln M_H$$

Threshold scan of *WW* cross section at ILC could reduce the total error on M_W to $\delta M_W \sim 6\text{MeV}$ [Wilson '01] with $\mathcal{L} = 100\text{fb}^{-1}$ (just one year!)



[Heinemeyer et al. '06]

Total theoretical uncertainties must be reduced to 1‰!

- ▶ **Effective Field Theory** approach (again) provides excellent approximation for inclusive cross sections

A toy example: the $e^-e^+ \rightarrow 4f$ Born cross section

How does the EFT work? → To understand apply it to the calculation of the [Born](#) cross section
Extract the total cross section from unitarity cuts of the [forward-scattering amplitude](#)

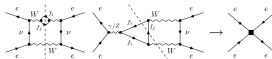
LO ($\sim \alpha_{ew} v$)

From **leading-order** operators and propagators



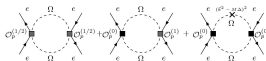
$\sqrt{\text{NLO}}$ ($\sim \alpha_{ew}^2 \Gamma_W / M_W$)

From **singly-resonant** configurations



NLO ($\sim \alpha_{ew}^2 v \times (v^2, \Gamma_W / M_W)$)

From **higher-dimensional** operators

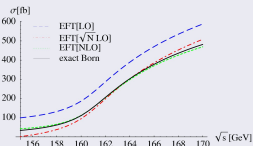


Pietro Falgari (TPE, RWTH-Aachen)

$\sigma_{\text{Born}}(e^-e^+ \rightarrow \mu^- \nu \mu \bar{\nu})$

Comparison with numerical result from [Whizard/CompHep](#)

[Killian, Boos et al. '04, Pukhov et al. '99]



Navigation icons: back, forward, search, etc.

ILC-ECFA 5 / 12

- ▶ **Effective Field Theory** approach (again) provides excellent approximation for inclusive cross sections

A toy example: the $e^-e^+ \rightarrow 4f$ Born cross section

How does the EFT work? \rightarrow To understand apply it to the calculation of the [Born](#) cross section
Extract the total cross section from unitarity cuts of the [forward-scattering amplitude](#)

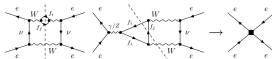
LO ($\sim \alpha_{ew}^2 v$)

From **leading-order** operators and propagators



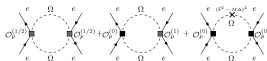
$\sqrt{\text{NLO}}$ ($\sim \alpha_{ew}^2 \Gamma_W/M_W$)

From **singly-resonant** configurations



NLO ($\sim \alpha_{ew}^2 v \times (v^2, \Gamma_W/M_W)$)

From **higher-dimensional** operators

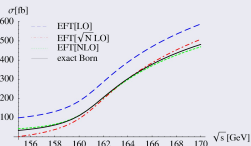


Pietro Falgari (TPE, RWTH-Aachen)

$\sigma_{\text{Born}}(e^-e^+ \rightarrow \mu^- \nu \mu \bar{\nu})$

Comparison with numerical result from [Whizard/CompHep](#)

[Killian, Boos et al. '04, Pukhov et al. '99]



Navigation icons: back, forward, search, etc.

ILC-ECFA 5 / 12

- ▶ cuts can be implemented as well

Navigation icons: back, forward, search, etc.

Two-loop hadronic corrections to Bhabha scattering

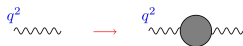
- ▶ **Bhabha**-Scattering **essential** for luminosity monitoring: at ILC **not** only at small angles!

Two-loop hadronic corrections to Bhabha scattering

- ▶ **Bhabha-Scattering essential** for luminosity monitoring: at ILC **not** only at small angles!
- ▶ non-perturbative hadronic contributions via dispersion relation from the measured **R** ratio

Warsaw – June 9-12, 2008

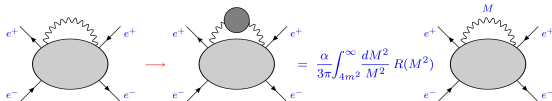
Hadronic corrections



$$\frac{-ig_{\alpha\beta}}{q^2 + i\epsilon} \longrightarrow \frac{-ig_{\alpha\delta}}{q^2 + i\epsilon} i(q^2 g^{\delta\epsilon} - q^\delta q^\epsilon) \Pi(q^2) \frac{-ig_{\epsilon\beta}}{q^2 + i\epsilon} \longrightarrow \frac{-ig_{\alpha\beta}}{q^2 + i\epsilon} \Pi(q^2)$$

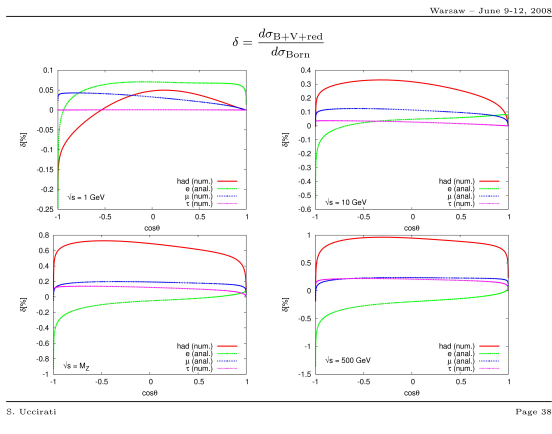
Dispersion relation

$$\Pi(q^2) = \frac{\alpha}{3\pi} \int_{4m^2}^{\infty} dz \frac{q^2}{z} \frac{R(z)}{q^2 - z + i\epsilon},$$



$$= \frac{\alpha}{3\pi} \int_{4m^2}^{\infty} \frac{dM^2}{M^2} R(M^2)$$

- hadronic NNLO corrections reach 1% at $\sqrt{s} = 500$ GeV:



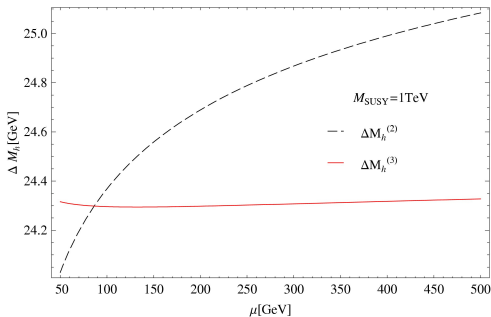
Three-Loop Corrections to the MSSM Higgs Boson Mass

- ▶ if there were no NLO corrections, LEP2 would have found the lightest MSSM Higgs

Three-Loop Corrections to the MSSM Higgs Boson Mass

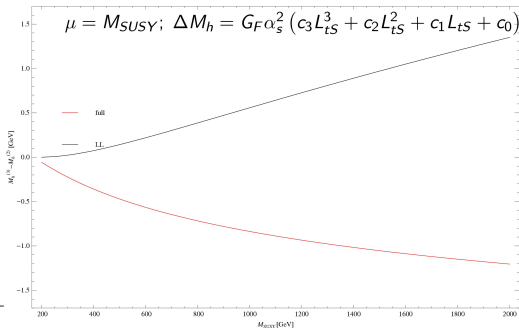
- ▶ if there were no NLO corrections, LEP2 would have found the lightest MSSM Higgs
- ▶ need to estimate NNNLO corrections for reliable predictions, because NNLO still suffer from sizable **scale uncertainties**:

Reduced Scale Dependency



- ▶ *caveat emptor*: leading logarithms can be misleading

Full Result vs LL Approximation



theory is alive and well!!!

- ▶ leading order parton level event generators for **6 and more final state particles** continue to multiply

theory is alive and well!!!

- ▶ leading order parton level event generators for 6 and more final state particles continue to multiply
- ▶ complete NLO parton level event generators for $2 \rightarrow 4$ have arrived

theory is alive and well!!!

- ▶ leading order parton level event generators for **6 and more final state particles** continue to multiply
- ▶ **complete NLO parton level event generators** for $2 \rightarrow 4$ have arrived
- ▶ the **next generation** of **general purpose event generators** including the non-perturbative QCD muck (e. g. HERWIG++) has arrived

theory is alive and well!!!

- ▶ leading order parton level event generators for **6 and more final state particles** continue to multiply
- ▶ **complete NLO parton level event generators** for $2 \rightarrow 4$ have arrived
- ▶ the **next generation** of **general purpose event generators** including the non-perturbative QCD muck (e. g. HERWIG++) has arrived
- ▶ **NLO parton showers** are on the horizon

theory is alive and well!!!

- ▶ leading order parton level event generators for **6 and more final state particles** continue to multiply
- ▶ **complete NLO parton level event generators** for $2 \rightarrow 4$ have arrived
- ▶ the **next generation** of **general purpose event generators** including the non-perturbative QCD muck (e. g. HERWIG++) has arrived
- ▶ **NLO parton showers** are on the horizon
- ▶ the **effective field theory** technology for systematic threshold expansions (W^+W^- and $t\bar{t}$) has matured

theory is alive and well!!!

- ▶ leading order parton level event generators for **6 and more final state particles** continue to multiply
- ▶ **complete NLO parton level event generators** for $2 \rightarrow 4$ have arrived
- ▶ the **next generation** of **general purpose event generators** including the non-perturbative QCD muck (e. g. HERWIG++) has arrived
- ▶ **NLO parton showers** are on the horizon
- ▶ the **effective field theory** technology for systematic threshold expansions (W^+W^- and $t\bar{t}$) has matured
- ▶ **complete NNLO** $2 \rightarrow 2$ cross sections are available

theory is alive and well!!!

- ▶ leading order parton level event generators for **6 and more final state particles** continue to multiply
- ▶ **complete NLO parton level event generators** for $2 \rightarrow 4$ have arrived
- ▶ the **next generation** of **general purpose event generators** including the non-perturbative QCD muck (e. g. HERWIG++) has arrived
- ▶ **NLO parton showers** are on the horizon
- ▶ the **effective field theory** technology for systematic threshold expansions (W^+W^- and $t\bar{t}$) has matured
- ▶ **complete NNLO** $2 \rightarrow 2$ cross sections are available
- ▶ **complete NNNLO** corrections for some observables are waiting to be tested by experimental observations