

carlomat

*a program for automatic computation of multiparticle
cross sections*

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Motivation

Increasing energy of initial beams at particle colliders such as LHC, or ILC \Rightarrow reactions with a few heavy particles at a time become possible.



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SM radiative corrections should be included, at least the leading ones.



Example

If the Higgs boson has mass below the $t\bar{t}$ threshold, $m_H < 2m_t$, then the $t\bar{t}H$ Yukawa coupling can be best determined from

$$e^+e^- \rightarrow t\bar{t}H$$

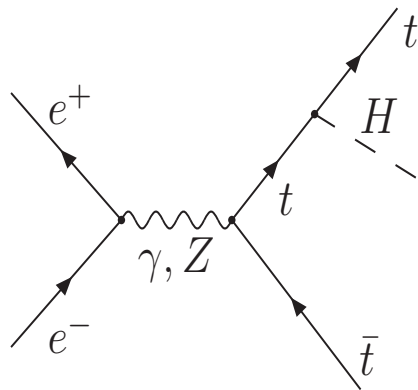
[Djouadi, Kalinowski, Zerwas]

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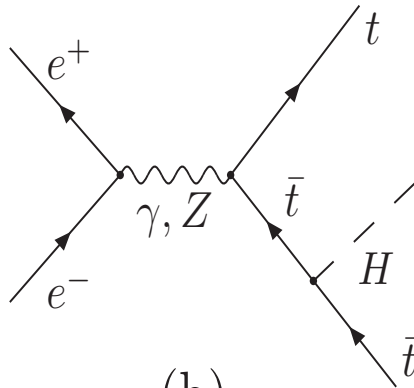
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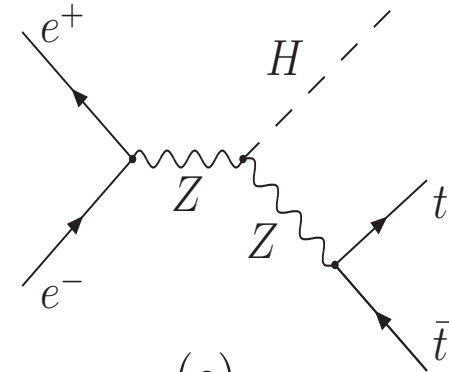
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(a)



(b)



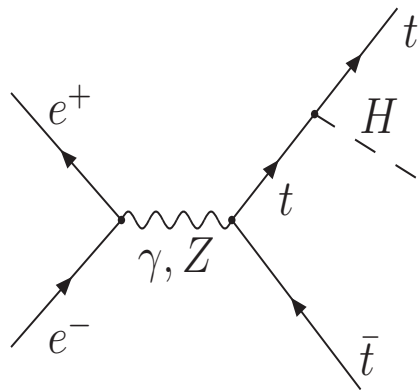
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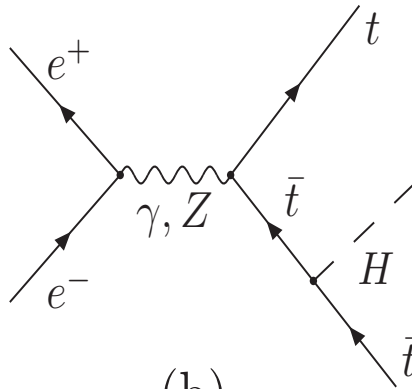
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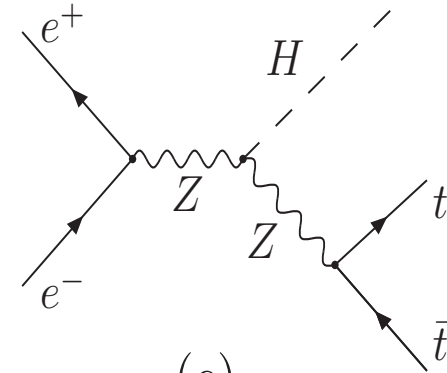
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(a)



(b)



(c)

Diagrams (a) i (b) dominate \Rightarrow the cross section $\sim g_{ttH}^2$.



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- the **top** and **antitop** decay before they hadronize, predominantly into bW^+ and $\bar{b}W^-$
- the W 's decay into $f\bar{f}'$ -pairs,
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\Rightarrow reactions of the form

$$e^+e^- \rightarrow b f_1 \bar{f}'_1 \bar{b} f_2 \bar{f}'_2 b \bar{b},$$

where $f_1, f_2 = \nu_e, \nu_\mu, \nu_\tau, u, c$ and $f'_1, f'_2 = e^-, \mu^-, \tau^-, d, s$, should

be studied with **a complete set of the Feynman diagrams,**

possibly including **radiative corrections,** at least the leading ones.


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Lowest order, in the unitary gauge, neglecting the Yukawa couplings of the fermions lighter than c quark and τ lepton.

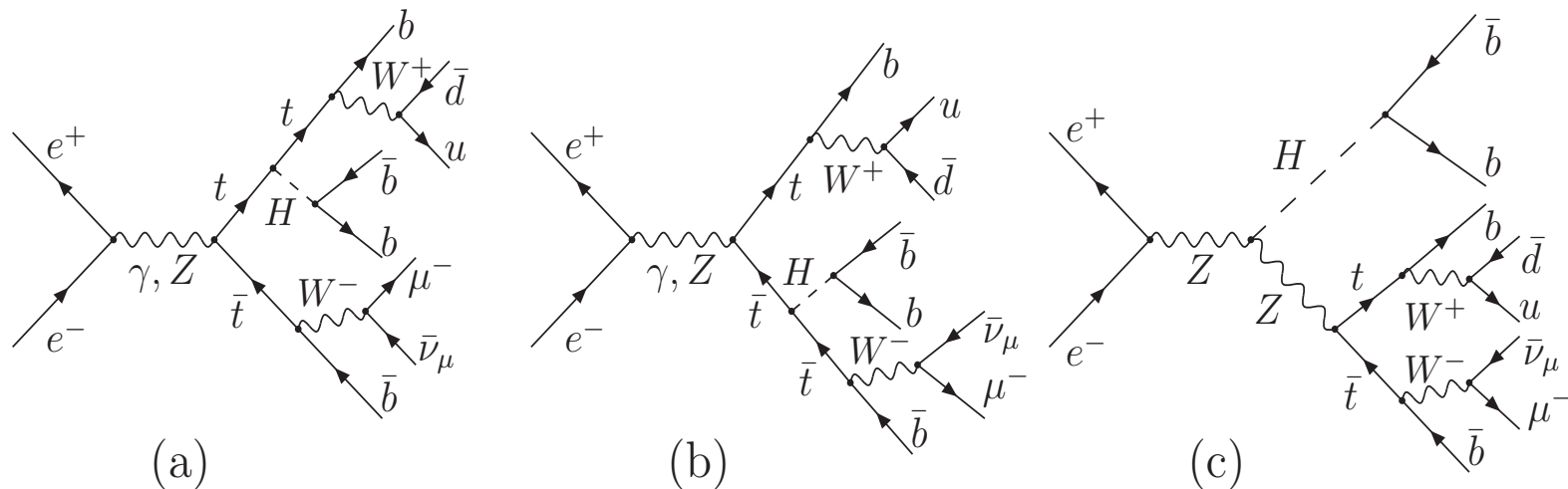
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“Signal” diagrams in the semileptonic channel: [20 diagrams]





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Publicly available versions of multipurpose Monte Carlo generators as [HELAC/PHEGAS](#), [AMAGIC++/Sherpa](#), [O'Mega/Whizard](#), [MadGraph/MadEvent](#), [ALPGEN](#), or [CompHEP/CalcHEP](#) may have problems while trying to handle reactions with that large numbers of the Feynman diagrams.



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Do it with carlomat!



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- the maximum number of external particles is 12
- **only the Standard Model is implemented at the moment**



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They are copied to another directory where the numerical program is executed.



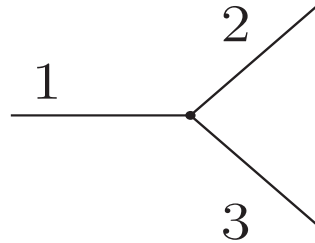
Generation of topologies

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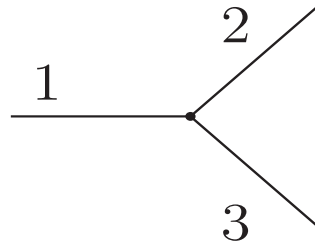
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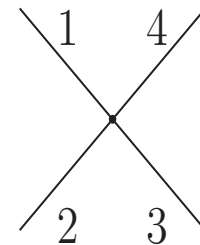
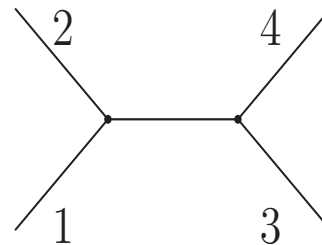
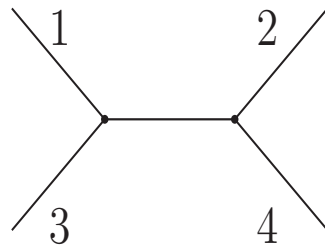
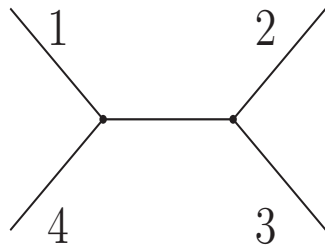


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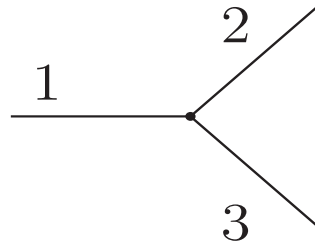


Attach **line 4** to **each line** and to **the vertex** \Rightarrow **4 topologies** of a **4 particle** process.

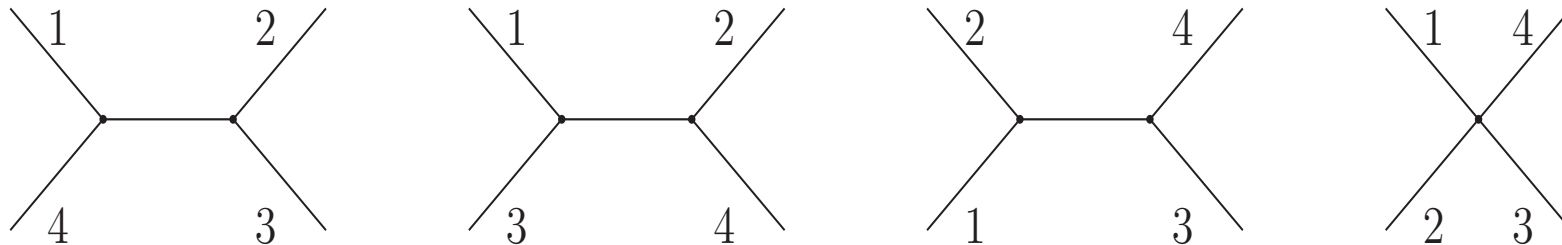


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Attach **line 5** to **each line**, including the internal ones, and to each **triple vertex** \Rightarrow **25 topologies** of a **5 particle** process.



Generation of topologies

No. of topologies grows dramatically with No. of external particles.

No. of particles	No. of topologies
6	220
7	2 485
8	34 300
9	559 405
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Topologies can be pregenerated and stored on a disk.



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The 'longer' part is further divided \Rightarrow the Feynman diagram is made of 3 or 4 parts, merged into a triple or quartic vertex of the model.



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All the topologies checked \Rightarrow subroutines for the matrix element, colour matrix and phase space integration are written.



Helicity amplitudes

Use is made of the routines developed for a Monte Carlo program `eett6f` v. 1.0 [K. K., *Comput. Phys. Commun.* **151** (2003) 339], for calculating lowest order cross sections of $e^+e^- \rightarrow 6$ fermions relevant for a $t\bar{t}$ -pair production and decay which have been tailored to meet needs of the automatic generation of amplitudes.



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Explicit summing over helicities is also possible. \Rightarrow Spinors or polarization vectors representing particles, both on- and off-shell ones, are computed only once, for all the helicities of the external particles they are made of, and stored in arrays \Rightarrow a novel feature with respect to *e.g.* MadGraph.



Helicity amplitudes

The **constant widths** of unstable particles are introduced through the complex mass parameters:

$$M_V^2 = m_V^2 - im_V\Gamma_V, \quad V = W, Z,$$
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which replace masses in the corresponding propagators, **both in the s - and t -channel Feynman diagrams**,

$$\Delta_F^{\mu\nu}(q) = \frac{-g^{\mu\nu} + q^\mu q^\nu / M_V^2}{q^2 - M_V^2},$$
$$\Delta_F(q) = \frac{1}{q^2 - M_H^2}, \quad S_F(q) = \frac{\not{q} + M_t}{q^2 - M_t^2}.$$

Propagators of a **photon** and **gluon** are taken in **the Feynman gauge**.



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Colour matrix is calculated only once at the beginning of execution of the numerical program after having reduced its size with the use of the SU(3) algebra properties.



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Weights with which different kinematical channels contribute are adapted iteratively.



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Matrix elements, for randomly selected sets of momenta, of



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Total cross sections checked against

- [ee4fgamma](#) [K.K., F. Jegerlehner] for $e^+e^- \rightarrow 4$ fermions and a photon
- [eett6f](#) [K.K.] for several reactions of $e^+e^- \rightarrow 6$ fermions

Agreement, within one standard deviation.

Top quark pair production in e^+e^- annihilation

Final state	\sqrt{s}	carlomat	AMAGIC++	HELAC
$b\bar{b}u\bar{u}d\bar{d}$	360	32.98(11)	32.90(15)	33.05(14)
	500	50.31(19)	49.74(21)	50.20(13)
$b\bar{b}u\bar{d}e^-\bar{\nu}_e$	360	11.448(26)	11.460(36)	11.488(15)
	500	17.424(56)	17.486(66)	17.492(41)
$b\bar{b}e^+\nu_e\mu^-\bar{\nu}_\mu$	360	3.843(5)	3.847(15)	3.848(7)
	500	5.856(11)	5.865(24)	5.868(10)
$b\bar{b}\mu^+\nu_\mu\mu^-\bar{\nu}_\mu$	360	3.837(5)	3.808(16)	3.861(19)
	500	5.834(10)	5.840(30)	5.839(12)

\sqrt{s} in **GeV**, cross sections in **fb**.

[T. Gleisberg, et al.] carlomat - p. 18



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Cross sections of $e^+e^- \rightarrow b\bar{b}b\bar{b}u\bar{d}\mu^-\bar{\nu}_\mu$ without QCD contributions have been checked against Whizard.

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Cross sections of $e^+e^- \rightarrow b\bar{b}b\bar{b}u\bar{d}\bar{\mu}^-\bar{\nu}_\mu$

\sqrt{s} [GeV]	σ_{all} [ab]	$\sigma_{\text{no QCD}}$ [ab]	σ_{signal} [ab]	$\sigma_{\text{signal}}^{\text{no cuts}}$ [ab]	$\sigma_{\text{NWA}}^{\text{no cuts}}$ [ab]
500	26.8(4)	7.80(3)	3.095(3)	3.796(3)	3.920(1)
800	100.2(8)	66.8(1)	46.27(2)	58.36(2)	60.03(2)
1000	93.1(3)	61.4(1)	40.18(2)	51.74(2)	52.42(3)
2000	47.4(2)	28.5(1)	15.14(3)	22.14(4)	20.68(3)

$5^\circ < \theta(q, \text{beam}), \theta(l, \text{beam}) < 175^\circ, \theta(q, q'), \theta(l, q) > 10^\circ,$

$E_q, E_l, \cancel{E}^T > 15 \text{ GeV}$

Cross sections of $e^+e^- \rightarrow b\bar{b}b\bar{b}u\bar{d}\bar{\mu}^-\bar{\nu}_\mu$

\sqrt{s} [GeV]	σ_{all} [ab]	$\sigma_{\text{no QCD}}$ [ab]	σ_{signal} [ab]	$\sigma_{\text{signal}}^{\text{no cuts}}$ [ab]	$\sigma_{\text{NWA}}^{\text{no cuts}}$ [ab]
500	26.8(4)	7.80(3)	3.095(3)	3.796(3)	3.920(1)
800	100.2(8)	66.8(1)	46.27(2)	58.36(2)	60.03(2)
1000	93.1(3)	61.4(1)	40.18(2)	51.74(2)	52.42(3)
2000	47.4(2)	28.5(1)	15.14(3)	22.14(4)	20.68(3)

$$5^\circ < \theta(q, \text{beam}), \theta(l, \text{beam}) < 175^\circ, \theta(q, q'), \theta(l, q) > 10^\circ,$$

$$E_q, E_l, \cancel{E}^T > 15 \text{ GeV}$$

Large off resonance background!

[K.K., S. Szczypiński]

Cross sections [ab] at $\sqrt{s} = 500 \text{ GeV}$ of $e^+e^- \rightarrow$

m_{bb}^{cut}	$b\bar{b}b\bar{b}u\bar{d}s\bar{c}$		$b\bar{b}b\bar{b}u\bar{d}\mu^-\bar{\nu}_\mu$		$b\bar{b}b\bar{b}\tau^+\nu_\tau\mu^-\bar{\nu}_\mu$	
[GeV]	σ_{all}	$\sigma_{\text{sig.}}$	σ_{all}	$\sigma_{\text{sig.}}$	σ_{all}	$\sigma_{\text{sig.}}$
20	13.88(6)	8.70(2)	3.50(2)	2.38	4.03(9)	0.86
5	10.17(4)	8.66(2)	2.62(1)	2.33	1.89(7)	0.86
1	9.07(4)	8.65(1)	2.37(1)	2.31	1.09(2)	0.86

$$60 \text{ GeV} < m(\sim b_1, \sim b_2) < 90 \text{ GeV}, \quad m(\mu, \cancel{E}^T) < 90 \text{ GeV}$$

$$|m(b, \sim b_1, \sim b_2) - m_t| < 30 \text{ GeV},$$

$$m_t - 30 \text{ GeV} < m_T(b, \mu, \cancel{E}^T) < m_t + 10 \text{ GeV},$$

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Background substantially reduced!

[K.K., S. Szczypiński]



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- Leading SM radiative corrections can be implemented, if corresponding subroutines are provided.



EW radiative corrections

$$e^+ e^- \rightarrow t \bar{t} \rightarrow b f_1 \bar{f}'_1 \bar{b} f_2 \bar{f}'_2$$



EW radiative corrections

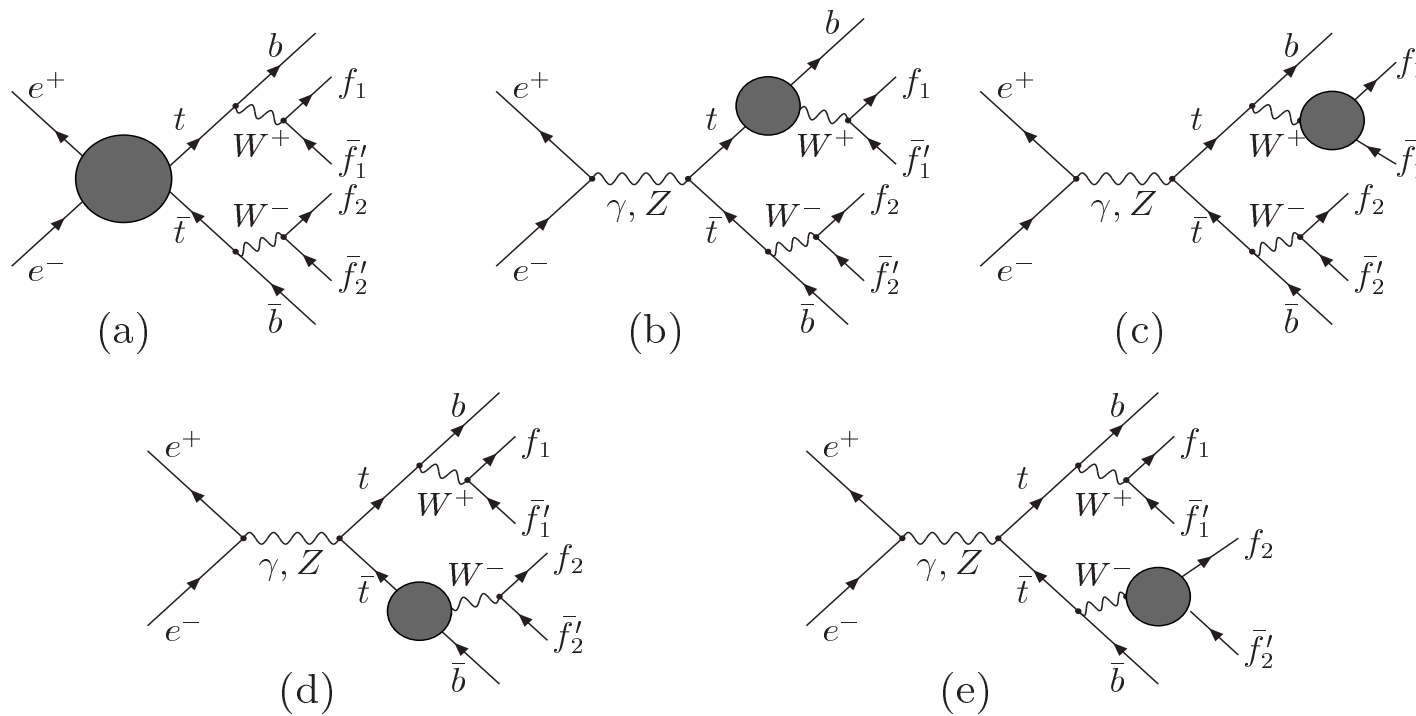
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K. Kołodziej, A. Staroń, A. Lorca, T. Riemann, Eur. Phys. J. C 46 (2006) 357.

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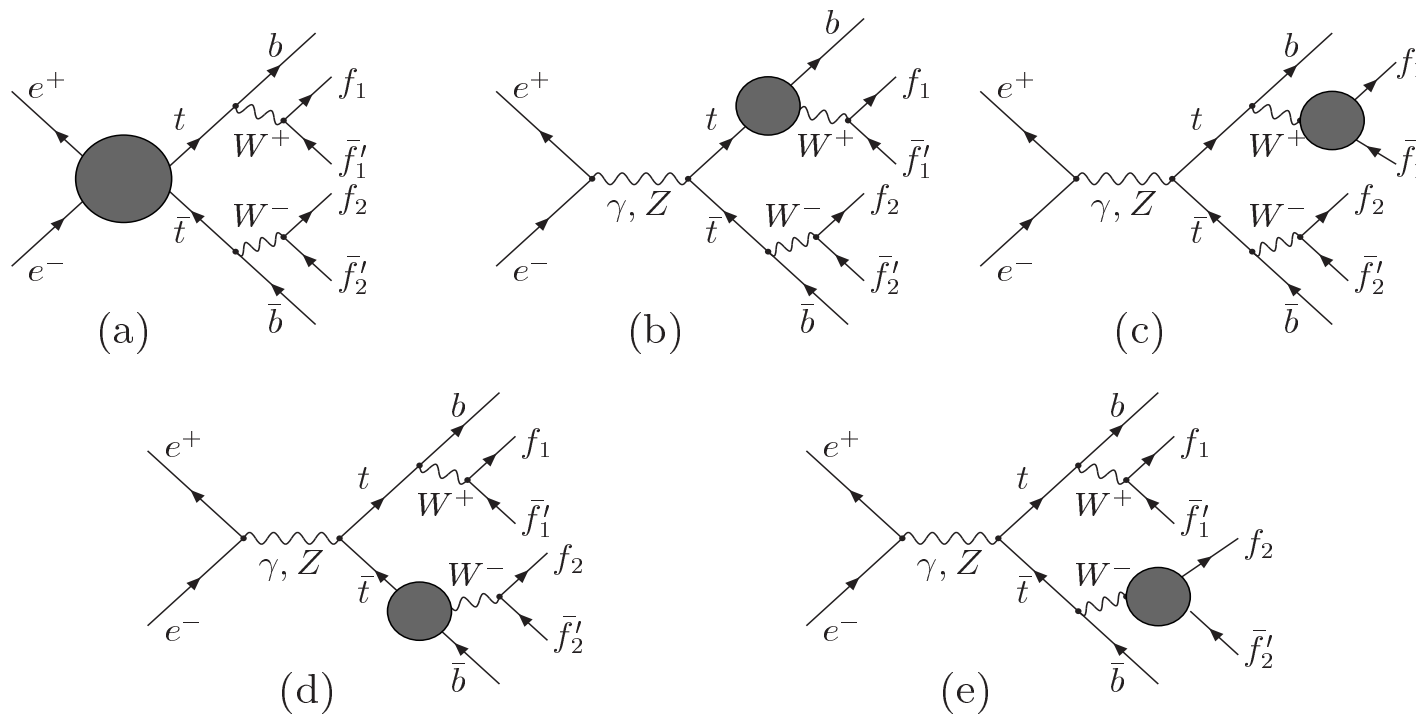
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- (a) calculated with a subroutine based on `topfit`, by T. Riemann, *et al.*,
- (b)–(e) with subroutines written by A. Staroń.