

# Tracking performance: Fast simulation studies

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# Outline

- 1 Scope of study
- 2 Tool
- 3 Cases studied
- 4 Comparison
- 5 The best combination
- 6 Conclusions

# Scope of study

What is the effect of different **geometries** on **track resolution** using **analytical calculation**

- Not detector technology
- Not pattern recognition
- Not calorimetry
- Not full simulation, ie. non-Gaussian tails are not included

There is no statistical uncertainty on the curves: If the curves of two designs differ, they **are** different.

# Tool

The tool for this study is **SGV**:

- Fast simulation based on precise analytical calculation of the Covariance matrix - the **Billoir fit**, ie. the covariance machinery of the Kalman filter used eg. in MarlinReco. **Hence it is not parametric.**
- Geometry, B-field, Multiple scattering, point-resolution used as in the Kalman filter.
- Follow the track-helix to find
  - What layers are crossed
  - Where they are crossed
  - and at which angles

This information is combined to calculate the covariance matrix of the 5 helix parameters

# SGV and full simulation

How well does the analytical calculation compare to the full simulation and reconstruction? (Thanks Steve Aplin!)

## Momentum resolution

- $\Delta(1/p)$  vs  $p$
- $\Delta(1/p)$  vs  $\Theta$

## Impact parameter resolution

- $\sigma_{ip}$  vs  $p$
- $\sigma_{ip}$  vs  $\Theta$

# SGV and full simulation

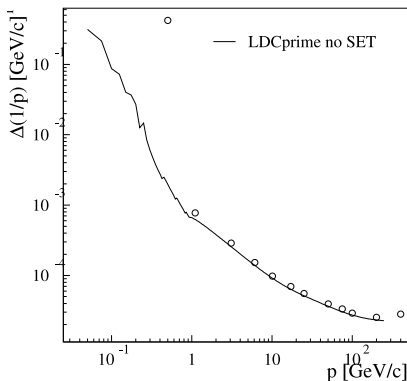
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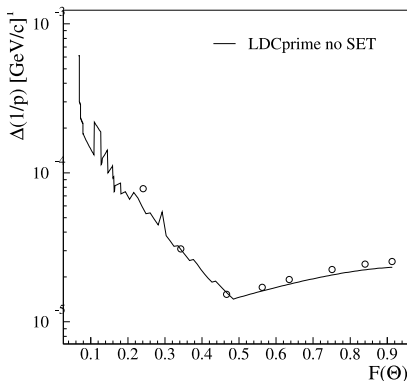
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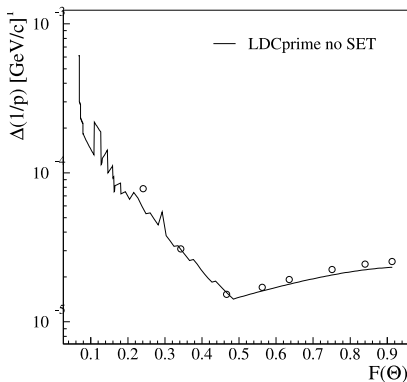
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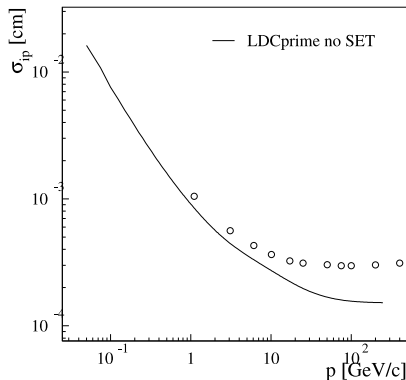
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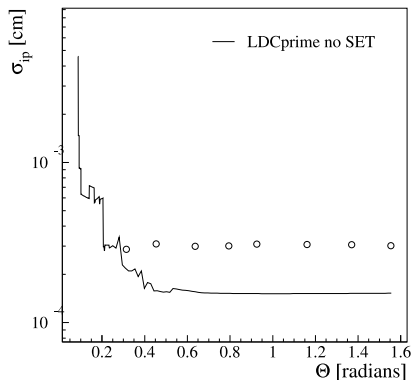
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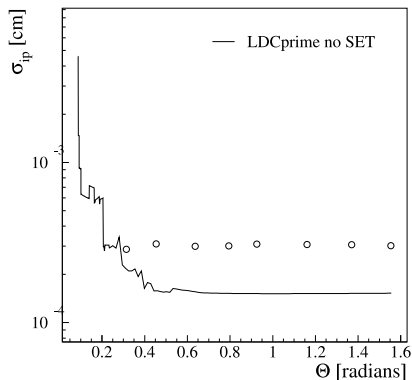
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**Not so well.** Full sim is right - the SGV numbers are too low. Under investigation.



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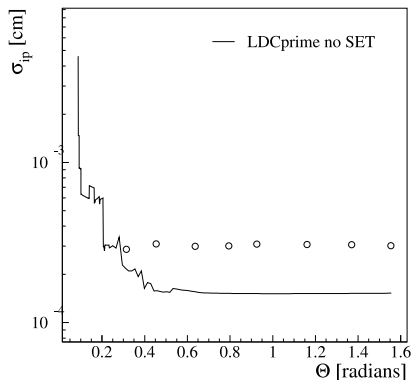
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## Impact parameter resolution

- $\sigma_{ip}$  vs  $p$
- $\sigma_{ip}$  vs  $\Theta$

**Not so well.** Full sim is right - the SGV numbers are too low. Under investigation. Nevertheless, the shape is similar, so comparisons should be relevant.



# Geometries and variables

- LDC, LDC', LDC-GLD (GLD size LDC), J4LDC (LDC size GLD), GLD' and GLD.
- Geometry as described in the Marlin GEAR files. (VXD described as cylinders, however)
- Take out all differences except geometry (ie. same point res and material budget in all setups.)
- No new elements.
- Adjust geometry somewhat.
- Shuffle sub-detectors
- Plots shown here are  $\Delta(1/p)$  and  $\sigma_{ip}$  (in  $R\phi$ ) vs  $p$  and  $\Theta$ .
- Try to make physically relevant plots :  $\sigma(p)$ , not  $\sigma(p_T)$ , choose angular variable reflecting differential crosssection.
- Then combine to the best compromise.

# The baselines

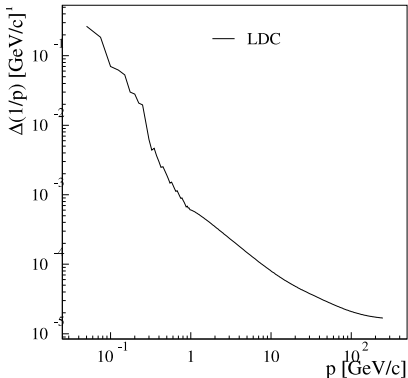
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- Momentum vs momentum
  - LDC
  - GLD
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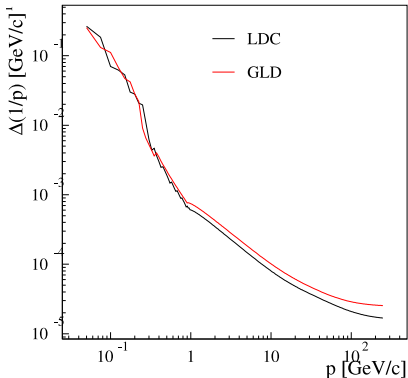
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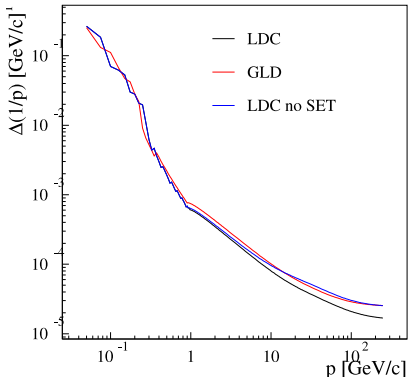




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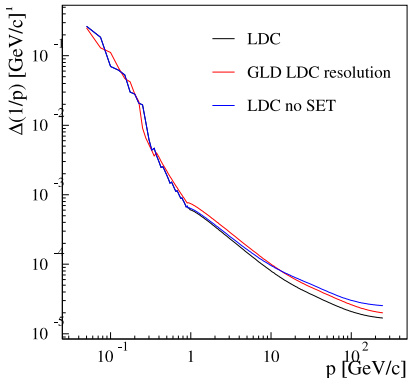
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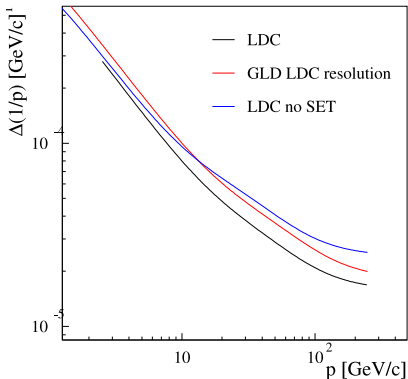
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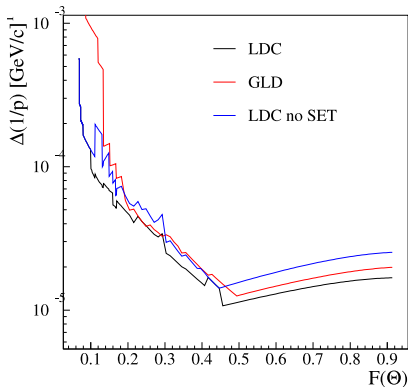
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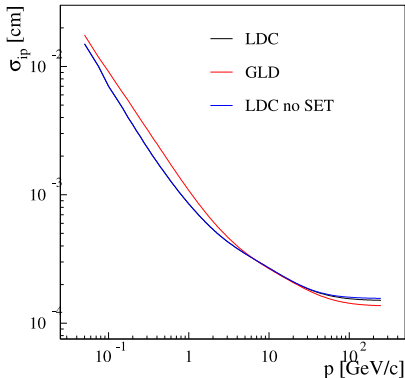
- Momentum vs angle
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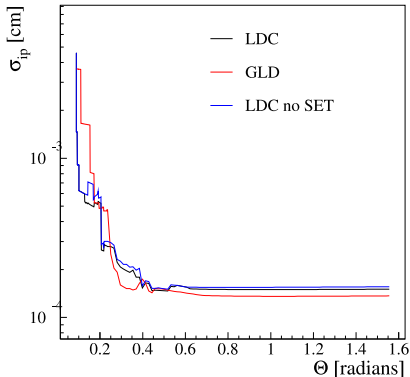
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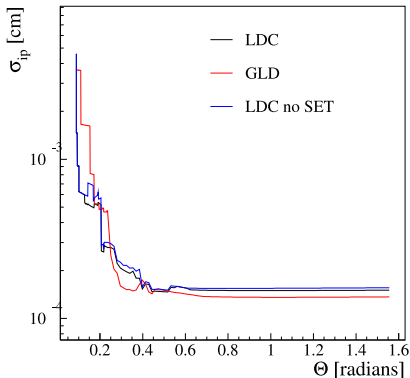


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**LDC** better in  $\Delta(1/p)$ , **GLD** in  $\sigma_{ip}$ .  
 The **SET** and the LDC **FTD** are useful. The LDC **ETD** also is at low angles.



# Geometry

Comparing changes in size for a single concept:

- Momentum vs momentum

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- LDC'
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- Impact parameter vs momentum

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# Geometry

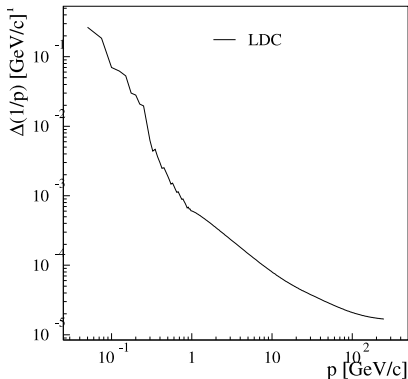
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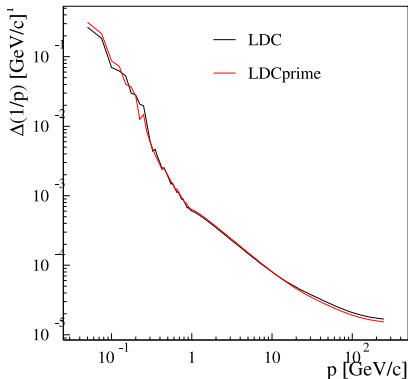
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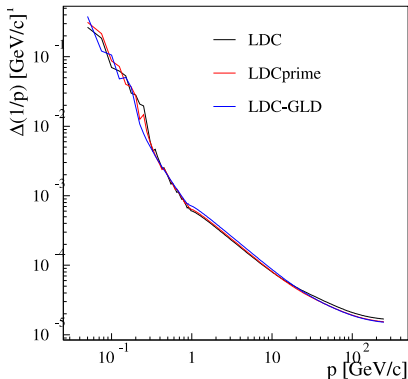
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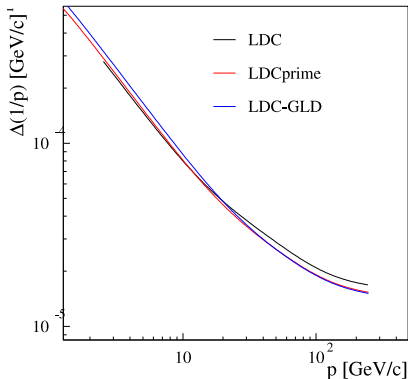
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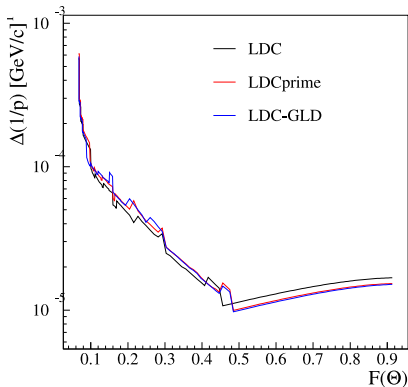
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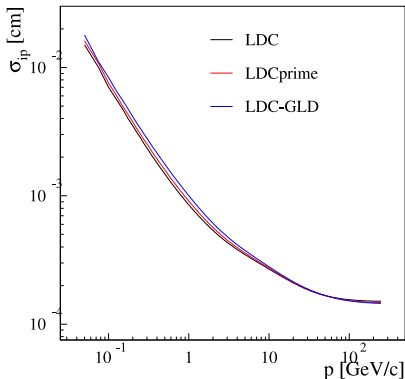
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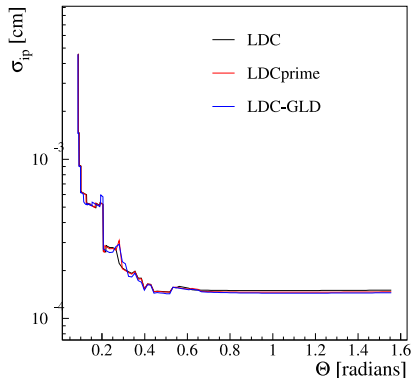
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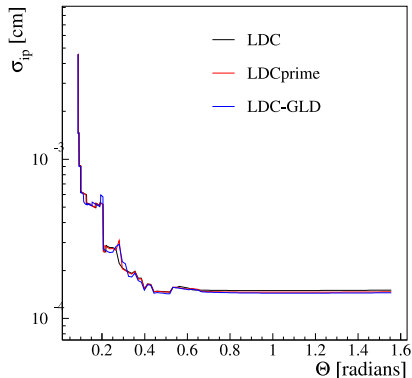


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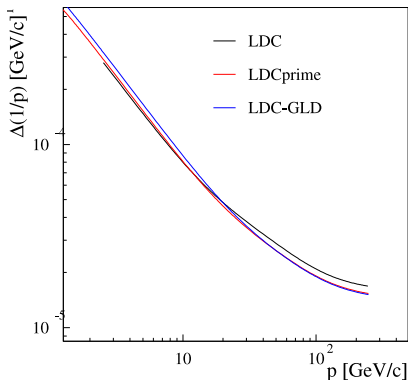
Very similar, but **LDC** performs slightly worse.



# Geometry

Why is LDC worse ?

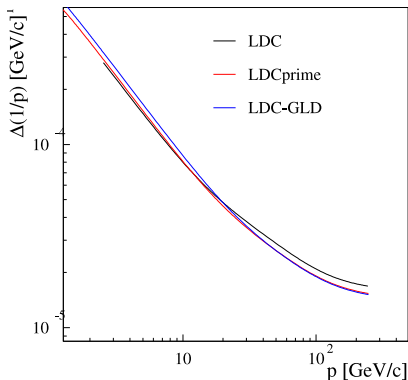
- LDC
- LDCprime at 3.1 T
- LDC-GLD at 2.5 T



# Geometry

Why is LDC worse ? Because  $R^2B$  is *not the same* in the different setups: LDCs 4T field corresponds to 2.5 T in GLD, not 3 T !

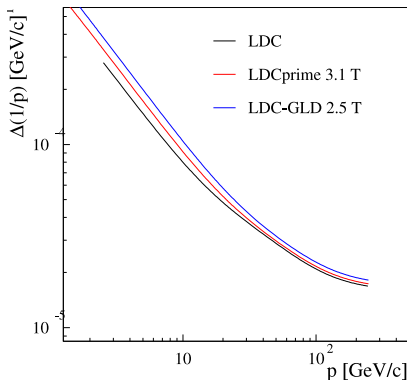
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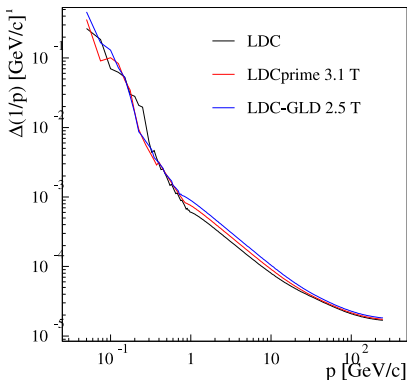
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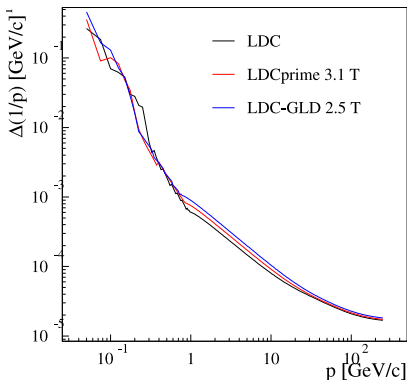


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Hence for equal  $R^2B$ , the smaller detector performs best, due to less material.

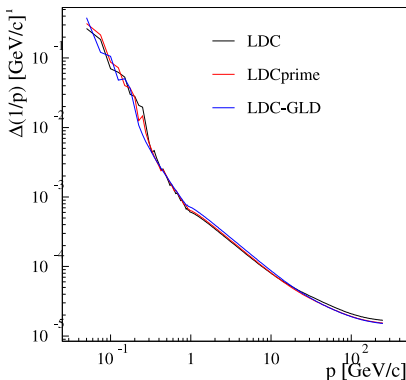


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Hence for equal  $R^2B$ , the smaller detector performs best, due to less material. The actual choice minimises the difference. Was that serendipitous ?



# Geometry

Larger TPC  $\rightarrow$  larger total signal in the TPC.

It can be exploited by :

- **More** pads, ie more points.
- **Bigger** pads, ie. more precise points.

Which is best ?

- LDC
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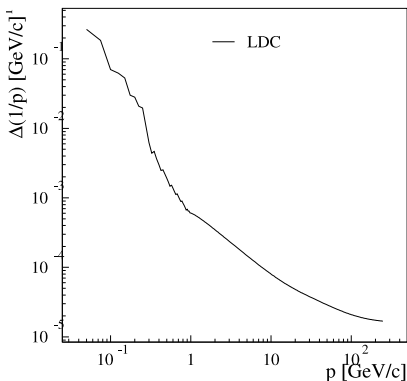
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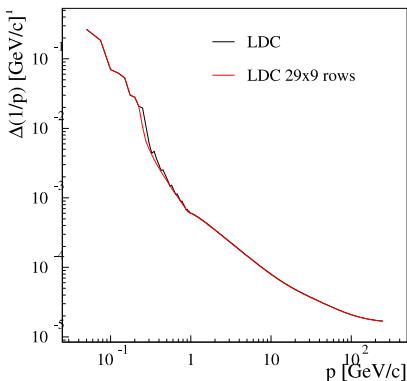
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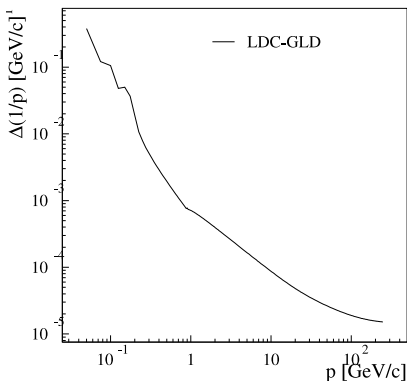
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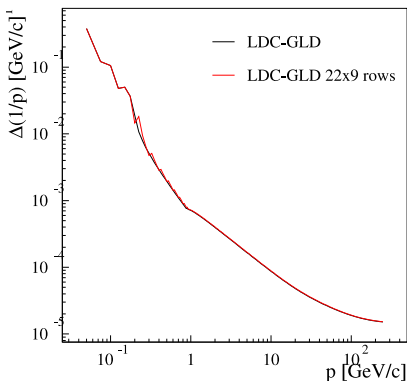
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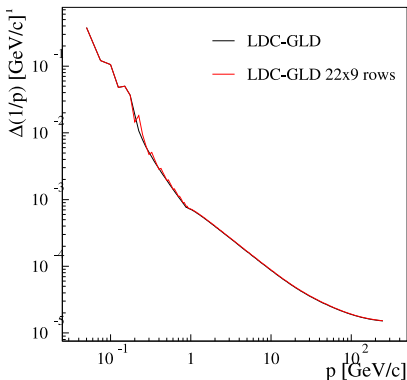
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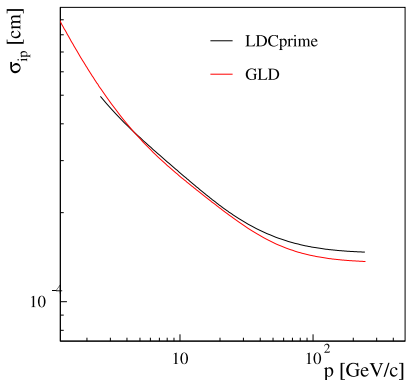
**It doesn't matter.**



# Vertex detector

Noticeably better resolution in GLD

- LDC-GLD
- GLD

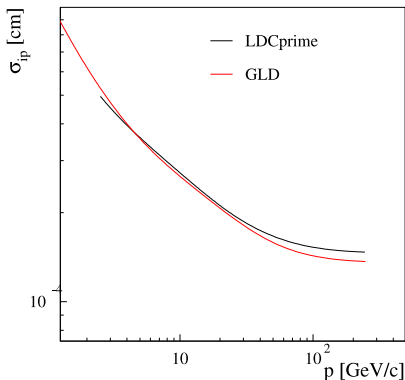


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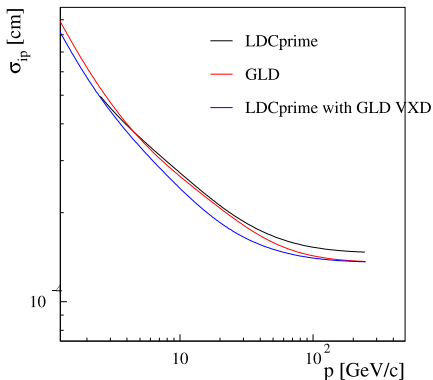


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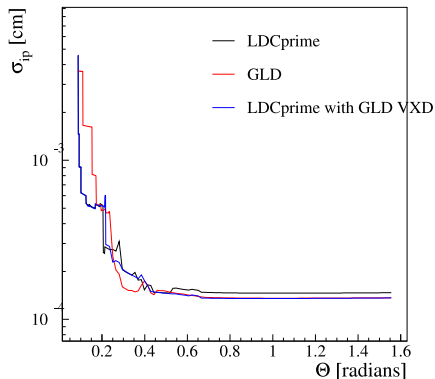


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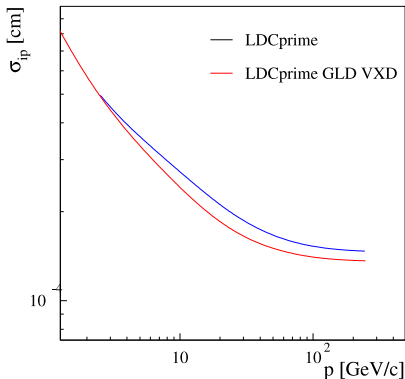
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# Vertex detector

## Noticeably better resolution in GLD: Why

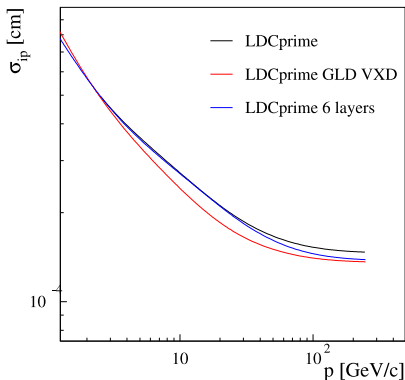
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- GLD model has no support and cooling structures



# Vertex detector

Noticeably better resolution in GLD: Why

- 6 against 5 points ?
- GLD model has no support and cooling structures



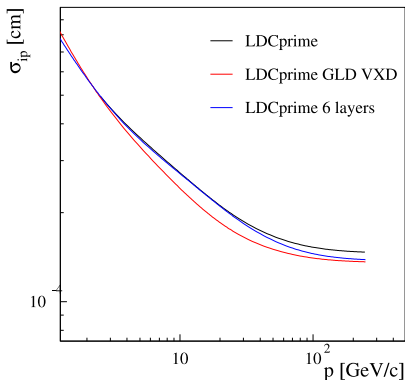
# Vertex detector

Noticeably better resolution in GLD: Why

- 6 against 5 points ?

Some effect...

- GLD model has no support and cooling structures



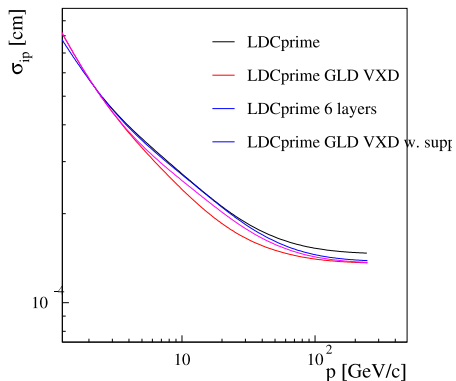
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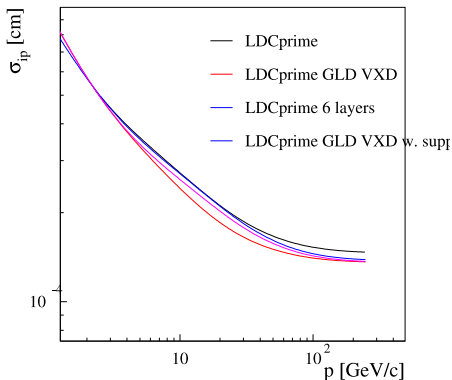
Some effect...

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Also an effect, but still GLD is the best.

Probably a better first point ( $\sqrt{2}$ !) ?

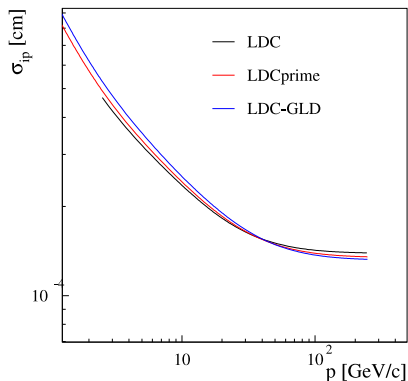
To be studied.



# Vertex detector

Note that LDC is better than LDC-GLD. Why ?

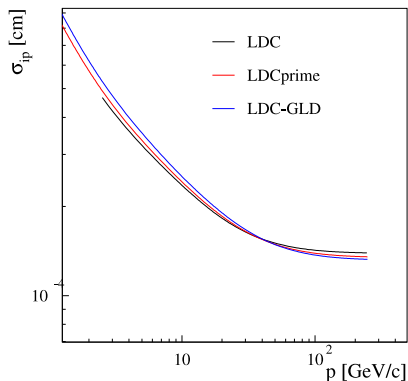
- Radius of first layer ?



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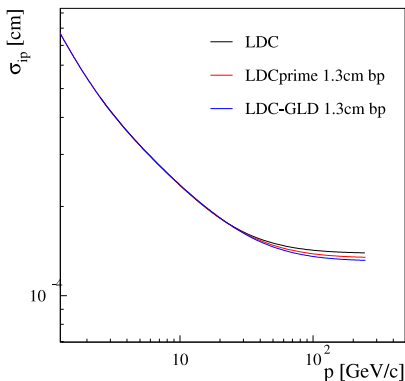


# Vertex detector

Note that LDC is better than LDC-GLD. Why ?

- Radius of first layer ?

**Yes.** This completely explains the difference.



# TPC inner radius

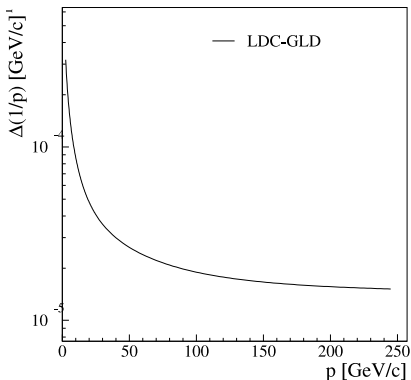
The GLD models have larger inner radius of the TPC, and consequently larger internal trackers. What effect does that have ?

- LDC-GLD
- LDC-GLD with GLD inner radius

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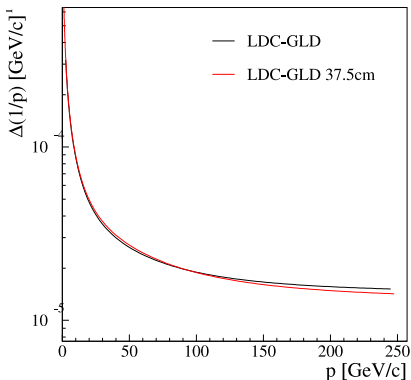
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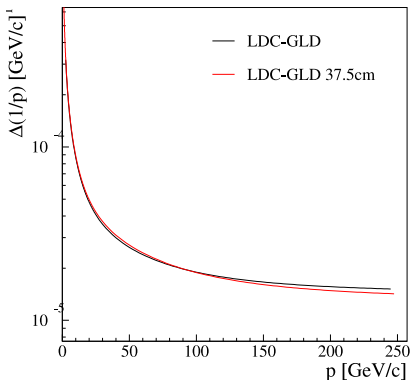


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- LDC-GLD with GLD inner radius

A **slight amelioration** of the momentum resolution.



# The best choice

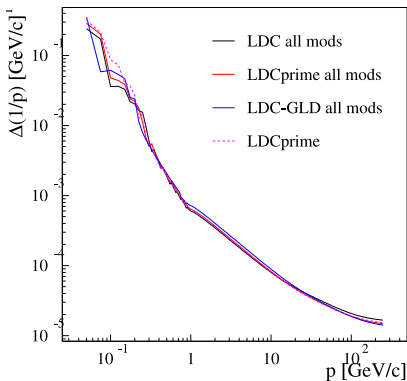
Take the best choice for all the sub-detectors. Compare with the best baseline for each of the quantities.

- Momentum. Best original design is LDCprime.
- Impact parameter. Best original design is GLD.

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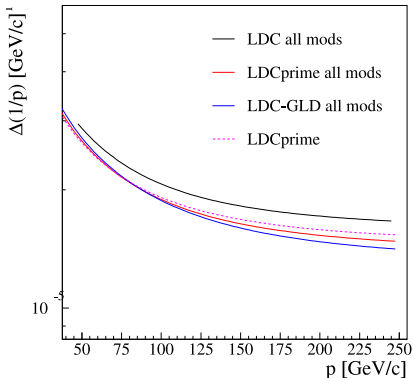
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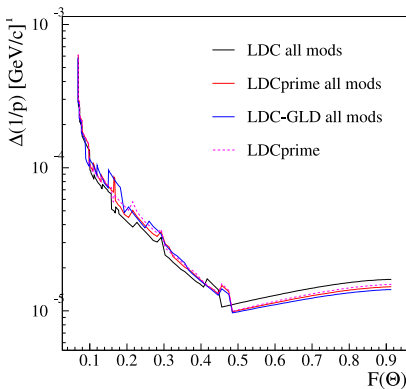




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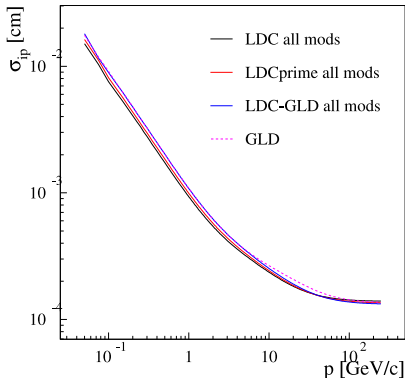
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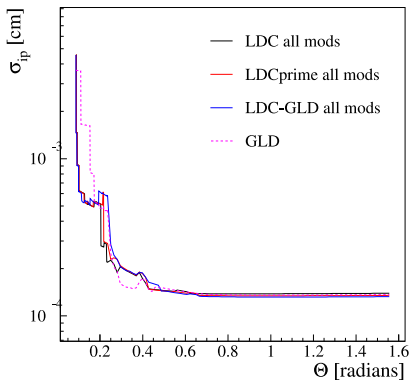
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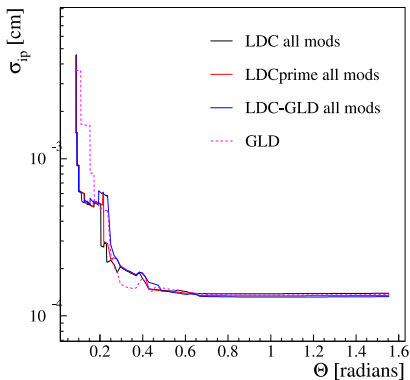


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The combination does better than the best original design in at all places. The largest detector does best.



# Conclusions

My conclusions on the optimal detector from the **pure track resolution** point-of-view:

- GLD vertex detector.
- LDC forward tracker.
- LDC external tracker in barrel.
- If  $B$  vs  $R$  is **as in the models**, the largest detector is preferable.
- If  $R^2B$  is **held constant**, the smallest detector is preferable.
- If a large option is chosen, the GLD dimensions of the TPC are preferable.
- With a TPC end-plate as thin as in the study, LDCs external forward tracker is useful.
- For the internal tracker in the barrel, this study provides no guidance: two or four layers are equivalent.

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