# Higgs Recoil Mass and Cross Section Analysis at ILD_00 

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## Introductory Remarks

## ZH Recoil Ana. Group:

(EU) Hengne Li, Roman Poeschl, Francois Richard, Manqi Ruan, Zhiqing Zhang (JP) Kazutoshi Ito, Yosuke Takubo, Hitoshi Yamamoto Reviewers:
(EU) Klaus Desch, (JP) Akiya Miyamoto

- Higgs-Strahlung Process:

- Higgs Recoil Mass:

$$
m_{h^{0}}^{2}=s+m_{Z^{0}}^{2}-2 E_{Z^{0}} \sqrt{s}
$$

- Cross Section and Coupling

Strength Measurement:

$$
g^{2} \propto \sigma=N / \mathcal{L} \epsilon
$$

- Mh = 120 GeV
- Ecm $=250 \mathrm{GeV}$
- Beam Energy Spread:
0.3\% for each beam
- Luminosity: $500 \mathrm{fb}-1$ in Analysis
$250 \mathrm{fb}-1$ results will also be reported as requested by the ILD LOI
- Detector Model:

ILD_00

- Event Generation:

SLAC

- Simulation \& Reconstruction:

DESY \& KEK

## Introductory Remarks

|  |  |  | $\begin{gathered} \mathrm{e}^{+} \mathrm{L} \mathrm{e}^{-} \mathrm{R} \\ \mathrm{e}+:-1.0, \mathrm{e}-:+1.0 \end{gathered}$ |  |
| :---: | :---: | :---: | :---: | :---: |
| $\mu \mu X$ | Reactions | Cross-Section | Reactions | Cross-Section |
|  | $\mu \mu \boldsymbol{X}$ | 17.1 fb | $\mu \mu \boldsymbol{X}$ | 10.97 fb |
|  | $\mu \mu$ | $17.1 \mathrm{pb}(330.4 \mathrm{fb})$ | $\mu \mu$ | $12.9 \mathrm{pb}(215.6 \mathrm{fb})$ |
|  | $\tau \tau$ | 17.1 pb | $\tau \tau$ | 12.9 pb |
|  | $\mu \mu \nu \nu$ | 849.0 fb | $\mu \mu \nu \nu$ | 45.0 fb |
|  | $\mu \mu \mu \mu$ | 11.4 fb | $\mu \mu \mu \mu$ | 7.2 fb |
|  | $\mu \mu \mathrm{e}$ | 1106.7 fb | $\mu \mu \mathrm{e}$ | 1088.6 fb |
|  | $\mu \mu \tau \tau$ | 23.1 fb | $\mu \mu \tau \tau$ | 14.7 fb |
|  | $\mu \mu \mathrm{qq}$ | 277.7 fb | $\mu \mu \mathrm{qq}$ | 148.6 fb |
| eeX | Reactions | Cross-Section | Reactions | Cross-Section |
|  | $e e X$ | 17.9 fb | $e e X$ | 11.29 fb |
|  | ee | $17.3 \mathrm{nb}(733.9 \mathrm{fb})$ | ee | $17.3 \mathrm{nb}(658.9 \mathrm{fb})$ |
|  | $\tau \tau$ | 17.1 pb | $\tau \tau$ | 12.9 pb |
|  | ee $\nu \nu$ | 1015.6 fb | ee $\nu \nu$ | 27.5 fb |
|  | ее $\mu \mu$ | 1106.7 fb | ее $\mu \mu$ | 1088.6 fb |
|  | еeee | 995.6 fb | еeee | 982.4 fb |
|  | ee $\tau \tau$ | 965.1 fb | $\mathrm{ee} \tau \tau$ | 948.8 fb |
|  | eeqq | 1366.5 fb | eeqq | 1168.9 fb |

(1) $\mu \mu v v$ and eevv have major contribution from WW, but also from ZZ.
(2) In the analysis, $\mu \mu f f$ refers to $\mu \mu e e+\mu \mu \mu \mu+\mu \mu \pi \tau+\mu \mu q q$,

Pre-cuts for ee and $\mu \mu$ : (cross-sections after pre-cuts are in blankets)
Pre-cuts for $\mu \mu$ :

- $M_{\mu^{+} \mu^{-}} \in(71.18,111.18) \mathrm{GeV}$
- $P_{T \mu^{+} \mu^{-}}>10 \mathrm{GeV}$
- $M_{\text {recoil }} \in(105,165) \mathrm{GeV}$

Pre-cuts for $e e$ :

- $\left|\cos \theta_{e^{+} / e^{-}}\right|<0.95$
- $M_{e^{+} e^{-}} \in(71.18,111.18) \mathrm{GeV}$
- $P_{T e^{+} e^{-}}>10 \mathrm{GeV}$
- $M_{\text {recoil }} \in(105,165) \mathrm{GeV}$


## Preparation 1: Lepton ID

- Refer to the study of Hajrah Tabassam, from discussions with Roberval Walsh, we define our cuts for lepton ID as:

$$
\begin{array}{cc}
\text { muon ID } & \text { electron ID } \\
E_{\text {ecal }} / E_{\text {total }}<0.5 & E_{\text {ecal }} / E_{\text {total }}>0.6 \\
E_{\text {cal }} / P_{\text {track }}<0.3 & E_{\text {cal }} / P_{\text {track }}>0.9
\end{array}
$$

| Pol. ( $e^{+}$Re-L) for illustration | Cuts (for $\mathrm{P}>15 \mathrm{GeV}$ ): single particle | $\mu \mu \mathrm{X}$ (muon ID) | eeX (electron ID) |
| :---: | :---: | :---: | :---: |
|  | $N_{\text {true }}$ ( N truth) | 31833 | 34301 |
|  | Ntrueniden | 31063 | 33017 |
|  | $\mathrm{N}_{\text {iden }}$ | 33986 | 34346 |
|  | Efficiency ( $\mathrm{N}_{\text {trueniden }} / \mathrm{N}_{\text {true }}$ ) | 97.6\% | 96.3\% |
|  | Purity ( $\mathrm{N}_{\text {trueniden }} / \mathrm{Niden}_{\text {a }}$ ) | 91.4\% | 96.1\% |
|  | Efficiency Both lepton ID: (no Prequest, select according to Mz) | 95.4\% | 98.8\% |

We dropped the improvements on the two muon ID applied in previous study, which is to search for the other muon from tracks if only one muon identified, (refer to my previous reports).

## Preparation 2: $\Delta \mathrm{P} / \mathrm{P}^{2}$ criterion in the selection of lepton candidates

- Parameterize $\Delta \mathrm{P} / \mathrm{P}^{2}$ for central region

$$
\begin{aligned}
& \Delta P / P^{2}=a \oplus b / P \\
& \text { where } a=2.5 \times 10^{-5} ; b=8 \times 10^{-4}
\end{aligned}
$$

- The criterion $\Delta P / P^{2}$ applied

| $\Delta \mathrm{P} / \mathrm{P}^{2}$ <br> Criterion | N evts on recoil mass peak, <br> Mh within $(119,121) \mathrm{GeV}$ |
| :--- | :---: |
| Before <br> Apply | 2812 |
| After <br> Apply | 2791 |

$$
\begin{array}{ll}
|\cos \theta|<0.78: & \Delta P / P^{2}<2 \times\left(2.5 \times 10^{-5} \oplus 8 \times 10^{-4} / P\right) \\
|\cos \theta|>0.78: & \Delta P / P^{2}<5 \times 10^{-4}
\end{array}
$$




## Preparation 3: Fitting Methods

$\square$ Two methods applied for the signal:
$\square$ Gaussian Peak Exponential Tail (GPET)

$$
f(x)=N \begin{cases}e^{-\frac{\left(x-x_{0}\right)^{2}}{2 \sigma^{2}}} & : \frac{x-x_{0}}{\sigma} \leq k \\ \beta e^{-\frac{\left(x-x_{0}\right)^{2}}{2 \sigma^{2}}}+(1-\beta) e^{-\left(x-x_{0}\right) \frac{k}{\sigma}} e^{\frac{k^{2}}{2}} & : \frac{x-x_{0}}{\sigma}>k\end{cases}
$$

$\square$ Convolution of Empirical with Gaussian (CEG)

$$
\begin{aligned}
& F(x)=N e^{-A x} \int_{x_{0}-x}^{\sqrt{s}-x} F_{H}(x+t) e^{-\frac{t^{2}}{2 \sigma^{2}}} d t \\
& F_{H}(x)=\left(\frac{x-x_{0}}{\sqrt{s}-x_{0}}\right)^{\beta-1}
\end{aligned}
$$

Background:
$\square$ Polynomial with 3 coefficients

## Analysis Procedures

| Higgs Decay <br> Model | SM Higgs Decay | Model Independent |
| :---: | :---: | :---: |
| Background <br> Rejection | SM Cut-chain | MI Cut-chain |
|  | Likelihood Further Rej. | Likelihood Further Rej. |
| Fitting |  |  |

- Background Rejection
- Rejection by Cuts
- SM Cut-Chain: Assume SM Higgs Decay
- MI Cut-Chain: Independent of Higgs Decay Model
- Further Rejection by Likelihood
- Fitting and Results


## BKG Rejection by Cuts: SM Cut-Chain

- For SM Higgs decay, multiplicity in the final states is the most efficient criterion to reject the $2 f$ and WW

Pol. ( $\mathrm{e}^{+} \mathrm{Re}^{-}$L)
for illustration

- In order to keep the $\mathrm{H}->\mathrm{Tt}$ in the signals :
- At most: Ntks>1
- How to reject evts with Ntks=2 in $\mu \mu$, $\tau \tau$ and WW ?
- Define $\Delta \theta_{\text {2tk }}: \Delta \theta$ between these two additional tracks for Ntks=2.


H->TT Additional Number of Tracks besides the two lepton candidates


# BKG Rejection by Cuts: SM Cut-Chain 

Pol. ( $\mathrm{e}^{+}{ }^{\text {Re}}{ }^{-}$- $)$ for illustration

| Nevts remained: | ZH-> $\mu \mu \mathrm{X}$ | ee-> $\mu \mu$ | ee->tr | ee-> $\mu \mu \mathrm{vv}$ |
| :---: | :---: | :---: | :---: | :---: |
| before any restriction: | 8563 | 8.5M | 8.6M | 425k |
| Both $\mu$ identified | 8169 (95.4\%) | 143k (1.7\%) | 257k (3\%) | 374k(88.1\%) |
| + pre-cuts | 7166 (83.7\%) |  | 17k (0.2\%) | 54k (12.6\%) |
| + Ntks>1 | 7112 (83.0\%) | 8.8k (0.10\%) | 2k (0.025\%) | 959 (0.23\%) |
| $+\left\|\Delta \theta_{2 t k}\right\|>0.01$ | 7100 (82.9\%) | 819 (0.01\%) | 1558 (0.02\%) | 122 (0.03\%) |
| $+\left\|\Delta \theta_{\text {min }}\right\rangle>0.01$ | 7000 (81.7\%) | 506 (0.006\%) | 346 (0.004\%) | 18 (0.004\%) |
| + acop (0.2, 3.0) | 6495(75.8\%) | 354 (0.004\%) | 0 (0\%) | 18 (0.004\%) |
| + Mh (115, 150) GeV | 6130(71.6\%) | 229 (0.003\%) | 0 (0\%) | 16 (0.004\%) |
| Nevts remained: | ZH->eeX | ee->ee | ee->tt | ee->eevv |
| before any restriction: | 8588 | 8.7G | 8.6M | 508k |
| Both e identified: | 8439 (98.3\%) |  | 965k(11.3\%) | 415k (81.6\%) |
| + pre-cuts | 5593 (62.5\%) | 267k | 29k (0.3\%) | 61k (12.1\%) |
| + Ntks>1 : | 5548 (62.0\%) | $16 \mathrm{k}\left(2 \times 10^{-6}\right)$ | 8309 (0.1\%) | 1708 (0.34\%) |
| $+\left\|\Delta \theta_{2 t k}\right\|>0.01$ | 5540 (61.9\%) | $2607\left(3 \times 10^{-7}\right)$ | 5885 ( $7 \times 10^{-4}$ ) | 279 (0.05\%) |
| $+\mid \Delta \theta_{\text {min }} \gg 0.01$ | 5448 (60.9\%) | $844\left(1 \times 10^{-7}\right)$ | $1212\left(1 \times 10^{-4}\right)$ | 31 (0.006\%) |
| + acop (0.2, 3.0) | 5054 (56.5\%) | $712\left(8 \times 10^{-8}\right)$ | 0 (0\%) | 30 (0.006\%) |
| $+\mathrm{Mh}(115,150) \mathrm{GeV}$ | 4631 (51.8\%) | $456\left(5 \times 10^{-8}\right)$ | 0 (0\%) | 11 (0.002\%) |

Nevts are weighted according to the cross-sections and luminosity $500 \mathrm{fb}^{-1}$

- Seems $\Delta \theta_{\text {2tk }}$ is not enough
- Define $\Delta \theta_{\min }$ :
- the smallest $\Delta \theta$ between the additional tracks and the muon candidates
$\Delta \theta$ between Additional Tracks and $\mu$ candidates

- Because mis-identification of other particles to be muons/ electrons


## BKG Rejection by Cuts: MI Cut-Chain

- muon channel with pol.
$\mathrm{e}^{+} \mathrm{R}^{-}$ц for illustration
$\mu \mu$ are pre-cutted
Cuts, based on lepton pair properties:
- $P_{T d l}>20 \mathrm{GeV}$
- $M_{d l} \in(80,100) G e V$

Pol. $\mathrm{e}^{+} \mathrm{R}^{-} \mathrm{L}$
for illustration

- $\operatorname{acop} \in(0.2,3.0)$

| Nevts remained: | ZH-> $\mu \mu \mathrm{X}$ | ee-> $\mu \mu$ | ee->tit | ee-> $\mu \mu \mathrm{vv}$ | ee-> $\mu \mu \mathrm{ff}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| before any restriction: | 8563 | 8.5M | 8.6M | 425k | 710k |
| Both $\mu$ id + pre-cuts | 7166 (83.7\%) | 143k (1.7\%) | 17k (0.2\%) | 54k (12.6\%) | 48k (6.7\%) |
| + $\mathrm{P}_{\text {Tall }}>20 \mathrm{GeV}$ | 6777(79.1\%) | 71k(0.81\%) | 12k(0.14\%) | 46k(10.8\%) | 38k(5.4\%) |
| + $\mathrm{Mdl} \in(80,100) \mathrm{GeV}$ | 6230(72.7\%) | 54k(0.64\%) | 6578(0.08\%) | 27k(6.4\%) | 30k(4.2\%) |
| + acop (0.2, 3.0) | 5827(68.0\%) | $45 k(0.53 \%)$ | 0(0\%) | 25k(6.0\%) | 27k(3.8\%) |


| Nevts remained: | ZH->eeX | ee->ee | ee->Tt | ee->eevv | ee->eeff |
| :--- | :--- | :--- | :--- | :--- | :--- |
| before any restriction: | 8588 | 8.7 G | 8.6 M | 508 k | 2.2 M |
| Both e id + pre-cuts | $5593(62.5 \%)$ | $267 \mathrm{k}(0.003 \%)$ | $29 \mathrm{k}(0.3 \%)$ | $61 \mathrm{k}(12.1 \%)$ | $41 \mathrm{k}(1.8 \%)$ |
| $+\mathrm{P}_{\mathrm{Tdl}}>20 \mathrm{GeV}$ | $5283(59.1 \%)$ | $195(0.002 \%)$ | $20 \mathrm{k}(0.24 \%)$ | $53 \mathrm{k}(10.4 \%)$ | $35 \mathrm{k}(1.6 \%)$ |
| $+\mathrm{M}_{\mathrm{dl}} \in(80,100) \mathrm{GeV}$ | $4508(50.4 \%)$ | $108(0.001 \%)$ | $12(0.14 \%)$ | $29 \mathrm{k}(5.8 \%)$ | $25 \mathrm{k}(1.1 \%)$ |
| $+\operatorname{acop}(0.2,3.0)$ | $4211(47.1 \%)$ | $98 \mathrm{k}(0.001 \%)$ | $866(0.01 \%)$ | $28 \mathrm{k}(5.4 \%)$ | $23 \mathrm{k}(1.0 \%)$ |




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## BKG Rejection by Cuts: Independent of Higgs Decay Model

## NEW!

## ISR $P_{T}$ balance for $\mu \mu$ and ee rejection

Idea: (Thanks to Francois' idea)

- For $\mu \mu$ and ee: $\mathrm{P}_{\mathrm{T}}$ of ISR photon should balance the $\mathrm{P}_{\mathrm{t}}$ of di-lepton system;
- For signal: Impossible to have ISR to balance Z $\mathrm{P}_{\mathrm{T}}$, independent of Higgs decay model.
Requirements:
- $M_{d ı} \in(80,100) \mathrm{GeV}$ : large FSR events are removed
- $\mathrm{P}_{\mathrm{Tdl}}>20 \mathrm{GeV}$ : Large $\mathrm{P}_{\mathrm{T}}$ ISR photon can be detected

Define $\Delta \mathrm{P}_{\text {Tbal }}=\mathrm{P}_{\text {Tdl }}-\mathrm{P}_{\mathrm{T} Y}$


Reduces $\mu \mu$ and
$\mathbf{P}_{\text {Toll }}$ vs. $\mathbf{P}_{\mathrm{T}_{y}}$ of ISR Photon, $u \mu$
 ee further by 1 to 2 orders of magnitude Signal lost: ~1\%

ISR photon conversions


## BKG Rejection by Cuts: Independent of Higgs Decay Model

To reject the ISR Photon conversions:

- Cut $\left|\Delta \theta_{2 \text { tk }}\right|>0.01$ : Only apply on events with 2 additional tracks
- Reject $\mu \mu$ and ee Further by a factor of 2.

Pol. $\mathrm{e}^{+}{ }^{\text {R }} \mathrm{e}^{-} \mathrm{f}$ for illustration

| Nevts remained: | ZH-> $\mu \mu \mathrm{X}$ | ee-> $\mu \boldsymbol{\mu}$ | ee->tr | ee-> $\boldsymbol{\mu} \mu \mathrm{vv}$ | ee-> $\mu \boldsymbol{\mu f f}$ |
| :--- | :--- | :--- | :--- | :--- | :--- |
| before any restriction: | 8563 | 8.5 M | 8.6 M | 425 k | 710 k |
| cuts applied before | $5827(68.0 \%)$ | $45 \mathrm{k}(0.53 \%)$ | $0(0 \%)$ | $25 \mathrm{k}(6.0 \%)$ | $27 \mathrm{k}(3.8 \%)$ |
| $+\Delta \mathrm{P}_{\text {Tbal. }}>10 \mathrm{GeV}$ | $5712(66.7 \%)$ | $2618(0.03 \%)$ | $0(0 \%)$ | $23 \mathrm{k}(5.5 \%)$ | $25 \mathrm{k}(3.6 \%)$ |
| $+\mathrm{I} \mathrm{\Delta} \mathrm{\theta}_{2 \text { tkl }}>0.01$ | $5704(66.6 \%)$ | $1044(0.01 \%)$ | $0(0 \%)$ | $23 \mathrm{k}(5.4 \%)$ | $25 \mathrm{k}(3.6 \%)$ |
| $+\mathrm{Mh}(115,150) \mathrm{GeV}$ | $5553(64.8 \%)$ | $761(0.009 \%)$ | $0(0 \%)$ | $16 \mathrm{k}(3.8 \%)$ | $15.5 \mathrm{k}(2.2 \%)$ |


| Nevts remained: | ZH->eeX | ee->ee | ee->TT | ee->eevv | ee->eeff |
| :--- | :--- | :--- | :--- | :--- | :--- |
| before any restriction: | 8588 | 8.7 G | 8.6 M | 508 k | 2.2 M |
| eeX | cuts applied before | $4211(47.1 \%)$ | $98 \mathrm{k}(0.001 \%)$ | $866(0.01 \%)$ | $28(5.4 \%)$ |
| $+\Delta \mathrm{P}_{\text {Tbal. }}>10 \mathrm{GeV}$ | $4095(45.8 \%)$ | $6618\left(8 \times 10^{-7}\right)$ | $606(0.007 \%)$ | $24 \mathrm{k}(4.7 \%)$ | $22 \mathrm{k}(1.0 \%)$ |
| $+\mid \Delta \theta_{2 \text { tk }} \mathrm{l}>0.01$ | $4089(45.7 \%)$ | $3660\left(4 \times 10^{-7}\right)$ | $519(0.006 \%)$ | $23.5 \mathrm{k}(4.6 \%)$ | $21.5 \mathrm{k}(0.98 \%)$ |
| $+\mathrm{Mh}(115,150) \mathrm{GeV}$ | $3960(44.3 \%)$ | $2706\left(3 \times 10^{-7}\right)$ | $260(0.003 \%)$ | $16.5 \mathrm{k}(3.3 \%)$ | $13 \mathrm{k}(0.59 \%)$ |

## BK Further Rejection by Likelihood

 PDFsAfter Cuts Rejection, Apply Further Rejection using Likelihood Method

## Likelihood:

$$
\begin{aligned}
& \text { lihood: } \\
& L=\prod_{i} P_{i} \text { ith Variable }
\end{aligned}
$$

Likelihood Fraction:

$$
\underset{\text { within }(0,1)}{f_{L}}=L_{S} /\left(L_{S}+L_{B}\right)
$$

Decide the $f_{L}$ cut by the maximum significance

$\mathrm{f}_{\mathrm{L}}$ Distribution ${ }^{\mathrm{L}^{\mathrm{L}}}$

Nevts remained vs. $f_{\llcorner }$cuts


Significance vs. $f_{L}$ cuts


Significance ${ }^{\text {the }}$




Taken:
Pol. $\mathrm{e}^{+}{ }^{+} \mathrm{e}^{-}$L muon channel SM Analysis

For illustration

## Background Rejection Summary Table

| Ana. | Pol. | Ch. | Cuts | $\mu \mu \mathrm{X} / \mathrm{eeX}$ | $\mu \mu / \mathrm{ee}$ | TT | $\mu \mu \mathrm{V}$ /eevV | $\mu \mu \mathrm{ff} / \mathrm{eeff}$ | S/B | $S / \sqrt{ }(S+B)$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| SM | $\begin{aligned} & \mathrm{e}^{+} \mathrm{R}^{2} \\ & \mathrm{e}^{-L} \end{aligned}$ | $\mu$ | SM cut-chain: | 6130(71.6\%) | 229 | 0 | 16 | 21.9k |  |  |
|  |  |  | + $\mathrm{f}_{\mathrm{L}}>0.31$ | 5116(59.7\%) | 63 | 0 | 7 | 11.3k | 0.45 | 39.8 |
|  |  | e | SM cut-chain: | 4631(51.8\%) | 456 | 0 | 11 | 20.2k |  |  |
|  |  |  | + $\mathrm{f}_{\mathrm{L}}>0.33$ | 3939(44.0\%) | 180 | 0 | 6 | 10.5k | 0.37 | 32.6 |
|  | $e^{+} L$ $e^{-}{ }^{-}$ | $\mu$ | SM cut-chain: | 3947(72.0\%) | 146 | 0 | 0 | 11.0k |  |  |
|  |  |  | + $\mathrm{f}_{\mathrm{L}}>0.27$ | 3435(62.6\%) | 31 | 0 | 0 | 5.3k | 0.64 | 36.7 |
|  |  | e | SM cut-chain: | 3947(72.0\%) | 338 | 0 | 2 | 9.9k |  |  |
|  |  |  | + $\mathrm{f}_{\mathrm{L}}>0.30$ | 2480(43.9\%) | 112 | 0 | 0 | 4.7k | 0.52 | 29.0 |
| MI | $e^{+} R$ $e^{-}$L | $\mu$ | MI cut-chain: | 5553(64.8\%) | 761 | 0 | 16k | 15.5k |  |  |
|  |  |  | + $\mathrm{f}_{\mathrm{L}}>0.19$ | 4600(53.7\%) | 471 | 0 | 8244 | 9297 | 0.26 | 30.6 |
|  |  | e | MI cut-chain: | 3960(44.3\%) | 2706 | 260 | 16.5k | 13 k |  |  |
|  |  |  | + $\mathrm{f}_{\mathrm{L}}>0.17$ | 3374(37.7\%) | 1524 | 260 | 9403 | 8175 | 0.17 | 22.4 |
|  | $\mathrm{e}^{+} \mathrm{L}$$e^{-}{ }_{R}$ | $\mu$ | MI cut-chain: | 3605(65.7\%) | 518 | 0 | 1452 | 7309 |  |  |
|  |  |  | + $\mathrm{f}_{\mathrm{L}}>0.24$ | 3208(58.5\%) | 362 | 0 | 1075 | 4563 | 0.53 | 33.4 |
|  |  | e | MI cut-chain: | 2511(44.5\%) | 2457 | 195 | 1339 | 6119 |  |  |
|  |  |  | $+\mathrm{f}_{\mathrm{L}}>0.29$ | 2154(38.2\%) | 1463 | 195 | 837 | 3439 | 0.36 | 24.0 |

## Fittings

| Ana. | Pol. | $\mu \mu \mathrm{X}$ |  | eeX |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | GPEG | CEG | GPET | CEG |
| SM | $\mathrm{e}^{+} \mathrm{R}$ $\mathrm{e}_{\text {- }}$ |  |  |  |  |
|  |  |  |  |  |  |
| MI |  |  |  |  |  |
|  |  |  |  |  |  |

M Higgs :
My Favorite Fitting I: (GPET)
$119.981 \pm 0.50 \mathrm{GeV}$ Cross-Section:
$11.31 \pm 0.39 \mathrm{fb}(0.34 \%)$



## My Favorite Fitting II: (CEG)

Higgs Recoil Mass Spectrum, $\mu$ channel, $\sqrt{\mathbf{s}}=250 \mathrm{GeV}$, ILD_00


## Mass Resolution vs. Beam Energy Spread

An Important Issue, before give you all the results:

- The Mass Resolution introduced by Beam Energy Spread ( $0.3 \%$ for each beam), is larger than we expected.
By (Gaussian) fitting the left side of the Mass Peak of:
- the Generator Data: $\Delta M_{\text {beam }}=730 \mathrm{MeV}$
- the Simulation Data: $\Delta M_{\text {total }}=870 \mathrm{MeV}$

$$
\begin{aligned}
& \Delta M_{\text {total }}=\Delta M_{\text {beam }} \oplus \Delta M_{\text {detector }} \\
& \Rightarrow \Delta M_{\text {detector }}=470 \mathrm{MeV}
\end{aligned}
$$

Which means:
The Machine Introduced more inaccuracy into the Recoil Mass measurement than our ILD Detector!

In reporting the results: I Will Separate the Stat. Err. of Mh into $\delta M_{\text {beam }}$ and $\delta M_{\text {detector }}$ accordingly .

## Results Summary Table

Results in Blue: according to $500 \mathrm{fb}^{-1}$,
Results in Red: according to $250 \mathrm{fb}^{-1}$, as requested by the ILD LOI.

| Ana. | Pol. | Ch. | $M_{\mathrm{h}}$ stat. err. ( MeV ) |  |  |  |  |  | Cross-Section stat. err. (\%) |  | S/B | $\mathrm{S} / \sqrt{ }(\mathrm{S}+\mathrm{B})$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | $\delta M_{\text {total }}$ |  | $\delta M_{\text {beam }}$ |  | $\delta M_{\text {detector }}$ |  |  |  |  |  |
| SM | $\mathrm{e}^{+} \mathrm{Re}^{-} \mathrm{L}$ | $\mu$ | 44 | 62 | 37 | 52 | 24 | 34 | 3.1 | 4.4 | 0.45 | 39.8 |
|  |  | e | 72 | 102 | 54 | 76 | 47 | 66 | 4.4 | 6.2 | 0.37 | 32.6 |
|  | $\mathrm{e}^{+} \mathrm{Le}^{-} \mathrm{R}$ | $\mu$ | 50 | 71 | 42 | 59 | 27 | 38 | 3.4 | 4.8 | 0.64 | 36.7 |
|  |  | e | 82 | 116 | 62 | 88 | 54 | 76 | 4.8 | 6.8 | 0.52 | 29.0 |
| MI | $\mathrm{e}^{+} \mathrm{R}^{-} \mathrm{L}$ | $\mu$ | 49 | 69 | 41 | 58 | 27 | 38 | 3.8 | 5.4 | 0.26 | 30.6 |
|  |  | e | 100 | 141 | 75 | 106 | 66 | 93 | 5.2 | 7.4 | 0.17 | 22.4 |
|  | $\mathrm{e}^{+} \mathrm{Le}^{-} \mathrm{R}$ | $\mu$ | 52 | 74 | 44 | 62 | 28 | 40 | 3.7 | 5.2 | 0.53 | 33.4 |
|  |  | e | 112 | 158 | 84 | 119 | 73 | 103 | 5.8 | 8.2 | 0.36 | 24.0 |

- The Stat. Err. of $M_{h}$ is separated into $\delta M_{\text {beam }}$ and $\delta M_{\text {detector }}$ according to the $\Delta M_{\text {beam }}$ and $\Delta M_{\text {detector }}$, (different for $\mu \mu \mathrm{X}$ and eeX; for eeX, $\Delta M_{\text {total }}=970 \mathrm{MeV}, \Delta M_{\text {beam }}=730 \mathrm{MeV}$ and $\Delta M_{\text {detector }}=640 \mathrm{MeV}$ )
- Stat. Err.s of Cross-Section are reported relatively (in \%), since the cross-sections are different between two polarization setups


## Conclusions and To Do List

## Conclusions

- Analyses are done and methods are validated for $\mu \mu \mathrm{X}$ and eeX channels, with full polarizations.
- Both fitting methods give the similar good results
- Machine introduced larger error into the Higgs mass measurement than the ILD Detector
- Mh stat. err.s are separated into machine contributions and detector contributions: Helpful for the detector performance study


## To Do List

- Results with LOI requested polarizations (e:+80\%, p:-30\%) and (e:-80\%, p:+30\%) will be given as soon as possible.
- Up to now, no gamma-gamma backgrounds taken into the fittings: results are coming soon.

Kazutoshi is going to give the talk about the gamma-gamma rejection next.

## Thanks!

## Backup Slides

## $\Delta \mathrm{P} / \mathrm{P}^{2}$ criterion in the selection of lepton candidates

- Protect our study from bad measured tracks
- $\Delta \mathrm{P} / \mathrm{P}^{2}$ criterion for our lepton candidates is applied
- With Francois' directions and validations step by step





## Background Rejection Summary Table

| Pol. | Ana. | Cha. | Cuts | $\mu \mu \mathrm{X} /$ eeX | $\mu \mu /$ ee | TT | $\mu \mu v v / e e v v$ | $\mu \mu \mathrm{ff} / \mathrm{eeff}$ | S/B | $\mathrm{S} / \sqrt{ }(\mathrm{S}+\mathrm{B})$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\begin{aligned} & e+R \\ & e-L \end{aligned}$ | SM | $\mu$ | SM cut-chain: | 6130(71.6\%) | 229 | 0 | 16 | 21.9k |  |  |
|  |  |  | + fL $>0.31$ | 5116(59.7\%) | 63 | 0 | 7 | 11.3k | 0.45 | 39.8 |
|  |  | e | SM cut-chain: | 4631(51.8\%) | 456 | 0 | 11 | 20.2k |  |  |
|  |  |  | + fL $>0.33$ | 3939(44.0\%) | 180 | 0 | 6 | 10.5k | 0.37 | 32.6 |
|  | MI | $\mu$ | MI cut-chain: | 5553(64.8\%) | 761 | 0 | 16k | 15.5k |  |  |
|  |  |  | + fL>0.19 | 4600(53.7\%) | 471 | 0 | 8244 | 9297 | 0.53 | 33.4 |
|  |  | e | MI cut-chain: | 3960(44.3\%) | 2706 | 260 | 16.5k | 13k |  |  |
|  |  |  | + fL>0.17 | 3374(37.7\%) | 1524 | 260 | 9403 | 8175 | 0.36 | 24.0 |
| $\begin{aligned} & \text { e+L } \\ & \text { e-R } \end{aligned}$ | SM | $\mu$ | SM cut-chain: | 3947(72.0\%) | 146 | 0 | 0 | 11.0k |  |  |
|  |  |  | + fL>0.27 | 3435(62.6\%) | 31 | 0 | 0 | 5.3k | 0.26 | 30.6 |
|  |  | e | SM cut-chain: | 3947(72.0\%) | 338 | 0 | 2 | 9.9k |  |  |
|  |  |  | + fL>0.30 | 2480(43.9\%) | 112 | 0 | 0 | 4.7k | 0.17 | 22.4 |
|  | MI | $\mu$ | MI cut-chain: | 3605(65.7\%) | 518 | 0 | 1452 | 7309 |  |  |
|  |  |  | + fL>0.24 | 3208(58.5\%) | 362 | 0 | 1075 | 4563 | 0.64 | 36.7 |
|  |  | e | MI cut-chain: | 2511(44.5\%) | 2457 | 195 | 1339 | 6119 |  |  |
|  |  |  | + fL $>0.29$ | 2154(38.2\%) | 1463 | 195 | 837 | 3439 | 0.52 | 29.0 |

## Results

| Pol. | Ch. | Fit. | $\mathrm{M}_{\mathrm{h}}(\mathrm{GeV})$ | Cross-Section (fb) |
| :--- | :--- | :--- | :--- | :--- |
| $\mathrm{e}_{\mathrm{R}}^{+} \mathrm{e}_{\mathrm{L}}^{-}$ | $\mu \mu X$ | GPET | $119.977 \pm 0.044$ | $17.15 \pm 0.54(3.1 \%)$ |
|  |  | CEG | $120.158 \pm 0.046$ | $17.21 \pm 0.54(3.1 \%)$ |
|  | $e e X$ | GPET | $119.954 \pm 0.072$ | $18.38 \pm 0.81(4.4 \%)$ |
|  |  | CEG | $120.226 \pm 0.078$ | $18.35 \pm 0.80(4.4 \%)$ |
| $\mathrm{e}_{\mathrm{L}}^{+} \mathrm{e}_{\mathrm{R}}^{-}$ | $\mu \mu X$ | GPET | $119.981 \pm 0.050$ | $11.31 \pm 0.39(3.4 \%)$ |
|  |  | CEG | $120.069 \pm 0.051$ | $11.33 \pm 0.39(3.4 \%)$ |
|  | $e e X$ | GPET | $119.997 \pm 0.084$ | $11.46 \pm 0.55(4.8 \%)$ |
|  |  | CEG | $120.021 \pm 0.082$ | $11.41 \pm 0.55(4.8 \%)$ |


| Pol. | Ch. | Fit. | $\mathrm{M}_{\mathrm{h}}(\mathrm{GeV})$ | Cross-Section $(\mathrm{fb})$ |
| :--- | :--- | :--- | :--- | :--- |
| $\mathrm{e}_{\mathrm{R}}^{+} \mathrm{e}_{\mathrm{L}}^{-}$ | $\mu \mu X$ | GPET | $119.938 \pm 0.049$ | $16.75 \pm 0.65(3.9 \%)$ |
|  |  | CEG | $120.073 \pm 0.054$ | $16.73 \pm 0.64(3.8 \%)$ |
|  | $e e X$ | GPET | $120.094 \pm 0.110$ | $20.29 \pm 1.06(5.3 \%)$ |
|  |  | CEG | $120.286 \pm 0.100$ | $20.35 \pm 1.06(5.3 \%)$ |
| $\mathrm{e}_{\mathrm{L}}^{+} \mathrm{e}_{\mathrm{R}}^{-}$ |  | GPET | $120.004 \pm 0.052$ | $11.24 \pm 0.42(3.7 \%)$ |
|  |  | CEG | $120.102 \pm 0.054$ | $11.05 \pm 0.41(3.7 \%)$ |
|  | $e e X$ | GPET | $119.981 \pm 0.112$ | $10.79 \pm 0.63(5.8 \%)$ |
|  |  | CEG | $119.922 \pm 0.112$ | $10.77 \pm 0.63(5.8 \%)$ |

## SM Rejection

| $\mathrm{N}_{\text {evts }}$ Remained: | $\mu \mu X$ | $\mu \mu$ | $\tau \tau$ | $\mu \mu \nu \nu$ |
| :--- | :--- | :--- | :--- | :--- |
| Before any restriction: | 8563 | 8.5 M | 8.6 M | 425 k |
| Both $\mu$ identified | $8169(95.4 \%)$ |  | $257 \mathrm{k}(3 \%)$ | $374 \mathrm{k}(88.1 \%)$ |
| + pre-cuts | $7166(83.7 \%)$ | $143 \mathrm{k}(1.7 \%)$ | $17 \mathrm{k}(0.2 \%)$ | $54 \mathrm{k}(12.6 \%)$ |
| $+\mathrm{N}_{\text {add. } \mathrm{TK}}>1$ | $7112(83.0 \%)$ | $8.8 \mathrm{k}(0.10 \%)$ | $2 \mathrm{k}(0.025 \%)$ | $959(0.23 \%)$ |
| $+\Delta \theta_{2 \mathrm{tk}}>0.01$ | $7100(82.9 \%)$ | $819(0.01 \%)$ | $1558(0.02 \%)$ | $122(0.03 \%)$ |
| $+\Delta \theta_{\min }>0.01$ | $7000(81.7 \%)$ | $506(0.006 \%)$ | $346(0.004 \%)$ | $18(0.004 \%)$ |
| $+\mathrm{acop}(0.2,3.0)$ | $6495(75.8 \%)$ | $354(0.004 \%)$ | $0(0 \%)$ | $18(0.004 \%)$ |
| $+\mathrm{M}_{\mathrm{h}}(115,150) \mathrm{GeV}$ | $6130(71.6 \%)$ | $229(0.003 \%)$ | $0(0 \%)$ | $16(0.004 \%)$ |

Table 4: Number of events remained after each cuts for $\mu \mu \mathrm{X}$, Polarization $\mathrm{e}_{\mathrm{R}}^{+} \mathrm{e}_{\mathrm{L}}^{-}$

| $\mathrm{N}_{\text {evts }}$ Remained: | $e e X$ | $e e$ | $\tau \tau$ | $e e \nu \nu$ |
| :--- | :--- | :--- | :--- | :--- |
| Before any restriction: | 8588 | 8.7 G | 8.6 M | 508 k |
| Both e identified | $8439(98.3 \%)$ |  | $965 \mathrm{k}(11.3 \%)$ | $415 \mathrm{k}(81.6 \%)$ |
| + pre-cuts | $5593(62.5 \%)$ | $267 \mathrm{k}(0.003 \%)$ | $29 \mathrm{k}(0.3 \%)$ | $61 \mathrm{k}(12.1 \%)$ |
| $+\mathrm{N}_{\text {add.TK }}>1$ | $5548(62.0 \%)$ | $16 \mathrm{k}\left(2 \times 10^{-6}\right)$ | $8309(0.1 \%)$ | $1708(0.34 \%)$ |
| $+\Delta \theta_{2 \mathrm{tk}}>0.01$ | $5540(61.9 \%)$ | $2607\left(3 \times 10^{-7}\right)$ | $5885\left(7 \times 10^{-4}\right)$ | $279(0.05 \%)$ |
| $+\Delta \theta_{\min }>0.01$ | $5448(60.9 \%)$ | $844\left(1 \times 10^{-7}\right)$ | $1212\left(1 \times 10^{-4}\right)$ | $31(0.006 \%)$ |
| $+\operatorname{acop}(0.2,3.0)$ | $5054(56.5 \%)$ | $712\left(8 \times 10^{-8}\right)$ | $0(0 \%)$ | $30(0.006 \%)$ |
| $+\mathrm{M}_{\mathrm{h}}(115,150) \mathrm{GeV}$ | $4631(51.8 \%)$ | $456\left(5 \times 10^{-8}\right)$ | $0(0 \%)$ | $11(0.002 \%)$ |

Table 5: Number of events remained after each cuts for eeX, Polarization $\mathrm{e}_{\mathrm{R}}^{+} \mathrm{e}_{\mathrm{L}}^{-}$

## SM Rejection

| $\mathrm{N}_{\text {evts }}$ Remained: | $\mu \mu X$ | $\mu \mu$ | $\tau \tau$ | $\mu \mu \nu \nu$ |
| :--- | :--- | :--- | :--- | :--- |
| Before any restriction: | 5484 | 6.4 M | 6.4 M | 22.5 k |
| Both $\mu$ identified | $5248(95.7 \%)$ |  | $193 \mathrm{k}(3 \%)$ | $17.8 \mathrm{k}(79.2 \%)$ |
| + pre-cuts | $4620(84.2 \%)$ | $93.5 \mathrm{k}(1.5 \%)$ | $13.4 \mathrm{k}(0.2 \%)$ | $3883(17.3 \%)$ |
| $+\mathrm{N}_{\text {add. }} \mathrm{TK}>1$ | $4592(83.7 \%)$ | $5680(0.09 \%)$ | $1626(0.025 \%)$ | $58(0.26 \%)$ |
| $+\Delta \theta_{2 \mathrm{tk}}>0.01$ | $4584(83.6 \%)$ | $526(0.008 \%)$ | $1171(0.02 \%)$ | $6(0.03 \%)$ |
| $+\Delta \theta_{\min }>0.01$ | $4513(82.3 \%)$ | $335(0.005 \%)$ | $260(0.004 \%)$ | $0(0 \%)$ |
| $+\operatorname{acop}(0.2,3.0)$ | $4172(76.1 \%)$ | $249(0.004 \%)$ | $0(0 \%)$ | $0(0 \%)$ |
| $+\mathrm{M}_{\mathrm{h}}(115,150) \mathrm{GeV}$ | $3947(72.0 \%)$ | $146(0.002 \%)$ | $0(0 \%)$ | $0(0 \%)$ |

Table 6: Number of events remained after each cuts for $\mu \mu \mathrm{X}$, Polarization $\mathrm{e}_{\mathrm{L}}^{+} \mathrm{e}_{\mathrm{R}}^{-}$

| $\mathrm{N}_{\text {evts }}$ Remained: | $e e X$ | $e e$ | $\tau \tau$ | $e e \nu \nu$ |
| :--- | :--- | :--- | :--- | :--- |
| Before any restriction: | 5645 | 8.7 G | 6.4 M | 35.2 k |
| Both e identified | $5544(98.2 \%)$ |  | $725 \mathrm{k}(11.3 \%)$ | $21.6 \mathrm{k}(61.3 \%)$ |
|  | + pre-cuts | $3534(62.6 \%)$ | $241 \mathrm{k}(0.003 \%)$ | $22 \mathrm{k}(0.3 \%)$ |
| $+\mathrm{N}_{\text {add.TK }}>1$ | $3503(62.1 \%)$ | $14.6 \mathrm{k}\left(1.7 \times 10^{-6}\right)$ | $6244(0.1 \%)$ | $71(0.2 \%)$ |
| $+\Delta \theta_{2 \mathrm{tk}}>0.01$ | $3497(61.9 \%)$ | $2216\left(3 \times 10^{-7}\right)$ | $4423(0.07 \%)$ | $8(0.02 \%)$ |
| $+\Delta \theta_{\min }>0.01$ | $3445(61.0 \%)$ | $645\left(7 \times 10^{-8}\right)$ | $911(0.01 \%)$ | $2(0.0006 \%)$ |
| $+\operatorname{acop}(0.2,3.0)$ | $3209(56.9 \%)$ | $552\left(6 \times 10^{-8}\right)$ | $0(0 \%)$ | $2(0.006 \%)$ |
| $+\mathrm{M}_{\mathrm{h}}(115,150) \mathrm{GeV}$ | $2935(52.0 \%)$ | $338\left(4 \times 10^{-8}\right)$ | $0(0 \%)$ | $2(0.006 \%)$ |

Table 7: Number of events remained after each cuts for eeX, Polarization $e_{L}^{+} e_{R}^{-}$

## MI Rejection

| $\mathrm{N}_{\text {evts }}$ Remained: | $\mu \mu X$ | $\mu \mu$ | $\tau \tau$ | $\mu \mu \nu \nu$ | $\mu \mu f f$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Before any restriction | 8563 | 8.5M | 8.6M | 425k | 710k |
| + Both $\mu$ identified | 8169.5 (95.4\%) | 143k (1.7\%) | 257k (3.0\%) | 374 k (88.1\%) | $\begin{aligned} & 432 \mathrm{k}(60.9 \%) \\ & 48 \mathrm{k}(6.7 \%) \end{aligned}$ |
| + pre-cuts | 7166 (83.7\%) |  | 18k (0.2\%) | 53k (12.6\%) |  |
| $+P_{\text {Tdl }}>20 \mathrm{GeV}$ | 6777 (79.1\%) | 71k (0.81\%) | 12k (0.14\%) | 46k (10.8\%) | 38k (5.4\%) |
| $+M_{d l} \in(80,100) G e V$ | 6230 (72.7\%) | 54k (0.64\%) | 6578 (0.08\%) | 27k (6.4\%) | 30k (4.2\%) |
| + acop $\in(0.2,3.0)$ | 5827 (68.0\%) | 45k (0.53\%) | 0 (0\%) | 25k (6.0\%) | 27k (3.8\%) |
| $+\Delta P_{\text {Tbal. }}>10 \mathrm{GeV}$ | 5712 (66.7\%) | 2618 (0.03\%) | 0 (0\%) | 23k (5.5\%) | 25k (3.6\%) |
| $+\left\|\Delta \theta_{2 t k}\right\|>0.01$ | 5704 (66.6\%) | 1044 (0.01\%) | 0 (0\%) | 23k (5.4\%) | 25k (3.6\%) |
| $+M_{\text {recoil }} \in(115,150) \mathrm{GeV}$ | 5553 (64.8\%) | 761 (0.009\%) | 0 (0\%) | 16k (3.8\%) | 15.5k (2.2\%) |

Table 13: Number of events remained after each cuts for $\mu \mu \mathrm{X}$, Polarization $\mathrm{e}_{\mathrm{R}}^{+} \mathrm{e}_{\mathrm{L}}^{-}$.

| $\mathrm{N}_{\text {evts }}$ Remained: | $e e X$ | $e e$ | $\tau \tau$ | $e e \nu \nu$ | $e e f f$ |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Before any restriction | 8588 | 8.7 G | 8.6 M | 508 k | 2.2 M |
| + Both $\mu$ identified | $8791(98.3 \%)$ |  | $965 \mathrm{k}(11.3 \%)$ | $415 \mathrm{k}(81.7 \%)$ | $880 \mathrm{k}(40.0 \%)$ |
| + pre-cuts | $5593(62.5 \%)$ | $267 \mathrm{k}(0.003 \%)$ | $29 \mathrm{k}(0.34 \%)$ | $61 \mathrm{k}(12.1 \%)$ | $41 \mathrm{k}(1.8 \%)$ |
| $+P_{\text {Tdl }}>20 \mathrm{GeV}$ | $5283(59.1 \%)$ | $195(0.002 \%)$ | $20 \mathrm{k}(0.24 \%)$ | $53 \mathrm{k}(10.4 \%)$ | $35 \mathrm{k}(1.6 \%)$ |
| $+M_{d l} \in(80,100) \mathrm{GeV}$ | $4508(50.4 \%)$ | $108(0.001 \%)$ | $12(0.14 \%)$ | $29 \mathrm{k}(5.8 \%)$ | $25 \mathrm{k}(1.1 \%)$ |
| + acop $\in(0.2,3.0)$ | $4211(47.1 \%)$ | $98 \mathrm{k}(0.001 \%)$ | $866(0.01 \%)$ | $28(5.4 \%)$ | $23 \mathrm{k}(1.0 \%)$ |
| $+\Delta P_{\text {Tbal. }}>10 \mathrm{GeV}$ | $4095(45.8 \%)$ | $6618\left(8 \times 10^{-7}\right)$ | $606(0.007 \%)$ | $24 \mathrm{k}(4.7 \%)$ | $22 \mathrm{k}(0.98 \%)$ |
| $+\left\|\Delta \theta_{2 t \mathrm{k}}\right\|>0.01$ | $4089(45.7 \%)$ | $3660\left(4 \times 10^{-7}\right)$ | $519(0.006 \%)$ | $23.5 \mathrm{k}(4.6 \%)$ | $21.5 \mathrm{k}(0.98 \%)$ |
| $+M_{\text {recoil }} \in(115,150) \mathrm{GeV}$ | $3960(44.3 \%)$ | $2706\left(3 \times 10^{-7}\right)$ | $260(0.003 \%)$ | $16.5 \mathrm{k}(3.3 \%)$ | $13 \mathrm{k}(0.59 \%)$ |

Table 14: Number of events remained after each cuts for eeX, Polarization $e_{R}^{+} e_{L}^{-}$.

## MI Rejection

| $\mathrm{N}_{\text {evts }}$ Remained: | $\mu \mu X$ | $\mu \mu$ | $\tau \tau$ | $\mu \mu \nu \nu$ | $\mu \mu f f$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Before any restriction | 5484 | 6.4 M | 6.4 M | 22.5 k | 629.6k |
| + Both $\mu$ identified | 5248 (95.7\%) | 93k (1.5\%) | 193k (3.0\%) | 17.8k (79.2\%) | $\begin{aligned} & 363(57.6 \%) \\ & 26 \mathrm{k}(4.2 \%) \end{aligned}$ |
| + pre-cuts | 4620 (84.2\%) |  | 13k (0.21\%) | 3883 (17.3\%) |  |
| $+P_{T d l}>20 \mathrm{GeV}$ | 4380 (79.9\%) | 47k (0.74\%) | 9041 (0.14\%) | 3478 (15.5\%) | 19k (3.1\%) |
| $+M_{d l} \in(80,100) \mathrm{GeV}$ | 4046 (73.8\%) | 36k (0.56\%) | 4943 (0.08\%) | 2692 (12.0\%) | 14k (2.2\%) |
| + acop $\in(0.2,3.0)$ | 3771 (68.8\%) | 29k (0.46\%) | 0 (0\%) | 2492 (11.1\%) | 13k (2.0\%) |
| $+\Delta P_{\text {Tbal. }}>10 \mathrm{GeV}$ | 3697 (67.4\%) | 1701 (0.027\%) | 0 (0\%) | 2421 (10.8\%) | 11.8k (1.9\%) |
| $+\left\|\Delta \theta_{2 t k}\right\|>0.01$ | 3692 (67.3\%) | 710 (0.011\%) | 0 (0\%) | 2392 (10.6\%) | 11.7k (1.9\%) |
| $+M_{\text {recoil }} \in(115,150) \mathrm{GeV}$ | 3605 (65.7\%) | 518 (0.008\%) | 0 (0\%) | 1452 (6.5\%) | 7309 (1.2\%) |

Table 15: Number of events remained after each cuts for $\mu \mu \mathrm{X}$, Polarization $\mathrm{e}_{\mathrm{L}}^{+} \mathrm{e}_{\mathrm{R}}^{-}$.

| $\mathrm{N}_{\text {evts }}$ Remained: | $e e X$ | $e e$ | $\tau \tau$ | $e e \nu \nu$ | $e e f f$ |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Before any restriction | 5645 | 8.7 G | 6.4 M | 35200 | 2.1 M |
| + Both $\mu$ identified | $5544(98.2 \%)$ |  | $725 \mathrm{k}(11.3 \%)$ | $22 \mathrm{k}(61.4 \%)$ | $773 \mathrm{k}(36.8 \%)$ |
|  | $3534(62.6 \%)$ | $241 \mathrm{k}(0.0028 \%)$ | $22 \mathrm{k}(0.34 \%)$ | $3998(11.4 \%)$ | $21 \mathrm{k}(1.0 \%)$ |
| + pre-cuts | $3334(59.1 \%)$ | $182 \mathrm{k}(0.002 \%)$ | $15 \mathrm{k}(0.24 \%)$ | $3562(10.1 \%)$ | $18(0.8 \%)$ |
| $+P_{\text {Tdl }}>20 \mathrm{GeV}$ | $2845(50.4 \%)$ | $98 \mathrm{k}(0.001 \%)$ | $8781(0.14 \%)$ | $2495(7.1 \%)$ | $12 \mathrm{k}(0.57 \%)$ |
| $+M_{d l} \in(80,100) \mathrm{GeV}$ | $2673(47.4 \%)$ | $89 \mathrm{k}(0.001 \%)$ | $650(0.01 \%)$ | $2317(6.6 \%)$ | $11 \mathrm{k}(0.52 \%)$ |
| + acop $\in(0.2,3.0)$ | $2606(46.2 \%)$ | $5984\left(7 \times 10^{-7}\right)$ | $455(0.007 \%)$ | $2221(6.3 \%)$ | $10 \mathrm{k}(0.48 \%)$ |
| $+\Delta P_{\text {Tbal. }}>10 \mathrm{GeV}$ | $2602(46.1 \%)$ | $3307\left(4 \times 10^{-7}\right)$ | $390(0.006 \%)$ | $2191(6.2 \%)$ | $10 \mathrm{k}(0.48 \%)$ |
| $+\left\|\Delta \theta_{2 t \mathrm{k}}\right\|>0.01$ | $2457\left(3 \times 10^{-7}\right)$ | $195(0.003 \%)$ | $1339(3.8 \%)$ | $6119(0.29 \%)$ |  |
| $+M_{\text {recoil }} \in(115,150) \mathrm{GeV}$ | $2511(44.5 \%)$ | $2457(3)$ |  |  |  |

Table 16: Number of events remained after each cuts for eeX, Polarization $e_{L}^{+} e_{R}^{-}$.

