

# Rigidity of the cryostat

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## Contents

Introduction

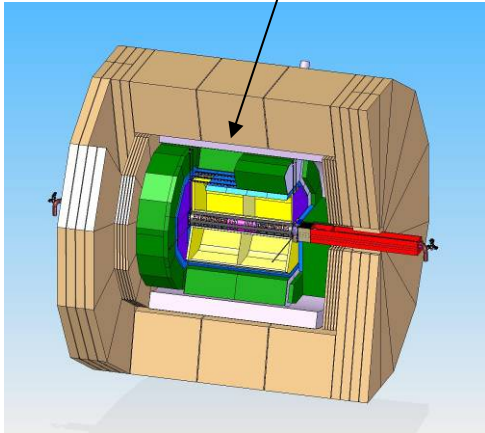
Calculations

- Thermal shrinkage
- H-Cal weight
- Unbalanced force
- Combined force

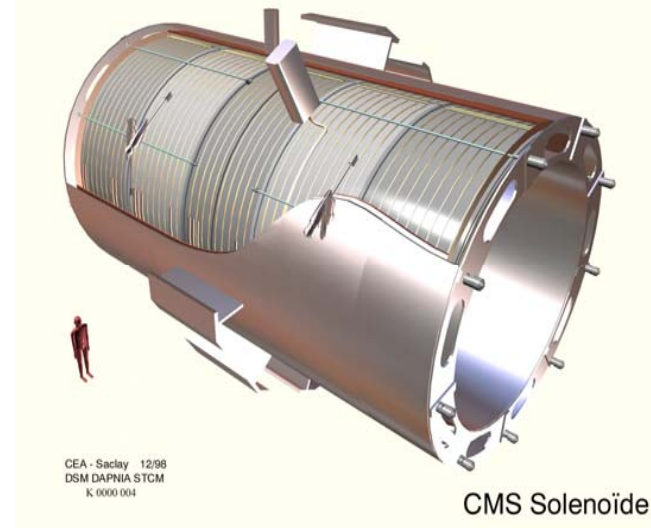
Conclusion

# Introduction

Mechanical strength of the cryostat and the support system has been studied.



The support system of the CMS solenoid was referred in this calculation.



## Load condition against;

1. Thermal shrinkage:  $\Delta t=300K$
2. Cold mass: 180tonnes
3. Vacuum pressure: 1atm
4. H-Cal. Weight: 701tonnes
5. Unbalanced force: 840kN in Z-dir.  
→ Not calculated. Referred from the CMS.
6. Combined calculation with above forces

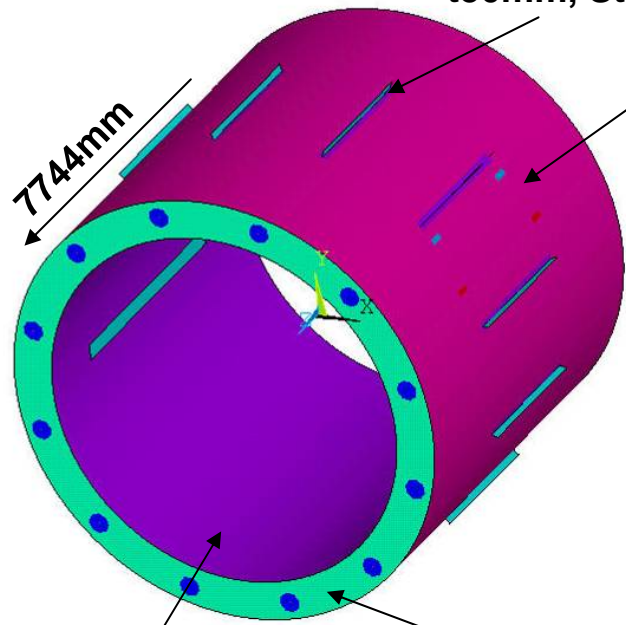
B. 0.15G of horizontal force.

## Referred parameters (Old version)

		ILD0	ILD
2			
3	magnet	4T, 1,7 GJ	
4	Barrel Y Rin		4270
5	Barrel Y Rout	6420??	
6	Barrel 1/2 length		4647
7	thick	2150??	
8	Yoke plug front		3922
9	Yoke plug back		4022
10	Yoke plug Rin		350
11	Yoke plug Rout		3190
12	thick	100	
13	Yoke nose front	4022	
14	Yoke nose back	4672	
15	Yoke nose Rin	350	
16	Yoke nose Rout	4070	
17		650	
18	Yoke endcap front	4672	
19	Yoke endcap back	6362	
20	Yoke endcap Rin	350	
21	Yoke endcap Rout	6420??	
22			
23	Coil cryostat		
24	Rin		3440
25	Rout		4190
26	cryo 1/2 length		3872
27	thick	750	
28	Coil Rin		3590
29	Coil Rout		3940
30	coil 1/2 length		3672
		SS/Scinti, 5.3 λ, max 48 layers barrel, 48	

# FEM model

## Cryostat

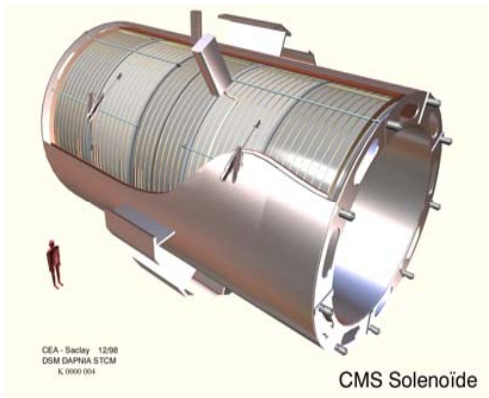


Solenoid support:  
t50mm, Stainless

Outer vac. Wall:  
t50mm, Stainless  
→ R4190mm

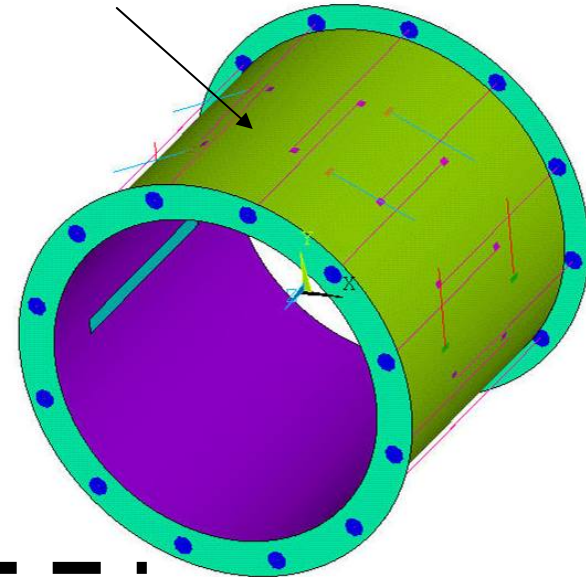
Inner vac. wall:  
t60mm, Stainless  
→ R3440mm

Bulk head: t50mm  
(Stainless steel)



## Coil:

t350mm, Al-alloy  
→ R3765mm, L= 7344mm



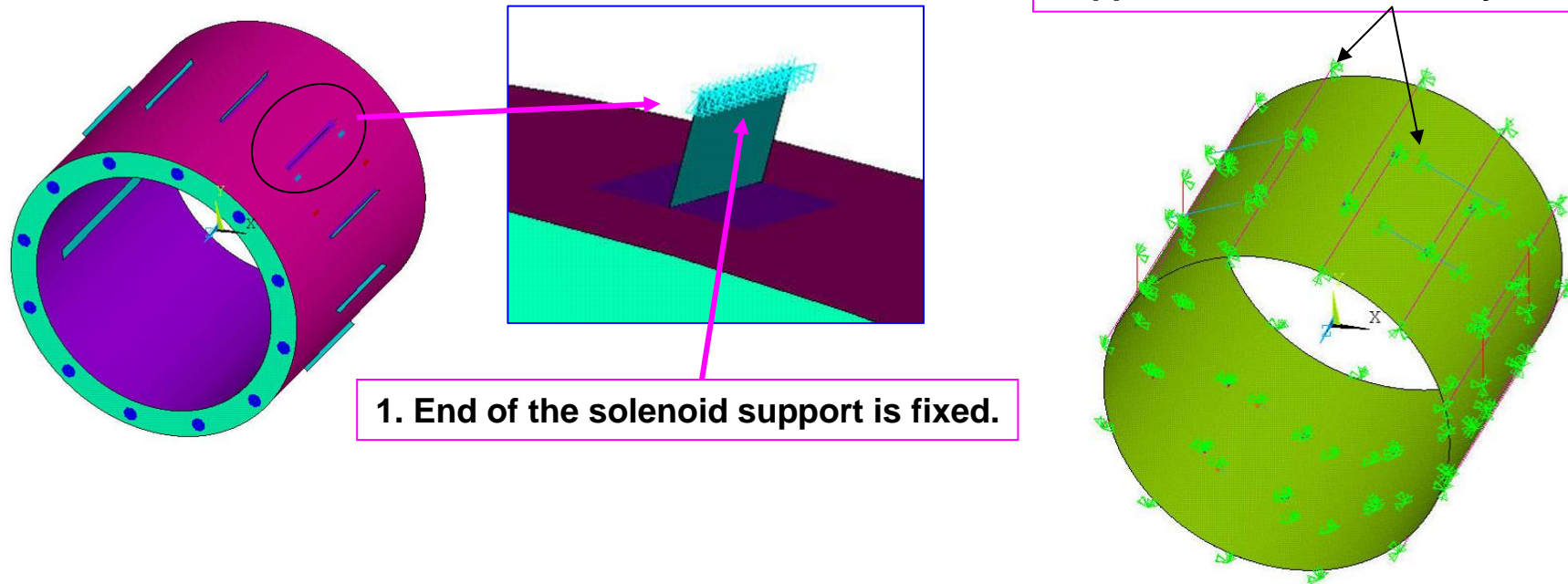
## Support rods

Z-support rods:  
24 x dia.45mm, Titanium alloy

Radial support rods:  
8 x dia.35mm, Ti-alloy

Vertical support rods:  
4 x dia.60mm, Ti-alloy

## Constraints positions



## Load conditions

1. Thermal shrinkage:  $\Delta t=300\text{K}$
2. Cold mass: 180tonnes
3. Vacuum pressure: 1atm
4. H-Cal. Weight: 701tonnes
5. Unbalanced force: 840kN in Z-dir.  
→ Not calculated. Referred from the CMS.
6. Combined calculation with above forces

B. 0.15G of horizontal force.

## Material properties

### 1. Stainless steel

$E=210\text{GPa}$ ,  $\nu=0.3$ ,  $\gamma=7.85$ ,  $\alpha=10\text{e-}5/\text{K}$

### 2. Coil

$E=77\text{GPa}$ ,  $\nu=0.3$ ,  $\gamma=3.0$ ,  $\alpha=14\text{e-}5/\text{K}$

### 3. Ti-alloy

$E=133\text{GPa}$ ,  $\nu=0.33$ ,  $\gamma=4.5$ ,  $\alpha=6\text{e-}5/\text{K}$

# Calculation-1

Condition: The Coil is cooling down to LHe temp.

→ dt= 300K

$$dR = \alpha \cdot dt \cdot R$$

$$= 14 \times 10^{-6} \cdot 300 \cdot 3765$$

$$= 16mm$$

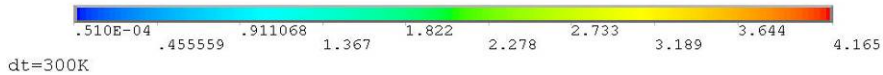
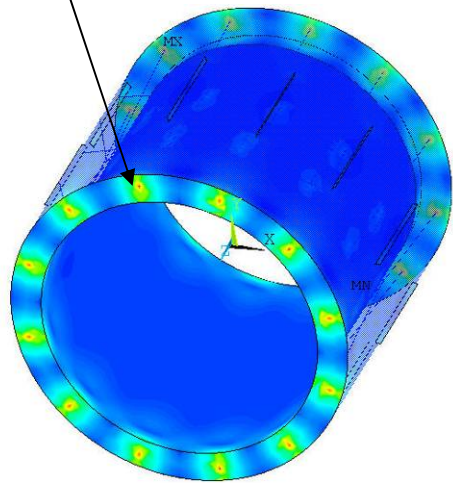
$$dL = \alpha \cdot dt \cdot L$$

$$= 14 \times 10^{-6} \cdot 300 \cdot 3672$$

$$= 15mm$$

Von. M Stress : 41MPa

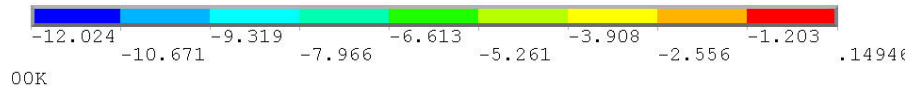
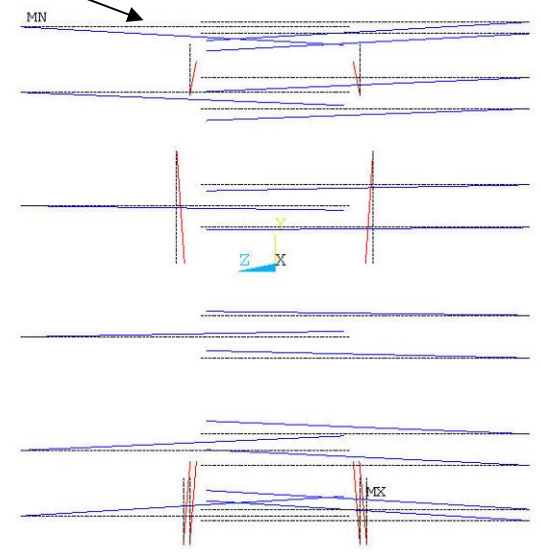
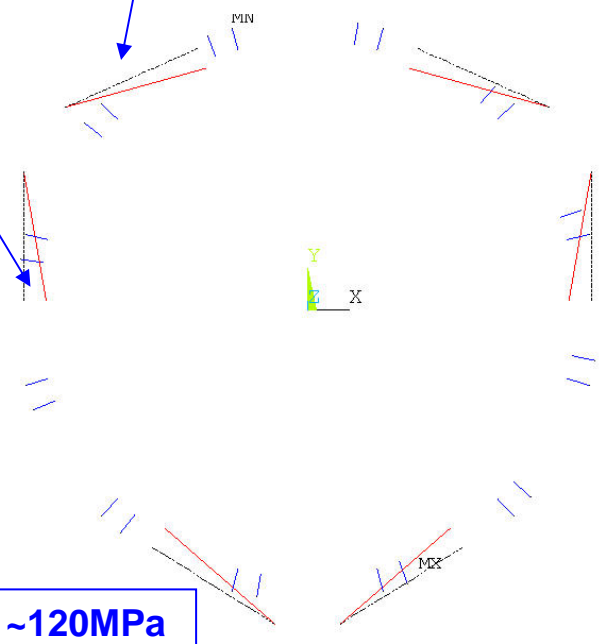
SEQV (AVG)  
DMX =22.495  
SMN =.510E-04  
SMX =4.165



Radial support rods: ~0MPa

Vertical support rods: ~0MPa

Z-support rods: ~120MPa





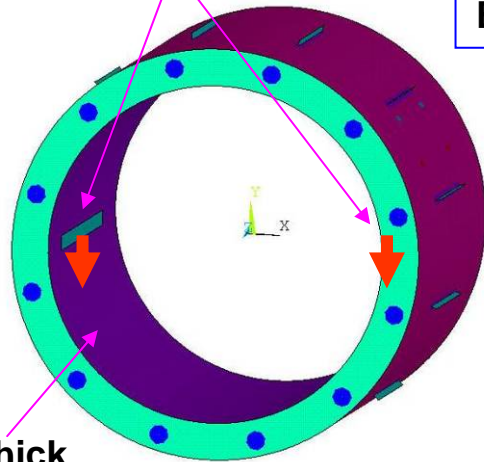
# Calculation-2

Condition: Cal-weight on the inner wall.

→  $W_{cal} = 701$ tonnes

B. Hcal=626tonnes  
B. Ecal= 75tonns

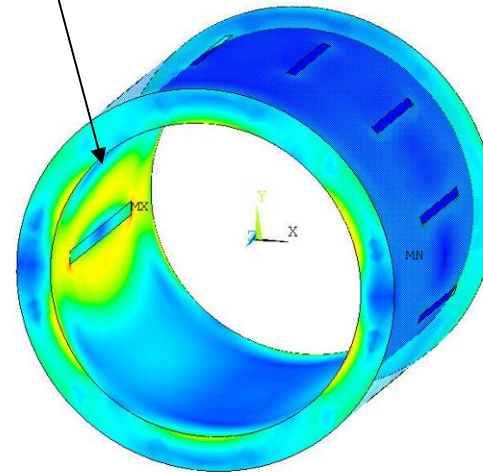
60mm-thick  
Stainless steel



Von. M Stress : 45MPa

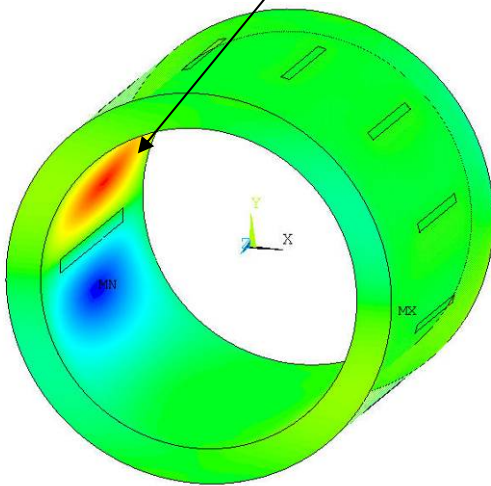
t60: 45MPa  
t50: 63MPa  
t40: 119MPa

(AVG)  
3.224  
.117E-04  
4.547



2.7mm(Horizontal-dir.)

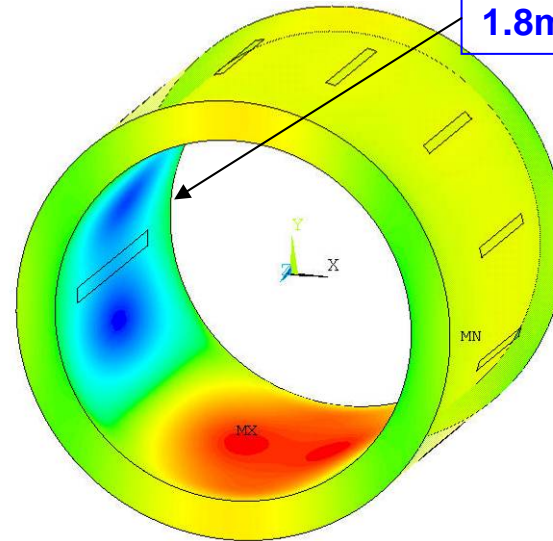
(AVG)  
3.224  
-2.665  
2.666



t60: 2.7mm  
t50: 3.7mm  
t40: 5.4mm

1.8mm(Verical-dir.)

(AVG)  
3.224  
-1.816  
.602939



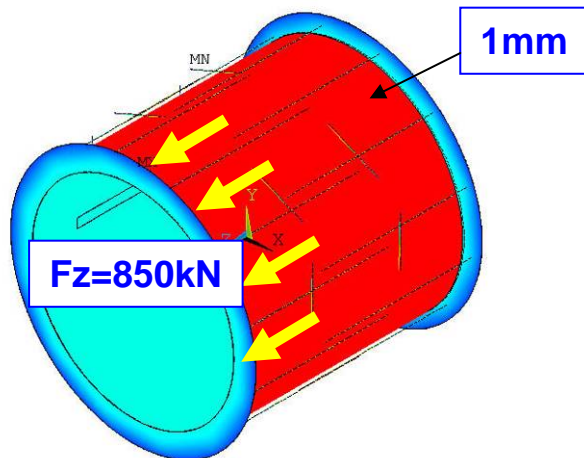
t60: 1.8mm  
t50: 2.3mm  
t40: 3.0mm



# Calculation-3 Condition: Unbalanced force in Z-direction → $F_z = 850\text{kN}$

## Deformation of the coil

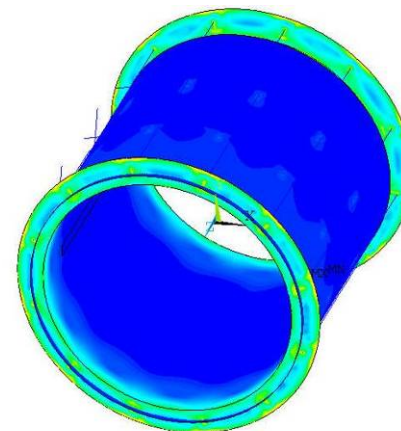
USUM (AVG)  
 RSYS=0  
 DMX =1.015  
 SMN =.002117  
 SMX =1.015



Unbalanced force: Z--> 850kN

## Von. M Stress on the bulkheads: 10MPa

SEQV (AVG)  
 DMX =1.015  
 SMN =.116E-04  
 SMX =1.078

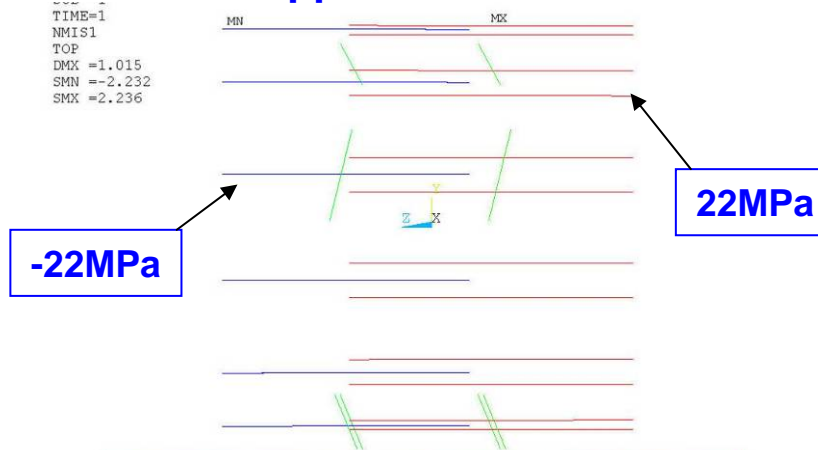


Unbalanced force: Z--> 850kN

**\*) The unbalanced force of the ILD solenoid has not been calculated yet. A 850kN was taken from calculation results of the CMS solenoid.**

## Stress in the support rods.

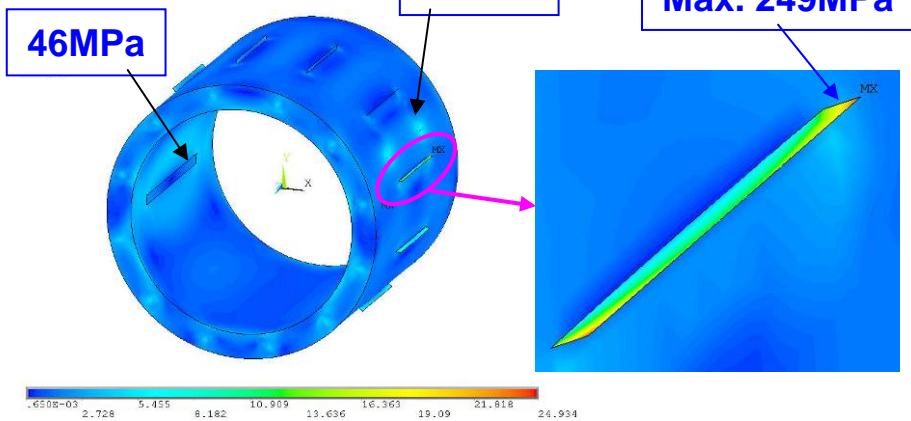
TIME=1  
 NMIS1  
 TOP  
 DMX =1.015  
 SMN =-2.232  
 SMX =2.236



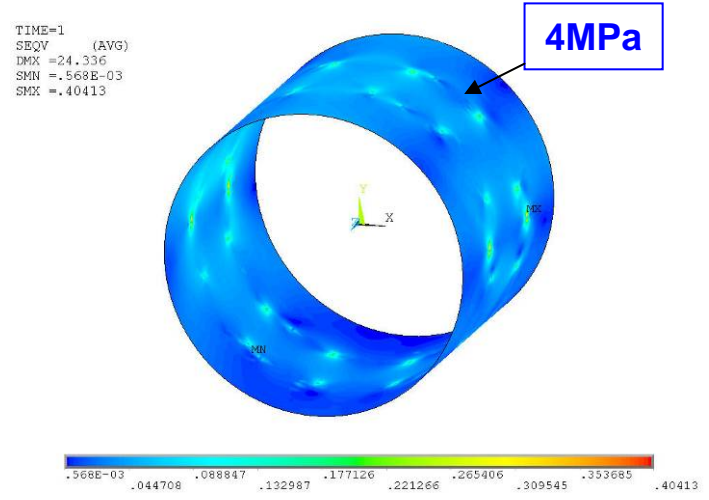
Unbalanced force: Z--> 850kN

## Calculation-4 Condition: *Combined with all forces*

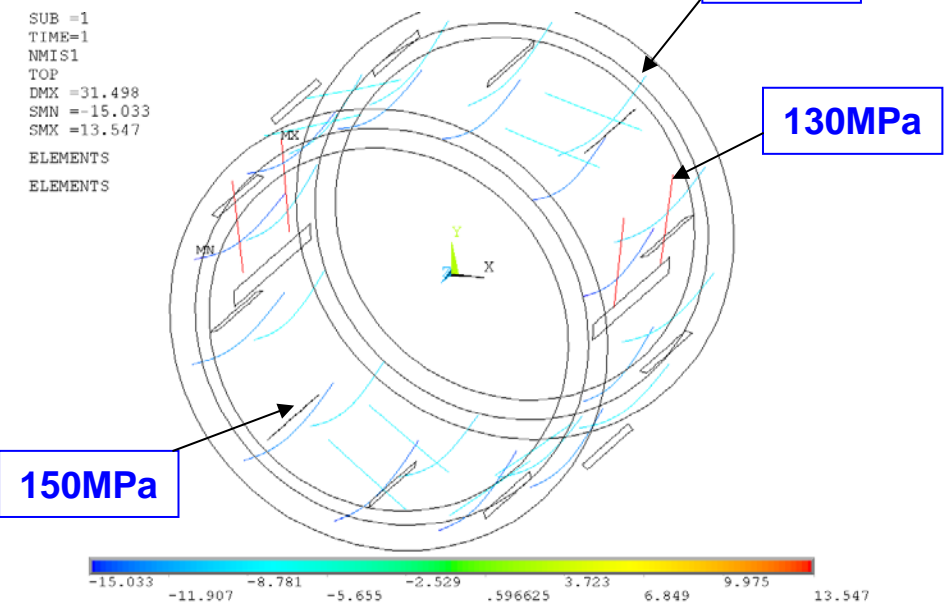
Stress: Cryostat



Stress on the coil: Small enough  
 \*) Stress due to the excitation is not included.



Stress: Support rods

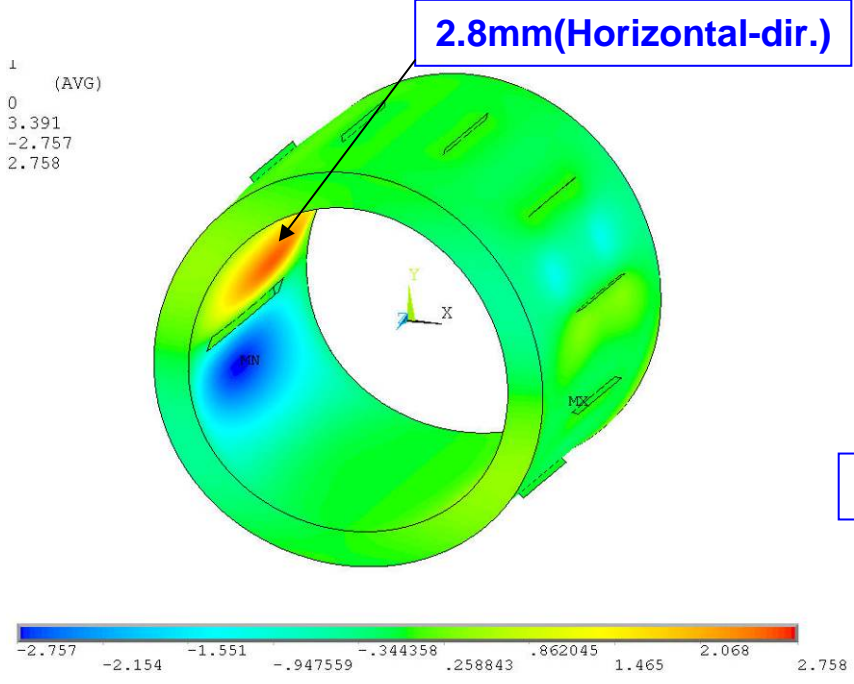
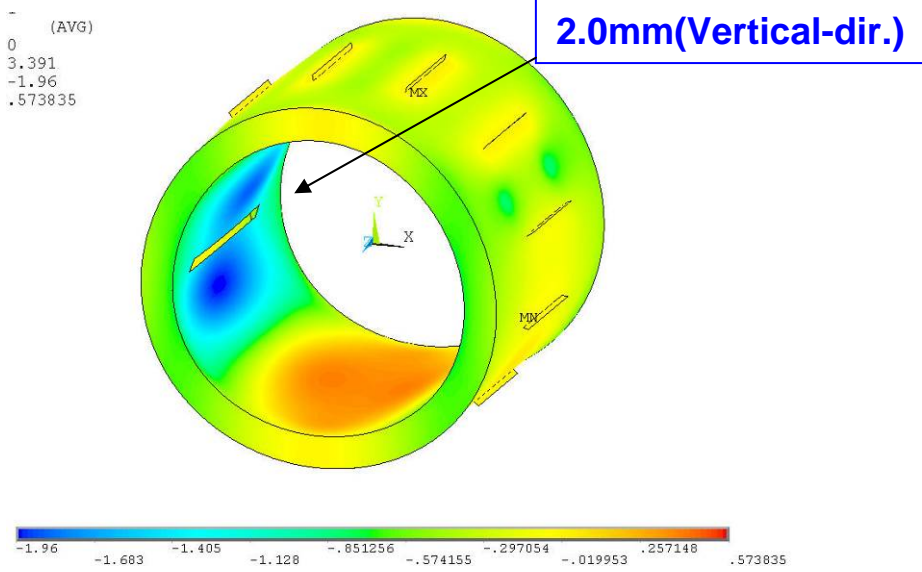


- Combined with the below forces;
1. Thermal shrinkage:  $dt=300K$
  2. Cold mass: 180tonnes
  3. Vacuum pressure: 1atm
  4. H-Cal. Weight: 701tonnes
  5. Unbalanced force: 840kN in Z-dir.
- Not calculated. Referred from the CMS.

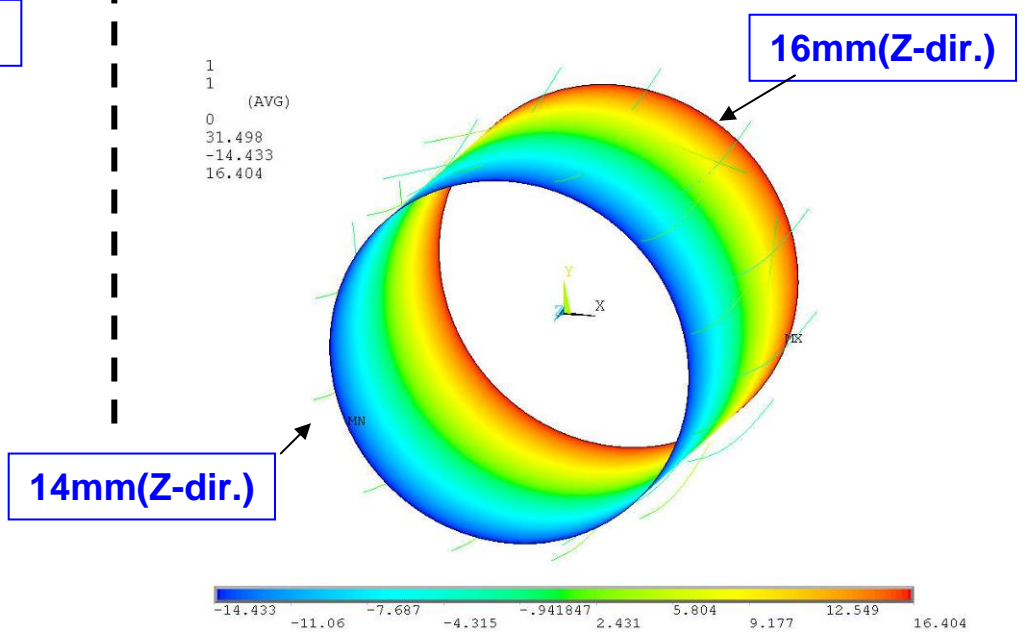
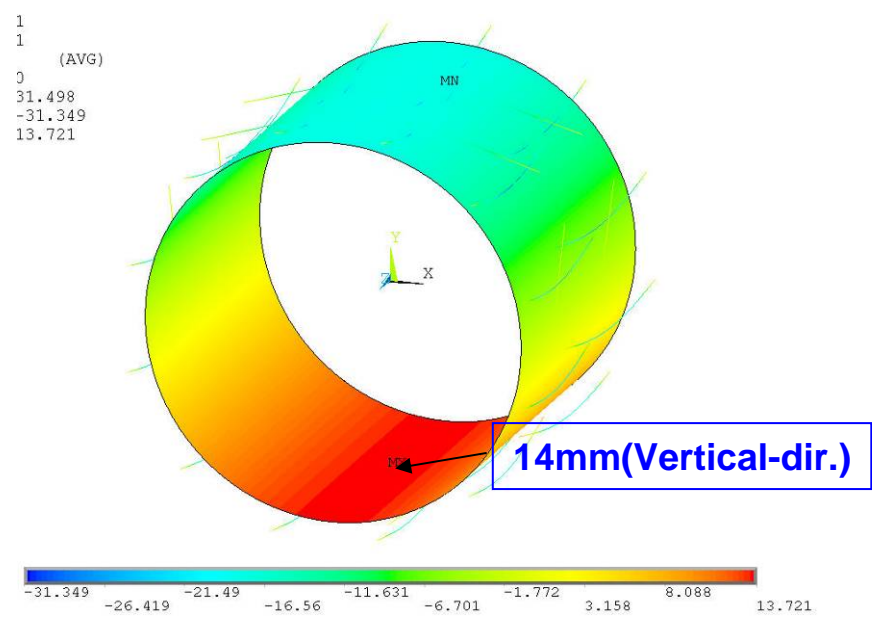


# Calculation-4 Condition: *Combined with all forces*

## Deformation of the cryostat



## Deformation of the coil



# Calculation-5

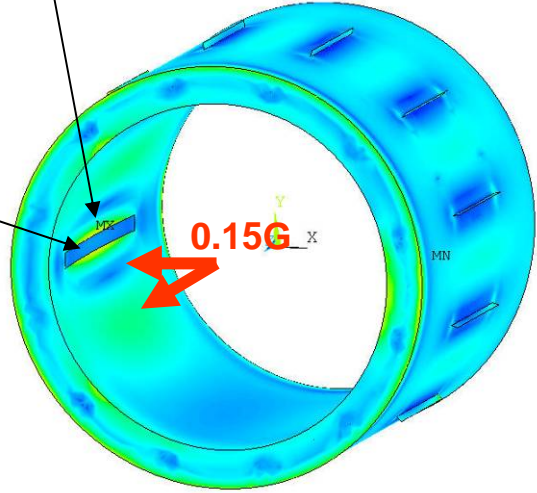
Condition: 0.15G in the horizontal direction.

*\*) Effect of the thermal shrinkage is not included.*

Von. M Stress : 42MPa

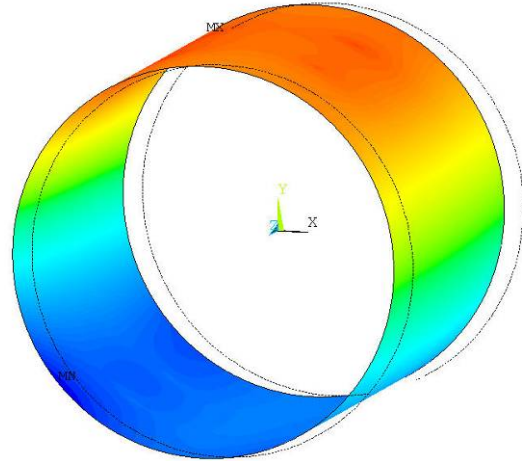
(AVG)  
3.781  
.141E-03  
1.233

3.8mm



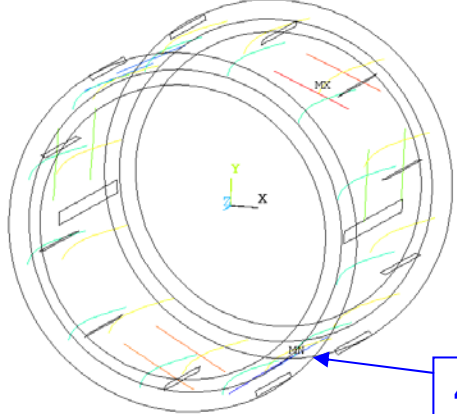
Deformation - Coil : 0.8mm

(AVG)  
0  
.800227  
-.752639  
-.701111

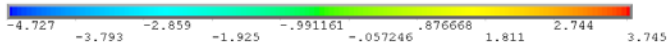


Stress - Support rods

-1  
1  
=3.781  
=-4.794  
=3.745  
ENTS

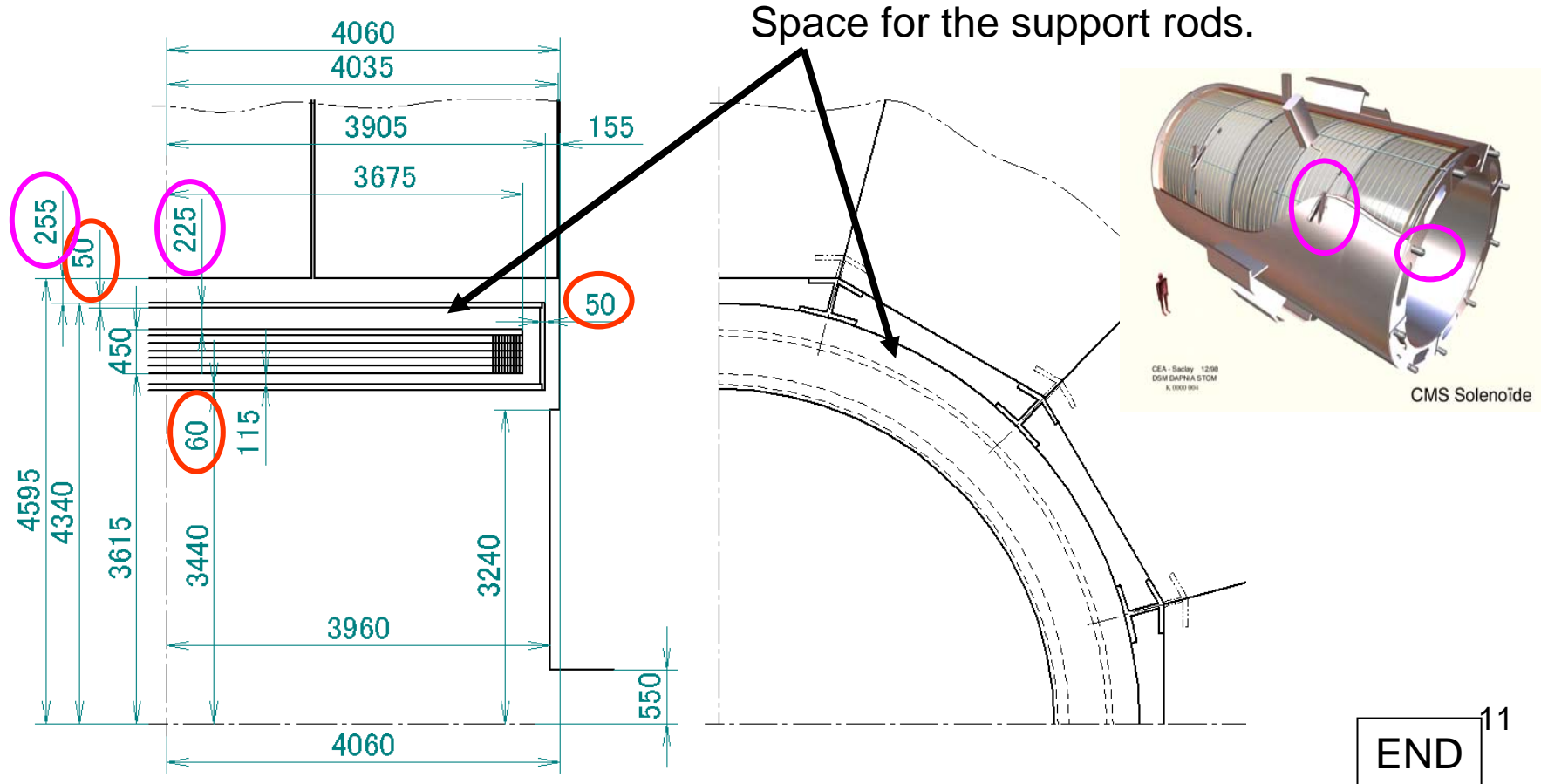


47MPa@R-sup.



# Conclusion

		Cryostat	Coil	R-supp.	V-supp.	Z-supp.	Cryostat		Coil		
		(MPa)	(MPa)	(MPa)	(MPa)	(MPa)	Hori.(mm)	UD(mm)	Hori.(mm)	UD(mm)	Z-dir.(mm)
Thermal shrinkage	dt=300K	41.0		0.0	0.0	120.0		0.0	-16.0	-16.0	-15.0
Cold mass	180tonnes	64.0		0.0	138.0	0.0		0.0	2.3	2.4	
Vac. Pressure	1atm	14.0					0.3	0.3			
Cal.weight	701tonnes	45.0					2.7	1.8			
Shifted force(Z-dir.)	850kN	10.0		0.0	0.0	22.0	0.0	0.0	0.0	0.0	1.0
<b>Combined force</b>		<b>96.0</b>	<b>4.0</b>	<b>10.0</b>	<b>130.0</b>	<b>150.0</b>	<b>2.8</b>	<b>2.0</b>	<b>-14.0</b>	<b>-14.0</b>	<b>-16.0</b>
0.15G (horizontal)		42.0		47.0		18.0	3.8		0.8	0.3	-16.0



Ref.

# Calculation-2

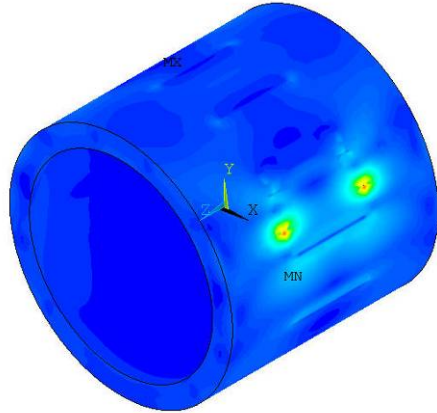
Condition: Self-weight of the coil.

→  $W_{coil}=180\text{tonnes}(\text{Coil-thick}=350\text{mm})$

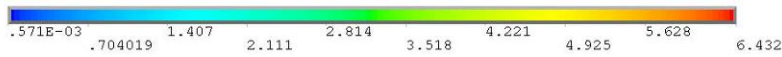
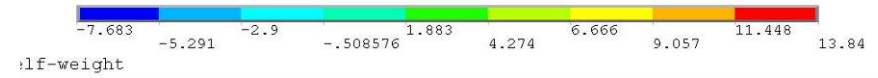
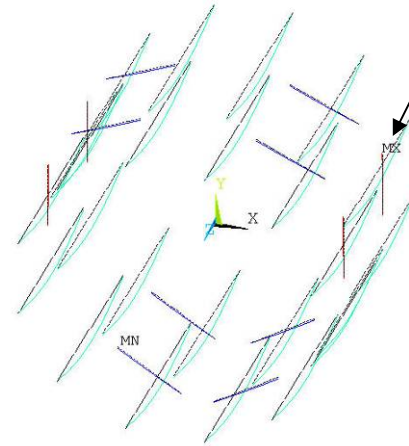
Verical support rods: 138MPa

Von. M Stress : 64MPa

SEQV (AVG)  
DMX =23.008  
SMN =-.571E-03  
SMX =6.432

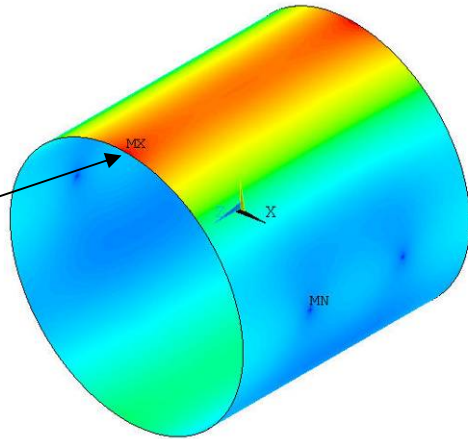


NMIS1  
TOP  
DMX =23.008  
SMN =-7.683  
SMX =13.84

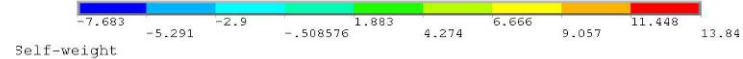
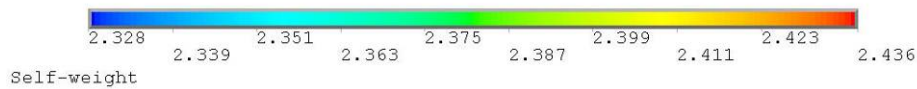
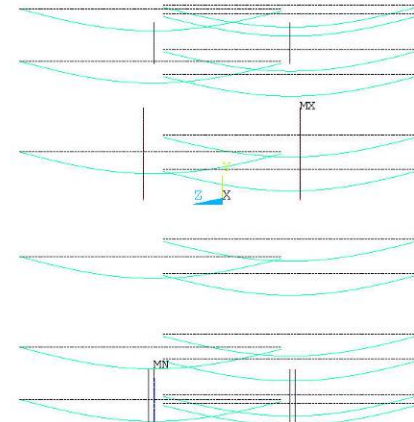


USUM (AVG)  
RSYS=0  
DMX =2.436  
SMN =2.328  
SMX =2.436

2.4mm



SUP -1  
TIME=1  
NMIS1  
TOP  
DMX =23.008  
SMN =-7.683  
SMX =13.84



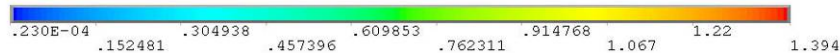
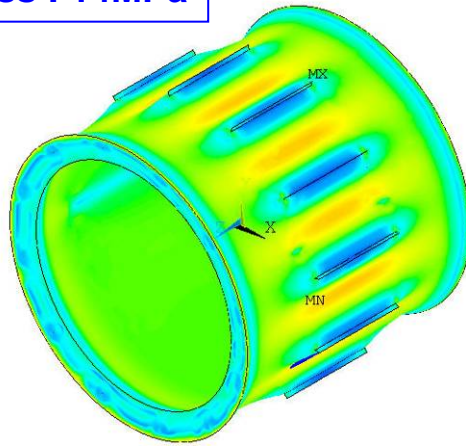


# Calculation-3

Condition: Under Vacuum pressure

**Von. M Stress : 14MPa**

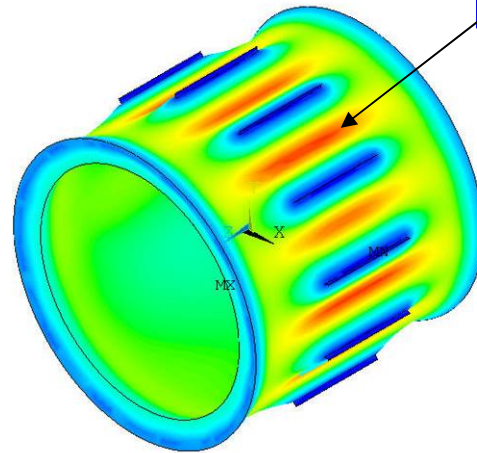
SMN = .230E-04  
SMX = 1.394



Vac.

USUM (AVG)  
RSYS=0  
DMX = .267677  
SMX = .267677

**0.3mm**



Vac.

**Required thickness of the outer vacuum wall to withstand buckling pressure**

Ref.: NASA SP8007

$$P_{cr} = \frac{0.855}{(1-\mu^2)^{\frac{3}{4}}} \cdot \frac{E\sqrt{\gamma}}{\left(\frac{r}{t}\right)^{\frac{5}{2}} \left(\frac{L}{r}\right)}$$

$$t = \frac{r}{\left\{ \frac{0.855E \cdot \sqrt{\gamma}}{P_{cr} (1-\mu^2)^{\frac{3}{4}} \cdot \left(\frac{L}{r}\right)} \right\}^{\frac{2}{5}}}$$

If  $P_{cr} = 2atm$ ,  $\sqrt{\gamma} = 0.75$ ,

$$t = \frac{4190}{\left\{ \frac{0.855 \cdot 2.1 \times 10^4 \cdot 0.75}{0.02 \cdot (1-0.3^2)^{\frac{3}{4}} \cdot \left(\frac{7744}{4190}\right)} \right\}^{\frac{2}{5}}}$$

= 24.3mm

**→ Thicker than 24.3mm is required.**

# Coefficient of thermal expansion

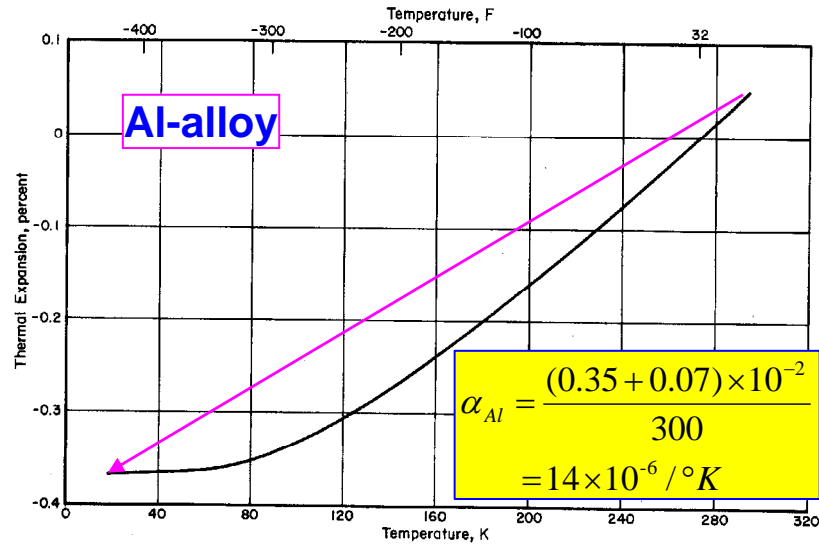


FIGURE 4.2.3-E1. THERMAL EXPANSION VERSUS TEMPERATURE FOR ALUMINUM ALLOY 5456-H343

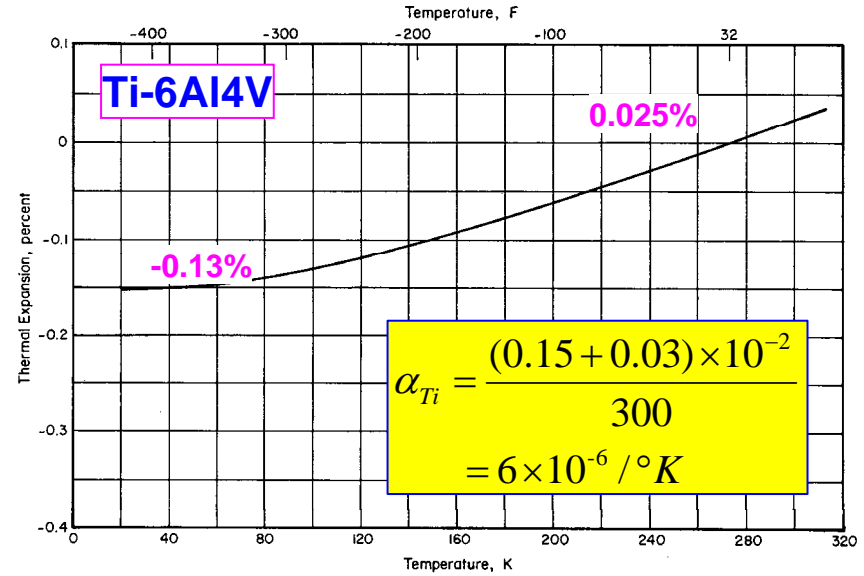


FIGURE 9.3.2-E1. THERMAL EXPANSION VERSUS TEMPERATURE FOR Ti-6 Al-4 V ALLOY

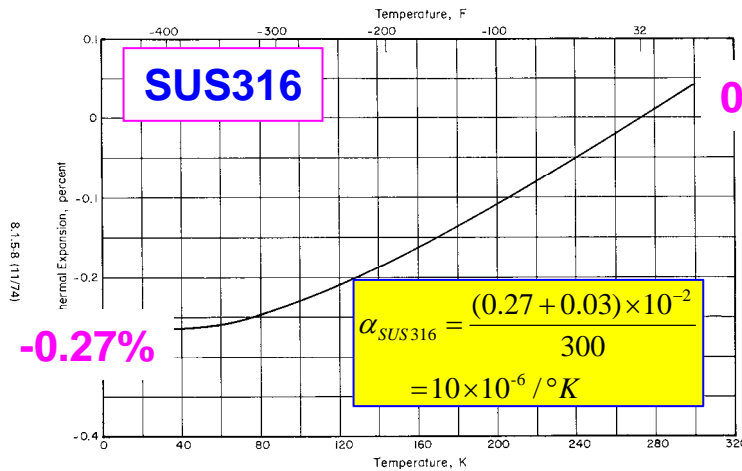


FIGURE 8.1.5-E1. THERMAL EXPANSION VERSUS TEMPERATURE FOR TYPE 316 STAINLESS STEEL

Ref.: HANDBOOK ON MATERIALS FOR SUPERCONDUCTING MACHINERY, MCIS-HP-04, Jan. 1977