

# Simulation Studies on Coupler Wakefield and RF Kicks in ILC Bunch Compressor with SLEPT

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# Coupler's wakefields ( I )

- In the ILC cavities, the power and HOM couplers break the structure symmetry =>transverse wakefields are excited by the beam even if it goes through the center of cavities, which are different from usual dipole mode wakefield.
- Coupler wake has been newly introduced to SLEPT.
- We need a short-range  $\delta$  wake function for point charge in order to get the transverse wakepotential  $W_t(s)$ .

$$W_t(s) = \int_{-\infty}^s \lambda(s')W(s-s')ds' / \int_{-\infty}^{\infty} \lambda(s')ds'$$

We try to use the simplified model for  $\delta$  wake function of couplers of ILC cavity.

$$W(s) = as + b\sqrt{s}$$

# Coupler's wakefields ( II )

- Numerical results of the coupler wakepotentials for three different bunch lengths (0.3mm, 1.0mm and 9.0mm) were provided from Andrea Latina <sup>[1]</sup> (see Fig. 1 and Fig. 2).

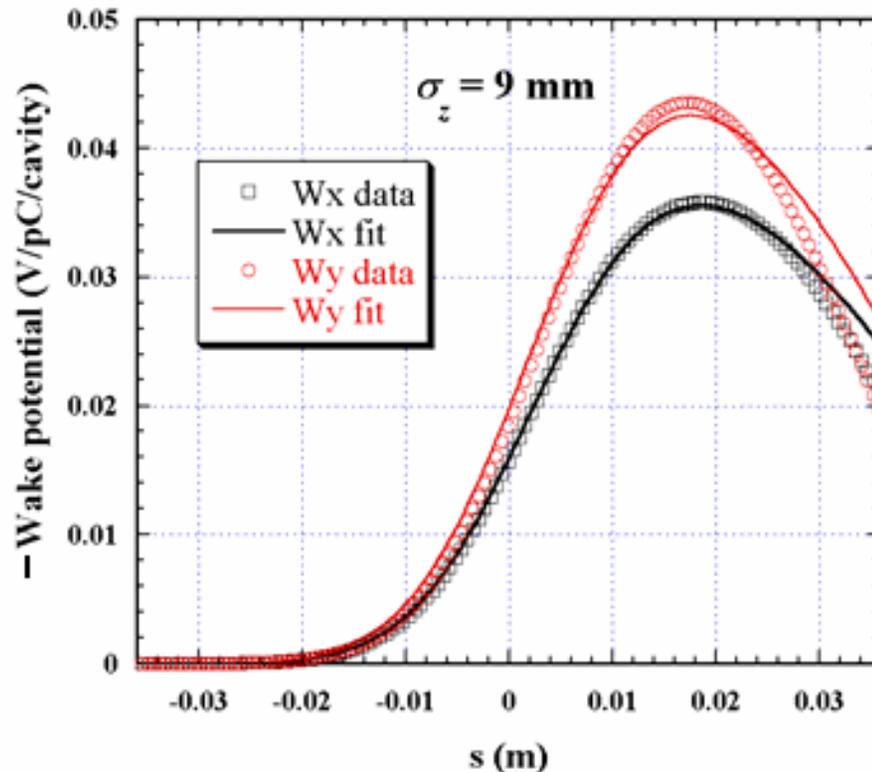


Fig. 1, Wake potential for 9 mm bunch. Data from cavity field calculation (rectangular: horizontal, circle: vertical) and from the simplified model for long bunch (lines).

# Coupler's wakefields (III)

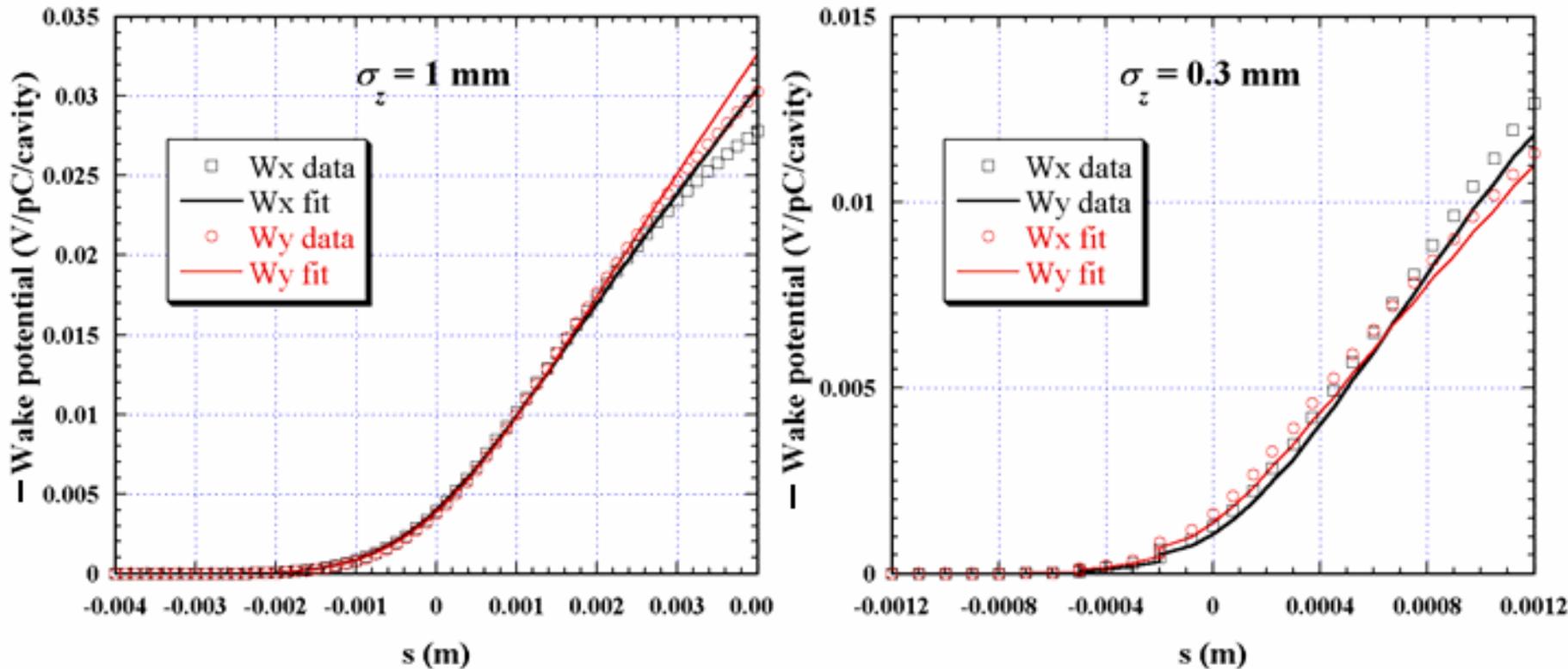


Fig. 2, Wake potential for 1 mm bunch and 0.3 mm bunch. Data from cavity field calculation (rectangular: horizontal, circle: vertical) and from the simplified model for short bunch (lines).

# Coupler's wakefields (IV)

- The approximate wake function in SLEPT:

Long bunch (9 mm) :

$$\begin{cases} W_x(s)[V / pC] = 2.862s[m] - 0.6786\sqrt{s[m]} \\ W_y(s)[V / pC] = 3.731s[m] - 0.8545\sqrt{s[m]} \end{cases}$$

Short bunch (0.3 mm and 1 mm) :

$$\begin{cases} W_x(s)[V / pC] = -5.928s[m] - 0.1500\sqrt{s[m]} \\ W_y(s)[V / pC] = -6.770s[m] - 0.0894\sqrt{s[m]} \end{cases}$$

- Within 3-sigma of the bunch lengths, the calculated wakepotentials from this simplified model have a good agreement with the data from cavity field calculation.

# RF kick ( I )

- The couplers also introduce an asymmetry into the accelerating RF field and thereby additional transverse field components. —RF kick
- RF-kick voltage is [2] :

$$\vec{V}(s) = \left(\frac{\vec{V}_0}{V_a}\right)GL e^{i(\varphi_{rf} + \varphi_c + ks)}$$

(  $\vec{V}_0$  -vector of RF kick on axis,  $V_a$ -accelerating voltage on axis,  $k$ -wave number of RF field,  $G$ -accelerating gradient on axis,  $L$ -cavity length,  $\varphi_{rf}$ —RF phase,  $\left|\frac{\vec{V}_0}{V_a}\right|$ -RF kick amplitude,  $\varphi_c$ -RF kick phase.)

# RF kick ( II )

- The RF kick on axis for an on-crest-accelerated particle in ILC cavity (from numerical calculations) is <sup>[3]</sup> :

$$\frac{\vec{V}_0}{V_a} \times 10^6 = \begin{pmatrix} -105.3 + 69.8i \\ -7.3 + 11.1i \end{pmatrix}$$

- Parameters used in SLEPT:

Horizontal:

$$\left| \frac{V_{0x}}{V_a} \right| = \sqrt{105.3^2 + 69.8^2} = 126.3 \times 10^{-6}, \varphi_c = \pi + \arctg\left(\frac{69.8}{-105.3}\right) = 2.5562$$

Vertical:

$$\left| \frac{V_{0y}}{V_a} \right| = \sqrt{7.3^2 + 11.1^2} = 13.3 \times 10^{-6}, \varphi_c = \pi + \arctg\left(\frac{11.1}{-7.3}\right) = 2.1525$$

# Simulation Results ( I )

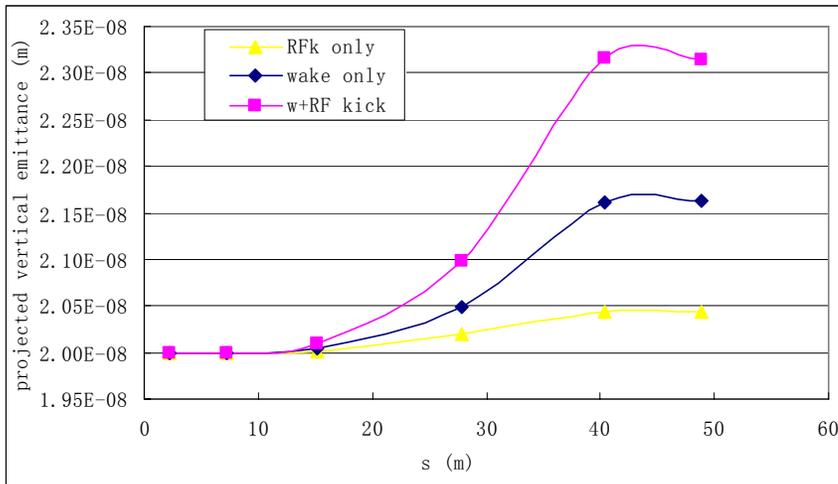
- Simulations are done only in the RF sections, not in the wiggler sections.
- Lattice of RDR base design was used.
- only single bunch emittance growth is considered

| Parameter             | BC1                  | BC2                  |
|-----------------------|----------------------|----------------------|
| Bunch Charge          | $2 \times 10^{10} e$ | $2 \times 10^{10} e$ |
| Initial Energy        | 5.0 GeV              | 4.88 GeV             |
| Initial Energy Spread | 0.15%                | 2.5%                 |
| Initial Bunch Length  | 9.0 mm               | 1.0 mm               |
| RF Gradient           | 18 MV/m              | 30 MV/m              |
| RF Phase              | $-105^\circ$         | $-27.6^\circ$        |
| Initial Emittance X/Y | 8 $\mu$ m/ 20 nm     | 8 $\mu$ m/ 20 nm     |

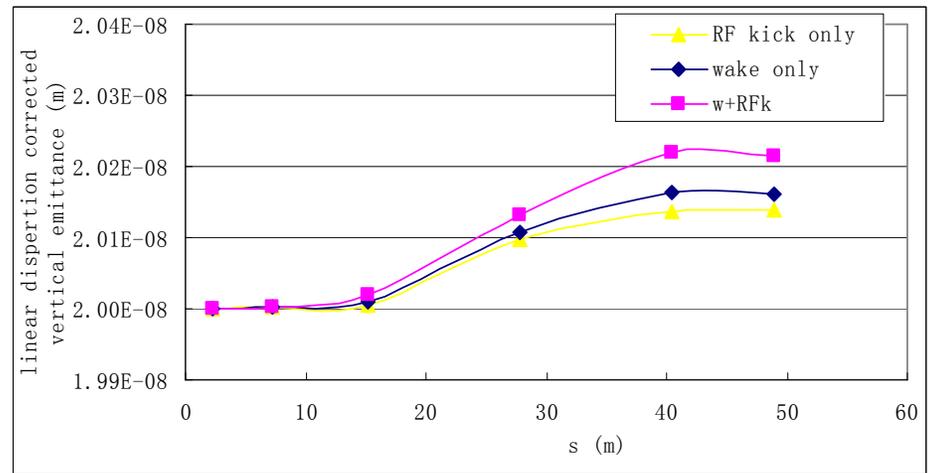
# Simulation Results ( II )

- BC1 RF section (1-to-1 correction, no misalignment)

projected vertical emittance vs. distance from the entrance



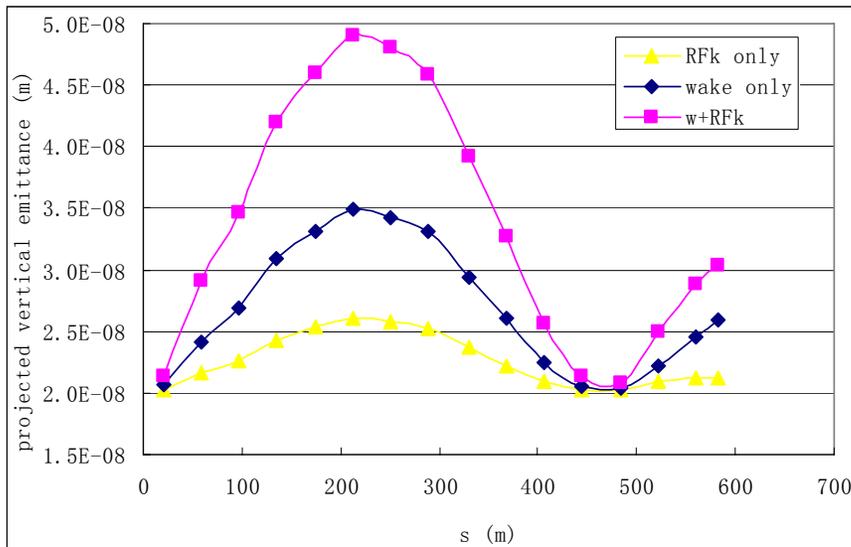
linear dispersion corrected vertical emittance vs. distance from the entrance



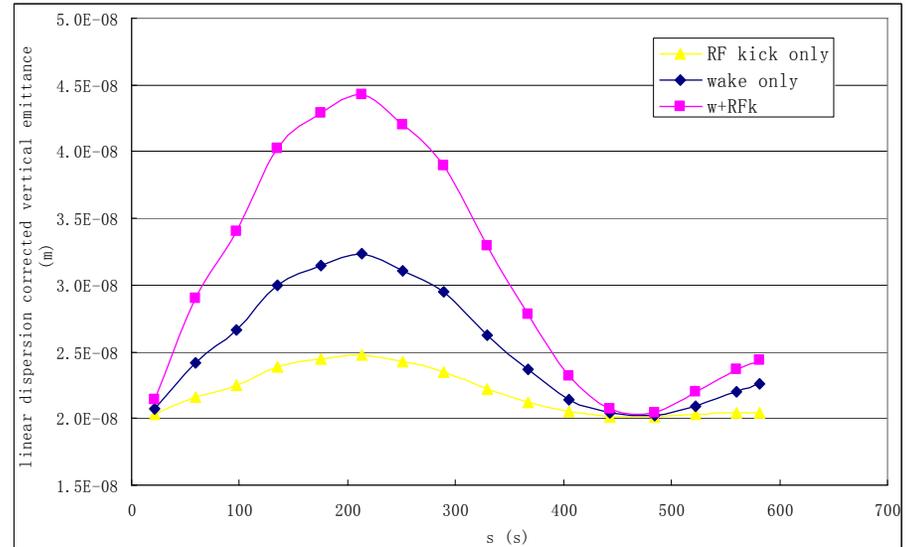
# Simulation Results (III)

- BC2 RF section (1-to-1 correction, no misalignment)

projected vertical emittance vs. distance from the entrance



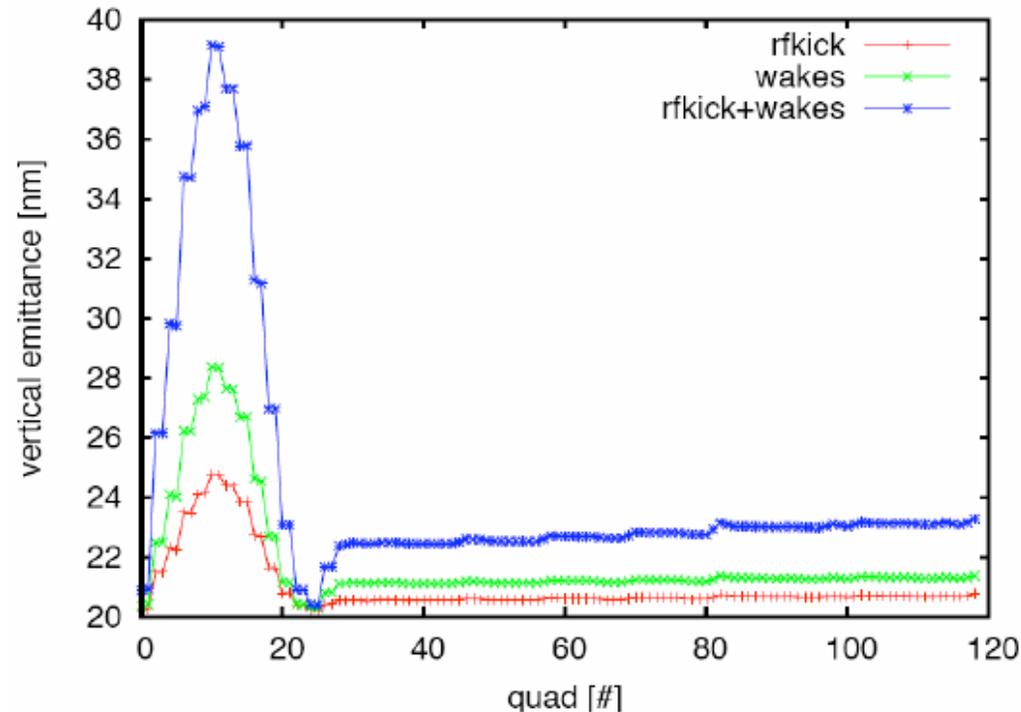
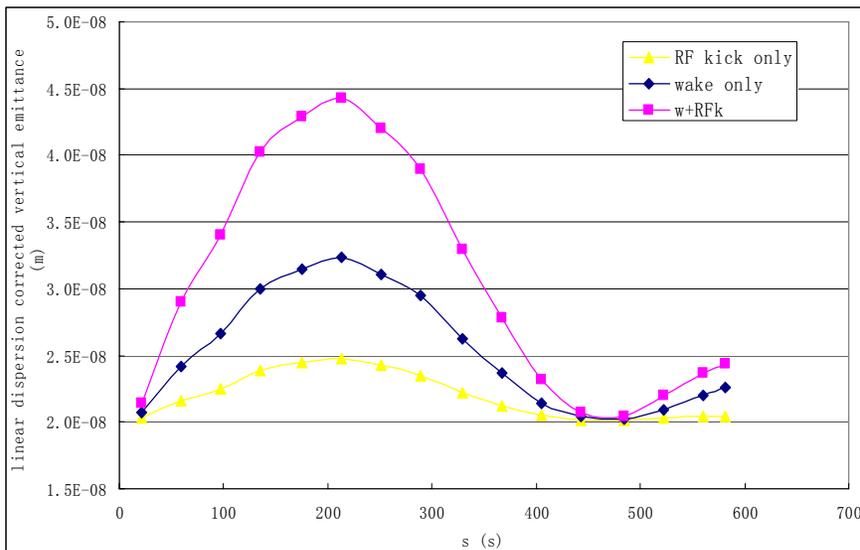
linear dispersion corrected vertical emittance vs. distance from the entrance



# Simulation Results (IV)

- Comparison with A. Latina's result (using PLACET) for BC2 [2]

Two results about RF kick effect agree well, but the wakefield effect from our result is larger than A. Latina's .



# Conclusions

- Final vertical emittance growth in ILC BC RF section including coupler RF kick and Wakes is :
  - BC1: 0.21 nm
  - BC2: 4.41 nm
- The emittance oscillates along the Linac according to the betatron oscillation. We can change the betatron phase advance to make the minimum coincidently at the exit.

# References

- [1] Andrea Latina, private communication, (2008).
- [2] Andrea Latina, et al, “Emittance Growth in ML and BC with Couplers’ RF-Kick and Wakefields”, LCWS, Chicago, November 2008.
- [3] N. Solyak, et al, “RF Kick in the ILC Acceleration Structure”, MOPP042, EPAC08.