

A feasibility study of top-quark Yukawa coupling measurement in $e^+e^- \rightarrow t\bar{t}H$ at $\sqrt{s}=500\text{GeV}$

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for

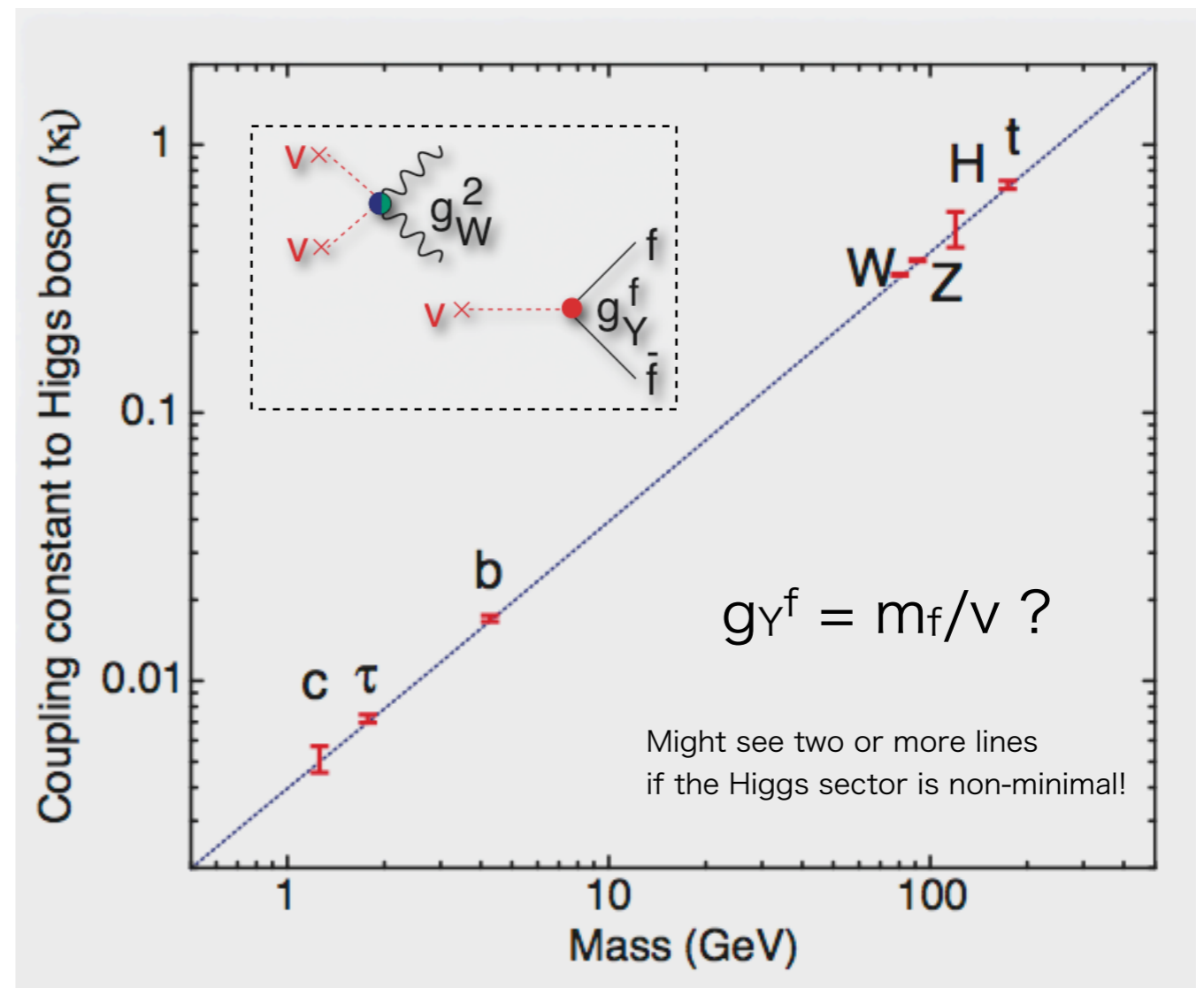
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Introduction

- Unique role of the top quark for Electroweak symmetry breaking (EWSB) studies
 - Top mass is by far the largest and approximates the EWSB scale
 - Suggests top couples strongly to the physics that breaks the EW symmetry
 - Important to investigate properties of the top in detail, for the purpose of **probing the EWSB physics** as well as to **gain deeper understanding of the origin of the flavor structure**
 - Measurement of **top-quark Yukawa coupling** will be the **most decisive test of the mass generation mechanism for matter particles!**
- **Goal of our study: evaluate measurement accuracy** for the **direct measurement of the top Yukawa coupling at 500GeV**
 - Need to demonstrate its feasibility in the **first phase of the ILC project!**

If the Higgs boson is the one to give masses to all the SM particles, we need to observe proportionality between mass and coupling



Measurement of top Yukawa coupling

- LHC** ($2 \times 300 \text{ fb}^{-1}$)

- Cross section for Gluon fusion \rightarrow H

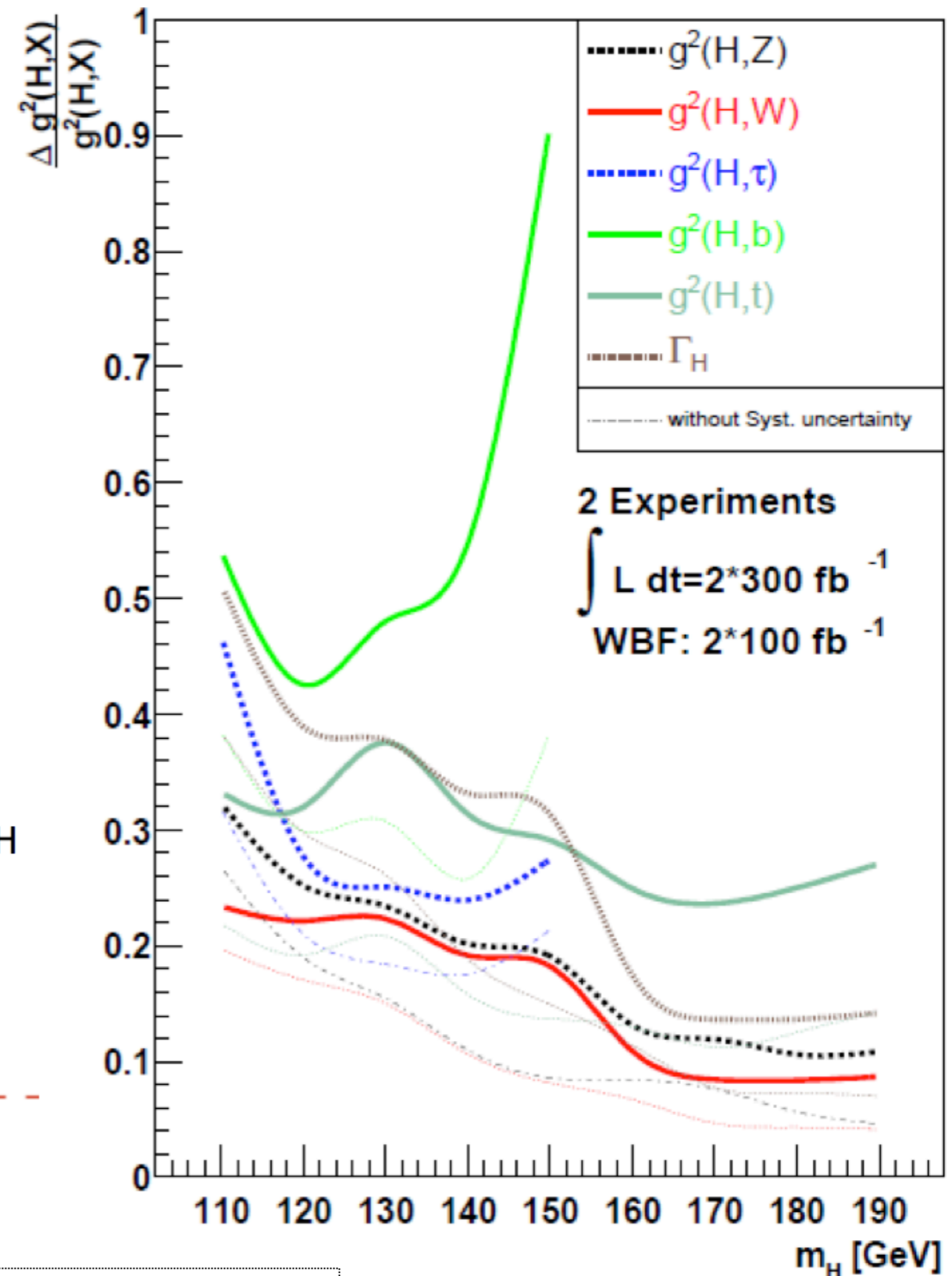
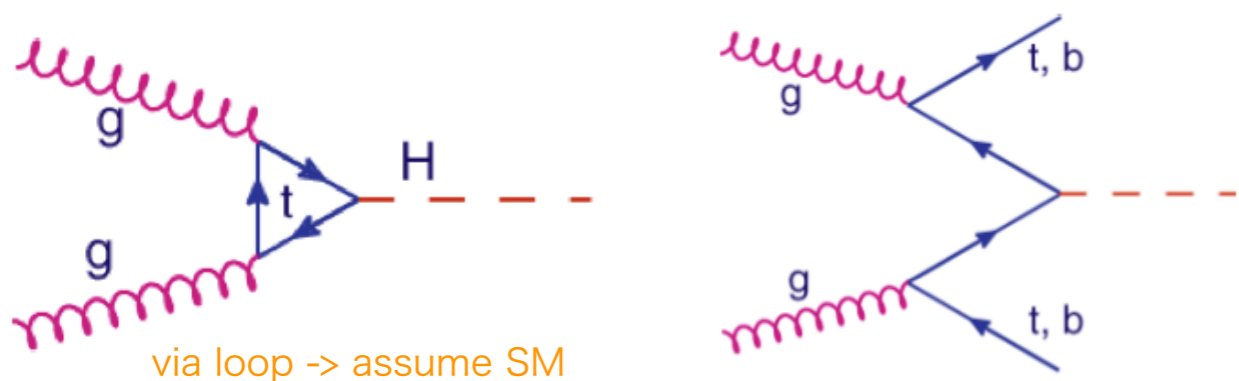
$$\sigma_{ggH} = \alpha_{ggH} \cdot g_t^2$$

- Cross section for Gluon fusion \rightarrow ttH
(seems difficult...)

$$\sigma_{ttH} = \alpha_{ttH} \cdot g_t^2$$

- Branching ratio for $H \rightarrow \gamma\gamma$

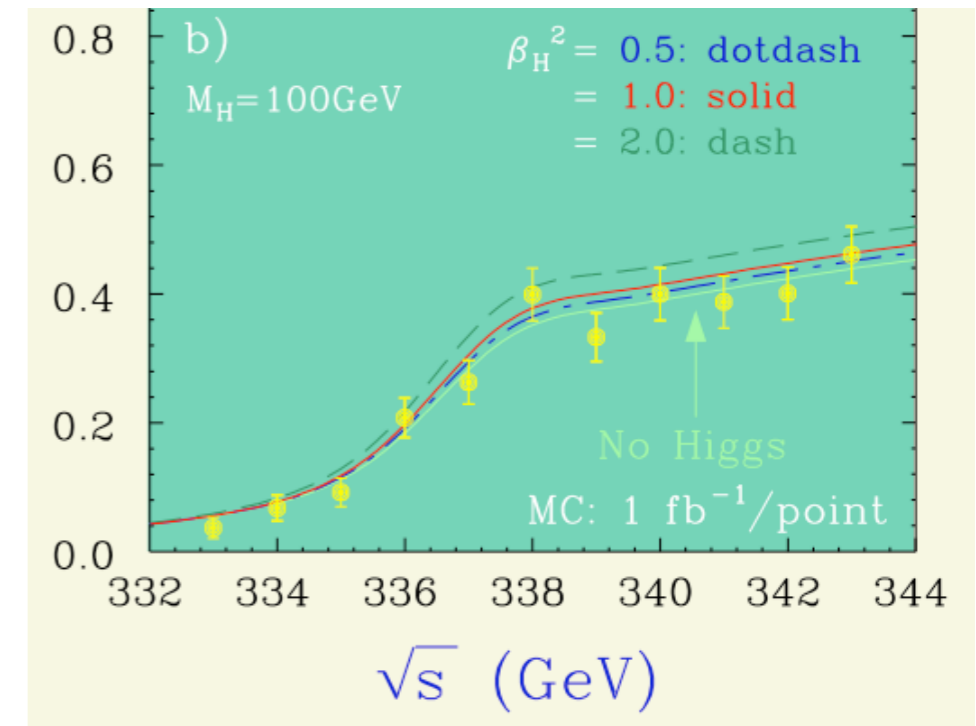
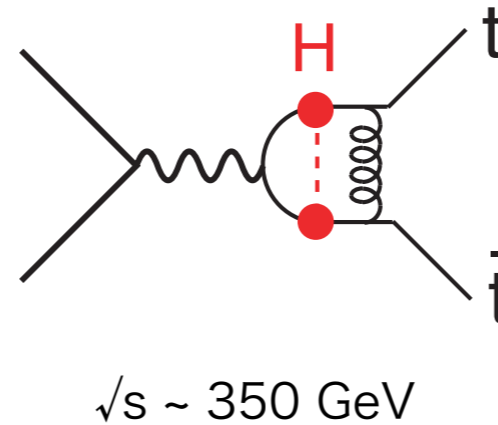
$$\text{BR}(H \rightarrow \gamma\gamma) = (\beta_{\gamma W} \cdot g_W - \beta_{\gamma t} \cdot g_t)^2 / \Gamma_H$$



From J. Tanaka (U. Tokyo/ICEPP)'s slide

Measurement of top Yukawa coupling

- **ILC: indirect measurement**
 - Higgs exchange between tops affects the potential near $t\bar{t}$ threshold
 - 11 points $t\bar{t}$ threshold scan
 $\Rightarrow \sigma_{t\bar{t}}(m_H, g_Y^t)$
 - Need theoretical progress in the predictions of $t\bar{t}$ threshold observables

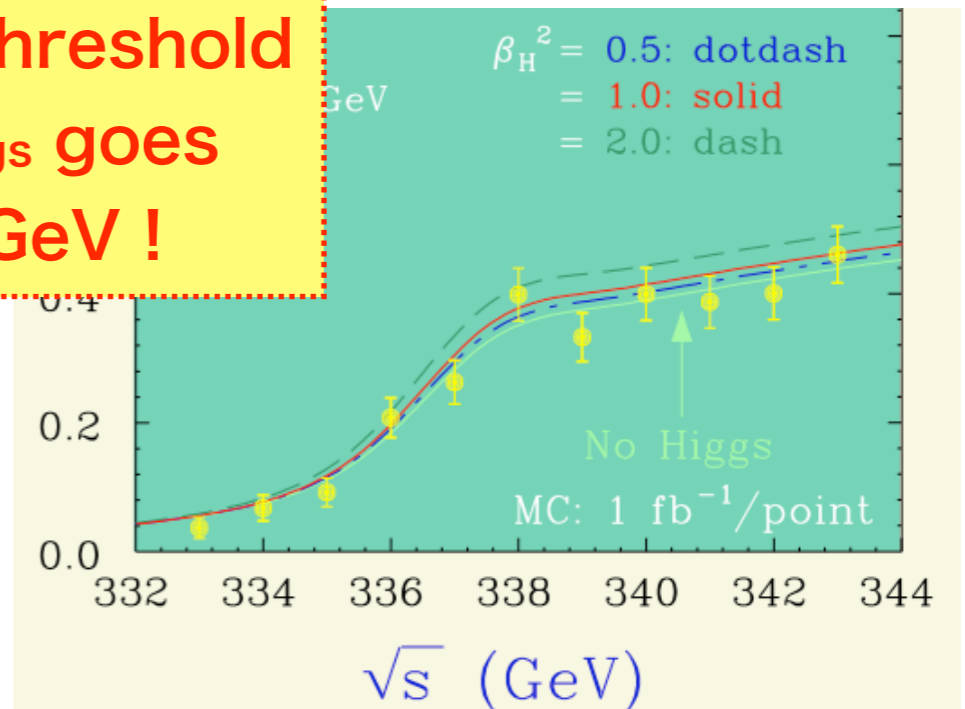
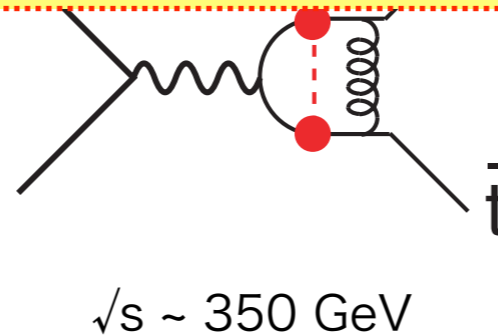


Measurement of top Yukawa coupling

- **ILC: indirect measurement**

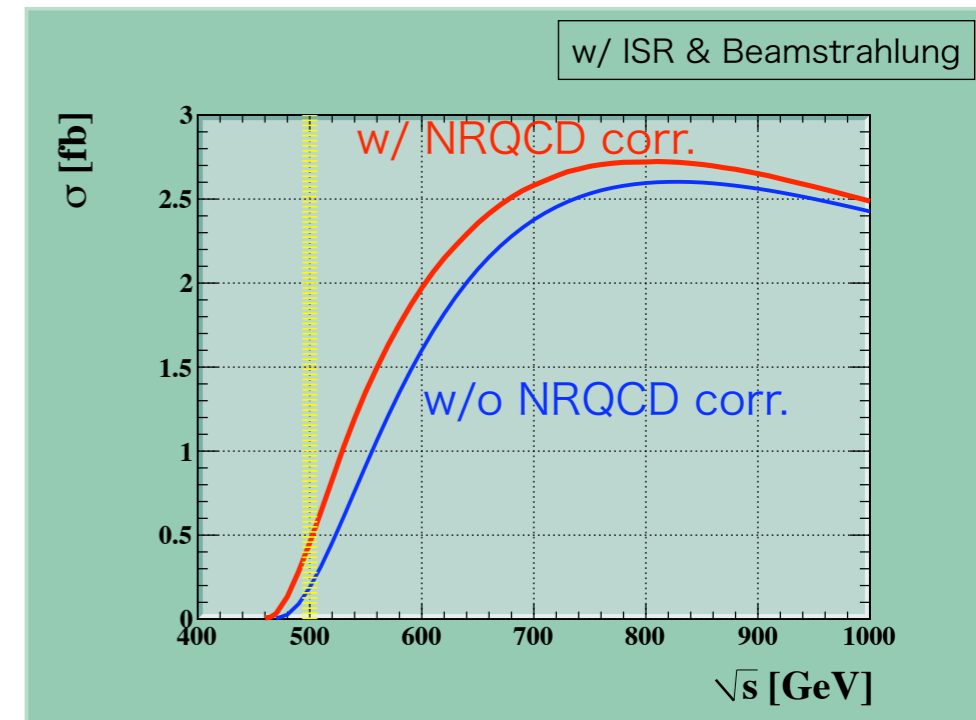
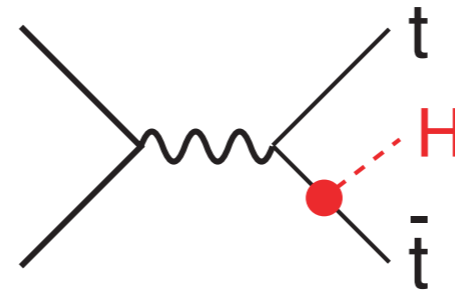
- Higgs exchange between the potential near $t\bar{t}$ threshold
- 11 points $t\bar{t}$ threshold scan $\Rightarrow \sigma_{t\bar{t}}(m_H, g_Y^t)$
- Need theoretical progress in the predictions of $t\bar{t}$ threshold observables

top Yukawa effect at $t\bar{t}$ threshold quickly vanishes as M_{Higgs} goes up from 110GeV to 120GeV !



- **ILC: direct measurement**

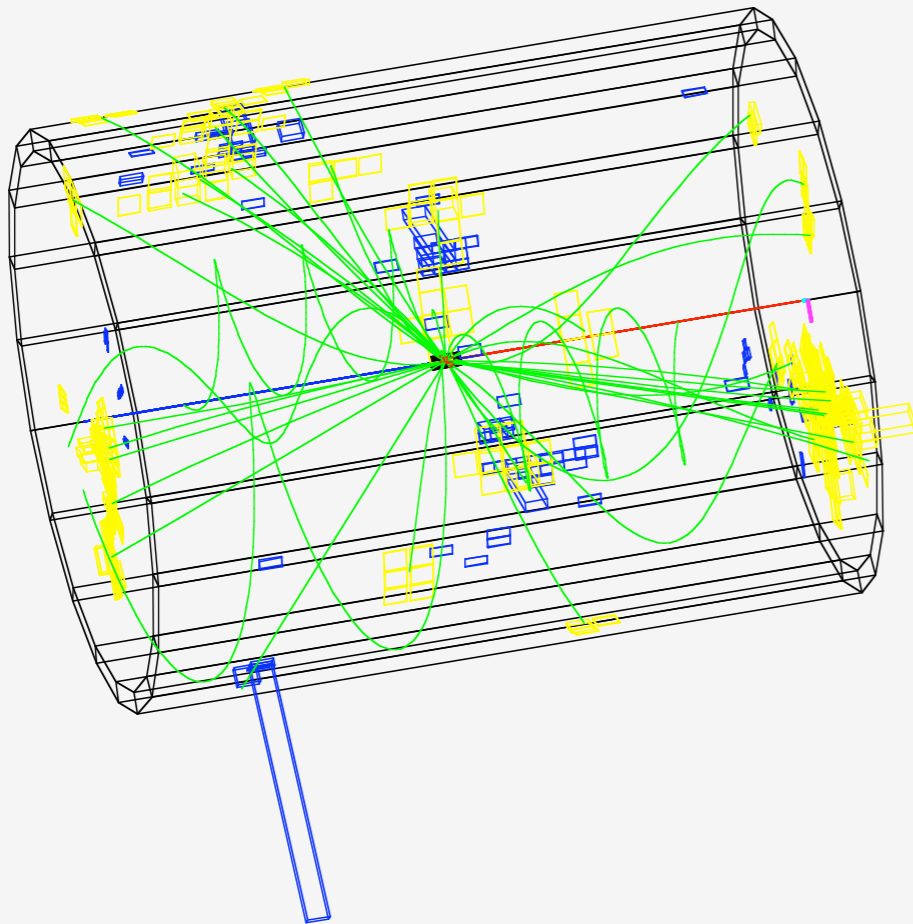
- Most of the past studies were done assuming at $\sqrt{s} \sim 700\text{GeV}$ since the cross section for $e^+e^- \rightarrow t\bar{t}H$ attains its maximum around this energy region
- However, pointed out that the **NRQCD threshold correction enhances the cross section significantly** and might open the possibility of directly measuring g_Y^t **at $\sqrt{s} = 500\text{GeV}$**



$e^+e^- \rightarrow t\bar{t}H$ event display

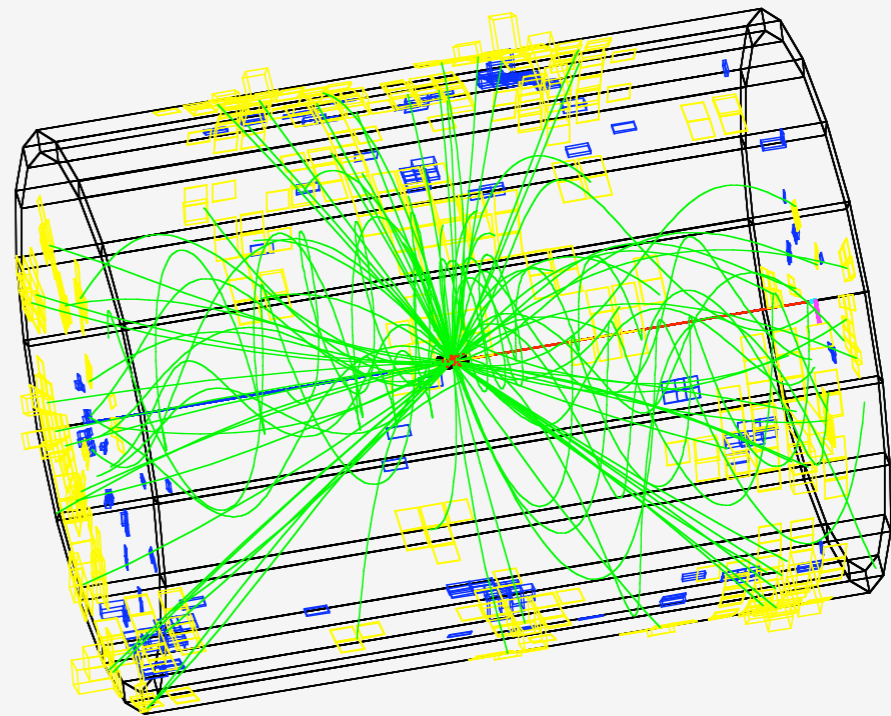
- Dense 8-fermion ($H \rightarrow b\bar{b}$) and/or 10-fermion ($H \rightarrow WW^*$) events
- Challenging for correct jet-parton association w/ quad b-tagging
 - Di-jet & Tri-jet invariant masses: $M_W(jj)$, $M_t(bjj)$ & $M_H(bb)$ for background events rejection

Lepton + 6-jets mode



$t\bar{t}H \rightarrow (bW)(bW)(b\bar{b}) \rightarrow (bcs)(b|\nu)(b\bar{b})$

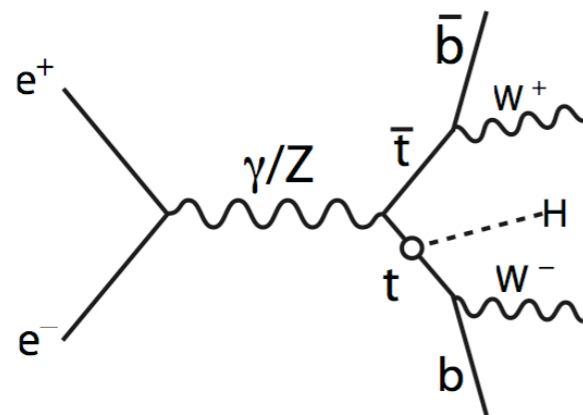
8-jets mode



$t\bar{t}H \rightarrow (bW)(bW)(b\bar{b}) \rightarrow (bcs)(bcs)(b\bar{b})$

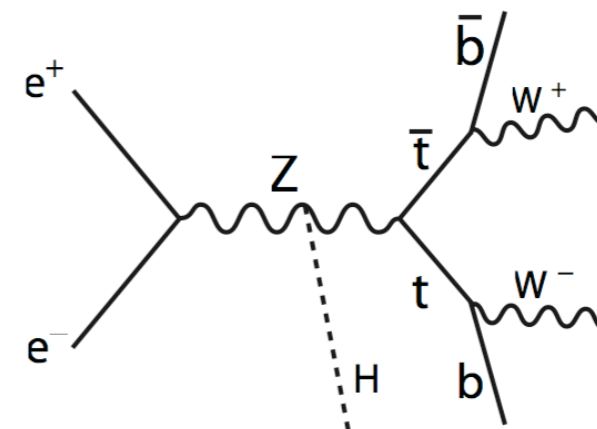
Signal processes: $e^+e^- \rightarrow ttH$

- In this study: concentrate on the **dominant decay mode** $H(120\text{GeV}) \rightarrow bb$ (68%)
 - $ttH \rightarrow bW^+bW^- bb$ signal events can be classified into **3 groups**
 - 8-jets, **1-lepton + 6-jets**, and 2-leptons + 4-jets



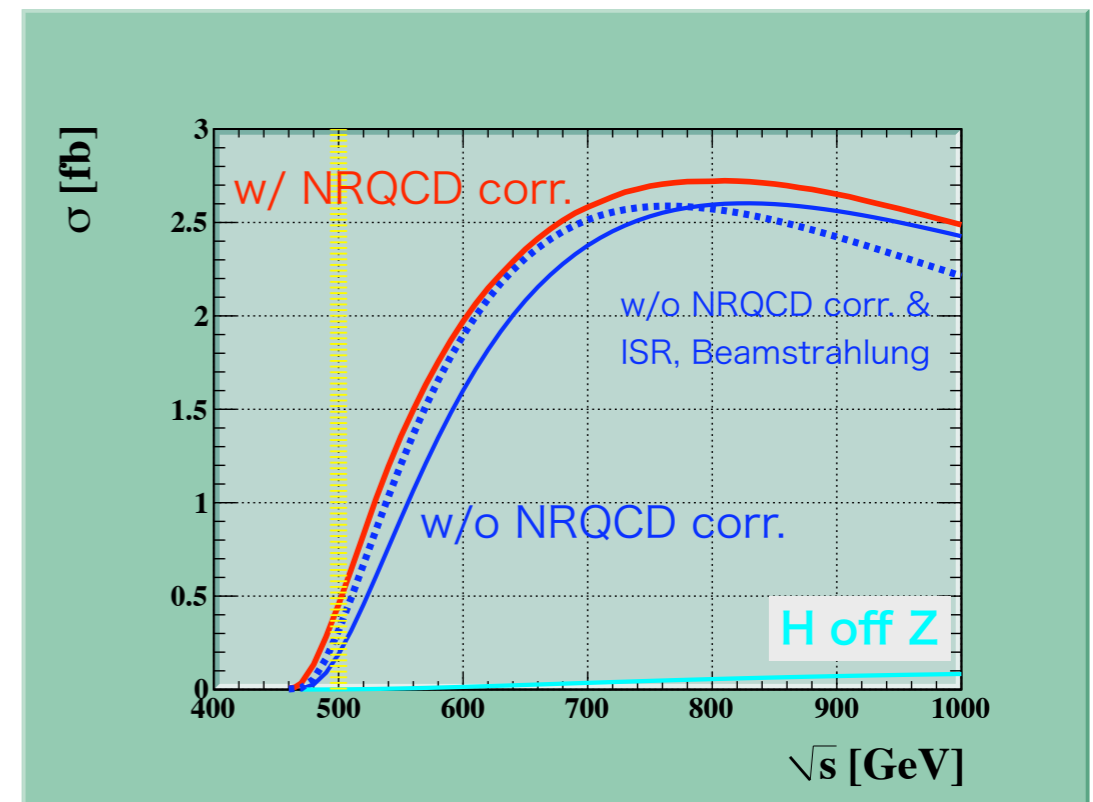
Contains the top Yukawa coupling

$$\sigma_{ttH} \propto (g_Y^t)^2$$



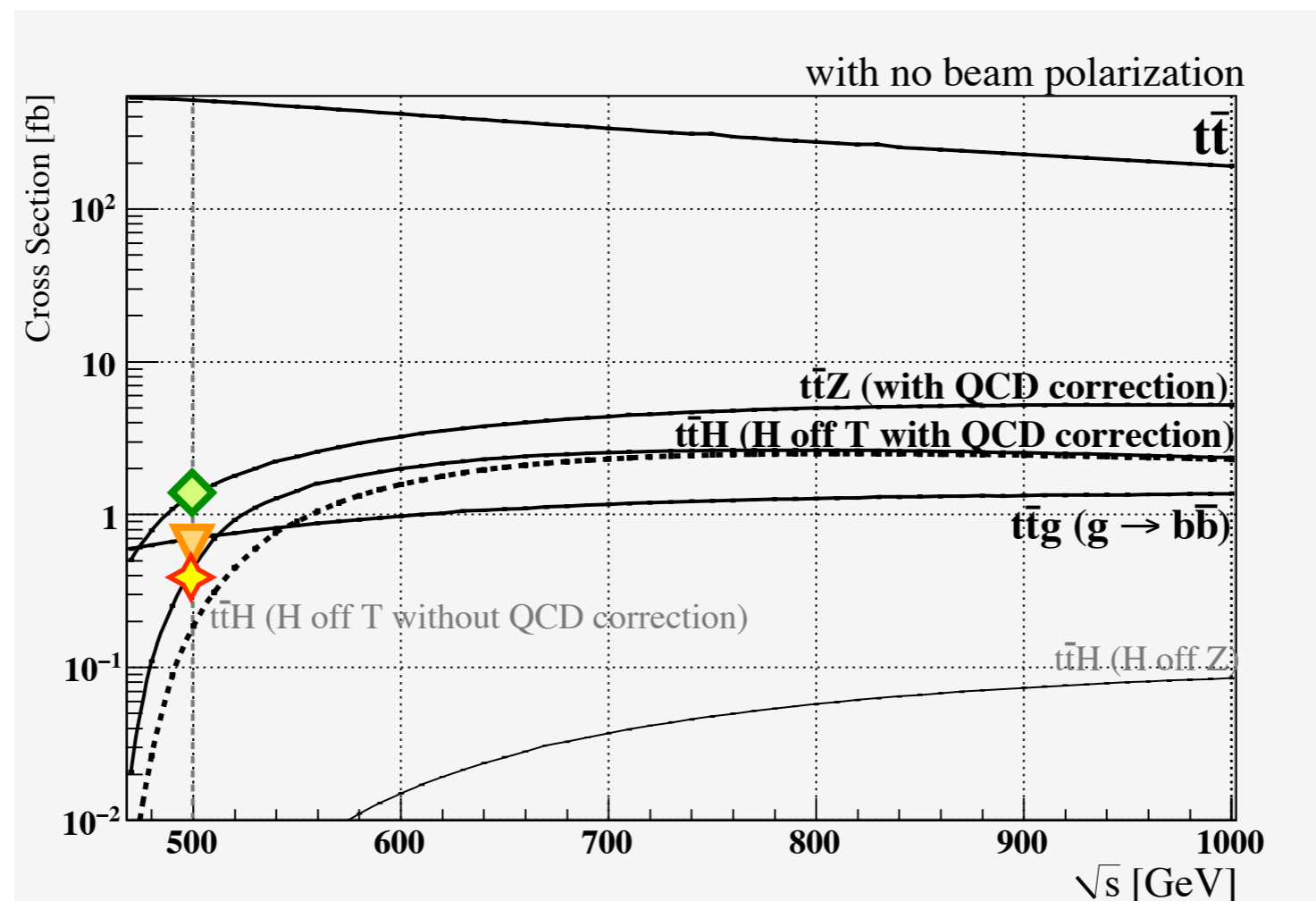
Does not contain top Yukawa coupling

- Dominant contribution to ttH production at $\sqrt{s} = 500\text{GeV}$ is γ/Z exchange (= **very small contribution from Higgs radiated off the Z**)
 - Can determine g_Y^t by just counting the number of signal events
 - But the **signal cross section is sub-fb order...**
- Initial state radiation (ISR) and Beamstrahlung
 - σ_{ttH} decreases by a factor ~ 2 at $\sqrt{s} = 500\text{GeV}$
- NRQCD threshold correction** (to $t\bar{t}$ system)
 - Enhances σ_{ttH} significantly: $\sigma_{ttH} = 0.45\text{fb}$ (with no beam pol.)



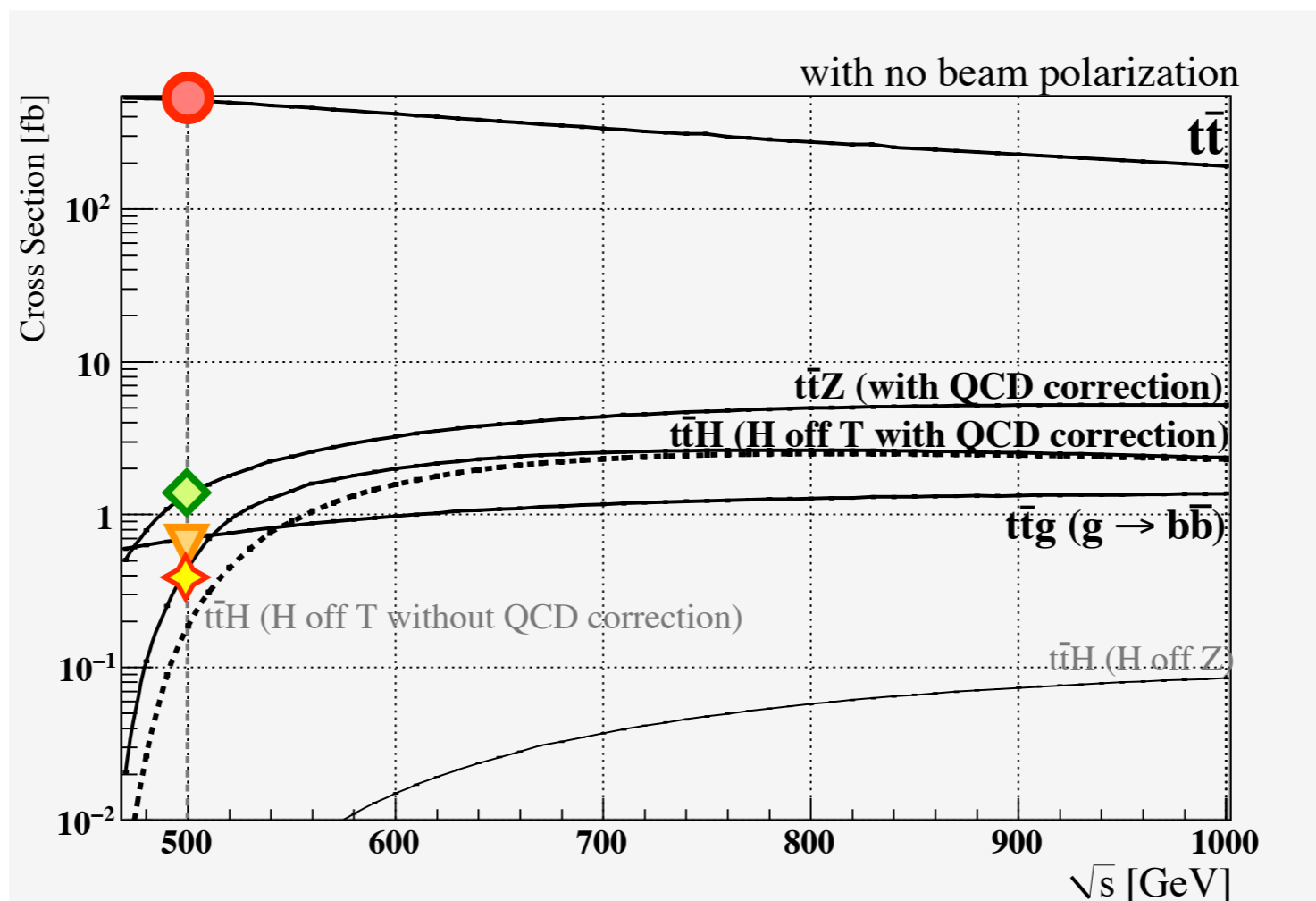
Possible BGs (Interfering)

- Interfering BGs (same final state: $t\bar{t}b\bar{b} \rightarrow bqq\ b\bar{l}\nu\ b\bar{b}$)
 - Electroweak: $t\bar{t}Z \rightarrow t\bar{t}b\bar{b}$ ($Z \rightarrow b\bar{b}$: 15%) $\sim 0.2\text{fb}$ with no beam polarization
 - ▶ NRQCD threshold correction enhances $\sigma_{t\bar{t}Z}$ from 0.7fb to 1.3fb
 - ▶ Dangerous if $M_{\text{Higgs}}(120\text{GeV})$ is close to $M_{b\bar{b}}$
 - Electroweak: $W^*W^*/ZZ^* \rightarrow t\bar{t}b\bar{b}$: small contribution ($< 0.01\text{fb}$)
 - QCD: $t\bar{t}g \rightarrow t\bar{t}b\bar{b}$ ($g \rightarrow b\bar{b}$: dominant) $\sim 0.7\text{fb}$ with no beam polarization
 - ▶ Not so dangerous when $M_{b\bar{b}} < M_{\text{Higgs}}(120\text{GeV})$



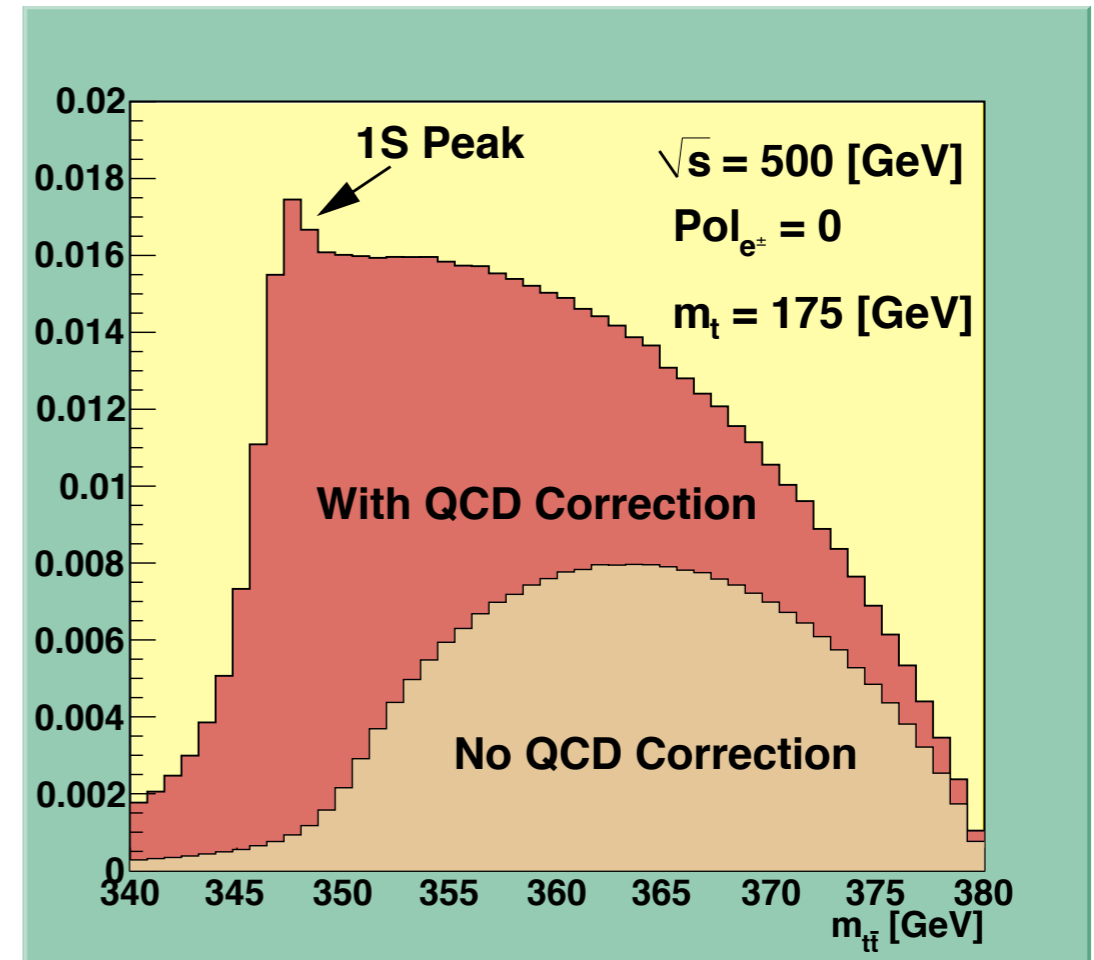
Possible BGs (Non-interfering)

- Non-interfering BGs (but, **huge cross sections**)
 - $t\bar{t}$ $\sim 500\text{fb}$ with no beam polarization
 - ▶ **Hard gluon emission from bottom quarks**
 - ▶ Small fraction of **mis-reconstruction** and/or **failure in b-tagging** may lead to **significant BG contamination**
 - qq (5 flavors) $\sim 4\text{pb}$: negligible \leq 1-isolated lepton + 6-jets (w/ **quad b-tagging**)
 - WW $\sim 8\text{pb}$: negligible w/ **quad b-tagging** / ZZ $\sim 0.58\text{pb}$: not huge = negligible



Analysis framework

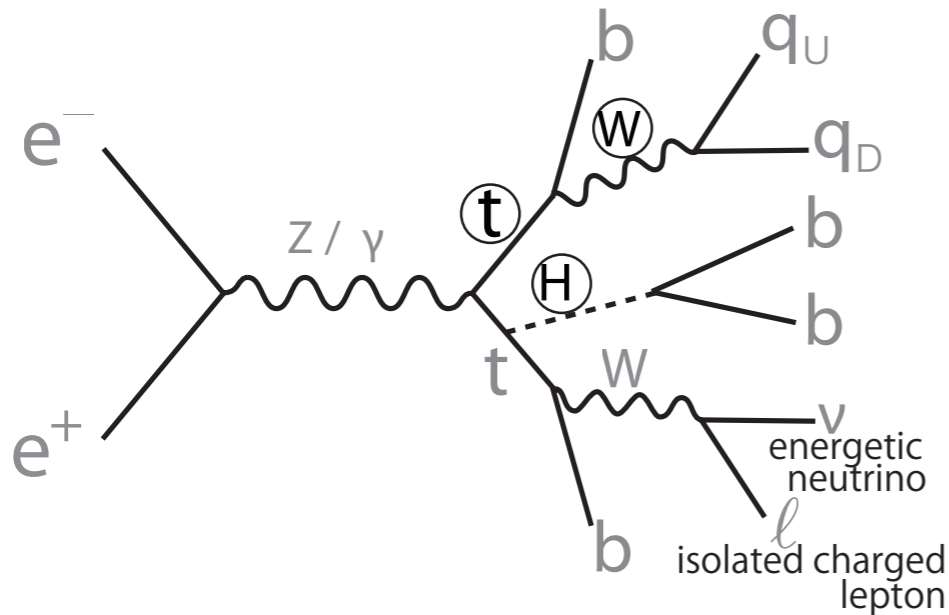
- Event generator
 - **physsim** package: based on **full helicity amplitudes** (6 or 8-fermion final states) calculated with **HELAS** including **gauge boson decays** (correctly taking into account angular distribution of the decay products)
 - **BASES/SPRING**: MC phase space integration / 4-momenta of the final-state quarks and leptons
 - Included **ISR & Beamstrahlung**
 - **NRQCD** threshold enhancement to the **ttbar** system (**ttH/ttZ**)
- Parton shower / Hadronization
 - **Pythia 6.4**
- Detector simulator / energy flow reconstruction
 - **JSFQuickSim** (smearing based fast MC simulator) / **Track-cluster matching**



Detector	Performance	Coverage
Vertex detector	$\sigma_b = 7.0 \oplus (20.0/p) / \sin^{3/2} \theta \mu m$	$ \cos \theta \leq 0.90$
Central drift chamber	$\sigma_{P_T} / P_T = 1.1 \times 10^{-4} p_T \oplus 0.1\%$	$ \cos \theta \leq 0.95$
EM calorimeter	$\sigma_E / E = 15\% / \sqrt{E} \oplus 1\%$	$ \cos \theta \leq 0.90$
Hadron calorimeter	$\sigma_E / E = 40\% / \sqrt{E} \oplus 2\%$	$ \cos \theta \leq 0.90$

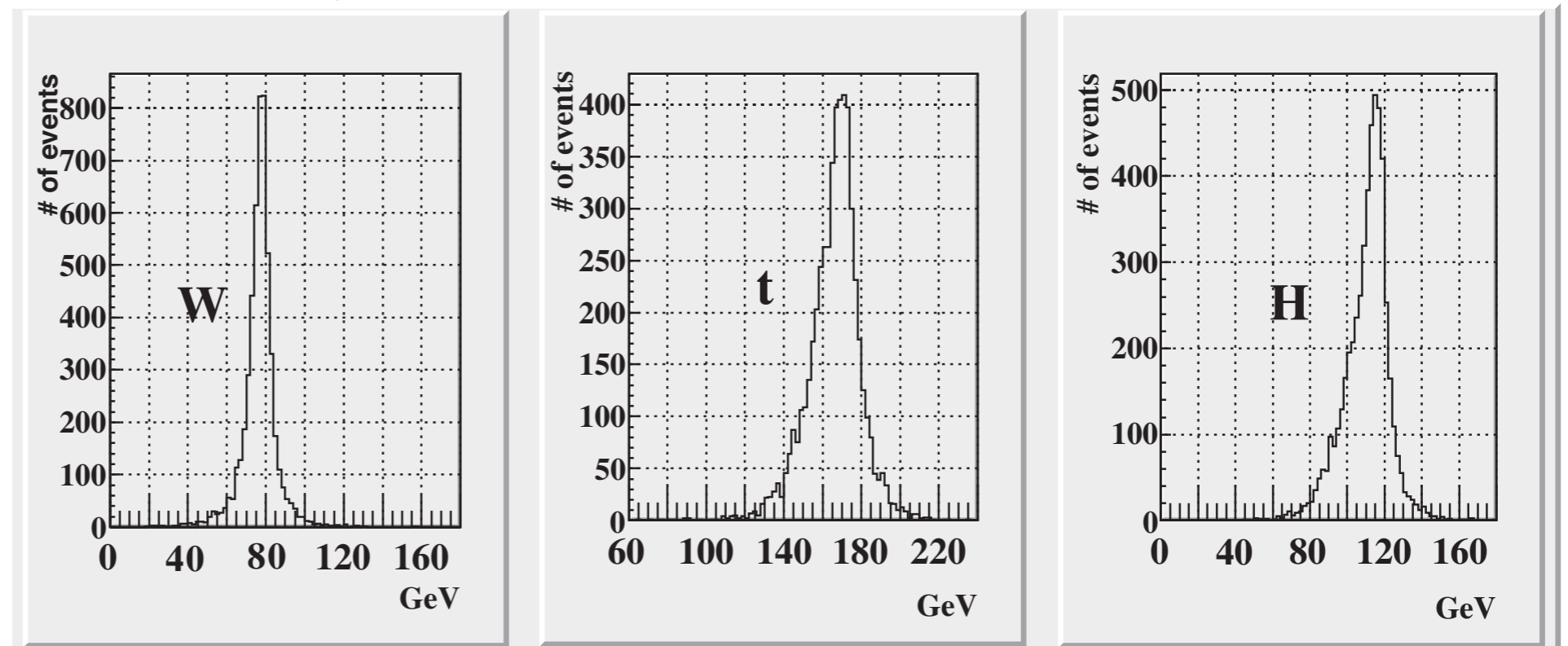
Event selection

- Concentrate on 1-lepton + 6-jets mode as our first step
 - not so low branching ratio: 35% where the lepton is required to be either e^\pm or μ^\pm
 - not so high jet multiplicities



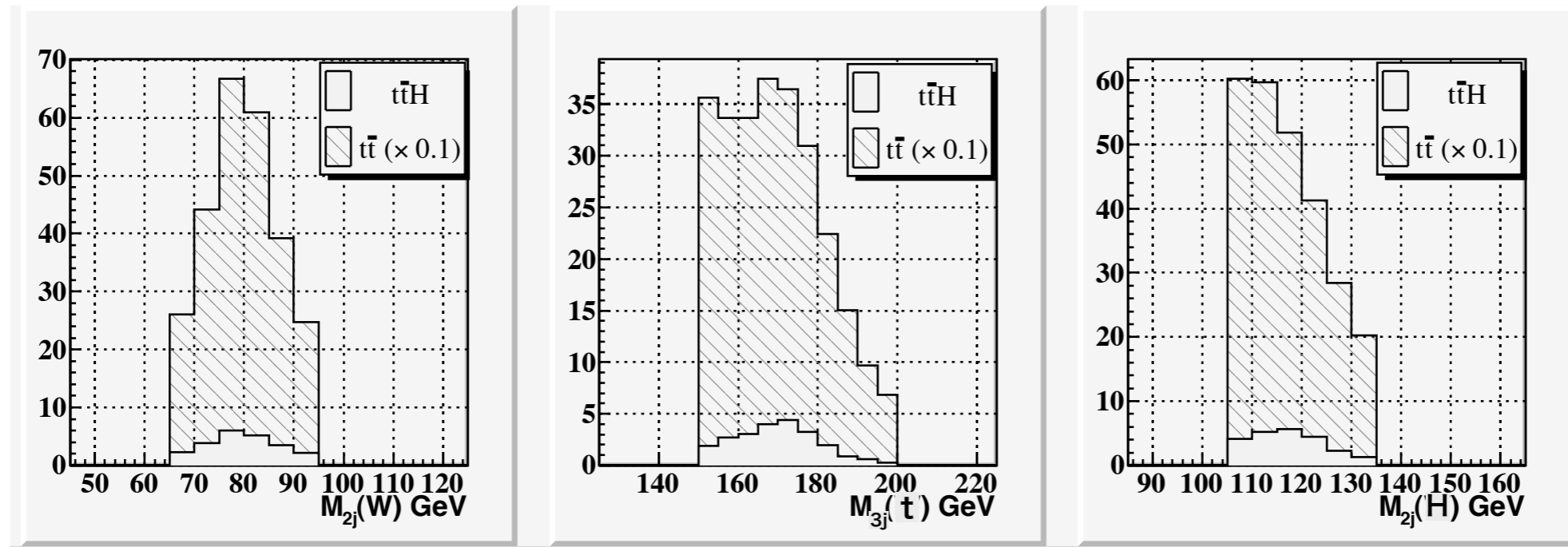
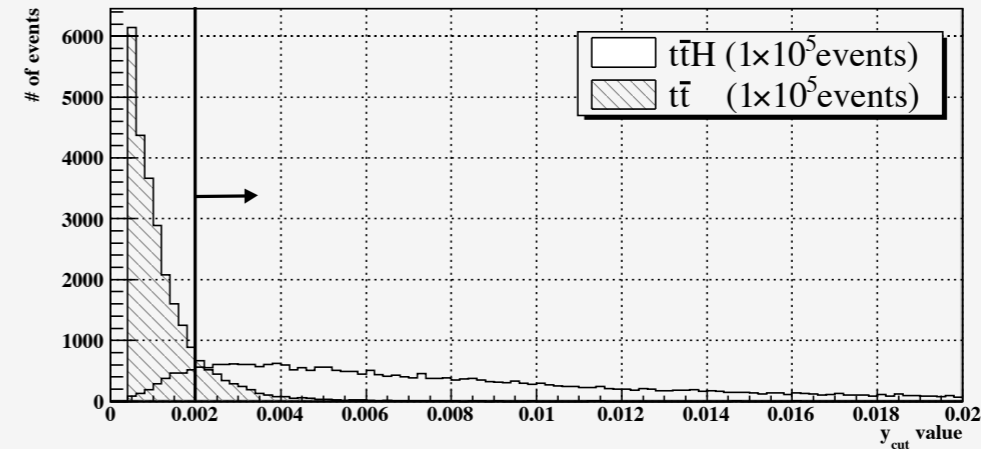
- Signatures of the 1-lepton + 6-jets mode
 - 1 isolated energetic e^\pm or μ^\pm
 - 6 jets including 4 b-jets, 2 of which form a Higgs
 - Remaining 2-jets being consistent with a W
 - 1 of the 2 unused b-jets together with this W candidate comprising a top

Reconstructed mass dists. using generator information
(Cheated jet-finder = perfect jet-parton association)



Reduction of huge tt BGs

- 1) Finding and eliminating **an energetic isolated lepton**
- 2) Force the events to cluster into 6 jets by choosing an appropriate Y_{cut} value on the event-by-event basis (**force 6-jet clustering**)
- 3) **Y_{cut} cut**
 - Y_{cut} value for a **tt BG event to form 6-jets should be lower than the one for a signal (ttH -> ttbb)**
 - Effective tt BG rejection by cutting Y_{cut} values at 0.002



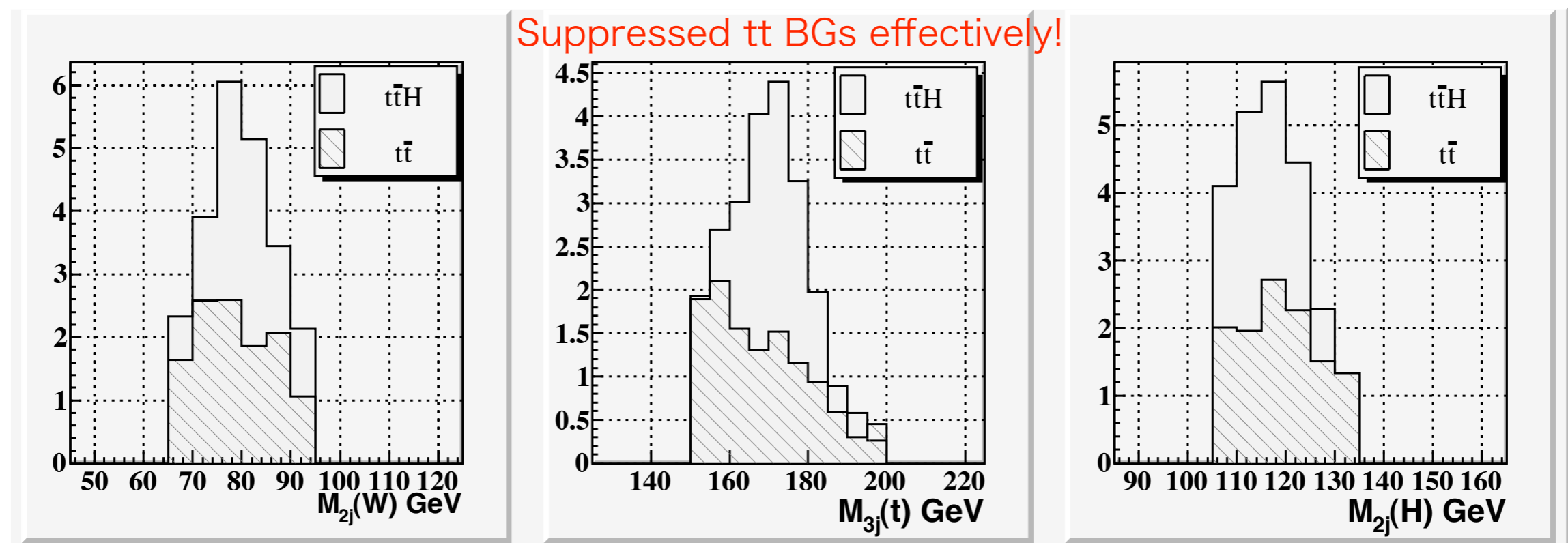
4) **Jet-parton association => Mass cut**

- Looping over **all the 2-jet combinations** => Look for a pair having an invariant mass => $\pm 15\text{GeV}$ from $M_W(80.0\text{GeV})$
- From the **remaining 4-jets** => **Pick up one** and attach it to the pair making a W candidate => $\pm 25\text{GeV}$ from $M_t(175\text{GeV})$
- Search **a pair from the 3-jets left over** => $\pm 15\text{GeV}$ from $M_H(120\text{GeV})$
- Chance to have **multiple combinations** since these mass window cuts are rather loose
- **Select the combination with the smallest χ^2**

$$\chi^2 = \left(\frac{M_{2\text{-jet}(W)} - M_W}{\sigma_{M_W}} \right)^2 + \left(\frac{M_{3\text{-jet}(t/\bar{t})} - M_t}{\sigma_{M_t}} \right)^2 + \left(\frac{M_{2\text{-jet}(H)} - M_H}{\sigma_{M_H}} \right)^2$$

Reduction of huge tt BGs (cont'd)

- For the tt BG rejection, **quad b-tagging is very powerful** since ttH has 4 b-jets, while tt BG has **only 2 b-jets**
- Use ordinary **n-sig method** for the quad b-tagging for the moment
- Defined **tight b-tagging** ($n_{\sigma b}$, #off-vtx-trk) = (3.0, 2) / **loose b-tagging** ($n_{\sigma b}$, #off-vtx-trk) = (2.0, 2)
- Require all of the 4 b-jet candidates have to satisfy the loose b-tagging condition and there has to be at least one tight b-tagged jet from each of the H and t/tbar candidates



Mass dists. after using both **mass cut** and the **quad b-tagging**

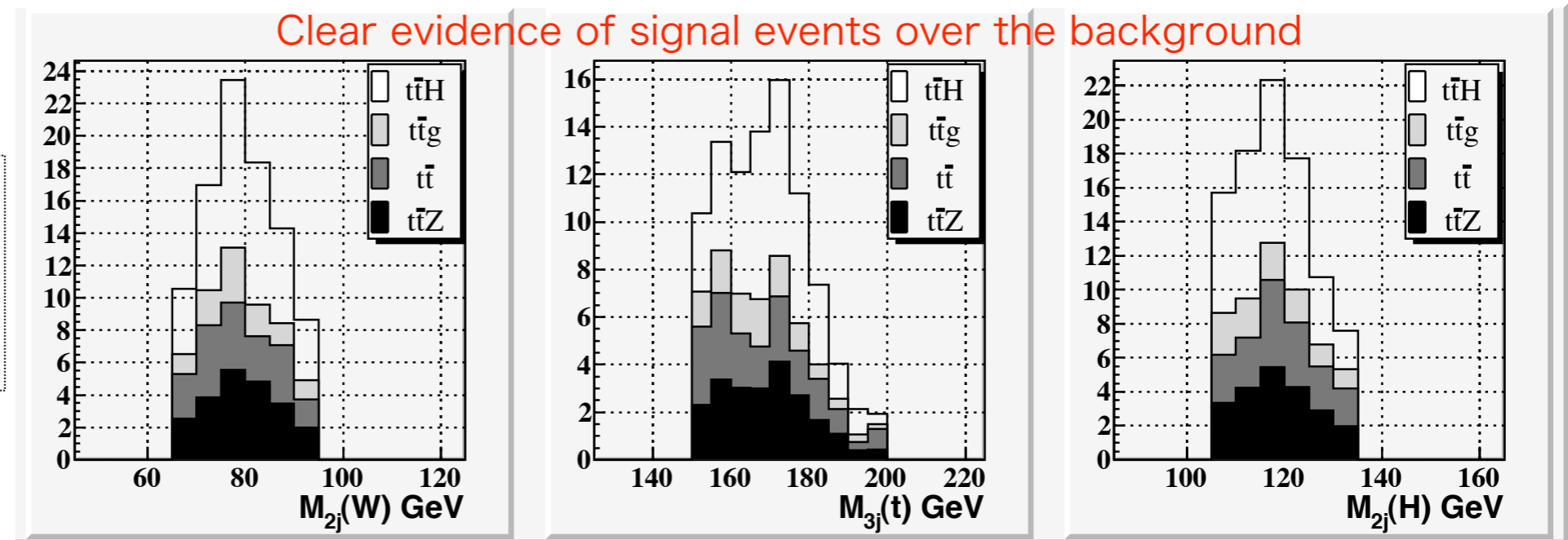
- **ttZ (Z->bb)** and **ttg (g->bb)** BGs have similar signature as a ttH
 → can be separated only with the invariant mass of the H candidate

Final cut statistics

- Normalized to integrated luminosity: 1 ab^{-1}
 - # generated events: 5M for $t\bar{t}$ / 50k for $t\bar{t}H, t\bar{t}Z, t\bar{t}g$ ($g \rightarrow b\bar{b}$)

Beam Polarization Processes	(0.0,0.0)				(-0.8,+0.3)			
	$t\bar{t}H$	$t\bar{t}Z$	$t\bar{t}$	$t\bar{t}g$ ($b\bar{b}$)	$t\bar{t}H$	$t\bar{t}Z$	$t\bar{t}$	$t\bar{t}g$ ($b\bar{b}$)
No Cut	449.0	1340.0	514040.5	697.5	759.0	2407	863500.4	1159.6
$N_{iso.lep}=1$	159.4	435.9	209718.4	242.2	269.4	783.0	303879.0	397.7
Y_{cut} (6 jets) > 0.002	139.2	307.8	22851.3	152.5	235.4	552.9	38477.2	249.6
btag & mass cut	23.0	12.2	11.9	6.9	38.9	21.8	19.7	11.3

Mass dists. (cumulative) for the final selected samples for the beam polarization combination: $(e^-, e^+) = (-0.8, +0.3)$



Beam pol. combination	No beam pol.	$(e^-, e^+) = (-0.8, +0.3)$
Significance	4.1σ	5.4σ
$\Delta g_{\gamma^t} / g_{\gamma^t}$	± 0.12	± 0.093

Summary

- Performed a **feasibility study of measuring the top-quark Yukawa coupling at $\sqrt{s} = 500\text{GeV}$** , taking advantage of the **NRQCD threshold enhancement to the t-tbar sub-system**
- Implemented the threshold correction in the ttH and ttZ event generators in the `physsim` package
- For **1-lepton + 6-jets mode of $e^+e^- \rightarrow \text{ttH}$** process, **signal significance 4.1σ without beam polarization**, and **5.4σ with the beam polarization combination: $(e^-, e^+) = (-0.8, +0.3)$** for an integrated luminosity of **1 ab^{-1}**
- **Measurement accuracy for the top-quark Yukawa coupling about 10%** using **only 1-lepton + 6-jets mode at $\sqrt{s} = 500\text{GeV}$** , which is the energy already available in the first stage of the ILC

Future prospects

- Increase signal statistics by **analyzing 8-jets mode** (45%)
- Introduce a **multivariate analysis** instead of cut-bases analysis
- Derive measurement accuracy for **\sqrt{s} dependence**

- Apply **full MC detector simulator** => realistic particle flow algorithm
- Adopt a high performance flavor tagging by using **LCFIVertex** package
- Do **full SM backgrounds scan**