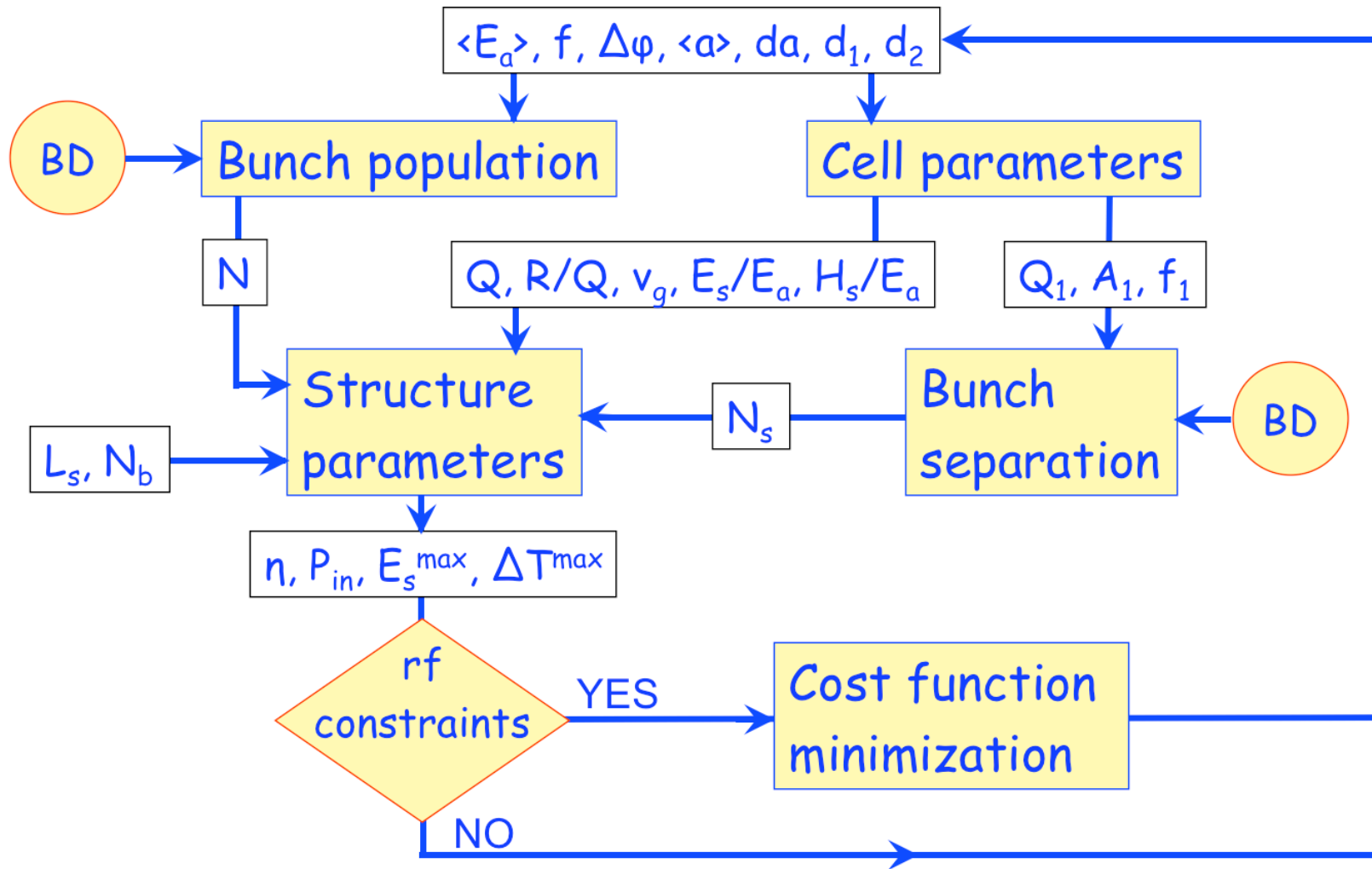


# Parameter Optimisation

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Beijing September 2009

# Work Flow



# Luminosity

Simplified treatment and approximations used throughout

$$\mathcal{L} = H_D \frac{N^2 f_{rep} n_b}{4\pi \sigma_x \sigma_y}$$

$$\mathcal{L} \propto H_D \frac{N}{\sqrt{\beta_x \epsilon_x} \sqrt{\beta_y \epsilon_y}} \eta P$$

$$\epsilon_x = \epsilon_{x,DR} + \epsilon_{x,BC} + \epsilon_{x,BDS} + \dots$$

$$\epsilon_y = \epsilon_{y,DR} + \epsilon_{y,BC} + \epsilon_{y,linac} + \epsilon_{y,BDS} \\ + \epsilon_{y,growth} + \epsilon_{y,offset} \dots$$

$$\sigma_{x,y} \propto \sqrt{\beta_{x,y} \epsilon_{x,y} / \gamma}$$

$$N f_{rep} n_b \propto \eta P$$

typically  $\epsilon_x \gg \epsilon_y$ ,

$$\beta_x \gg \beta_y$$

Fundamental limitations from

- beam-beam:  $N / \sqrt{\beta_x \epsilon_x}$ ,  $N / \sqrt{\beta_x \epsilon_x \beta_y \epsilon_y}$
- emittance generation and preservation:  $\sqrt{\beta_x \epsilon_x}$ ,  $\sqrt{\beta_y \epsilon_y}$
- main linac RF:  $\eta$

# Potential Limitations

- Efficiency  $\eta$ :  
depends on beam current that can be transported  
Decrease bunch distance  $\Rightarrow$  long-range transverse wakefields in main linac  
Increase bunch charge  $\Rightarrow$  short-range transverse and longitudinal wakefields in main linac, other effects
- Horizontal beam size  $\sigma_x$   
beam-beam effects, final focus system, damping ring, bunch compressors
- vertical beam size  $\sigma_y$   
damping ring, main linac, beam delivery system, bunch compressor, need to collide beams, beam-beam effects
- Will try to show how to derive  $L_{bx}(f, a, \sigma_a, G)$

# Beam Size Limit at IP

- The vertical beam size had been  $\sigma_y = 1 \text{ nm}$  (BDS)  
 $\Rightarrow$  challenging enough, so keep it  $\Rightarrow \epsilon_y = 10 \text{ nm}$
- Fundamental limit on horizontal beam size arises from beamstrahlung  
 Two regimes exist depending on beamstrahlung parameter

$$\Upsilon = \frac{2\hbar\omega_c}{3E_0} \propto \frac{N\gamma}{(\sigma_x + \sigma_y)\sigma_z}$$

$\Upsilon \ll 1$ : classical regime,  $\Upsilon \gg 1$ : quantum regime

At high energy and high luminosity  $\Upsilon \gg 1$

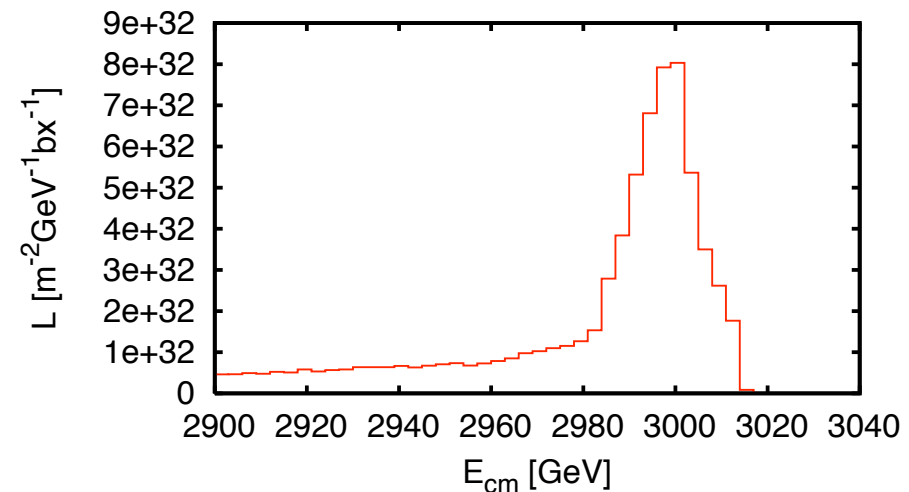
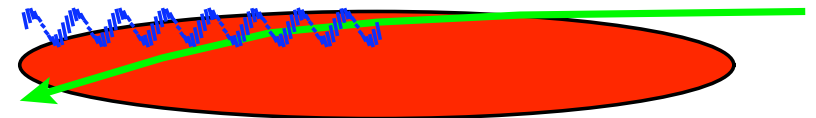
$$\mathcal{L} \propto \Upsilon\sigma_z/\gamma P\eta$$

$\Rightarrow$  partial suppression of beamstrahlung

$\Rightarrow$  coherent pair production

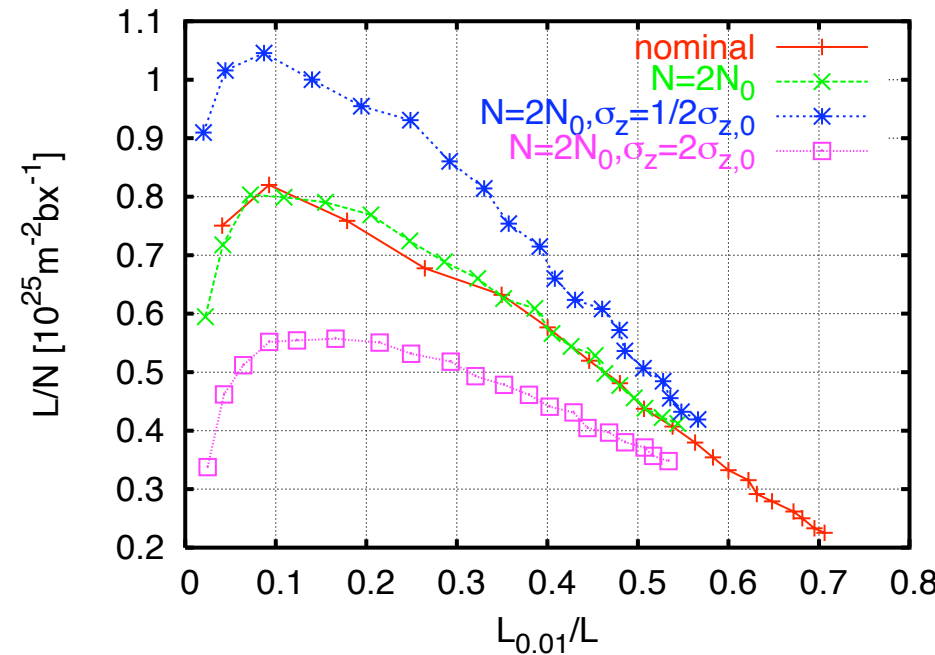
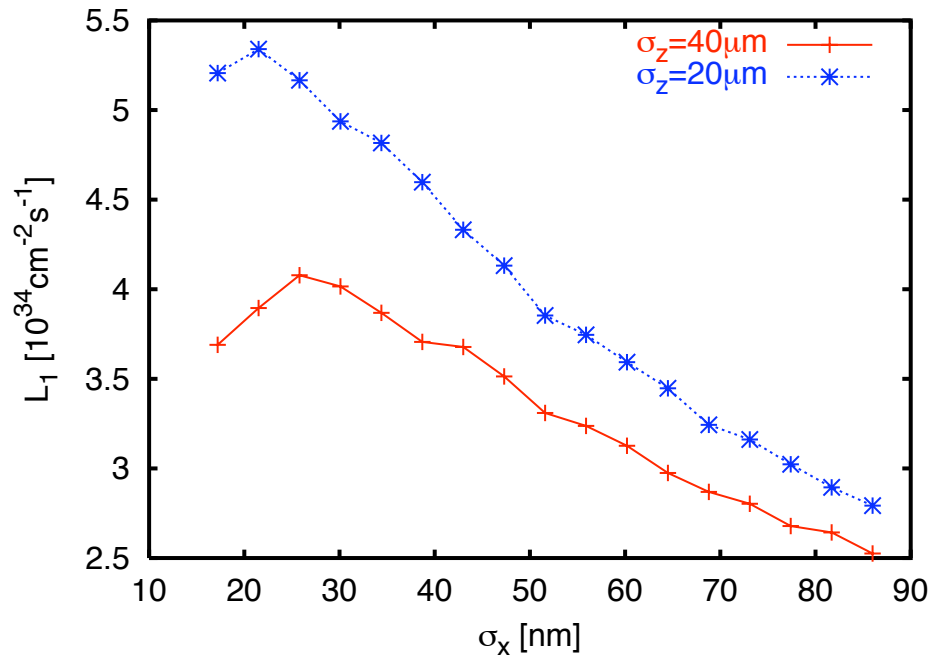
In CLIC  $\langle \Upsilon \rangle \approx 6$ ,  $N_{coh} \approx 0.1N$

$\Rightarrow$  somewhat in quantum regime



$\Rightarrow$  Use luminosity in peak as figure of merit

# Luminosity Optimisation at IP



Total luminosity for  $\Upsilon \gg 1$

$$\mathcal{L} \propto \frac{N}{\sigma_x \sigma_y} \eta \propto \frac{n_\gamma^{3/2}}{\sqrt{\sigma_z}} \frac{\eta}{\sigma_y}$$

large  $n_\gamma \Rightarrow$  higher  $\mathcal{L} \Rightarrow$  degraded spectrum

chose  $n_\gamma$ , e.g. maximum  $L_{0.01}$  or  $L_{0.01}/L = 0.4$  or ...

$$\mathcal{L}_{0.01} \propto \frac{\eta}{\sqrt{\sigma_z} \sigma_y}$$

# Other Beam Size Limitations

- Final focus system squeezes beams to small sizes with main problems:
    - beam has energy spread (RMS of  $\approx 0.35\%$ )  $\Rightarrow$  avoid chromaticity
    - synchrotron radiation in bends  $\Rightarrow$  use weak bends  $\Rightarrow$  long system
    - radiation in final doublet (Oide Effect)
  - Large  $\beta_{x,y} \Rightarrow$  large nominal beam size
  - Small  $\beta_{x,y} \Rightarrow$  large distortions
  - Beam-beam simulation of nominal case: effective  $\sigma_x \approx 40$  nm,  $\sigma_y \approx 1$  nm
- $\Rightarrow$  lower limit of  $\sigma_x \Rightarrow$  for small  $N$  optimum  $n_\gamma$  cannot be reached
- new FFS reaches  $\sigma_x \approx 40$  nm,  $\sigma_y \approx 1$  nm
- Assume that the transverse emittances remain the same
    - not strictly true
    - emittance depends on charge in damping ring (e.g.  $\epsilon_x(N = 2 \times 10^9) = 450$  nm,  $\epsilon_x(N = 4 \times 10^9) = 550$  nm)

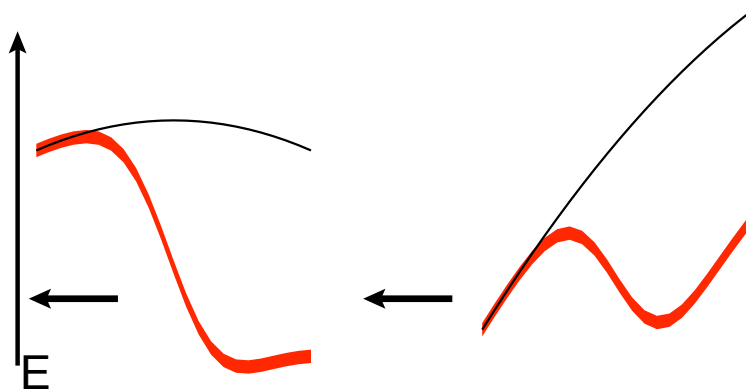
# Beam Dynamics Work Flow

- The parameter optimisation has been performed keeping the main linac beam dynamics tolerances at the same level as for the original 30 GHz design
  - The minimum spot size at the IP is dominated by BDS and damping ring
    - adjusted  $N/\sigma_x$  for large bunch charges to respect beam-beam limit
  - For each of the different frequencies and values of  $a/\lambda$  a scan in bunch charge  $N$  has been performed
    - the bunch length has been determined by requiring the final RMS energy spread to be  $\sigma_E/E = 0.35\%$  and running  $12^\circ$  off-crest
    - the transverse wake-kick at  $2\sigma_z$  has been determined
    - the bunch charge which gave the same kick as the old parameters has been chosen
  - The wakefields have been calculated using some formulae from K. Bane
    - used them partly outside range of validity
    - ⇒ but still a good approximation, confirmed by RF experts
- ⇒  $N$  and  $L_{bx}(f, a, \sigma_a, G)$  given to RF experts



# Beam Loading and Bunch Length

- Aim for shortest possible bunch (wakefields)
- Energy spread into the beam delivery system should be limited to about 1% full width or 0.35% RMS
- Multi-bunch beam loading compensated by RF
- Single bunch longitudinal wakefield needs to be compensated  
⇒ accelerate off-crest



- Limit around average  $\Delta\Phi \leq 12^\circ$   
⇒  $\sigma_z = 44 \mu\text{m}$  for  $N = 3.72 \times 10$

# Specific Wakefields

- Longitudinal wakefields contain more than the fundamental mode
- We will use wakefields based on fits derived by Karl Bane

$l$  length of the cell

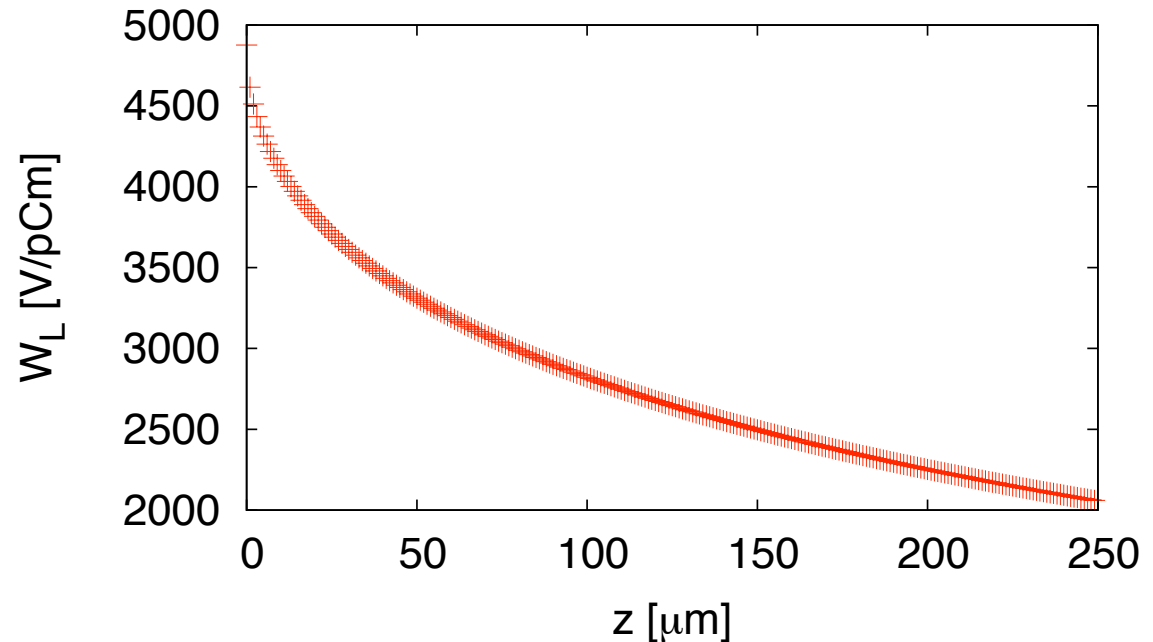
$a$  radius of the iris aperture

$g$  length between irises

$$s_0 = 0.41a^{1.8}g^{1.6}\left(\frac{1}{l}\right)^{2.4}$$

$$W_L = \frac{Z_0c}{\pi a^2} \exp\left(-\sqrt{\frac{s}{s_0}}\right)$$

- Use CLIC structure parameters



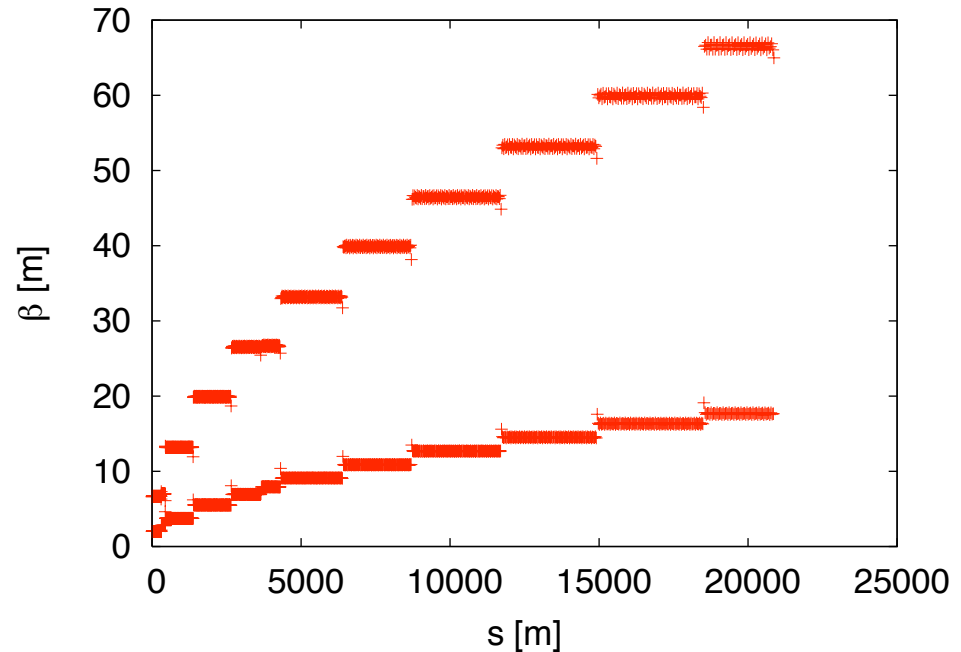
- Summation of an infinite number of cosine-like modes
  - calculation in time domain or approximations for high frequency modes

# Recipe for Choosing the Bunch Parameters

- Decide on the average RF phase
  - OK, we fix  $12^\circ$
- Decide on an acceptable energy spread at the end of the linac
  - OK, we chose 0.35%
- Determine  $\sigma_z(N)$ 
  - chose a bunch charge
  - vary the bunch length until the final energy spread is acceptable
  - chose next charge
- Determine which bunch charge (and corresponding bunch length) can be transported stably

# CLIC Lattice Design

- Used  $\beta \propto \sqrt{E}$ ,  $\Delta\Phi = \text{const}$ 
  - balances wakes and dispersion
  - roughly constant fill factor
  - phase advance is chosen to balance between wakefield and ground motion effects
- Preliminary lattice
  - made for  $N = 3.7 \times 10^9$
  - quadrupole dimensions need to be confirmed
  - some optimisations remain to be done
- Total length 20867.6m
  - fill factor 78.6%



- 12 different sectors used
- Matching between sectors using 7 quadrupoles to allow for some energy bandwidth

# CLIC Fill Factor

- Want to achieve a constant fill factor
  - to use all drive beams efficiently
- Scaling  $f = f_0 \sqrt{E/E_0}$  yields

$$L_q \propto \frac{E}{\sqrt{\frac{E}{E_0}}} \propto \sqrt{E}$$

using a quadrupole spacing of  $L = L_0 \sqrt{E/E_0}$  leads to

$$\frac{L_q}{L} \propto \frac{\sqrt{E}}{\sqrt{E}} \propto \text{const}$$

- ⇒ The choice allows to maintain a roughly constant fill factor
- ⇒ It maximises the focal strength along the machine

# Magnet Considerations

- The maximum strength of a focusing magnet is limited
  - for a normal conducting design rule of thumb is 1 T at the poletip

⇒ Required integrated magnet strength is

$$\frac{\text{T}}{\text{m}} \frac{E}{0.3 \text{ GeV}} \frac{\text{m}}{f}$$

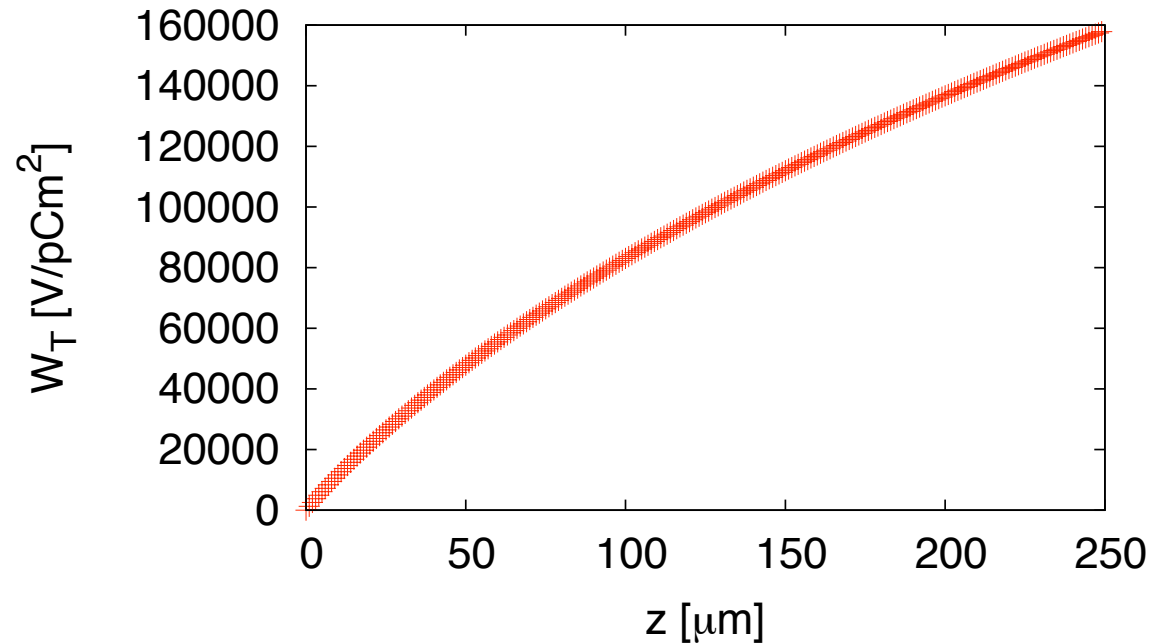
- For CLIC poletip radius is given by practical considerations of magnet design  $a \approx 5 \text{ mm}$  yielding a gradient of 200 T/m
- We chose about 10% of the machine to be quadrupoles
  - ⇒ fill factor is  $\approx 80\%$ 
    - 10% are lost for flanges (mainly on structures)
- Use  $L_0 = 1.5 \text{ m}$  and  $f_0 = 1.3 \text{ m}$  yields

$$\eta_q = \frac{E_0}{0.3 \text{ GeV}} \frac{\text{T/m}}{200 \text{ T/m}^2} \frac{\text{m}}{f_0} \frac{1}{L_0}$$
$$\Rightarrow \eta_q \approx 7.7\%$$

- We use discrete lengths hence we loose a bit more

# Example of a Transverse Wakefield (CLIC)

Fit obtained by K. Bane  
 For short distances the wake-field rises linear  
 Summation of an infinite number of sine-like modes with different frequencies



$$s_0 = 0.169a^{1.79}g^{0.38} \left(\frac{1}{l}\right)^{1.17}$$

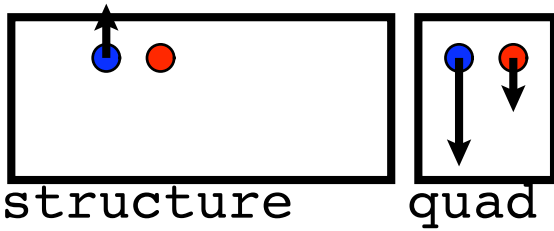
$$w_{\perp}(s) = 4 \frac{Z_0 c s_0}{\pi a^4} \left[ 1 - \left( 1 + \sqrt{\frac{s}{s_0}} \right) \exp \left( -\sqrt{\frac{s}{s_0}} \right) \right]$$

$$w_{\perp}(s) \approx 4 \frac{Z_0 c s_0}{\pi a^4} \left[ 1 - \left( 1 + \sqrt{\frac{s}{s_0}} \right) \left( 1 - \sqrt{\frac{s}{s_0}} \right) \right] = 4 \frac{Z_0 c s_0}{\pi a^4} \left[ 1 - \left( 1 - \frac{s}{s_0} \right) \right] = 4 \frac{Z_0 c s}{\pi a^4}$$

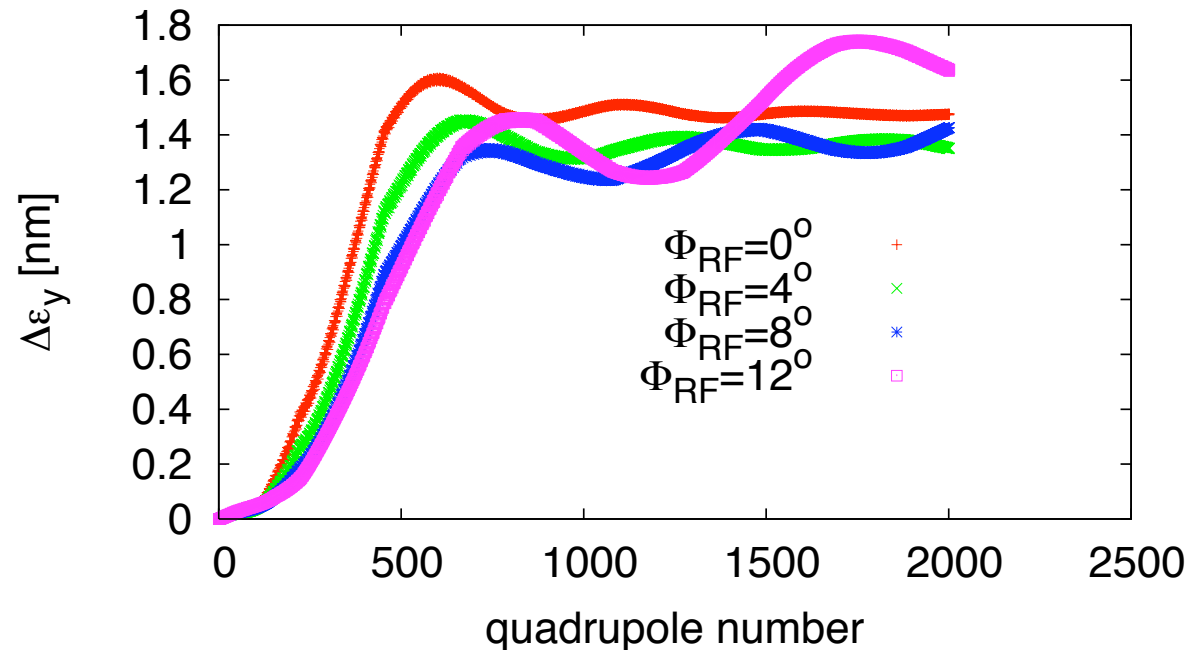
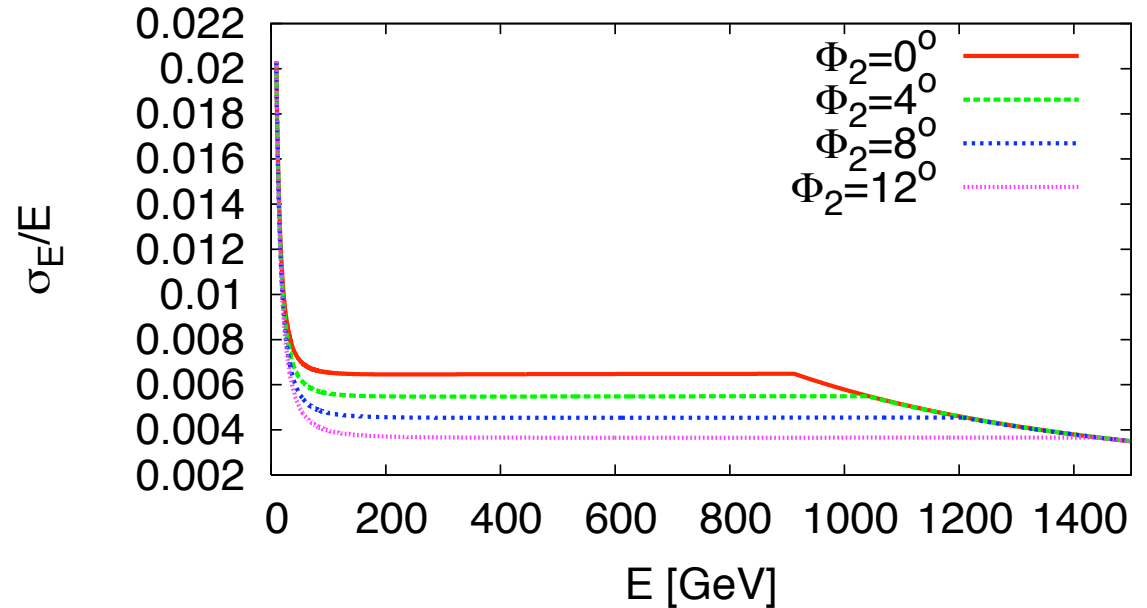
# Energy Spread and Beam Stability

- Trade-off in fixed lattice
  - large energy spread is more stable
  - small energy spread is better for alignment

⇒ Beam with  $N = 3.7 \times 10^9$  can be stable



⇒ Tolerances are not a unique number



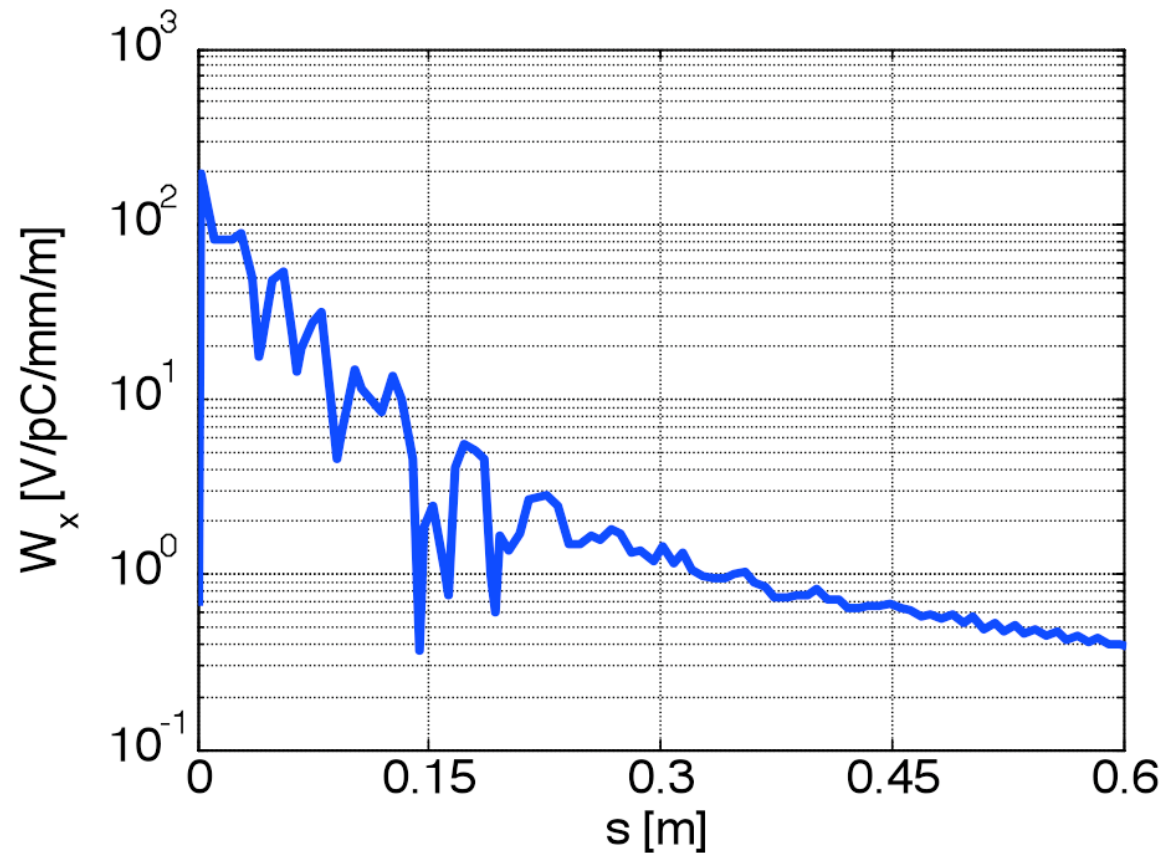


# Remember: Multi-Bunch Wakefields

- Long-range transverse wakefields have the form

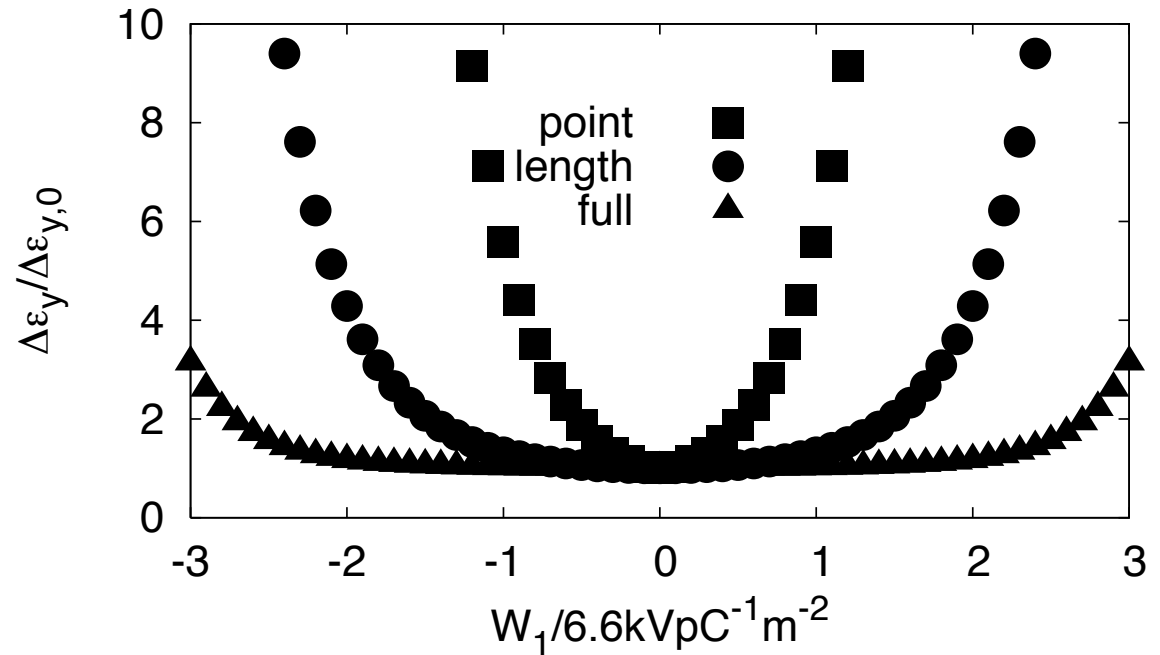
$$W_{\perp}(z) = \sum_i^{\infty} 2k_i \sin\left(2\pi \frac{z}{\lambda_i}\right) \exp\left(-\frac{\pi z}{\lambda_i Q_i}\right)$$

- In practice need to consider only a limited number of modes
- Their impact can be reduced by detuning and damping



# Multi-Bunch Jitter

- If bunches are not point-like the results change
  - an energy spread leads to a more stable case
- Simulations show
  - point-like bunches
  - bunches with energy spread due to bunch length
  - including also initial energy spread

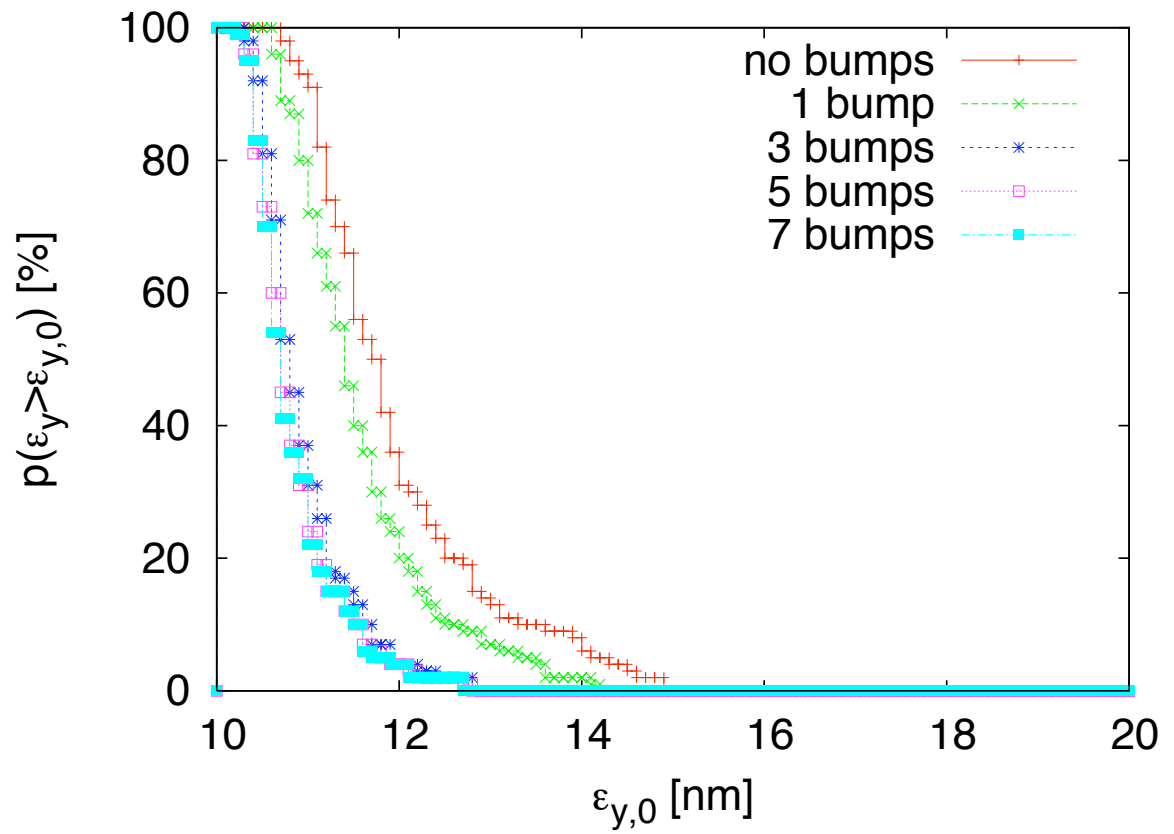


⇒ Point-like bunches is a pessimistic assumption for the dynamic effects

# Final Emittance Growth (CLIC)

| imperfection                  | with respect to    | symbol         | value                  | emitt. growth     |
|-------------------------------|--------------------|----------------|------------------------|-------------------|
| BPM offset                    | wire reference     | $\sigma_{BPM}$ | 14 $\mu\text{m}$       | 0.367 nm          |
| BPM resolution                |                    | $\sigma_{res}$ | 0.1 $\mu\text{m}$      | 0.04 nm           |
| accelerating structure offset | girder axis        | $\sigma_4$     | 10 $\mu\text{m}$       | 0.03 nm           |
| accelerating structure tilt   | girder axis        | $\sigma_t$     | 200 $\mu\text{radian}$ | 0.38 nm           |
| articulation point offset     | wire reference     | $\sigma_5$     | 12 $\mu\text{m}$       | 0.1 nm            |
| girder end point              | articulation point | $\sigma_6$     | 5 $\mu\text{m}$        | 0.02 nm           |
| wake monitor                  | structure centre   | $\sigma_7$     | 5 $\mu\text{m}$        | 0.54 nm           |
| quadrupole roll               | longitudinal axis  | $\sigma_r$     | 100 $\mu\text{radian}$ | $\approx 0.12$ nm |

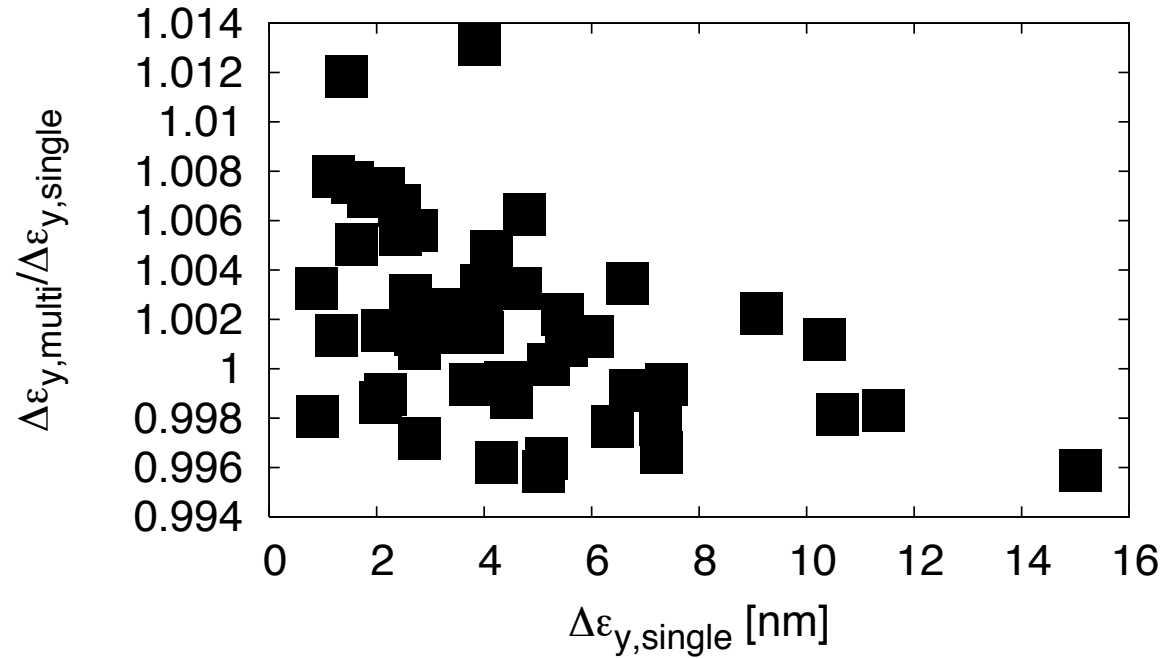
- Selected a good DFS implementation
  - trade-offs are possible
- Multi-bunch wakefield misalignments of 10  $\mu\text{m}$  lead to  $\Delta\epsilon_y \approx 0.13$  nm
- Performance of local pre-alignment is acceptable



# Multi-Bunch Static Imperfections

- In CLIC

- we misalign all structures
- perform one-to-one steering with a multi-bunch beam
- perform one-to-one steering with a single bunch
- compare the emittance growth



# CLIC Example of Fast Imperfection Tolerances

- Many sources exist

| Source                               | Luminosity budget | Tolerance   |
|--------------------------------------|-------------------|---|
| Damping ring extraction jitter       | 1%                |   |
| Magnetic field variations            | ?%                |   |
| Bunch compressor jitter              | 1%                |   |
| Quadrupole jitter in main linac      | 1%                | $\Delta\epsilon_y = 0.4 \text{ nm}$<br>$\sigma_{jitter} \approx 1.8 \text{ nm}$       |
| Structure pos. jitter in main linac  | 0.1%              | $\Delta\epsilon_y = 0.04 \text{ nm}$<br>$\sigma_{jitter} \approx 800 \text{ nm}$      |
| Structure angle jitter in main linac | 0.1%              | $\Delta\epsilon_y = 0.04 \text{ nm}$<br>$\sigma_{jitter} \approx 400 \text{ nradian}$ |
| RF jitter in main linac              | 1%                |   |
| Crab cavity phase jitter             | 1%                | $\sigma_\phi \approx 0.01^\circ$  |
| Final doublet quadrupole jitter      | 1%                | $\sigma_{jitter} \approx 0.1 \text{ nm}$  |
| Other quadrupole jitter in BDS       | 1%                |   |
| ...                                  | ?%                |   |

# RF Constraints

- To limit the breakdown rate and the severeness of the breakdowns
- The maximum surface field has to be limited

$$\hat{E} < 260 \text{ MV/m}$$

- The temperature rise at the surface needs to be limited

$$\Delta T < 56 \text{ T}$$

- The power flow needs to be limited
  - related to the badness of a breakdown

empirical parameter is

$$P/(2\pi a)\tau^{\frac{1}{3}} < 18 \frac{\text{MW}}{\text{mm}} \text{ns}^{\frac{1}{3}}$$

# RF Work Flow

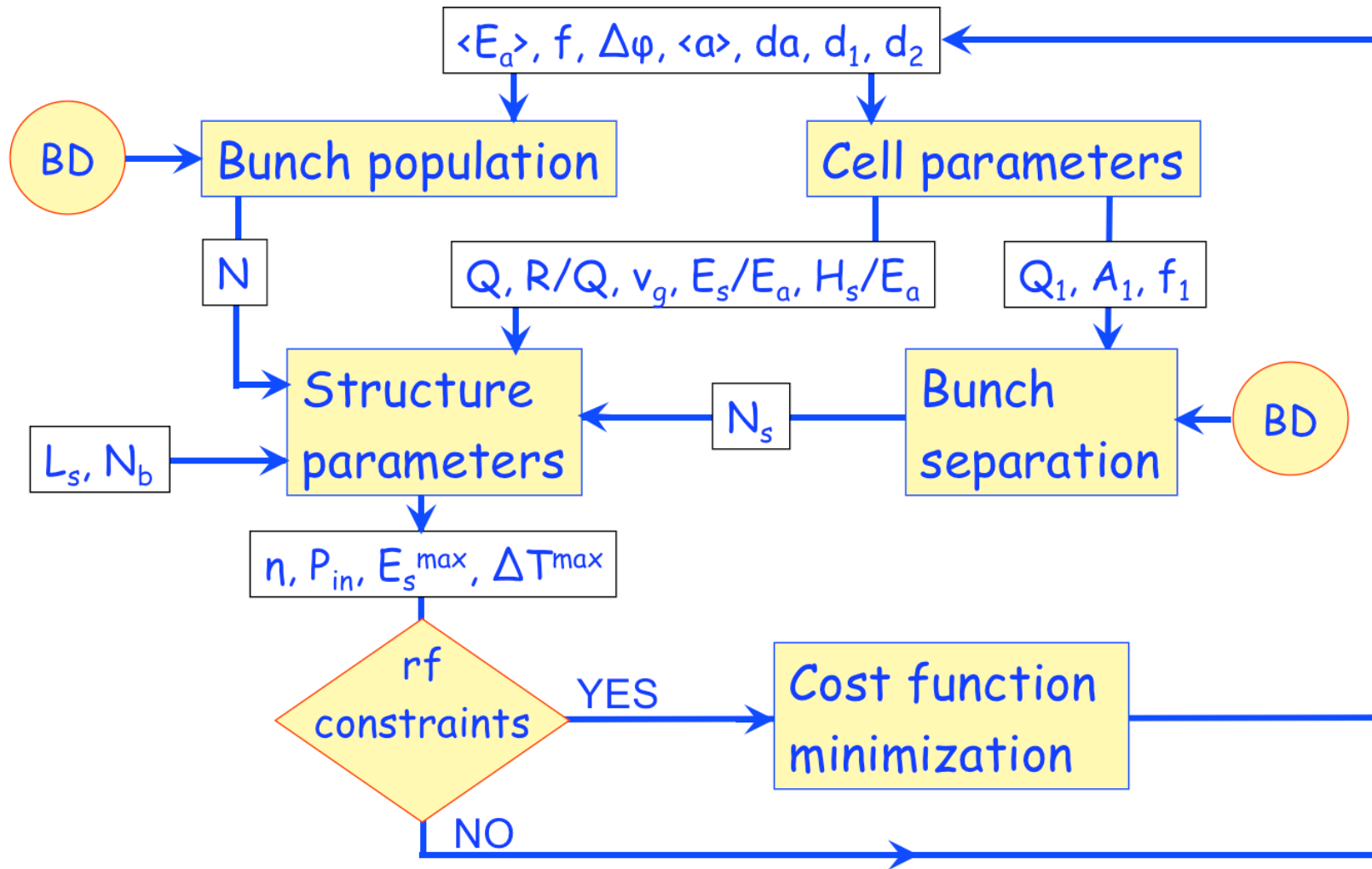
- Calculate RF properties of cells with different  $a/\lambda$ 
  - structures can be constructed by interpolating between these values
- Remove all structures with a too high surface field
- Determine the pulse length supported by the structure
- Estimate long-range wake and chose bunch distance
  - bunch charge is given by beam dynamics
- Calculate RF to beam efficiency for the structure

# Cost Model

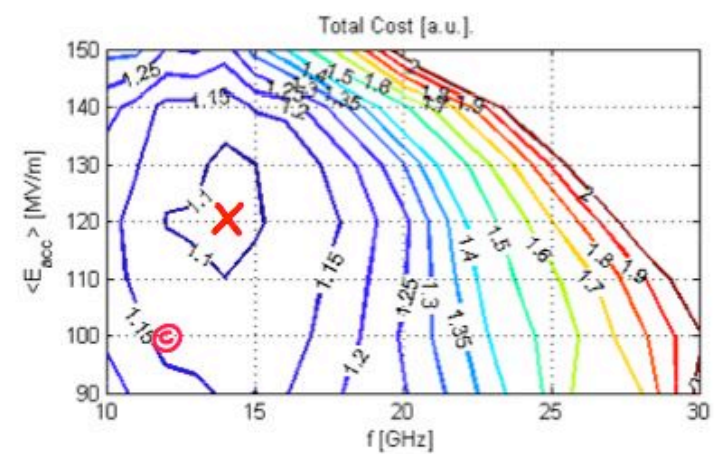
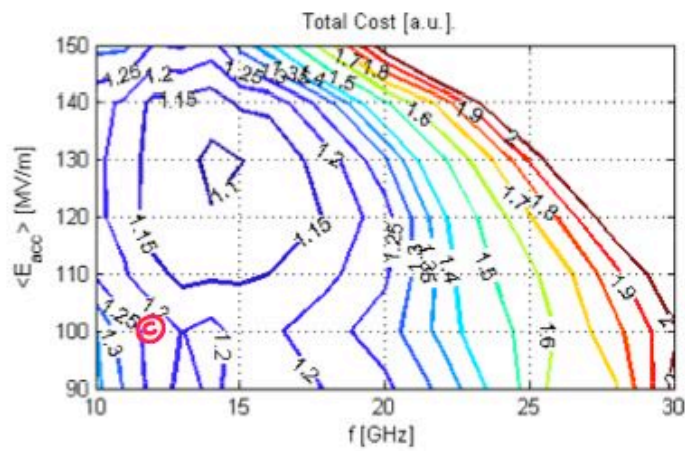
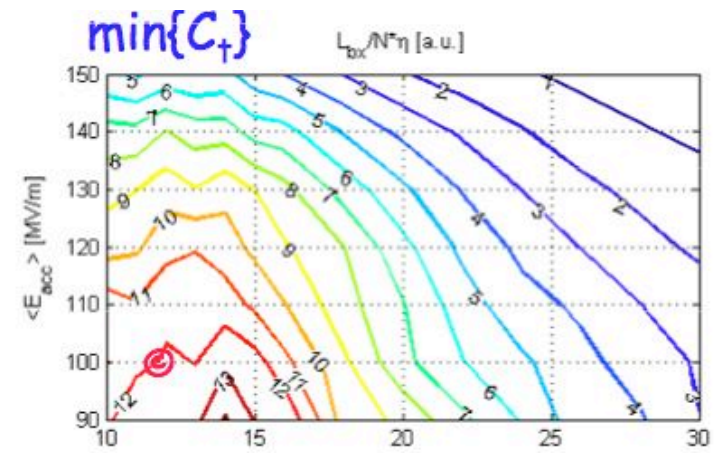
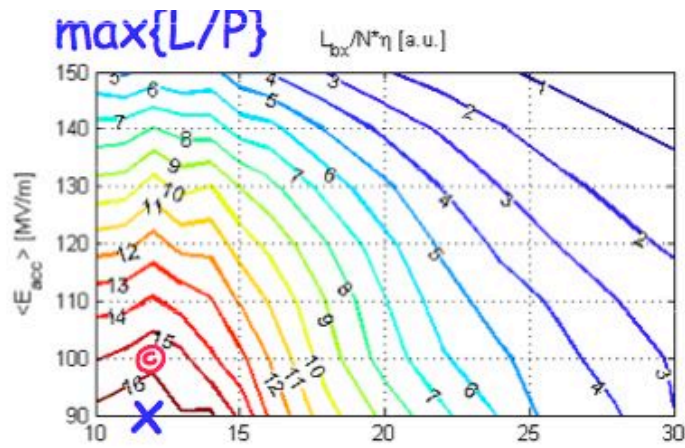
- The machine should be optimised for lowest cost
  - power consumption will also limit the choice
- A simplified cost model can be developed
  - e.g. cost per unit length of linac
  - energy to be stored in drive beam accelerator modulators per pulse
  - ...
- With this model one can identify the cheapest machine



# Work Flow

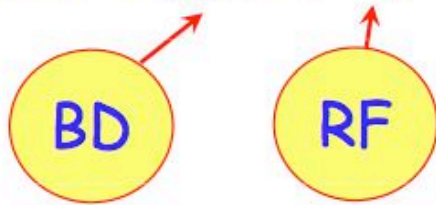


# Results



## Results 2

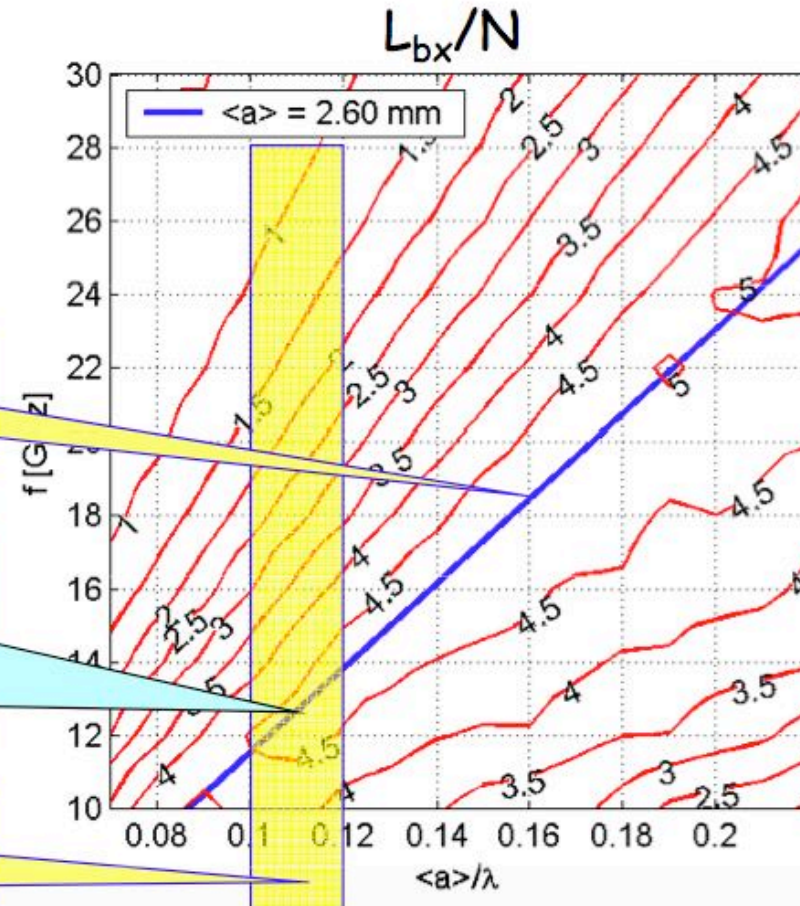
$$\text{FoM} = L_{bx}/N \cdot n$$



BD optimum aperture:  
 $\langle a \rangle = 2.6 \text{ mm}$

**Why X-band ?**  
 Crossing gives optimum frequency

RF optimum aperture:  
 $\langle a \rangle / \lambda = 0.1 \div 0.12$

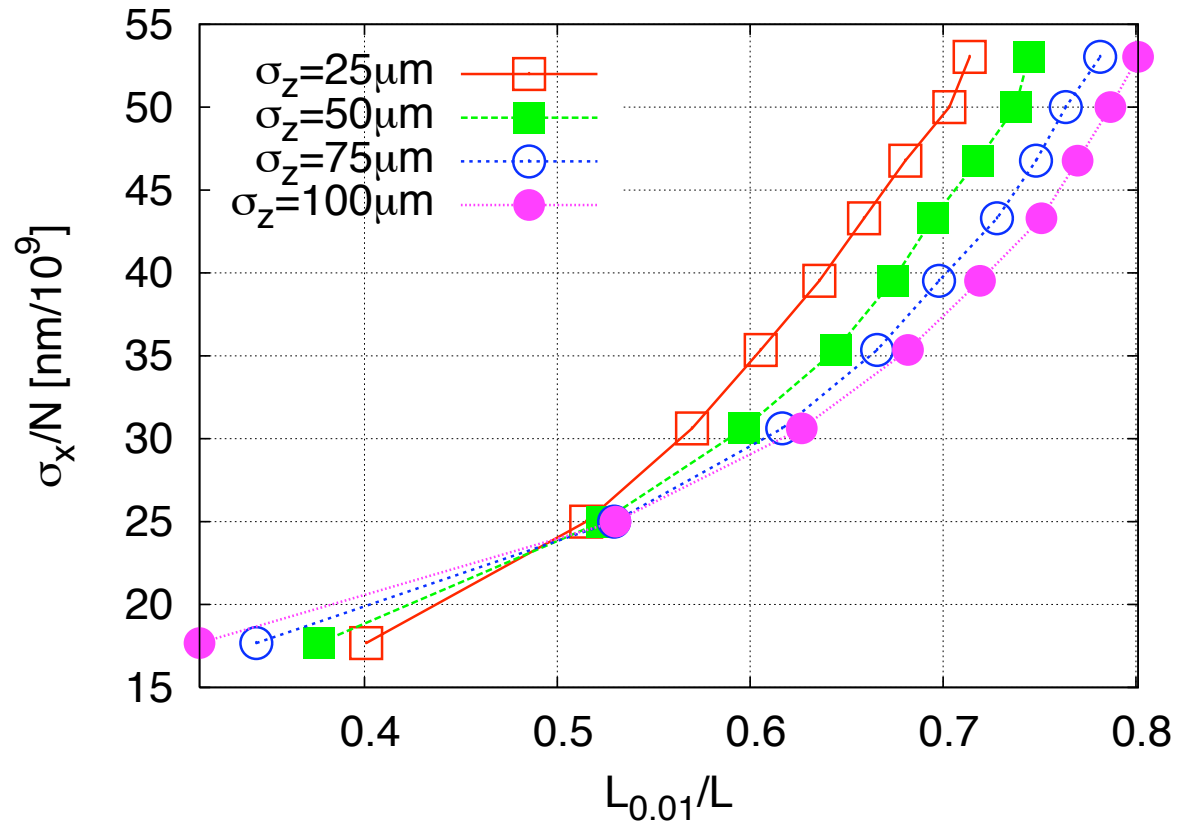


# Lattice at Lower Energy

# Required Beam Size (CLIC 500GeV)

- Roughly constant luminosity spectrum quality for constant  $N/\sigma_x$
- Required beam size is between 25 and 40 nm for beam with  $N = 10^9$  particles
  - scales with the square of the charge
- For  $\beta_x = 10$  mm and  $N = 4 \times 10^9$  requires  $\epsilon_x \approx 1 \mu\text{m}$

$$\epsilon_{x,opt} \approx \left( \frac{N}{4 \times 10^9} \right)^2 \frac{10 \text{ mm}}{\beta_x} \mu\text{m}$$



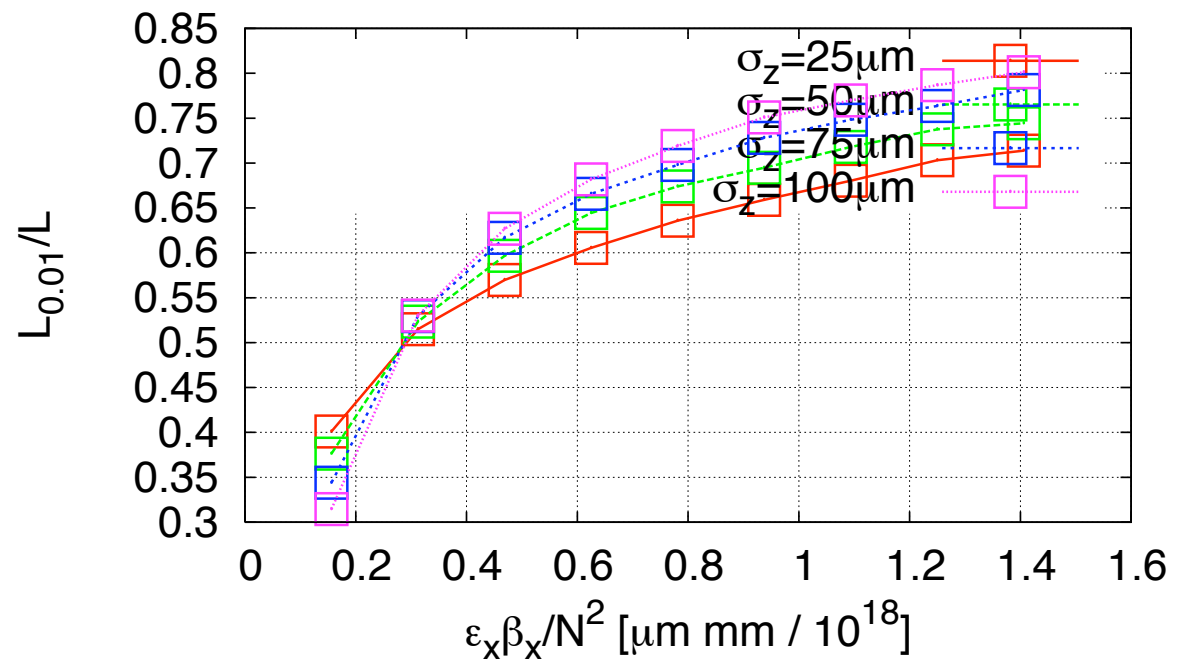
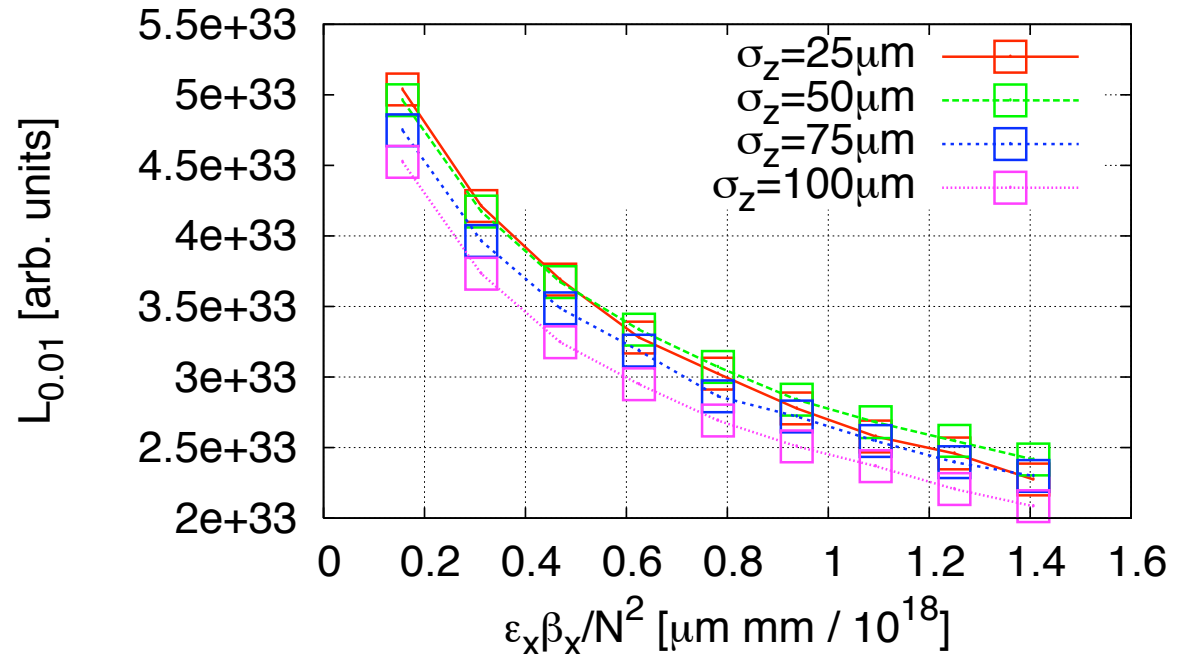
# Relative Luminosity

- Relevant parameter is

$$D = \frac{\beta_x}{\text{mm}} \frac{\epsilon_x}{\mu\text{m}} \left( \frac{10^9}{N} \right)^2$$

$$\frac{L_{bx}}{N} \propto \frac{1}{\sqrt{D}}$$

- Require this value to be in the range 0.3–0.7
    - $\approx 30\%$  more luminosity for lower value
  - NLC had  $N = 7.5 \times 10^9$ ,  $\beta_x = 10 \text{ mm}$  and  $\epsilon_x = 4 \mu\text{m}$ 
    - $D = 0.7$
- $\Rightarrow$  close to optimum



# Beam Jitter at Lower Energy

- Two main limitations
  - local beam stability
  - integrated residual effect along the machine
- To keep the local beam stability constant yields the limitation
  - $Nw_{\perp}(2\sigma_z) = \text{const}$
  - keeps the beam energy spread constant

- A second limitation arises from the integral effect

$$\frac{d}{ds} \frac{\Delta y' / \sigma'_y}{y / \sigma_y} \propto \frac{Nw_{\perp} \sigma_y}{E \sigma'_y}$$

- Integral using lattice scaling  $\beta = \beta_0 \sqrt{E(s)/E_0}$  yields

$$\frac{\Delta y' / \sigma'_y}{y / \sigma_y} \propto \frac{Nw_{\perp} \beta_0}{G} \sqrt{\frac{E_f}{E_0}}$$

- $Nw_{\perp}(2\sigma_z) = \text{const}$  is stronger limitation as long as
  - $G \geq \sqrt{E_f/E_{f,0}} G_0$
  - For 500 GeV  $G \geq 41 \text{ MV/m}$

# Emittance Growth at Lower Energy

- Express structure induced emittance growth as function of energy and gradient

$$\frac{d}{ds} \frac{\Delta\epsilon(s)}{\epsilon} \propto \left( \frac{Nw_{\perp}(2\sigma_z)\Delta y L_{cav}}{E(s)} \frac{1}{\sigma'_y(s)} \right)^2 \frac{1}{L_{cav}}$$

using the lattice scaling  $\beta = \beta_0 \sqrt{E(s)/E_0}$  one finds

$$\Delta\epsilon_{cav} \propto \frac{N^2 w_{\perp}^2 (2\sigma_z) \Delta y^2 \beta_0 L_{tot,cav}}{G} \sqrt{\frac{E_f}{E_0}}$$

⇒ Could increase  $Nw_{\perp}(2\sigma_z)$  by factor 2.4 at 500 GeV

- for constant gradient

- For constant  $Nw_{\perp}$  and  $L_{cav}$  we find  $G \geq 41$  MV/m
- For constant  $Nw_{\perp}$  and doubled  $L_{cav}$  we find  $G \geq 82$  MV/m
  - but for  $G = 50$  MV/m still only 1.6 times as high as at 3 TeV
- Dispersive emittance growth scales as

$$\Delta\epsilon_{tot,disp} \propto \frac{\Delta E^2 \Delta y^2}{G} \sqrt{\frac{E_f}{E_0}}$$

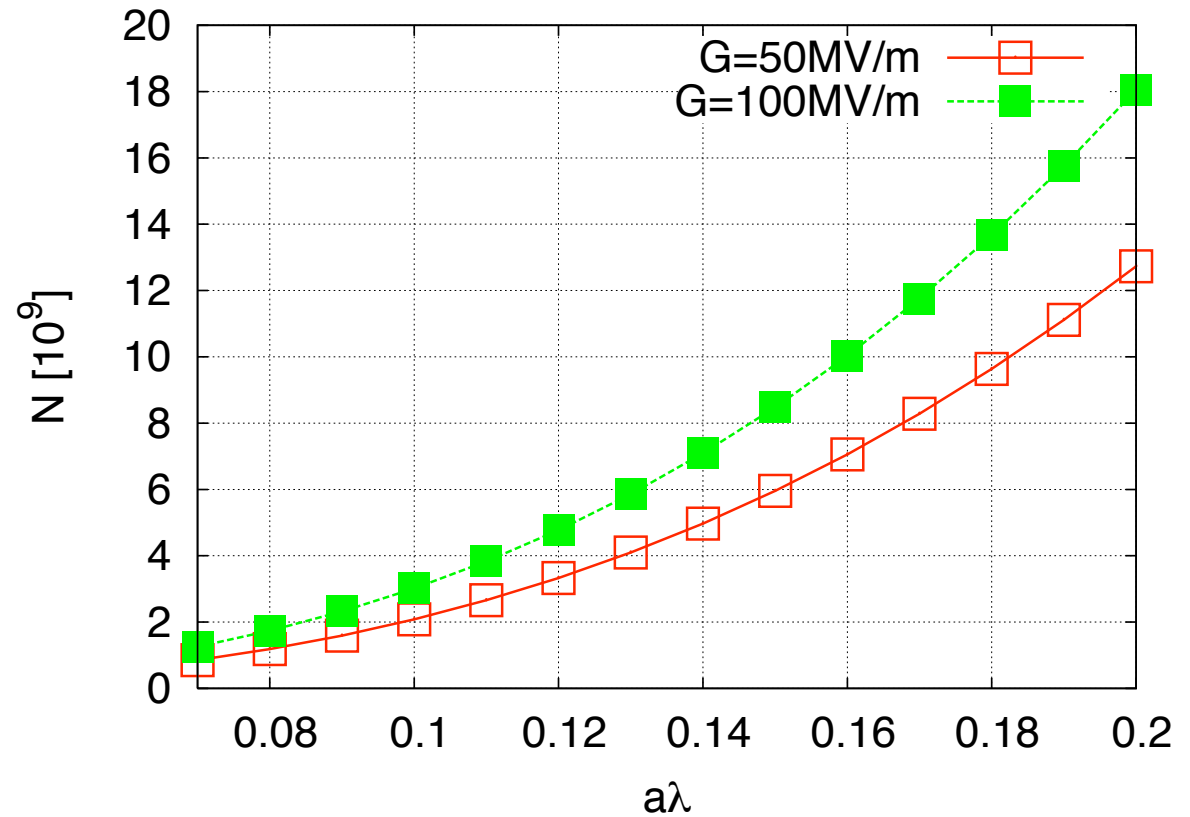
⇒ independent of structure length

- Total emittance growth should not increase much, first simulations confirm this



# Aperture and Bunch Charge

- Procedure is similar to the one for 3 TeV
  - $\sigma_y(N)$  from single bunch longitudinal wake
  - $N, \sigma_z$  from transverse single bunch wake
- Keep local beam stability constant
  - leads to less bunch charge than for 3 TeV
  - but longer bunches



# Luminosity

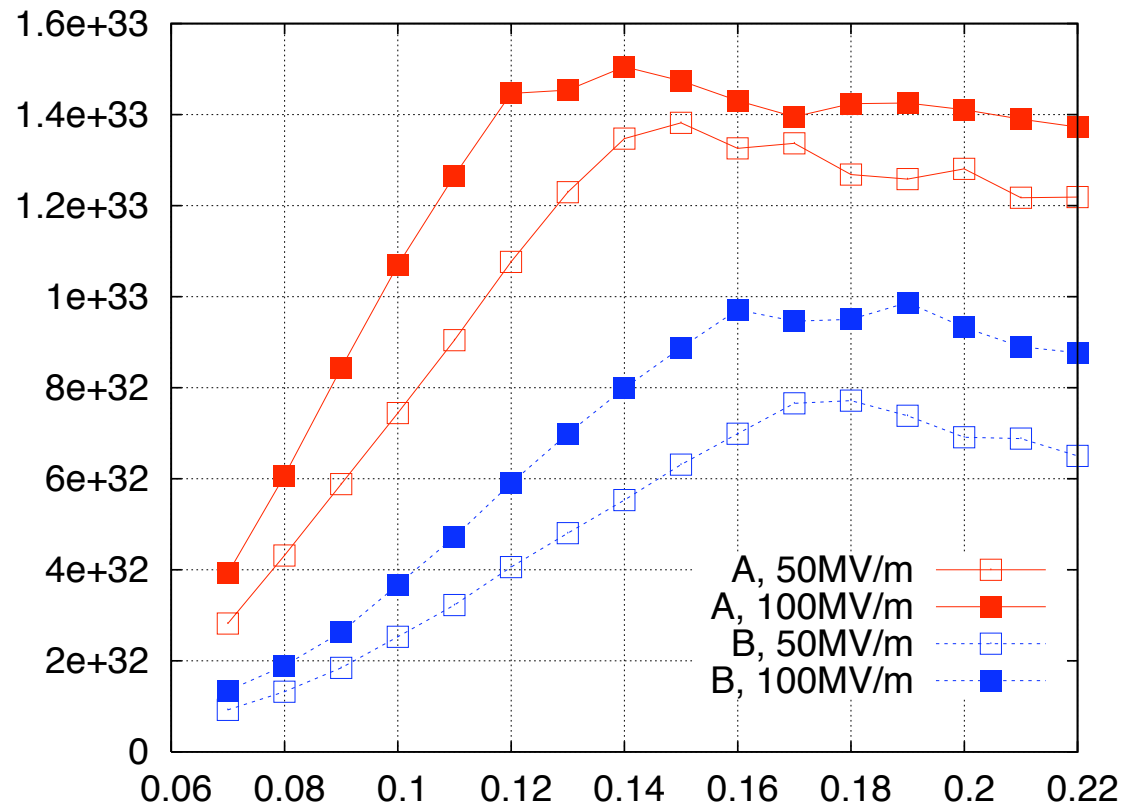
Assume the following

- case A

- emittance from 3 TeV
- beta-functions of  $\beta_x = 10 \text{ mm}$  and  $\beta_y = 0.1 \text{ mm}$  at the interaction point

- case B

- horizontal emittance from  $\epsilon_x = 3 \mu\text{m}$  at the damping ring to  $\epsilon_x = 4 \mu\text{m}$  at the interaction point
- vertical emittance from  $\epsilon_y = 10 \text{ nm}$  at the damping ring to  $\epsilon_y = 40 \text{ nm}$  at the interaction point
- beta-functions of  $\beta_x = 8 \text{ mm}$  and  $\beta_y = 0.1 \text{ mm}$  at the interaction point



# Thanks



Many thanks to you for listening (I hope) and to those who helped prearing lecture