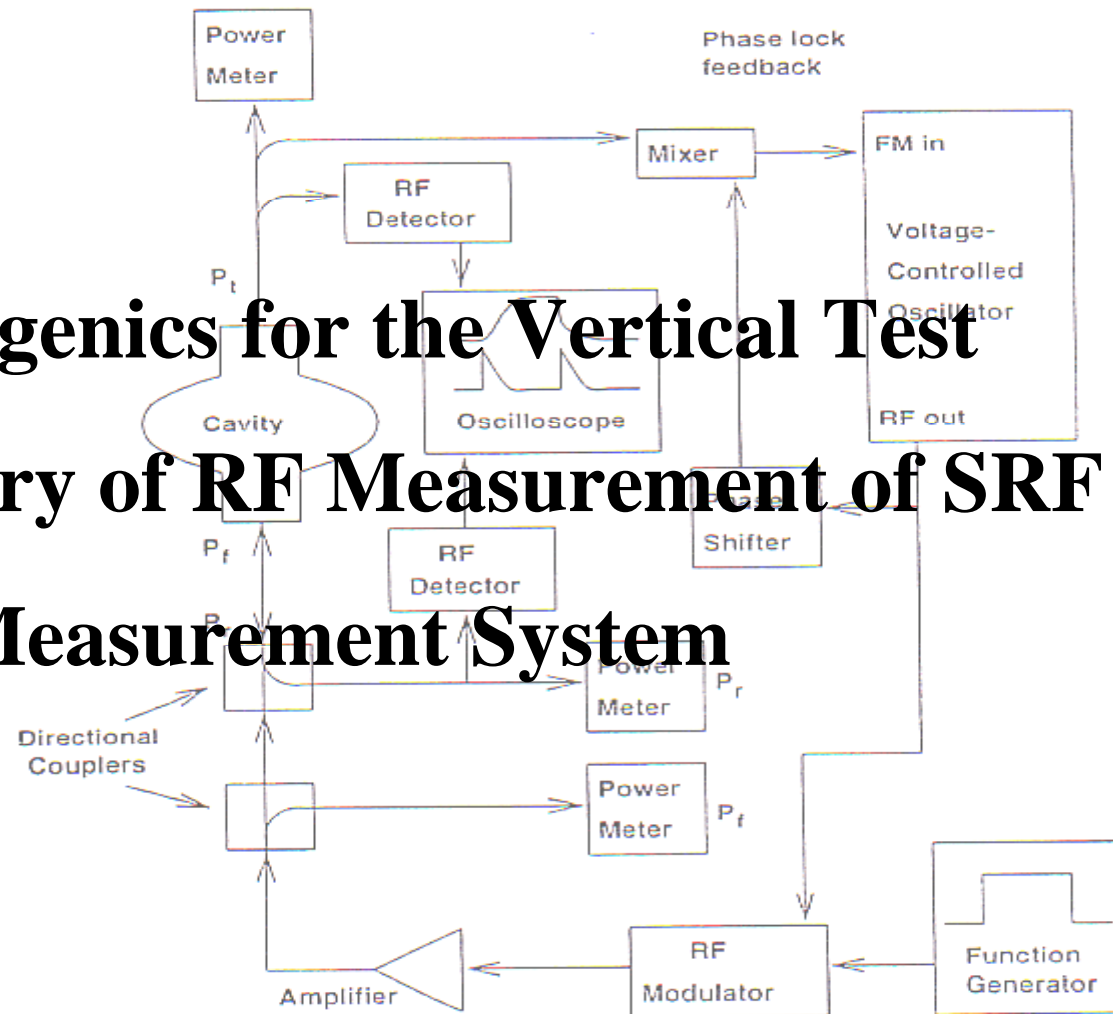


9. Performance Evaluation (Vertical Test)

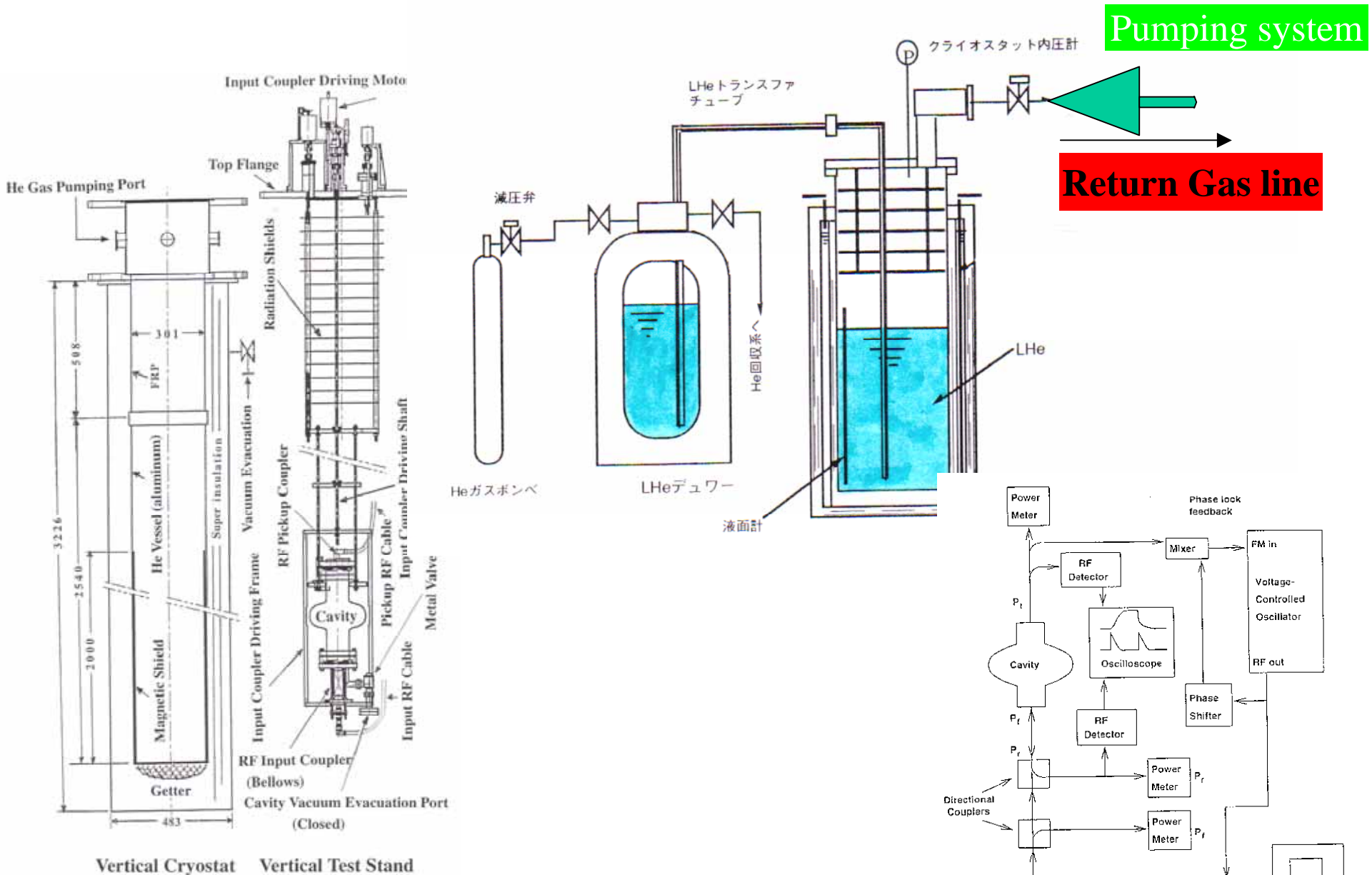
9.1 Cryogenics for the Vertical Test

9.2 Theory of RF Measurement of SRF Cavities

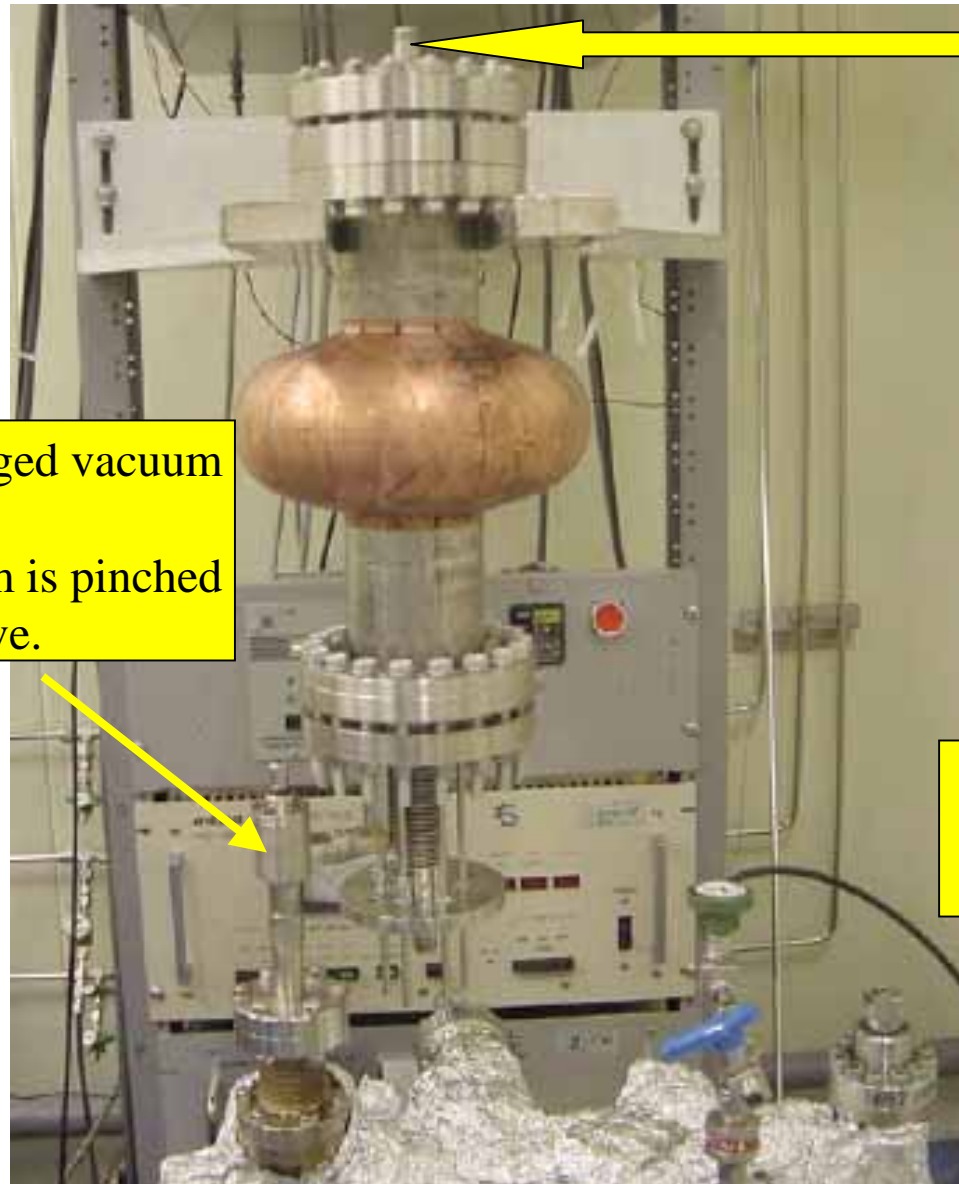
9.3 RF Measurement System



9.1 Cryogenics System for Vertical Test



SRF Cavity (a Nb/Cu clad cavity)

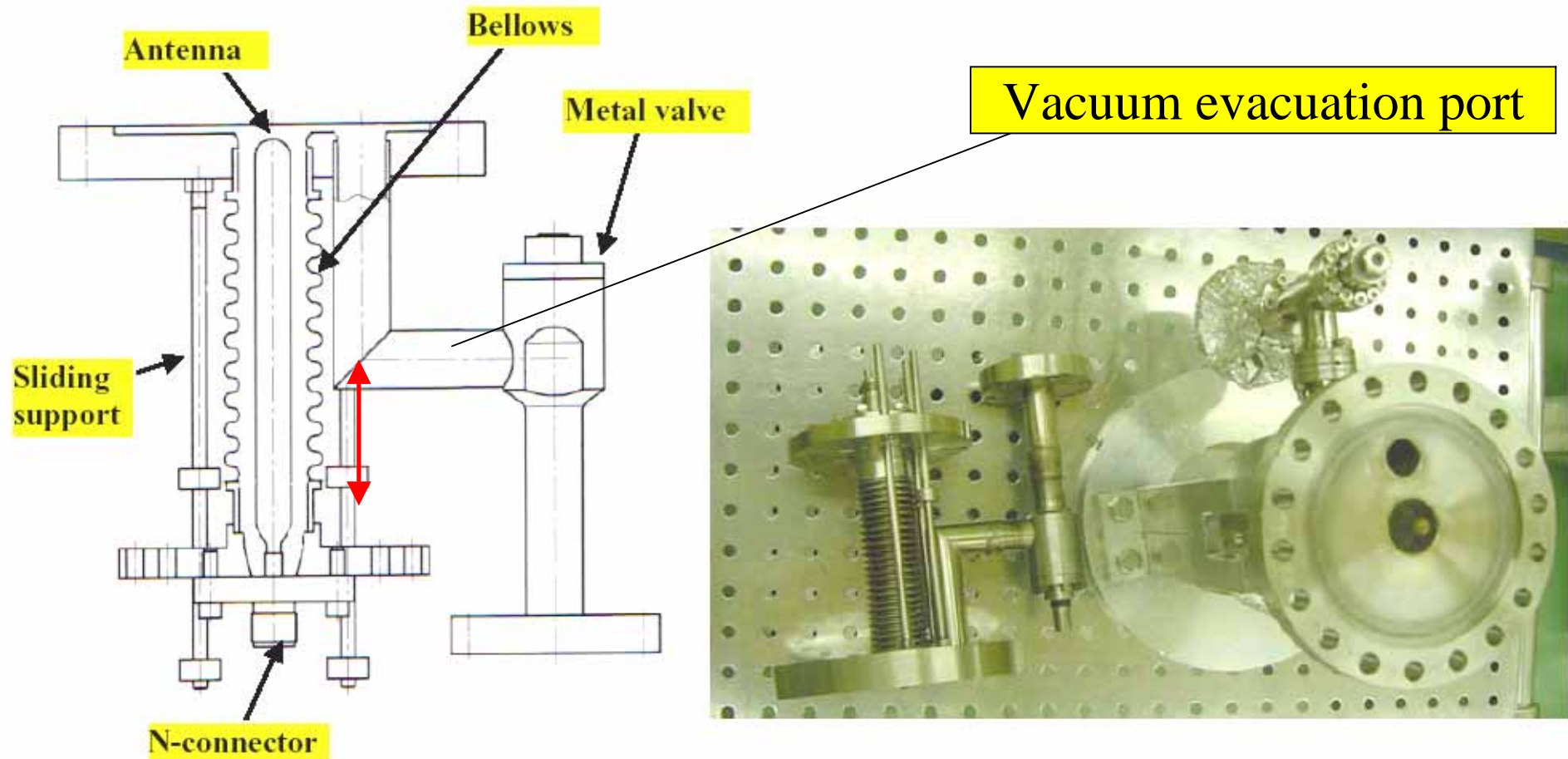


Pickup coupler

A SRF cavity hanged vacuum evacuation stand.
The cavity vacuum is pinched off by a metal valve.

**Variable
RF Input coupler**

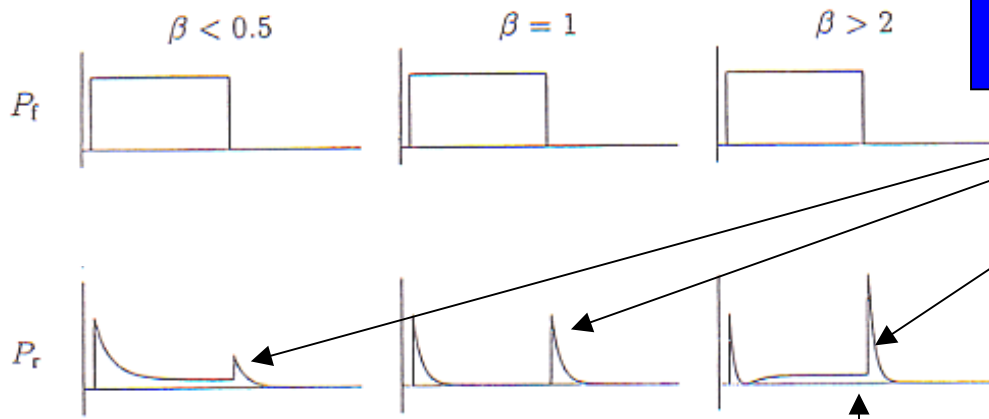
Structure of the Variable RF Input Coupler



Variable input coupler for the vertical test in KEK

9.2 Theory of RF Measurement of SRF Cavities

Pulse method



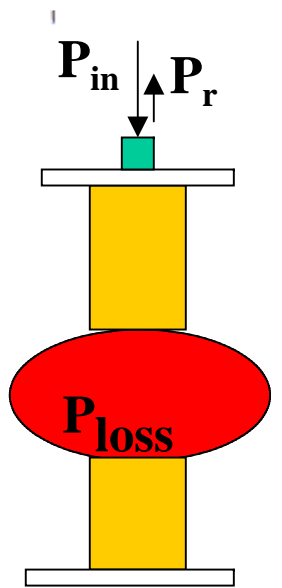
$$P_t(t) = P_o \exp\left(-\frac{\omega}{Q_L} t\right)$$

$\omega = 2\pi f$, Q_L : Loaded Q

One-port

Decatime : $\tau_{1/2}$

$$P_t(\tau_{1/2}) = \frac{1}{2} P_o = P_o \exp\left(-\frac{\omega}{Q_L} \cdot \tau_{1/2}\right)$$



$$Q_L = 2\pi f \cdot \frac{\tau_{1/2}}{\ln(2)}$$

$$\ln(2) = \frac{2\pi f}{Q_L} \tau_{1/2}$$

One-Port Cavity

$$Q_0 \equiv \frac{\omega U}{P_{\text{loss}}},$$

$$Q_L \equiv \frac{\omega U}{P_{\text{loss}} + P_e} = \frac{\omega U}{P_{\text{loss}} \left(1 + \frac{P_e}{P_{\text{loss}}}\right)} \quad (\text{for one port})$$

$$= \frac{Q_0}{(1 + \beta_{in})}$$

$$Q_0 = (1 + \beta_{in}) \cdot Q_L$$

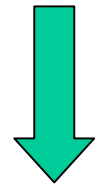
Equivalent Circuit model

Judgment from Pr

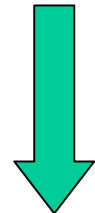
$$\beta_{in} \equiv \frac{P_e}{P_{\text{loss}}} = \frac{1 \pm \sqrt{\frac{P_r}{P_{in}}}}{1 \mp \sqrt{\frac{P_r}{P_{in}}}} \quad (\text{over} > 1 / \text{under} < 1)$$

$\tau_{1/2}$
 P_{in}
 P_r

Measurement



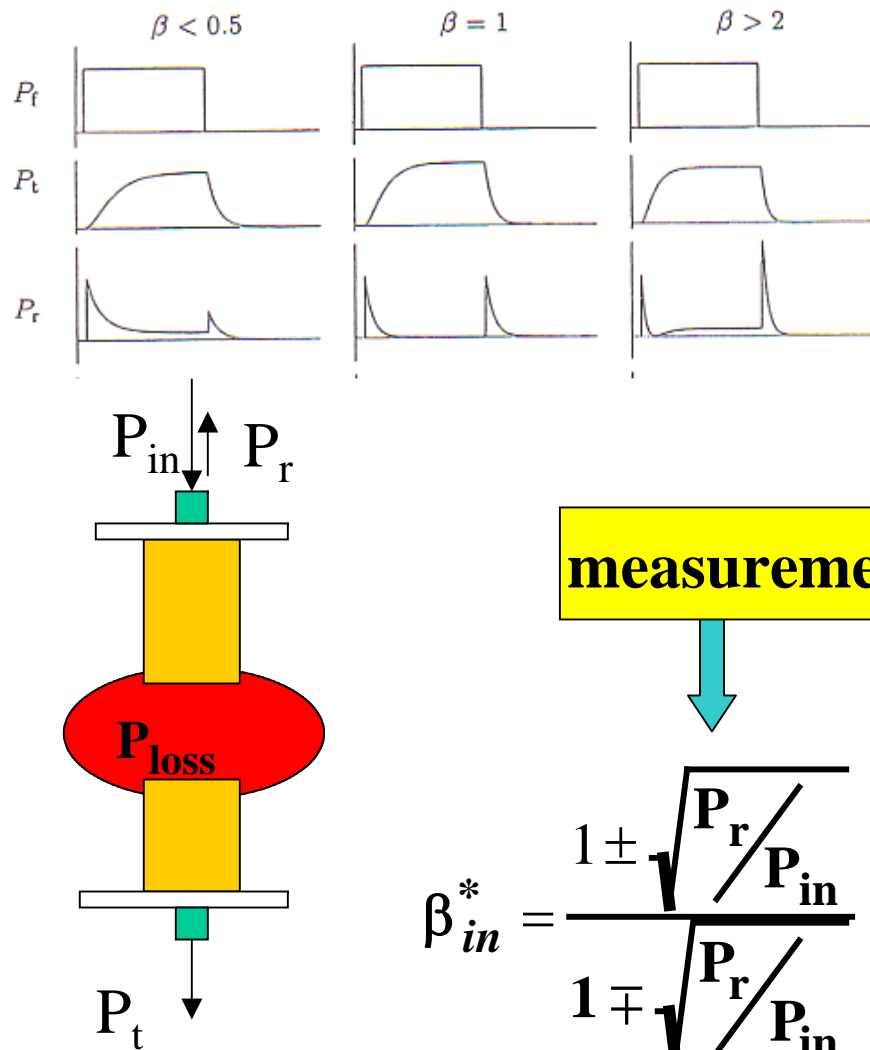
Calculation Q_L, β_{in}



Calculation Q_0

$$R_s = \frac{\Gamma}{Q_0}$$

Two-Port Cavity



$$\begin{aligned}
 P_{loss}^* &= P_{loss} + P_t \\
 Q_o^* &= \frac{\omega U}{P_{loss}^*} = \frac{\omega U}{P_{loss} + P_t} \\
 &= \frac{\omega U}{P_{loss} \left(1 + \frac{P_t}{P_{loss}} \right)} \quad \text{measurement} \\
 &= \frac{Q_o}{(1 + \beta_t)} \quad \because \beta_t \equiv \frac{P_t}{P_{loss}} \\
 &= (1 + \beta_{in}^*) Q_L
 \end{aligned}$$

(over > 1 / under < 1)

$$Q_o^* = \frac{Q_o}{(1 + \beta_t)} = (1 + \beta_{in}^*) \cdot Q_L$$

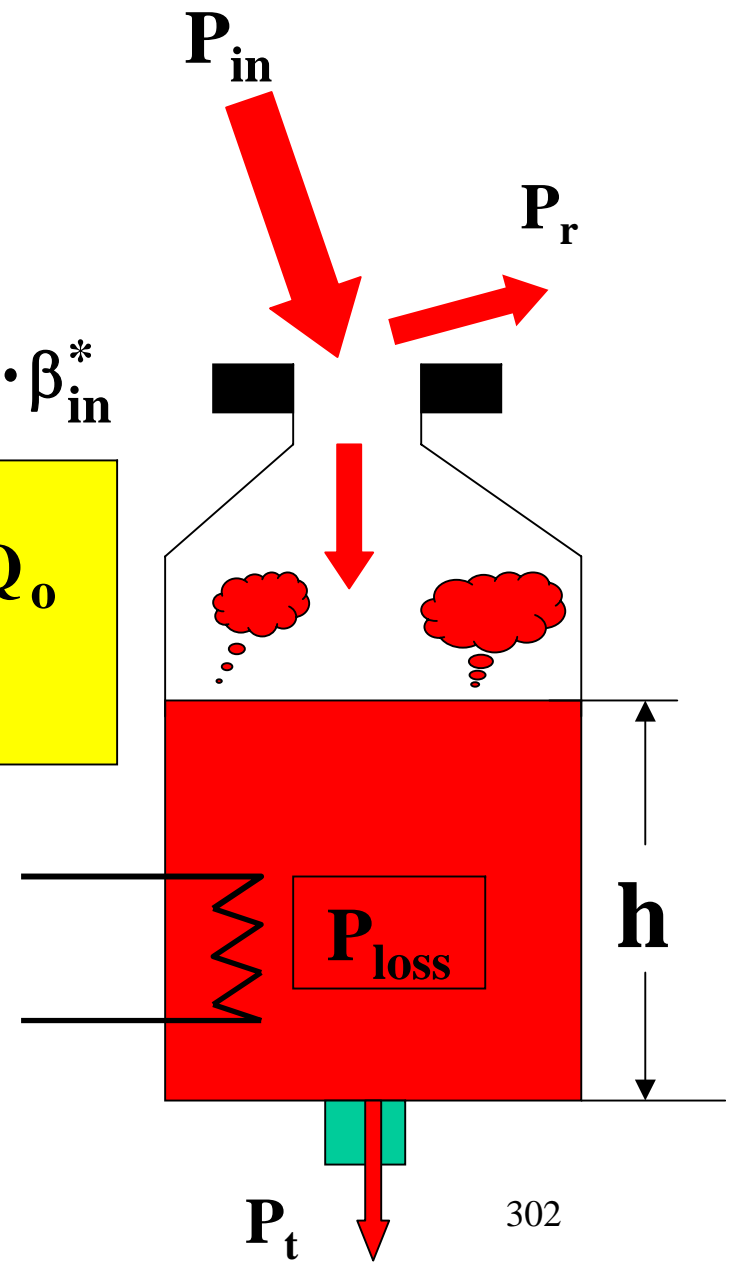
$$\begin{aligned} Q_o &= (1 + \beta_{in}^*) \cdot (1 + \beta_t) \cdot Q_L \\ &= \left[1 + (1 + \beta_t) \cdot \beta_{in}^* + \beta_t \right] \cdot Q_L \\ &= (1 + \beta_{in} + \beta_t) \cdot Q_L \quad \because \beta_{in} \equiv (1 + \beta_t) \cdot \beta_{in}^* \end{aligned}$$

$$Q_o \equiv \frac{\omega U}{P_{loss}}, \quad Q_t \equiv \frac{\omega U}{P_t} = \frac{\omega U / P_{loss}}{P_t / P_{loss}} = \beta_t \cdot Q_o$$

$$\omega U = Q_o \cdot P_{loss} = Q_t \cdot P_t$$

$$P_{loss} = P_{in} - P_r - P_t$$

Stationary state : $h = \text{const} \leftarrow U \text{ const}$



Calculation of Gradient

$$R_{sh} = \frac{V^2}{P_{loss}} \quad \because V = E_{acc} \cdot d_{eff}$$
$$= \frac{(E_{acc} \cdot d_{eff})^2}{P_{loss}}$$

Exercise VIII.

$$E_{acc} = \frac{1}{d_{eff}} \cdot \sqrt{R_{sh} \cdot P_{loss}} = \frac{\sqrt{R_{sh} / Q_0}}{d_{eff}} \cdot \sqrt{Q_0 \cdot P_{loss}} = Z \cdot \sqrt{Q_0 \cdot P_{loss}}$$
$$= Z \cdot \sqrt{Q_t \cdot P_t}$$

$$\because Q_0 \cdot P_{loss} = Q_t \cdot P_t$$

Once measured the Q_{t^2} you can calculate E_{acc} directly from P_t and Q_t .
 Q_0 is also directly calculated from them.

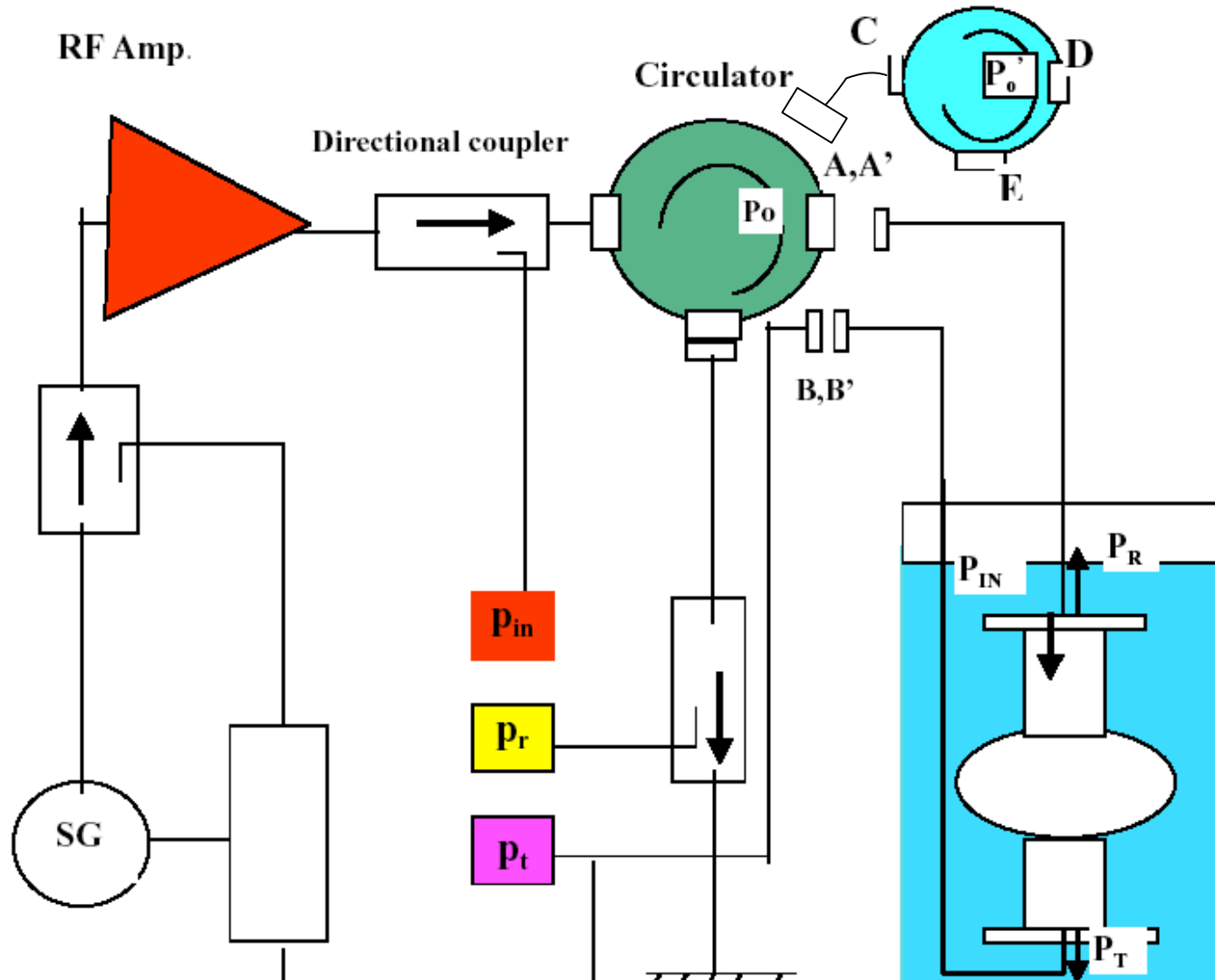
You don't need to measure the decay time for every gradient.

Cable Correction

Exercise VII.

P_{in}, P_r, P_t : measured in the measurement room

P_{IN}, P_R, P_T : Power at the cavity (cooled), $P_{IN} = c_{in} \cdot p_{in}$, $P_R = c_r \cdot p_r$, $P_T = c_t \cdot p_t$

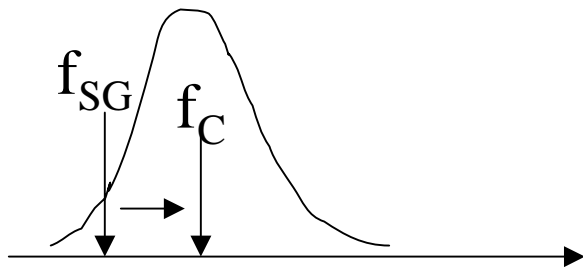
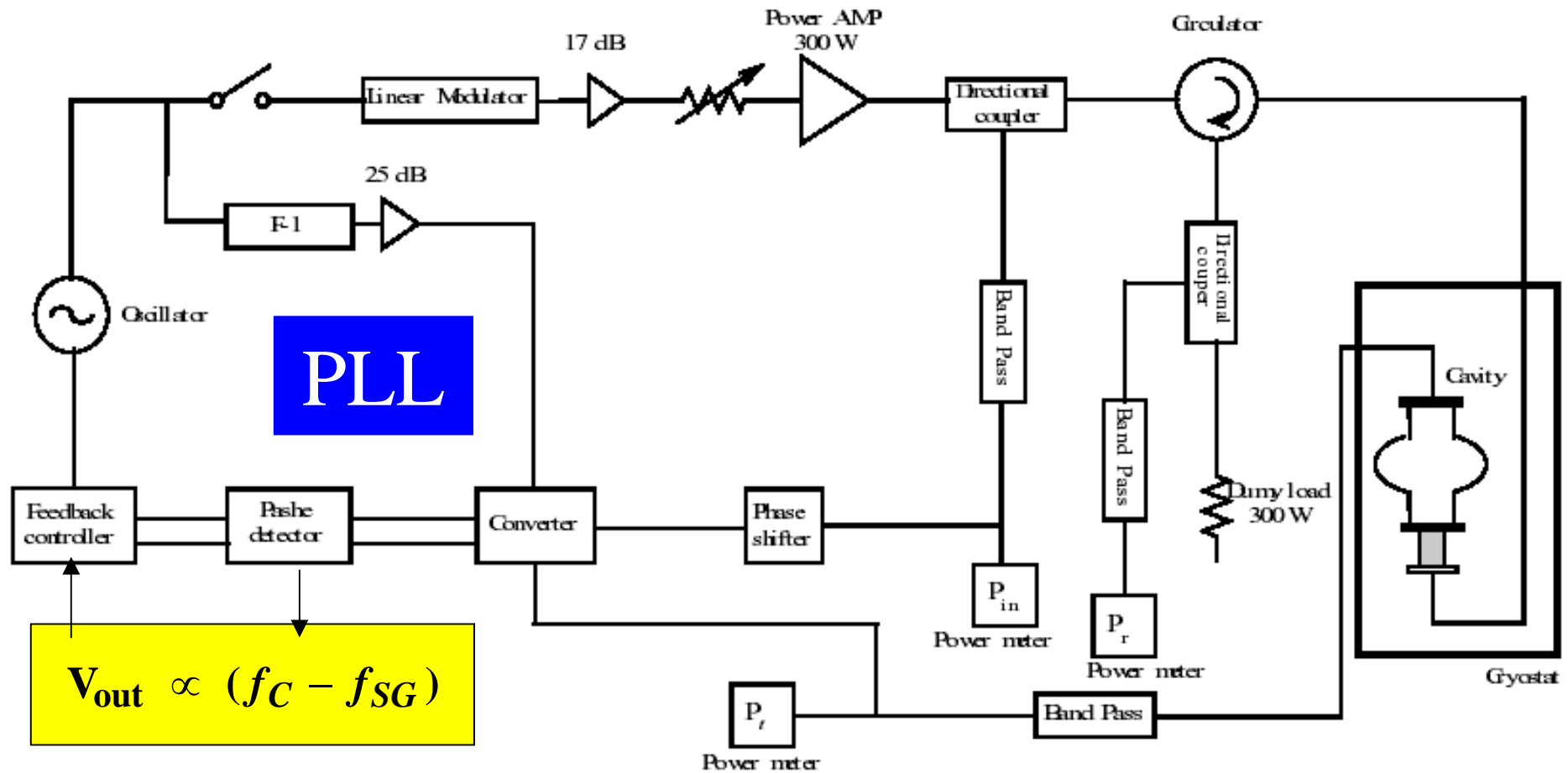


P_{in} , P_O at A,
 p_r : short A
 p_t : connect B to A
 P_O/p_{in} , P_O/p_r , P_O/p_t

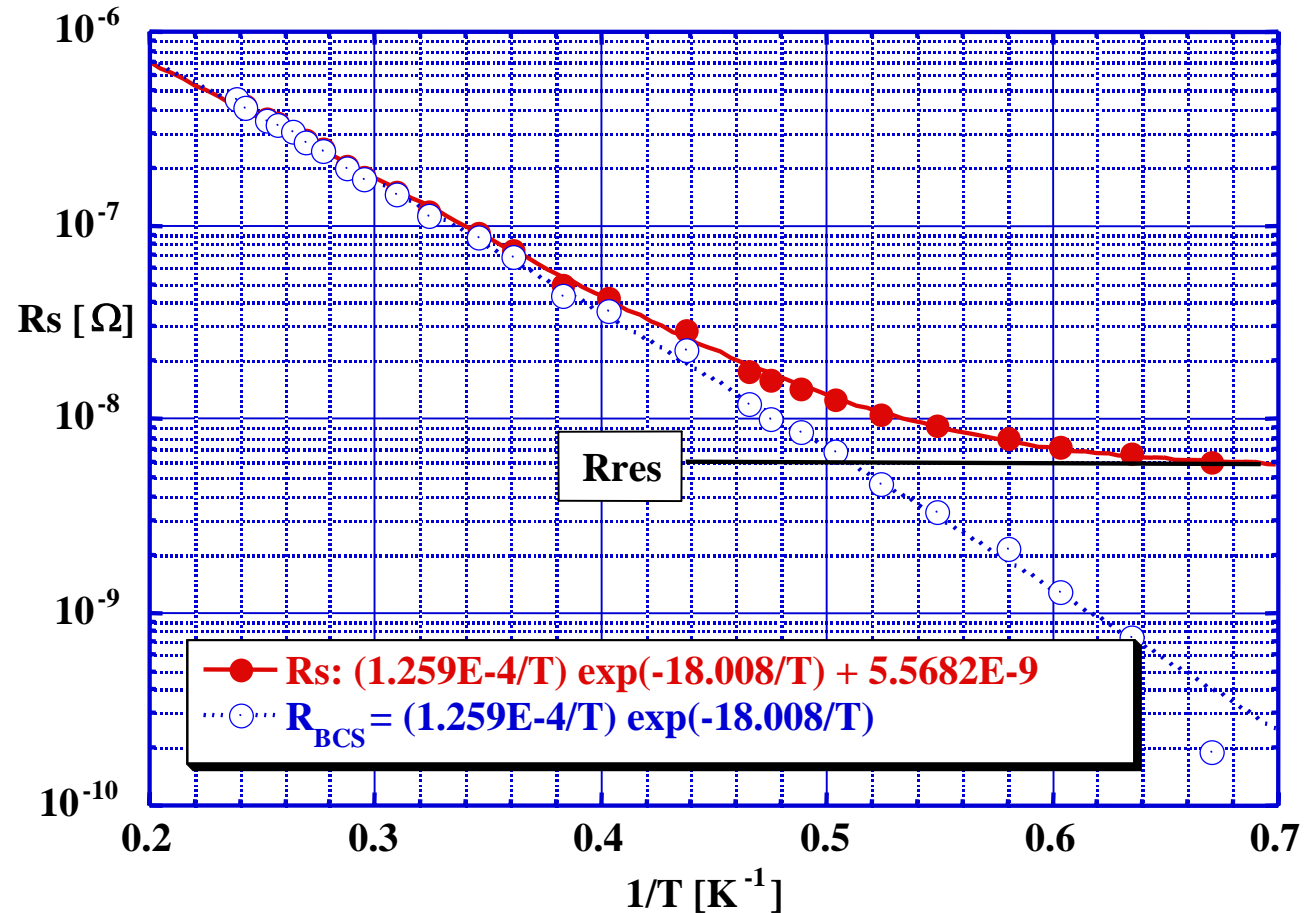
 $P_{O'}$ at E : connect A and C,
 and short D
 $P_{in'}$ at E : connect D to A'
 p_t' at E : connect D to B'
 $C_{in} = (P_O/p_{in}) \cdot (P_{in'}/P_{O'})^{1/2}$
 $C_r = (P_O/p_r) \cdot (P_{O'}/P_{in'})^{1/2}$
 $C_t = (P_O/p_t) \cdot (P_{O'}/p_t')^{1/2}$

 $P_{IN} = c_{in} \cdot P_{in}$
 $P_R = c_r \cdot P_r$
 $P_T = c_t \cdot P_t$

9.3 RF Measurement System



Measurement of Surface Resistance



$$R_s \text{ - fit : } R_s(T) = \frac{A}{T} \cdot \exp\left(-\frac{B}{T}\right) + R_{res}$$

$$B = \frac{\Delta}{k_B}$$

High Gradient Measurement Q₀-E_{acc} curve

