

Results from 9mA studies on achieving flat gradients with beam loading

P_K / Q_L studies at FLASH
during the Feb. 2011 test in DESY

OVERVIEW

- Problem statement and historical background
 - Why do we care about individual flat gradients?
 - What solutions were offered to achieve flat gradients with beam loading?
 - What can we actually implement at FLASH?
- The Feb.'11 study at FLASH
 - What approach have we followed during the FLASH test studies?
 - Results of the P_K / Q_L studies
- Conclusions and lessons learnt
 - Study insights
 - Approach limitations
 - Improvements

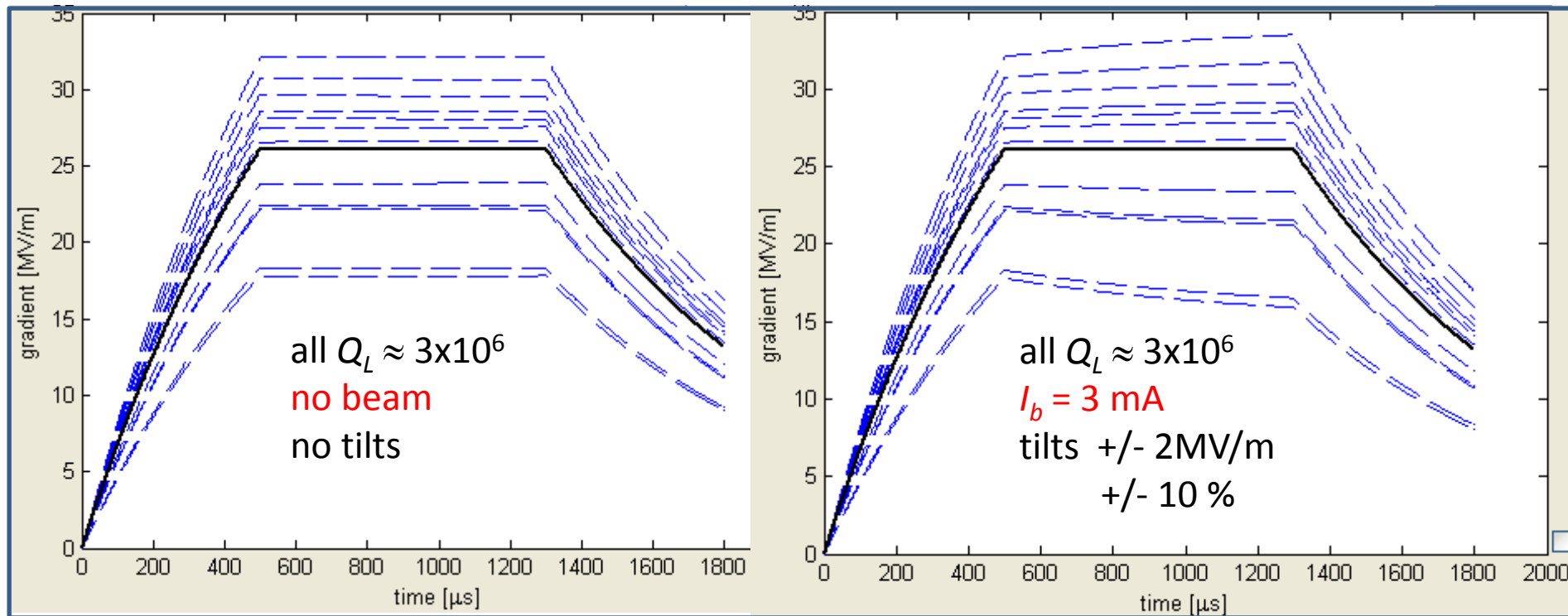
Introduction: problem statement

Why do we care about individual flat gradients?

“Effect of Cavity Tilt and RF Fluctuations to Transverse Beam Orbit Change in ILC Main Linac”

K. Kubo, Jan. 2010

FLASH ACC6 & ACC7

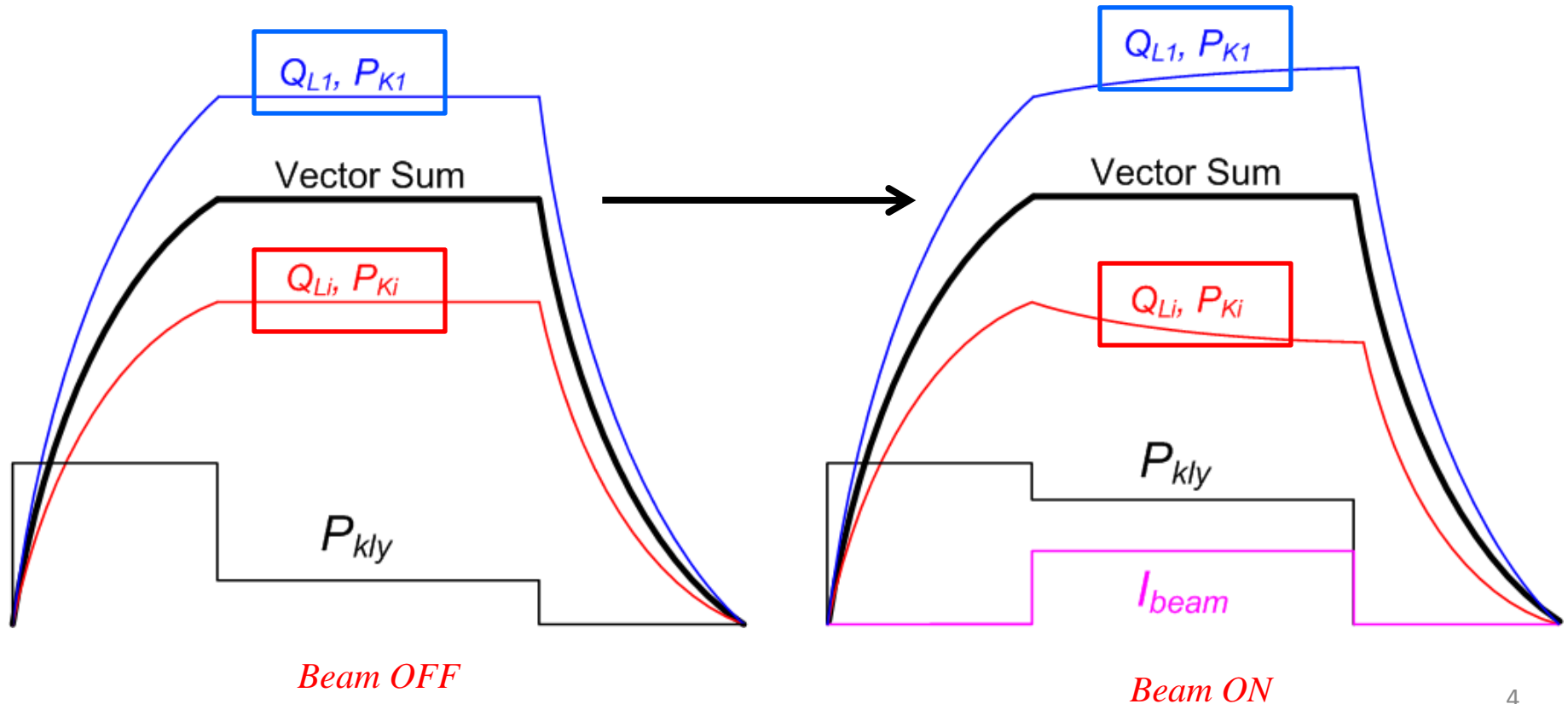


Introduction: problem statement

FNAL approach to cavity quench due to beam ON/OFF operations

“Optimal Coupler and Power Settings for Superconductive Linear Accelerators”, J. Branlard, B. Chase, Linac 2008

- produces fixed P_{Kl}/Q_L settings (unique to each cavity) which is safe for all beam loadings (i.e. no tuning action required to prevent quench)
- individual cavities gradients have tilts with beam



Introduction: problem statement

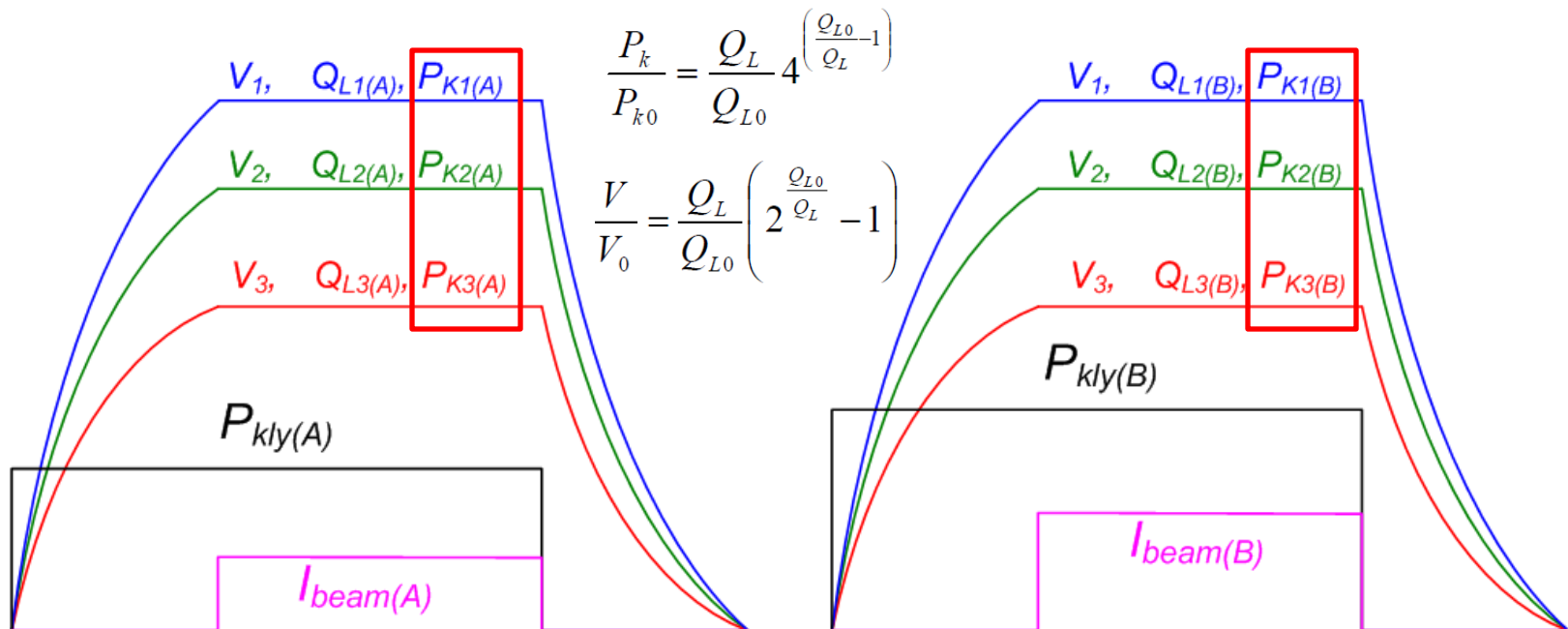
Published “solutions” to flat cavity gradient with beam

“RF Distribution Optimization in the Main Linacs of the ILC”

Bane, Adolphsen, Nantista - WEPMS037.pdf, 2007

→ Assumes a square forward power pulse

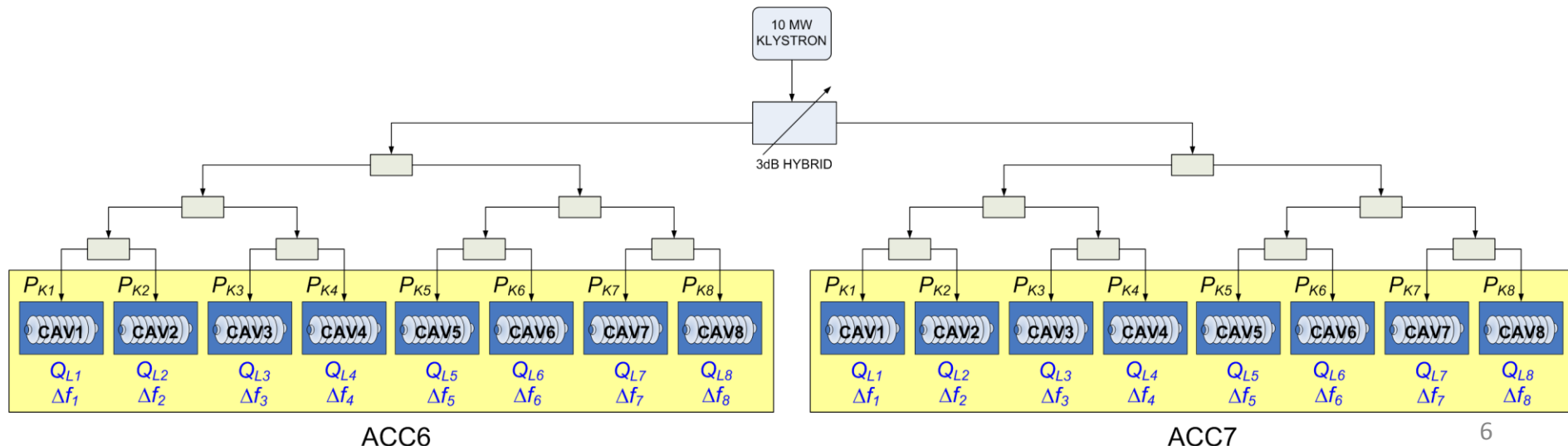
→ Assumes adjustable P_K 's



Introduction: problem statement

Problem space at FLASH

- Focus on ACC6 and ACC7
- Motorized couplers (Q_L adjustments, limited range)
- Fixed power distribution (i.e. P_K), except for 3dB hybrid
- Motorized static tuners
- Dynamic cavity resonance control with piezo



Introduction: problem statement

Published “solutions” to flat cavity gradient with beam

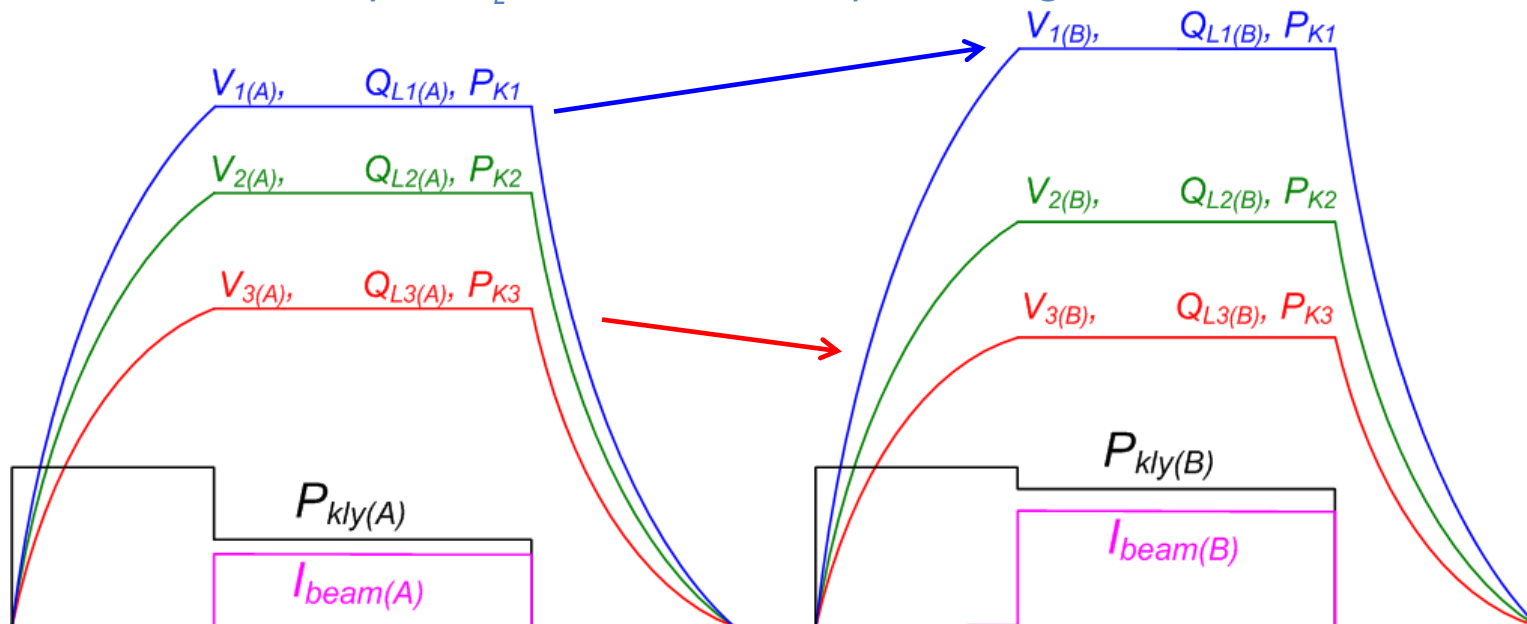
“PkQI-like control for ACC6/7 at FLASH” PkQI_FLASHver3.docx

Shin Michizono, Sept. 2010

“To flatten the cavity gradient for ACC6/7” FLASH101022BV2.pdf

Shin Michizono, Nov. 2010

- solves the same problem but using existing P_K distribution
- no PK adjustments for different beam loading, only Q_L changes
- version1: assumes a square forward power pulse
yield very low Q_L values
- version2: assumes a fill time / flat top power step
yield Q_L values within acceptable range



Introduction: problem statement

Published “solutions” to flat cavity gradient with beam

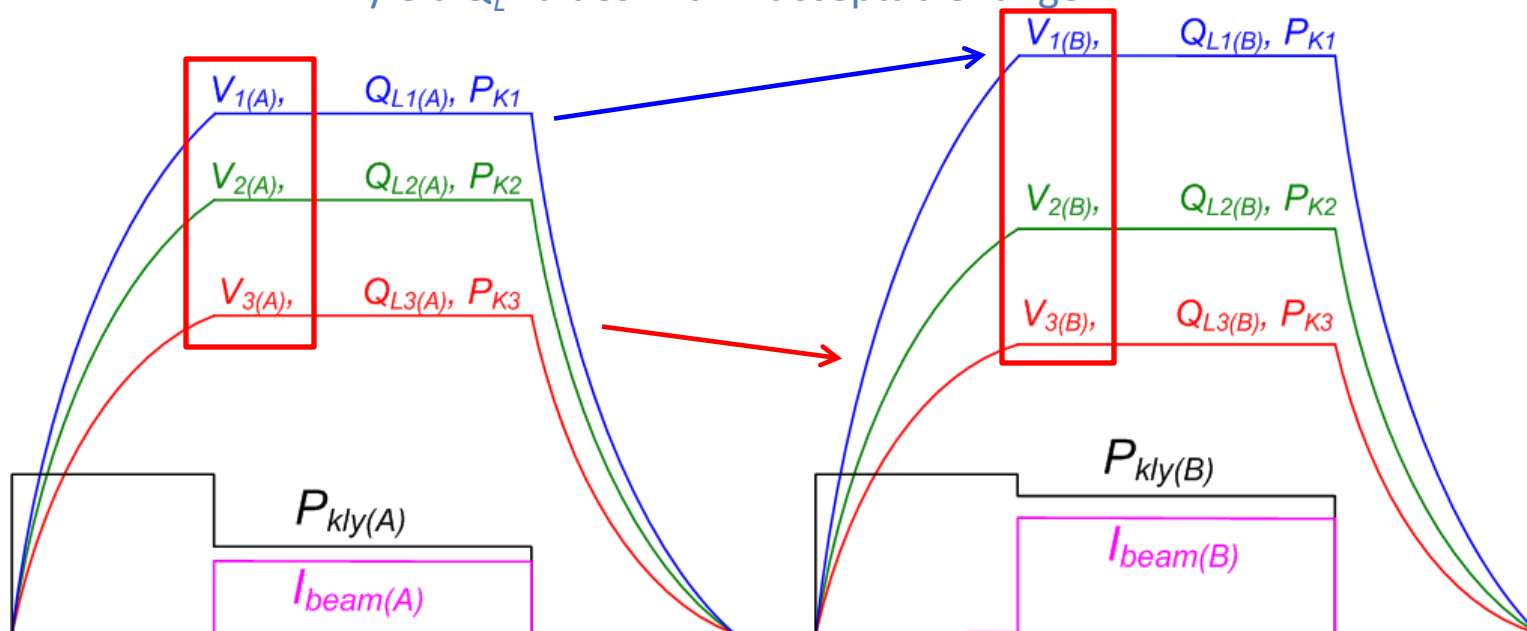
“PkQI-like control for ACC6/7 at FLASH” PkQI_FLASHver3.docx

Shin Michizono, Sept. 2010

“To flatten the cavity gradient for ACC6/7” FLASH101022BV2.pdf

Shin Michizono, Nov. 2010

- solves the same problem but using existing P_K distribution
- no PK adjustments for different beam loading, only Q_L changes
- version1: assumes a square forward power pulse
yield very low Q_L values
- version2: assumes a fill time / flat top power step
yield Q_L values within acceptable range



FLASH studies: 5 shift overview

- **Friday 2/4 night shift:** **no beam, low gradient**
 - no beam
 - ACC6/7 vector sum calibration 100 bunches, 1 MHz, 1.6 nC
 - QL tuners characterization for ACC6/7
 - simulator calibration to reflect ACC6/7 power distribution
- **Saturday 2/5 night shift:** **1 mA , low gradient**
 - 1mA beam, low gradient (100 MeV – 200 MeV)
 - Successfully implemented QL adjustments to flatten cavity gradients
 - beam loading tilts correction (all tilts below 1%) using simulator predicted values
 - Simulated values are reliable
- **Sunday 2/6 night shift:** **1.6 mA , mid-gradient**
 - 1.6mA beam, low gradient (200 MeV)
 - low gradient, beam loading tilts Q_L correction (below 1%)
 - beam current scan
 - QL scan
- **Monday 2/7 night shift:** **3.0 mA - 4.5 mA, mid and high gradient**
 - 3.0mA beam, 200 MeV
 - QL adjusted for gradient flat at 3mA
 - beam scan from 0.9 to 4.5 mA
 - 4.5mA beam, 300 MeV
 - QL adjusted for gradient flat at 4.5 mA
 - beam current scan
- **Tuesday 2/8 afternoon shift:** **4.2 mA, highest gradient**
 - 4.2mA beam, 360 MeV
 - Lorentz force detuning compensation
 - Use calculator to predict QL → gives very accurate prediction
 - Flatten ACC6/7 gradients tilts to ~ 1.5%
 - beam current scan

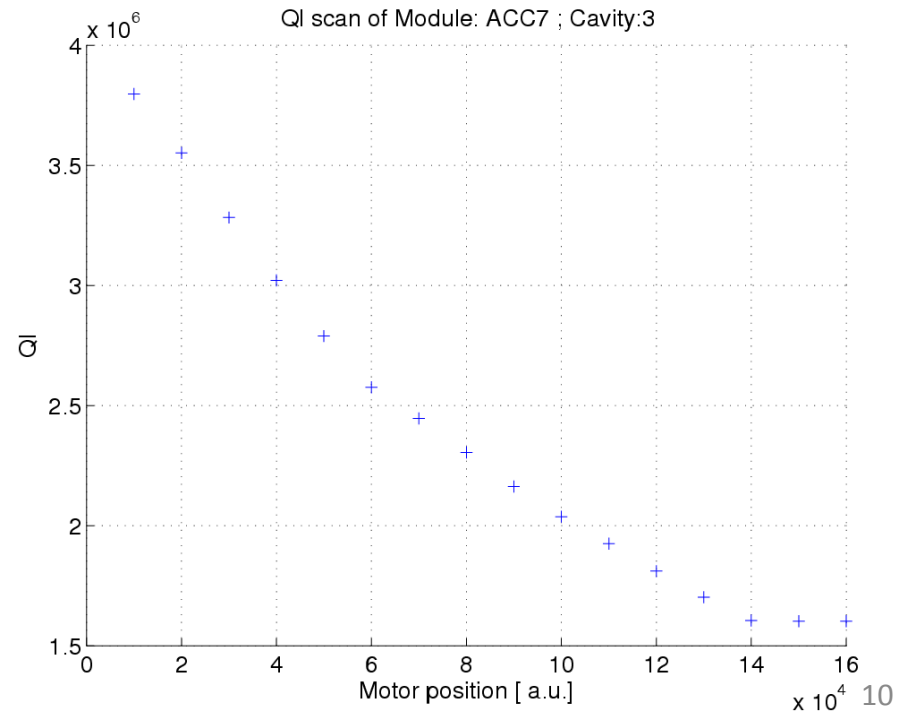
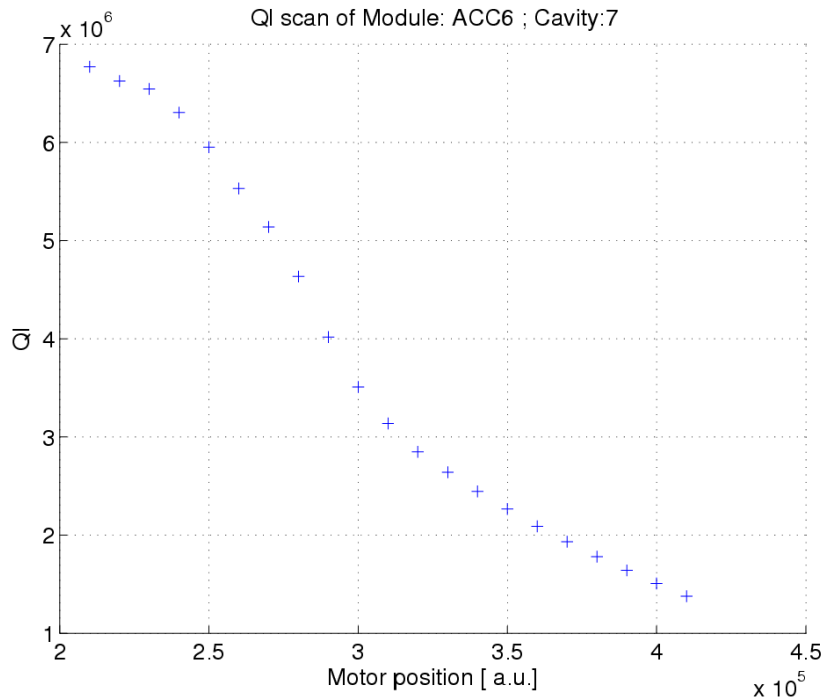
ACC6 & ACC7

Q_L settings limits

ACC6	cav1	cav2	cav3	cav4	cav5	cav6	cav7	cav8
Q_L min [$\times 10^6$]	1.2	1	1.2	1	1.5	1.5	1.5	1
Q_L max [$\times 10^6$]	7	5	7.5	5.5	8.5	7.5	6.5	4

ACC7	cav1	cav2	cav3	cav4	cav5	cav6	cav7	cav8
Q_L min [$\times 10^6$]	1.1	1.8	1.6	1.3	1.1	1.4	1.7	2.1
Q_L max [$\times 10^6$]	3.4	3.8	3.7	3.6	3.3	3.3	3.3	4.6

not "hard" limits



Beam: Ibo = 4.50 mA, Compensation 100.0 %

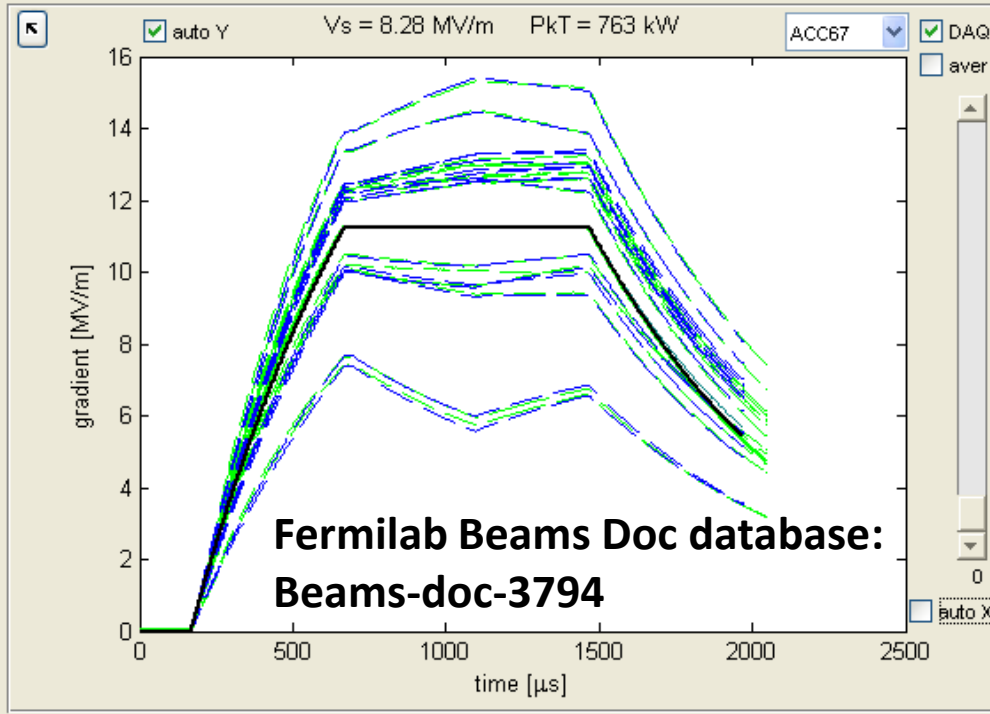
Generator: PkT = 763 kW, ratio ampl = 0.50, ratio phase = 0 deg

HLRF: ACC6 3dB hybrid ACC7, -2.7 dB 405 kW, -3.3 dB 358 kW, Waveguide losses (>0), ACC6 0 dB, ACC7 0 dB, Pmax 0 kW/cav

Timing: delay 168 usec, fill time 500 usec, flat top 800 usec, sample time 500 usec, decay start 1480 usec, decay stop 1580 usec

FeedBack: SP 11.25 MV/m, SP 0 deg, Kp 100, Ki 0, delay 0, ON

Lorentz Forces: mode fm Qm Km, 1 280 100 0.4, 2 340 100 0.3, 3 420 100 0.2, Hz Hz/(MV/m)², OFF



Cryomodules: Cryomodule: ACC6

	V lim [MV/m]	QL [x1e6]	Pk [dB]	Det [Hz]	Offset [deg]	Plot Power
1	34.0	3.09 3.09	8.38	-110 -110	0.00	55 kW
2	32.0	3.10 3.10	8.32	13 13	0.00	56 kW
3	34.0	2.97 2.97	8.47	122 122	0.00	54 kW
4	32.0	3.11 3.11	8.65	29 29	0.00	52 kW
5	21.0	3.11 3.11	12.55	1 1	0.00	21 kW
6	21.0	3.31 3.31	12.75	28 28	0.00	20 kW
7	29.0	3.12 3.12	10.05	86 86	0.00	37 kW
8	26.0	3.40 3.40	10.05	65 65	0.00	37 kW

RUN Amplitude

load DAQ 07Feb_2237-ACC67-4.5m/

load *.txt

save 07Feb_2237-ACC67-4.5m/

Snapshot

ACC6 : 7.74 MV/m	cav1	cav2	cav3	cav4	cav5	cav6	cav7	cav8
Eacc [MV/m]	9.10	9.16	9.09	8.81	5.63	5.39	7.48	7.28
margin [MV/m]	20.89	18.68	21.39	19.36	13.33	13.61	18.84	15.87
SIM tilt [%]	5.53	6.17	2.94	4.36	-24.42	-27.67	-5.03	-4.31
DAQ tilt [%]	5.17	5.57	2.83	4.12	-24.58	-25.33	-1.34	-4.04
ACC7 : 8.87 MV/m	cav1	cav2	cav3	cav4	cav5	cav6	cav7	cav8
Eacc [MV/m]	8.82	8.97	8.84	9.12	10.21	9.88	7.67	7.42
margin [MV/m]	16.39	18.08	21.07	16.60	19.59	24.55	16.50	15.96
SIM tilt [%]	4.28	5.13	5.30	6.47	10.01	7.30	-2.82	-7.34
DAQ tilt [%]	4.17	4.25	4.87	4.34	9.54	8.10	-2.94	-7.07

Tilt sample times:

SIM DAQ

start: 700 700 us

stop: 1100 1100 us



Beam: Ibo = 4.50 mA, Compensation 100.0 %

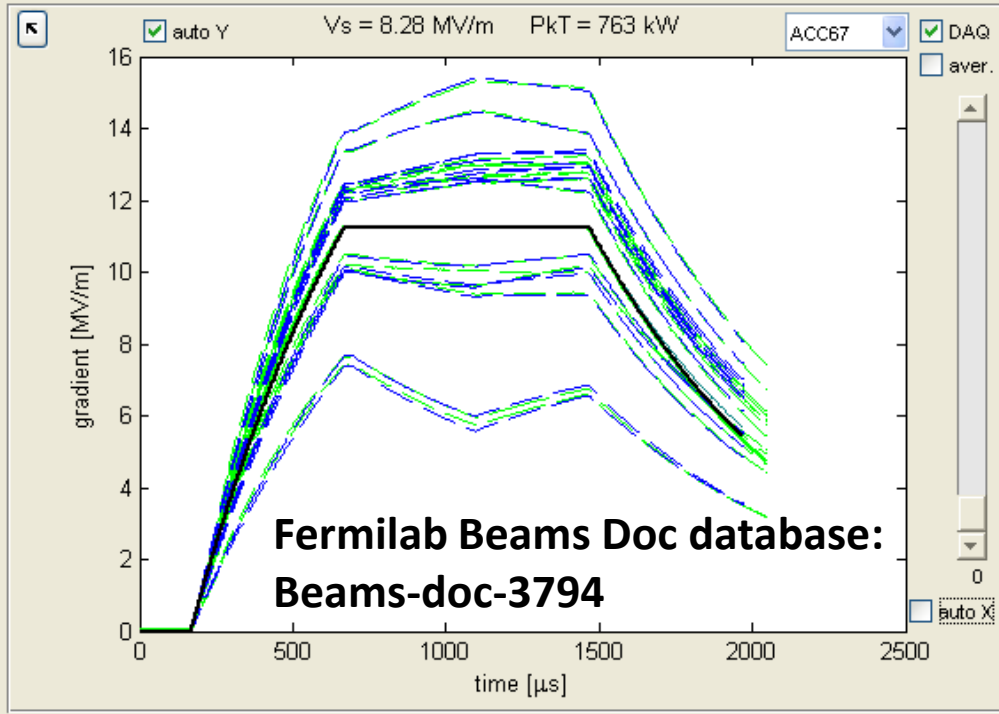
Generator: PkT = 763 kW, ratio ampl = 0.50, ratio phase = 0 deg

HLRF: ACC6 3dB hybrid 405 kW, ACC7 -3.3 dB 358 kW, Waveguide losses (>0)

Timing: delay: 168 usec, fill time: 500 usec, flat top: 800 usec, sample time: 500 usec, decay start: 1480 usec, decay stop: 1580 usec

FeedBack: SP 11.25 MV/m, SP 0 deg, Kp 100, Ki 0, delay 0

Lorentz Forces: mode fm Qm Km, 1 280 100 0.4, 2 340 100 0.3, 3 420 100 0.2



Cryomodules: Cryomodule: ACC6

	V lim [MV/m]	QL [x1e6]	Pk [dB]	Det [Hz]	Offset [deg]	Plot Power
1	34.0	3.09 3.09	8.38	-110 -110	0.00	55 kW
2	32.0	3.10 3.10	8.32	13 13	0.00	56 kW
3	34.0	2.97 2.97	8.47	122 122	0.00	54 kW
4	32.0	3.11 3.11	8.65	29 29	0.00	52 kW
5	21.0	3.11 3.11	12.55	1 1	0.00	21 kW
6	21.0	3.31 3.31	12.75	28 28	0.00	20 kW
7	29.0	3.12 3.12	10.05	86 86	0.00	37 kW
8	26.0	3.40 3.40	10.05	65 65	0.00	37 kW

RUN

load DAQ: 07Feb_2237-ACC67-4.5m/

load: *.txt

save: 07Feb_2237-ACC67-4.5m/

Snapshot

ACC6 : 7.74 MV/m	cav1	cav2	cav3	cav4	cav5	cav6	cav7	cav8
Eacc [MV/m]	9.10	9.16	9.09	8.81	5.63	5.39	7.48	7.28
margin [MV/m]	20.89	18.68	21.39	19.36	13.33	13.61	18.84	15.87
SIM tilt [%]	5.53	6.17	2.94	4.36	-24.42	-27.67	-5.03	-4.31
DAQ tilt [%]	5.17	5.57	2.83	4.12	-24.58	-25.33	-1.34	-4.04

ACC7 : 8.87 MV/m	cav1	cav2	cav3	cav4	cav5	cav6	cav7	cav8
Eacc [MV/m]	8.82	8.97	8.84	9.12	10.21	9.88	7.67	7.42
margin [MV/m]	16.39	18.08	21.07	16.60	19.59	24.55	16.50	15.96
SIM tilt [%]	4.28	5.13	5.30	6.47	10.01	7.30	-2.82	-7.34
DAQ tilt [%]	4.17	4.25	4.87	4.34	9.54	8.10	-2.94	-7.07

Tilt sample times:

SIM DAQ

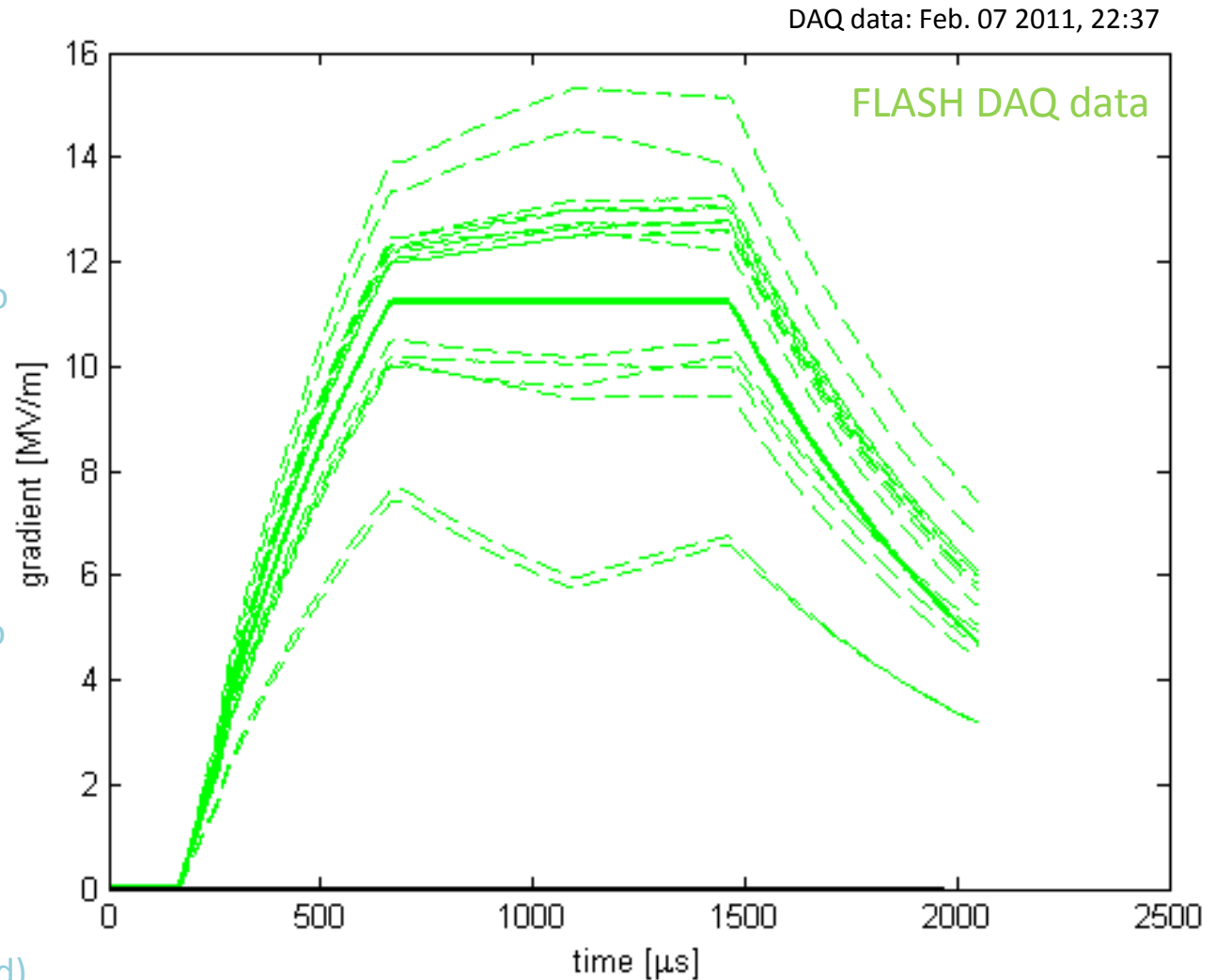
start: 700 700 us

stop: 1100 1100 us



Calibration procedure

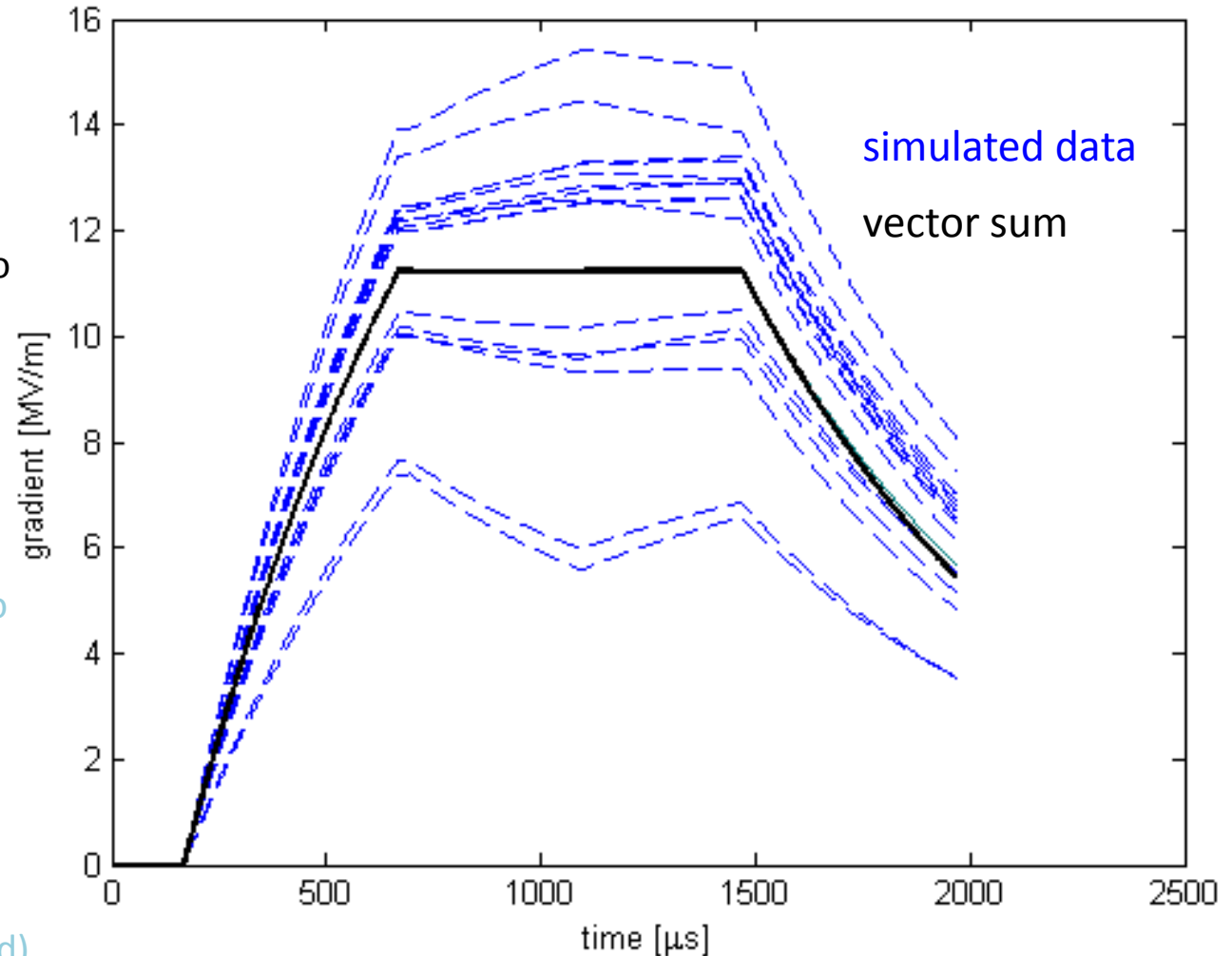
1. Load V_{cav} from DAQ
2. Compute actual Q_L , P_K and Δ_f from DAQ data
3. Type in Q_L , P_K and Δ_f into simulator
4. Check agreement between simulated and FLASH data
5. Adjust Q_L in simulator to flatten tilts
6. Implement Q_L corrections in FLASH
7. Check gradient flatness (retune cavities if needed)



$$I_b = 4.5 \text{ mA}$$

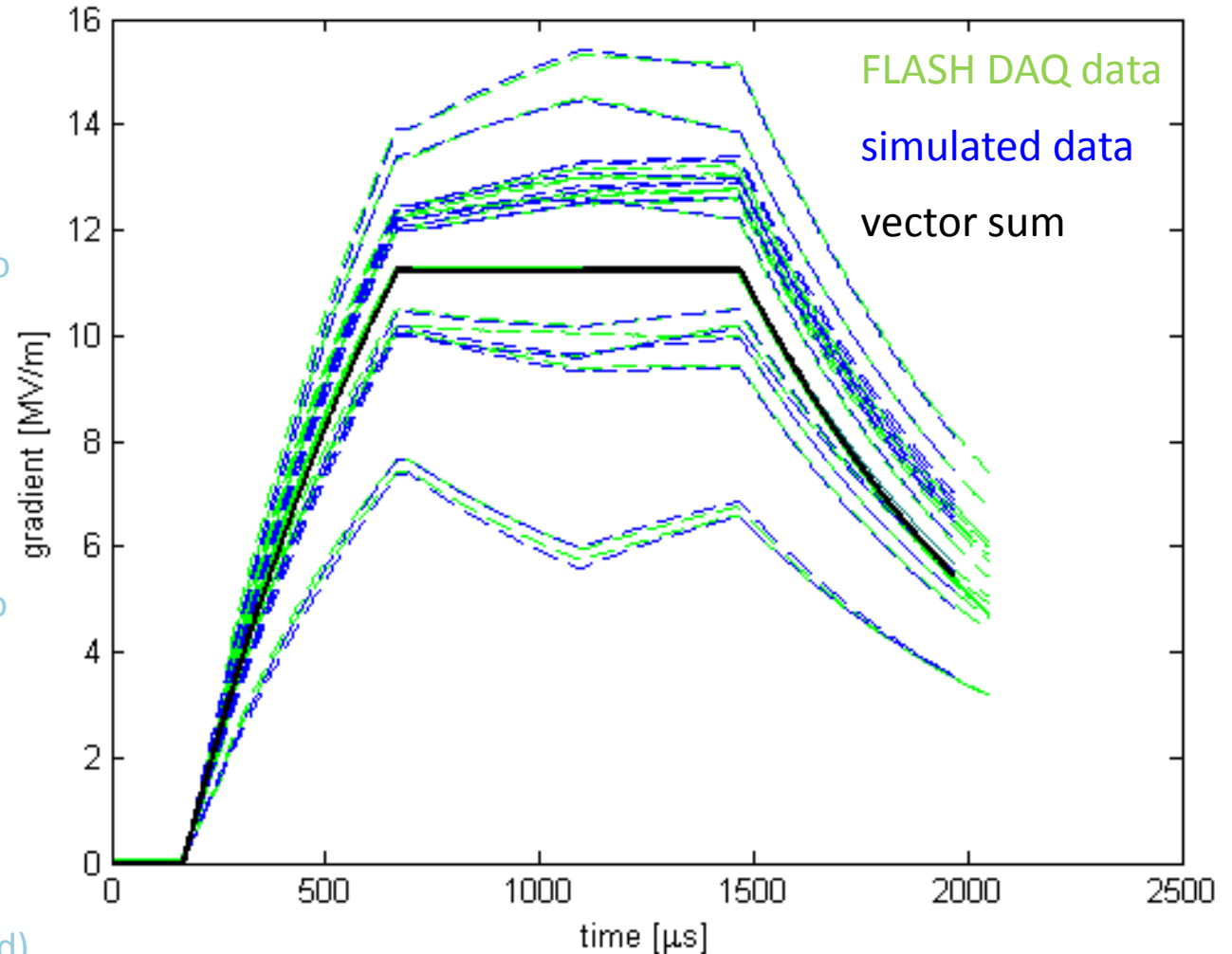
Calibration procedure

1. Load V_{cav} from DAQ
2. Compute actual Q_L , P_K and Δ_f from DAQ data
3. Type in Q_L , P_K and Δ_f into simulator
4. Check agreement between simulated and FLASH data
5. Adjust Q_L in simulator to flatten tilts
6. Implement Q_L corrections in FLASH
7. Check gradient flatness (retune cavities if needed)



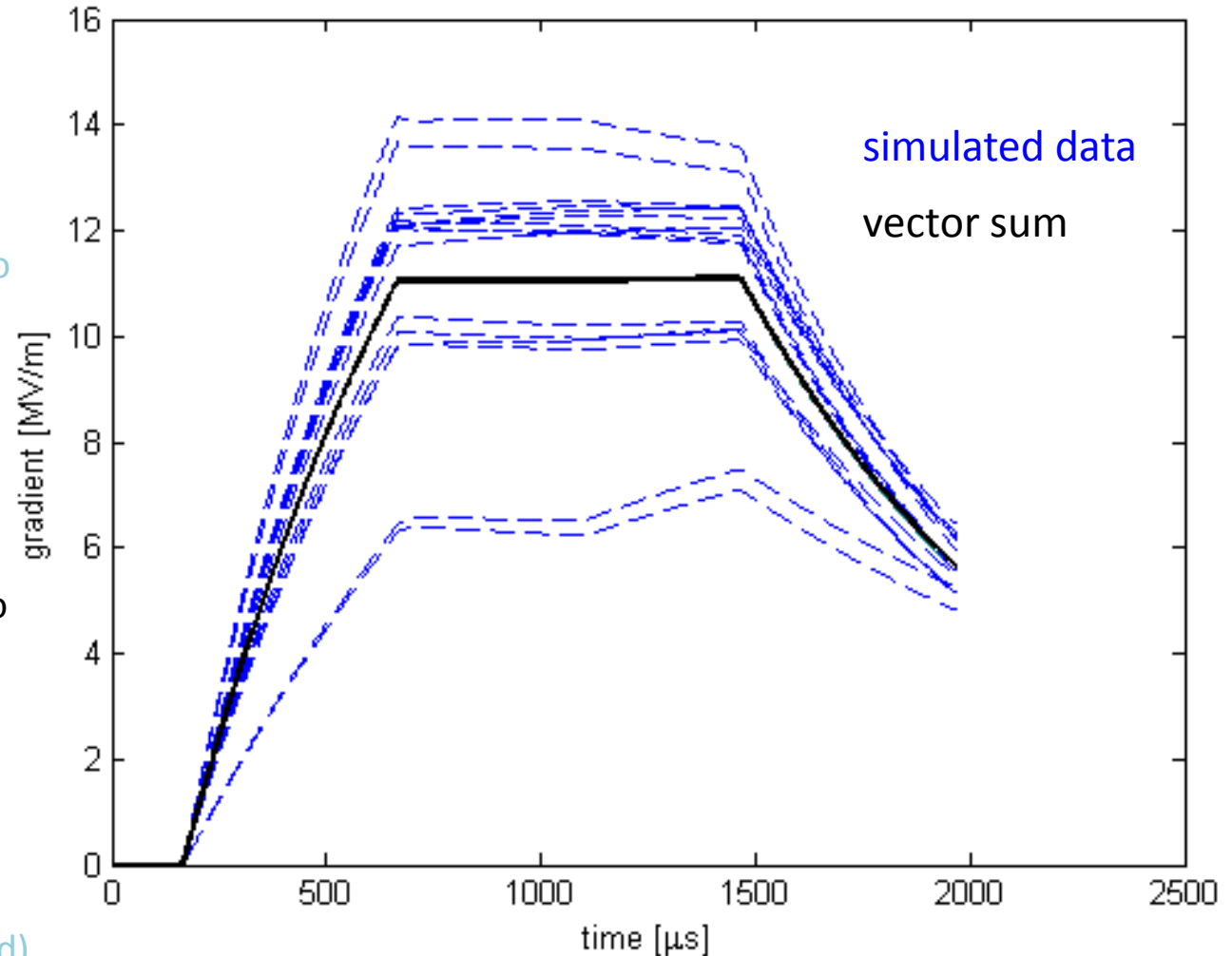
Calibration procedure

1. Load V_{cav} from DAQ
2. Compute actual Q_L , P_K and Δ_f from DAQ data
3. Type in Q_L , P_K and Δ_f into simulator
4. Check agreement between simulated and FLASH data
5. Adjust Q_L in simulator to flatten tilts
6. Implement Q_L corrections in FLASH
7. Check gradient flatness (retune cavities if needed)



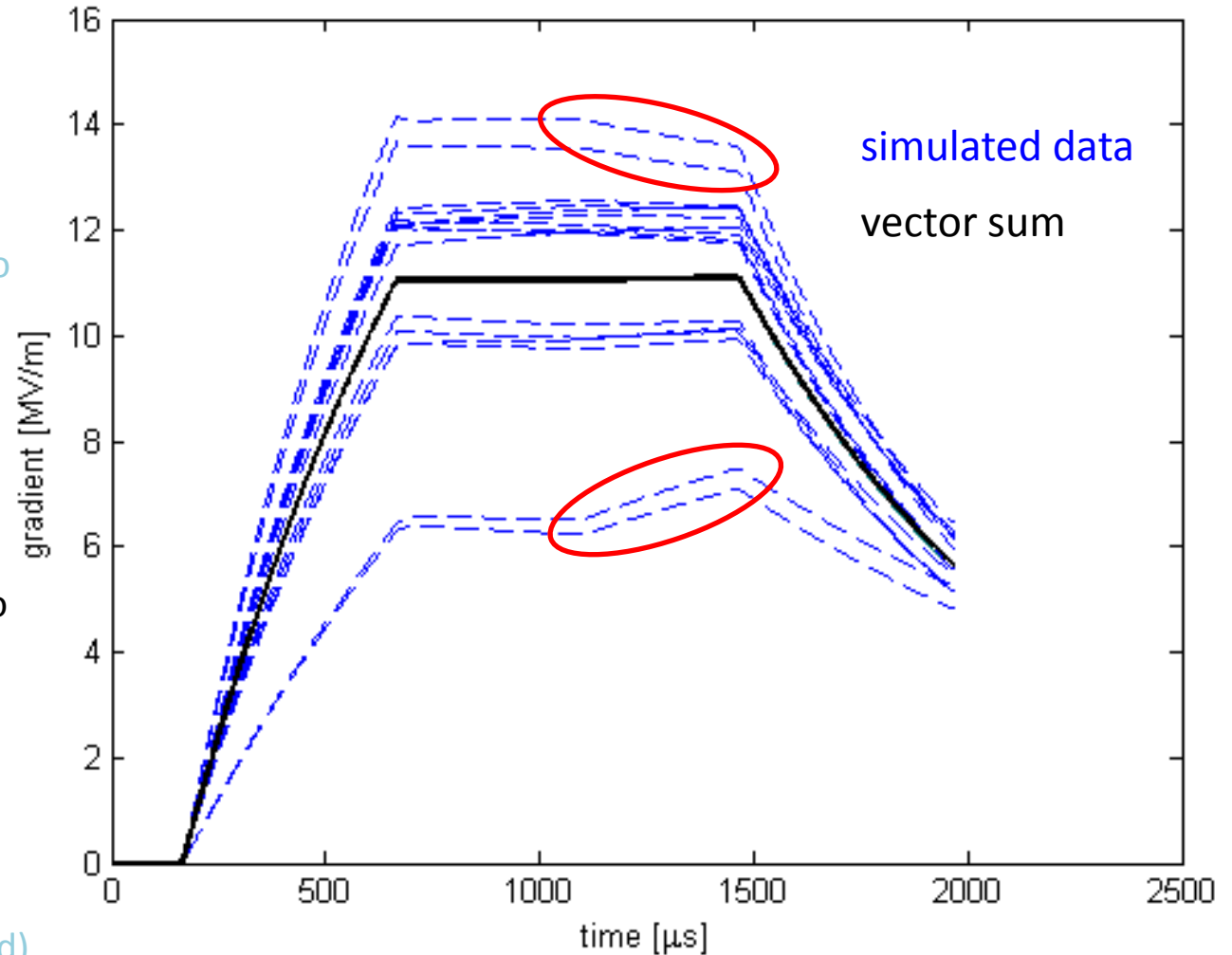
Calibration procedure

1. Load V_{cav} from DAQ
2. Compute actual Q_L , P_K and Δ_f from DAQ data
3. Type in Q_L , P_K and Δ_f into simulator
4. Check agreement between simulated and FLASH data
5. Adjust Q_L in simulator to flatten tilts
6. Implement Q_L corrections in FLASH
7. Check gradient flatness (retune cavities if needed)



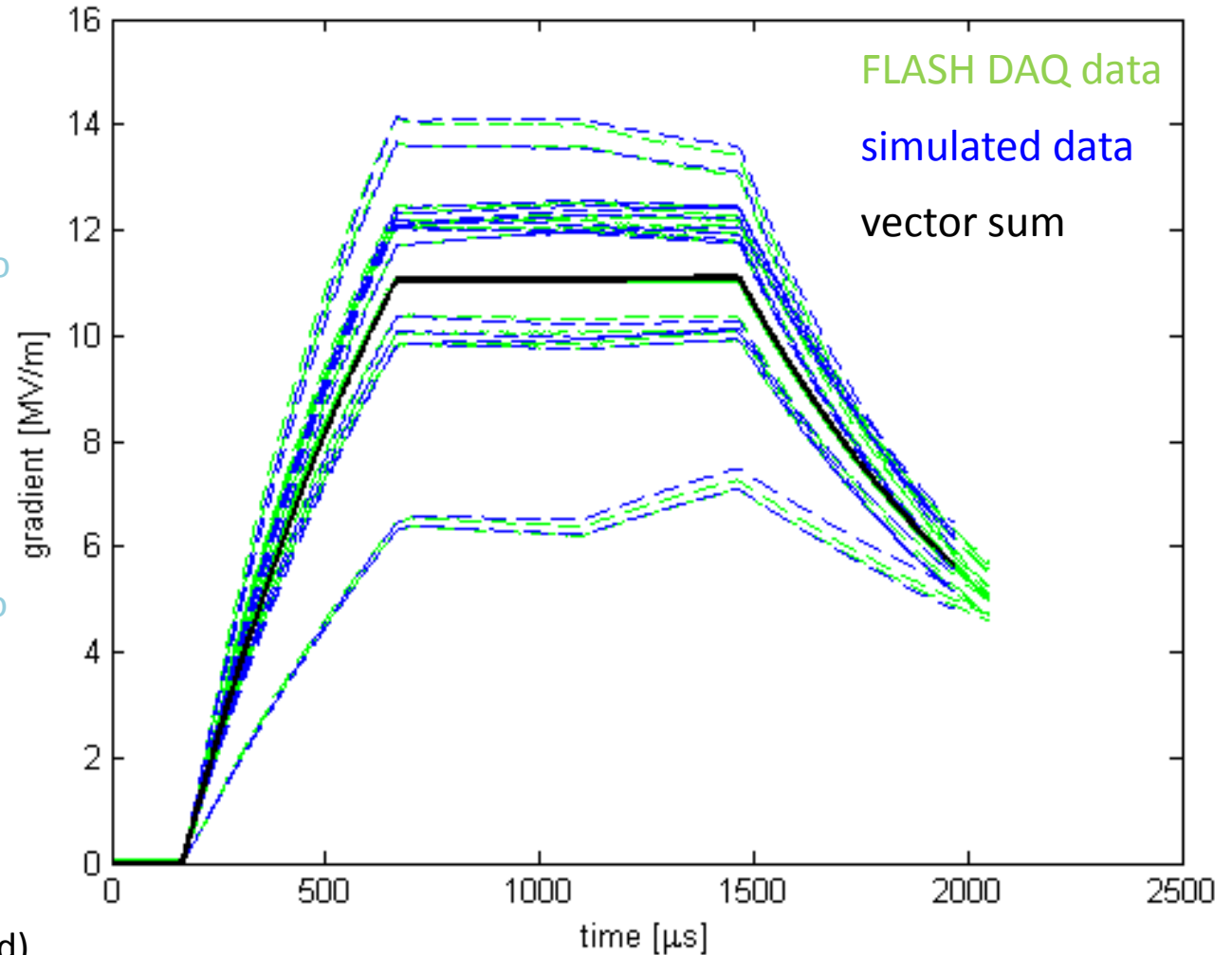
Calibration procedure

1. Load V_{cav} from DAQ
2. Compute actual Q_L , P_K and Δ_f from DAQ data
3. Type in Q_L , P_K and Δ_f into simulator
4. Check agreement between simulated and FLASH data
5. Adjust Q_L in simulator to flatten tilts
6. Implement Q_L corrections in FLASH
7. Check gradient flatness (retune cavities if needed)



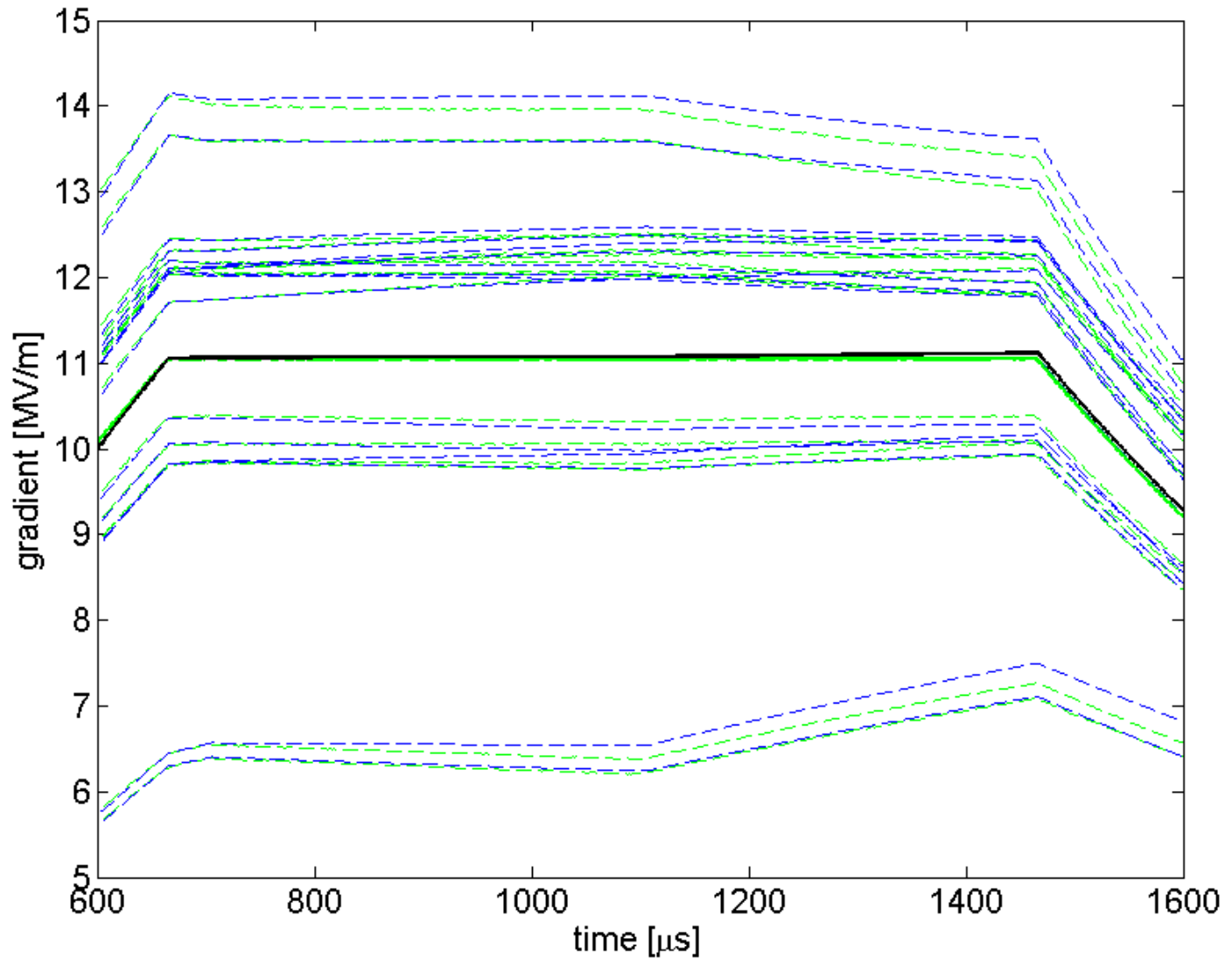
Calibration procedure

1. Load V_{cav} from DAQ
2. Compute actual Q_L , P_K and Δ_f from DAQ data
3. Type in Q_L , P_K and Δ_f into simulator
4. Check agreement between simulated and FLASH data
5. Adjust Q_L in simulator to flatten tilts
6. Implement Q_L corrections in FLASH
7. Check gradient flatness (retune cavities if needed)



Calibration procedure

1. Load V_{cc}
2. Compute Δ_f and $\Delta_f f$
3. Type in simulation
4. Check a between FLASH c
5. Adjust C flatten t
6. Implem correcti
7. Check g (retune



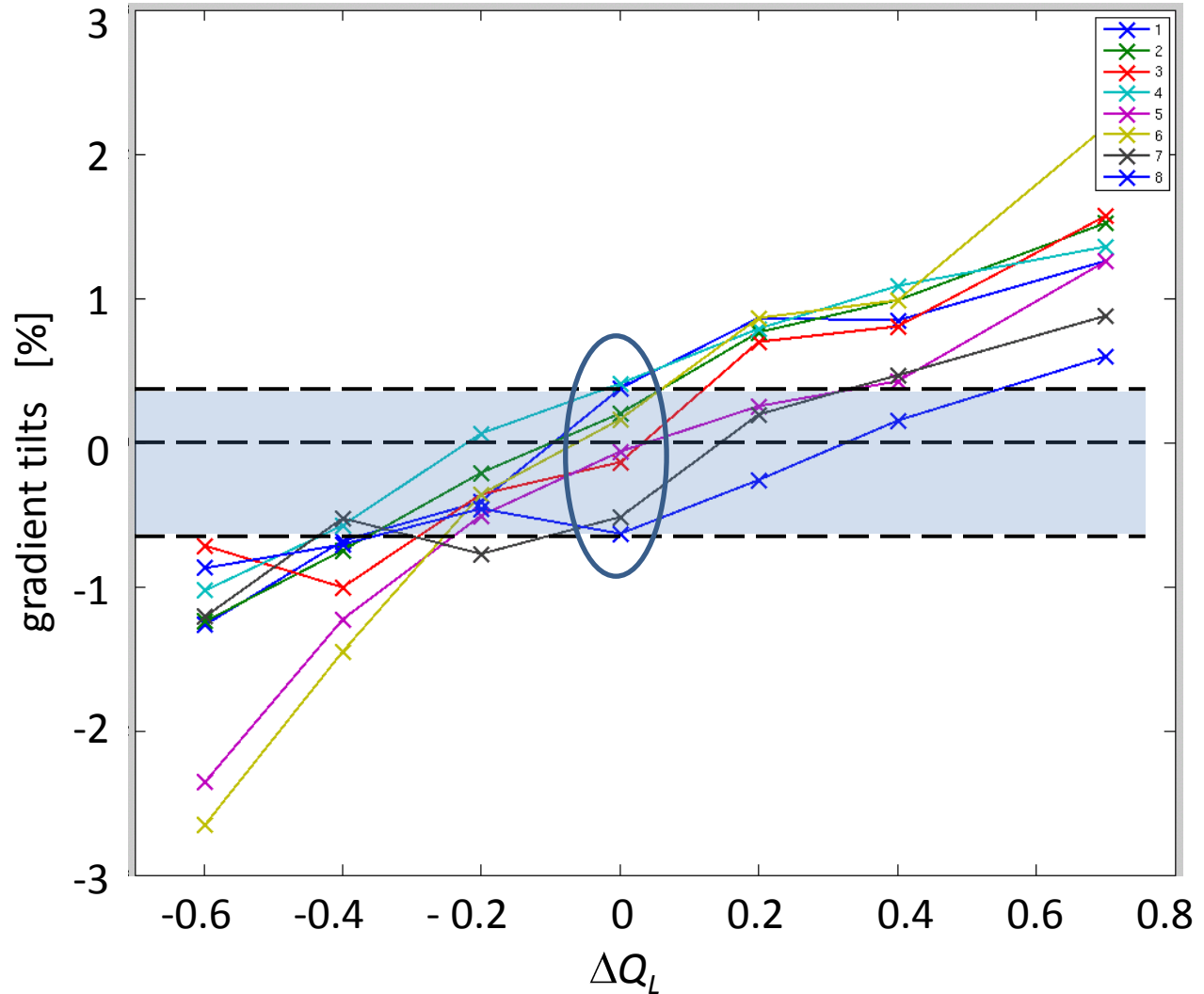
Assessing the accuracy of the model

- Q_L scan

→ Keep beam current constant but walk Q_L 's around optimized value

- I_B scan

→ Keep optimized Q_L 's but ramp beam up/down



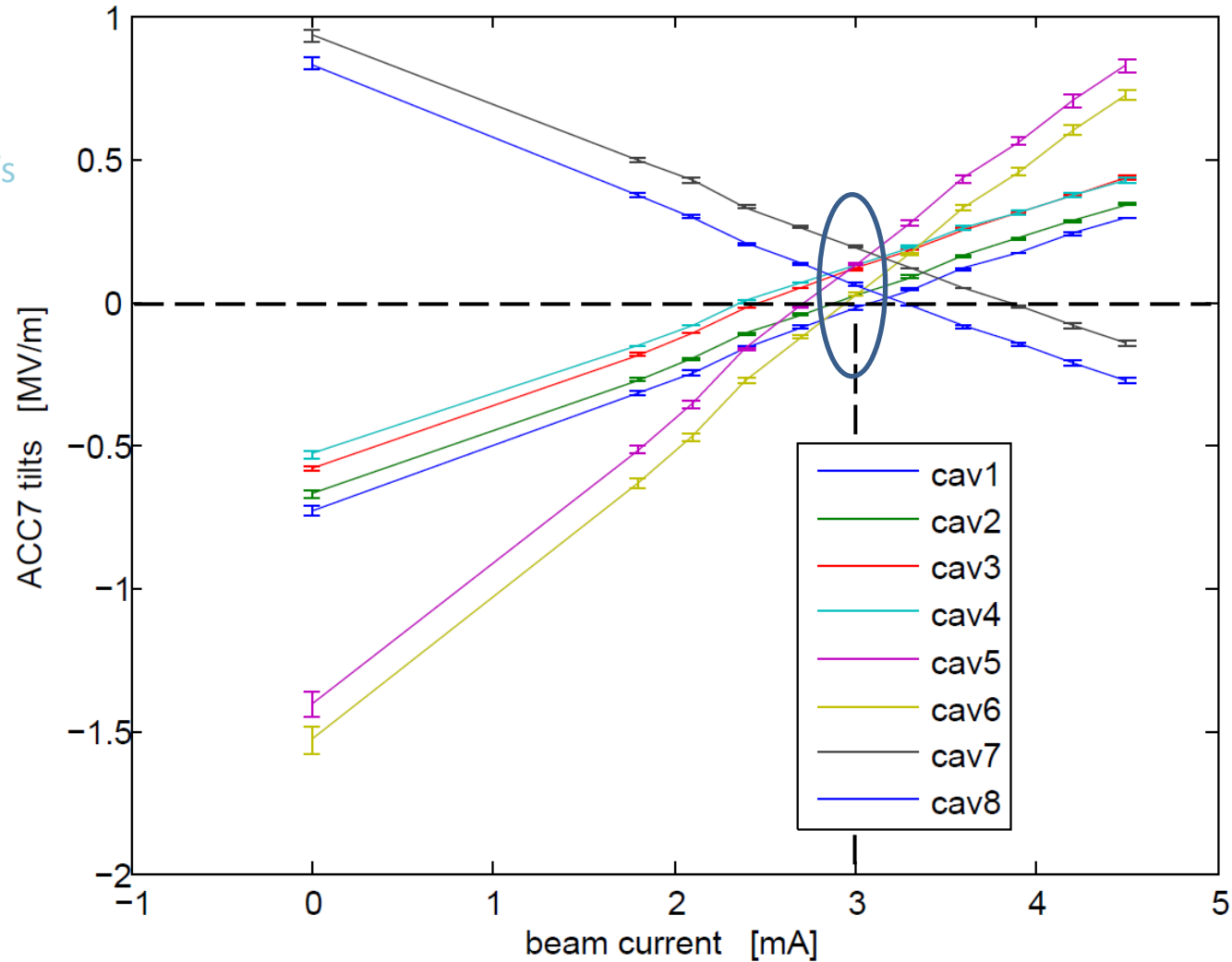
Assessing the accuracy of the model

- Q_L scan

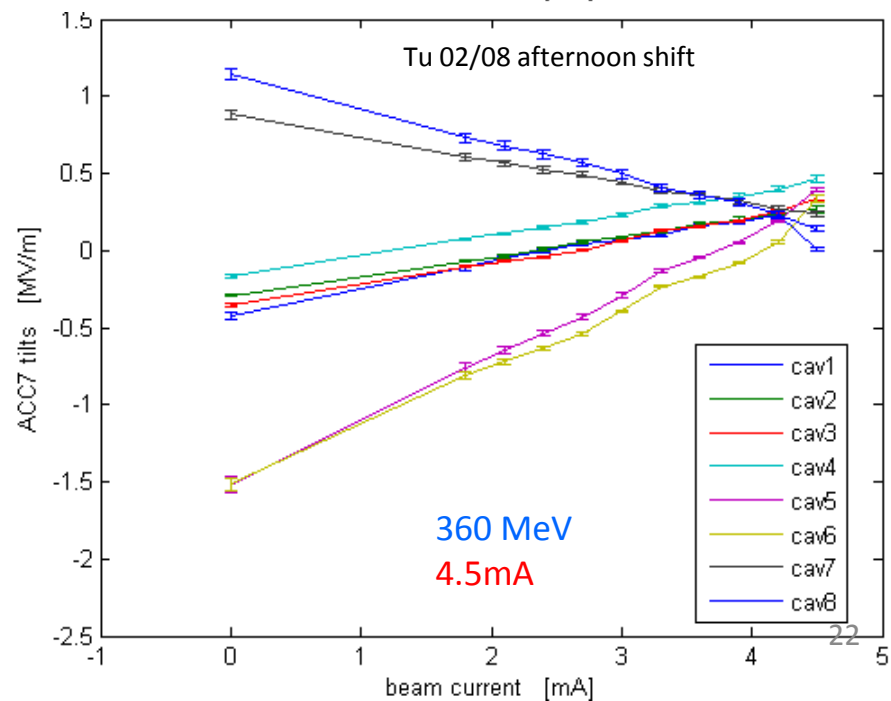
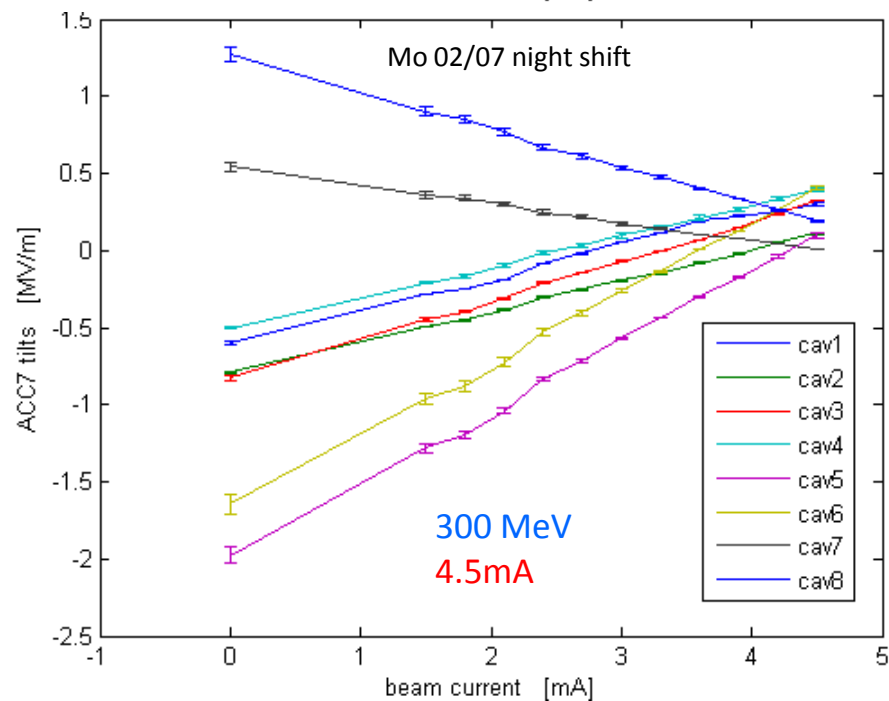
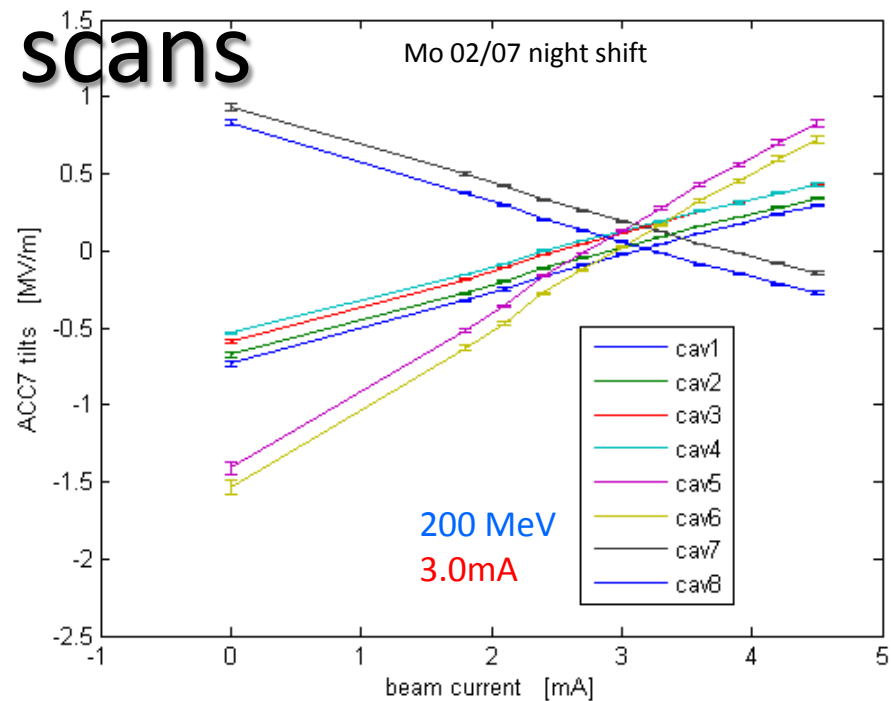
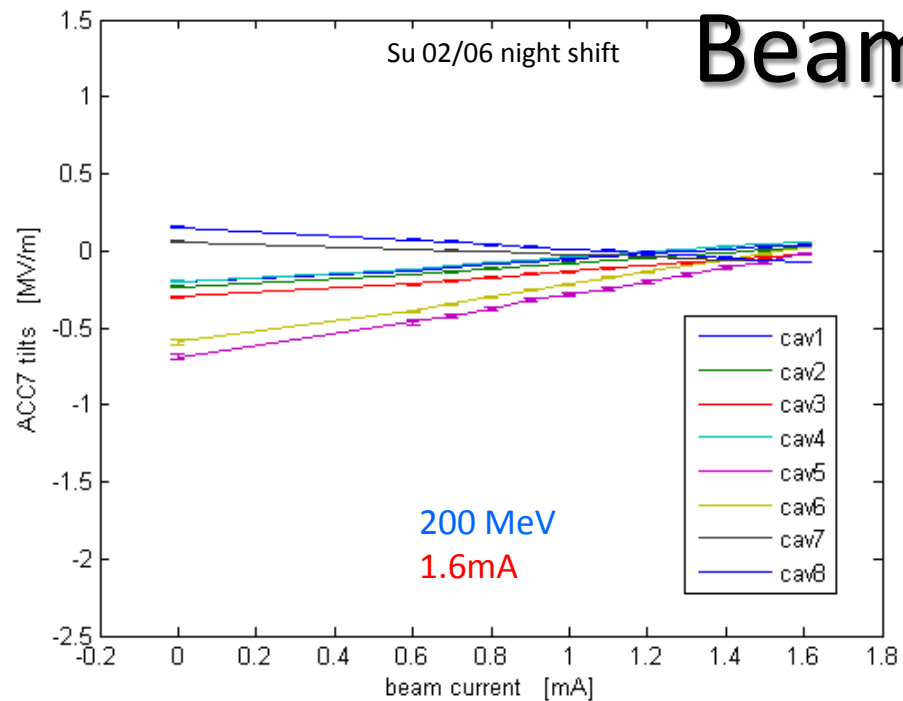
→ Keep beam current constant but walk Q_L 's around optimized value

- I_B scan

→ Keep optimized Q_L 's but ramp beam up/down



Beam scans



The analytical solution

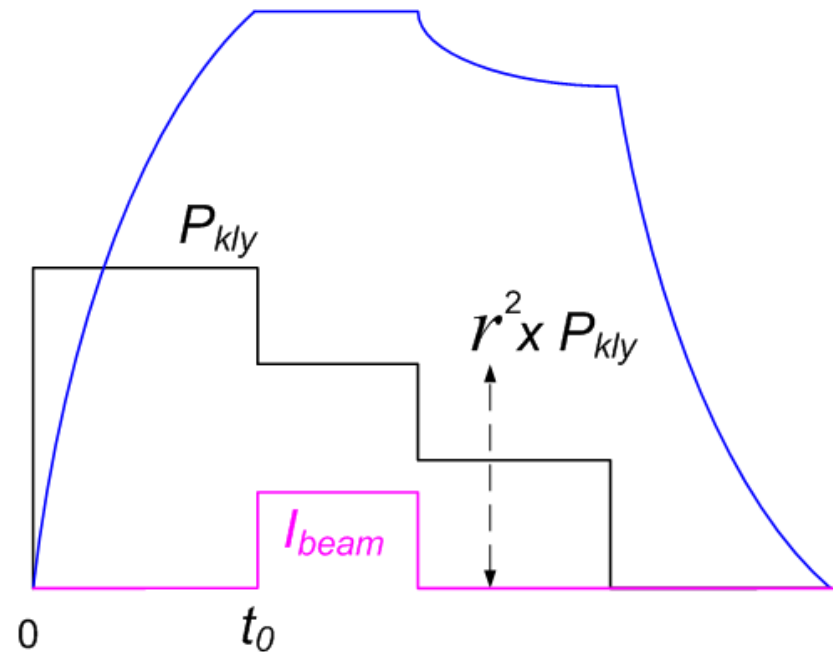
Given a fixed power distribution, a known beam current and beam compensation, find individual Q_L 's that will flatten cavity gradients during beam time

$$e^{-\frac{t_0 \omega_0}{2Q_{Li}}} - \sqrt{\frac{\frac{1}{4} \frac{R}{Q} Q_{Li} I_B^2}{P_{Ki}}} = 1 - r$$

*

→ assumes “perfect” tuning
→ solve for Q_{Li} when possible

- Q_{Li} cavity i loaded Q
- P_{Ki} cavity i forward power during fill time [W]
- I_B DC beam current [A]
- t_0 fill time (\sim beam arrival time) [s]
- r fill time to flat top voltage ratio (including beam compensation)

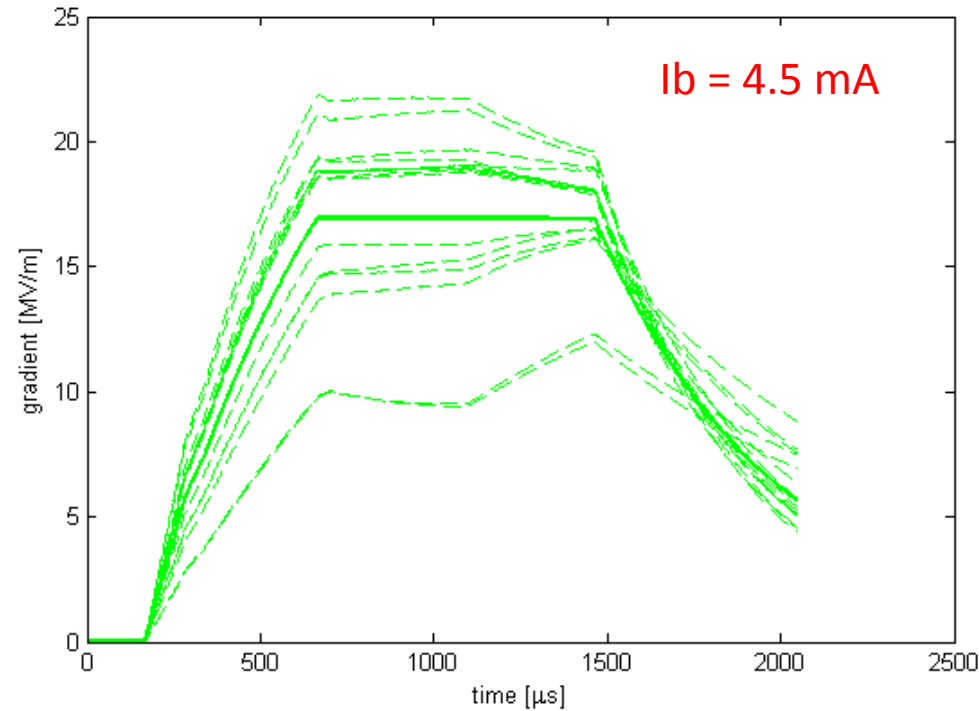


* “Note on solving QL for flat gradients at FLASH ACC6 and ACC7”, J. Branlard, Feb 2011, FNAL Beams-doc-3796
“Analytical solution to the cavity tilt problem.docx”, G. Cancelo, Feb 2011

Beam ON/OFF

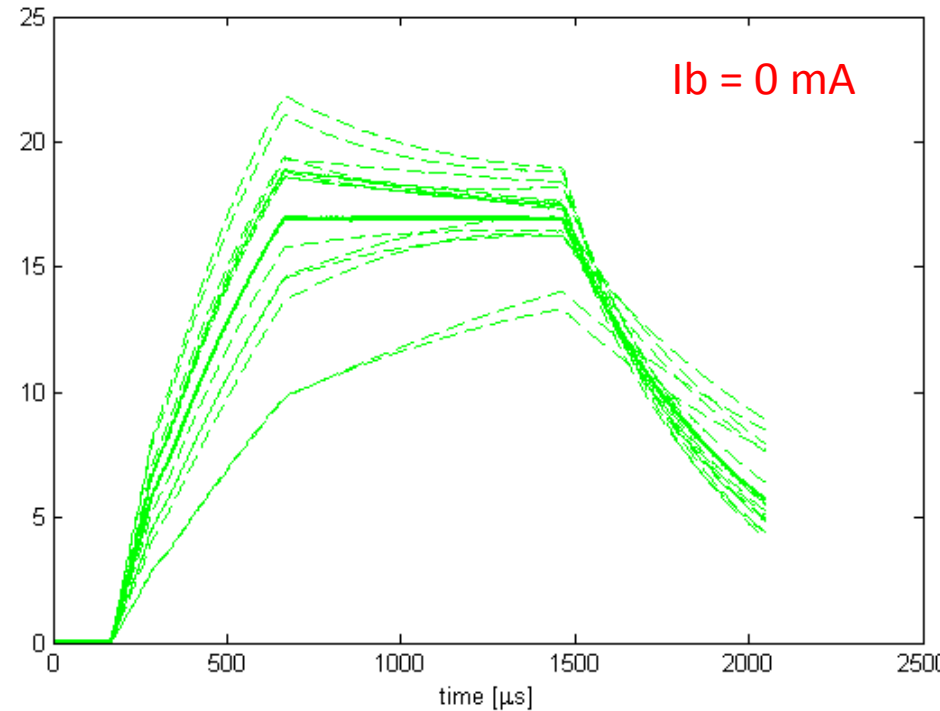
DAQ data 02/08 5:46:14

$I_b = 4.5 \text{ mA}$



DAQ data 02/08 5:51:36

$I_b = 0 \text{ mA}$



- Cavities **below** vector sum **rise** without beam
- Cavities **above** vector sum **drop** without beam
- Need for an **automatic** safety feature **to shorten RF pulse** to prevent quench

Study insights

What went well

- Very stable machine → long study time
- Motorized couplers / tuners → optimal study conditions
automated scripts + skilled operators
- Simulator proved to be very useful
- Predicted optimized Q_L values were accurate → to $0.2e6$
- Successfully implemented the tuning plan → tilts $< 0.1\text{MV/m}$

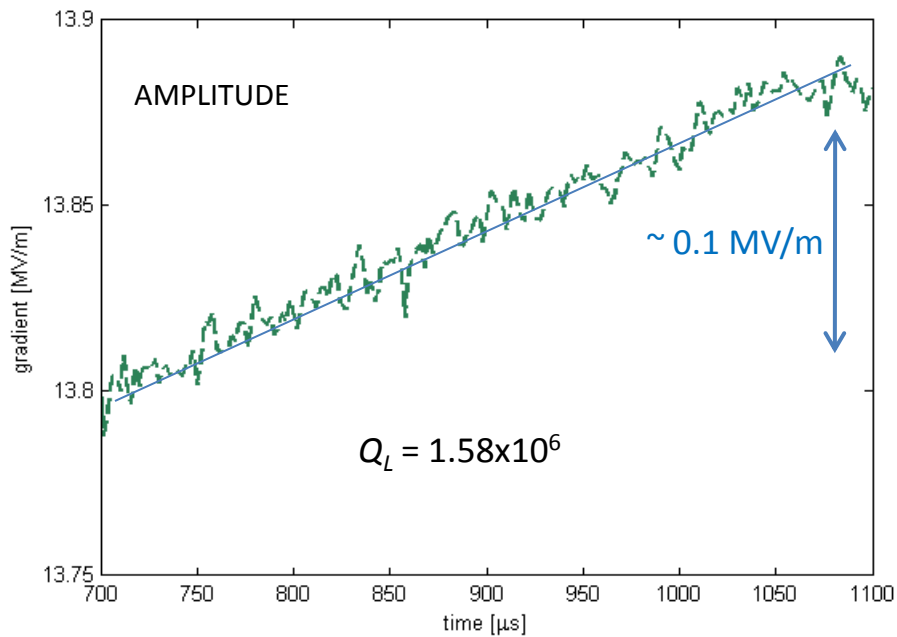
What we've learnt

- Cavity resonance control is crucial for gradient tilts
- Limitations to the simulation approach:
 - How accurately can we measure the power distribution? → John's slide
 - How accurately can we compensate for LFD OR include in model? → next slide
 - How accurately can we measure and set Q_L 's → +/- 2 to 5%
 - Fine tuning "by-eye" is compromised by operating in closed loop

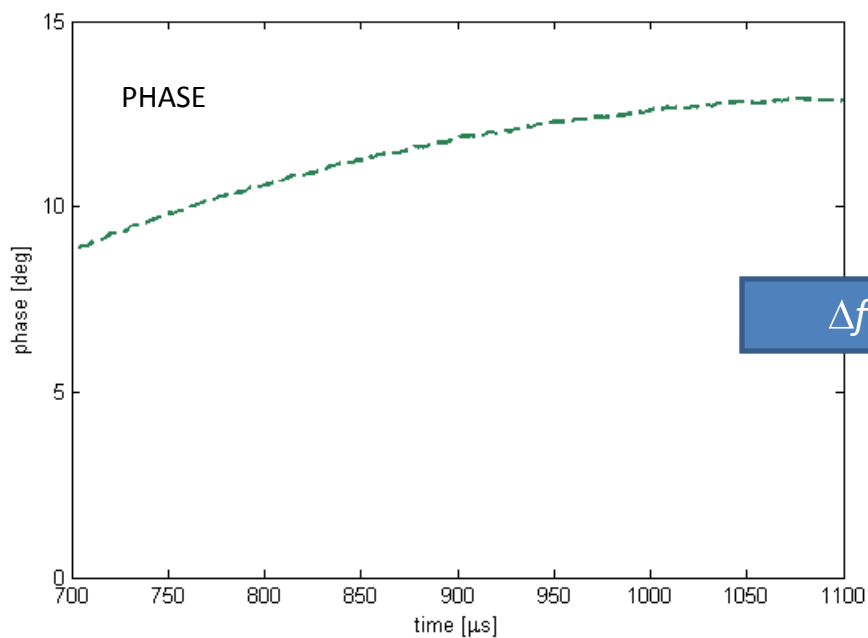
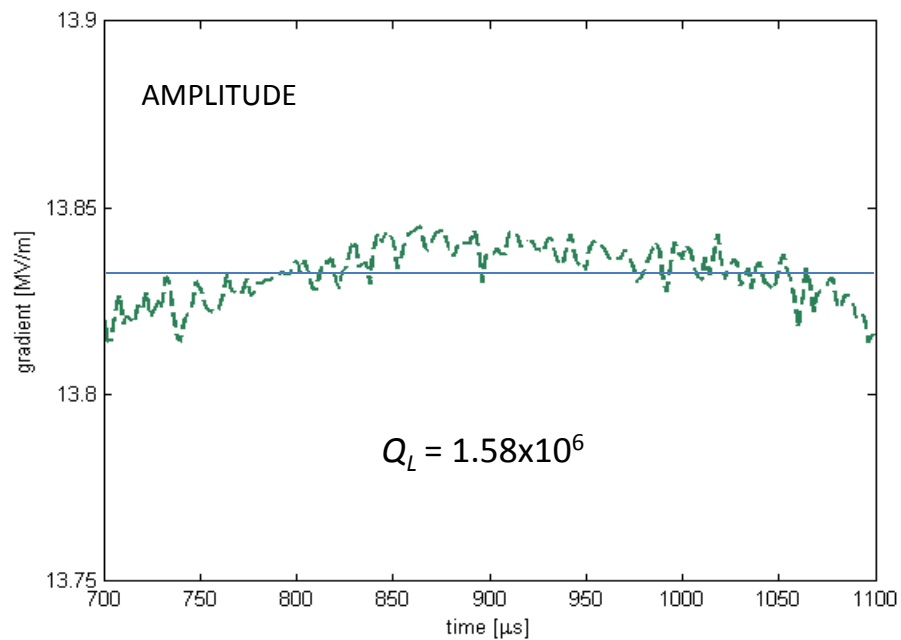
What is still unanswered

- No proposed solution for high beam currents ($>6\text{mA}$) implementable at FLASH
- There is not always a solution to flatten all cavities
(especially when gradient spread is large)
- No solution to bring up the machine at its highest gradient

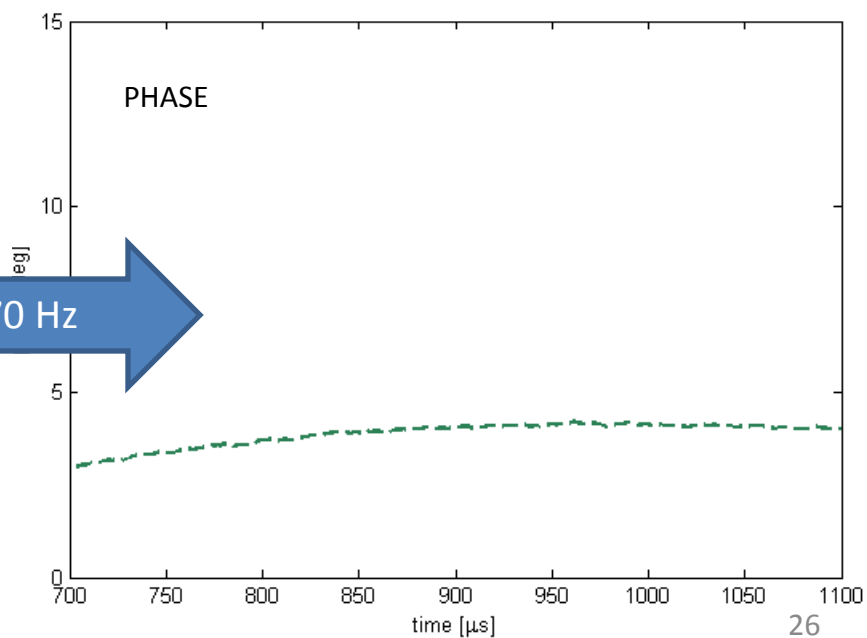
Before freq. tuner adjustments



After freq. tuner adjustments



$\Delta f = 70 \text{ Hz}$



Bringing up a linac

Traditional approach (i.e. FLASH)

1. Make target gradient with FF
2. Turn FB on
3. Compensate for LFD
4. Send a couple of pilot bunches (~10)
(automated beam loading compensation)
5. Minimize losses
6. Gradually increase bunch length to full train
(while minimizing beam losses)
7. Learning feed forward

One “possible” scenario for flat gradients

1. Bring cavity to their nominal gradient
 - typically: quench gradient -2-3 MV/m
2. Adjust Q_L so cavities are flat with beam
 - cavity will quench (because no beam)
3. Shorten pulse length to avoid quench
 - typically <200 usec for high beam currents Q_L 's
 - can't see LFD effects (can't compensate for LFD)
 - can't walk pilot bunch across flat top
4. As you increase bunch length
 - increase flat top length
 - compensate for LFD
 - minimize losses
5. The LLRF quench monitoring system should
 - truncate the flat top length to prevent quenches
 - every time bunch train is shorter than expected

References

- “RF Distribution Optimization in the Main Linacs of the ILC”, Bane, Adolphsen, Nantista - WEPMS037.pdf
- “Optimal Coupler and Power Settings for Superconductive Linear Accelerators”, J. Branlard, B. Chase, Linac 2008
- “Optimizing Cavity Gradient in Pulsed Linacs Using the Cavity Transient Response”, G. Cancelo, A. Vignoni, Linac 2008
- “Effect of Cavity Tilt and RF Fluctuations to Transverse Beam Orbit Change in ILC Main Linac”, K. Kubo, Jan. 2010
- “PkQI-like control for ACC6/7 at FLASH” S. Michizono, PkQI_FLASHver3.docx, Sept. 2010
- “To flatten the cavity gradient for ACC6/7” S. Michizono, FLASH101022BV2.pdf, Nov. 2010
- “Analytical solution to the cavity tilt problem.docx”, G. Cancelo, Feb 2011
- “Note on solving QL for flat gradients at FLASH ACC6 and ACC7”, J. Branlard, FNAL Beams-doc-3796
- SIMCAV version 4.8 (FLASH ACC6 and ACC7 16 cavity MATLAB simulator), FNAL Beams-doc-3794

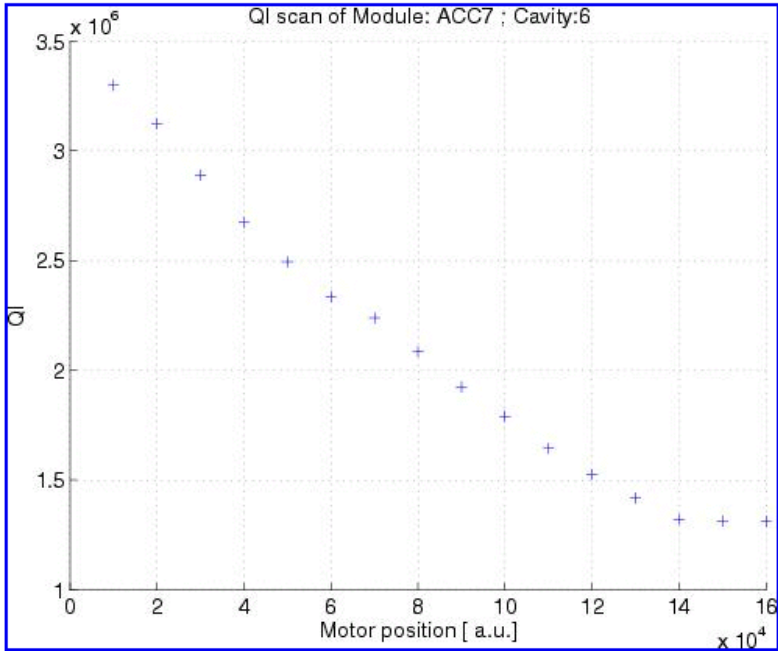
THANK YOU

BACKUP SLIDES

SUMMARY

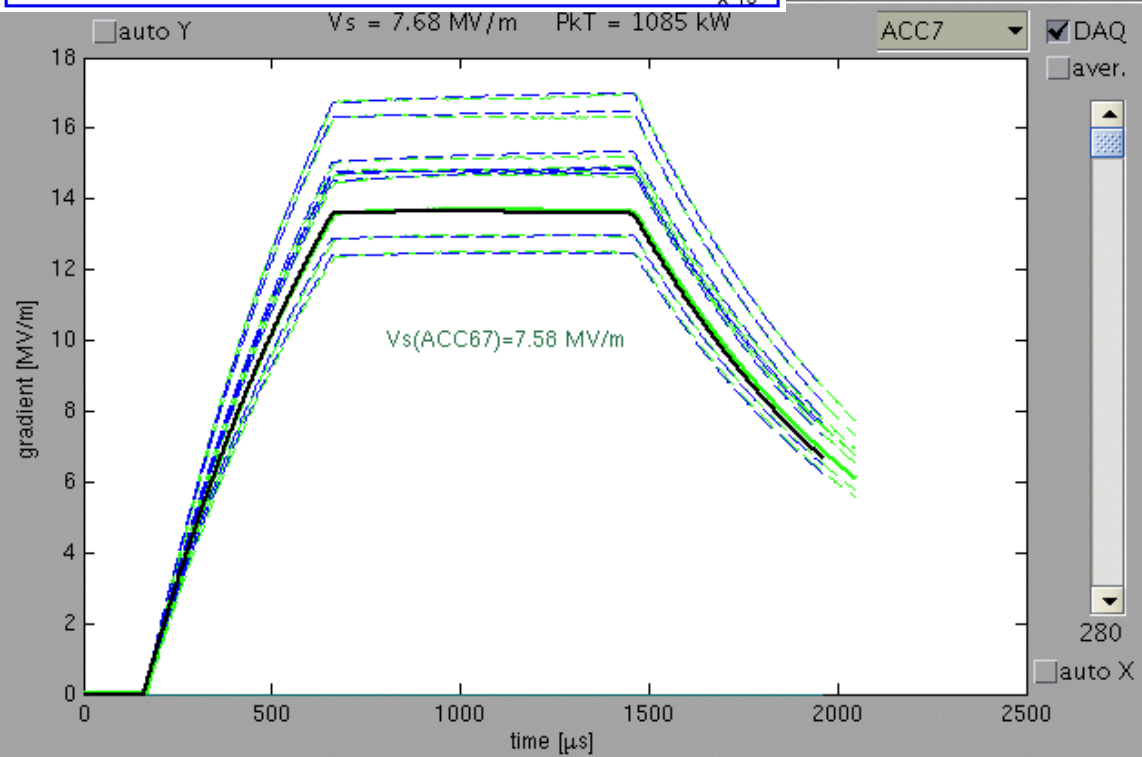
- Why do we care about individual flat gradients?
 - KEK paper
- What can we actually implement at FLASH?
 - No P_K adjustments
 - Only Q_L can be changed
 - Limited range in Q_L changes
- What solutions were offered to achieve flat gradients with beam loading?
 - SLAC paper , using Q_L and P_K adjustments
 - Shin's solution with square P_{fwd} pulse
 - Shin's solution with step ratio P_{fwd} pulse
- What approach have we followed during the FLASH test studies?
 - Procedure (issues with adjusting Q_L when beam is OFF)
 - When beam is ON, beam compensation is ON too
 - Which tools did we use
 - The analytical solution
- Results of the P_K / Q_L studies
 - Assess Q_L ranges
 - Low gradient / mid gradient
 - Low beam / mid beam current
 - Beam scans
 - Q_L scans
- Conclusions and lessons learnt
 - How accurate were the tuning adjustments?
 - What limited the accuracy of tuning adjustments?
 - Difference between solving the problem open / close loop
 - Impact of detuning on tilts (static & dynamic)
 - No solution to bringing the machine up to its maximum gradient

Shift-by shift highlights



Friday 2/4 night shift – highlights:

- no beam
- ACC6/7 vector sum calibration 100 bunches, 1 MHz, 1.6 nC
- Q_L tuners characterization for ACC6/7
- simulator calibration to reflect ACC6/7 power distribution



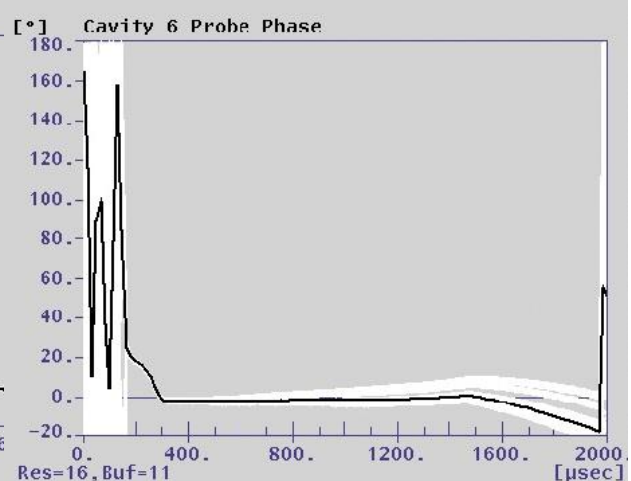
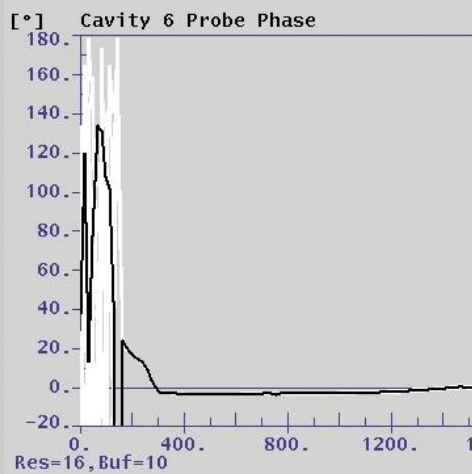
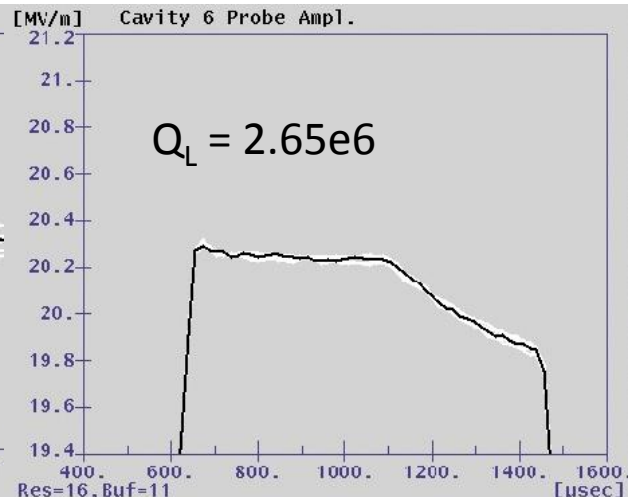
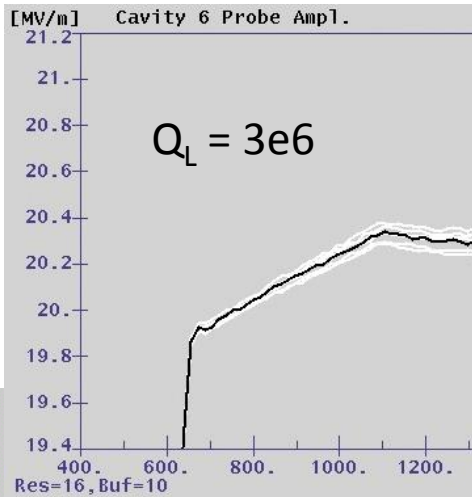
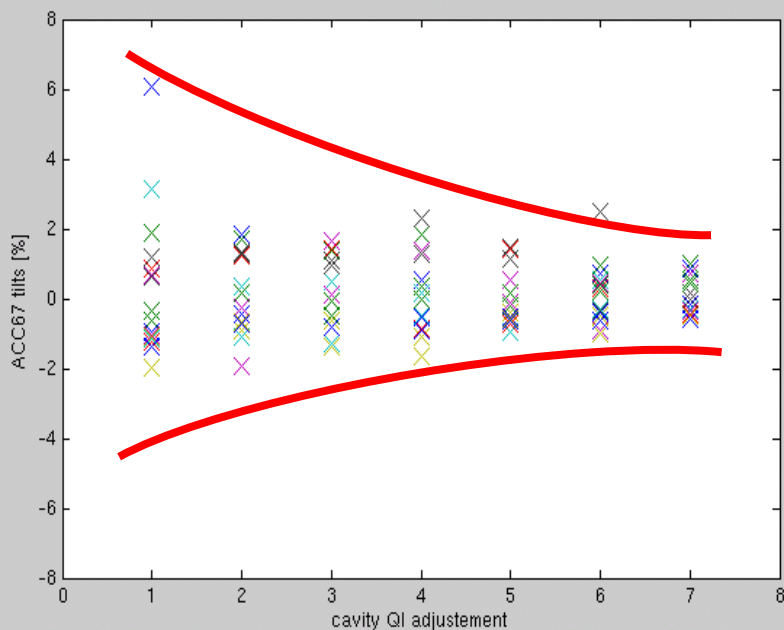
Cryomodules

Cryomodule ACC7

	V lim [MV/m]	$Q_L [\times 1e6]$	Pk [dB]	Det [Hz]		
1	29.0	3.09	3.09	8.75	-41	-41
2	31.0	2.93	2.93	8.68	-53	-53
3	34.0	3.00	3.00	8.68	34	34
4	30.0	3.05	3.05	8.45	-31	-31
5	35.0	3.04	3.04	7.55	28	28
6	39.0	2.97	2.97	7.8	-2	-2
7	27.0	2.96	2.96	9.85	-28	-28
8	26.0	2.97	2.97	10.17	-44	-44

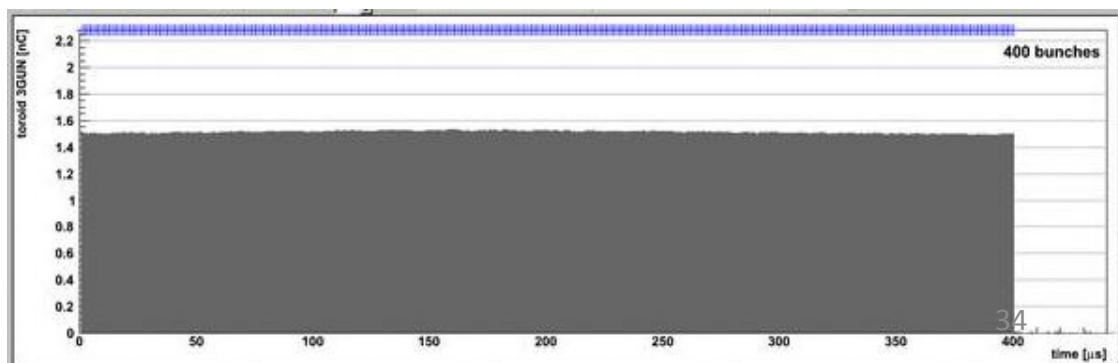
Saturday 2/5 night shift – highlights:

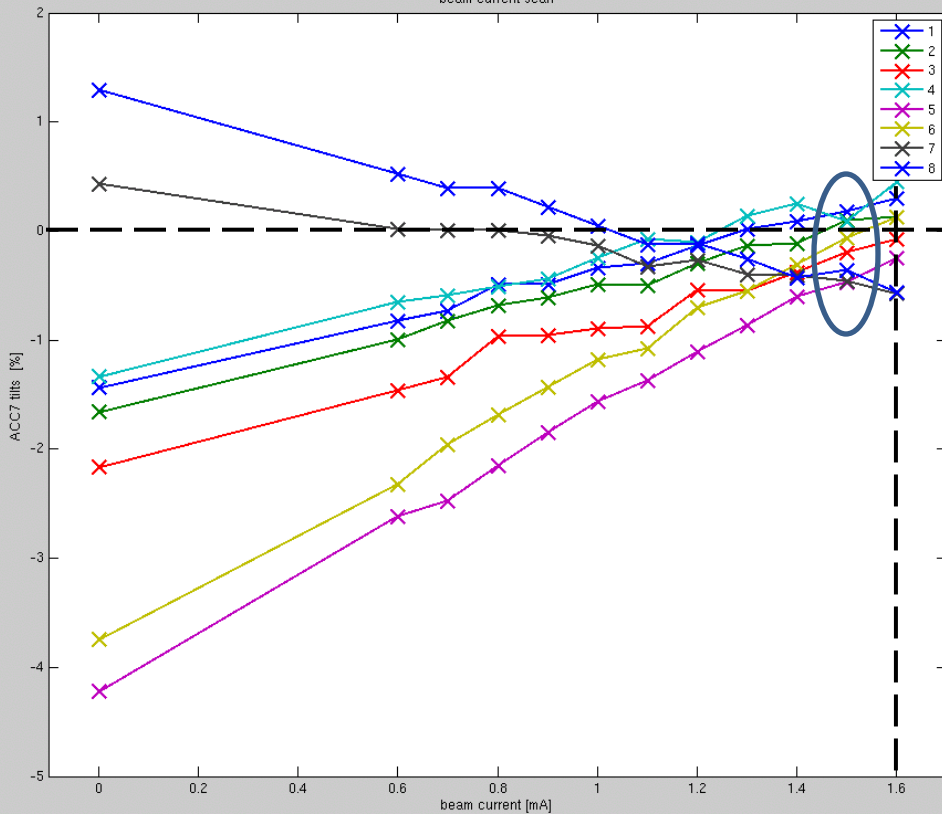
- 1mA beam, low gradient (100–200 MeV)
- Successfully implemented QL adjustments to flatten cavity gradients
- beam loading tilts correction (all tilts below 1%) using simulator predicted values
- Simulated values are reliable



ACC6	cav1	0.87 %
ACC6	cav2	1.01 %
ACC6	cav3	0.44 %
ACC6	cav4	0.70 %
ACC6	cav5	0.71 %
ACC6	cav6	-0.17 %
ACC6	cav7	0.15 %
ACC6	cav8	-0.17 %

ACC7	cav1	0.55 %
ACC7	cav2	-0.43 %
ACC7	cav3	-0.30 %
ACC7	cav4	-0.32 %
ACC7	cav5	-0.50 %
ACC7	cav6	-0.01 %
ACC7	cav7	-0.57 %
ACC7	cav8	0.45 %





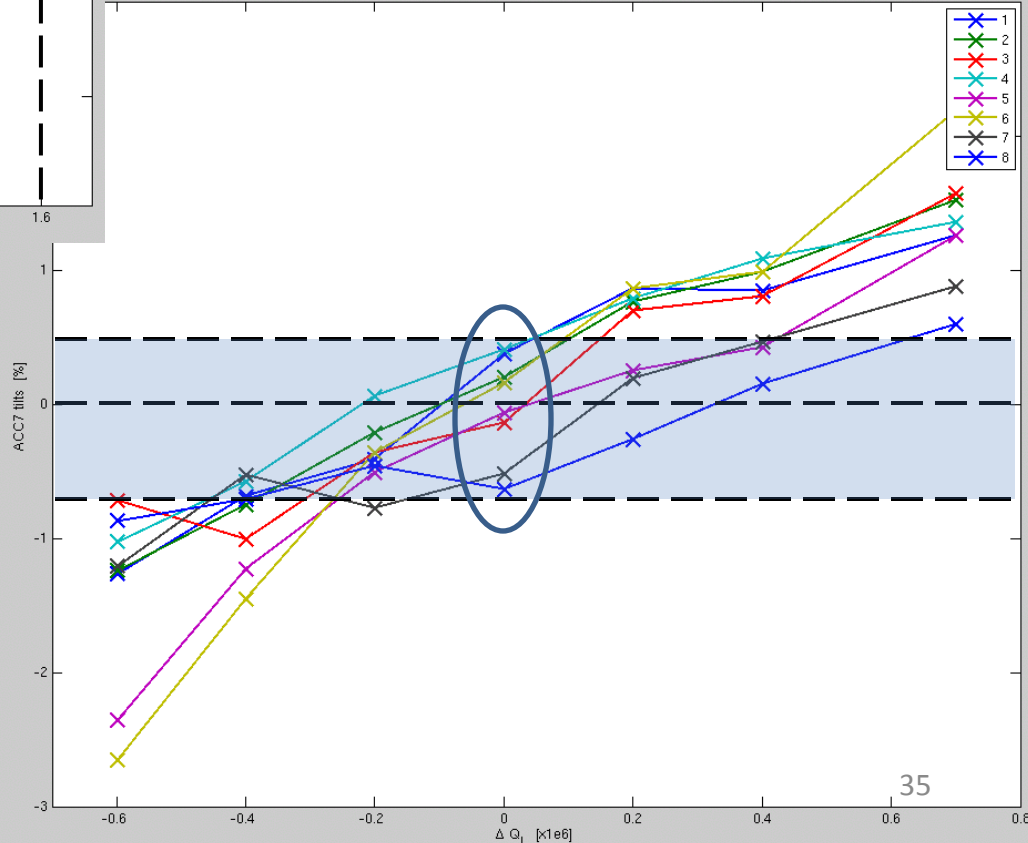
Sunday 2/6 night shift – highlights:

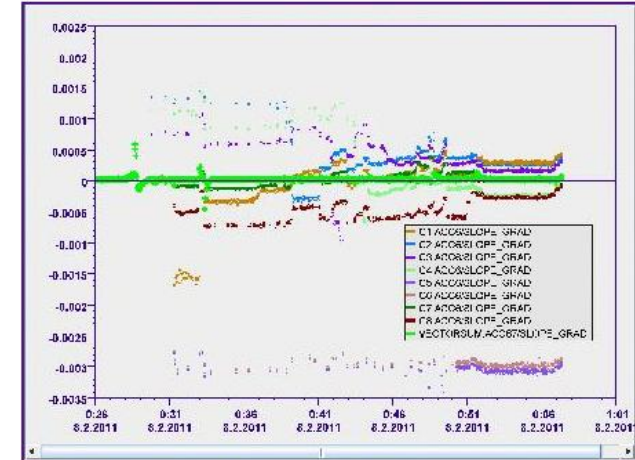
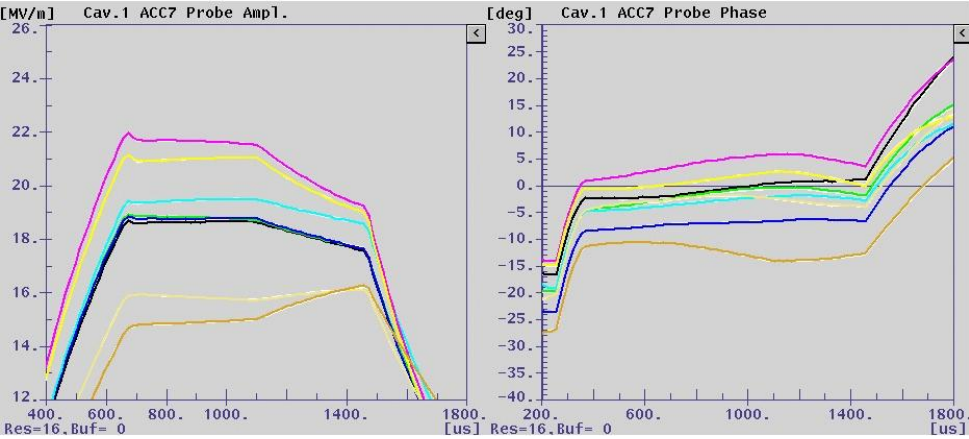
- 1.6mA beam, low gradient (200 MeV)
- beam loading tilts Q_L correction (below 1%) (several cavities at once, with beam on)
- beam current scan
- Q_L scan

ACC7-cav0= -0.23 %
 ACC7-cav1= 0.35 %
 ACC7-cav2= 0.17 %
 ACC7-cav3= -0.03 %
 ACC7-cav4= 0.32 %
 ACC7-cav5= -0.15 %
 ACC7-cav6= 0.15 %
 ACC7-cav7= -0.58 %
 ACC7-cav8= -0.59 %

Ql config is for ACC7:

cav1 : 2.8 e6
 cav2 : 2.8 e6
 cav3 : 2.8 e6
 cav4 : 2.8 e6
 cav5 : 2.5 e6
 cav6 : 2.5 e6
 cav7 : 3.1 e6
 cav8 : 3.2 e6

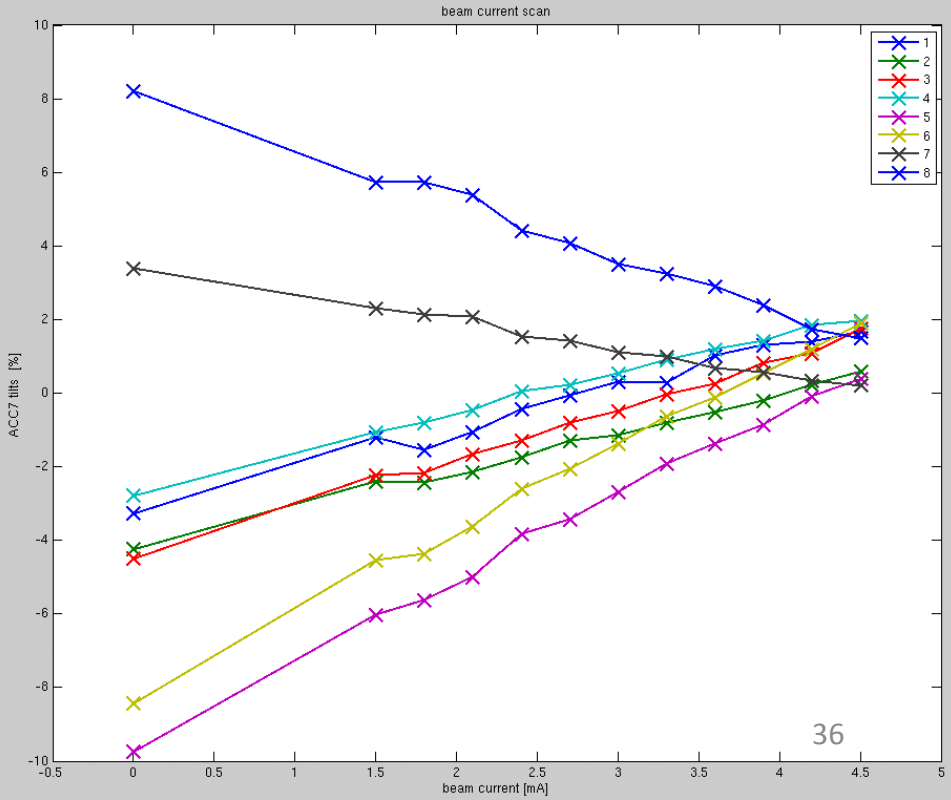
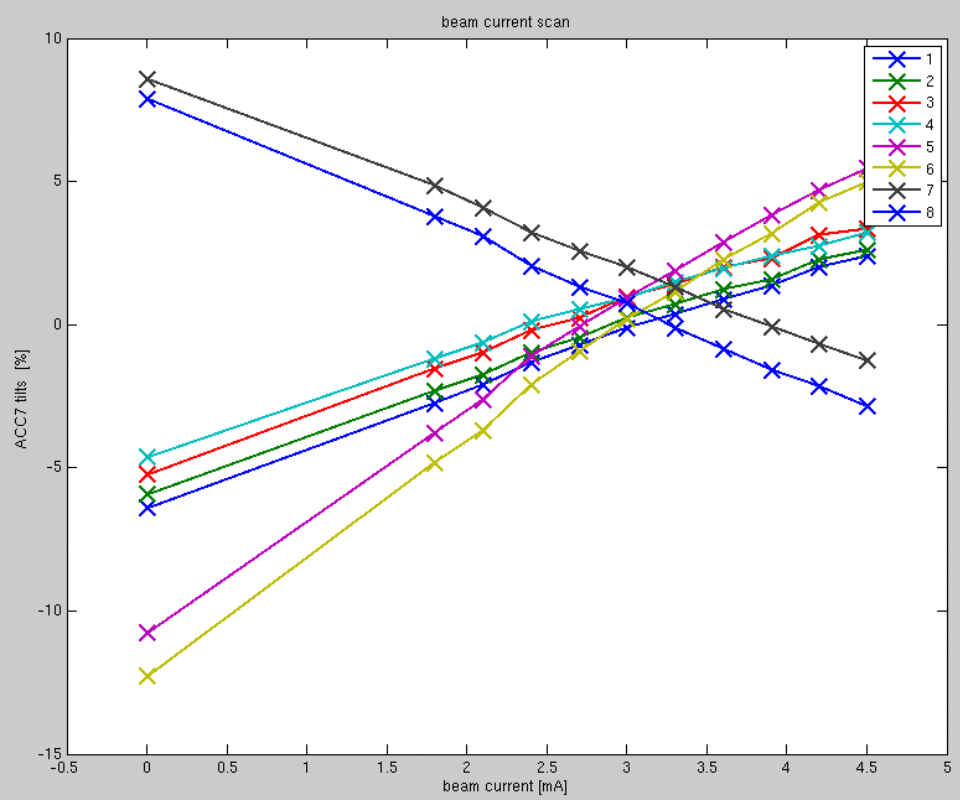




Monday 2/7 night shift – highlights:

- 3.0mA beam, 200 MeV
- Q_L adjusted for gradient flat at 3mA
- beam scan from 0.9 to 4.5 mA

- 4.5mA beam, 300 MeV
- Q_L adjusted for gradient flat at 4.5 mA
- beam current scan



Tuesday 2/8 afternoon shift – highlights:

- 4.2mA beam, 360 MeV
- Lorentz force detuning compensation
- Use calculator to predict QL \rightarrow very accurate prediction
- Flatten ACC6/7 gradients tilts to $\sim 1.5\%$ (tuned for 4.2mA)
- beam current scan to 4.5 mA

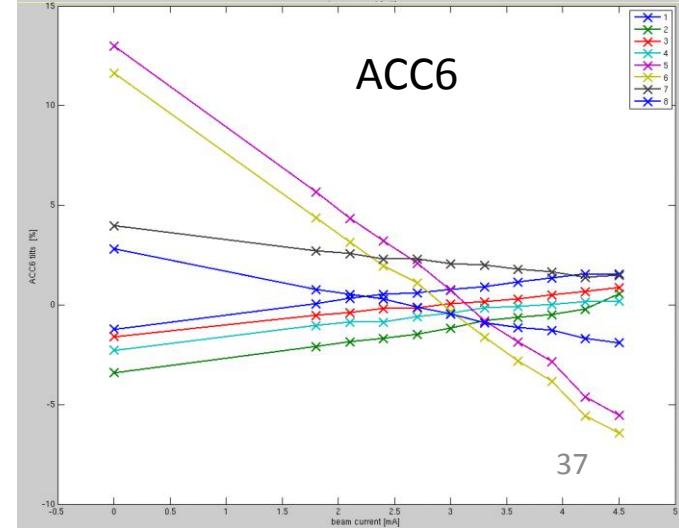
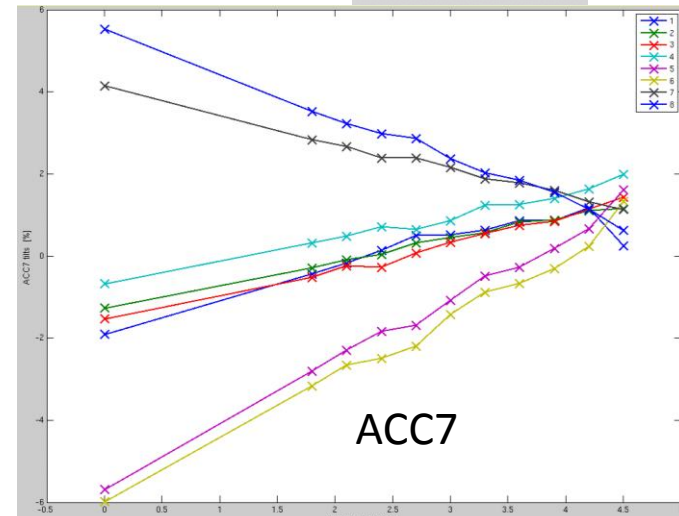
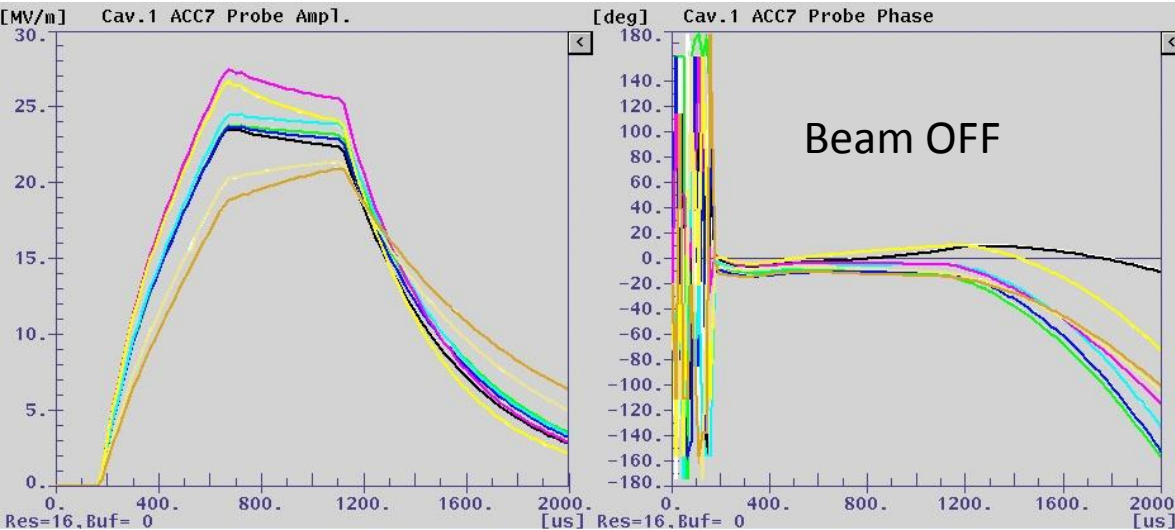
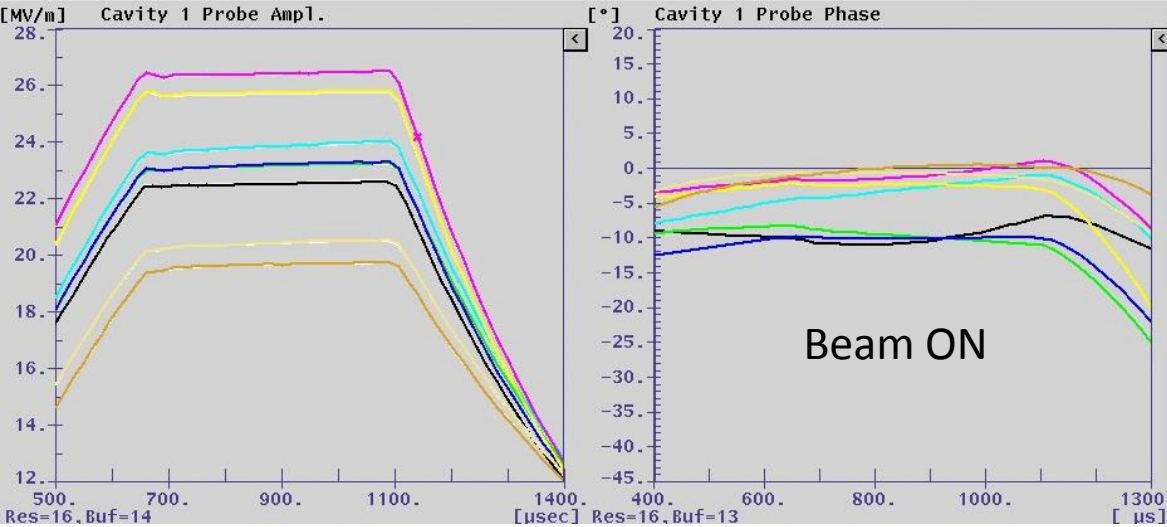
ACC7 Q_L values

Predicted

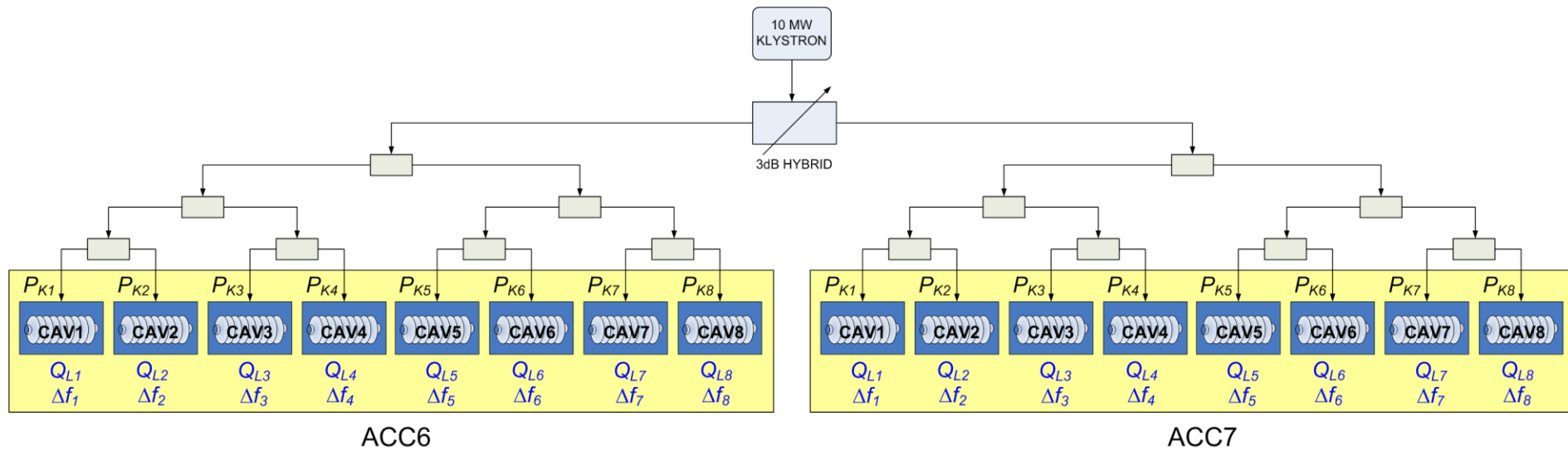
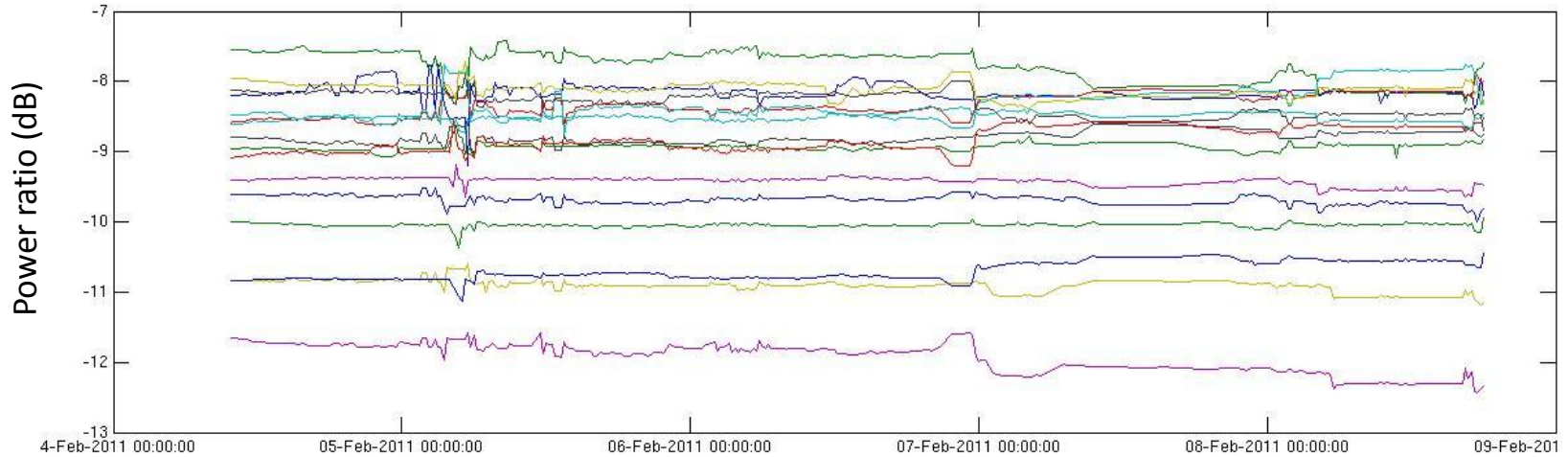
Implemented

cav1. 1.78 e6
 cav2. 1.74 e6
 cav3. 1.85 e6
 cav4. 1.88 e6
 cav5. 3.25 e6
 cav6. 3.12 e6
 cav7. 2.37 e6
 cav8. 2.40 e6

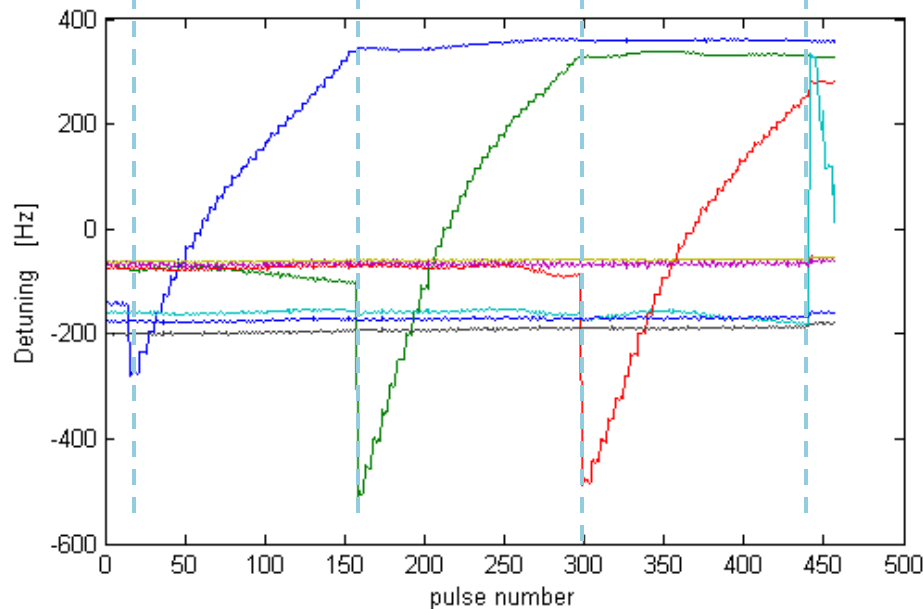
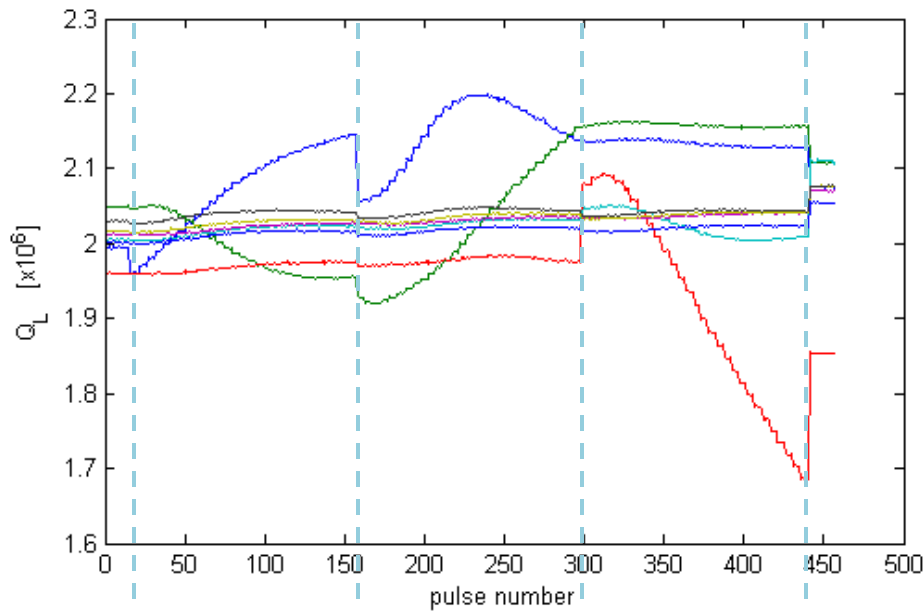
Cavity#	Loaded Q
1	1.79e+06
2	1.77e+06
3	1.84e+06
4	1.91e+06
5	3.28e+06
6	3.10e+06
7	2.37e+06
8	2.28e+06



Power ratios



Power coupling between adjacent cavities



- 3 sequences of detuning: cav1, then cav2 then cav3.

- when we reach the end of the detuning range of one cavity, the detuning of the adjacent cavity is affected

- Q_L changes with the detuning for all three cavity (cav1 and 2 in one direction, cav3 in the opposite direction)

- We see that $Q_L(\text{cav1})$ and $Q_L(\text{cav2})$ are coupled.

- Similarly, $Q_L(\text{cav3})$ and $Q_L(\text{cav4})$, but no cav3-cav1 coupling