

Study of Higgs Self- couplings at ILC

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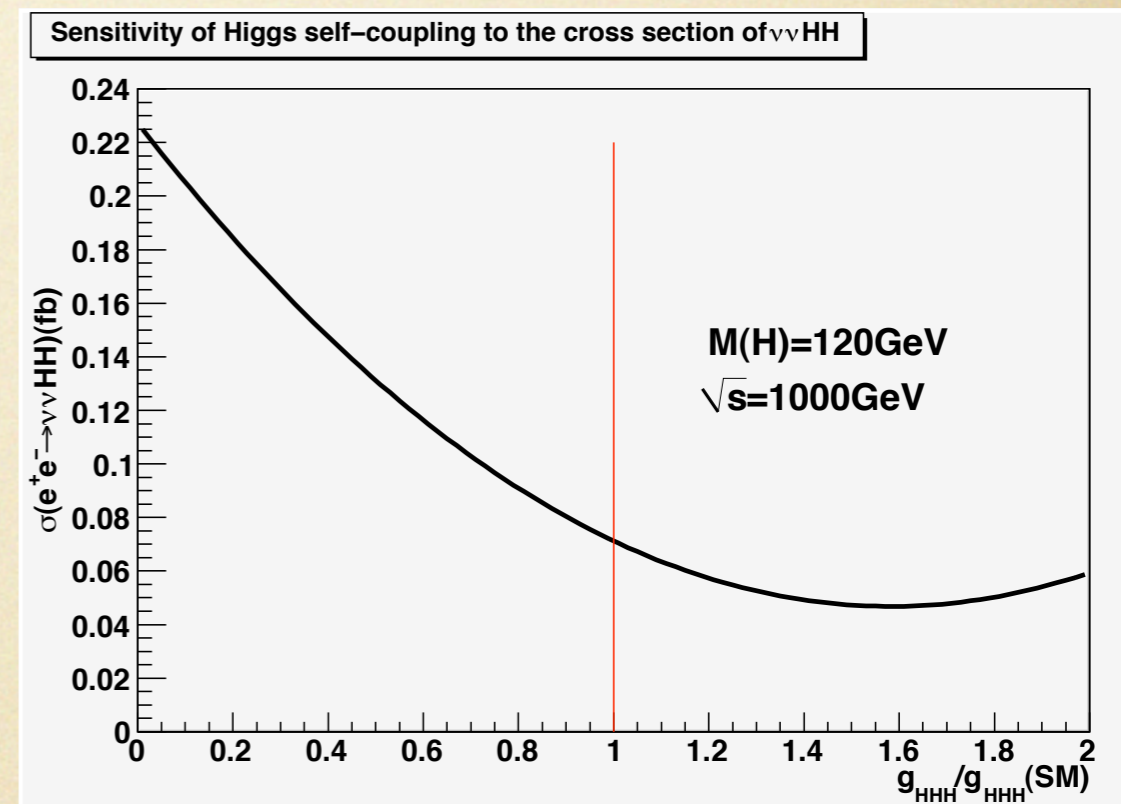
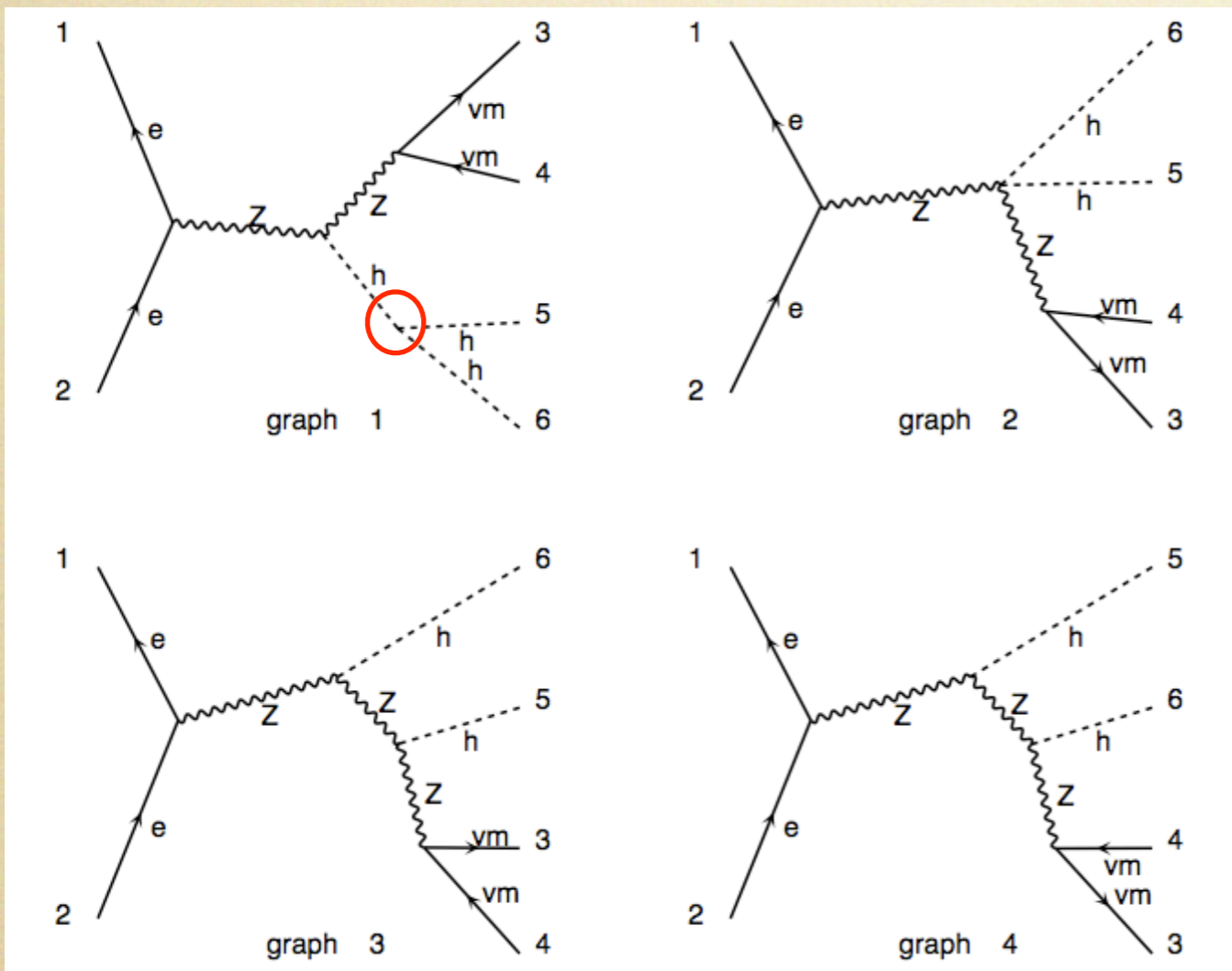
$$e^{-} + e^{+} \rightarrow \nu\bar{\nu}HH$$

(fast simulation)

$$\sigma = 71.3 \text{ ab} \quad @E_{\text{cm}} = 1\text{TeV}$$

ISR

No BeamStrahlung



$$\frac{\Delta\lambda}{\lambda} = 0.85 \frac{\Delta\sigma}{\sigma}$$

$$e^{-} + e^{+} \rightarrow \nu\bar{\nu} H H \rightarrow (\nu\bar{\nu})(b\bar{b})(b\bar{b})$$

previous!

Pre-selection:

- number of reconstructed particle ($E > 0.1 \text{ GeV}$) ≥ 40
- number of isolated lepton = 0
- force all the particles to four jets
- combine the four jets by minimizing

$$\chi^2 = \frac{(M(b, \bar{b}) - M_H)^2}{\sigma_{H_1}^2} + \frac{(M(b, \bar{b}) - M_H)^2}{\sigma_{H_2}^2}$$

constraint implied in the pre-selection:

$$|M(bb) - M(H)| < 80 \text{ GeV}$$

previous!

preliminary results

no beam polarization

$$E_{\text{cm}} = 1000\text{GeV}, M_H = 120\text{GeV}$$

$$\int Ldt = 2\text{ab}^{-1}$$

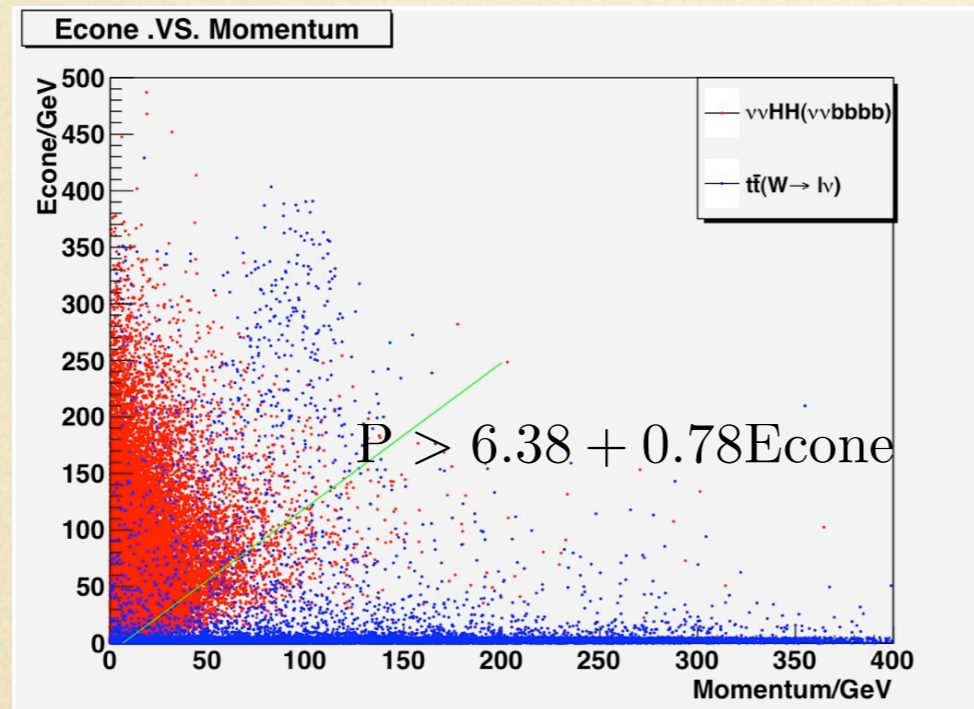
	$\nu\nu\text{HH}(\nu\nu\text{bbbb})$	tt-bar	WWZ	ZZZ	ZZH	$\nu\nu\text{ZZ}$	$\nu\nu\text{WW}$	ttH	$\nu\nu\text{ZH}$
MC	500K	500K	500K	500K	500K	50K	50K	50K	50K
expected	142.6(63.4)	377600	123400	1664	700	12100	30200	4960	2500
pre-selection	101.3(54.4)	146603	25653.6	586.1	219.4	5812	13658	134.2	1452
Evis<600	96.8(51.9)	25764.4	10361.4	310.3	119.8	5638	13237	57.8	1379
mvatt>0.8	25.1(15.0)	302.1	58.5	1.25	1.26	120.8	161	1.19	89.0
noff4>0	10.2(8.58)	31.0	2.22	0.08	0.20	6.8	0	0.50	12.8
noff3>2	7.18(6.72)	5.29	0.25	0.05	0.10	4.11	0	0.20	6.90
mjet4>2	7.10(6.71)	1.51	0	0.05	0.10	4.11	0	0.20	6.85

analysis strategy changed

- the previous non isolated lepton criterion is a bit tighter (85%) as a pre-selection. we used a new looser one (98%).
- in order to suppress the $\nu\nu ZZ$ and $\nu\nu ZH$ background, we need better mass resolution. there are two factors which effect the resolution: miss jet clustering and wrong jet pairing. first we defined a quantity to tag the jet, and then we can evaluate the wrong pairing possibility of a specified jet pairing algorithm.
- a new jet pairing algorithm based on the likelihood of the invariant mass of jet pairs was used.
- previously, we only trained the neural-net for $t\bar{t}$ background, now we trained another neural-net for $\nu\nu ZZ$ and $\nu\nu ZH$.

criterion of isolated lepton

previous:



red: all the particles from signal vvbhhh
blue: leptons from the semi-leptonic decay of tt-bar

coefficients from Fisher method in TMVA

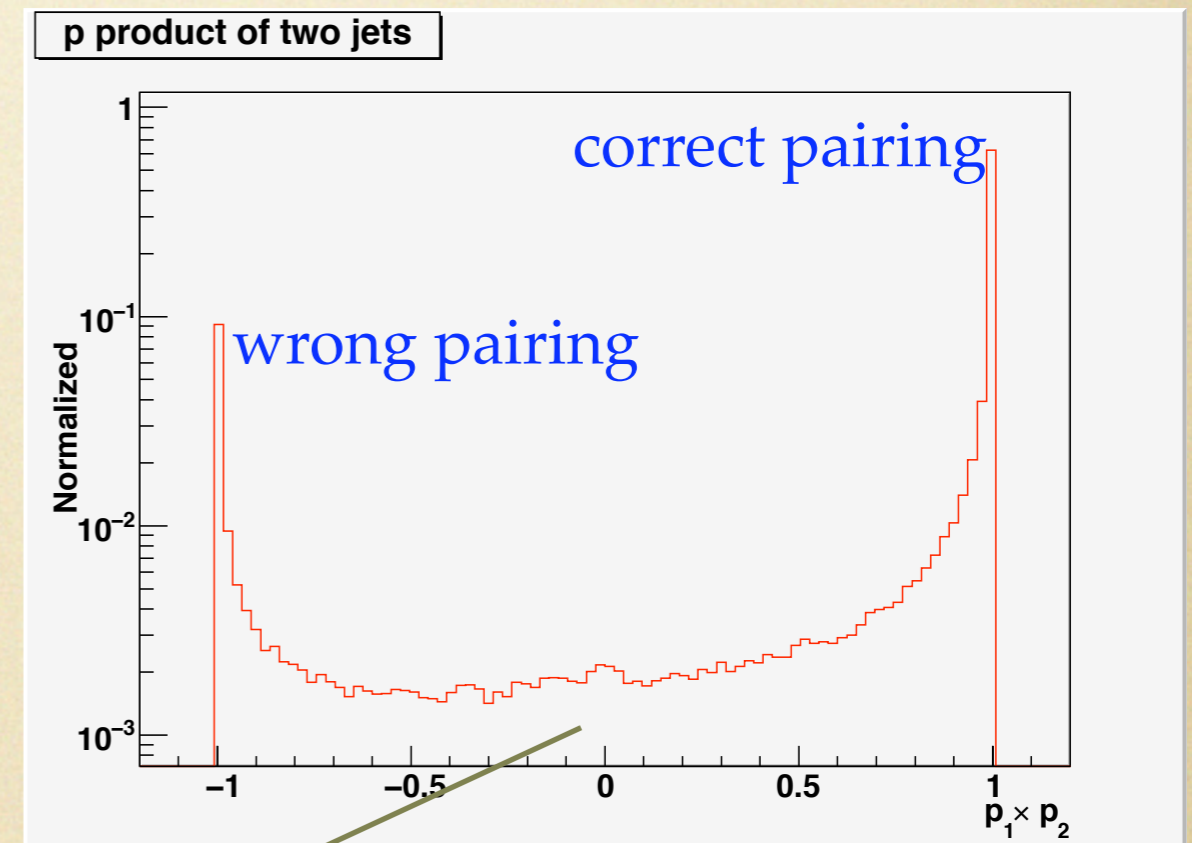
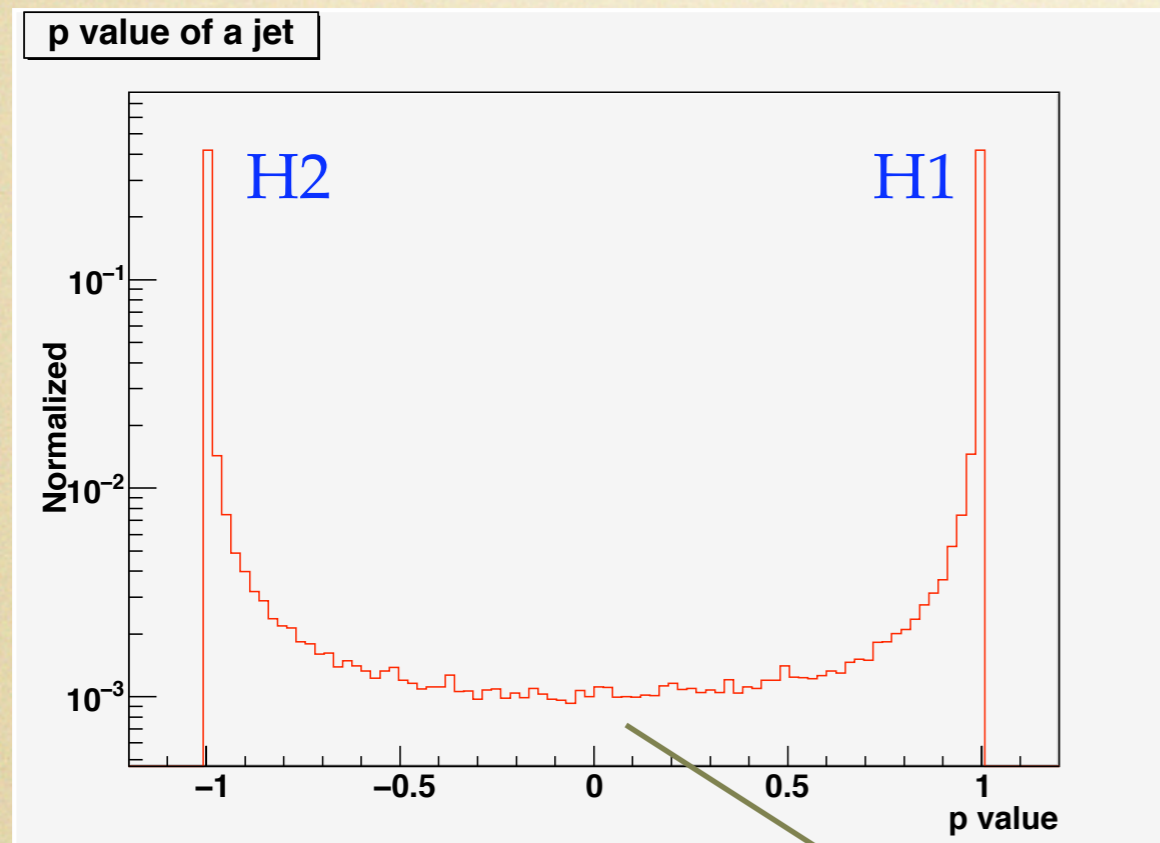
now:

$$E_{\text{cone}} < 20 \text{ GeV} \ \&\& \ P > 20 \text{ GeV}$$

tagging of color singlet id for a jet

- for signal events, the four b jets come from two color singlets: H1 and H2.
- for each track in a jet, by using the truth information we can know which color singlet it comes from.
- for a jet, we can count the number of tracks and the sum of energy belongs to H1 and H2 respectively.
- define a quantity:
$$p = \frac{n_1 E_1 - n_2 E_2}{n_1 E_1 + n_2 E_2}$$
- if $p > 0$, the jet comes from H1, otherwise H2.

typical distributions of p value and product of two p values



miss jet clustering

usual jet pairing algorithm(χ^2)

minimizing $\chi^2 = \frac{(M(j_1, j_2) - M_H)^2}{\sigma_{H_1}^2} + \frac{(M(j_3, j_4) - M_H)^2}{\sigma_{H_2}^2}$ $M_H = 120\text{GeV}$ $\sigma_H = 6\text{GeV}$

	$\nu\nu\text{HH}(\nu\nu\text{bbbb})$
MC	22224
pre-selection	21391(96.2%)
$p_1 \times p_2 \times p_3 \times p_4 > 0$	19404
$p_1 \times p_2 > 0$	15500(79.9%)

probability of correct pairing

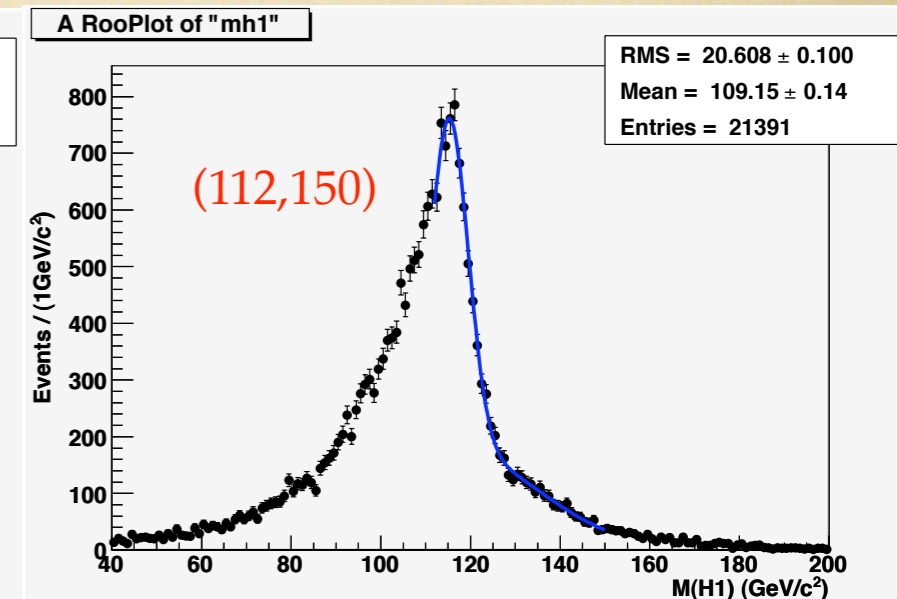
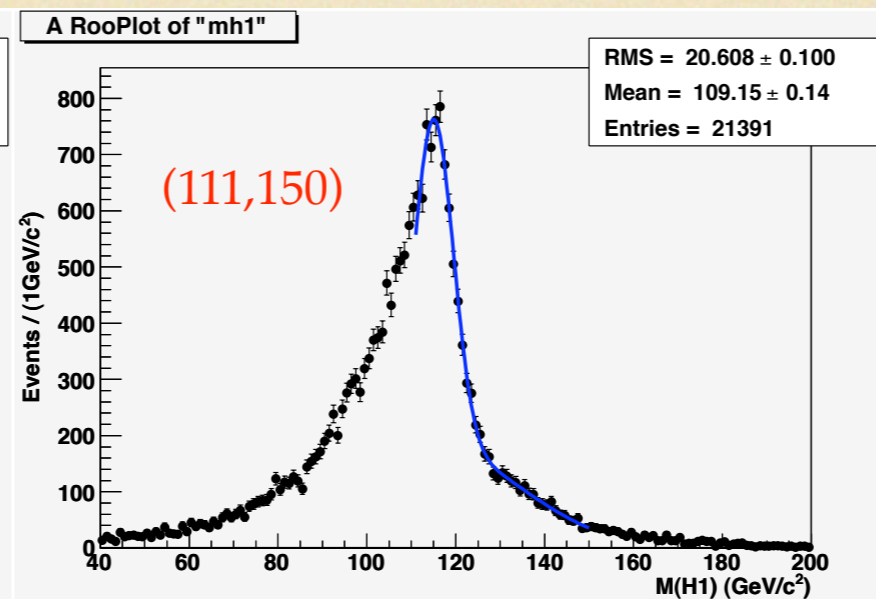
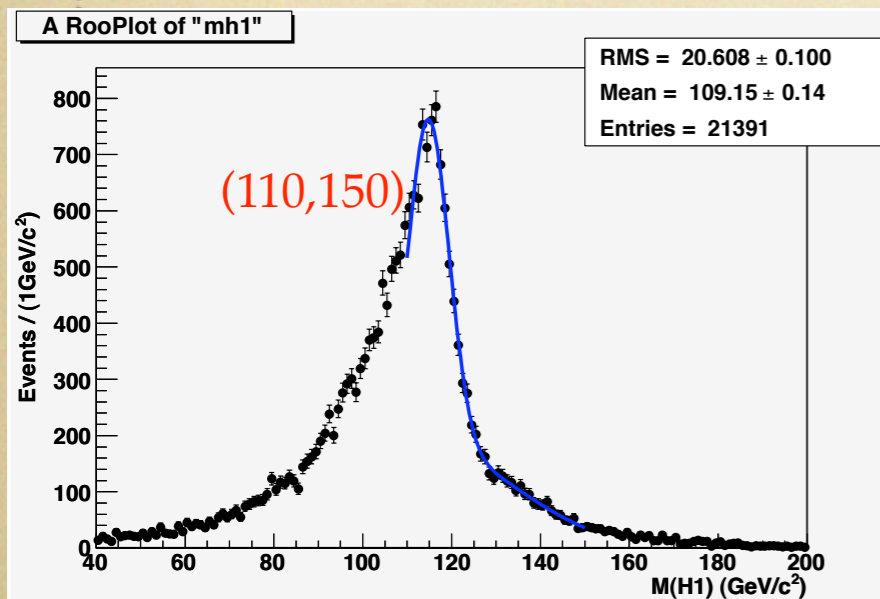
two issues:

- (i) the central value of invariant mass is not at 120 (115)
- (ii) the distribution of invariant mass is no longer a Gaussian, the resolution is not well defined, especially for resonance with natural width, like Z

Higgs mass resolution

dependence with fitting range

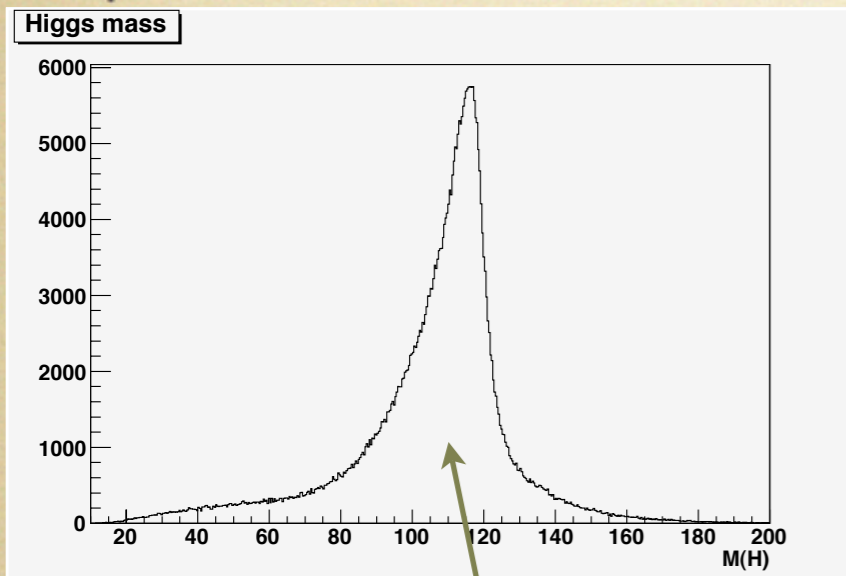
$m \pm \delta m, \sigma \pm \delta \sigma$	130	150	170
110	$114.8 \pm 0.1, 4.4 \pm 0.4$	$114.8 \pm 0.1, 4.6 \pm 0.1$	$114.7 \pm 0.1, 4.9 \pm 0.1$
111	$115.1 \pm 0.1, 3.9 \pm 0.3$	$115.0 \pm 0.1, 4.4 \pm 0.1$	$115.0 \pm 0.2, 4.8 \pm 0.2$
112	$115.3 \pm 0.1, 3.5 \pm 0.3$	$115.3 \pm 0.2, 4.2 \pm 0.2$	$115.1 \pm 0.2, 4.7 \pm 0.2$



a new jet pairing algorithm(likelihood)

- (i) estimate the p.d.f of $M(j_1, j_2)$, $M(j_3, j_4)$ in the case of correct pairing (using truth information of the four jets we can do the correct pairing): non-parametric kernel estimation
- (ii) define the likelihood of the real pairing: $L = f(M_{12})f(M_{34})$
and the corresponding χ^2 : $\chi^2 = -\ln L = -\ln(f(M_{12})) - \ln(f(M_{34}))$
- (iii) choose the pair which has the smallest χ^2

kernel estimation (binned)

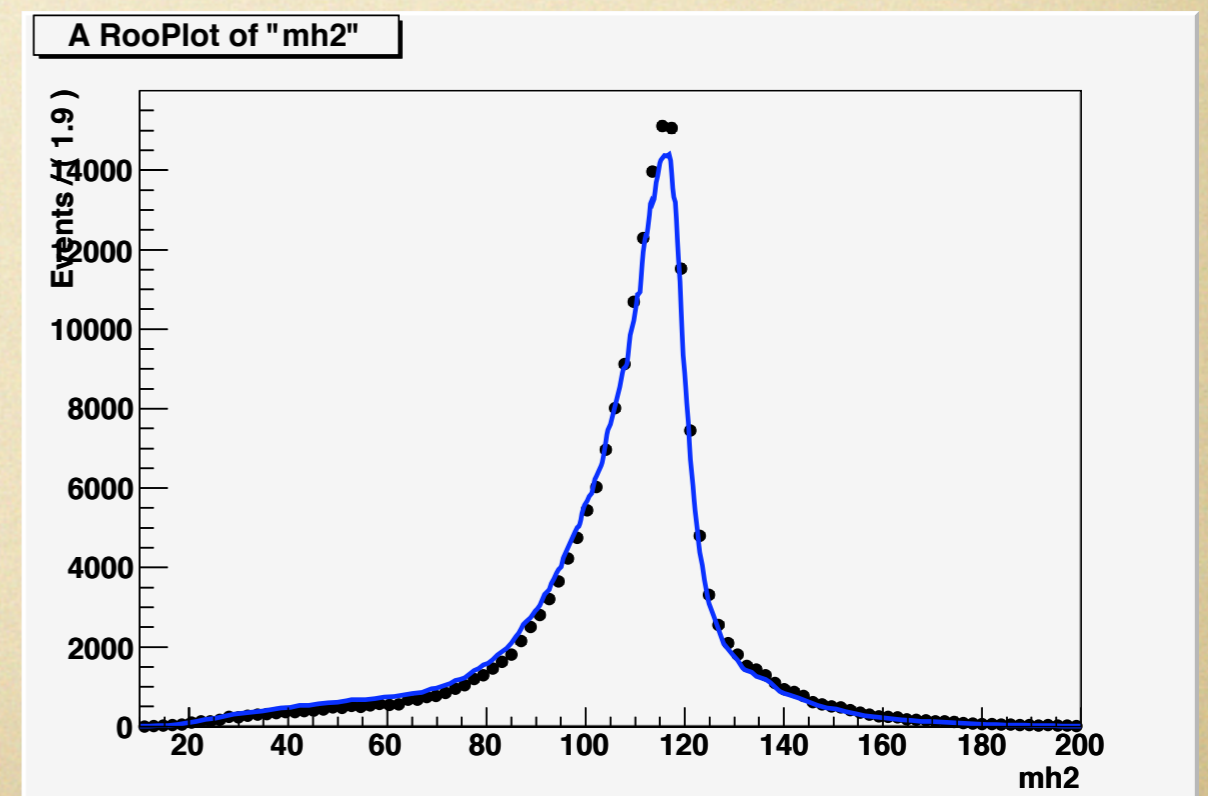
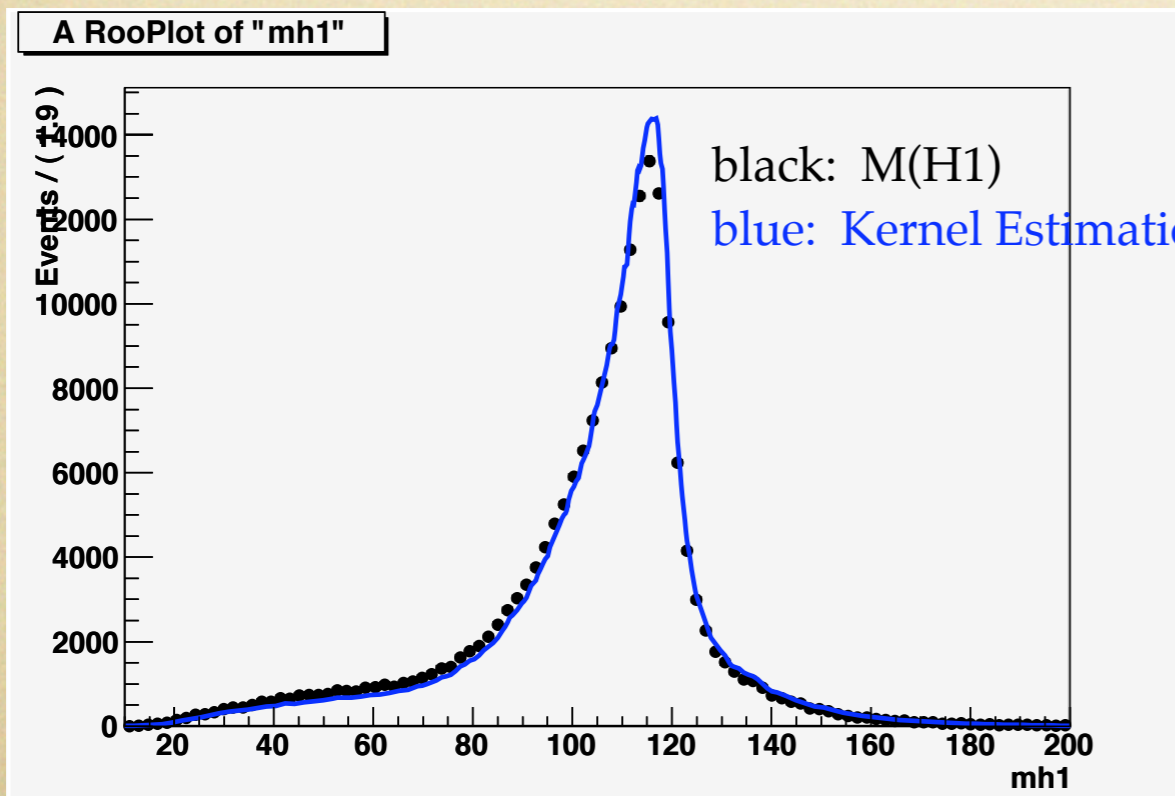


histogram of merged M(H1) and M(H2)

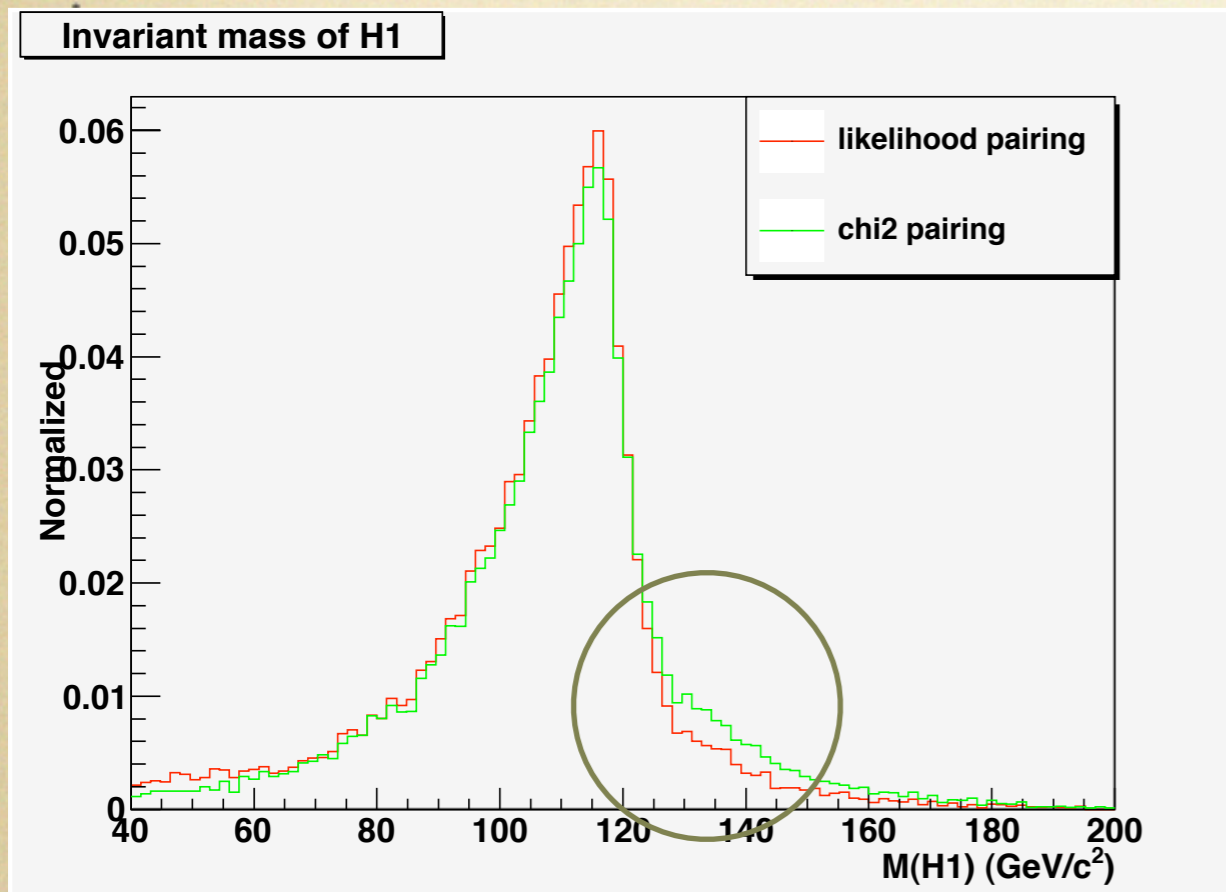
$$F(x) = \frac{1}{N} \sum_{j=1}^m n_j G(x; t_j, h_j)$$

$$h_j = \left(\frac{4}{3}\right)^{1/5} N^{-1/5} \Delta x \sqrt{\frac{N}{n_j}}$$

- N : total number of events
- n_j : number of events in that bin
- m: number of bins
- Δx : bin width
- t_j : center of that bin
- h_j : resolution of that bin
- $G(x; t_j, h_j)$: Gaussian Kernel



comparison of two jet pairing algorithms



$\nu\nu\text{HH}(\nu\nu\text{bbbb})$	χ^2	likelihood
MC	22224	222246
pre-selection	21391(96.2%)	21446
$p1 \times p2 \times p3 \times p4 > 0$	19404	19449
$p1 \times p2 > 0$	15500(79.9%)	16629(85.4%)

probability of correct pairing

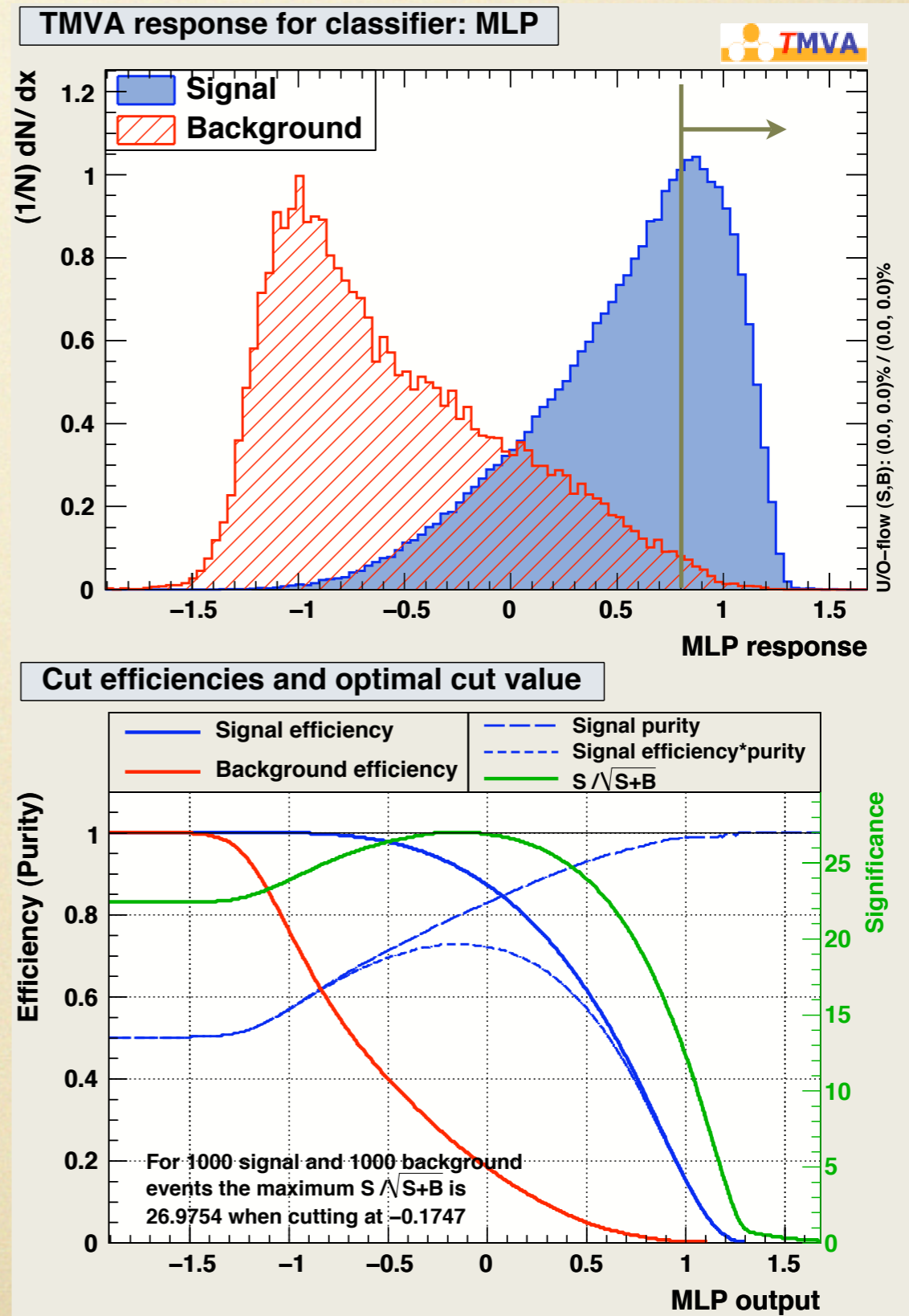
we also pair the jets under the hypothesis of $\nu\nu\text{ZZ}$ and $\nu\nu\text{ZH}$. the invariant masses of Z and H in each hypothesis also could be used to suppress the backgrounds.

suppression of tt-bar

input:

- M(H1)
- M(H2)
- Y value
- Miss Pt
- Cosθ(hh)
- Npart4

	$\nu\nu HH(\nu\nu bbbb)$	tt-bar
MC	500K	500K
expected	142.6(63.4)	377600
pre-selection	115.8(61.1)	160971
Evis<600	110.8(58.3)	32326



suppression of $\nu\nu ZZ$ and $\nu\nu ZH$

input:

M(Z1) $_{\nu\nu ZZ}$

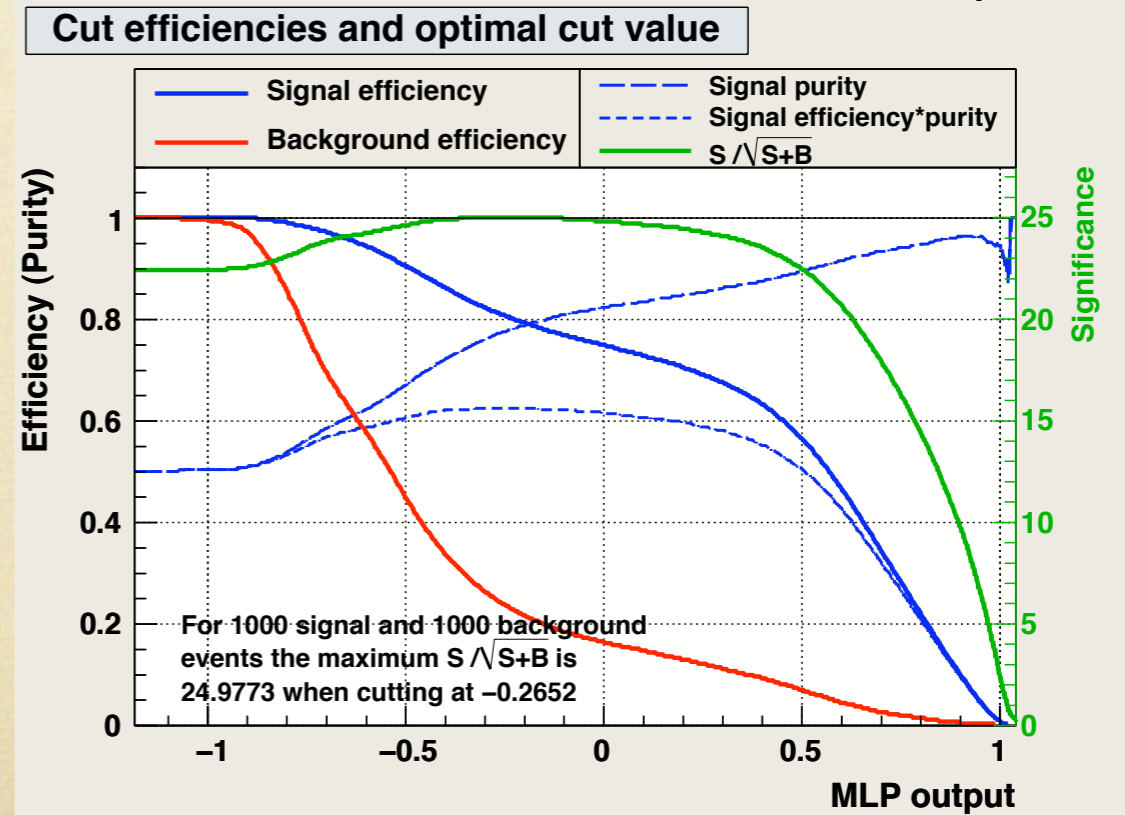
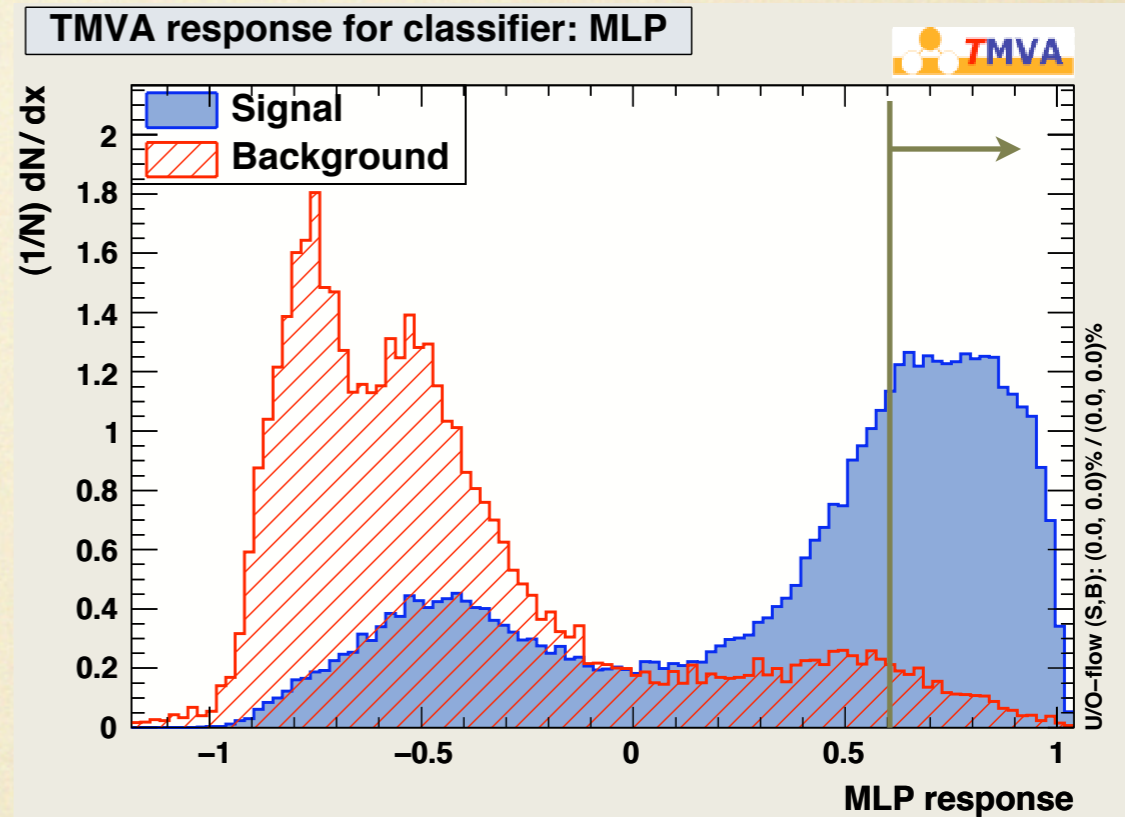
M(Z2) $_{\nu\nu ZZ}$

M(Z) $_{\nu\nu ZH}$

M(H) $_{\nu\nu ZH}$

decay angles of H1 and H2

	$\nu\nu HH$ ($\nu\nu bbb$)	$\nu\nu ZZ$	$\nu\nu ZH$
MC	500K	500K	500K
expected	142.6(63.4)	12100	2500
pre-selection	115.8(61.1)	6112	1620
Evis<600	110.8(58.3)	5932	1548
mvatt>0.8	33.0(20.7)	140.0	159.8



preliminary results

no beam polarization

$$E_{\text{cm}} = 1000\text{GeV}, M_H = 120\text{GeV}$$

$$\int Ldt = 2\text{ab}^{-1}$$

	$\nu\nu\text{HH}(\nu\nu\text{bbbb})$	tt-bar	WWZ	ZZZ	ZZH	$\nu\nu\text{ZZ}$	$\nu\nu\text{WW}$	ttH	$\nu\nu\text{ZH}$
MC	500K	500K	500K	500K	500K	500K	50K	50K	500K
expected	142.6(63.4)	377600	123400	1664	700	12100	14048	4960	2500
pre-selection	115.8(61.1)	160971	27772	609.2	239.7	6112	13626	184.3	1620
Evis<600	110.8(58.3)	32326	11512	330.2	134.8	5932	171.5	89.2	1548
mvatt>0.8	33.0(20.7)	376.8	57.5	1.95	2.42	140.0	4.83	2.38	159.8
mvazzzh>0.6	20.6(12.8)	182.8	17.0	0.45	0.60	6.32	0	1.78	22.0
noff4>0 noff3>2	6.17(5.8)	3.78	0	0.02	0.05	0.36	0	0.40	2.16
mjet4>2 econe>0.1	5.95(5.62)	1.51	0	0.02	0.04	0.36	0	0.20	2.04

summary

$\nu\nu HH$: 5.9

tt -bar: 3.9

i. excess significance: 2.5σ

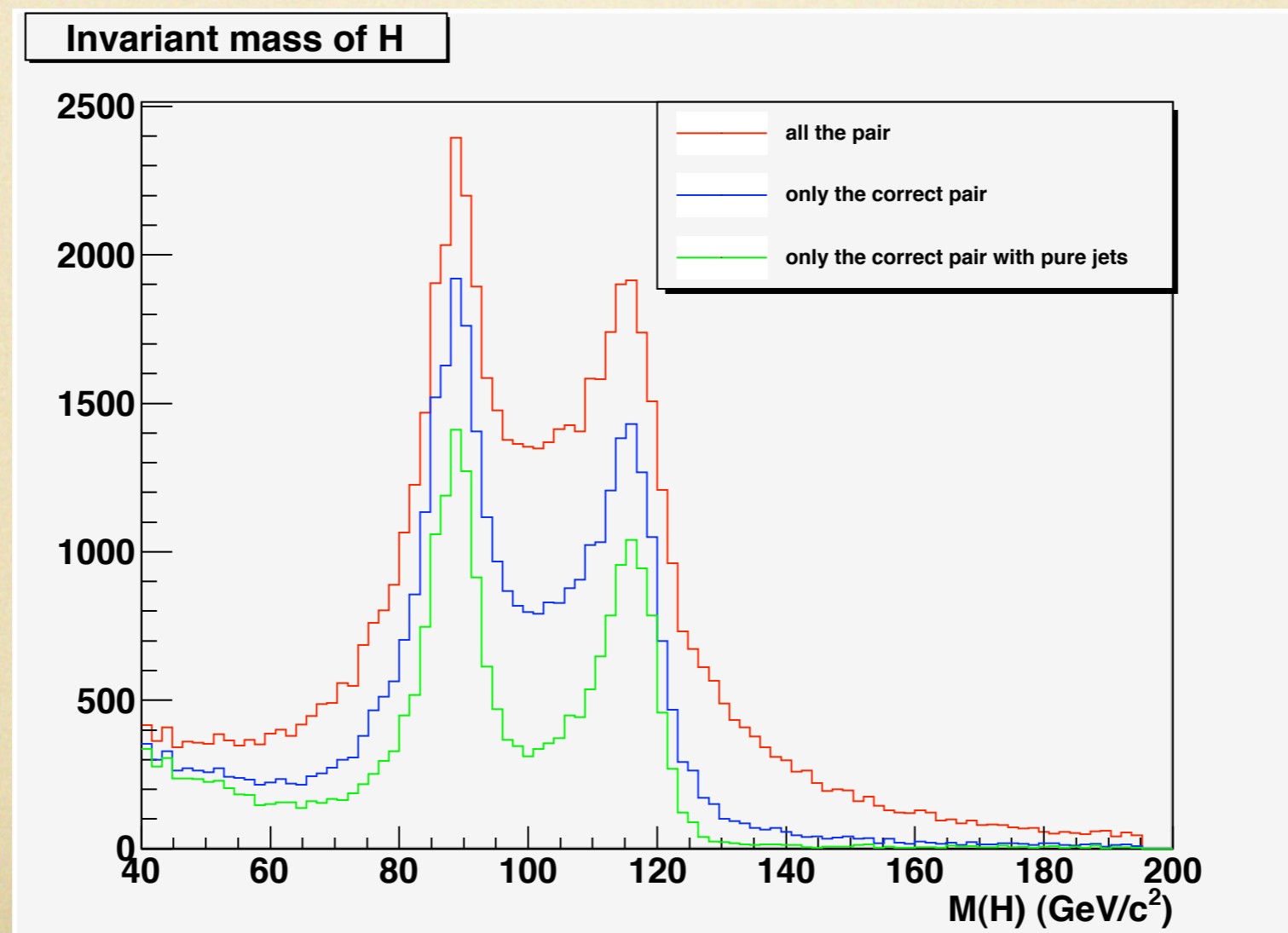
ii. precision for Higgs self-coupling: 45%

back up

$\mu\mu ZH$ background

sources of contamination:

- (i) mass resolution
- (ii) pair combination
- (iii) jet clustering



invariant mass of each jet

