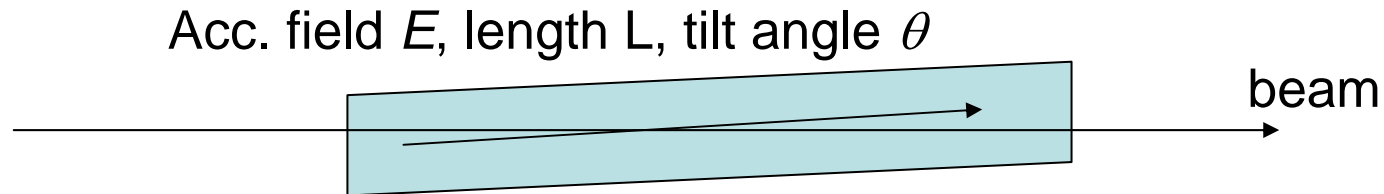


# On Cavity Tilt + Gradient Change

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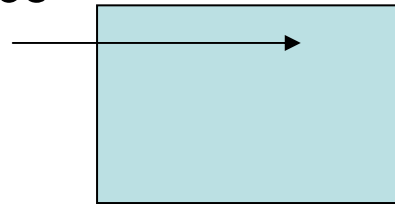
# Transverse effect of acc. field with cavity tilt



Transverse kick in the cavity:  $\Delta p_t = \sin \theta eV$

Edge (de)focus

entrance



offset:  $y_0 + L \sin \theta / 2$

exit



offset:  $y_0 - L \sin \theta / 2$

Transverse kick at the entrance:  $\Delta p_t = -eE (y_0 + \sin \theta L/2)/2$

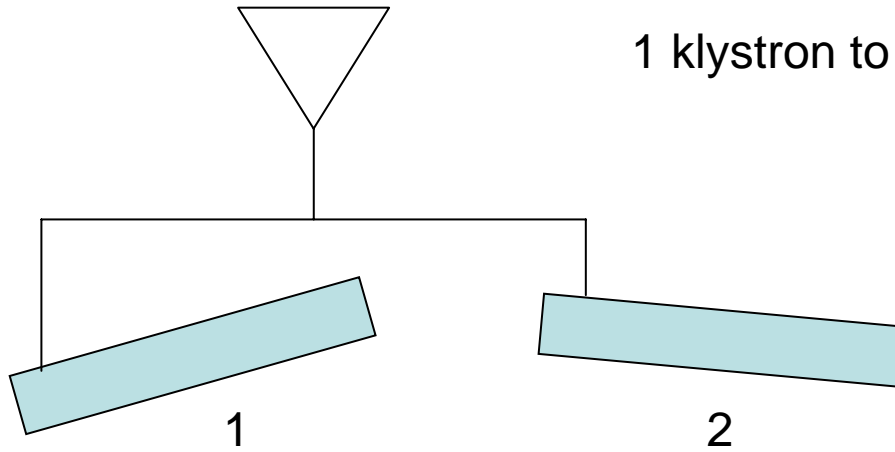
Transverse kick at the exit:  $\Delta p_t = eE (y_0 - \sin \theta L/2)/2$

→ Total transverse kick by the cavity:  $\Delta p_t = \sin \theta eV/2$

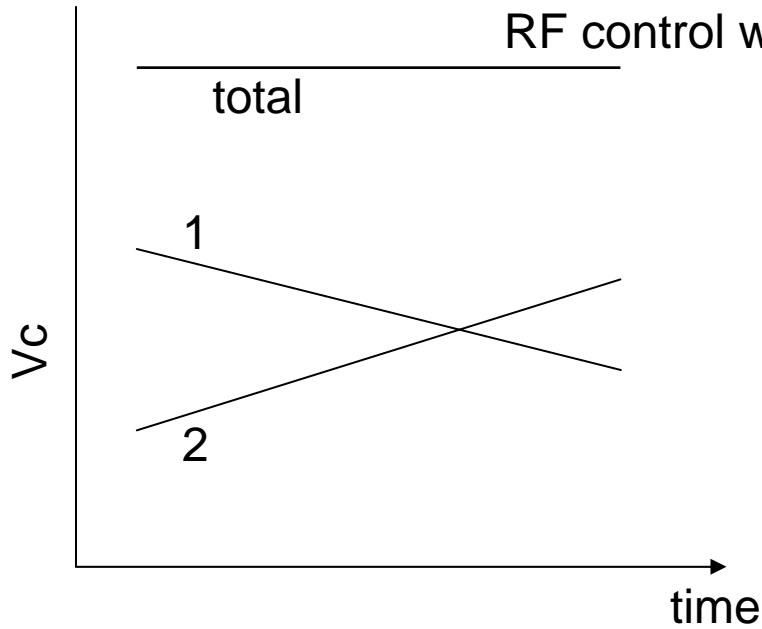
# Cavity tilt change (vibration) and Fixed cavity tilt + voltage change have the same effect

- 3 micro-rad. tilt angle change, cavity to cavity random
  - 0.8-sigma orbit change at the end of main linac
    - $\propto$  tilt change
  - 0.5 nm (2.5%) emittance growth
    - $\propto$  (tilt change)<sup>2</sup>
- Assuming fixed tilt angle (misalignment) RMS 300 micro-rad. 1% voltage change, cavity to cavity random
  - Same as above.
    - RF control stabilizes vector sum, not voltage of each cavity.
    - Cavities with different coupling, fed by one RF source.
      - voltage change during one pulse.
    - Different detuning (pulse to pulse)
      - pulse to pulse voltage change

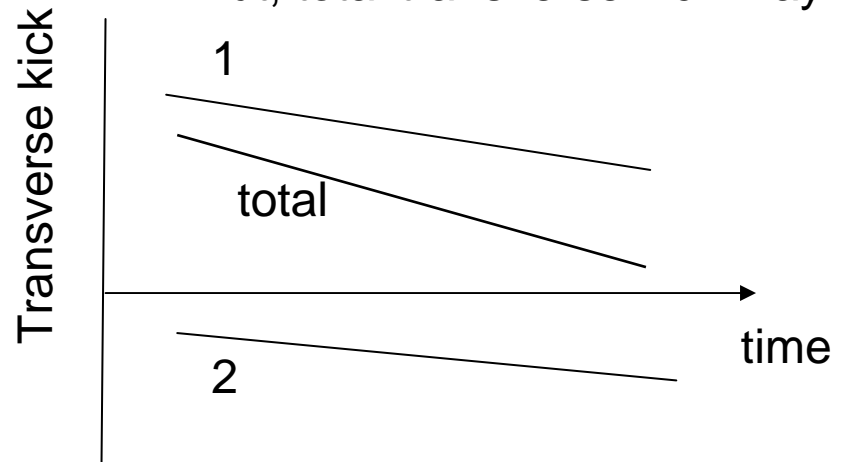
1 klystron to 2 cavities



RF control will keep total voltage flat.



But, total transverse kick may change.



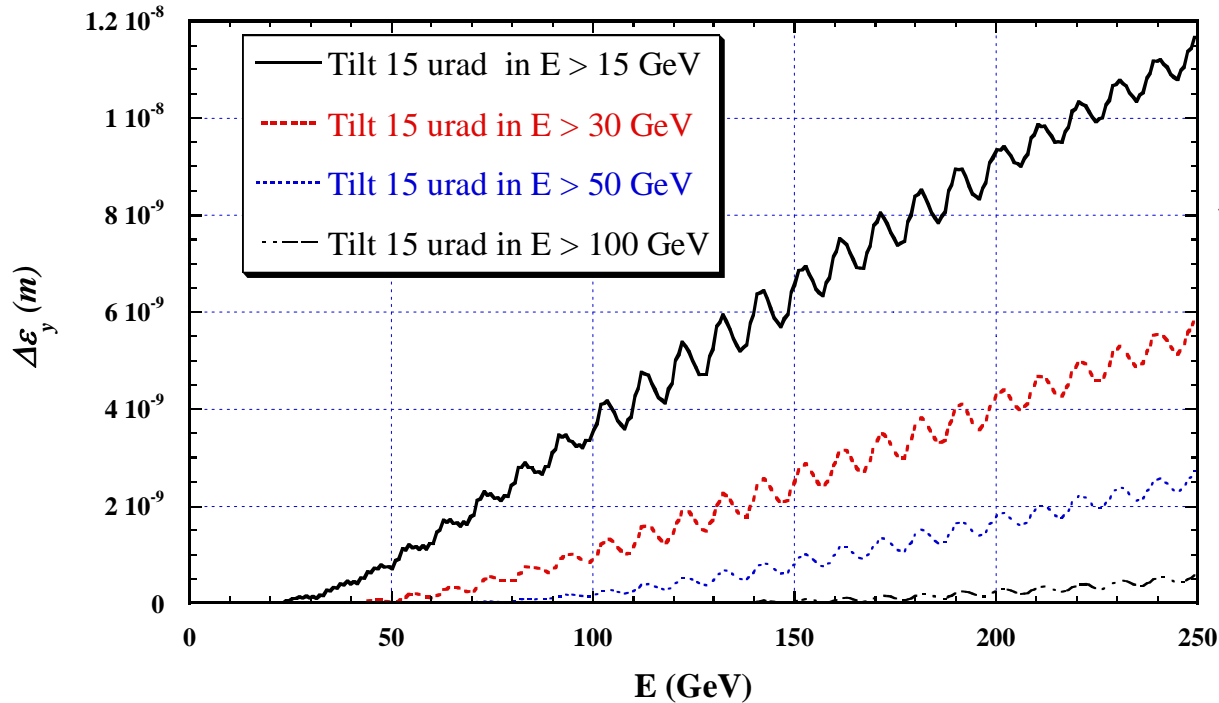
# Orbit jitter sources in ML

Source	Assumption (Tolerance?)	Induced orbit jitter	Induced emittance growth
Quad vibration (offset change)	100 nm	1.5 sigma	0.2 nm
Quad+steering strength jitter	1E-4	1 sigma	0.1 nm
Cavity tilt change	3 urad	0.8 sigma	0.5 nm
<b>Cavity to cavity strength change, assuming 300 urad fixed tilt</b>	<b>1%</b> <b>Too tight !</b>	<b>0.8 sigma</b>	<b>0.5 nm</b>

Tolerances, tolerable timescale depend on feedback performance.

# Result of simulation

Cavity tilt change 15 urad, equivalent to Fixed 300 urad + 5% gradient change (numbers are RMS)



$$\Delta\gamma\varepsilon \propto [\ln(E/E_0)]^3$$

Starting linac at different energies (to see effectiveness of orbit correction)

E.g. if orbit is corrected at 50 GeV, emittance growth will be

~ 1 nm from 15 to 50 GeV plus ~ 2.5 nm from 50 to 250 GeV

Total 3.5 nm, instead of 11 nm without such correction.

# Summary

- Fast change of tilt should be  $< 3$  urad (this looks easy?)
- (Fixed tilt)  $\times$  (Relative gradient change of each cavity) should be  $< 3$  urad (looks tight)
  - If gradient change is same for all pulses (predictable), orbit in one pulse may be corrected in the linac. Then the tolerance will be loosened. Probably about 15 urad.
  - Pulse to pulse different change can not be corrected.
- We assume fixed cavity tilt 300 urad

As conclusion, roughly, gradient of each cavity flatness in a pulse should be less than

- 1% for pulse to pulse different
- 5 % for predictable [If we can straighten a train at certain locations in the linac.]

# Discussion + comment

- Feedback in each pulse will loosen the tolerance of pulse to pulse change? (suggested by Yokoya and Ross)
- Measure orbit of head part of pulse and correct following part.
    - Voltage change of each cavity during a beam pulse should be a simple function of time. (Can following voltage change be predicted from voltage of head part?)
    - It looks difficult. But may be able to correct partially ???
  - Gradient change (then, orbit change) will not be so fast.
    - Intra-pulse feedback, similar to IP feedback (but can be much slower), may be used.
    - Can feedback in ML be fast enough?