

Feasibility study of measurement of Higgs pair creation in a gamma-gamma collider

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Outline

- Motivation
- Signal & Background
- Simulation & Analysis
- Result
- Summary

T. Takahashi's talk @ IWLC2010

Summary

- We tried to see $\gamma\gamma \rightarrow HH$ in a photon collider based on TESLA optimistic parameters.
- gg CM energy of 270GeV is optimum for $m_h = 120\text{GeV}$
- backgrounds
 - $\gamma\gamma \rightarrow WW$ has 10^6 times larger cross section
 - $\gamma\gamma \rightarrow ZZ$ has 10^3 times larger cross section
- It seems possible to suppress backgrounds with improved jet clustering technique.
 - statistical significance of 4.6 expected for WW and ZZ cut with perfect jet clustering
- more to do
 - optimize NN training
 - study jet clustering improvement
 - $\gamma\gamma \rightarrow bbbb$ background
 - we believe it is small for dangerous
 - higher Higgs mass

My talk is including these topics.

Motivation

Final goal : measuring Higgs self-coupling constant λ

$$\lambda = \lambda^{SM} (1 + \delta\kappa)$$

Higgs self-coupling constant
in the SM

deviation parameter
from the SM

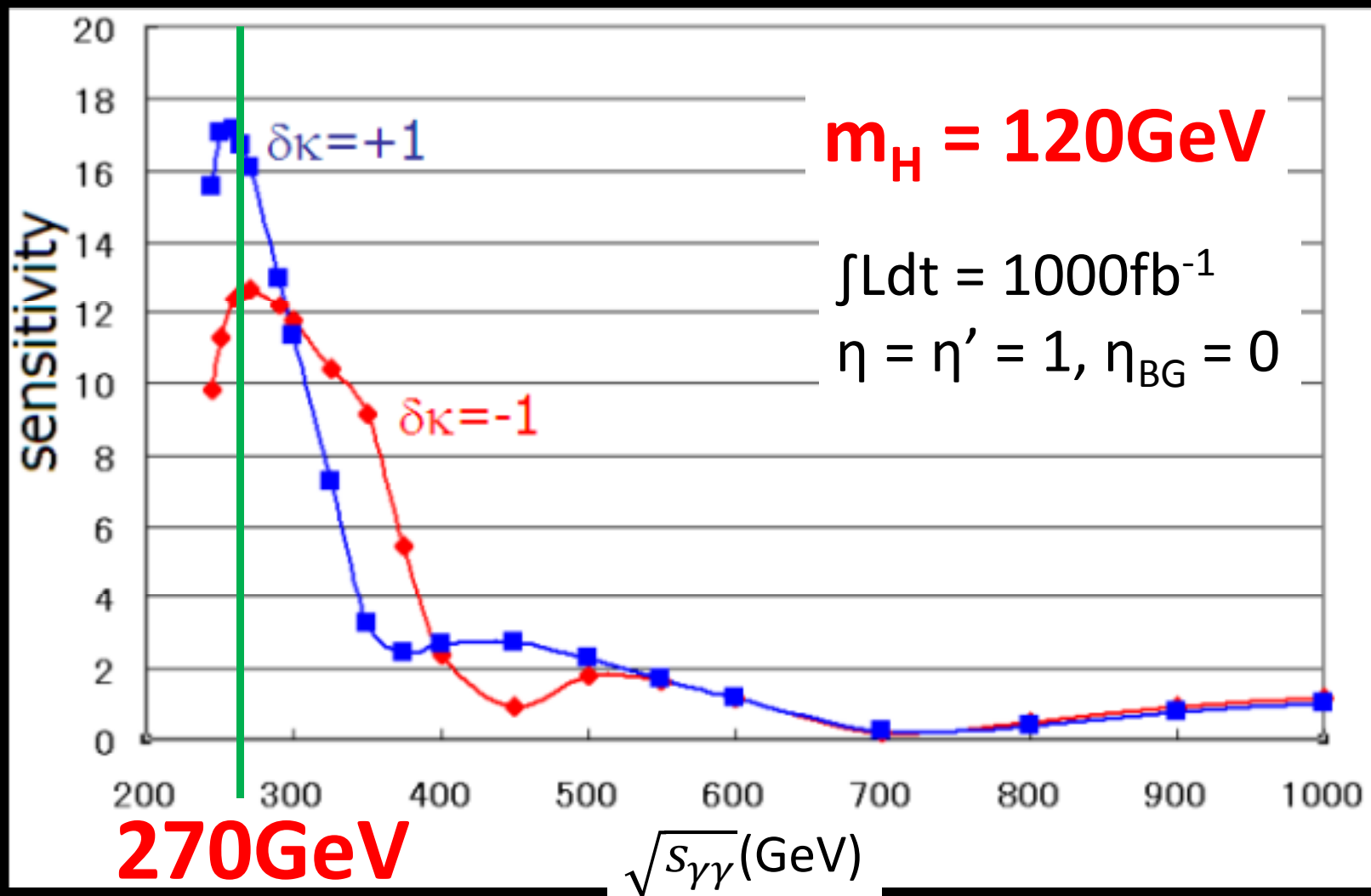
Before the final goal...



We have to investigate the feasibility of
measurement of Higgs pair creation in a PLC.

Optimizing collision energy

$$\text{sensitivity} \equiv \frac{|N(\delta\kappa) - N_{SM}|}{\sqrt{N_{obs}}} = \frac{L|\eta\sigma(\delta\kappa) - \eta'\sigma_{SM}|}{\sqrt{L(\eta\sigma(\delta\kappa) + \eta_{BG}\sigma_{BG})}}$$



Beam parameters

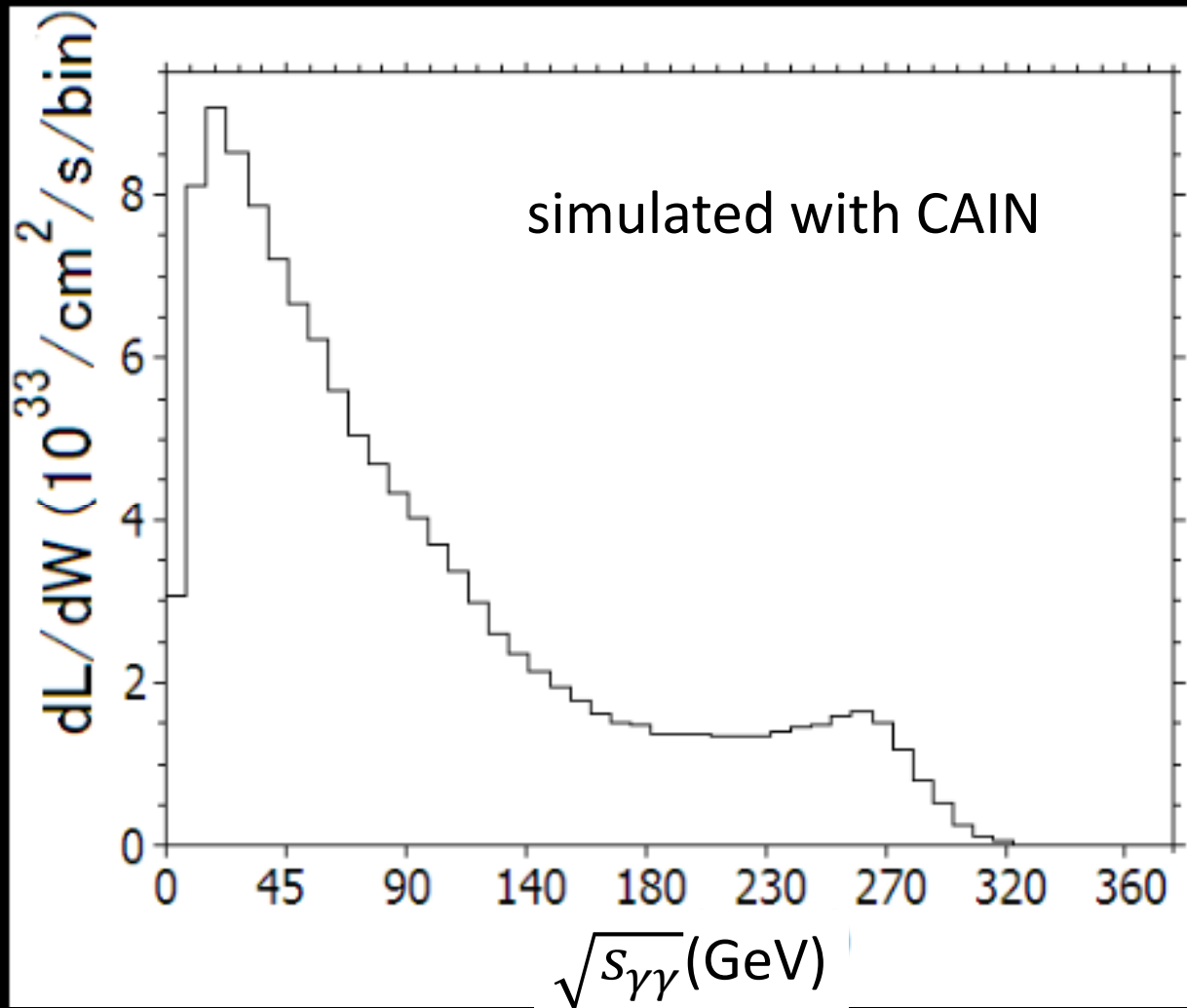
	x3.76	x4.8
E_e (GeV)	210	195
$n(10^{10})$	2	2
σ_z (mm)	0.35	0.35
$\gamma\epsilon_{x/y}$ (mrad)	2.5/0.03	2.5/0.03
$\beta_{x/y}$ (mm) @ IP	1.5/0.3	1.5/0.3
$\sigma_{x/y}$ (nm)	96/4.7	99/5.5
λ_L (nm)	1054	770
$x = 4\omega E_e/m_e^2$	3.76	4.8
Pulse Energy(J)	10	10
$L_{\text{geo}}(e-e-)[10^{34}\text{cm}^{-2}\text{s}^{-1}]$	8.7	8.1
$L_{\text{peak}}(\gamma\gamma)[10^{34}\text{cm}^{-2}\text{s}^{-1}]$	1.2	0.7
$L_{\text{tot}}(\gamma\gamma) [10^{34}\text{cm}^{-2}\text{s}^{-1}]$	12.6	5.88

based on
TESLA optimistic
parameter

x=3.76

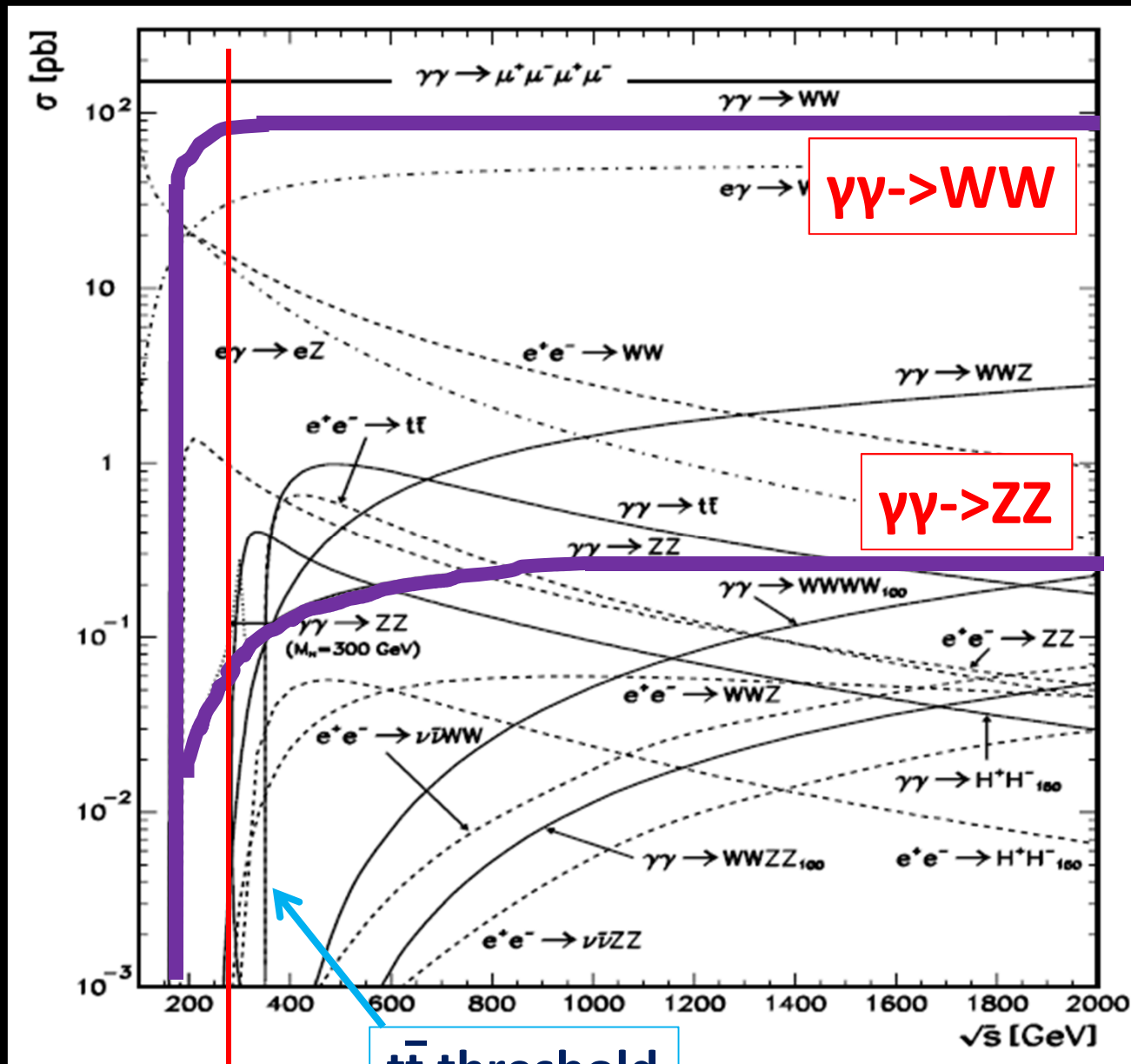
in this study

Luminosity distribution



$$L(/\text{year}) \int \sigma(W_{\gamma\gamma}) \frac{dL}{dW_{\gamma\gamma}} dW_{\gamma\gamma} = \mathbf{16 \text{ events/year}}$$

Signal & Backgrounds



270GeV

$t\bar{t}$ threshold

of events

$$N_{events} = L(/year) \int \sigma(W_{\gamma\gamma}) \frac{dL}{dW_{\gamma\gamma}} dW_{\gamma\gamma}$$

Signal

$\gamma\gamma \rightarrow HH$: 16 events/year

Main backgrounds

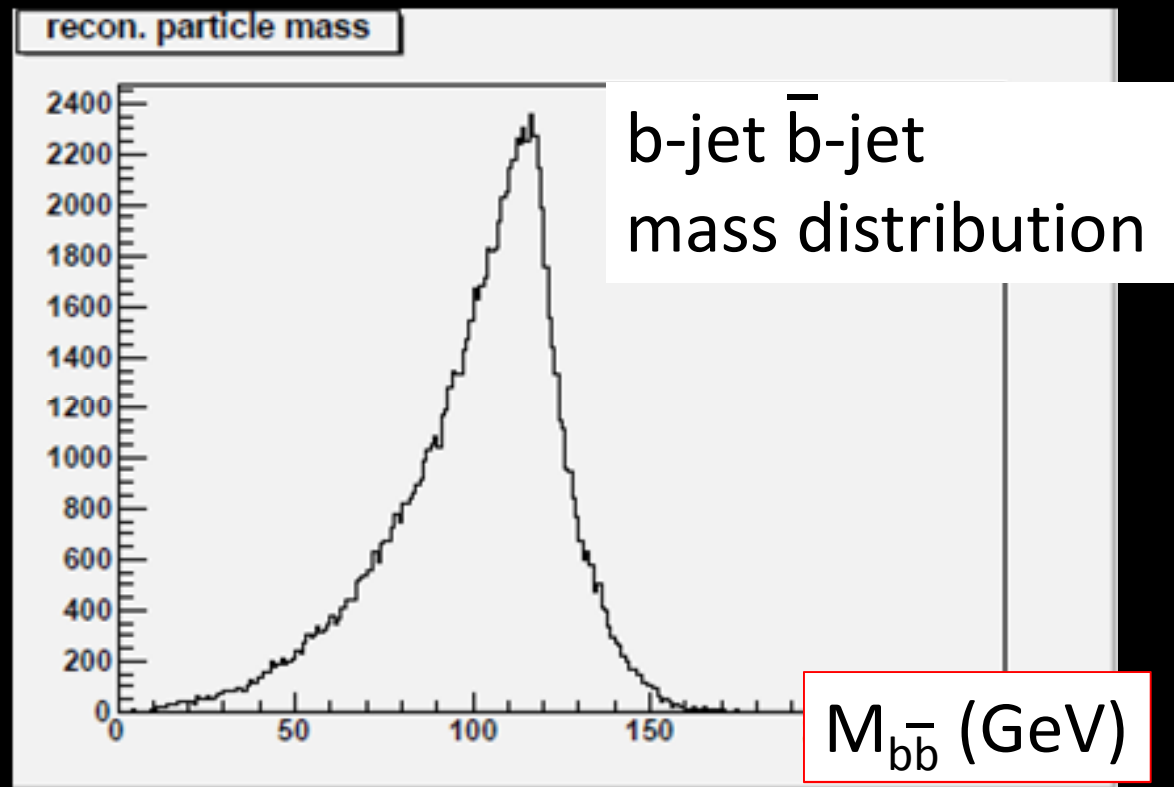
$\gamma\gamma \rightarrow WW$: $1.462 * 10^7$ events/year

$\gamma\gamma \rightarrow ZZ$: $1.187 * 10^4$ events/year

$\gamma\gamma \rightarrow 4b$: $1.37 * 10^5$ events/year

Event signature (1)

- $\gamma\gamma \rightarrow HH$
 - $HH \rightarrow 4b$
 - $M_{b\bar{b}} = M_H (120\text{GeV})$



Event signature (2)

- $\gamma\gamma \rightarrow WW$
 - $\sigma_{\gamma\gamma \rightarrow WW} \sim 10^6 \sigma_{\gamma\gamma \rightarrow HH}$
 - suppressed by b-tagging
- $\gamma\gamma \rightarrow ZZ$
 - $ZZ \rightarrow 4b$ same as $HH \rightarrow 4b$
 - discriminate only by mass difference
- $\gamma\gamma \rightarrow 4b$
 - Mass distribution is different from signal, but still have events near signal region ($\sim 120\text{GeV}$).
 - Angular distribution is different from signal.

Simulation & Analysis

1. Event generation & Detector simulation

2. Event reconstruction

1. jet clustering

2. b-tagging

- n_{sig} method

3. jet pairing

3. Event selection

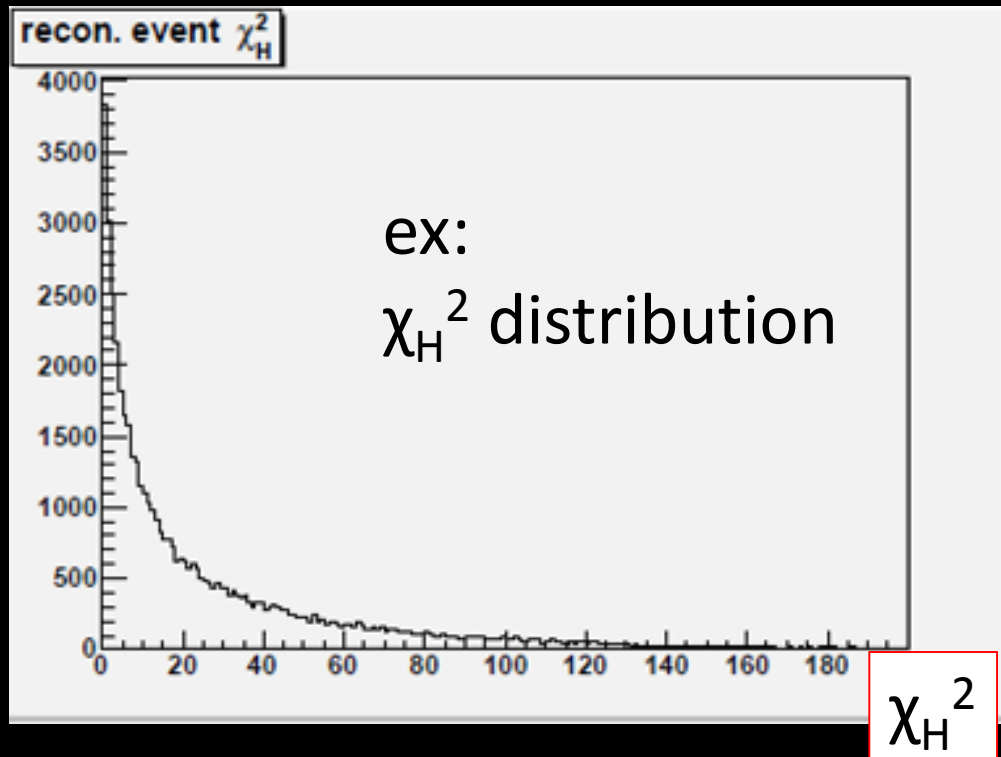
1. pre-selection

2. Neural Network (NN)

Event reconstruction (1)

information of mass

$$\chi_i^2 = \frac{(M_1 - M_i)^2}{\sigma_{2j}^2} + \frac{(M_2 - M_i)^2}{\sigma_{2j}^2}$$

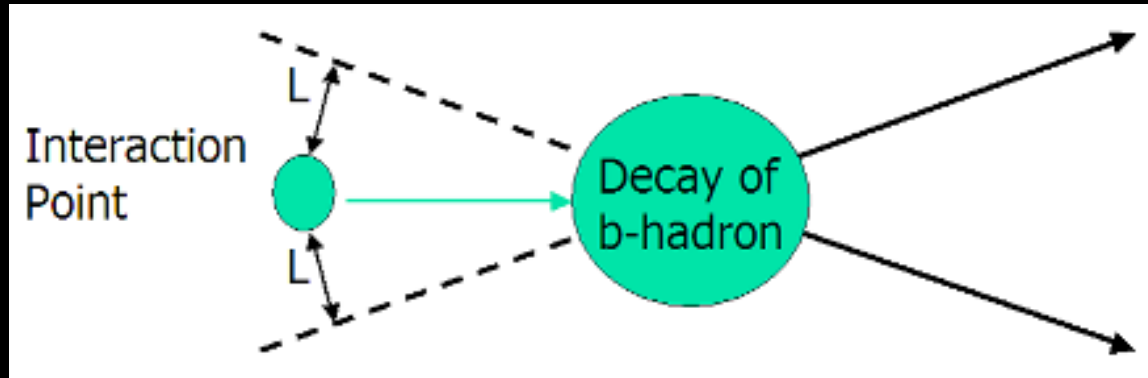


M_1, M_2 : reconstructed mass
 i : H, W, Z, $b\bar{b}$
 σ_{2j} : mass resolution

Event reconstruction (2) --- b-tagging

n_{sig} method

$$\frac{L}{\sigma_L} \geq n_{sig}$$



When there are n_{offv} tracks which satisfy this equation, we regarded this quark as a b-quark.

relatively simple b-tagging method

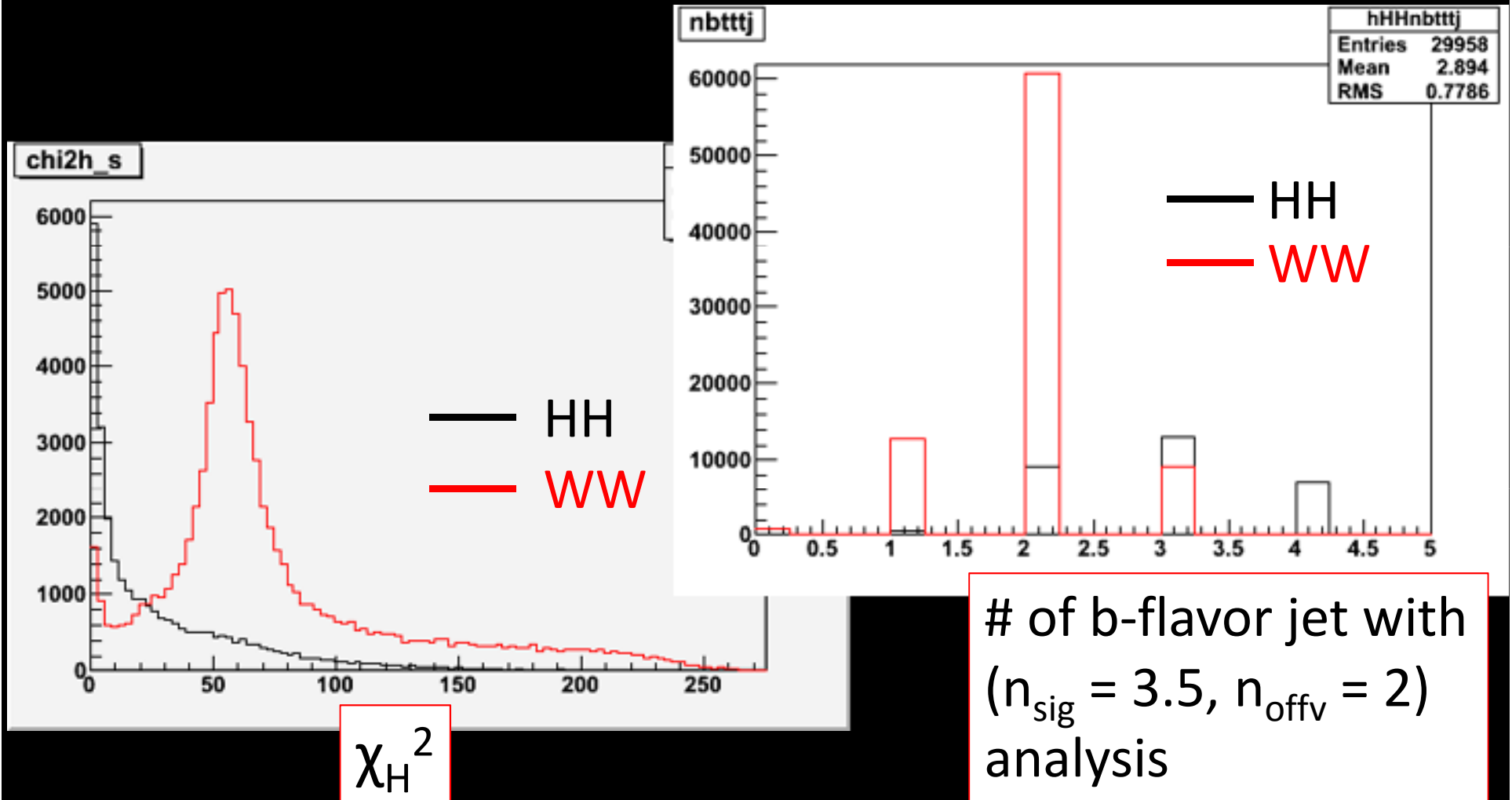
➡ can be improved by further study

Event selection by Neural Network (NN)

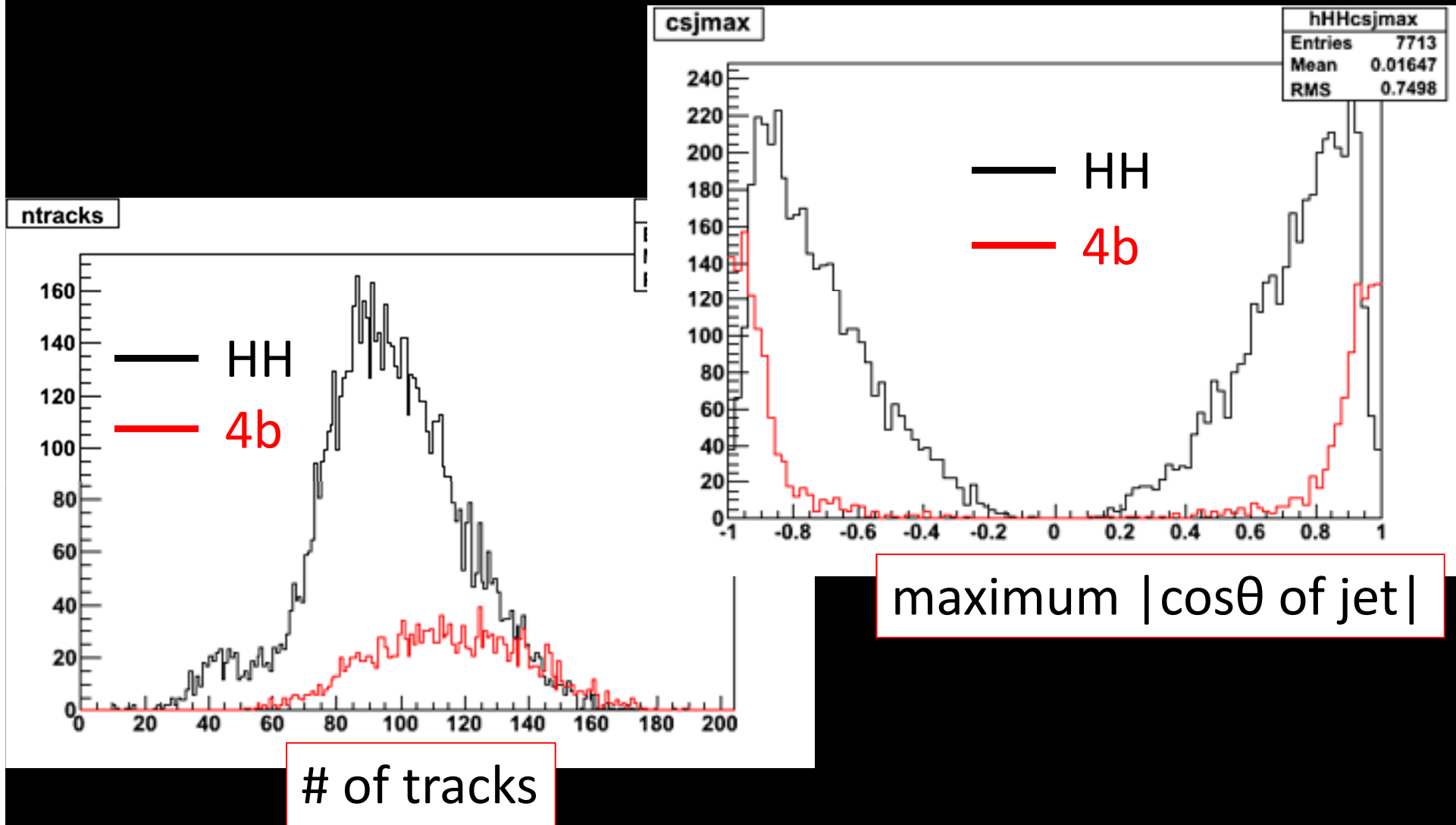
- 3 steps
 1. W filter
 2. 4b filter
 3. Z filter
- Maximize statistical significance

$$\text{significance} \equiv \frac{N_{\text{signal}}}{\sqrt{N_{\text{signal}} + N_{\text{BG}}}} \quad N : \# \text{ of events}$$

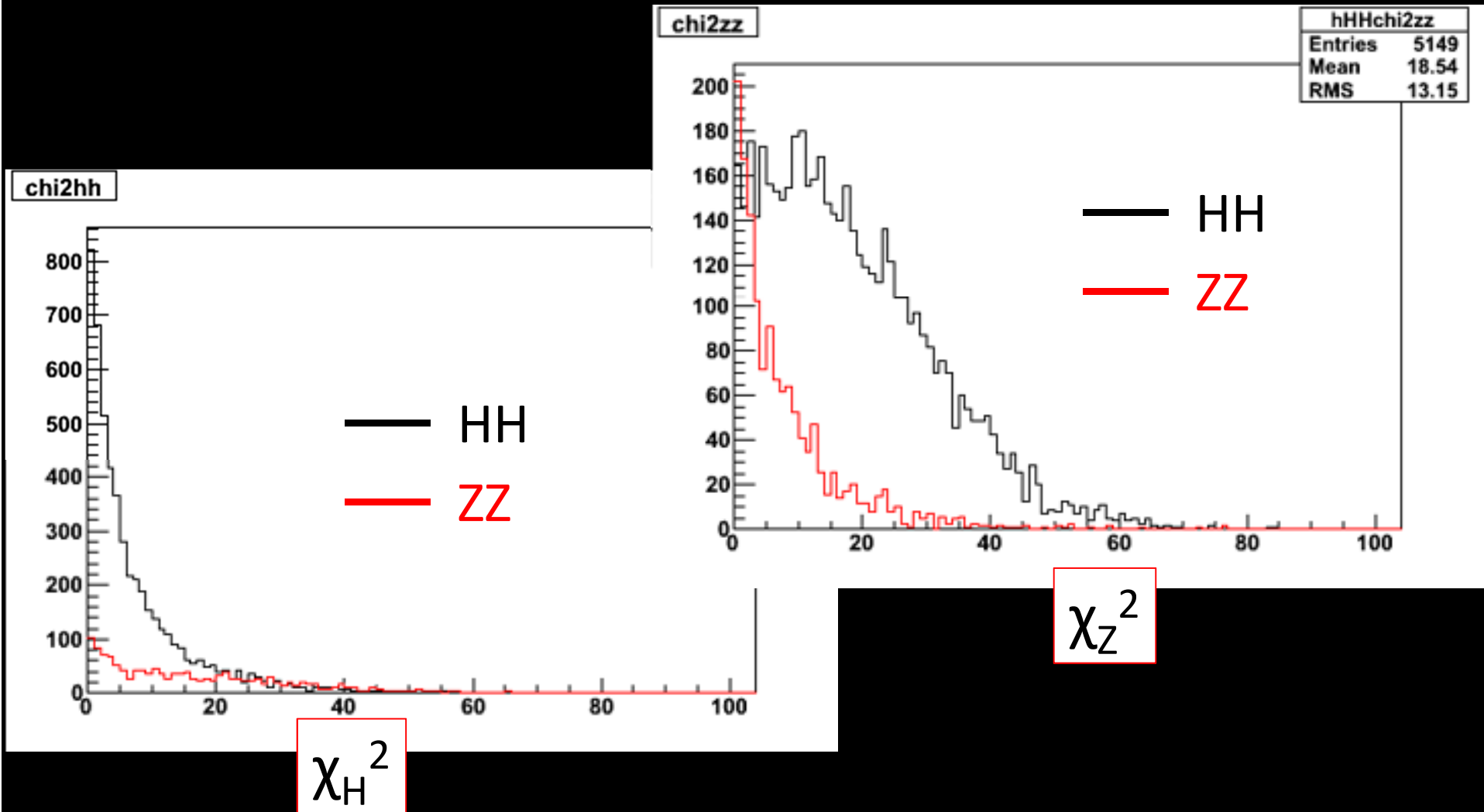
Distribution of NN inputs --- WW



Distribution of NN inputs --- 4b



Distribution of NN inputs --- ZZ



Cut summary

	HH	WW	ZZ	4b
expected events (# of MC samples)	80 (50000)	73100000 (750000000)	59350 (10000000)	293600 (10000000)
pre-selection	47.93 (29958)	81655 (83777)	5167 (87057)	84491 (287776)
W filter	12.34 (7713)	8.772 (9)	193.4 (3259)	568.4 (1936)
4b filter	8.238 (5149)	0 (0)	84.40 (1422)	13.21 (45)
Z filter	4.994 (3121)	0 (0)	7.359 (124)	5.872 (20)

$$\text{significance} = \frac{N_{\text{signal}}}{\sqrt{N_{\text{signal}} + N_{\text{BG}}}} = 1.17$$

Further improvement

- **WW BG : almost completely suppressed!**
- **4b & ZZ BG remained**
- Possible improvement --- **jet clustering**

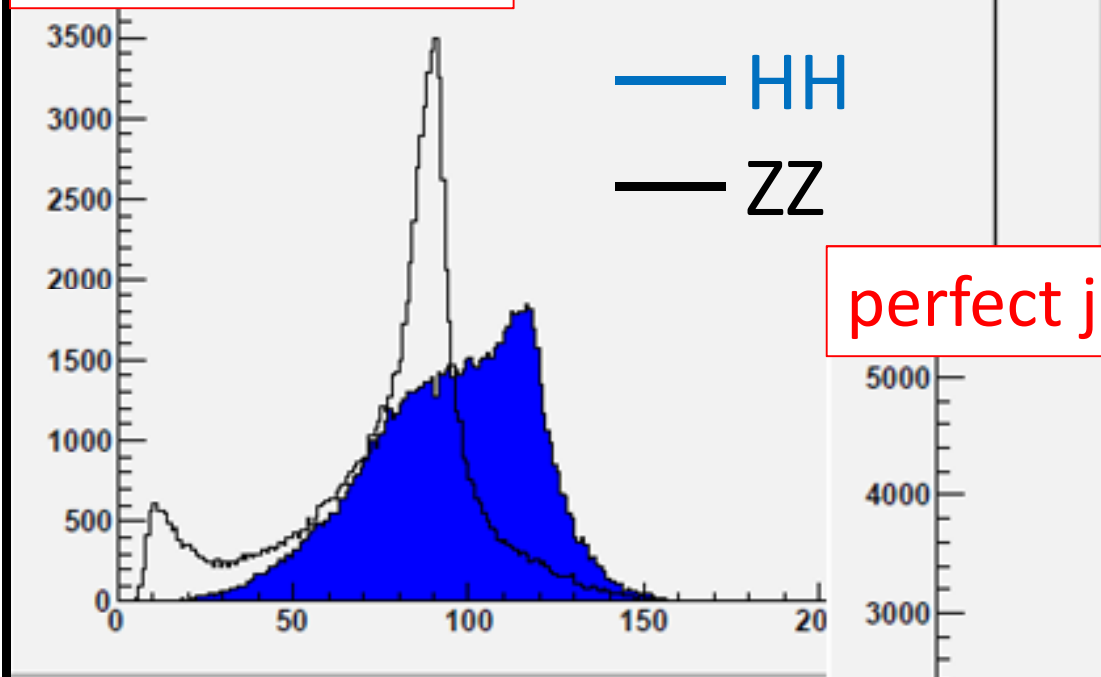
correct color singlet information

 improve mass resolution, b-tagging efficiency

We investigated using generator information for HH, WW, ZZ (not for 4b).

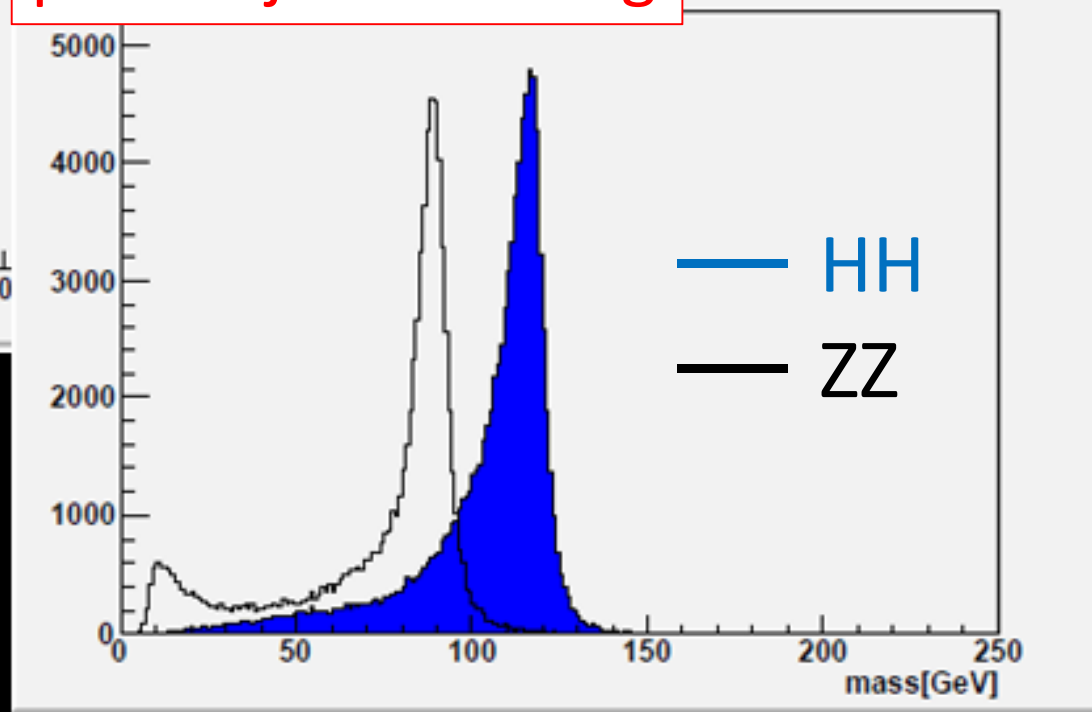
Improve mass resolution

JADE clustering



Ex:
mass distribution of
HH & ZZ BG

perfect jet clustering



Cut summary with perfect jet clustering

	HH	WW	ZZ	4b
expected events (# of MC samples)	80 (50000)	73100000 (75000000)	59350 (1000000)	293600 (1000000)
pre-selection	46.64 (29152)	55836 (57287)	4172 (70292)	84491 (287776)
W filter	38.58 (24115)	4.873 (5)	98.84 (1667)	2179 (7422)
4b filter	34.50 (21562)	2.924 (3)	27.66 (466)	2.642 (9)
Z filter	33.06 (20662)	2.924 (3)	5.935 (100)	2.642 (9)

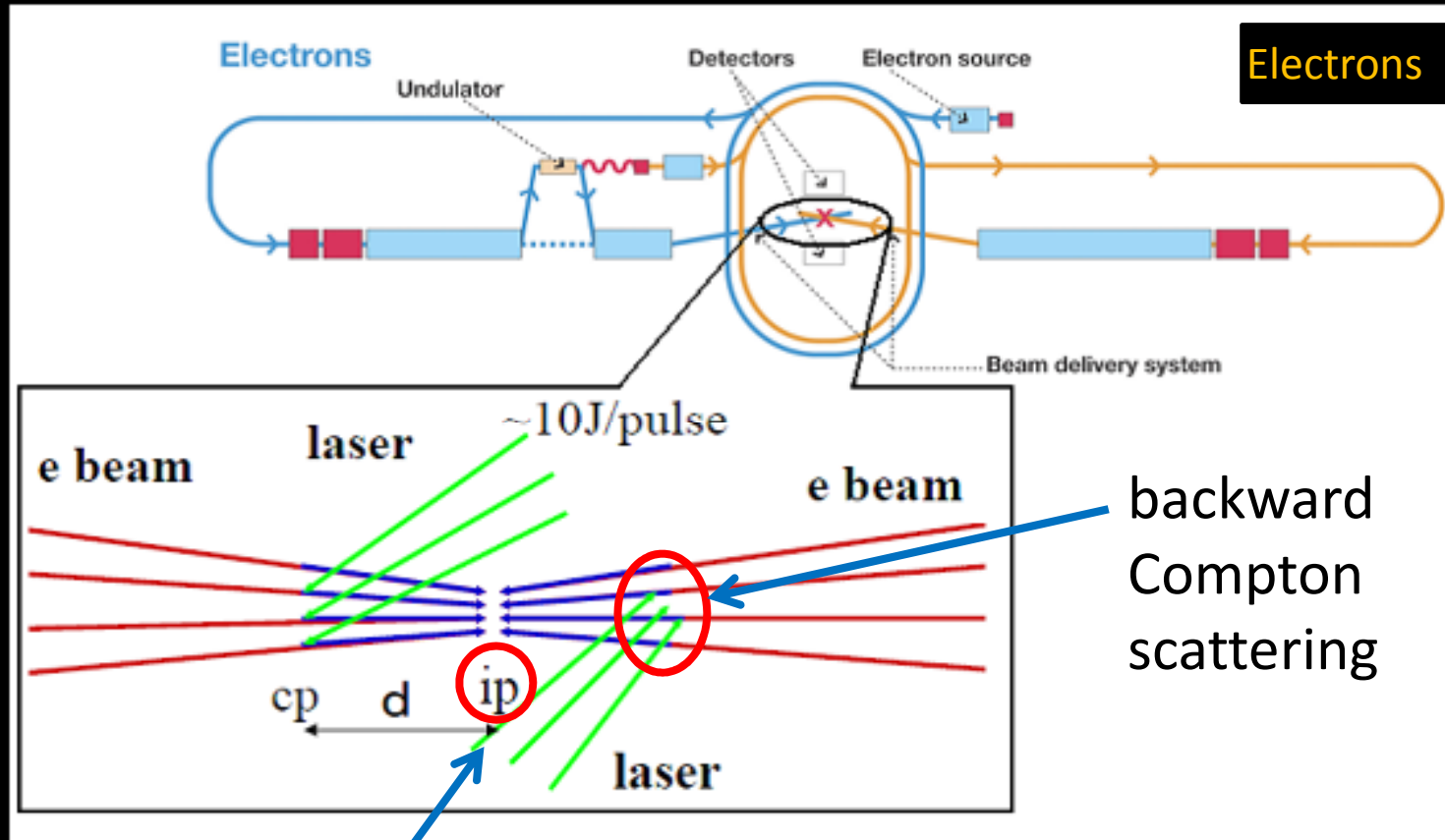
$$\text{significance} = \frac{N_{\text{signal}}}{\sqrt{N_{\text{signal}} + N_{\text{BG}}}} = 4.95$$

Summary

- We investigated $\gamma\gamma \rightarrow HH$ in a gamma-gamma collider based on TESLA optimistic parameters.
 - Possible to suppress huge backgrounds with improved jet clustering.
 - Significance ~ 5 with 5 year PLC run
 - Further study
 - jet clustering
 - b-tagging
 - other decay modes
- T. Suehara's talk, T. Tanabe's talk
in this workshop

Backup slides

About PLC

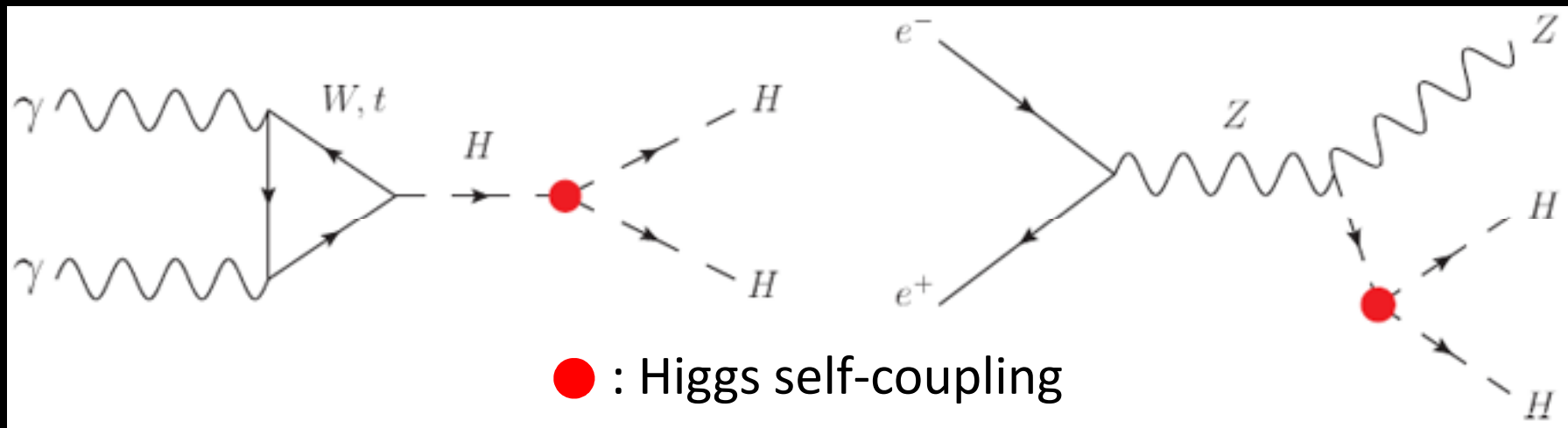


gamma-gamma collision

Comparison of $\gamma\gamma$ and e^+e^- process

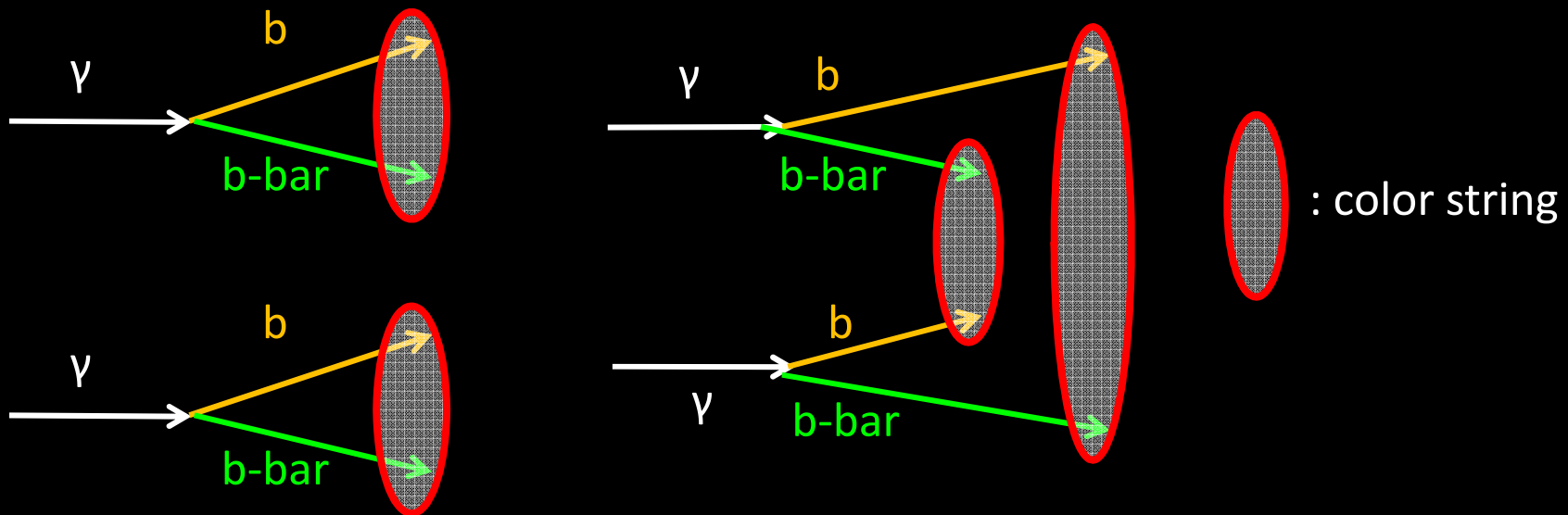
$$\gamma\gamma \rightarrow HH$$

$$e^+e^- \rightarrow ZHH$$



Contribution of self-coupling is different way.
Energy threshold of $\gamma\gamma$ process is lower than e^+e^- process.

$\gamma\gamma \rightarrow b \bar{b} b \bar{b}$ (4b) events



(2-jet invariant mass) $< 15\text{GeV}$ were cut.
We assume that we can cut these events.
 $\rightarrow 5.872 \cdot 10^4$ events/year

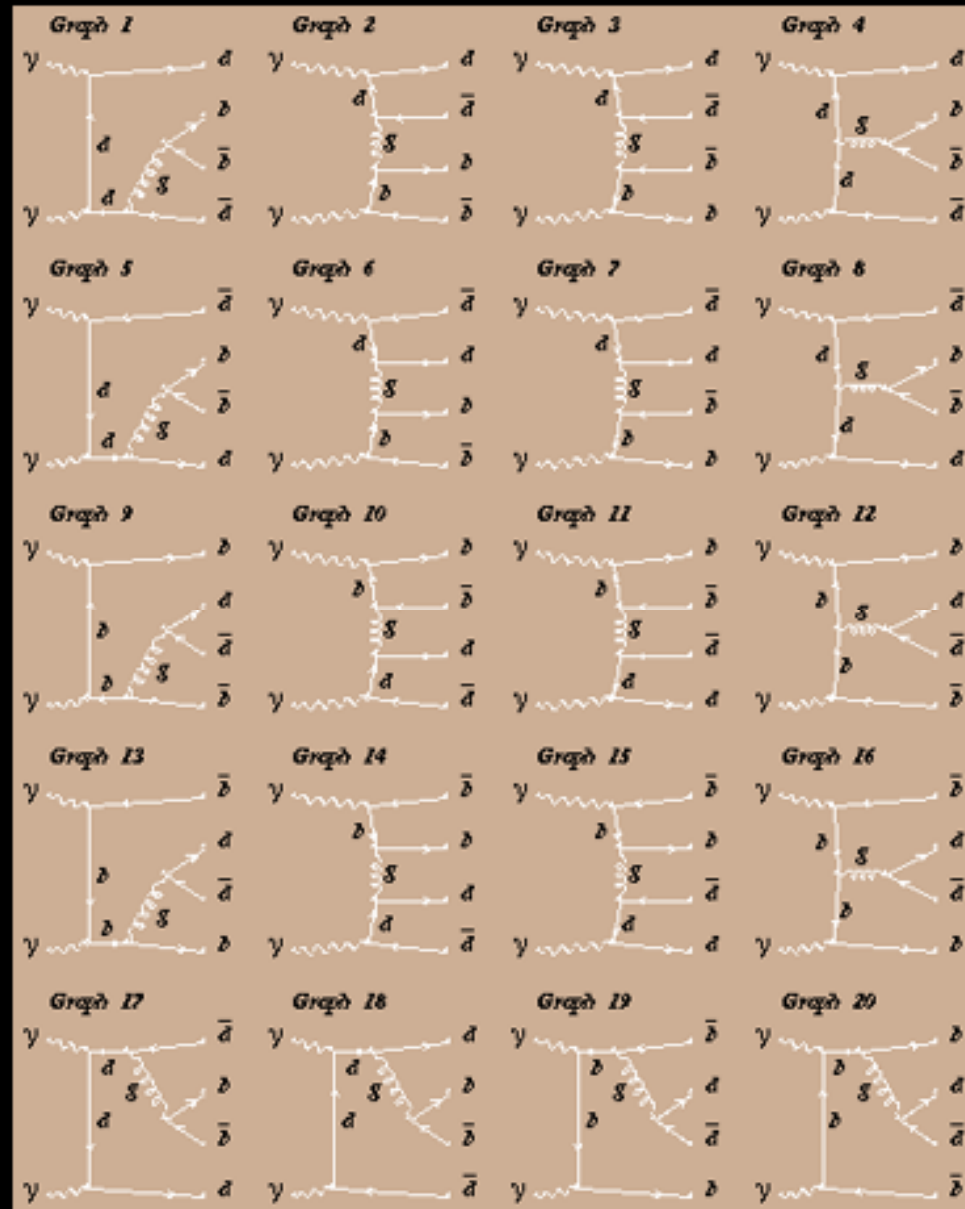
Calculation of 4b BG

d -> b

ELWK = 2

QCD = 2

Calculated with
GRACE



Jet clustering

JADE clustering

$$\frac{(p_i + p_j)^2}{E_{vis}^2} < Y_{cut}$$

p_i : 4-momentum of particle i

E_{vis} : visible energy

Y_{cut} : Y_{cut} value of jet clustering

Event selection --- pre-selection

pre-selection

$\beta > 0.05$, $|\cos\theta| < 0.99$

more than 3 b-flavor jets with ($n_{\text{sig}} = 3.0$, $n_{\text{offv}} = 1$) analysis

more than 2 b-flavor jets with ($n_{\text{sig}} = 3.0$, $n_{\text{offv}} = 2$) analysis

β : Lorentz factor of reconstructed particle

θ : angle between reconstructed particle and beam axis

b-tagging

to suppress huge WW BG mainly

Sphericity, Y-value

normalized momentum tensor M_{ab}

$$\textcircled{M_{ab}} = \sum_i p_{ia} p_{ib} / \sum_i p_i^2 \quad p_i : \text{momentum of particle } i$$

3*3 matrix

→ eigenvalue $Q_1, Q_2, Q_3 (Q_1 \leq Q_2 \leq Q_3)$

$$\text{sphericity} = \frac{3}{2} (Q_1 + Q_2)$$

$$Y - \text{value} = \frac{\sqrt{3}}{2} (Q_2 - Q_1)$$

W filter

- 9 input parameters

- χ_H^2, χ_Z^2

- visible energy

- # of tracks

- Y_{cut} value of jet clustering

- longitudinal momentum, transverse momentum

- # of b-flavor jets (nsig = 3.5, noffv = 1 analysis)

- # of b-flavor jets (nsig = 3.5, noffv = 2 analysis)

4b filter

- 17 input parameters

- no relation to χ^2 (11)

- visible energy, # of tracks, Y_{cut} value of jet clustering, thrust, sphericity, Y-value, $\cos\theta$ of jet (4), maximum $|\cos\theta$ of jet|

- jet pairing of least χ_H^2 (3)

- χ_H^2 , $\cos\theta$ of 2-jet (2)

- jet pairing of least χ_V^2 (3)

- χ_V^2 , $\cos\theta$ of 2-jet (2)

$$\chi_V^2 = \frac{(M_1 - 10)^2}{\sigma_{2j}^2} + \frac{(M_2 - 10)^2}{\sigma_{2j}^2}$$

10 : invariant mass of b b-bar system

Z filter

- 10 input parameters

- $\chi_H^2, \chi_W^2, \chi_Z^2$

- energy of 2-jet (2)

- visible energy

- # of tracks

- longitudinal momentum

- # of b-flavor jets (nsig = 3.5, noffv = 1 analysis)

- # of b-flavor jets (nsig = 3.5, noffv = 2 analysis)

Cut summary

JADE clustering & 4b (optimistic)

	signal	WW	ZZ	4b (opt)
expected events (# of MC samples)	80 (50000)	73100000 (75000000)	59350 (1000000)	293600 (1000000)
pre-selection	47.93 (29958)	81655 (83777)	5167 (87057)	70851 (241318)
W filter	12.34 (7713)	8.772 (9)	193.4 (3259)	318.0 (1083)
4b (opt) filter	7.262 (4539)	1.949 (2)	73.89 (1245)	7.340 (25)
Z filter	4.823 (3018)	0.9747 (1)	9.377 (158)	3.817 (13)

$$\text{significance} = \frac{4.823}{\sqrt{4.823 + 0.9747 + 9.377 + 3.817}} = 1.11$$

Cut summary

JADE clustering & 4b (pessimistic)

	signal	WW	ZZ	4b (pes)
expected events (# of MC samples)	80 (50000)	73100000 (75000000)	59350 (1000000)	293600 (1000000)
pre-selection	47.93 (29958)	81655 (83777)	5167 (87057)	84491 (287776)
W filter	12.34 (7713)	8.772 (9)	193.4 (3259)	568.4 (1936)
4b (pes) filter	8.238 (5149)	0 (0)	84.40 (1422)	13.21 (45)
Z filter	4.994 (3121)	0 (0)	7.359 (124)	5.872 (20)

$$\text{significance} = \frac{4.994}{\sqrt{4.994^2 + 0 + 7.359^2 + 5.872^2}} = 1.17$$

Cut summary

perfect jet clustering & 4b (optimistic)

	signal (cheat)	WW (cheat)	ZZ (cheat)	4b (opt)
expected events (# of MC samples)	80 (50000)	73100000 (75000000)	59350 (1000000)	293600 (1000000)
pre-selection	46.64 (29152)	55836 (57287)	4172 (70292)	70851 (241318)
W (cheat) filter	38.58 (24115)	4.873 (5)	98.84 (1667)	1331 (4535)
4b (opt) filter	35.56 (22223)	3.899 (4)	41.78 (704)	3.817 (13)
Z (cheat) filter	33.26 (20787)	1.949 (2)	5.045 (85)	3.817 (13)

$$\text{significance} = \frac{33.26}{\sqrt{33.26 + 1.949 + 5.045 + 3.817}} = 5.01$$

Cut summary

perfect jet clustering & 4b (pessimistic)

	signal (cheat)	WW (cheat)	ZZ (cheat)	4b (pes)
expected events (# of MC samples)	80 (50000)	73100000 (75000000)	59350 (1000000)	293600 (1000000)
pre-selection	46.64 (29152)	55836 (57287)	4172 (70292)	84491 (287776)
W (cheat) filter	38.58 (24115)	4.873 (5)	98.84 (1667)	2179 (7422)
4b (pes) filter	34.50 (21562)	2.924 (3)	27.66 (466)	2.642 (9)
Z (cheat) filter	33.06 (20662)	2.924 (3)	5.935 (100)	2.642 (9)

$$\text{significance} = \frac{33.06}{\sqrt{33.06 + 2.924 + 5.935 + 2.642}} = 4.95$$