

29.09. 2011

## New results for the 2HDM

**BSM  $\rightarrow$  2HDMs**  
**Various: potentials**  
**Yukawas**  
**vacua**  
**The Inert Doublet Model**  
**SM-like Higgs scenarios**  
**at ...**

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(University of Warsaw)

$$\gamma\gamma \rightarrow h \rightarrow b\bar{b}$$

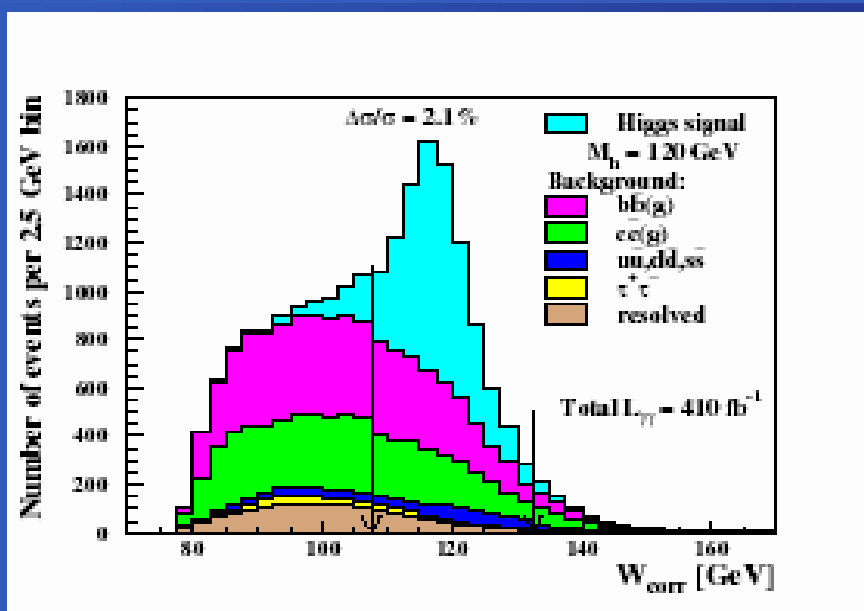
## SM summary

NZK

Niezurawski et al.,

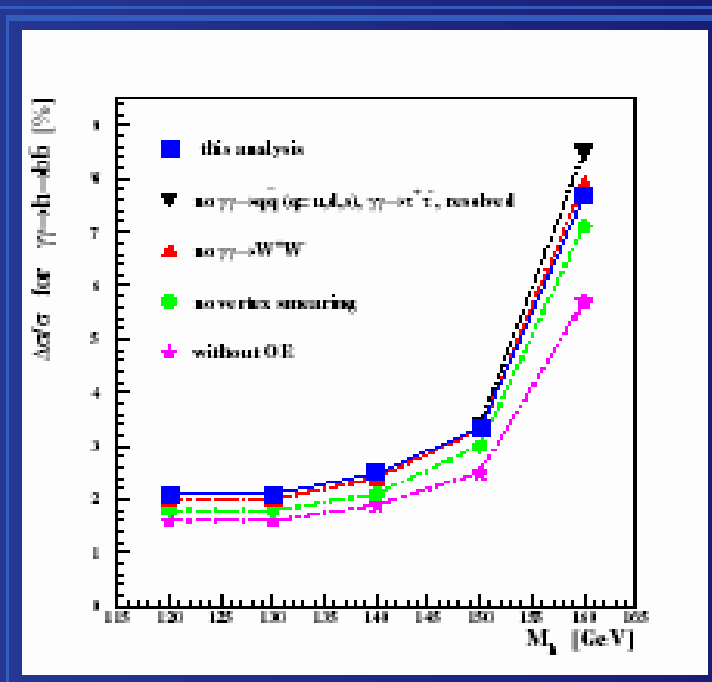
Monig, Rosca

→ Results for  $M_h = 120$  GeV



Corrected invariant mass distributions for signal and background events

Results for  $M_h = 120-160$  GeV



For  $M_h = 150, 160$  GeV additional cuts to reduce  $\gamma\gamma \rightarrow W^+W^-$

# THE THEORY OF MATTER and STANDARD MODEL(S)

F. Wilczek, LEPFest, Nov.2000 (hep-ph/0101187)

Theory of Matter =  $SU(2)_{I_{\text{weak}}}$  x  $U(1)_{Y_{\text{weak}}}$  x  $SU(3)_{\text{color}}$

The core concepts:

quantum field theory-gauge symmetry-spontaneous symmetry breaking-asymptotic freedom- the assignments of the lightest quarks and leptons

Brout-Englert-Higgs mechanism SSB of  $SU(2) \times U(1)$

Standard Models of scalar sector:

Choose the number of Higgs (scalar) doublets

SM=1HDM, 2HDM (as in MSSM), 3HDM ...

The lightest neutral scalar is often **SM-like...**

# Brout-Englert-Higgs mechanism

Spontaneous breaking of EW symmetry

$$SU(2) \times U(1) \rightarrow ?$$

*T.D. Lee 1973*

## Two Higgs Doublet Models

Two doublets of  $SU(2)$  ( $Y=1$ ,  $\rho=1$ ) -  $\Phi_1, \Phi_2$

Masses for  $W^{+/-}$ ,  $Z$ , no mass for photon?

Fermion masses via Yukawa interaction –

various models: Model I, II, III, IV, X, Y, ...

5 scalars:  $H^+$  and  $H^-$  and neutrals:

- CP conservation: CP-even  $h, H$  & CP-odd  $A$
- CP violation:  $h_1, h_2, h_3$  with indefinite CP parity\*

Sum rules (relative couplings to SM  $\chi$ )

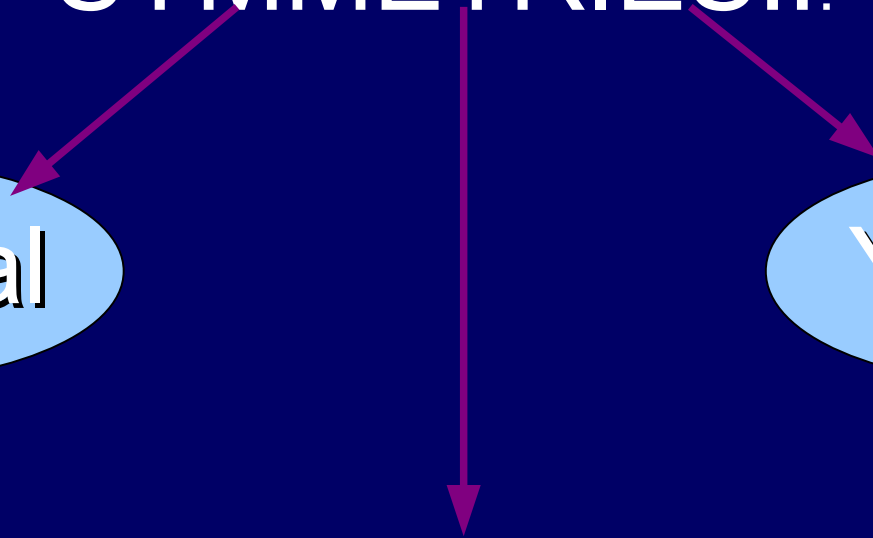
# 2HDMs

SYMMETRIES!!!

Potential

Yukawa

Vacuum



# Various models of Yukawa inter.

typically with some  $Z_2$  type symmetry to avoid FCNC

Model I - only one doublet interacts with fermions

Model II - one doublet with down-type fermions  $d, l$   
other with up-type fermions  $u$

Model III - both doublets interact with fermions

Model IV (X) - leptons interact with one  
doublet, quarks with the other

Model Y - one doublet with down-type quarks  $d$

other with up-type quarks  $u$  and leptons

Top 2HDM - top only with one doublet

Fermiophobic 2HDM - no coupling to the lightest Higgs

+ Extra dim 2HDM models

# 2HDM Potential

Lee, Haber, Gunion, Glashow, Weinberg, Paschos, Deshpande, Ma, Wudka, Branco, Rebelo, Lavoura, Ferreira, Barroso, Santos, Bottella, Silva, Diaz-Cruz, Grimus, Ecker, Ivanov, Ginzburg, Krawczyk, Osland, Nishi, Pilaftsis, Nachtmann, Maniatis, Akeroyd, Kanemura, Kalinowski, Grzadkowski, Hollik, Rosiek..

$$\begin{aligned} V = & \lambda_1(\Phi_1^\dagger\Phi_1)^2 + \lambda_2(\Phi_2^\dagger\Phi_2)^2 + \lambda_3(\Phi_1^\dagger\Phi_1)(\Phi_2^\dagger\Phi_2) \\ & + \lambda_4(\Phi_1^\dagger\Phi_2)(\Phi_2^\dagger\Phi_1) + [\lambda_5(\Phi_1^\dagger\Phi_2)^2 + \text{h.c.}] \\ & + [(\lambda_6(\Phi_1^\dagger\Phi_1) + \lambda_7(\Phi_2^\dagger\Phi_2))(\Phi_1^\dagger\Phi_2) + \text{h.c.}] \\ & - m_{11}^2(\Phi_1^\dagger\Phi_1) - m_{22}^2(\Phi_2^\dagger\Phi_2) - [m_{12}^2(\Phi_1^\dagger\Phi_2) + \text{h.c.}] \end{aligned}$$

$Z_2$  symmetry transformations:

$$\Phi_1 \rightarrow \Phi_1 \quad \Phi_2 \rightarrow -\Phi_2 \qquad \Phi_1 \rightarrow -\Phi_1 \quad \Phi_2 \rightarrow \Phi_2$$

Hard  $Z_2$  symmetry violation:  $\lambda_6, \lambda_7$  terms

Soft  $Z_2$  symmetry violation:  $m_{12}^2$  term (Re  $m_{12}^2 = \mu^2$ )

Explicit  $Z_2$  symmetry in V:  $\lambda_6, \lambda_7, m_{12}^2 = 0$

## • Symmetries of the 2HDM Potential

Pilaftsis, Scalars 2011

[R. A. Battye, G. D. Brawn, A.P., JHEP08 (2011) 020.]

$$V = -\frac{1}{2} M_A R^A + \frac{1}{4} L_{AB} R^A R^B .$$

## • Symmetries of the U(1)<sub>Y</sub>-Invariant 2HDM Potential

SO(5)-diagonally reduced basis:  $\text{Im } \lambda_5 = 0$  and  $\lambda_6 = \lambda_7$ .

The 2HDM potential exhibits a total of 13 = 6 + 7 accidental Higgs-Family (HF) and CP symmetries:

This talk

| Symmetry   | $\mu_1^2$ | $\mu_2^2$ | $m_{12}^2$ | $\lambda_1$ | $\lambda_2$ | $\lambda_3$  | $\lambda_4$              | $\text{Re } \lambda_5$      | $\lambda_6 = \lambda_7$ |
|--|-----------|-----------|------------|-------------|-------------|--------------|--------------------------|-----------------------------|-------------------------|
| $(Z_2)^2 \times \text{SO}(2)$                      | -         | -         | 0          | -           | -           | -            | -                        | -                           | 0                       |
| $\text{O}(2) \times \text{O}(2)$                   | -         | -         | 0          | -           | -           | -            | -                        | 0                           | 0                       |
| $\text{O}(3) \times \text{O}(2)$                   | -         | $\mu_1^2$ | 0          | -           | $\lambda_1$ | -            | $2\lambda_1 - \lambda_3$ | 0                           | 0                       |
| $Z_2 \times \text{O}(2)$                           | -         | -         | Real       | -           | -           | -            | -                        | -                           | Real                    |
| $(Z_2)^3 \times \text{O}(2)$                       | -         | $\mu_1^2$ | 0          | -           | $\lambda_1$ | -            | -                        | -                           | 0                       |
| $Z_2 \times [\text{O}(2)]^2$                       | -         | $\mu_1^2$ | 0          | -           | $\lambda_1$ | -            | -                        | $2\lambda_1 - \lambda_{34}$ | 0                       |
| <b>SO(5)</b>                                       | -         | $\mu_1^2$ | 0          | -           | $\lambda_1$ | $2\lambda_1$ | 0                        | 0                           | 0                       |
| <b><math>Z_2 \times \text{O}(4)</math></b>         | -         | $\mu_1^2$ | 0          | -           | $\lambda_1$ | -            | 0                        | 0                           | 0                       |
| <b>SO(4)</b>                                       | -         | -         | 0          | -           | -           | -            | 0                        | 0                           | 0                       |
| <b><math>\text{O}(2) \times \text{O}(3)</math></b> | -         | $\mu_1^2$ | 0          | -           | $\lambda_1$ | $2\lambda_1$ | -                        | 0                           | 0                       |
| <b><math>(Z_2)^2 \times \text{SO}(3)</math></b>    | -         | $\mu_1^2$ | 0          | -           | $\lambda_1$ | -            | -                        | $\lambda_4$                 | 0                       |
| <b><math>Z_2 \times \text{O}(3)</math></b>         | -         | $\mu_1^2$ | Real       | -           | $\lambda_1$ | -            | -                        | $\lambda_4$                 | Real                    |
| <b>SO(3)</b>                                       | -         | -         | Real       | -           | -           | -            | -                        | $\lambda_4$                 | Real                    |



# Inert Doublet Model

Ma'78

Barbieri'06

Symmetry under  $Z_2$  transf.  $\Phi_1 \rightarrow \Phi_1$   $\Phi_2 \rightarrow -\Phi_2$

both in L (V and Yukawa interaction = Model I)  
and in the vacuum:

$$\langle \Phi_1 \rangle = v$$

$$\langle \Phi_2 \rangle = 0$$

Today?

- $\Phi_1$  as in SM (BEH), with Higgs boson  $h$  (SM-like)
- $\Phi_2$  has no vev, with 4 scalars (no Higgs bosons!)  
no interaction with fermions (inert doublet)

Here  $Z_2$  symmetry exact  $\rightarrow Z_2$  parity, only  $\Phi_2$  has odd  $Z_2$ -parity

→ The lightest scalar stable -a dark matter candidate  
( $\Phi_2$  dark doublet with dark scalars).

$\Phi_1 \rightarrow \Phi_S$  Higgs doublet S

$\Phi_2 \rightarrow \Phi_D$  Dark doublet D

# Extrema of the 2HDM potential with explicit $Z_2$ symmetry

Ginzburg, Kanishev, MK, Sokołowska'09

Finding extrema:  $\partial V / \partial \Phi|_{\Phi = \langle \Phi \rangle} = 0$

Finding minima  $\rightarrow$  global minimum = vacuum

Positivity (stability) constraints (V with real parameters)

$$\left[ \lambda_1 > 0, \quad \lambda_2 > 0, \quad R + 1 > 0 \right]$$

$$\lambda_{345} = \lambda_3 + \lambda_4 + \lambda_5, \quad R = \frac{\lambda_{345}}{\sqrt{\lambda_1 \lambda_2}}$$

Extremum fulfilling the positivity constraints  
with the lowest energy = vacuum

# Possible extrema (vacuum) states

for  $V$  with explicit  $Z_2$

The most general extremum state

$$\langle \phi_S \rangle = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ v_S \end{pmatrix}, \quad \langle \phi_D \rangle = \frac{1}{\sqrt{2}} \begin{pmatrix} u \\ v_D \end{pmatrix}$$

$v_S, v_D, u$  - real

$v_S, u \geq 0$

$$v^2 = v_1^2 + v_2^2 + u^2$$

$$= (246 \text{ GeV})^2$$

EWs

EWs

$$u = v_D = v_S = 0$$

Inert

$I_1$

$$u = v_D = 0$$

Inert-like

$I_2$

$$u = v_S = 0$$

Mixed (Normal, MSSM like)

$M$

$$u = 0$$

Charge Breaking

$Ch$

$$u \neq 0 \quad v_D = 0$$

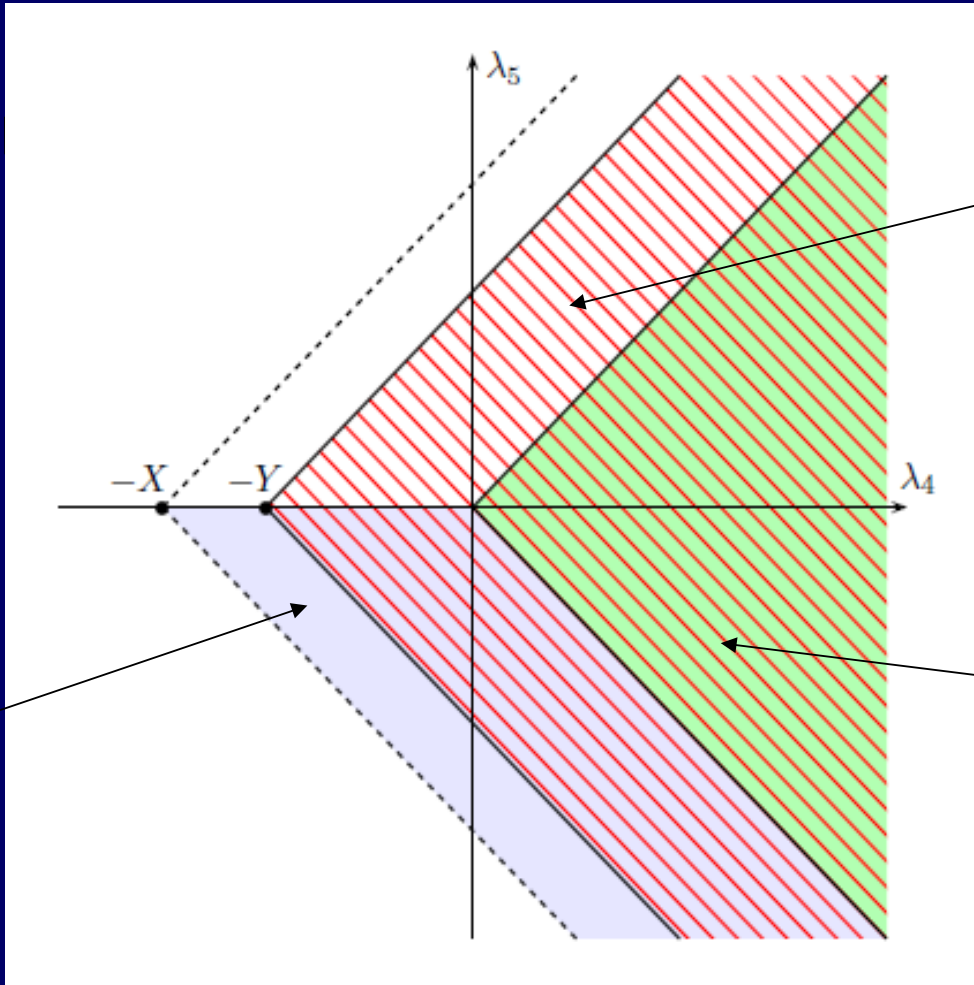
# Various extrema (vacua) on $(\lambda_4, \lambda_5)$ plane

Positivity constrains:  $\lambda_4 \pm \lambda_5 > -X$   $X = \sqrt{\lambda_1 \lambda_2 + \lambda_3} > 0$

Inert (Inert-like)  
 $Y = M_{H^+}^2 / v^2$

Charge  
Breaking  
Ch

Mixed



Note the overlap of the Inert with M and Ch !

# TODAY

2HDM with explicit  $Z_2$  (D) symmetry

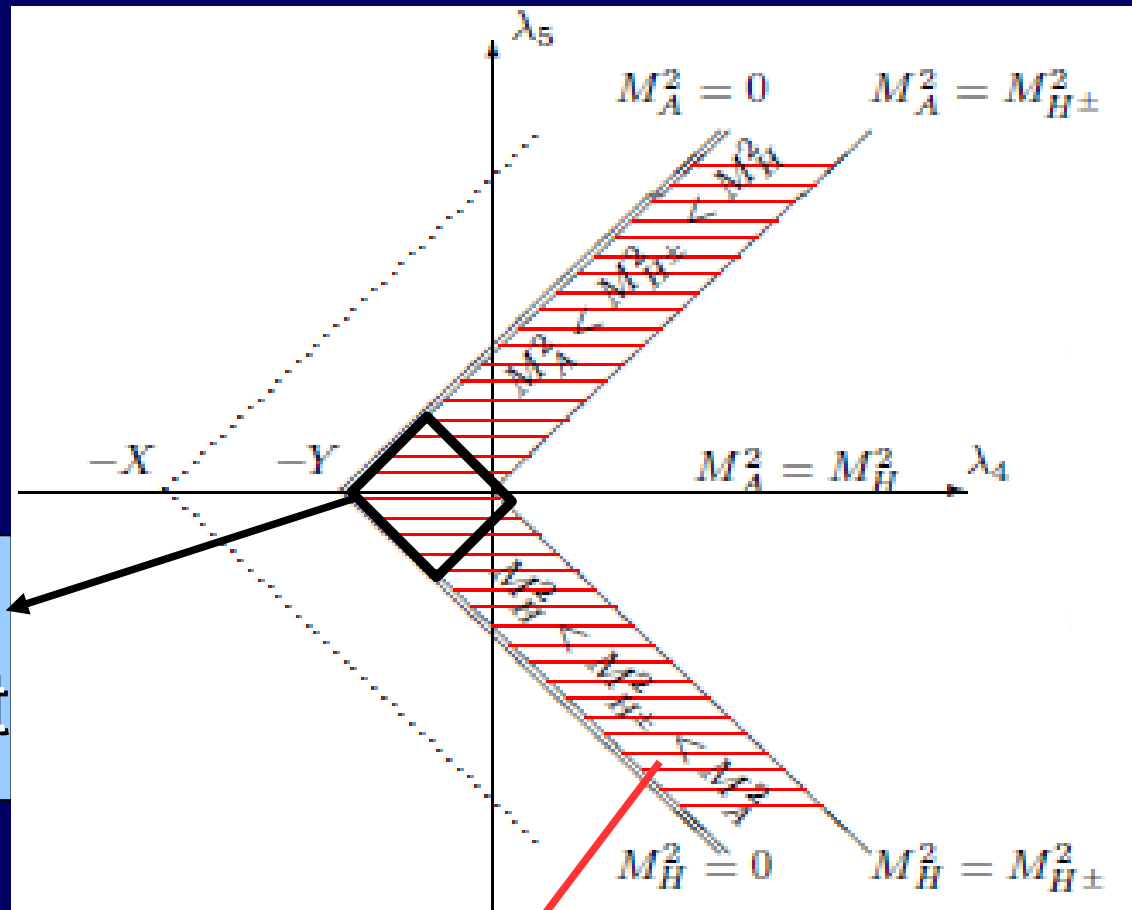
$$\Phi_S \rightarrow \Phi_S \quad \Phi_D \rightarrow -\Phi_D$$

Model I (Yukawa int. with  $\Phi_S$  only)

- Charge breaking phase Ch?  
photon is massive, el.charge is not conserved...  
→ No
- Neutral phases:
  - Mixed M ok, many data, but no DM
  - Inert I1 OK! In agreement with accelerator and astrophysical data (neutral DM)
  - Inert-like I2 No, all fermions massless, no DM

# Dark scalar masses

$$Y = M_{H^\pm}^2 - 2/v^2$$



here  $H^\pm$   
the heaviest

here  $H$  is the lightest ( $\lambda_5 < 0$ ) – our DM

# Constraining Inert Doublet Model

- Positivity, extrema, vacua, unitarity, perturbativity
- By considering properties of
  - the SM-like  $h$ ,  $M_h^2 = m_{11}^2 = \lambda_1 v^2$  (light and heavy)
  - the dark scalars  $D$  always in pairs!

$$\begin{aligned}M_{H^+}^2 &= -\frac{m_{22}^2}{2} + \frac{\lambda_3 v^2}{2} \\M_H^2 &= -\frac{m_{22}^2}{2} + \frac{\lambda_3 + \lambda_4 + \lambda_5}{2} v^2 \\M_A^2 &= -\frac{m_{22}^2}{2} + \frac{\lambda_3 + \lambda_4 - \lambda_5}{2} v^2\end{aligned}$$

$D$  couple to  $V = W/Z$  (eg.  $AZH$ ,  $H^- W^+ H$ ), not  $DV V$ !  
Quartic selfcouplings  $D^4$  proportional to  $\lambda_2$

hopeless to be measured at colliders!

Couplings with Higgs:  $hHH \sim \lambda_{345}$        $h H^+ H^- \sim \lambda_3$

# Unitarity constraints on parameters of $V$ ( $Z_2$ symmetry)

analysis by B. Gorczyca, MSc Thesis, July 2011

Full scattering matrix macierz 25x25 for scalars (including Goldstone's)

$$\mathcal{M} = \begin{pmatrix} \mathcal{M}_1 & & & & & \\ & \mathcal{M}_2 & & & & \\ & & \mathcal{M}_3 & & & \\ & & & \mathcal{M}_4 & & \\ & & & & \mathcal{M}_5 & \\ & & & & & \mathcal{M}_6 \end{pmatrix}.$$

in high energy limit

Block-diagonal  
form due electric  
charge and CP  
conservation

M1:  $G^+H^-$ ,  $G^-H^+$ ,  $hA$ ,  $GA$ ,  $GH$ ,  $hH$

M2:  $G^+G^-$ ,  $H^+H^-$ ,  $GG$ ,  $HH$ ,  $AA$ ,  $hh$

M3:  $Gh$ ,  $AH$

M4:  $G^+G$ ,  $G^+H$ ,  $G^+A$ ,  $G^+h$ ,  $GH^+$ ,  $HH^+$ ,  $AH^+$ ,  $hH^+$

M5:  $G^+G^+$ ,  $H^+H^+$

M6:  $G^+H^+$

Unitarity constraints  
 $\rightarrow |\text{eigenvalues}| < 8\pi$



# Constraints for lambdas

$$0 \leq \lambda_1 \leq 8.38$$

$$0 \leq \lambda_2 \leq 8.38$$

$$-13.64 \leq \lambda_3 \leq 16.52$$

$$-16.13 \leq \lambda_4 \leq 16.53$$

$$-8.24 \leq \lambda_5 \leq 0$$

$$-8.19 \leq \lambda_{345} \leq 15.54,$$

$$-7.65 \leq \lambda_{345}^- \leq 16.46,$$

$$-16.66 \leq \lambda_{45} \leq 16.50,$$

$$-15.80 \leq \lambda_{45}^- \leq 16.71.$$

Couplings for dark particles in IDM



$$\lambda_{345}^- = \lambda_3 + \lambda_4 - \lambda_5$$

$$\lambda_{45}^- = \lambda_4 - \lambda_5$$

# Unitarity bounds for IDM

Bounds for the case

$$m_{22}^2 = 0,$$

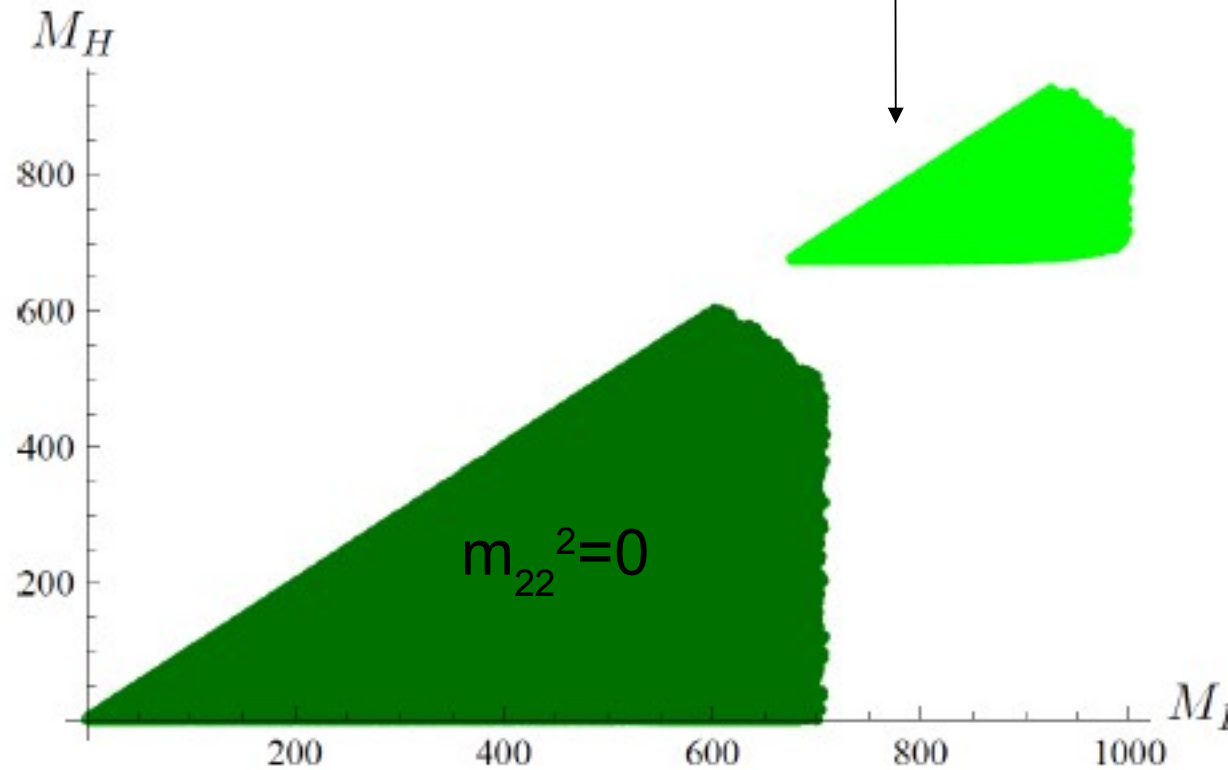
$M_h = 120$  GeV and

$M_h \in [114, 145]$  GeV:

$$M_H \leq 602 \text{ GeV},$$

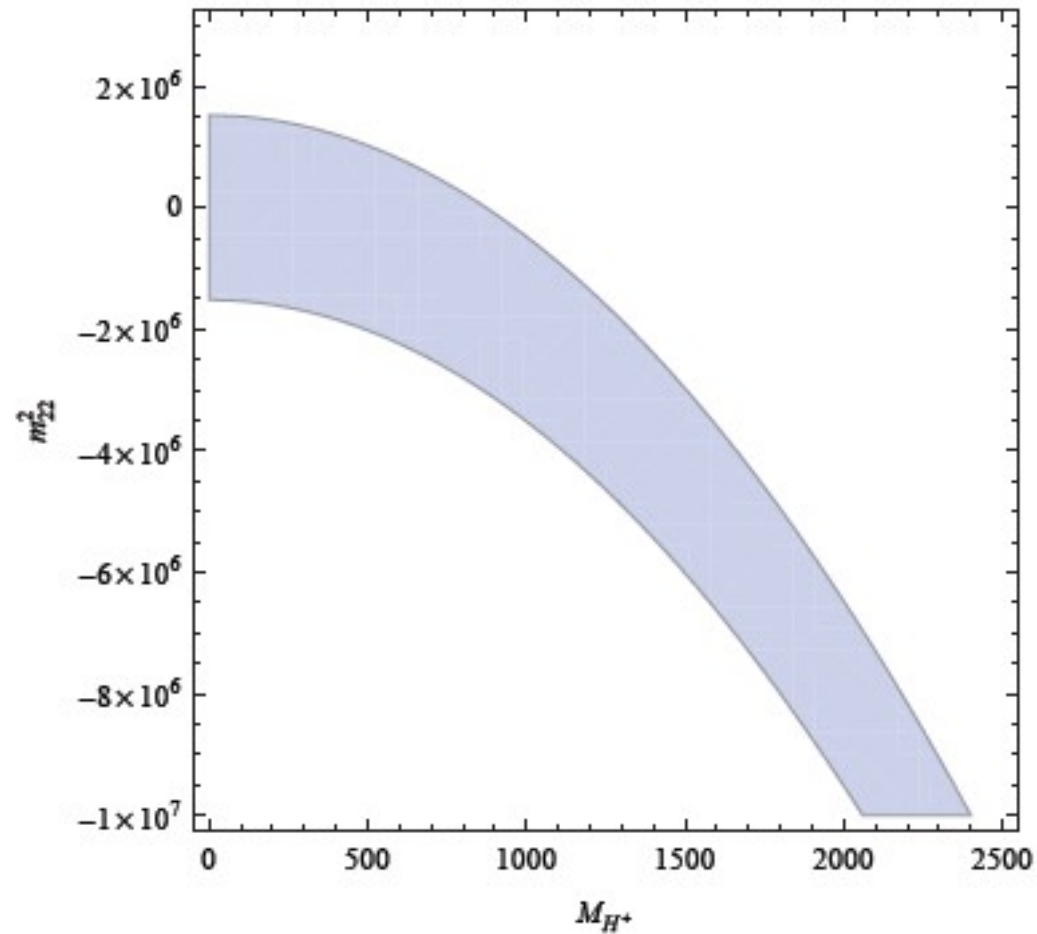
$$M_{H\pm} \leq 708 \text{ GeV},$$

$$M_A \leq 708 \text{ GeV}.$$



$M_{H\pm}, \text{ GeV}$

IDM



Simplified unitarity condition  
 $|\lambda_3| < 8\pi$

# Mixed Model=Mixed vacuum and Yukawa Model II

## Bounds for the Mixed Model

For the general case:

$$\begin{aligned}
 M_{H^\pm} &\leq 690 \text{ GeV}, \\
 M_A &\leq 702 \text{ GeV}, \\
 M_H &\leq 698 \text{ GeV}, \\
 M_h &\leq 501 \text{ GeV}
 \end{aligned}$$

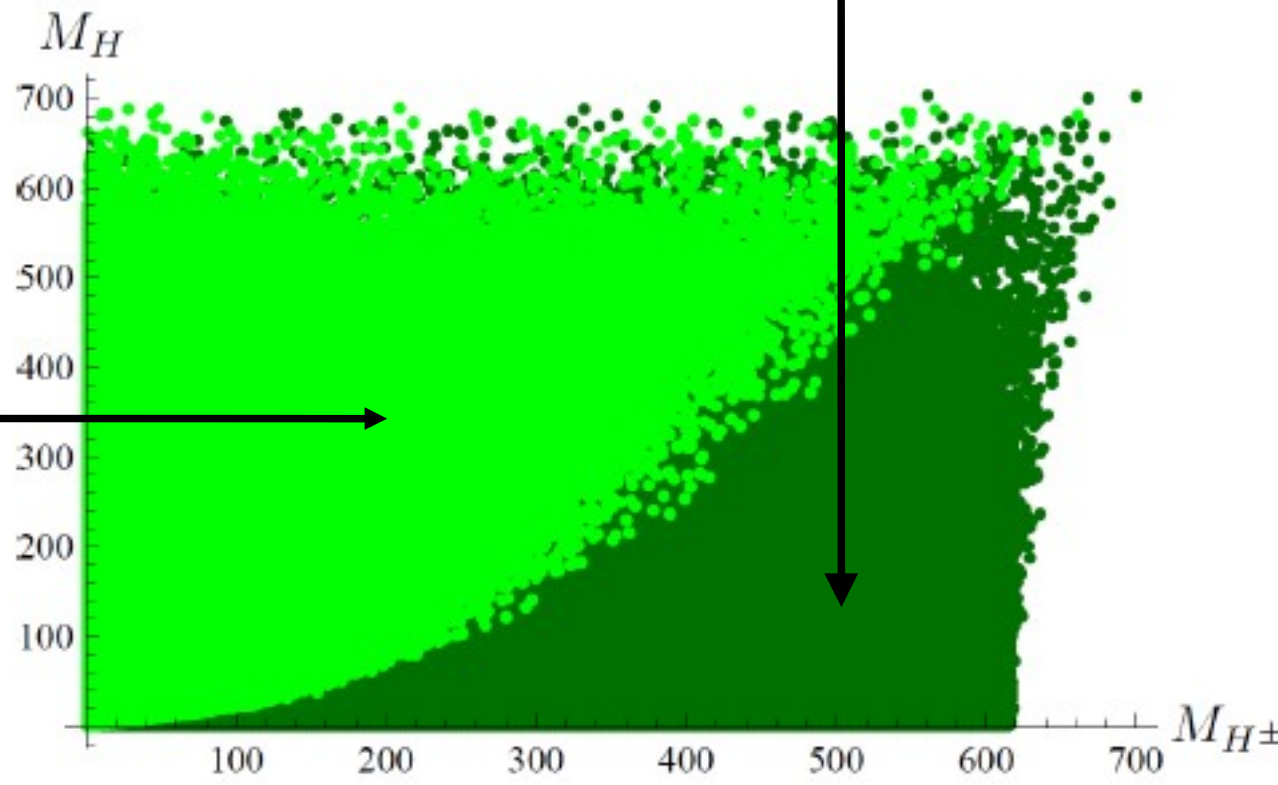
(Compare Kanemura *et al.* (1993)  
Hořejši & Kladiva (2006).)

Akeroyd, A. Arhrib, E. Naimi,

Light green =  
true allowed  
region

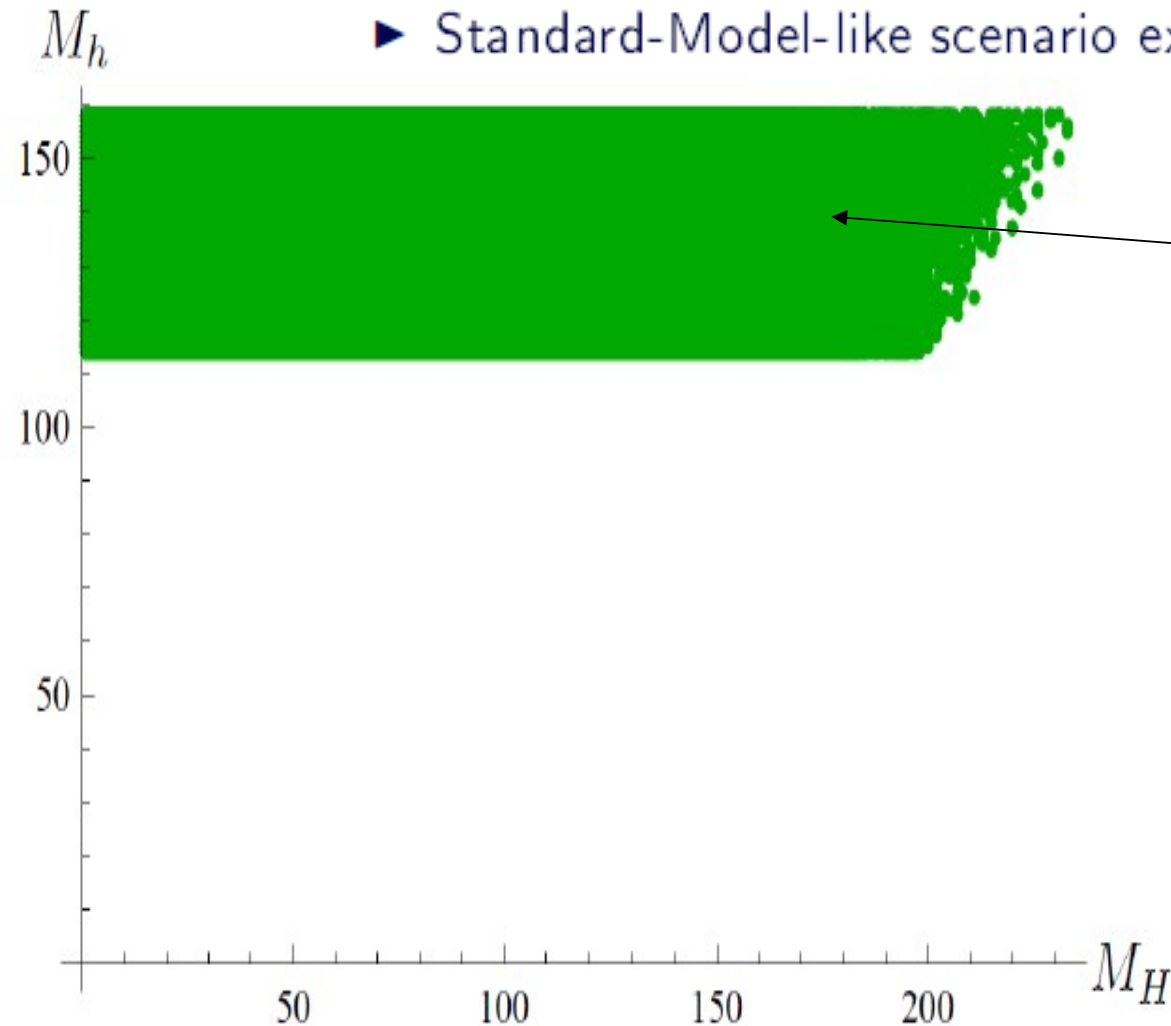
# MSSM type

Dark region - not allowed  
for Mixed vacuum !!!



For the SM-like Mixed Model ( $h$  couples like the standard Higgs boson and  $M_h \in [114, 145]$  GeV):

- ▶ unitarity:  $M_{H^\pm} \leq 224$  GeV.
- ▶  $b \rightarrow s\gamma$ :  $M_{H^\pm} \geq 300$  GeV (Misiak *et al.* (2007)).
- ▶ Standard-Model-like scenario excluded.



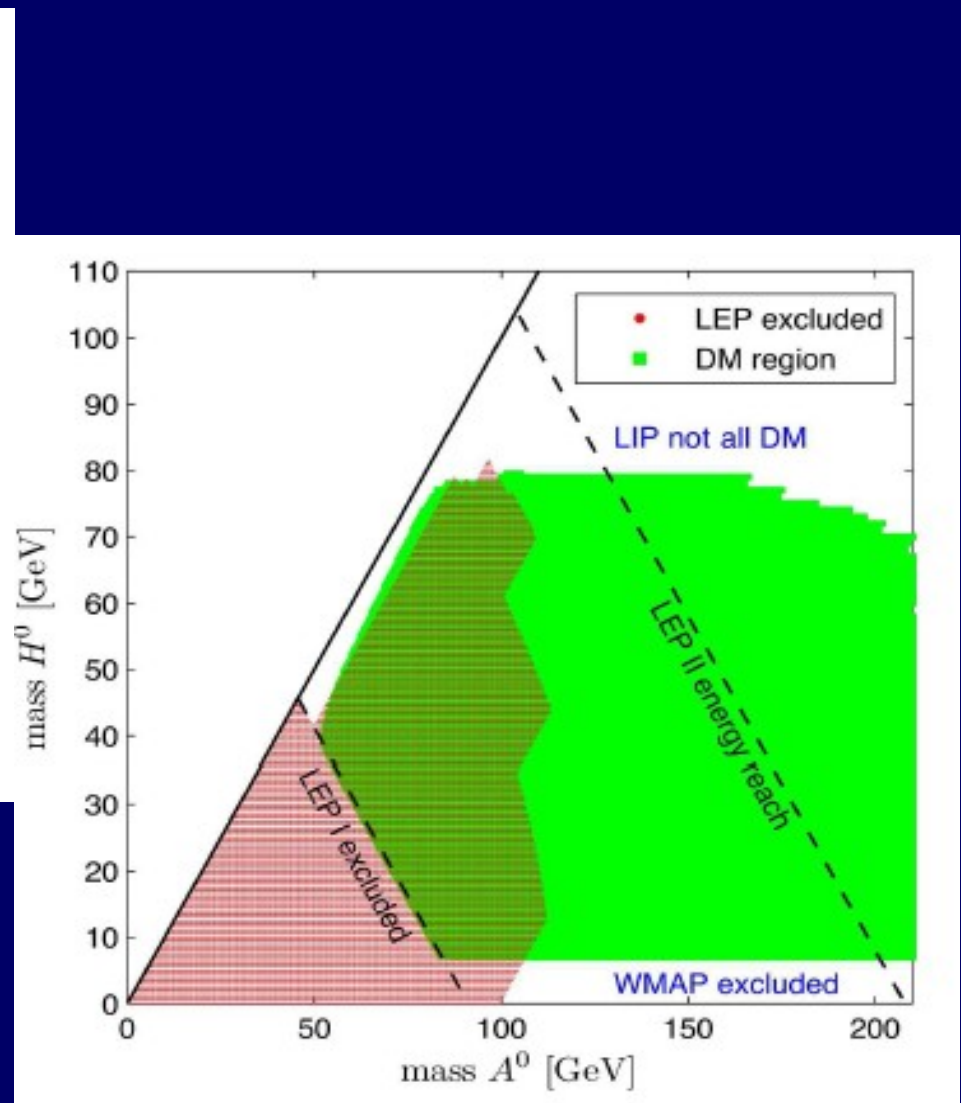
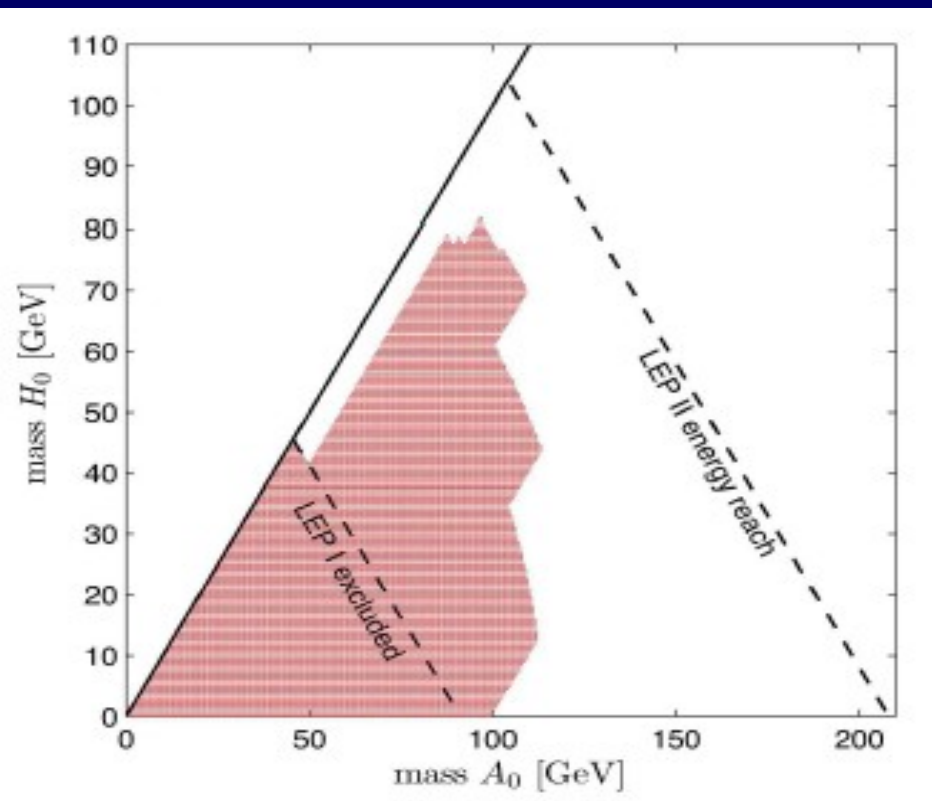
allowed region  
by unitarity

$$\begin{aligned} M_{H^\pm} &\leq 233 \text{ GeV}, \\ M_A &\leq 618 \text{ GeV}, \\ M_H &\leq 611 \text{ GeV}, \\ M_h &\leq 158 \text{ GeV}. \end{aligned}$$

$$\begin{aligned} -0.96 &\leq \sin \alpha \leq -0.17, \\ 0.29 &\leq \tan \beta \leq 6.16. \end{aligned}$$

# IDM: LEP II exclusion (masses $H$ vs $A$ )

Lundstrom... hep-ph/0810.3924



## LEP II + WMAP

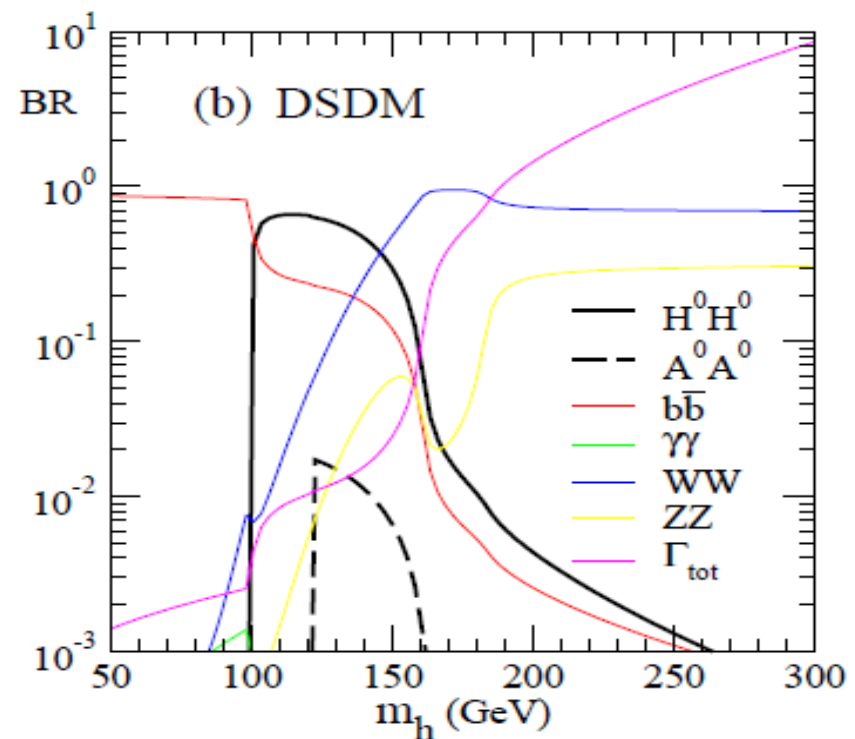
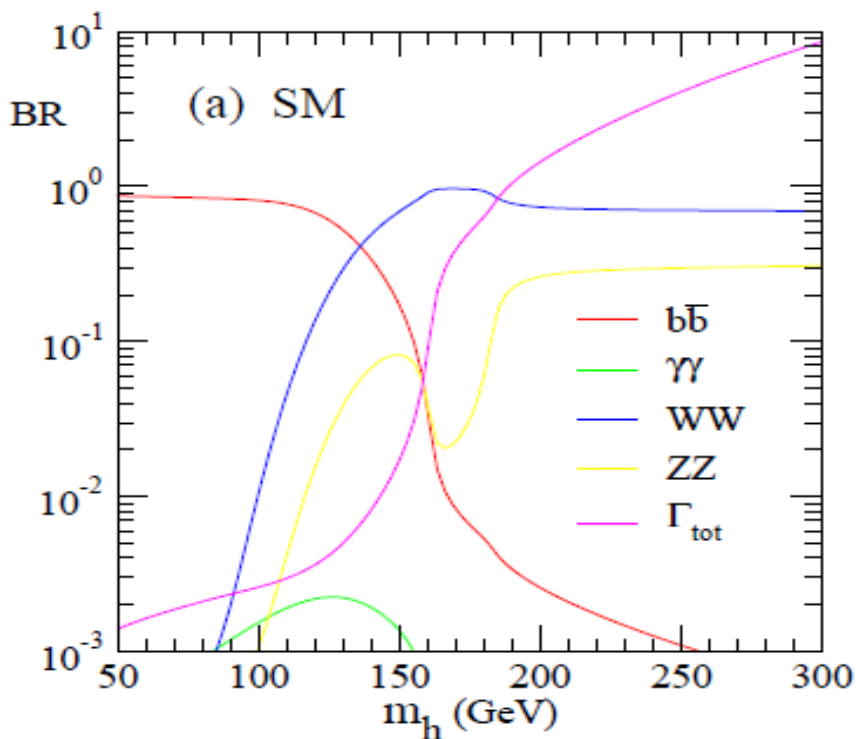
DM = low, medium, high mass

# Colliders signal/constraints for IDM

Barbieri et al '2006 for heavy h; Cao, Ma, Rajasekaren' 2007 for a light h, *later many others*

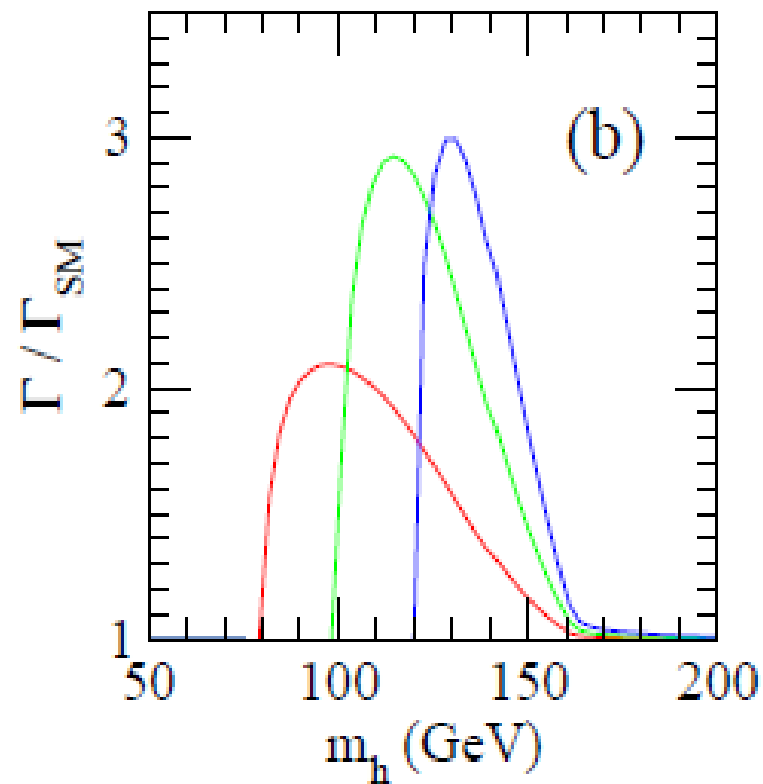
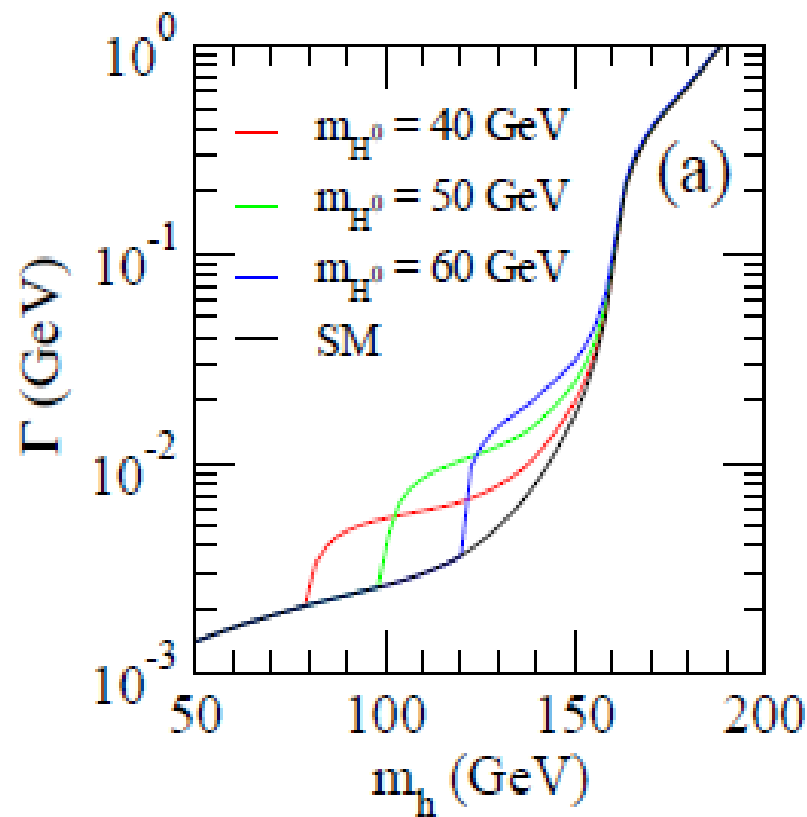
EW precision data:  $(M_{H^+} - M_A)(M_{H^+} - M_H) = M^2, M = 120^{+20}_{-30}$  GeV

For  $M_H = 50$  GeV



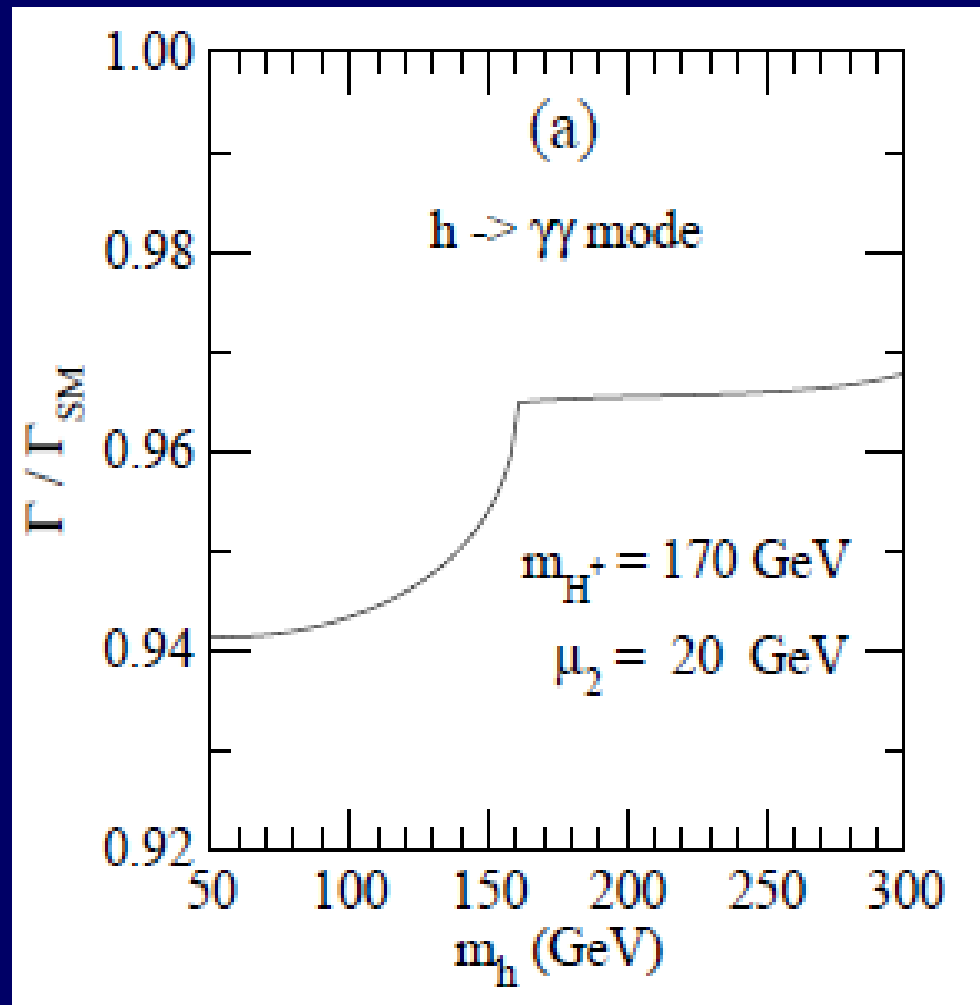
For  $M_H = 50$  GeV,  $\Delta(A, H) = 10$  GeV,  $M_{H^+} = 170$  GeV,  $m_{22} = 20$  GeV

# IDM – total width of h





# IDM: $\gamma\gamma h$



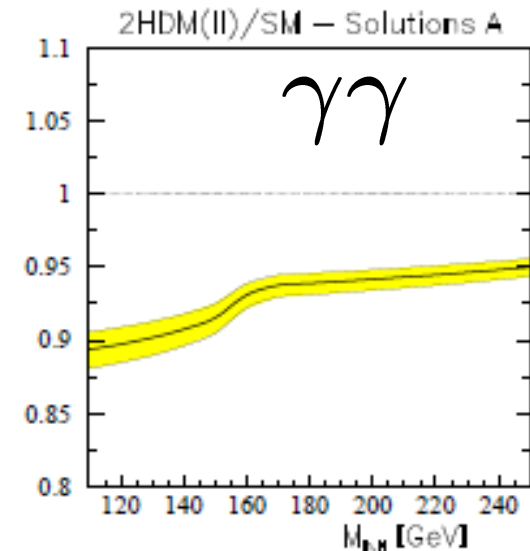
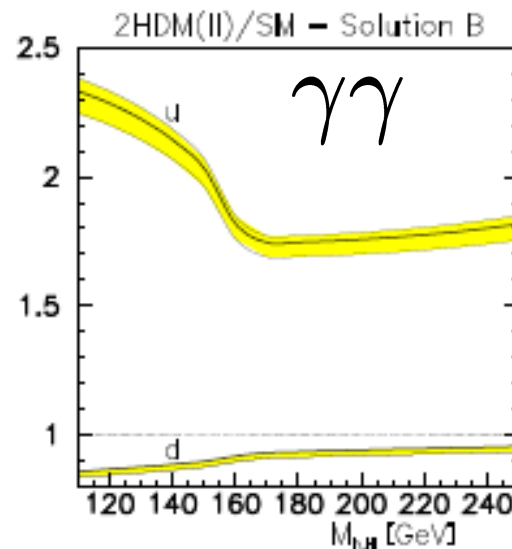
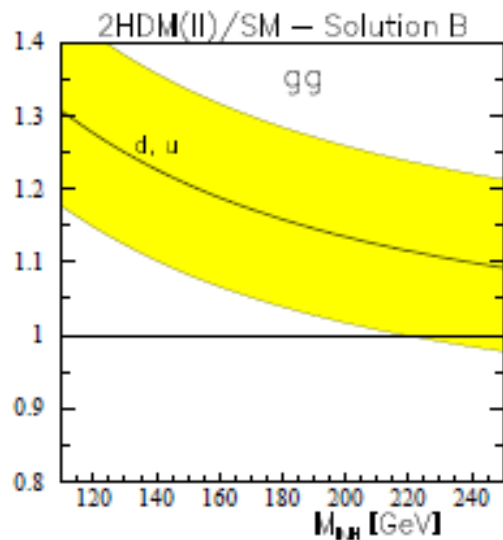
# Loop couplings $ggh, \gamma\gamma h$ in $Z_2$ 2HDM

(Mixed)

$\Gamma(h \rightarrow gg, \gamma\gamma)$   
including exp. uncertainties

Ginzburg, Osland, MK '2001

Even when  $hVV$  and  $hff$  as in SM, (SM-like scenario A)  $\rightarrow$   
large non-decoupling effects due to heavy  $H^\pm$ . 600 GeV



$ggh$  - solution B „wrong” signs of fermion couplings

# Conclusions

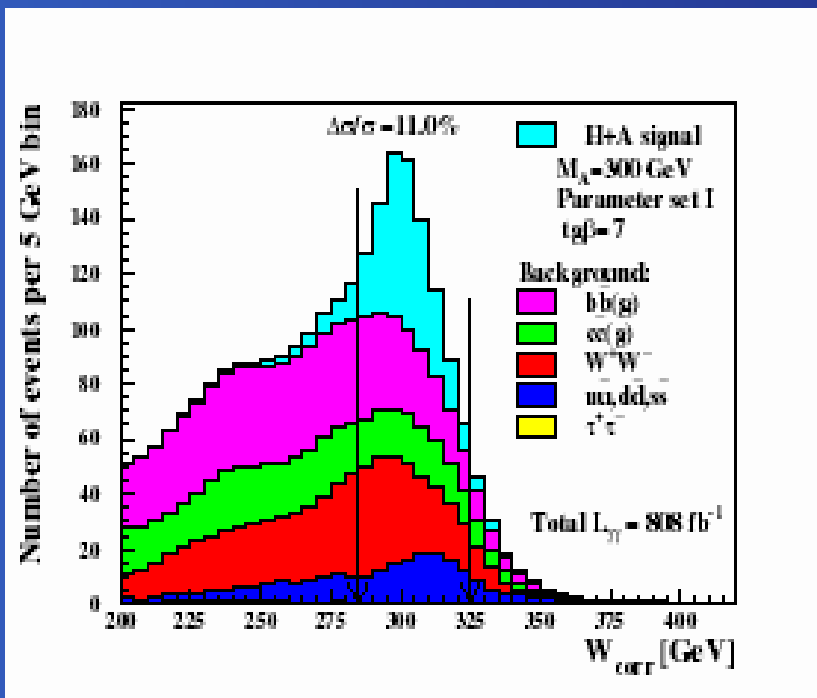
- 2HDM - a great laboratory for physics BSM
- In many Standard Models SM-like scenarios can be realized:
  - [Higgs mass  $>114$  GeV, SM tree-level couplings]
- In models with two doublets:
  - MSSM with decoupling of heavy Higgses  
→ *LHC-wedge*
  - 2HDM (Mixed) with and without CP violation *both  $h$  or  $H$  can be SM-like*
  - Intert Doublet Model

**Yes, Photon Linear Collider can distinguish...**

## Covering the LHC wedge

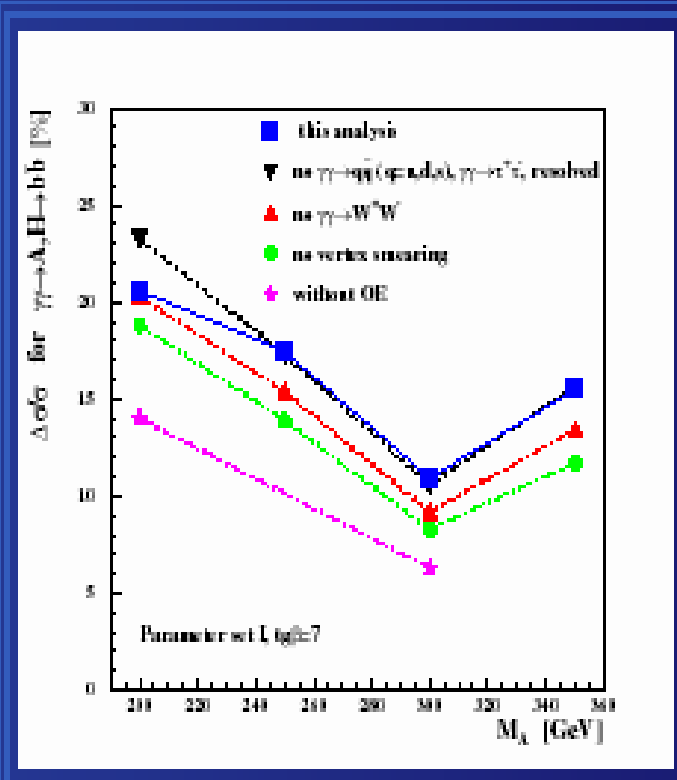
Precision of  $\sigma(\gamma\gamma \rightarrow A, H \rightarrow b\bar{b})$  measurement

Results for  $M_A = 300$  GeV



Corrected invariant mass distributions

Results for  $M_A = 200-350$  GeV



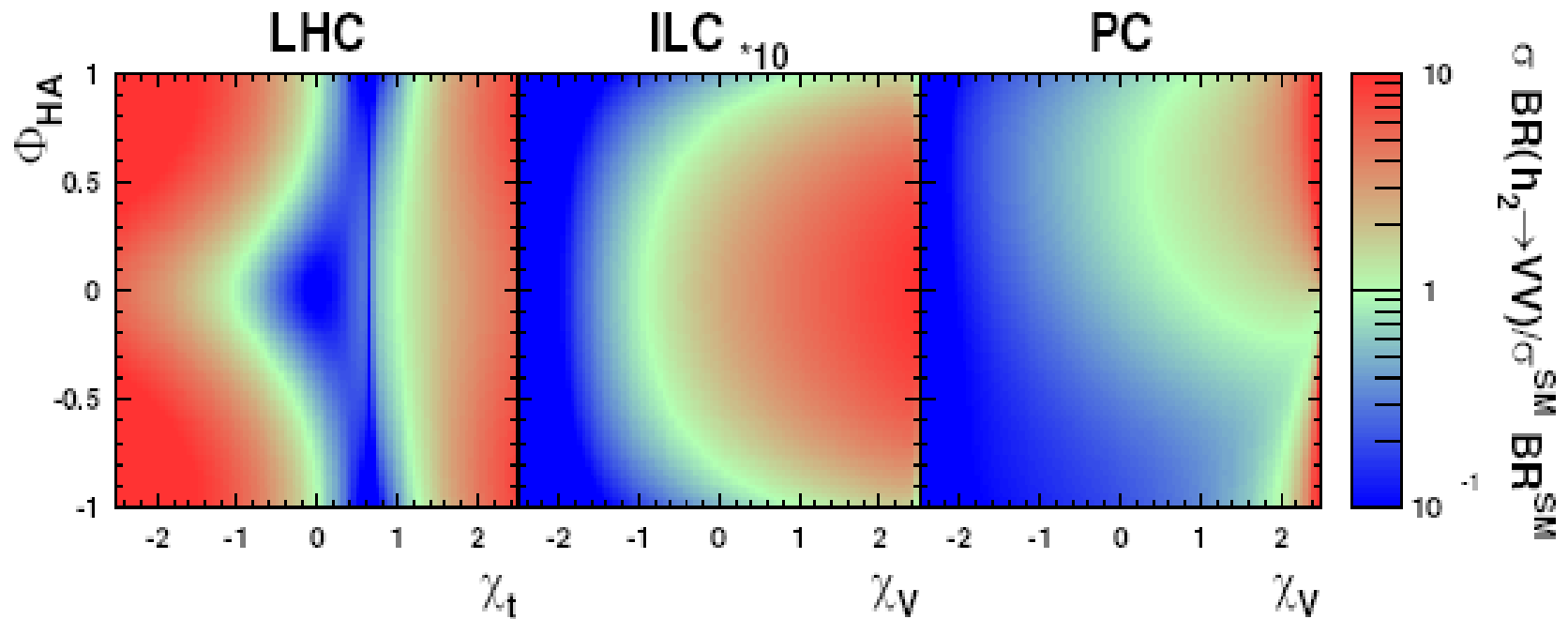
our previous results compared

# LHC $\oplus$ ILC $\oplus$ PC

Sensitivity of LHC, ILC and Photon Collider measurements to CP-violating mixing phase  $\Phi_{HA}$

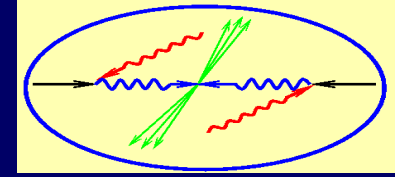
Cross sections  $\times$  BR relative to SM

$M_H = 250 \text{ GeV}$



# PLC: Photon Linear Collider

## $\gamma\gamma$ and $e\gamma$



- Resonance production of  $C=+$  states (eg. Higgs) Ginzburg et al
- Higher mass reach
- Polarised beams – CP filter Gunion, Grzadkowski, Godbole, Zarnecki
- $H\gamma\gamma$  coupling – sensitive to charged particles in theory (nondecoupling) Ginzburg et al., Gunion..
- Direct production of charged scalars, fermions and vectors – higher cross section Monig,
- Pair production of neutral particles (eg. light-on-light) via loops Jikia, Gounaris...
- Study of hadronic interaction of the photon Godbole, Pancheri; MK Brodsky, deRoeck, Zerwas