# Grid scan as lattice diagnostics

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## CERN

## 13th ATF2 Project Meeting - 12 January 2012

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# **Motivations**

## Lattice diagnostics

- Unexplained emittance growth during extraction
- Verification of the transfer matrices
- Some studies needs very low BPM scale errors

## Grid scan<sup>1</sup>

- Little influence of correctors scale errors
- Determine if there are BPM scale errors
- Clear evidence of non-linearities

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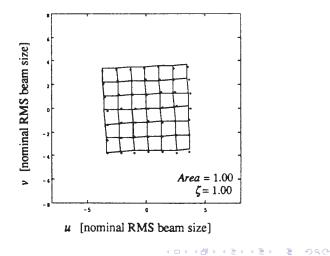
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# **Grid Scan Principle**

- Use 2 correctors to scan a grid in x and x' or in y and y'
- Use 2 BPMs to measure that grid.



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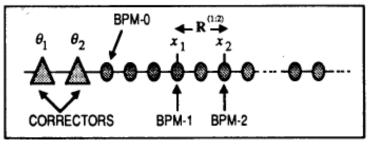
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# Angle Measurement

$$\begin{bmatrix} x_1 \\ x'_1 \end{bmatrix} = \begin{bmatrix} 1 & 0 \\ R_{11}^{(1:2)} & R_{12}^{(1:2)} \end{bmatrix}^{-1} \times \begin{bmatrix} x_1 \\ x_2 \end{bmatrix}$$

- Any BPM downstream of the correctors can be used.
- $X'_1$  measurement affected by:
  - BPM scale errors  $(A_1 and B_1)$ .
  - errors on transfer matrices
- These errors deform the grid.



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# Phase Space Normalization

## Normalization

Phase space normalization :

$$\begin{bmatrix} u \\ v \end{bmatrix} = \begin{bmatrix} \sqrt{1/\epsilon\beta_1} & 0 \\ \sqrt{\alpha_1/\epsilon\beta_1} & \sqrt{\beta_1/\epsilon} \end{bmatrix} \times \begin{bmatrix} x_1 \\ x'_1 \end{bmatrix}$$

with u and v in  $\sigma$  units.

• squareness of the grid (vectors  $\vec{h_i}$  and  $\vec{k_i}$  define element *i* of the grid):

$$\chi = \frac{1}{2N} \sum_{i=1}^{N} \frac{|\vec{h_i}|^2 + |\vec{k_i}|^2}{\det(\vec{h_i}, \vec{k_i})}$$

 in normalized phase space all grids have same squareness and area

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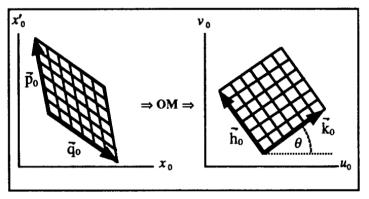
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# Grid Squaring

- by "choosing" the phase of the first BPM, the grid can be squared
- easier to see distortions
- squaring does not change the area of the grid
- but it does change influences of errors on the grid



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# Determination of scale factors Formalism

•  $a_i$  scale factor of BPM i ( $\tilde{x}$  is the measured value):

$$x_i = a_i \tilde{x}_i$$

as we have :

$$x_i'(j) = \frac{x_j - R_{11}^{i:j} x_i}{R_{12}^{i:j}}$$

. .

we got :

$$x'_i(j) = rac{a_j ilde{x}_j - R_{11}^{i:j} a_i ilde{x}_i}{R_{12}^{i:j}}$$

the area A(i,j) of the grid measured by BPM i and j is:

$$A(i,j) = \Delta u_i \Delta v_i(j)$$

with  $\Delta \tilde{u}_i$  and  $\Delta \tilde{v}_i(j)$  variating as  $\tilde{x}_i$  and  $\tilde{x}'_i(j)$ 

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# Determination of scale factors System of equations

From previous equations it comes that :

$$\tilde{A}(i,j) = a_i a_j A(i,j) - \frac{R_{11}^{i:j}}{R_{12}^{i:j}} \left(1 - \frac{a_i}{a_j}\right) \Delta u_i$$

- In EXT there is 24 BPMs, so for each plane :
  - 24 a<sub>i</sub> to determine
  - 300 non linear, coupled equations !!

Trick

• 
$$a_i \sim a_j \simeq 1 =>$$
 most of the cases (if  $\frac{R_{11}^{i:j}}{R_{12}^{i:j}} < 1$ ):

$$\tilde{A}(i,j) = a_i a_j A(i,j)$$

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# Algorithm

## Trick 2

- I don't know how to solve such a system :-(
- $\blacktriangleright$   $\Rightarrow$  Iterative method with :

$$\tilde{a}_k = < \tilde{A}(i,j) >_{i \text{ or } j=k} - < \tilde{A}(i,j) >_{i \text{ and } j\neq k} + 1$$

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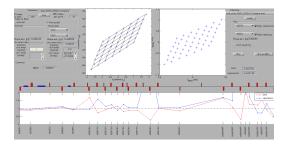
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# Implementation

- Implemented in the Flight Simulator for both planes
- Includes jitter subtraction
- Bad pulses detection
- Optional grid squaring



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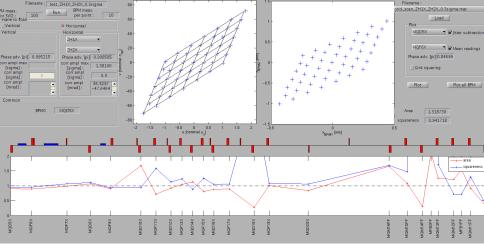
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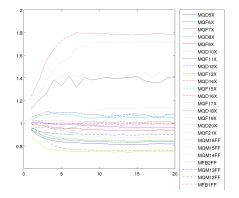
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# **BPM Scale Factors Determination**

- Used ZH1X and ZH2X with gain of 0.5 during iterations
- ZH1X and ZH2X have little phase advance => small amplitude scan (0.3σ).



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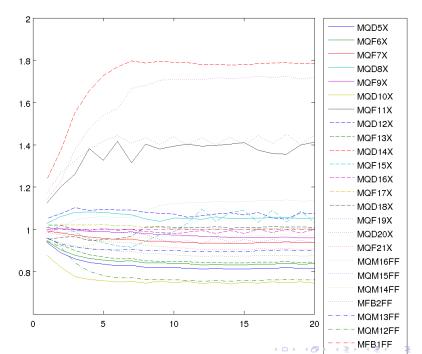
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# Horizontal Scan

## Scale Factors Results

- all EXT BPMs within 20% errors on scales except :
  - MQF11X and MQD14X
  - MQM15FF and MFB2FF (too large amplitude in FF to be believed)

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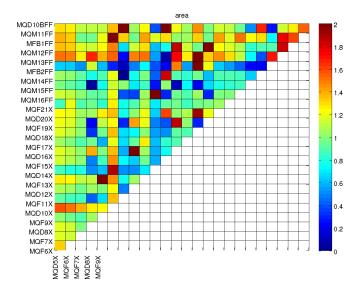
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# Area before BPM scale factors correction



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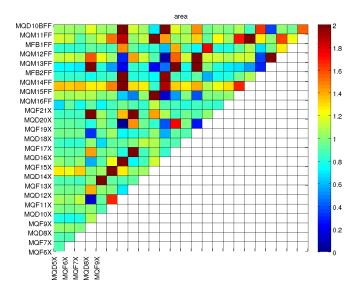
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# Area after BPM scale factors correction



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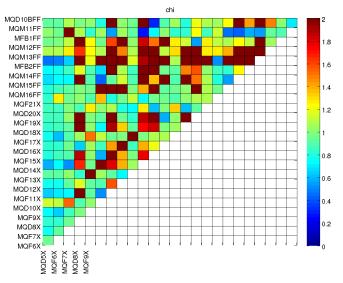
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# Squareness before BPM scale factors correction



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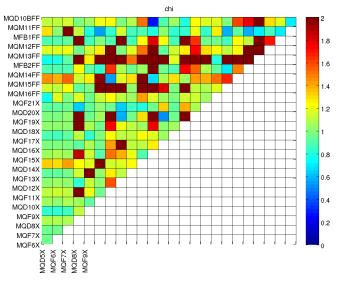
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# Squareness after BPM scale factors correction



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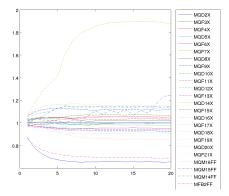
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# Vertical Scan

- Used ZV1X and ZV2X
- Vertical plane less sensitive to non linear fields
- 3σ scan
- 10% errors on scale factors found. (except MQD2X, MQD14X and MFB2FF)



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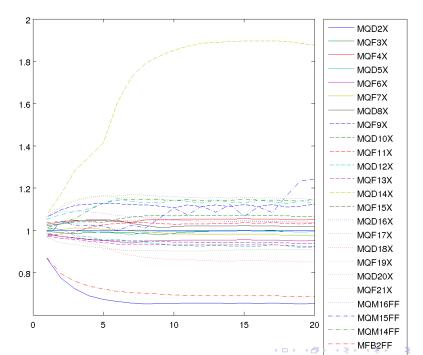
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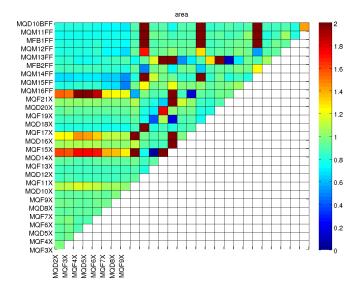
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# Area after BPM scale factors correction



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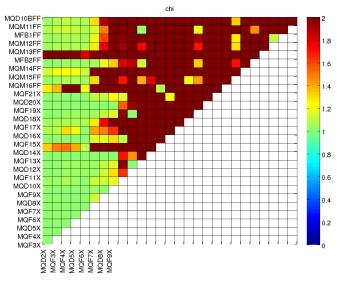
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# **Conclusions and Prospects**

## Conclusion

- Grid scans has been made at ATF2
- Might be used to determine BPM scale errors
- No evidence of any mismatch
- Some BPMs identified with bad scales

## Prospects

Improve scale factor fit method (any suggestions ?)

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