

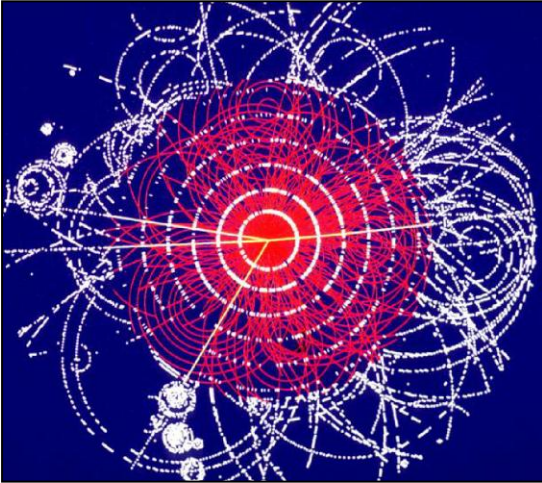
# Beam Instrumentation for Linear Collider

With a big “Thank You” to T. Lefevre for most of the splendid slides....

- Recap: Why Linear Collider ?
- What is special about the beam instrumentation of a Linear Collider ?
- What are the main Instruments ?

# Why do we need Leptons

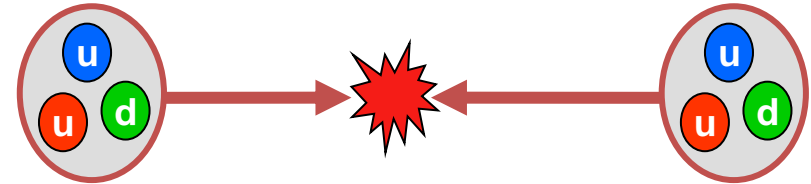
## Higgs event Simulation



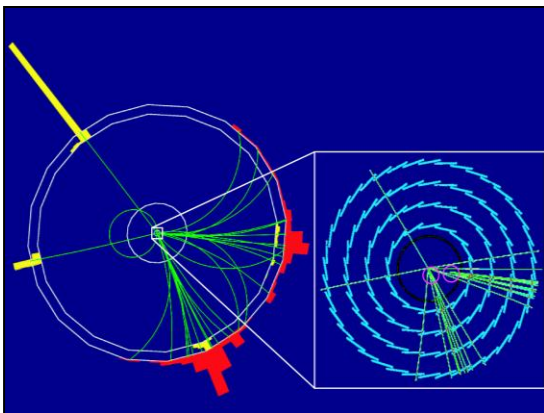
LHC

## Hadron Colliders (p, ions):

- Hadrons are composite objects



- Only part of proton energy available
- Huge QCD background



ILC

## Lepton Colliders:

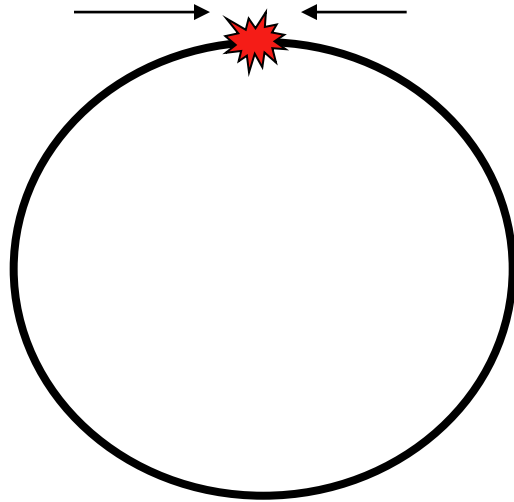
- Leptons are elementary particles



- Well defined initial state
- Momentum conservation eases decay product analysis
- Beam polarization



# What is the difference between Circular and Linear

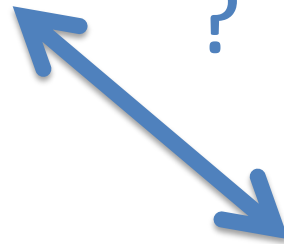


**Luminosity (number of collision)**  
**~ Machine repetition rate**

$$\text{LEP } f_{rep} = 11 \text{ kHz}$$

$$\text{ILC } f_{rep} = 5 \text{ Hz}$$

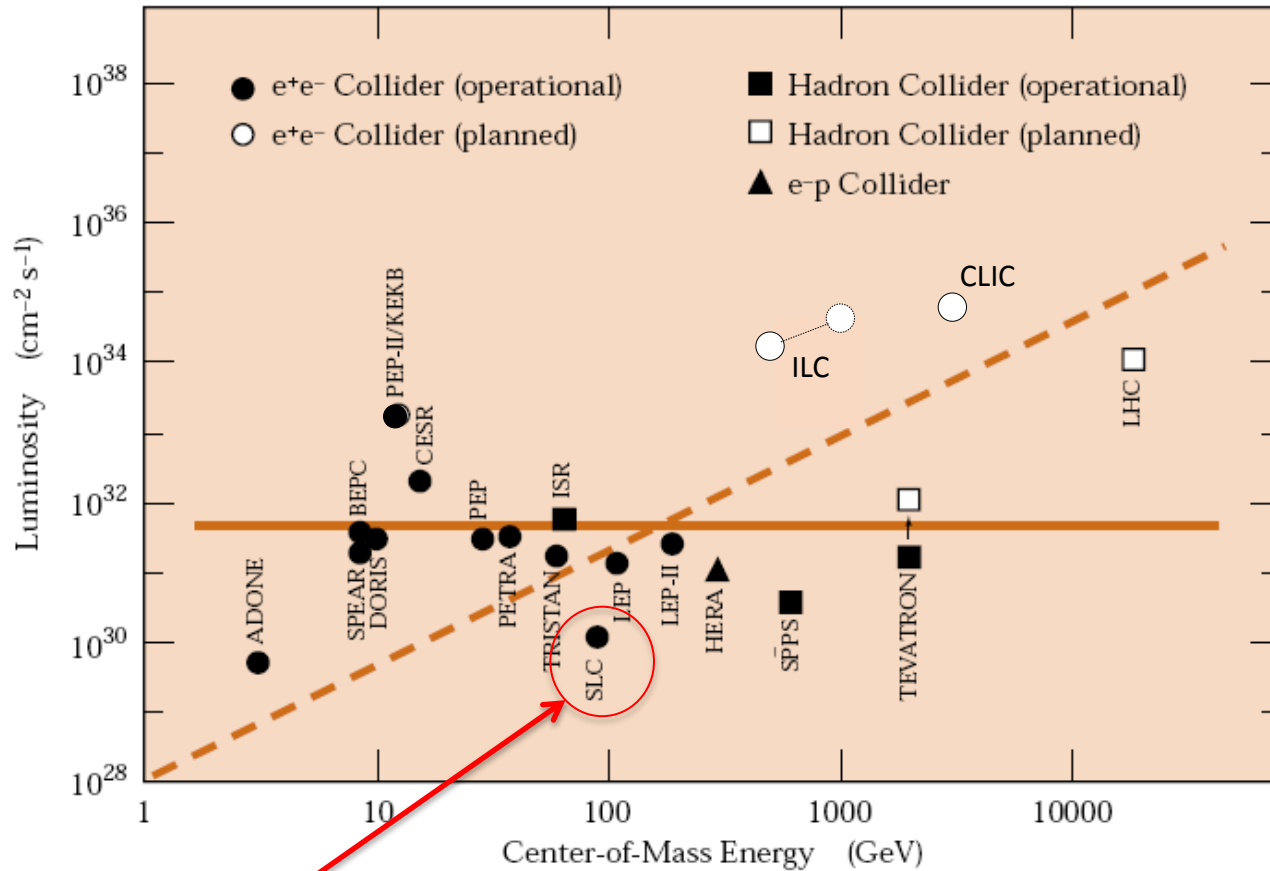
?  $\Rightarrow$  **factor 2200 in  $L$  already lost!**



**Linear Colliders are pulsed !!**

# Luminosity of high energy $e^+ e^-$ Collider

Particle physicists ask to increase Luminosity with energy...



SLAC Linear Collider

$E_{\text{cm}} = 92 \text{ GeV}$

$L = 3 \cdot 10^{30} \text{ cm}^{-2} \text{ s}^{-1}$

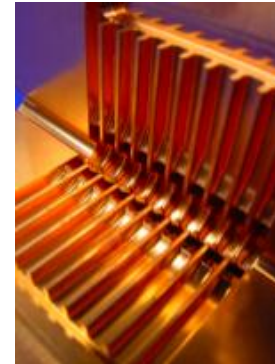
	Beams	Energy	Luminosity
<b>LEP</b>	$e^+ e^-$	200 GeV	$10^{32} \text{ cm}^{-2} \text{ s}^{-1}$
<b>LHC</b>	$p p$	14 TeV	$10^{34}$
	$Pb Pb$	1312 TeV	$10^{27}$

# What are the projects under-study ?



## FRIENDLY RIVALRY

*Nature 456,422, 27 Nov 08*



- 1.3 GHz supra conducting cavities
- Gradient 32 MV/m
- Energy: 500 GeV, though upgradable to 1.0 TeV

- 12GHz normal conducting cavities
- Gradient 100 MV/m
- Energy : 3 TeV

# Luminosity of high energy Collider

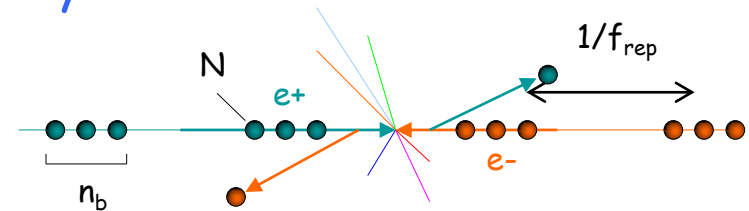
Collider luminosity [ $\text{cm}^{-2} \text{s}^{-1}$ ] is approximately given by

$$L = \frac{n_b N^2 f_{rep}}{4\pi\sigma_x^* \sigma_y^*} \times H_D$$

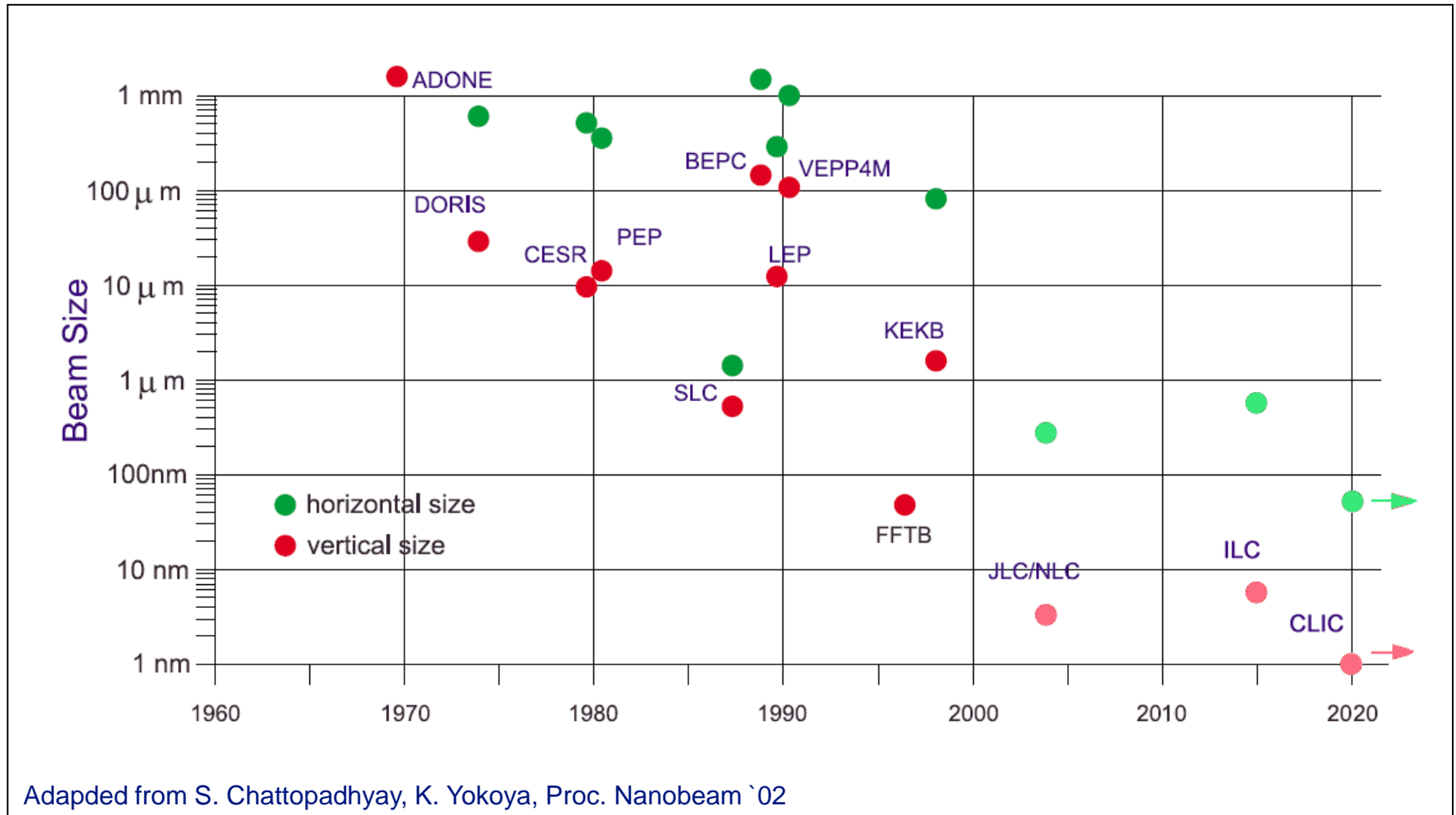
$n_b$  = bunches / train  
 $N$  = particles per bunch  
 $f_{rep}$  = repetition frequency  
 $\sigma_{x,y}$  = beam size at IP  
 $H_D$  = beam-beam enhancement factor

A linear collider uses the beam pulses only once:

- Need to accelerate lots of particles
- Need very small beam sizes



# The small beam size challenge



**LEP:**  $\sigma_x \sigma_y \approx 130 \times 6 \mu\text{m}^2$

**ILC:**  $\sigma_x \sigma_y \approx 500 \times (3-5) \text{nm}^2$



# Luminosity issue with intense beams - Disruption

Field of the opposite particle will distort the other beam during collision:

- Pinch effect (can become unstable if two strong)
- Beam-beam deflections – use to adjust beam overlap and luminosity

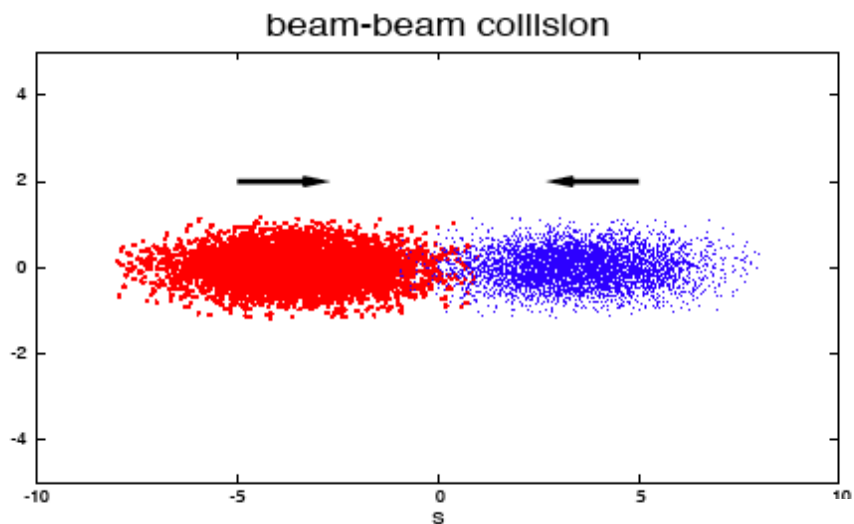
beam-beam characterised by **Disruption Parameter**:

$$D_{x,y} = \frac{2r_e N \sigma_z}{\gamma \sigma_{x,y} (\sigma_x + \sigma_y)} \quad \sigma_z = \text{bunch length}$$

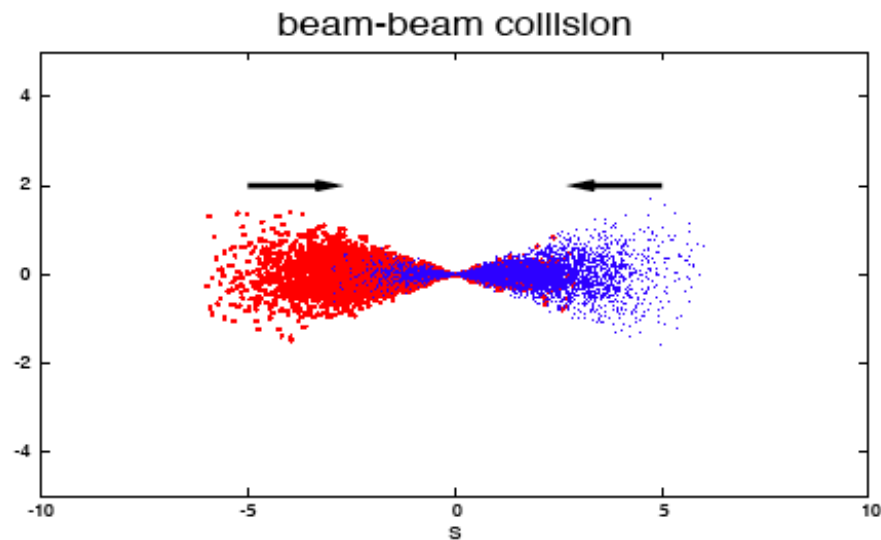
**Enhancement factor** (typically  $H_D \sim 1.5 \div 2$ ) is given by:

$$H_{Dx,y} = 1 + D_{x,y}^{1/4} \left( \frac{D_{x,y}^3}{1 + D_{x,y}^3} \right) \left[ \ln(\sqrt{D_{x,y}} + 1) + 2 \ln \left( \frac{0.8 \beta_{x,y}}{\sigma_z} \right) \right]$$

# Luminosity issue with intense beams - Disruption

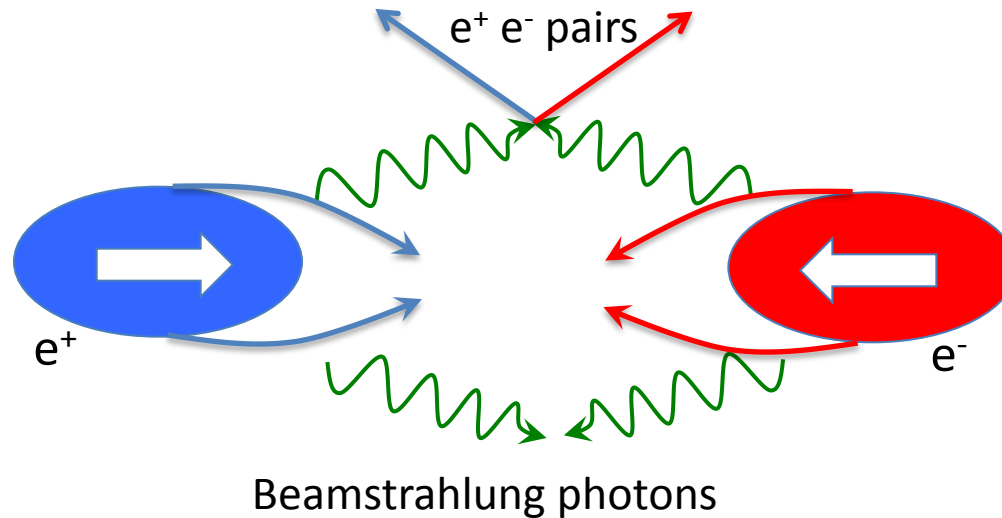


For LC, typical value of HD  $\sim$  1-2



# Luminosity issue with intense beams - Beamstrahlung

- Generation of Synchrotron Radiation photons of particles in the strong EM field of the opposite bunch



- High energy Beamstrahlung photons can convert in strong field into  $e^+/e^-$  pairs: background for the detector

## Coherent $e^+e^-$ pairs

- Direct photons conversion in strong fields
- Negligible for ILC but high for CLIC : Few  $10^8$  particles per Bunch crossing

## Incoherent $e^+e^-$ pairs

- Photons interacting with other electron/photon
- Few  $10^5$  particles/Bunch crossing

# Beam size for minimizing beamstrahlung

rms relative energy loss  
induced by Beamstrahlung

$$\delta_{BS} = 0.86 \frac{er_e^3}{2m_0c^2} \left( \frac{E_{cm}}{\sigma_z} \right) \frac{N^2}{(\sigma_x + \sigma_y)^2}$$

we would like to make  $(\sigma_x \sigma_y)$  small to maximise luminosity

and keep  $(\sigma_x + \sigma_y)$  large to reduce  $\delta_{BS}$

Trick: use “flat beams” with  $\sigma_x \gg \sigma_y$

$$\delta_{BS} \propto \left( \frac{E_{cm}}{\sigma_z} \right) \frac{N^2}{\sigma_x^2}$$

## Rule:

- Make  $\sigma_x$  large to limit  $\delta_{BS}$
- Make  $\sigma_y$  as small as possible to achieve high luminosity.



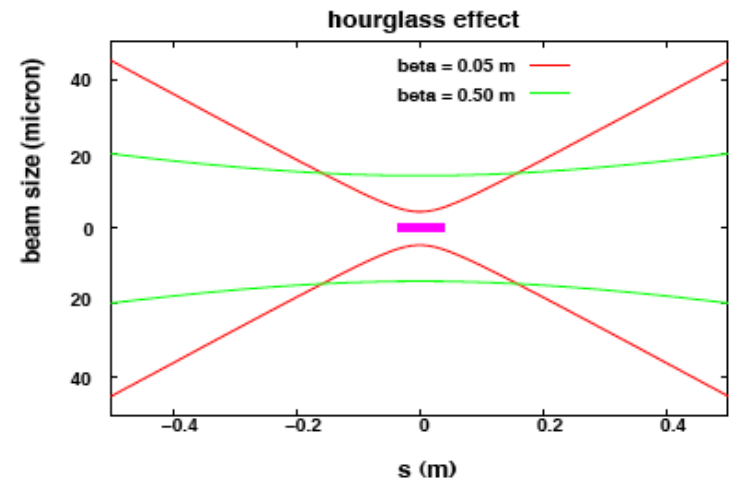
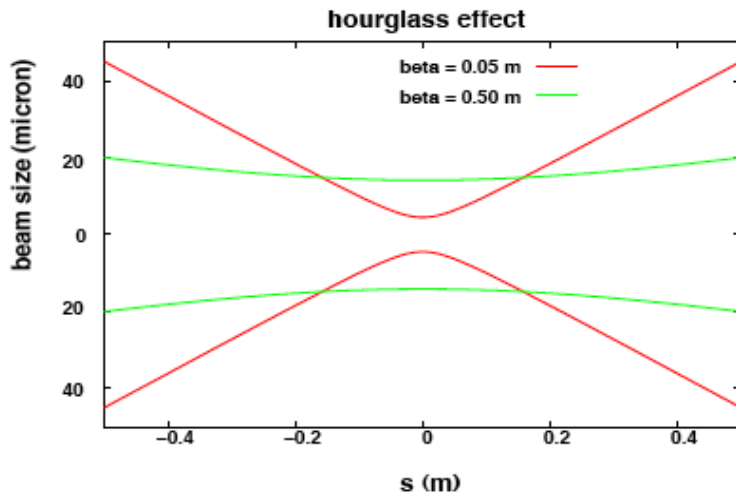
$$\delta_{BS} \sim 2.4\% \text{ @ ILC -- } \delta_{BS} \sim 29\% \text{ @ CLIC}$$

# Hour glass effect – Bunch length

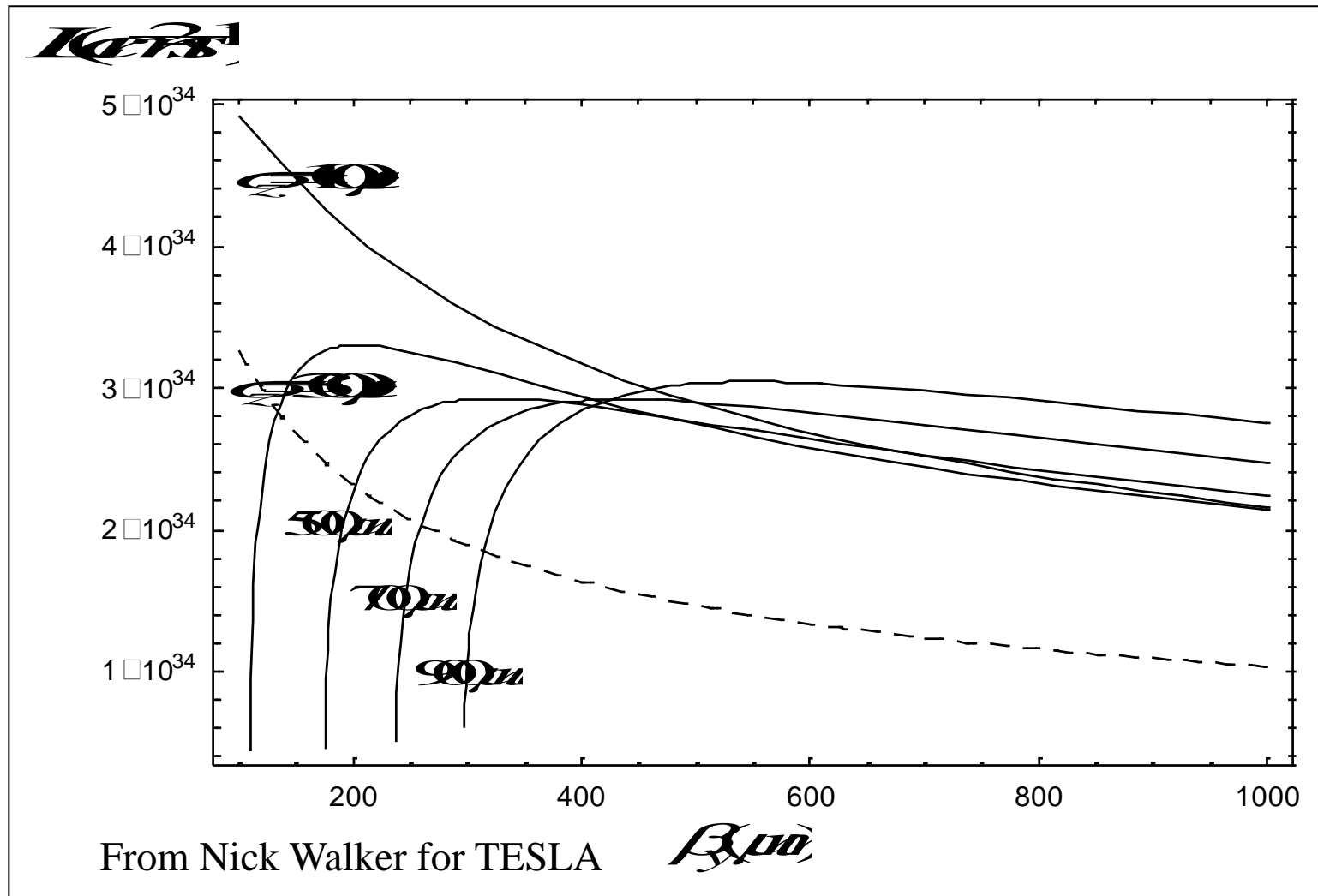


For achieving small Beta function ( small beam size) at IP, the beta function rapidly increases as the particle move away from the collision point

Variation of beam size along the bunch



# Hour glass effect – Bunch length



**Rule:** Keep  $\beta_y \sim \sigma_z$

# A final luminosity scaling for Linear collider ?

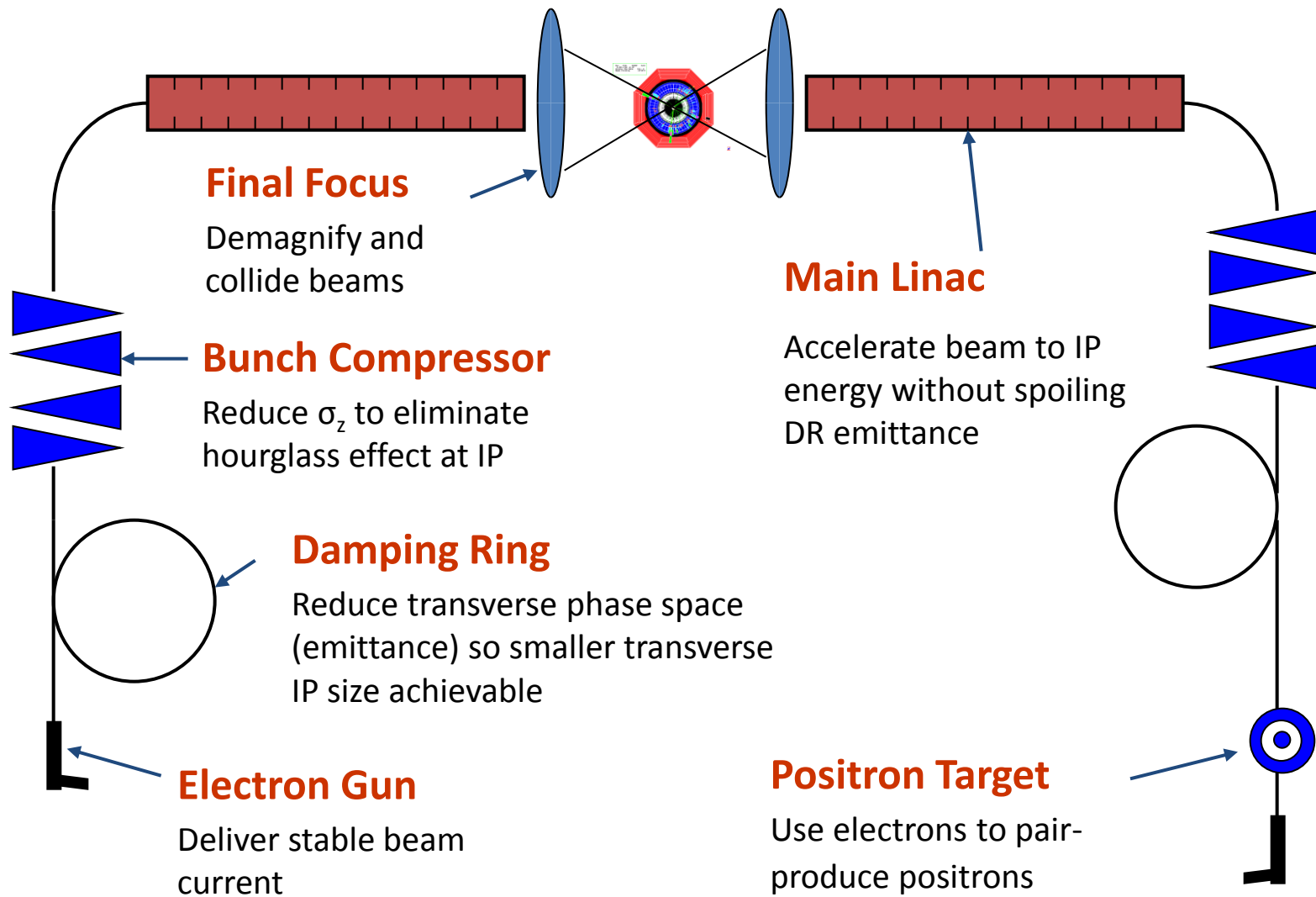
$$L \propto \frac{\eta_{RF} P_{RF}}{E_{cm}} \sqrt{\frac{\delta_{BS}}{\varepsilon_{n,y}}} H_D \quad \text{with} \quad \beta_y \approx \sigma_z$$

- high RF-beam conversion efficiency  $\eta_{RF}$  and RF power  $P_{RF}$
- **small normalised vertical emittance  $\varepsilon_{n,y}$**
- **strong focusing at IP (small  $\beta_y$  and hence small  $\sigma_z$ )**



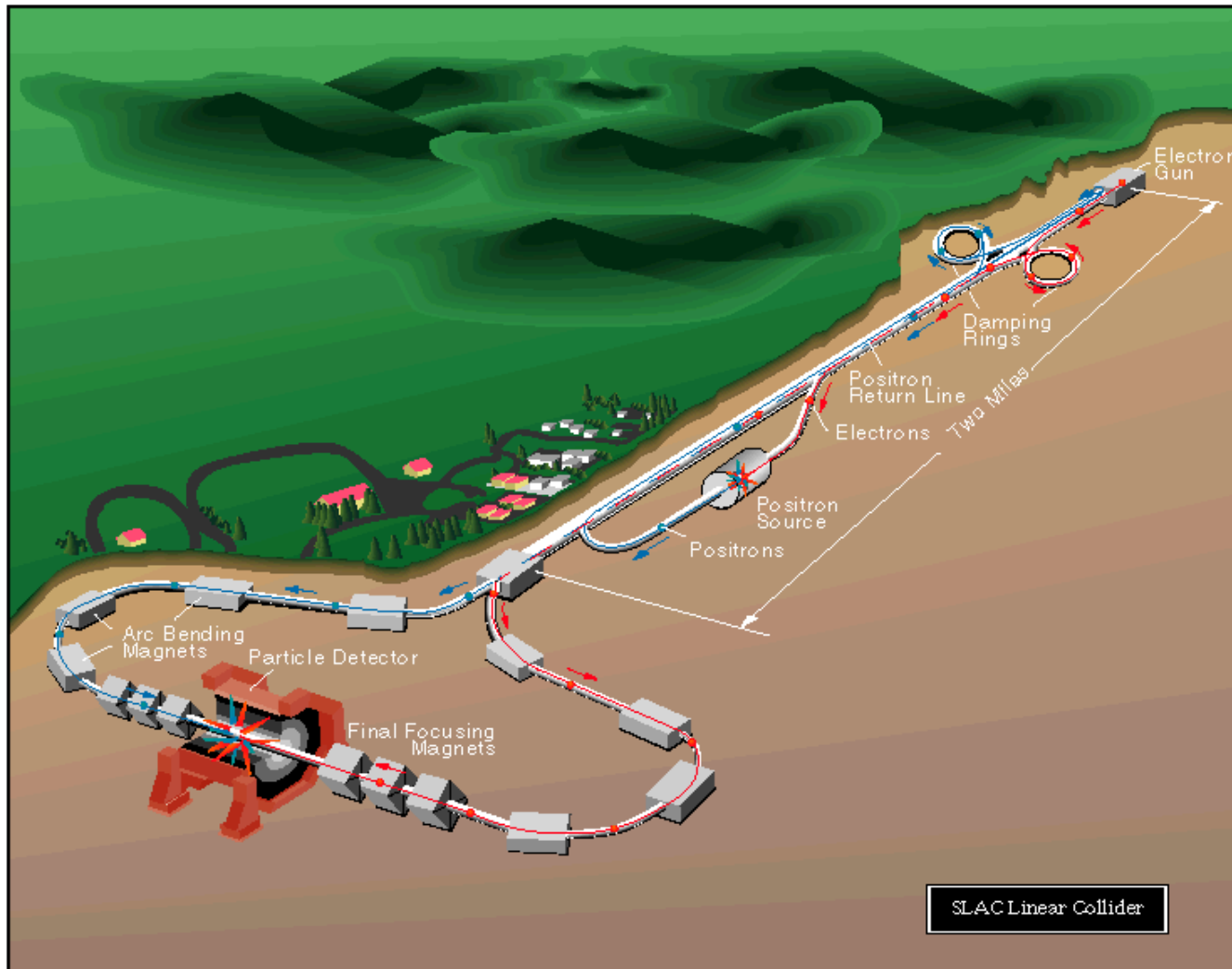
- Extremely small beam spot at Interaction Point beam delivery system,
  - Generation of small emittance
  - Conservation of small emittance
- Generation and acceleration of short bunches

# What would a future Linear collider look like ?





# Lesson from the first Linear collider : SLC



Built to study the  $Z_0$  and demonstrate linear collider feasibility

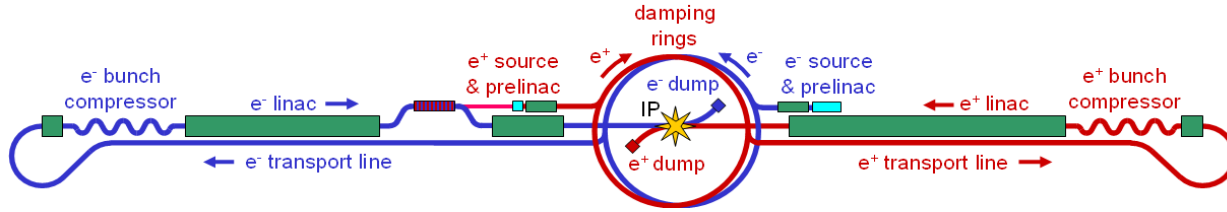
Single bunch

Energy = 92 GeV

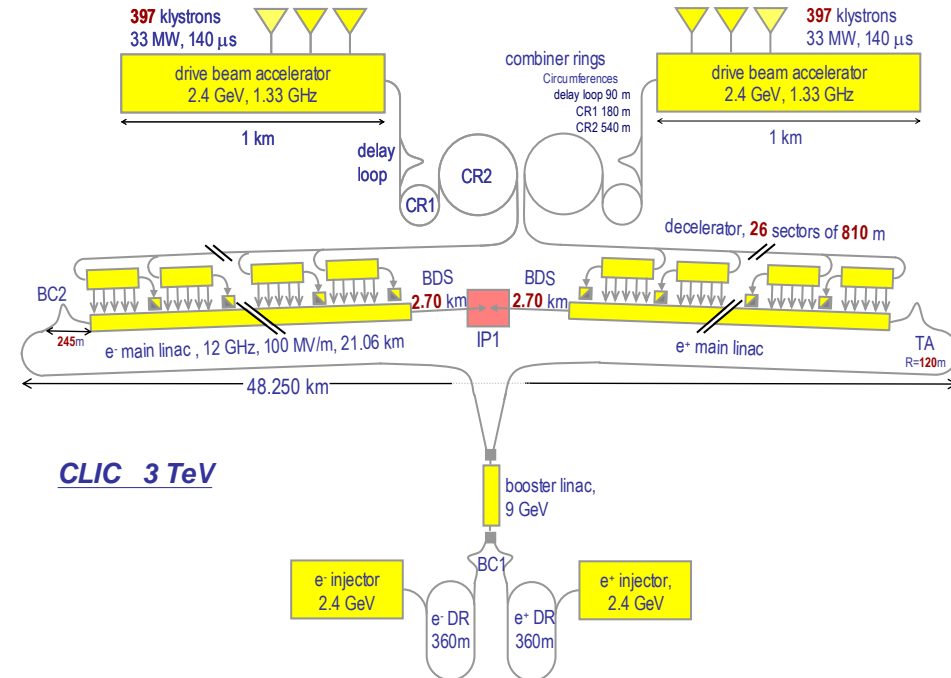
Luminosity =  $3e30$

Had all the features of a 2nd gen. LC except both  $e^+$  and  $e^-$  shared the same linac

# International Linear Collider / Compact Linear Collider



		CLIC	CLIC	ILC
$E_{cms}$	[TeV]	0.5	3.0	0.5
$f_{rep}$	[Hz]	50	50	5
$f_{RF}$	[GHz]	12	12	1.3
$G_{RF}$	[MV/m]	80	100	31.5
$n_b$		354	312	2625
$\Delta t$	[ns]	0.5	0.5	369
$N$	[ $10^9$ ]	6.8	3.7	20
$\sigma_x$	[nm]	202	40	655
$\sigma_y$	[nm]	2.26	1	5.7
$\epsilon_x$	[ $\mu\text{m}$ ]	2.4	0.66	10
$\epsilon_y$	[nm]	25	20	40
$\mathcal{L}_{total}$	[ $10^{34}\text{cm}^{-2}\text{s}^{-1}$ ]	2.3	5.9	2.0
$\mathcal{L}_{0.01}$	[ $10^{34}\text{cm}^{-2}\text{s}^{-1}$ ]	1.4	2.0	1.45



**CLIC 3 TeV**

# Main Instrumentation challenge for Linear Collider

- Measuring small emittance and small beam size  
~ 1 $\mu$ m spatial resolution Transverse Profile Monitors
- Measuring Short bunch length  
~ 20fs time resolution Longitudinal Profile Monitors
- Conservation of emittance over long distances relies on precise alignment  
high accuracy (5 $\mu$ m) high resolution (50nm) Beam Position Monitor



Not talking about Damping rings Beam size monitor (lectures by Volker) using Synchrotron radiation (Interferometer, P-Polarisation, X-ray imaging systems)

# Measuring small beam size in a Linear Collider

- Required high precision from the Damping ring to the Interaction Point (IP)
  - Beam energy ranges from 2.4GeV  $\rightarrow$  1.5TeV
  - Tens of km of beam lines – Big number of instruments

- Flat Beams ( $\varepsilon_x \gg \varepsilon_y$ ) : Think of a flat noodle !



- Small beam size
- High beam charge



High Charge Densities

$> 10^{10}$  nC/cm<sup>2</sup>

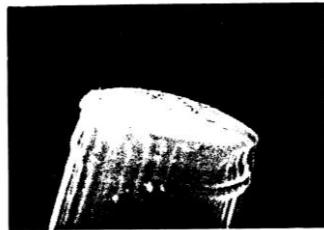
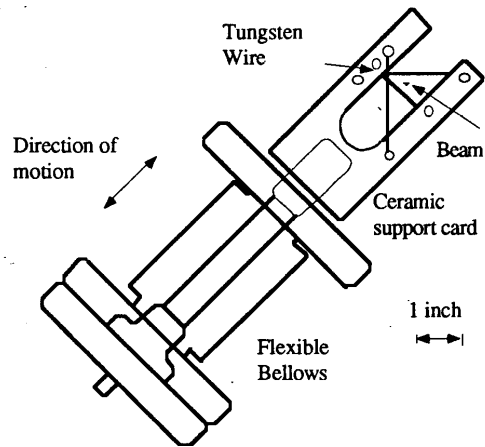
	ILC	CLIC
Beam Charge (nC)	7875	190
Hor. Emittance (nm)	655	40
Ver. Emittance (nm)	5.7	1



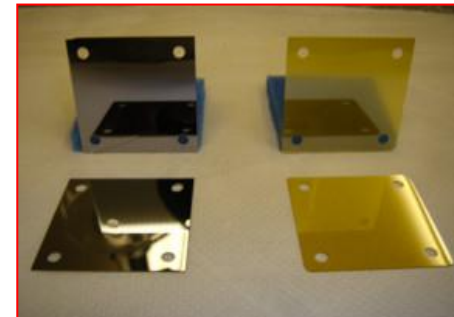
The thermal limit for 'best' material (C, Be, SiC) is  $10^6$  nC/cm<sup>2</sup>

# 'Beam Profile Horror Picture Show'

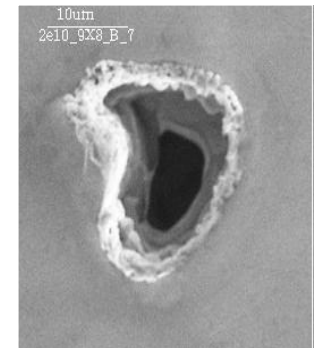
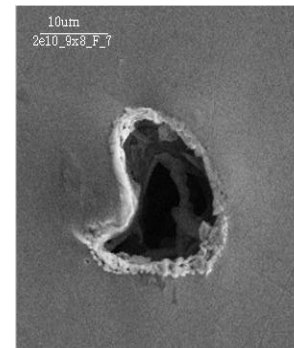
## Wire Scanner



## Optical Transition Radiation



200µm thick mirror polished Si and CVD SiC wafer



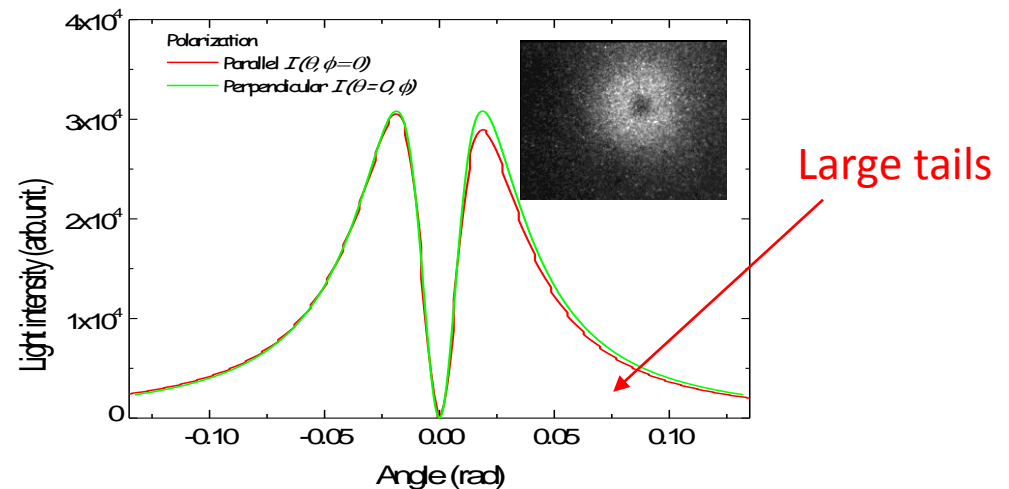
Intercepting devices limited to single (or few) bunch mode

# High Resolution Imaging System using OTR

- Diffraction effect would determine the resolution limit of the measurements

$$\Delta x \geq \frac{\lambda \text{ (wavelength)}}{\theta \text{ (useful opening angle)}}$$

- OTR angular distribution: Peak at  $1/\gamma$  but large tails
- Problem for very high energy particles



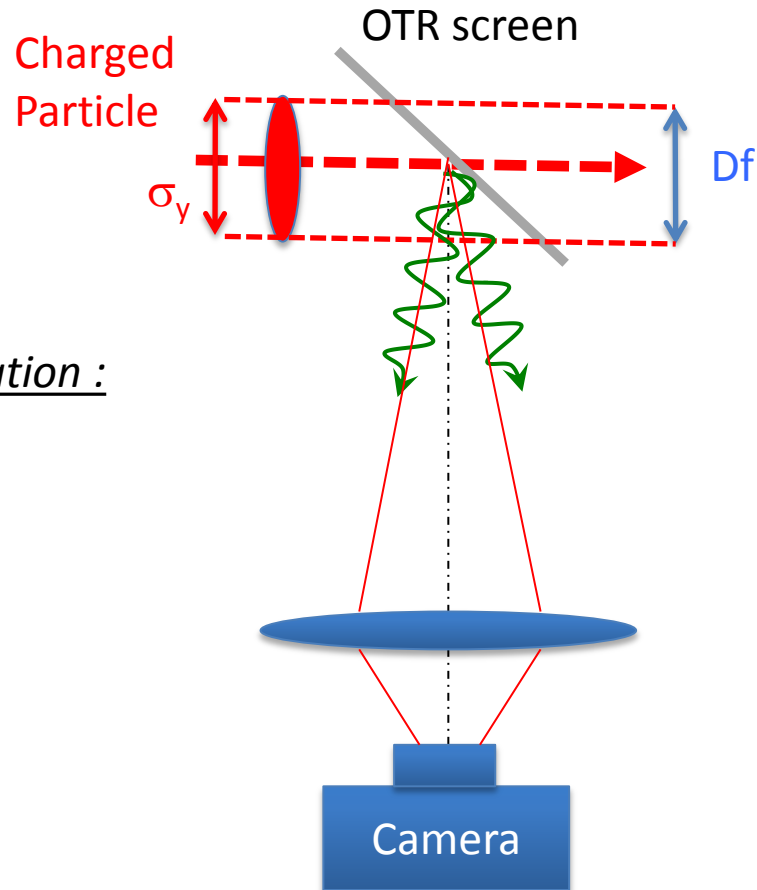
- Aperture of the focussing lens :  $\theta \gg 1/\gamma$

X. Artru et al, **NIM AB 145 (1998) 160-168**

C. Castellano and V.A. Verzilov, **Physical Review STAB 1, (1998) 062801**

# High Resolution Imaging System using OTR

- Depth of field limits the resolution because the image source is not normal to the optical axis

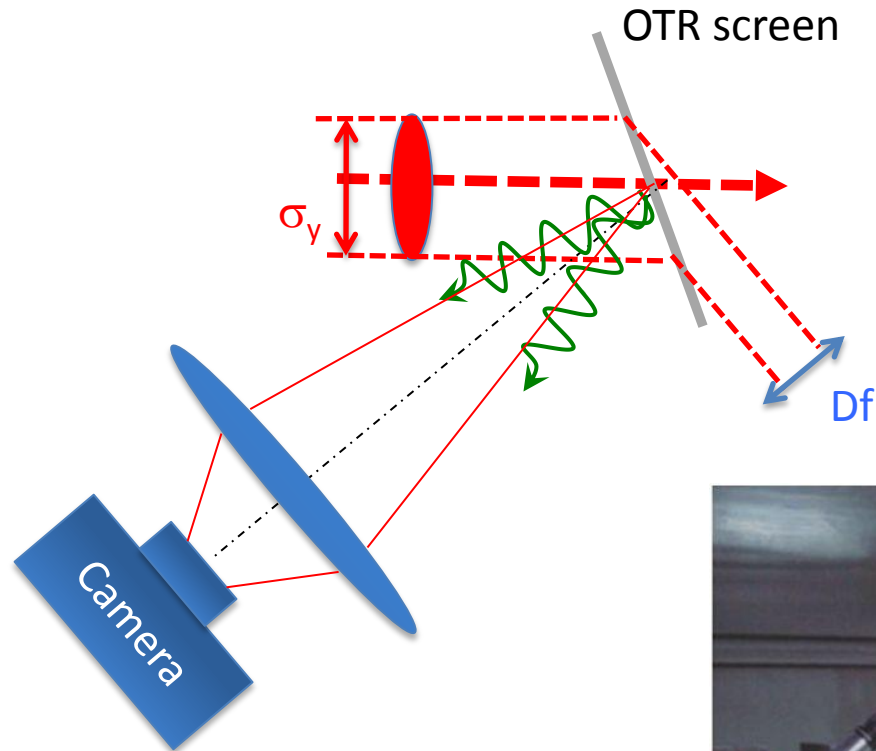


Classical OTR configuration :  
90° observation angle

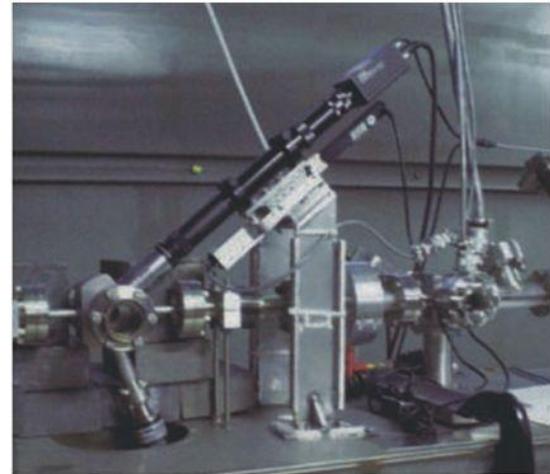
Make  $Df > \sigma_y$

# High Resolution Imaging System using OTR

- Imaging small beam size  $\rightarrow$  large magnification  $\rightarrow$  short Depth of field (Df)



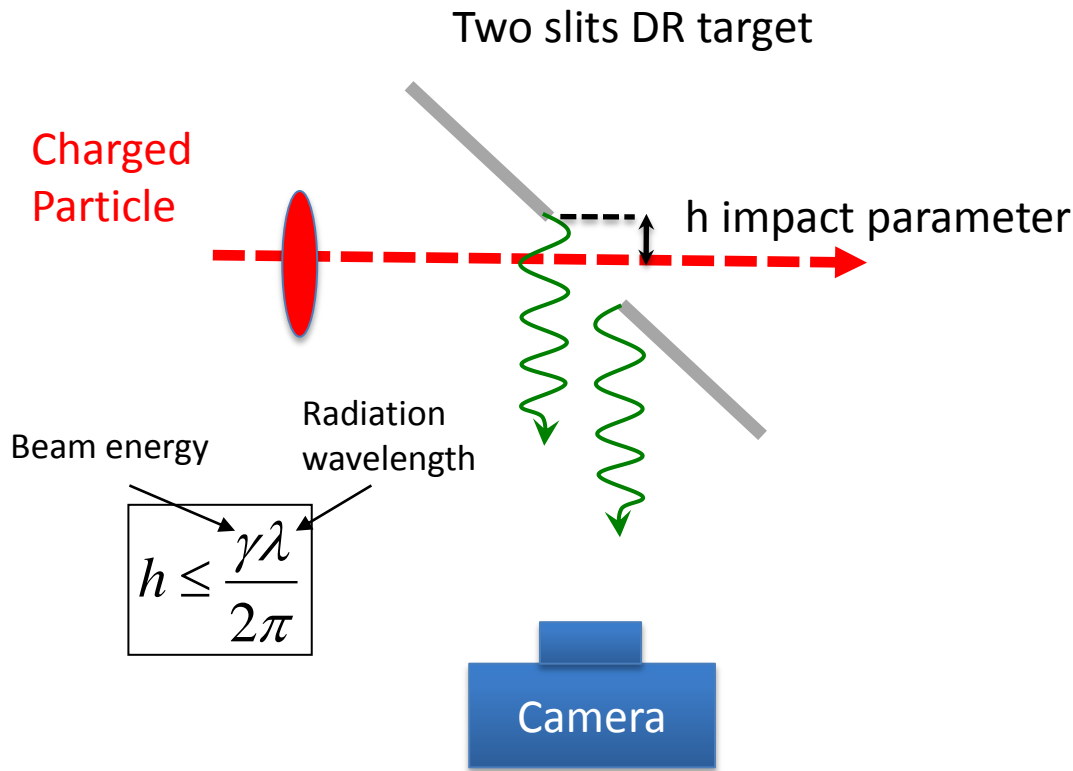
Smaller Df  $\rightarrow$  Tilt the screen



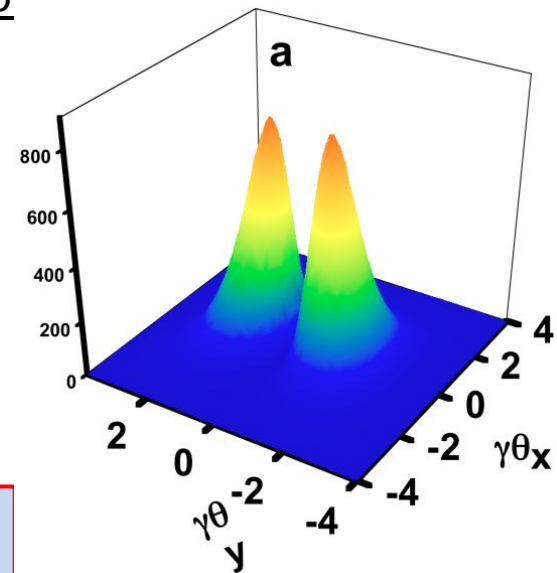


# Beam size monitoring with Diffraction Radiation

- Non destructive alternative for beam size measurement (not imaging anymore)



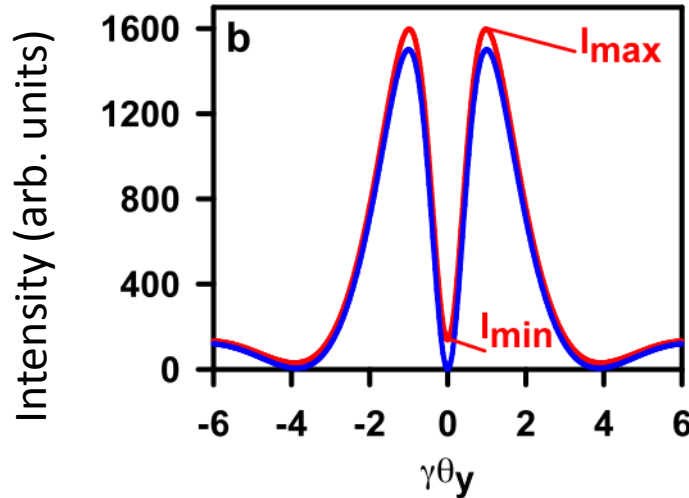
Measuring the angular distribution of the interference pattern between the DR emitted by the two



After the Damping ring the beam has few GeV and ODR is generated for reasonable values of  $h$

# Beam size monitoring with Diffraction Radiation

- Sensitivity to beam size is given by the visibility of the interference pattern
- Vertical (hor) polarization component depends on the vertical (hor) beam size



$$\sigma_y = 0$$

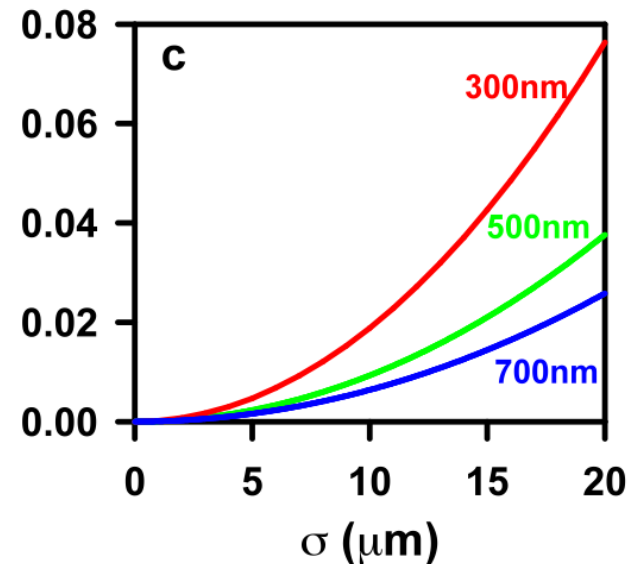
$$\sigma_y = 30 \mu\text{m}$$

- The visibility strongly depends on the wavelength with an beam size sensitivity limit as follows

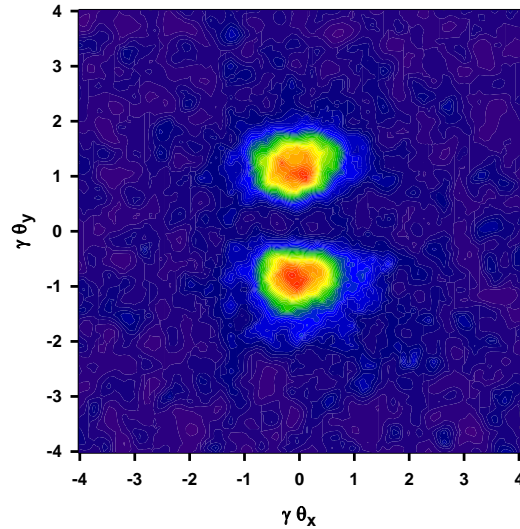
$$\sigma > 0.05 \frac{\gamma\lambda}{2\pi}$$



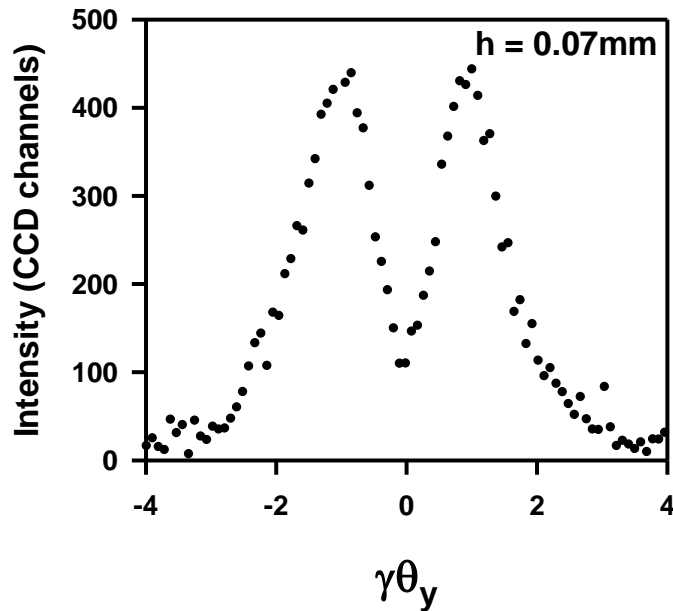
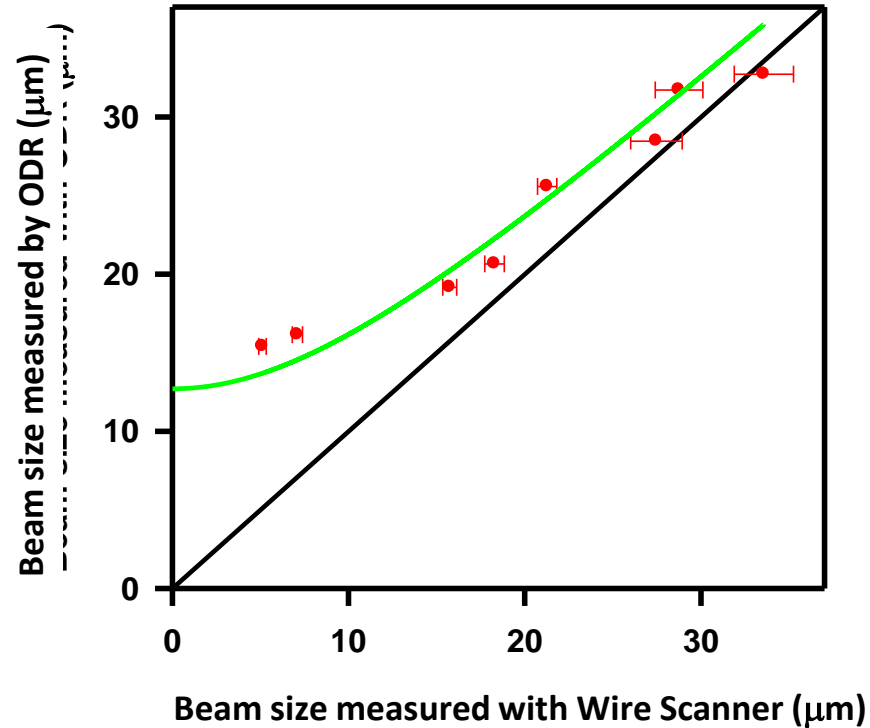
GO for short wavelength



# Beam size monitoring with Diffraction Radiation



Investigation on the low emittance beam at ATF, KEK, Japan  
 $E=1.28\text{GeV}$  ;  $\lambda=445\text{nm}$  ;  $h=70\mu\text{m}$



P. Karataev et al., Physical Review Letters **93** (2004) 244802  
P. Karataev et al, Physical Letters **A345** (2005) 428

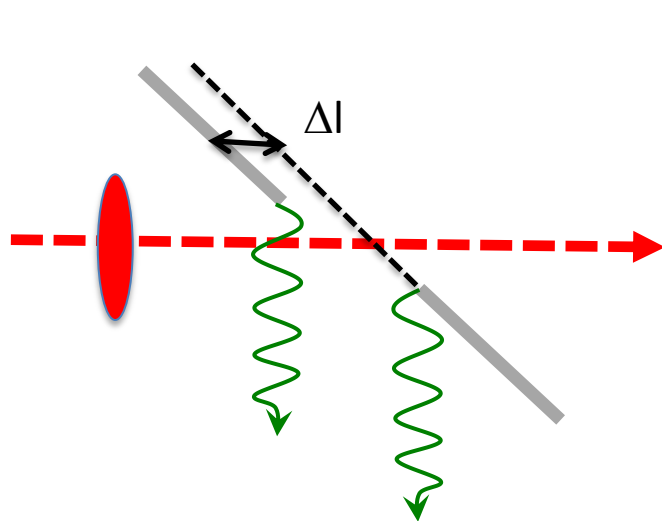
# Beam size monitoring with Diffraction Radiation

- Push the technology in the EUV regime ( $\sim 100\text{nm}$ ) to bring the resolution in the  $1\text{-}10\mu\text{m}$  range
- Not usable for ultra-high beam energy :  $>10\text{GeV}$



*Used in Linear collider from the Damping to the Main Linac (40kms of beam line -  $\sim 70$  Devices in CLIC)*

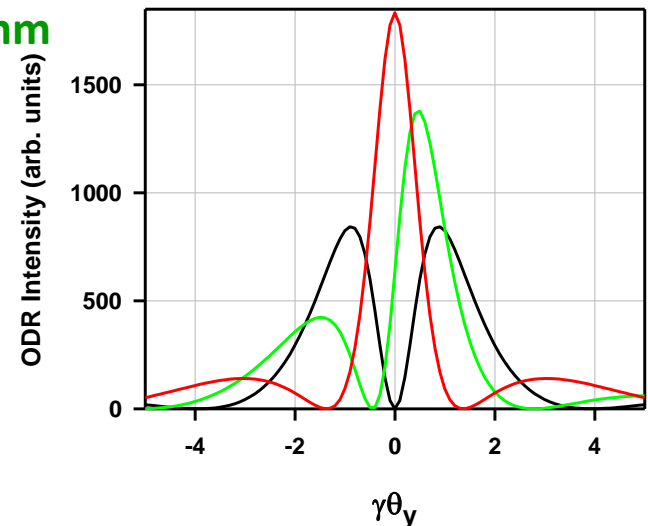
- Mechanical challenge for the slit technology



$$\Delta l = 0$$

$$\Delta l = \lambda/10 \sim 10\text{nm}$$

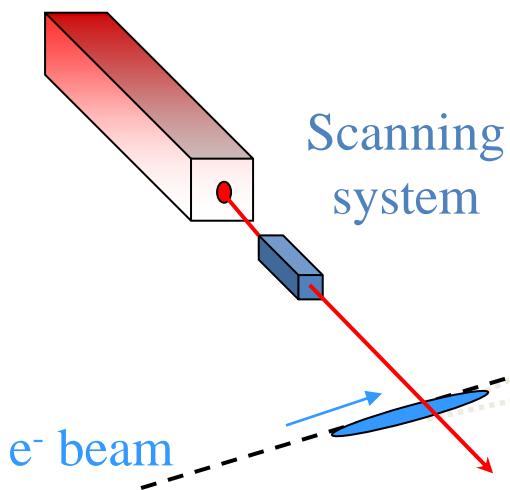
$$\Delta l = \lambda/4$$



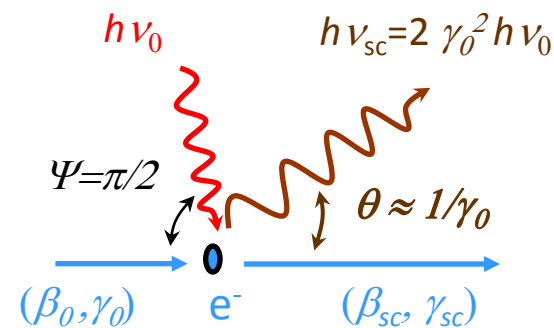
# Beam size monitoring with Laser Wire Scanner

Baseline solution for linear collider: high spatial resolution would rely on Laser Wire Scanner

High power laser



Thomson/Compton scattering



# Beam size monitoring with Laser Wire Scanner

## Laser Beam

$\lambda_0$  : Laser wavelength

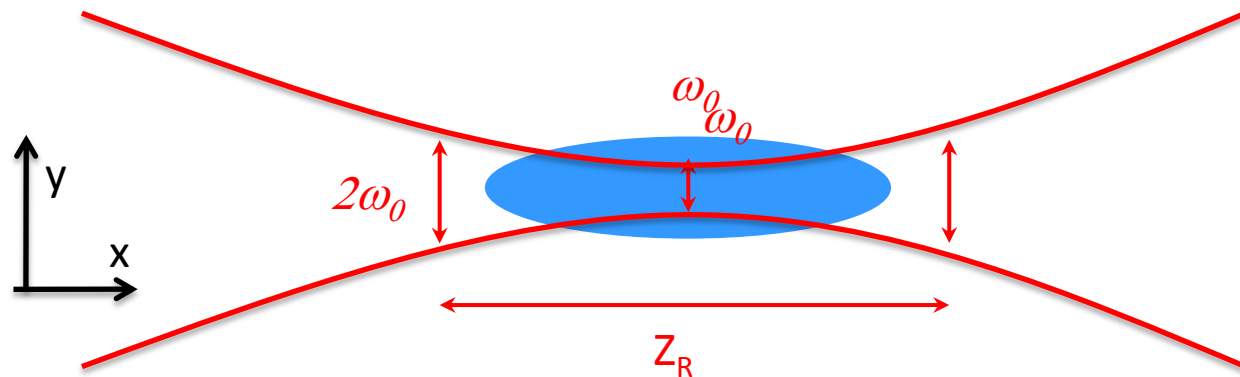
$\omega_0$  : Laser waist size

$Z_R$  : Rayleigh range

## Electrons Beam

$\sigma_y$  : ver. beam size

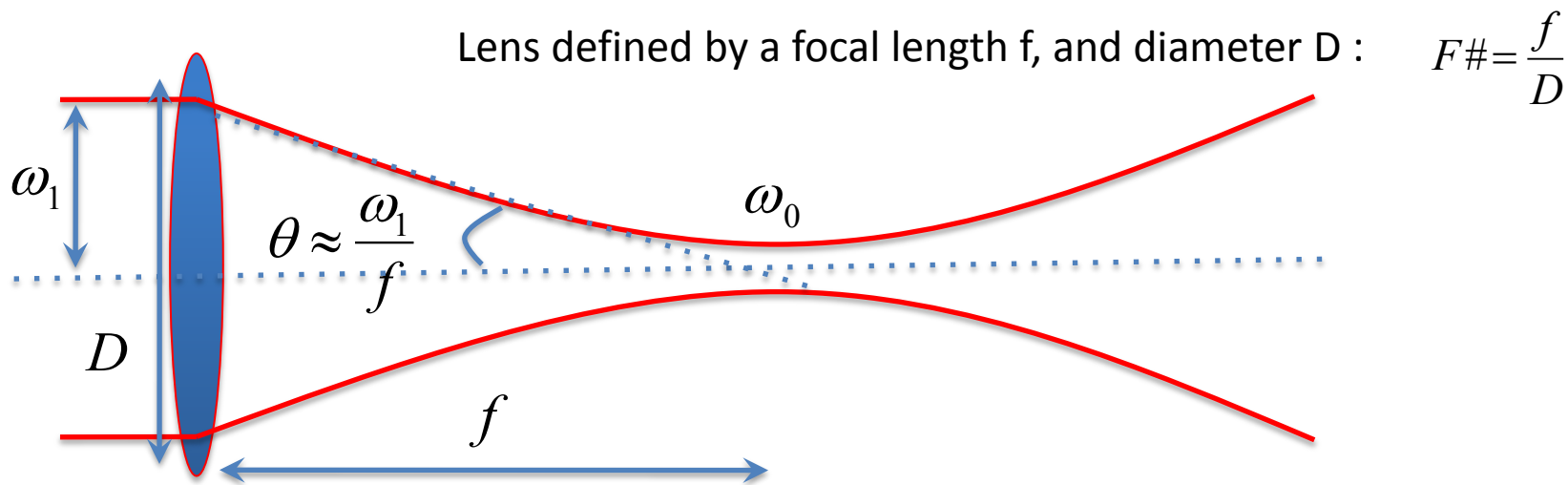
$\sigma_x$  : hor. beam size



- The number of X-rays produced is given by 
$$N_{\text{interaction}} \approx \frac{\sigma \cdot N_e \cdot N_{\text{laser}}}{A}$$
 with  $A$  the interaction area,  $N_e$  and  $N_{\text{laser}}$  are the number of electrons and photons in  $A$

# Beam size monitoring with Laser Wire Scanner

- High spatial resolution need very focused laser beam: Need a optimum Focusing system



Performance of Laser :  $M^2=1$  for pure Gaussian distribution

- Diffraction  $\omega_{diffraction} = \frac{M^2 \lambda}{\pi \theta} \approx \frac{M^2 \lambda}{\pi} F\#$

Smaller  $F\#$  is better

- Spherical aberration  $\omega_{spher} \propto \frac{D}{2F\#^2}$

For the single lens,  
small  $F\#$  makes spherical aberration large.



Minimize spherical aberration using several lenses

# Beam size monitoring with Laser Wire Scanner

*Design for ATF2 LWS by G. Blair et al*

$F\# = 2$

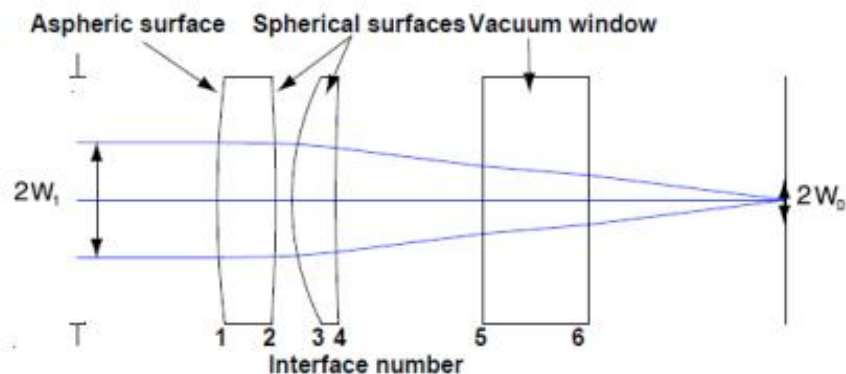


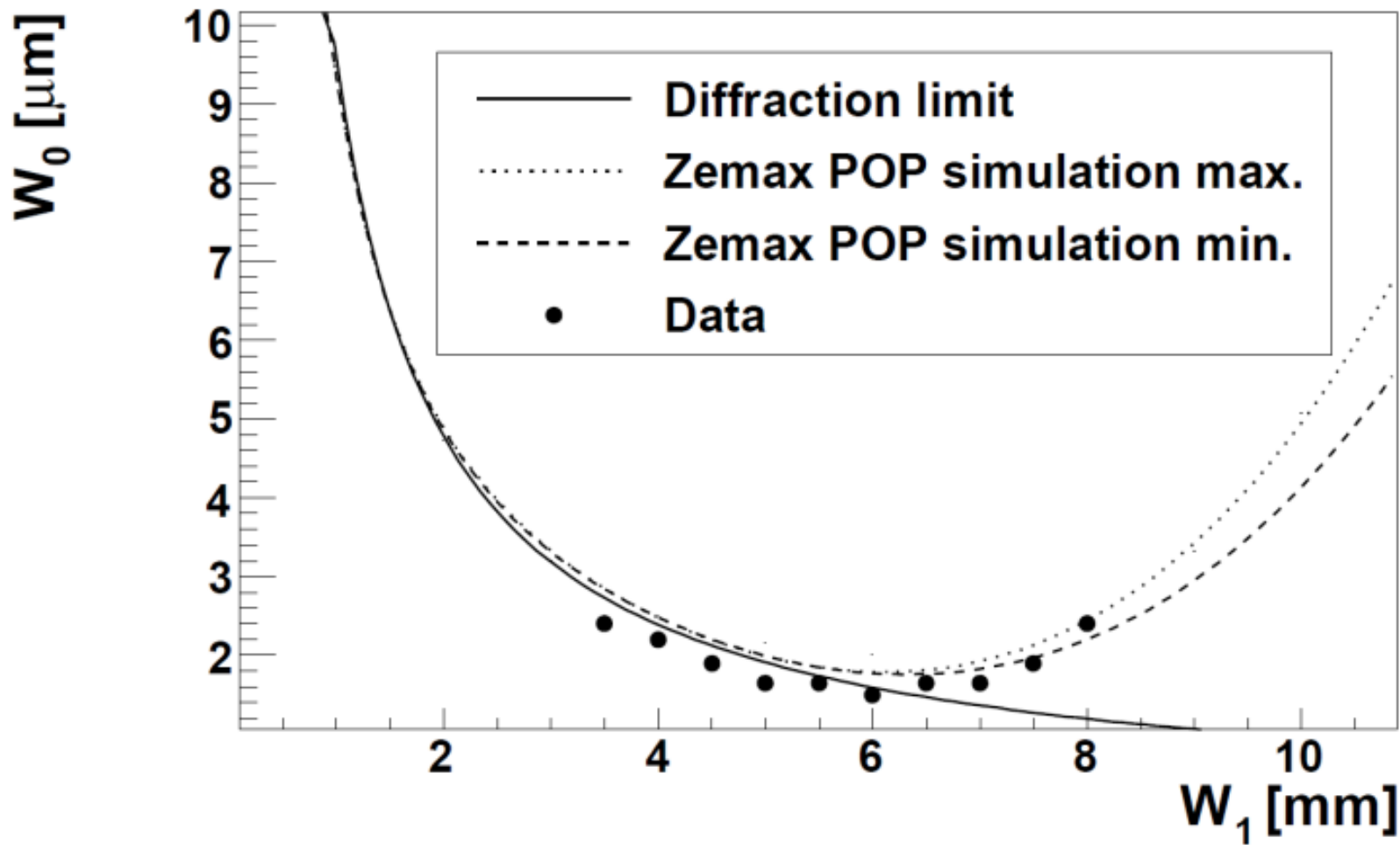
FIG. 7. Color online. Diagram of the final focus lens.

Interface number	Shape	Radius [mm]	Thickness [mm]	From	To
1	Even asphere	117.126106	7.093310	Air	Silica
2	Spherical	-250.070725	1.987140	Silica	Air
3	Spherical	33.118324	5.309160	Air	Silica
4	Spherical	274.998672	17.985135	Silica	Air
5	Spherical	Infinity	12.700000	Air	Silica
6	Spherical	Infinity	24.075710	Silica	Vacuum



# Beam size monitoring with Laser Wire Scanner

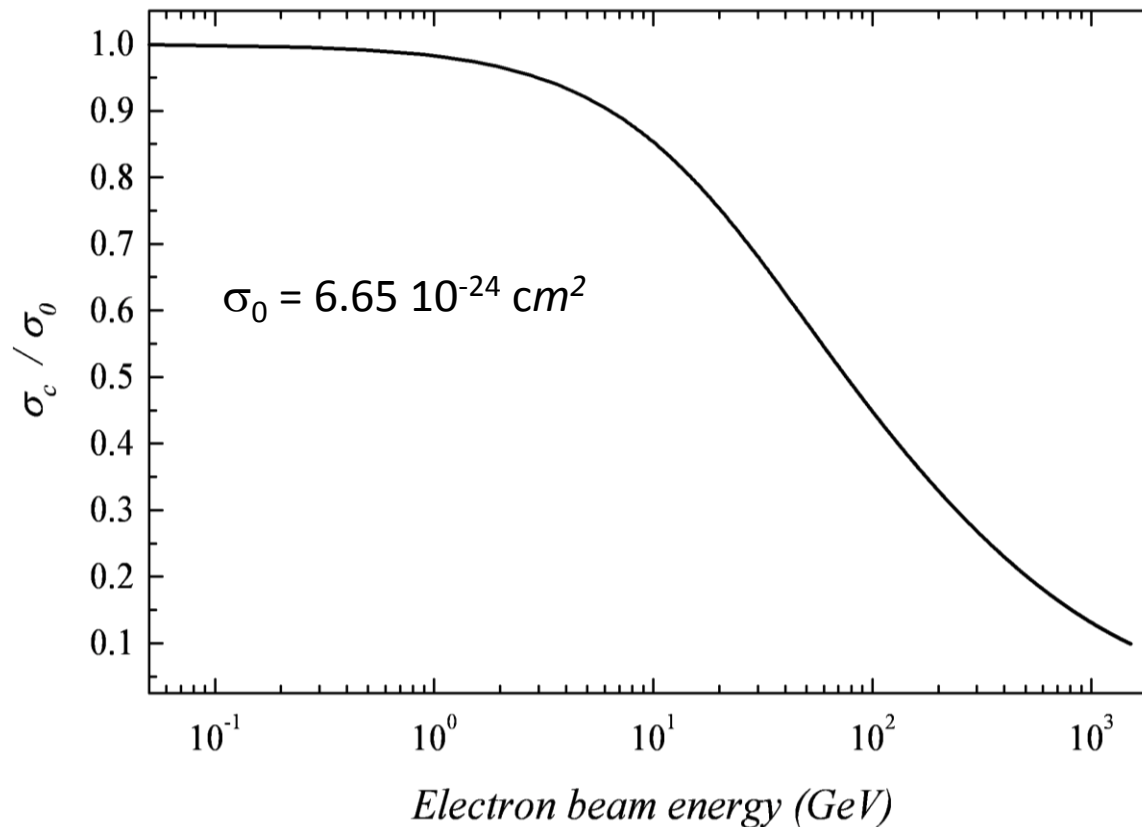
*Design for ATF2 LWS by G. Blair et al*



GO to smaller wavelength to do better (green  $\rightarrow$  UV)

# Beam size monitoring with Laser Wire Scanner

- At high energy, the Compton cross section gets smaller



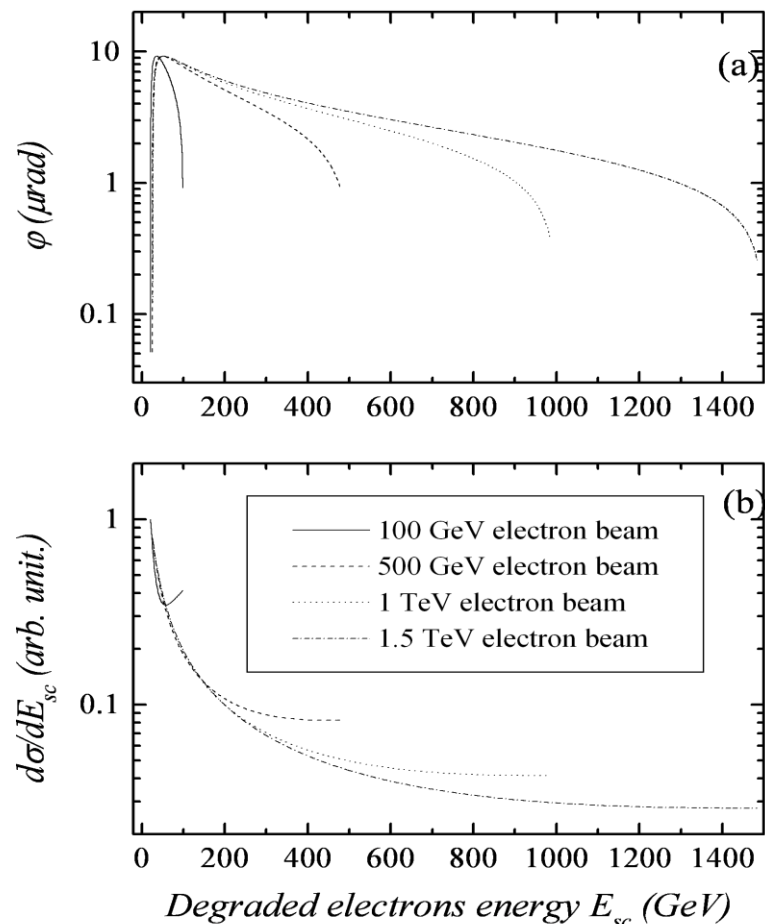
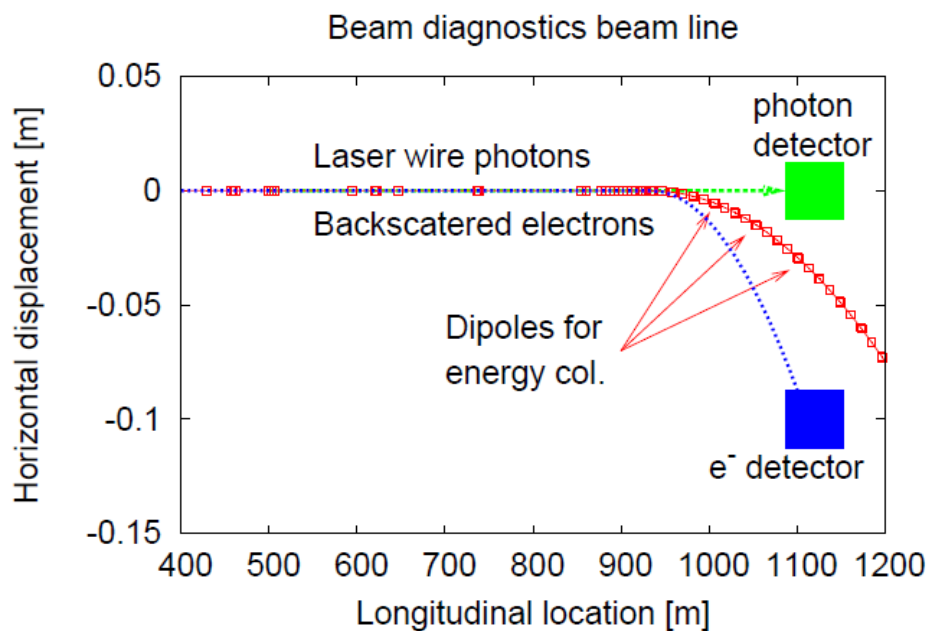
- The number of interaction produced is given by  $N_{\text{interaction}} \propto \sigma \cdot N_e \cdot N_{\text{laser}}$



Increase the Laser Power (10MW and more)

# Beam size monitoring with Laser Wire Scanner

- At high energy ( $>10\text{GeV}$ ) the detection system can be easily done either using the scattered photons or the scattered electrons



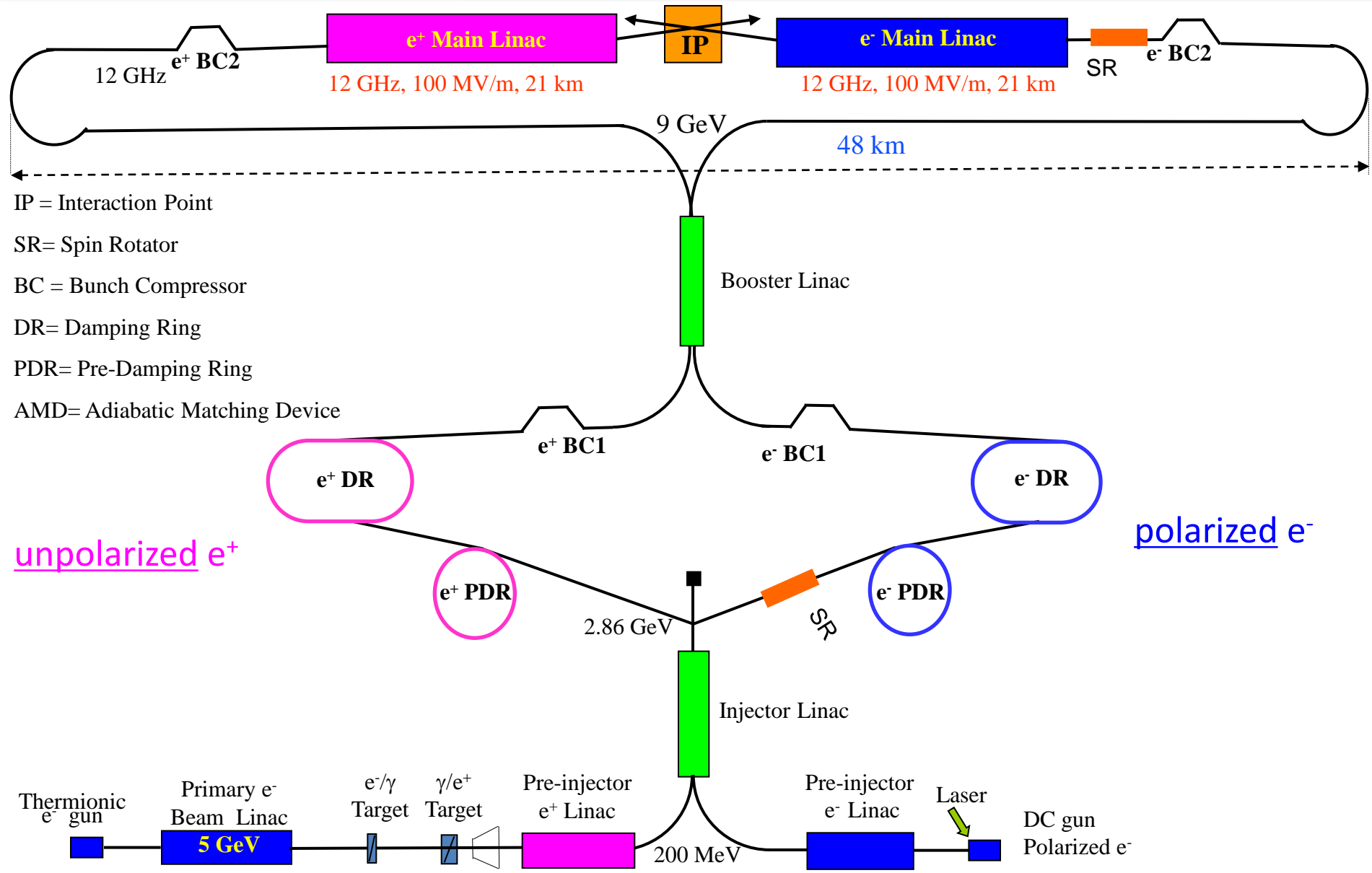
# Measuring Short bunches with femtosecond time resolution

- Want capability of compressing by a factor 50: Done in two steps to avoid emittance dilution

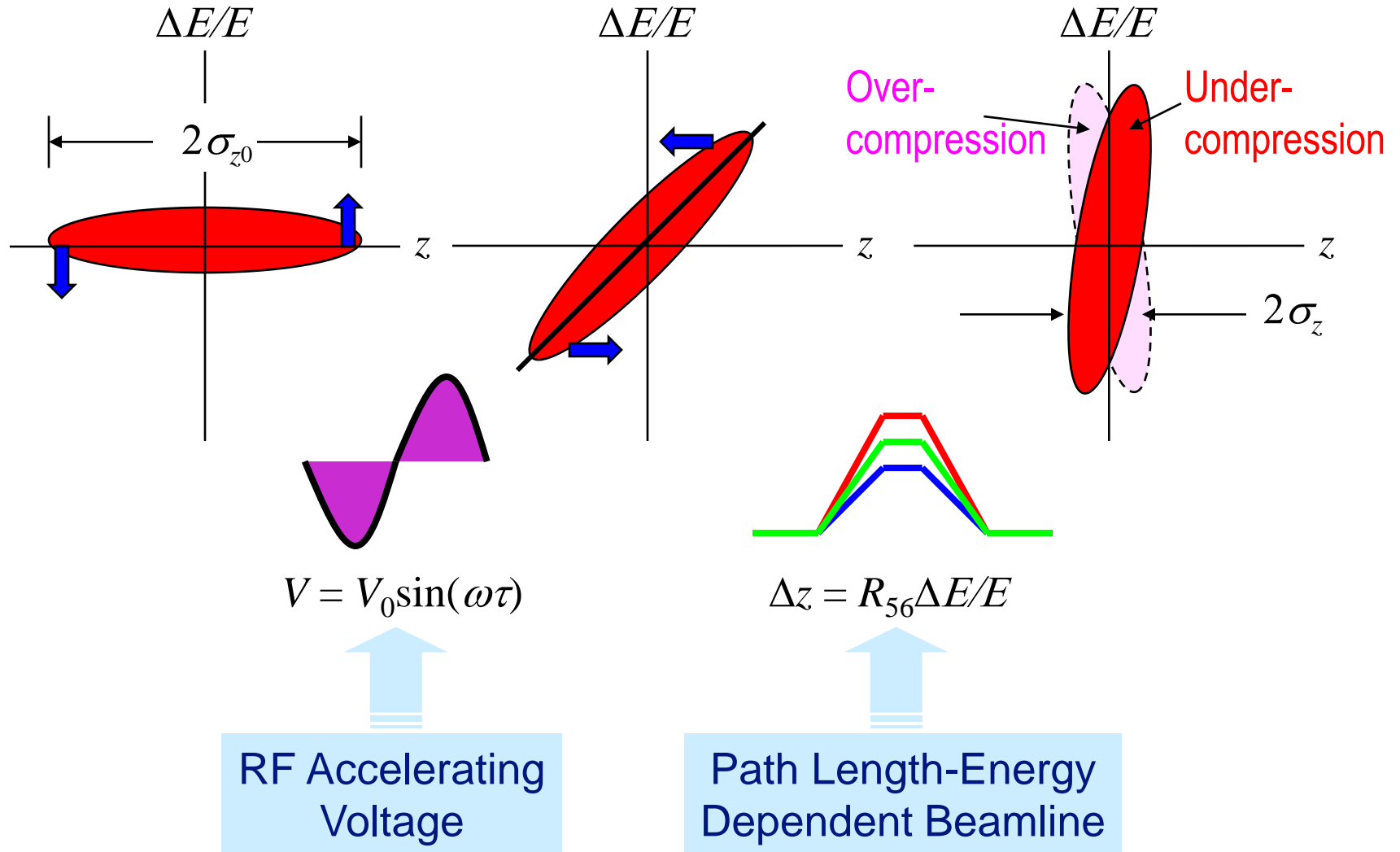
	ILC	CLIC linac	XFEL	LCLS
<i>Beam Energy (GeV)</i>	250	1500	20	15
<i>Linac RF Frequency (GHz)</i>	1.3	12	1.3	2.856
<i>Bunch charge (nC)</i>	3	0.6	1	1
<i>Bunch Length (fs)</i>	700	150	80	73

- High resolution monitor for single shot measurement
  - RF deflector : Excellent time resolution but destructive
  - *Coherent Diffraction radiation for online measurement and feedback system*
  - EO techniques for single shot longitudinal profile monitoring

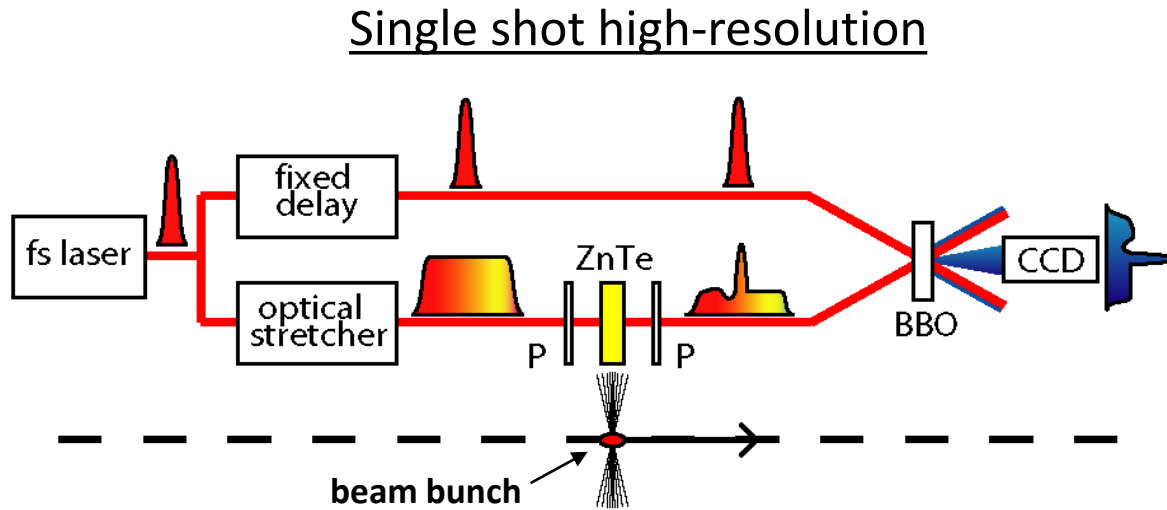
# Compact Linear Collider



# Bunch compressors



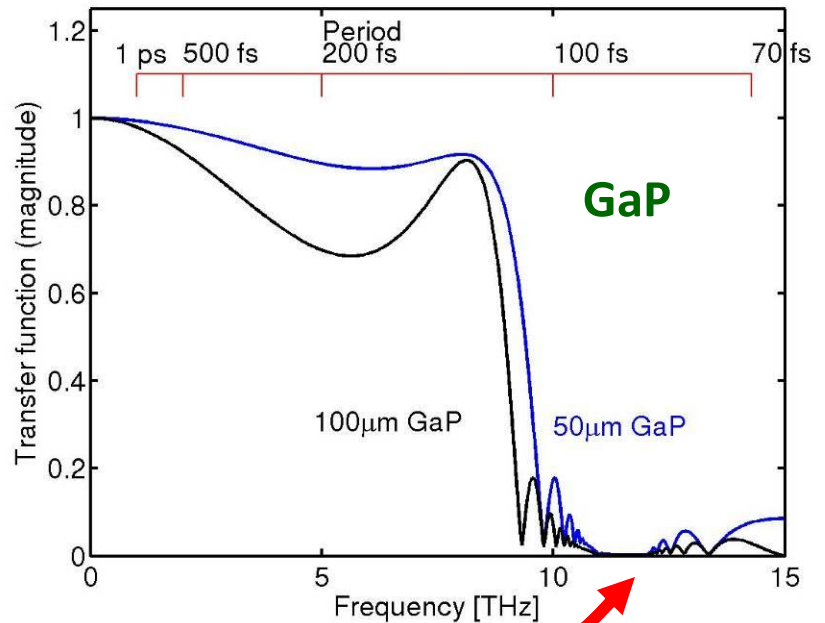
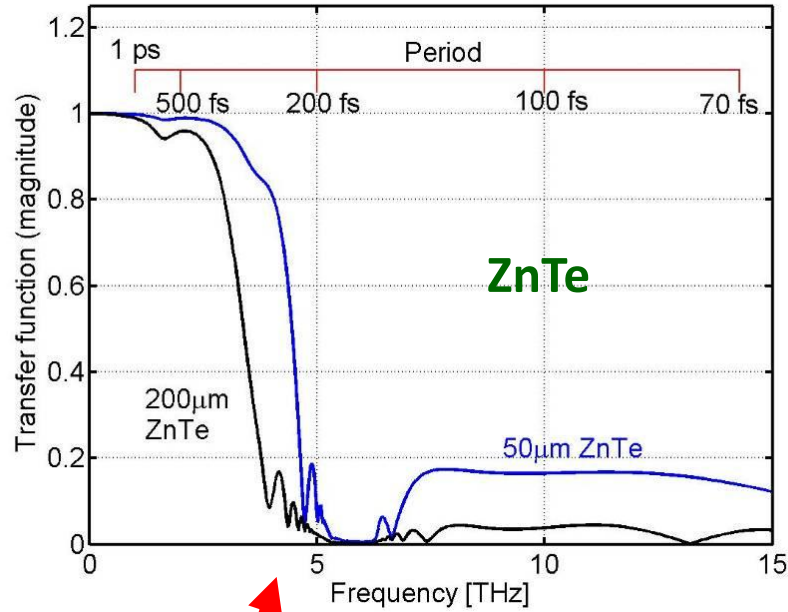
# EO Temporal decoding



- *Encoding the bunch long. Profile in an intensity modulation of a laser pulse amplitude*
- *Measured the laser pulse leaving EO crystal via single-shot cross correlation in BBO using a short laser pulse*

# Encoding Time resolution

## Spectral limitations of the Crystal

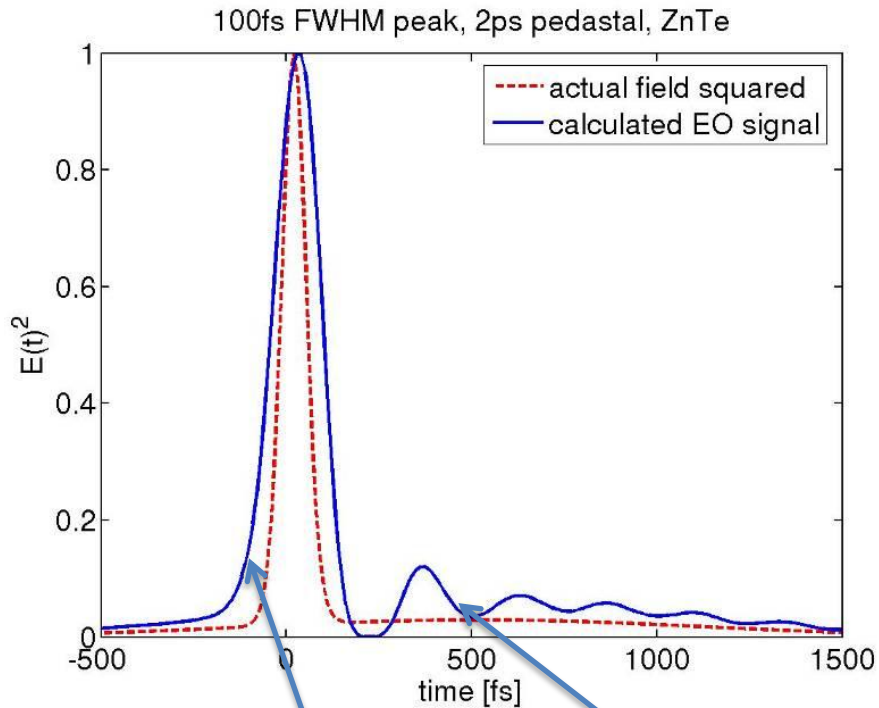


Phonon resonances

W.A. Gillespie & S. Jamison

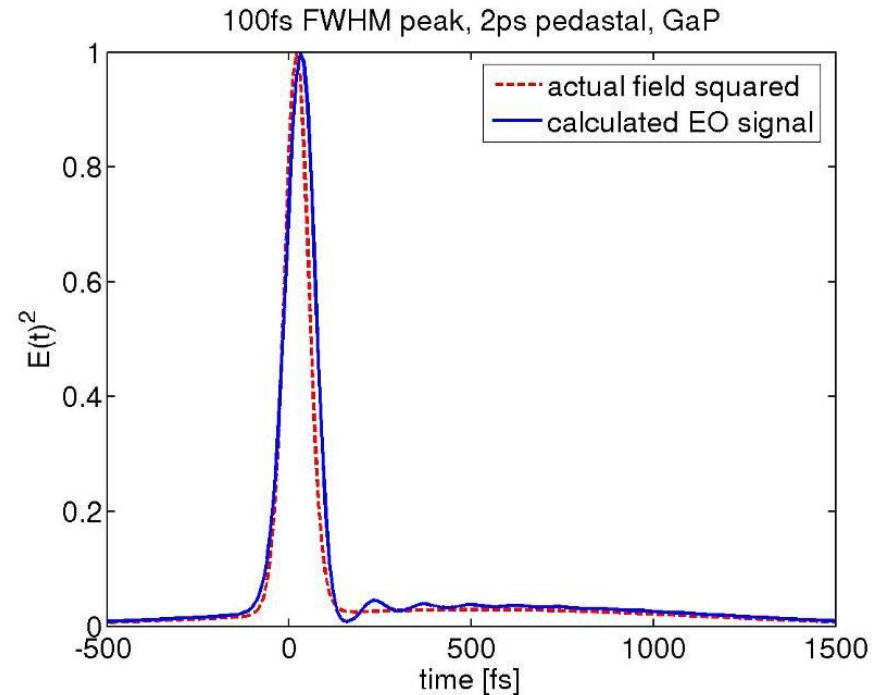


# Encoding Time resolution



Bandwidth limitation

ringing artefacts

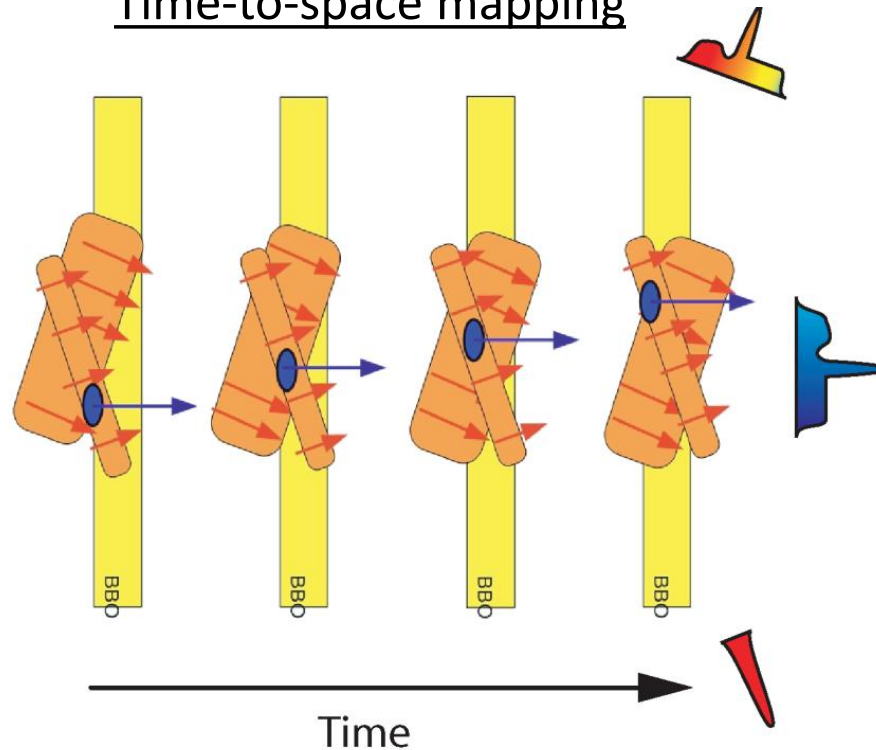


- *Thin crystal ( $>10\mu\text{m}$ )*
- *Consider new materials GaSe, DAST, MBANP ..... or poled organic polymers?*

W.A. Gillespie & S. Jamison

# Temporal decoding

## Time-to-space mapping



The non-collinear nature of the cross correlation geometry provides a mapping of time to spatial position in the BBO crystal and the CCD

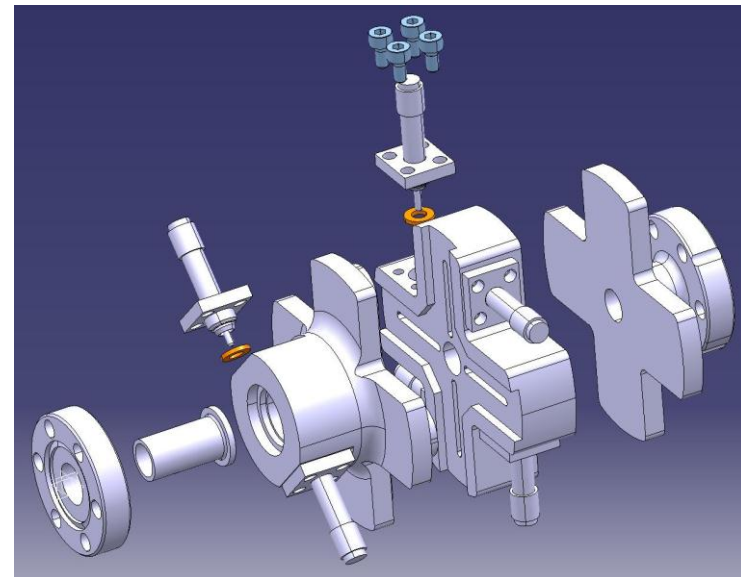
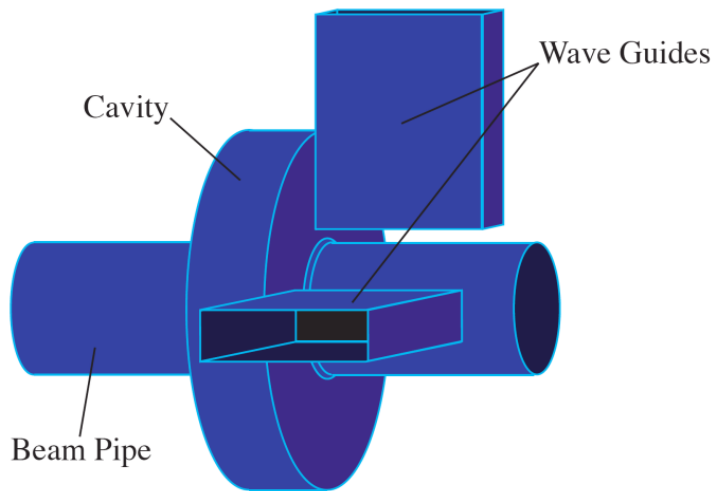


- *Very short laser pulse for time resolution*
- *High laser energy (1mJ) for frequency doubling efficiency*

W.A. Gillespie & S. Jamison

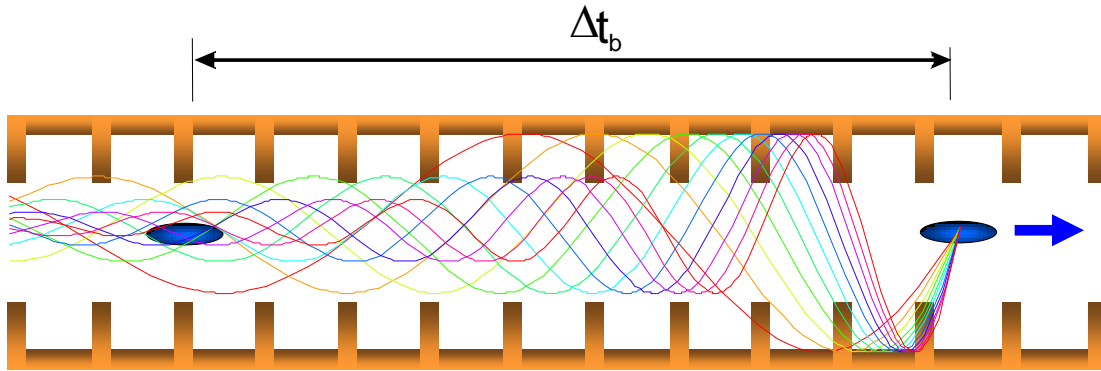
# Conserving small Emittance along the Main Linac

- Dispersive emittance dilutions : offset of quadrupoles
  - Beam based alignment to define a precise reference using high precision BPM (50nm resolution)
  - Dispersion free-steering - Align quadrupoles precisely
  - High resolution cavity BPM (50nm for CLIC)
  - Long linac → large number of BPMs: 2000@ILC – 4000@CLIC



# Conserving small Emittance along the Main Linac

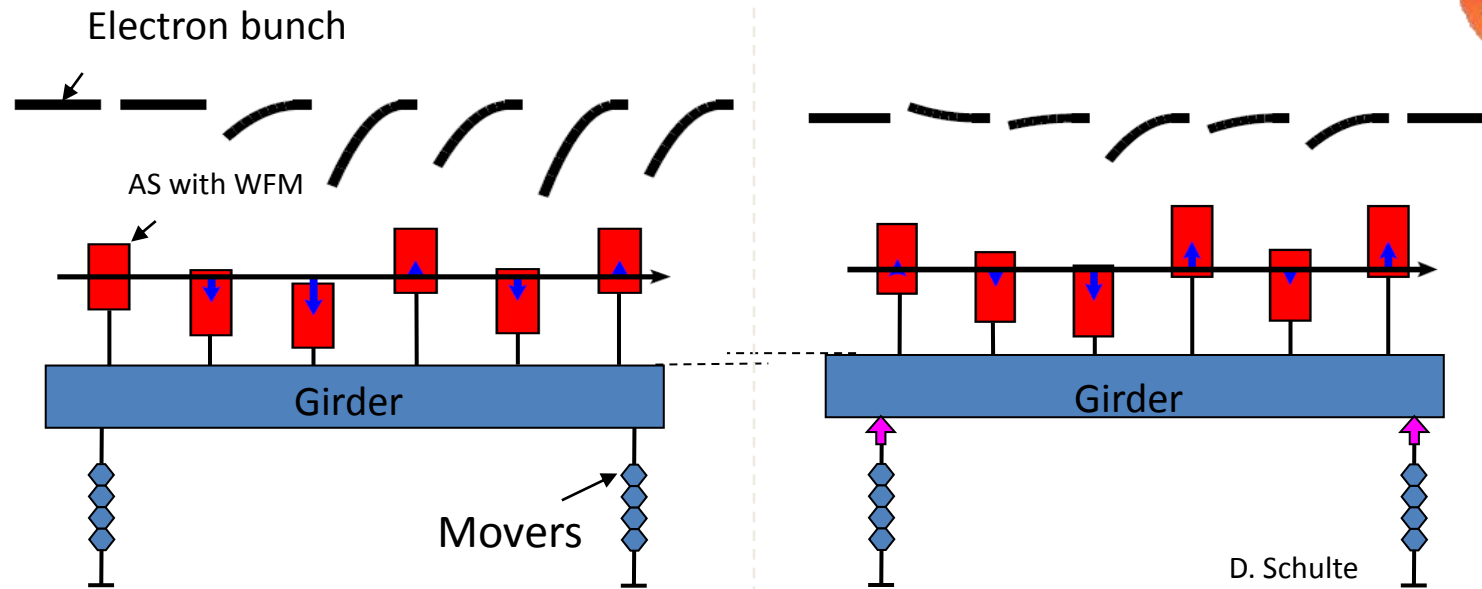
Wakefields in accelerating structures (damping of high order mode)



Bunches passing through an accelerating structure off-centre **excite high order modes** which **perturbs later bunches**

- Tolerances for acc. Structures alignment
- Cavity alignment at the 300  $\mu\text{m}$  level @ ILC compared to 5  $\mu\text{m}$  @ CLIC
- Need wakefield monitor to measure the relative position of a cavity with respect to the beam

# Proposed correction scheme

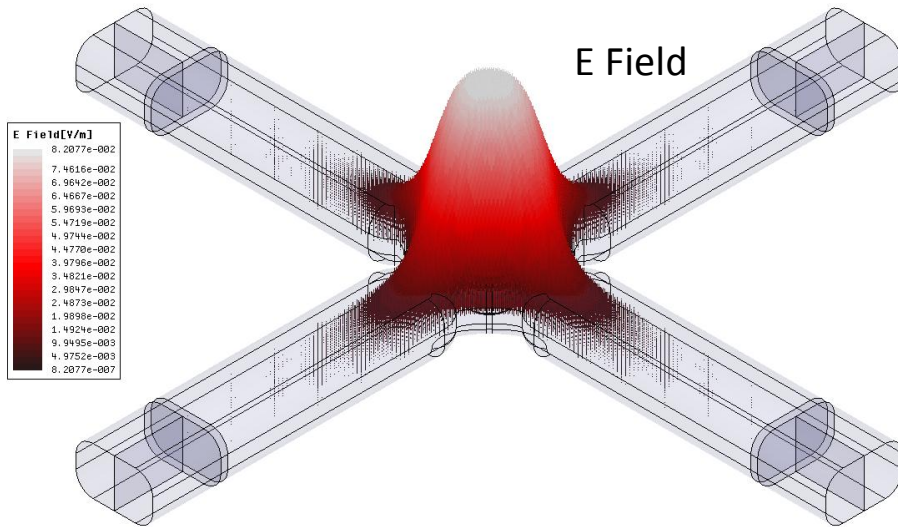


- Wakefield kicks from misaligned AS can be cancelled by another AS
- One WFM per structure (142000 monitors) and mean offset of the 8 AS computed
- WFM with 5 $\mu$ m resolution
- Need to get rid of the 100MW of RF power at 12GHz present in the structures

D. Schulte

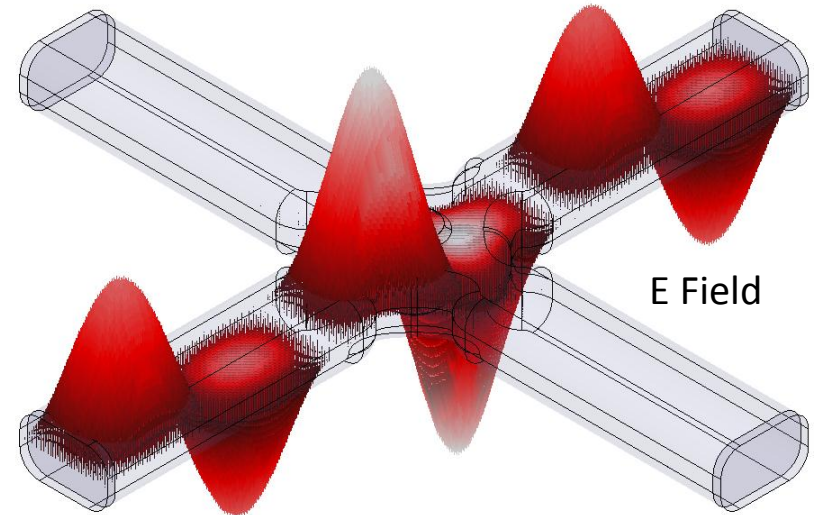
# WakeField Monitor design

## Monopole mode



Opposite ports signals  
are in phase

## Dipole mode



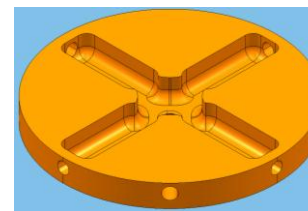
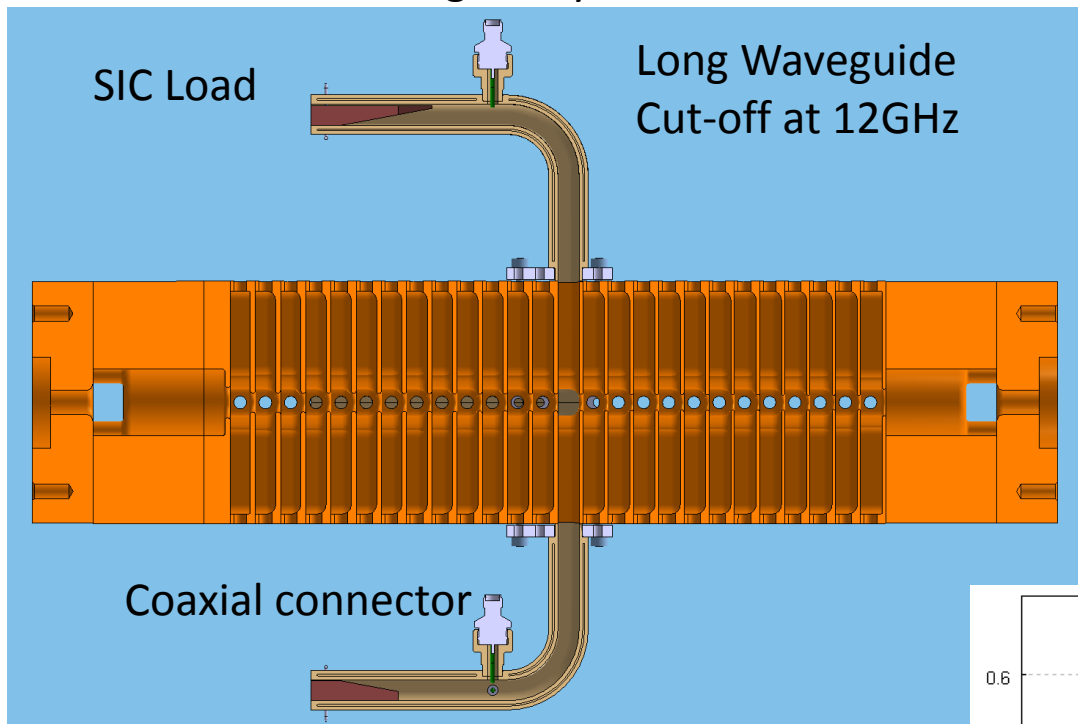
Opposite ports signal  
have opposite phase

When we subtract the opposite port signals, the monopole mode is cancelled and the dipole mode amplitude is increased



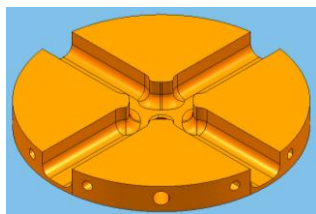
# WakeField Monitor design

12GHz accelerating cavity

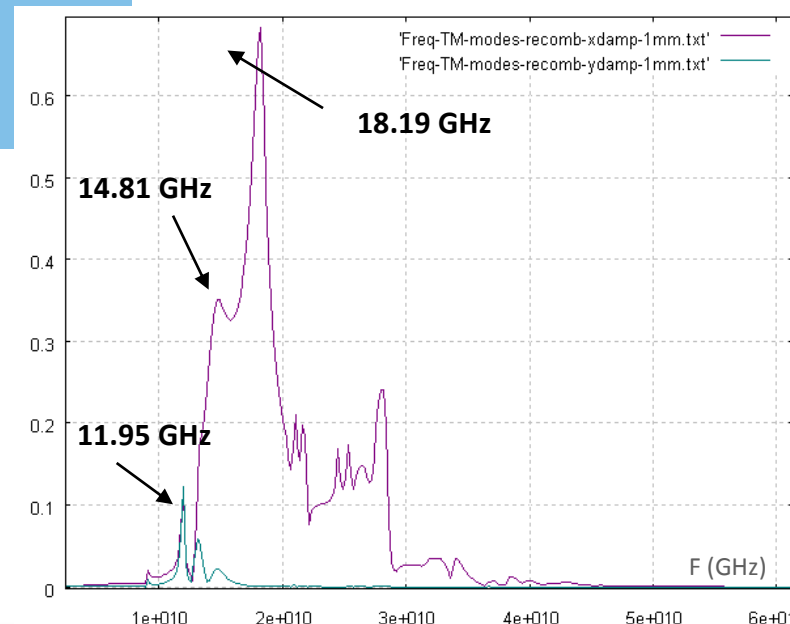


Regular cells with SIC load

Middle cell with WFM



Recombined port  
signal amplitude



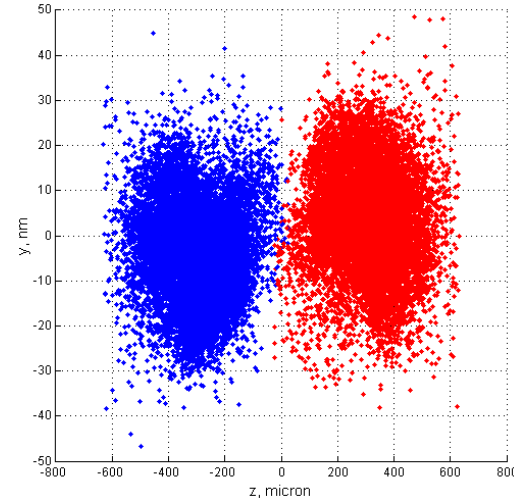
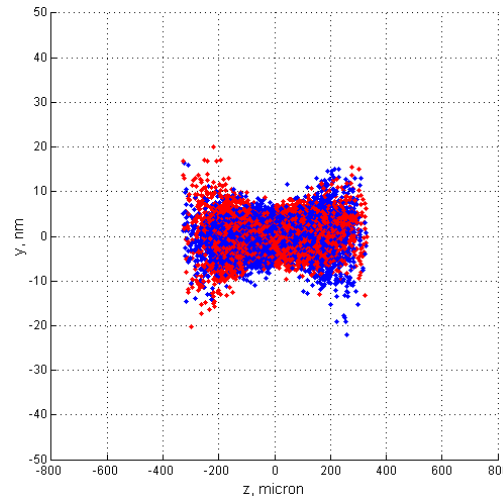
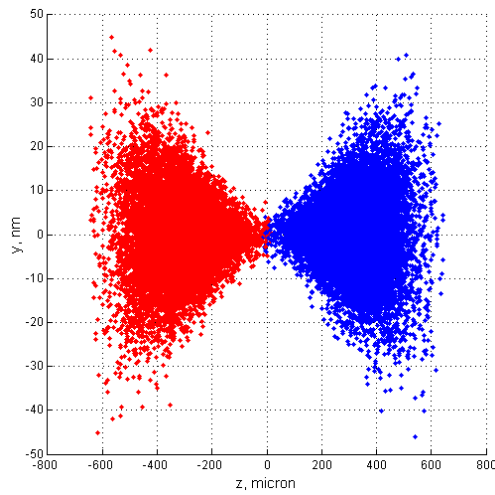
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Reserve Slides follow

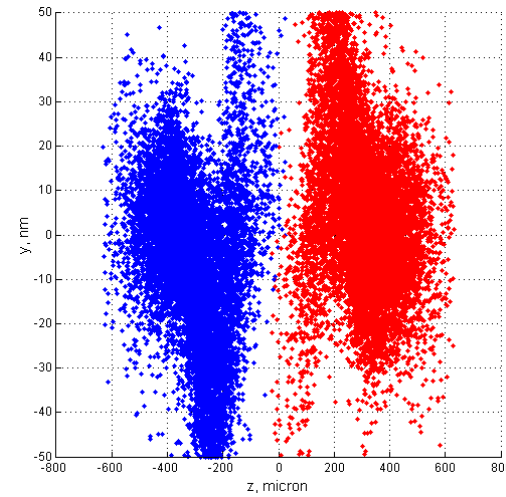
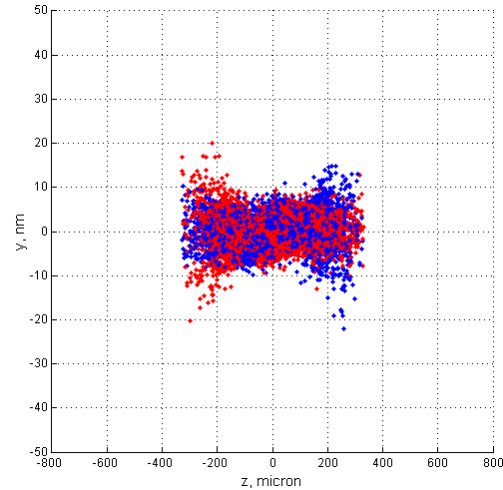
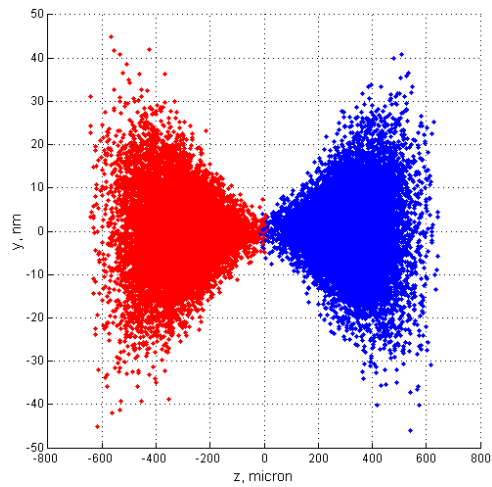


# Luminosity issue with intense beams - Disruption

due to 1% initial offset between beams



$$D_y = 12$$



$$D_y = 24$$

# Damping Ring : the mandate ?

Damping ring necessary to “cool” the beam to an extremely low emittance in all three dimensions

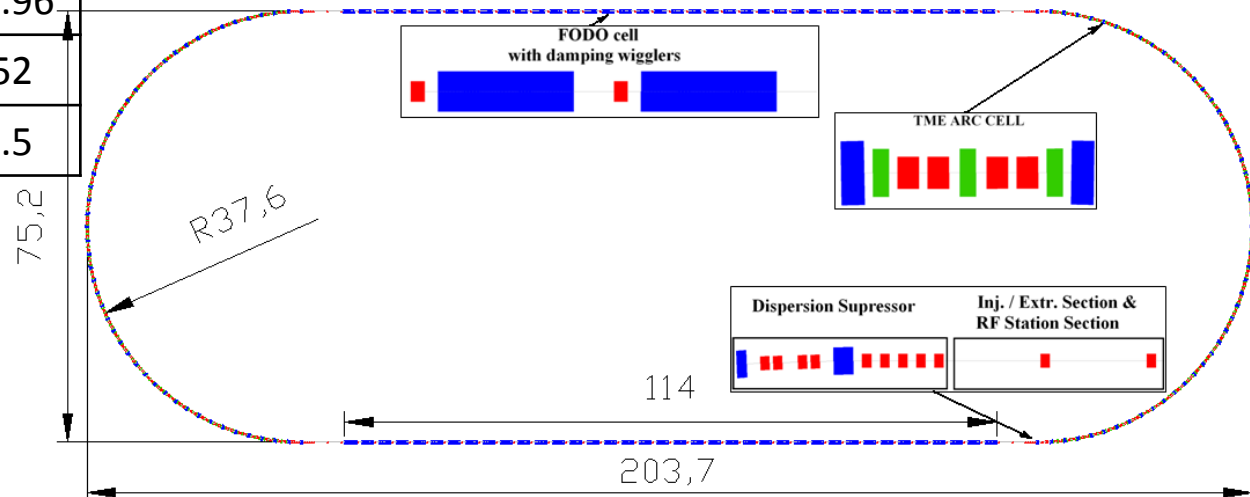
- High-bunch density
  - Emittance dominated by **Intrabeam Scattering**, driving energy, lattice, wiggler technology choice and alignment tolerances
  - **Electron cloud** in e<sup>+</sup> ring imposes chamber coatings and efficient photon absorption
  - **Fast Ion Instability** in the e<sup>-</sup> ring necessitates low vacuum pressure

PARAMETER	ILC	CLIC
bunch population (10 <sup>9</sup> )	75	41
bunch spacing [ns]	14	0.5
number of bunches/train	192	312
number of trains	3	1
Repetition rate [Hz]	120	50
Extracted hor. normalized emittance [nm]	2370	<500
Extracted ver. normalized emittance [nm]	<30	<5
Extracted long. normalized emittance [keV.m]	10.9	<5
Injected hor. normalized emittance [μm]	150	63
Injected ver. normalized emittance [μm]	150	1.5
Injected long. normalized emittance [keV.m]	13.18	1240

- Space charge sets energy, circumference limits
- Repetition rate and bunch structure
  - Fast damping achieved with wigglers
- Output emittance stability
  - Tight jitter tolerance driving kicker technology
- Positron beam dimensions from source
  - Pre-damping ring challenges (energy acceptance, dynamic aperture) solved with lattice design

# Damping Ring : the mandate ?

Design Parameters	CLIC
Energy [GeV]	2.86
Energy loss/turn [MeV]	4.2
RF voltage [MV]	4.9
Compaction factor	$8 \times 10^{-5}$
Damping time x / s [ms]	1.88/0.96
No bends / wigglers	100/52
Dipole/ wiggler field [T]	1.4/2.5



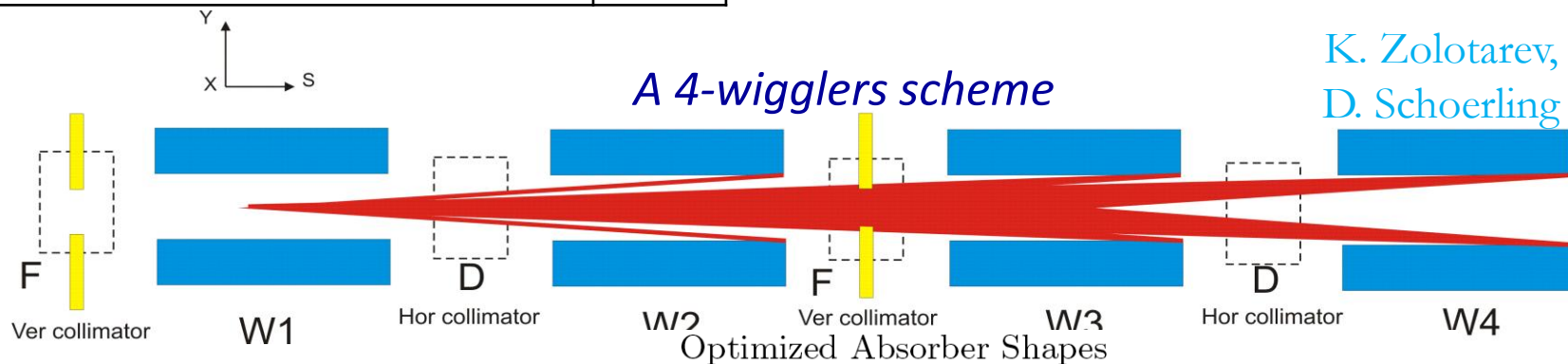
## Racetrack shape with

- 96 TME arc cells (4 half cells for dispersion suppression)
- 26 Damping wiggler FODO cells in the long straight sections (LSS)
- Space reserved upstream the LSS for injection/extraction elements and RF cavities

# Damping Ring : the Challenge ?

Radiation parameters	DR
Power per dipole [kW]	1.3
Power per wiggler [kW]	18.7
Total power [MW]	0.61
Critical energy for dipole [keV]	19.0
Critical energy for wiggler [keV]	40.7
Radiation opening angle [mrad]	0.11

- 90% of radiation power coming from the 52 SC wigglers
- Design of an absorption system is necessary and critical to protect machine components and wigglers against quench
- Radiation absorption equally important for PDR (but less critical, i.e. similar to light sources)



Element	Length [m]	V [mm]	H [mm]	Shape
Horizontal Absorber	0.5	13.5	12.3	Rectangular
Vertical Absorber	0.5	9.5	12.5	Rectangular

■ Gap of 13mm (10W)

■ Combination of collimators and absorbers (PETRAIII type, power density of up to 200W/cm)

■ Terminal absorber at the end of the straight section (10kW)

# Damping Ring Instrumentation

Very high synergy with

	CLIC DR	SLS	Diamond	Soleil
<i>Beam Energy (GeV)</i>	2.86	2.4	3	2.75
<i>Ring Circonfrence (m)</i>	493	288	561.6	354
<i>Bunch charge (nC)</i>	0.6	1	1	0.5
<i>Energy Spread (%)</i>	0.134	0.09	0.1	0.1
<i>Damping times (x,y,E) (ms)</i>	2,2,1	9,9,4.5	-	6.5,6.5,3.3
<i>Orbit stability (um)</i>	1	1	1	1

**300PUs**, turn by turn (every **1.6 $\mu$ s**)

**10 $\mu$ m** precision, for linear and non-linear optics measurements.

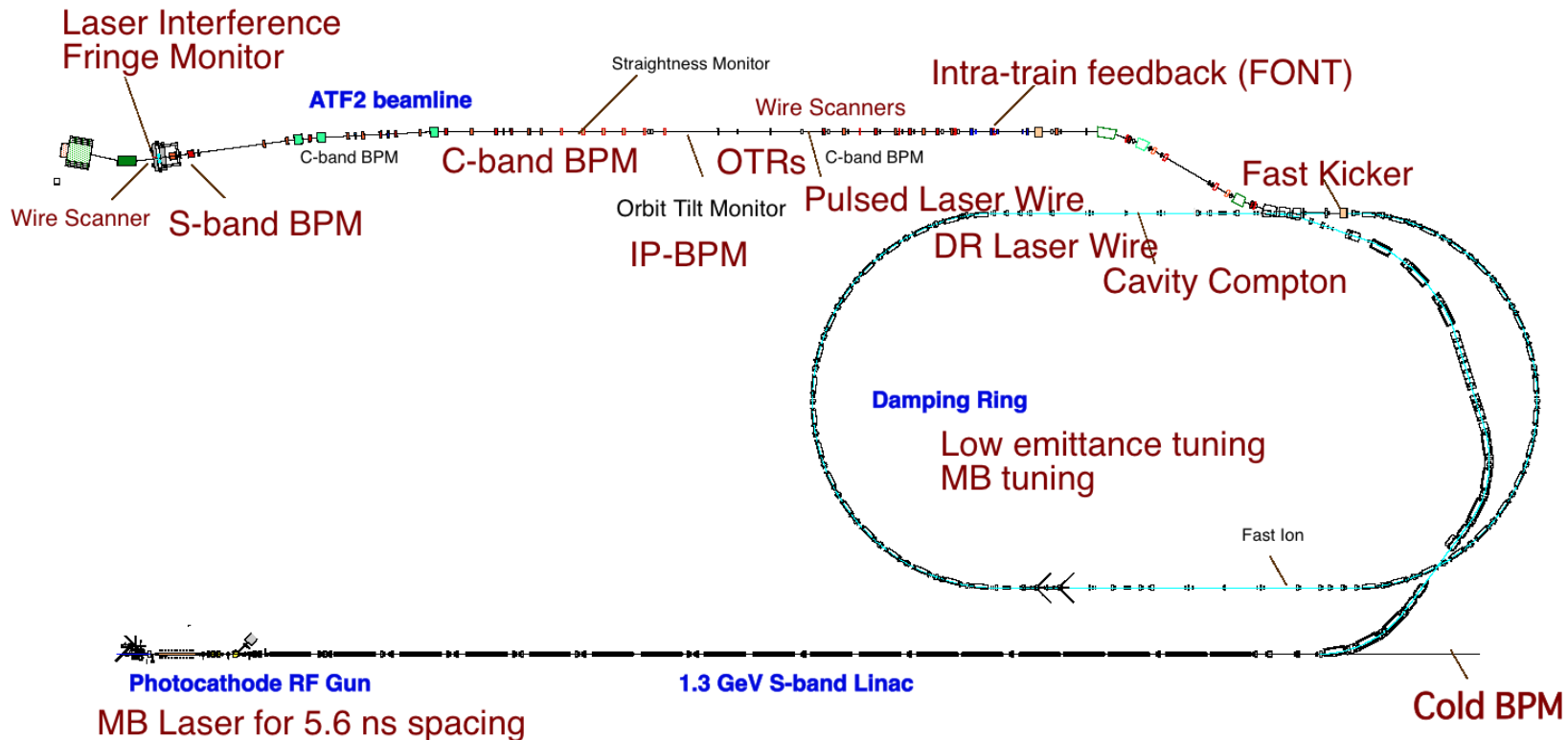
**2 $\mu$ m** precision for orbit measurements (vertical dispersion/coupling correction + orbit feedback).

WB PUs for bunch-by-bunch (bunch spacing of **0.5ns** for **312** bunches) and turn by turn position monitoring with high precision ( **$\sim$ 2 $\mu$ m**) for injection trajectory control, and bunch by bunch

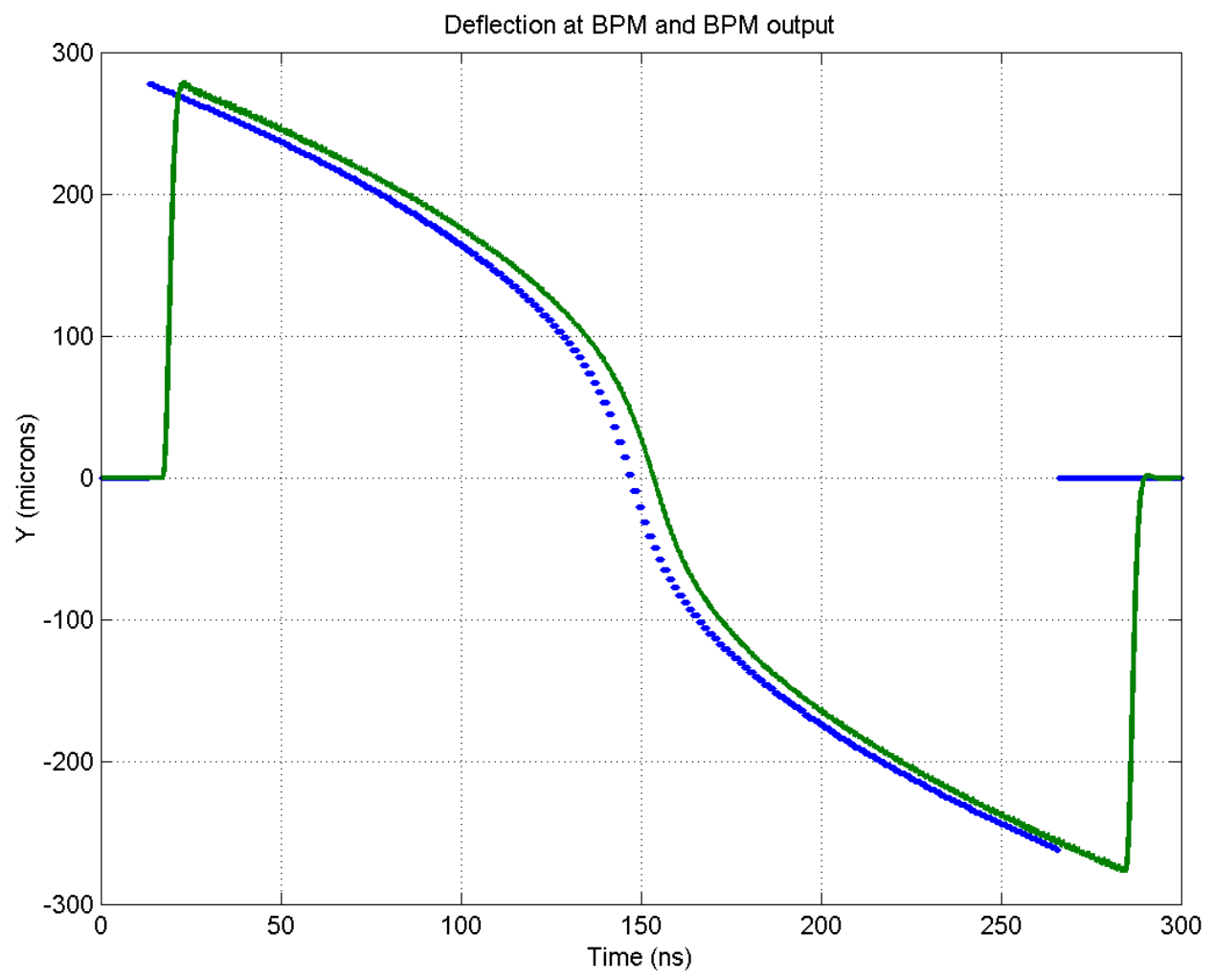
# Damping Ring Instrumentation

■ Turn by turn transverse profile monitors (X-ray?) with a wide dynamic range:

- Hor. geometrical emittance varies from 11nm.rad @ injection to 90pm.rad @ extraction and the vertical from 270pm.rad to 0.9pm.rad.

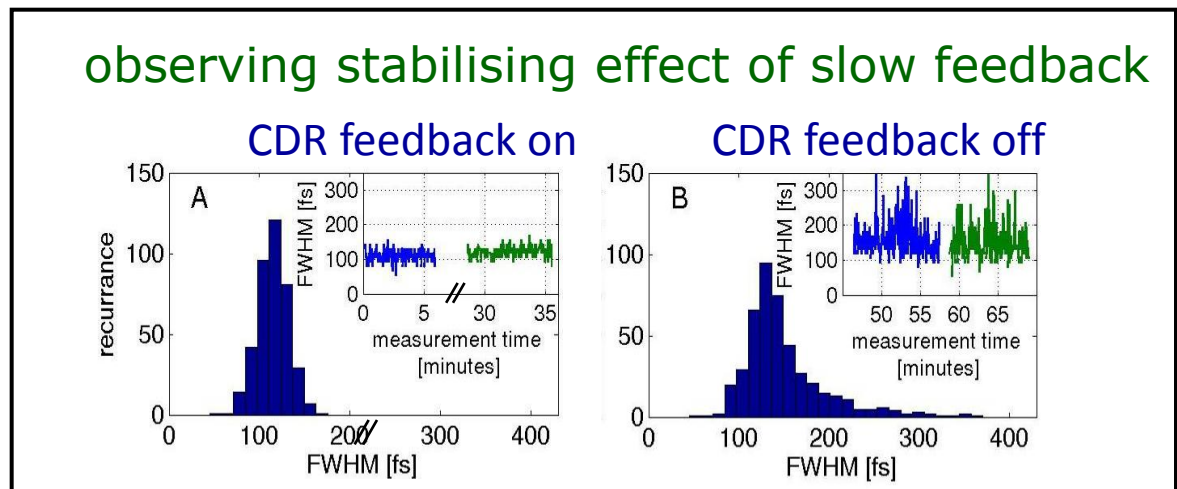
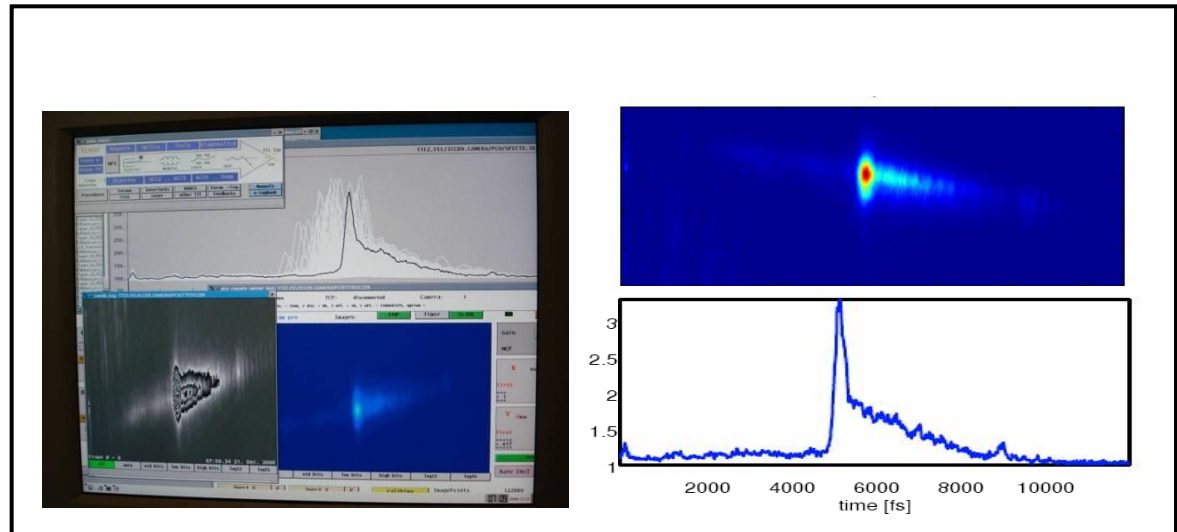
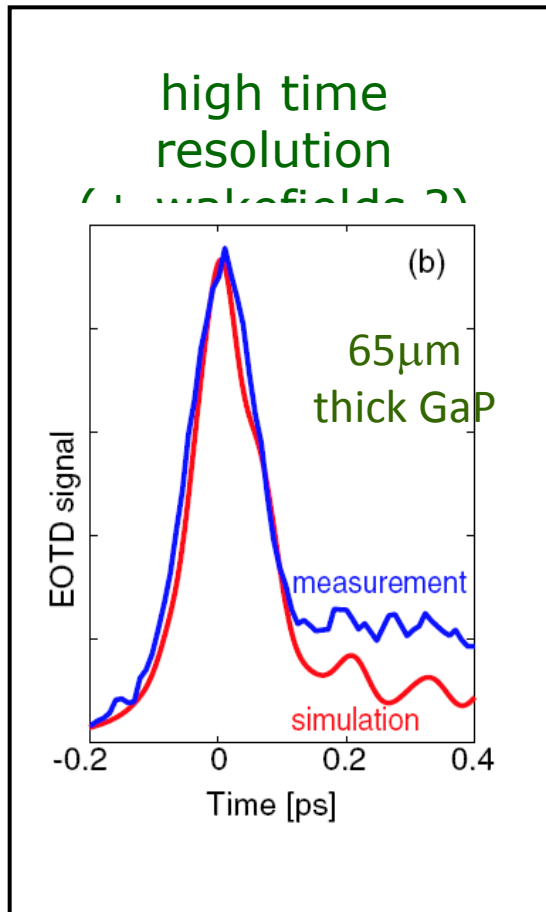


# Beam - Beam scan at IP



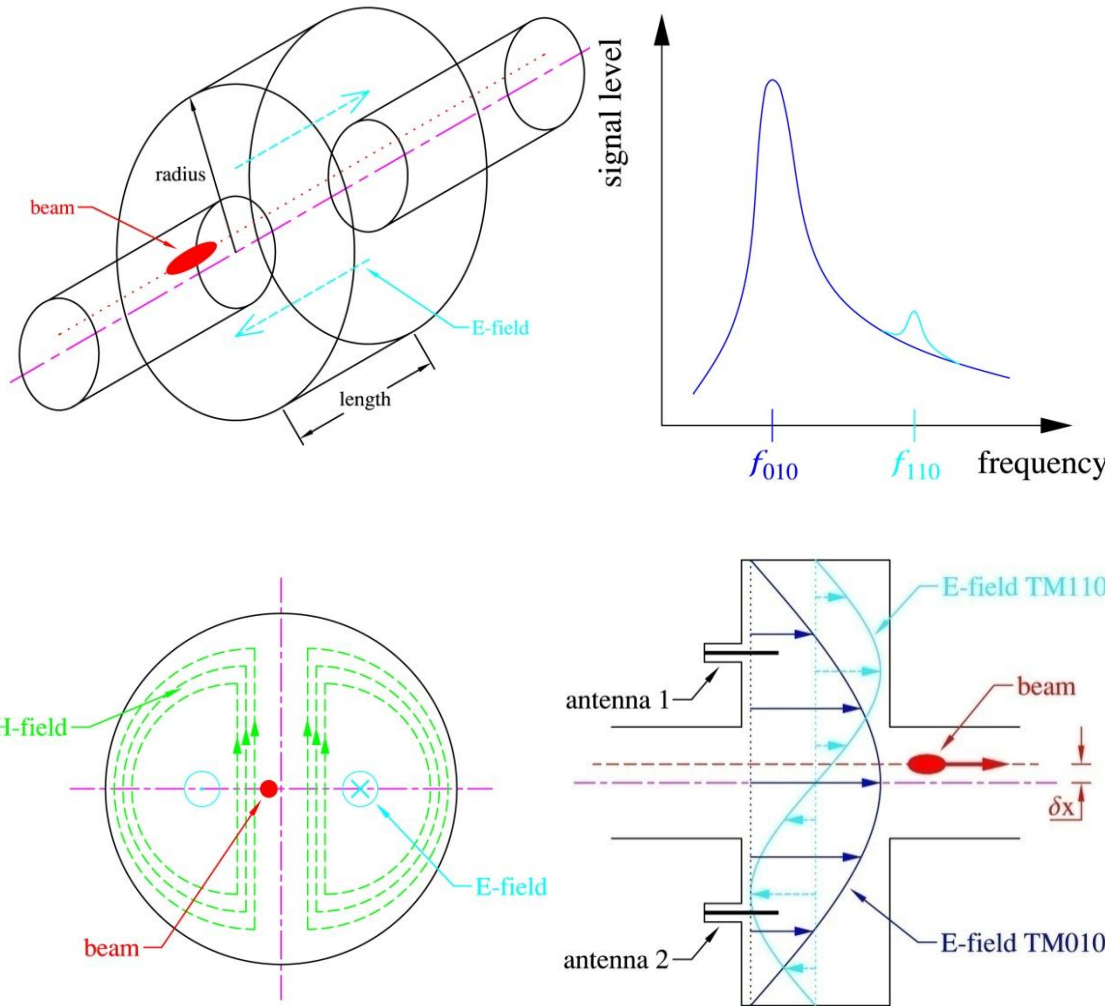
Beam bunches at IP: blue points  
BPM analog response: green line

# Temporal decoding





# Cavity BPM



## • “Pillbox” cavity BPM

### – Eigenmodes:

$$f_{mnp} = \frac{1}{2\pi\sqrt{\mu_0\epsilon_0}} \sqrt{\left(\frac{j_{mn}}{R}\right)^2 + \left(\frac{p\pi}{l}\right)^2}$$

### – Beam couples to

$$E_z = C J_1\left(\frac{j_{11}r}{R}\right) \cos\phi e^{i\omega t}$$

**dipole ( $TM_{110}$ ) and monopole ( $TM_{010}$ ) modes**

– **Common mode ( $TM_{010}$ ) suppression by frequency discrimination**

– **Orthogonal dipole mode polarization (xy cross talk)**

– **Transient (single bunch) response ( $Q_L$ )**

– **Normalization and phase reference**

# No circular $e^+e^-$ collider after LEP

Cost of Circular Accelerator : Length + Energy lost replaced by RF power  $\sim E^2$

Cost of Linear Accelerator : Length  $\sim E$

