



# Comparison of Tau-pair Performance with ILD ECAL candidates

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LCWS13  
12 / 11 / 2013 @ Tokyo  
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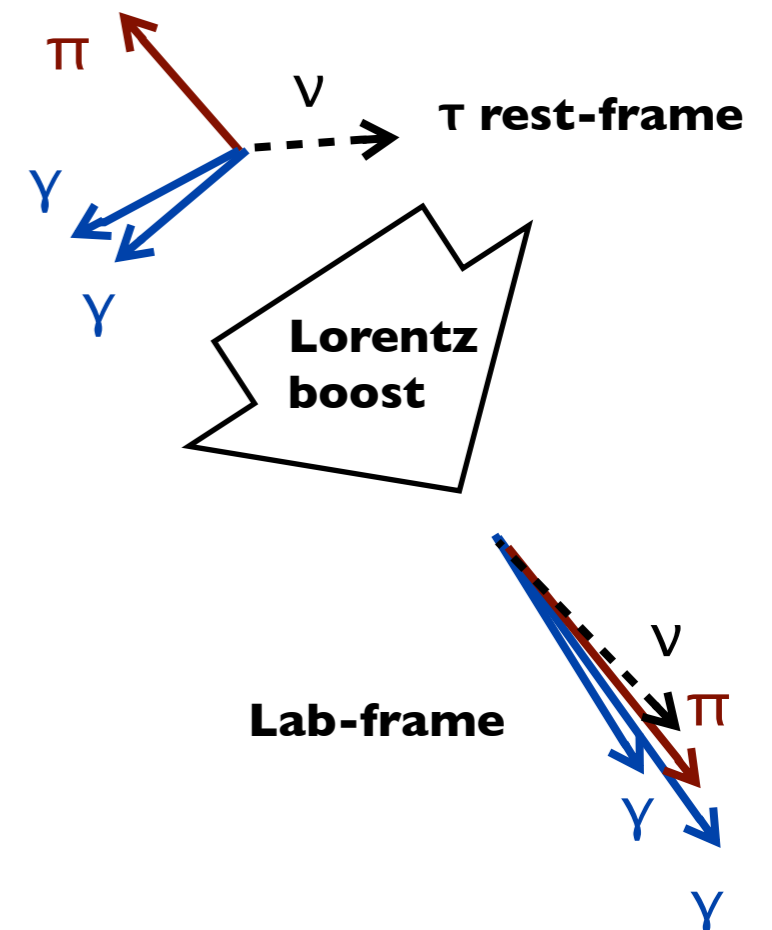
# Motivation of This Study

- we want to estimate the performance of ECALs with the ILD bench mark process  $ee \rightarrow \tau\tau$ .
- A potential criterion for ILC electromagnetic calorimeters (ECAL) is the ability to reconstruct gammas with a charged track near by.
- Also, the full reconstruction of taus may be yet more challenging and the physics opportunities are potentially crucial. (Taus appear in many New Physics signatures)
- At high energy, daughters of  $\tau$  decay are concentrated in a very narrow angle and a narrow area due to the Lorentz boost.
- Identifying and measuring gammas (from  $\pi\pi\gamma$ ) is difficult, because  $2\gamma$ s are very close.

→ **ILD demands well segmented ECAL.**

- We compare tau reconstruction performance (gamma separation) with some ILD ECAL candidates.

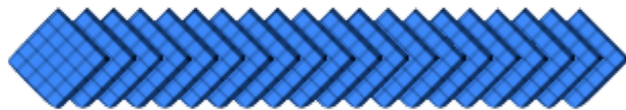
**How precisely do ECALs reconstruct tau?**



# ILD ECAL Candidates

- ECAL is high cost.
  - We want to decrease the price without losing performance as possible as we can.
- Basically, we examine with three types of ECALs

## - Si ECAL



- Pure silicon ECAL.
- Silicon thickness = 0.5 mm
- Silicon cell size = 5x5 mm
- ECAL module thickness = 185.0 mm

## - DoubleLayer Hybrid



- Si, Sci hybrid ECAL
- Silicon thickness = 0.5 mm
- Scintillator thickness = 1.0 mm
- ECAL module thickness = 190.796 mm
- Use Si 2-layer Sc 2-layer alternatively
- Apply SSA (strip split algorithm) at reconstruction step. → achieve 5x5 mm

## - Sci ECAL w/ SSA



- Pure scintillator ECAL
- Scintillator thickness = 1.0 mm
- ECAL module thickness = 197.42 mm
- Scintillator size = 45x5 mm
- Apply SSA (strip split algorithm) at reconstruction step. → achieve 5x5 mm
- The cost is about half of pure Si ECAL
- The problem of ghost hit.

- And we think further configuration...

- Single layer hybrid.
- Scintillator strip + Scintillator tile

※ Double - Hybrid cannot completely extract tail layer effect

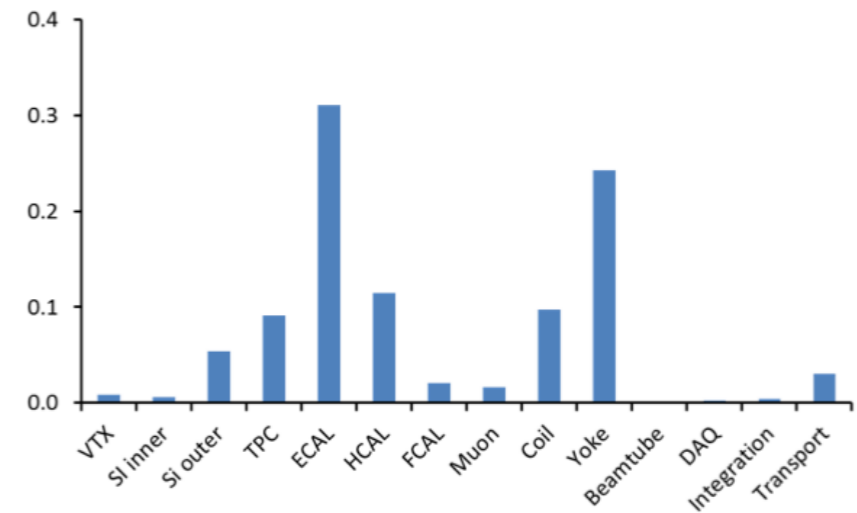


Figure 5.3.2: Summary plot of the relative contribution by the different sub-components to the total cost of the ILD detector.

# Event sample

## - Event sample

$e^+ e^- \rightarrow \tau^+ \tau^- \quad \sqrt{s} = 500\text{GeV}$  (ISR-off to simplify event)

Beam polarized :  $e^-, e^+ = -80\%, +30\%$

$e^-, e^+ = +80\%, -30\%$

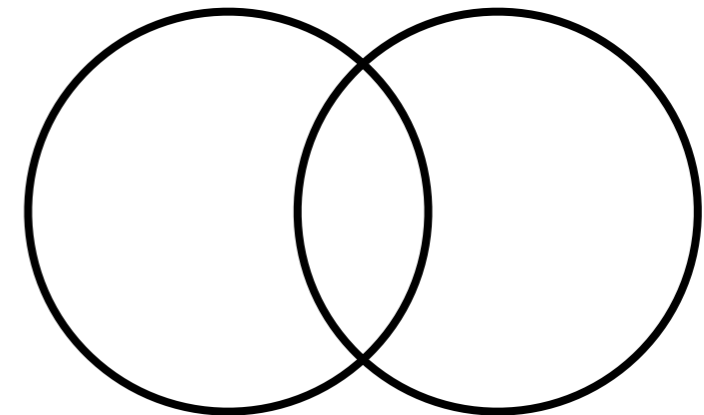
## - Estimation

- Reconstructed efficiency and purity at each tau decay.

$$\text{efficiency} = \frac{\text{DecayMode with MCTrue} \cap \text{DecayMode with DetectorReco}}{\text{DecayMode with MCTrue}}$$

$$\text{purity} = \frac{\text{DecayMode with MCTrue} \cap \text{DecayMode with DetectorReco}}{\text{DecayMode with DetectorReco}}$$

DecayMode with MCTrue      DecayMode with DetectorReco



- Physics observables :  $A_{fb}$ ,  $P(\tau)$ (tau polarization)

# Make tau jet and some Cut

## - Make tau jet

- Sort particles in energy order and select two energetic charged particles so as to satisfy back-to-back. → **Charged daughter of tau.**
- Gather particles around the charged daughter into the tau jet. and combine energy and momentum of associated particles. → **Combine < 8 deg from charged track.**

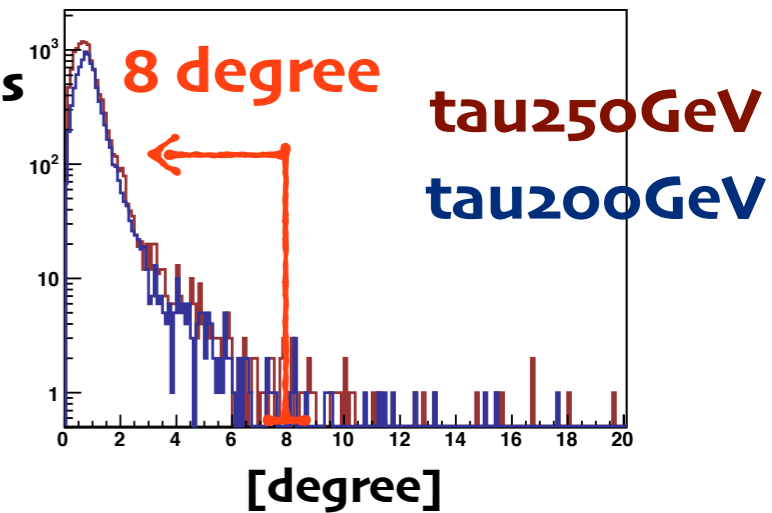
## - Applied cuts to suppress background.

main background :

- $e e \rightarrow \text{Bhabha}$
- $e e \rightarrow W W \rightarrow 2l + 2\nu$
- $2\text{-}\gamma \rightarrow \text{tau tau}$

Pre-cut : demand Back-to-Back.

Angle between gamma and main Track  
tau -> a1p1 mode  
on MCTrue



Cut / Signal(%)	Si ECAL	D-Hybrid	Sci w/SSA
No cut	100	100	100
Pre-cut	92.32	91.46	91.58
N of Tracks < 6	89.88	89.06	89.28
172 < Opening angle	87.22	86.42	86.68
-0.9 < Thrust angle < 0.9	87.22	86.42	86.68
70 < visible energy < 450	84.64	82.92	83.16

※ cuts applied to the whole event

Si/ScECAL N of Tracks

Si/ScECAL Opening Angle

Si/ScECAL Thrust Angle

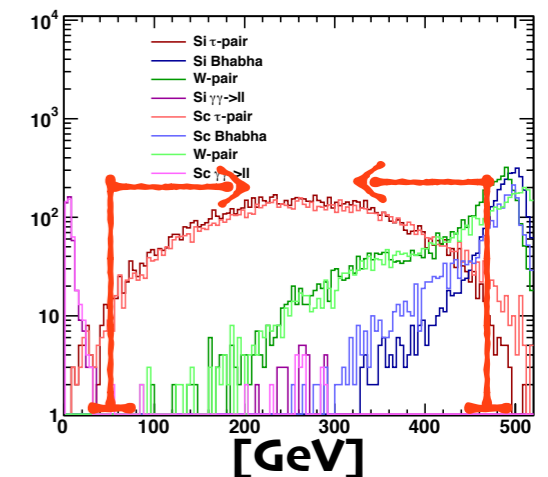
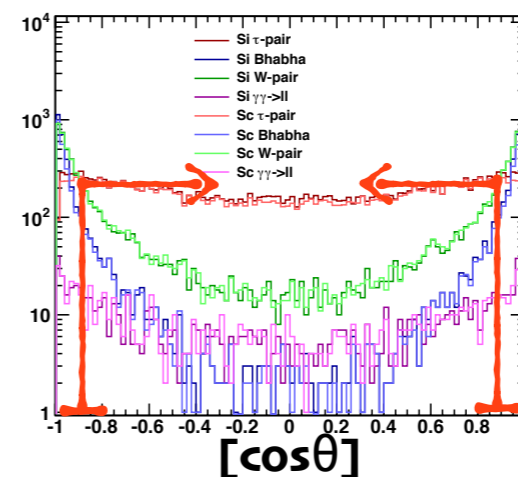
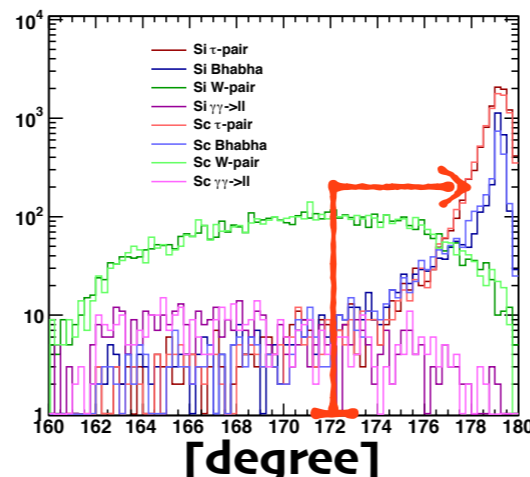
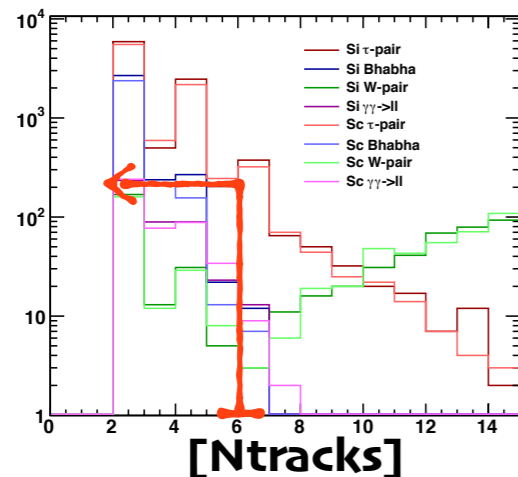
Si/ScECAL Vis Energy

Signal

Bhabha

W W -> 2l + 2ν

2-γ -> tau tau



# Selection of decay mode

- Applied two methods to distinguish decay modes of tau.

- Loose Cut : based on some cuts

1. Check whether track attached by Pandora is lepton or hadron.

2. Check energy of gammas.

Energy sum of gammas is less than 3.5GeV.  $\rightarrow$   $\pi$  mode.

Energy sum of gammas is more than 3.5GeV.

3. Check mass of gammas.

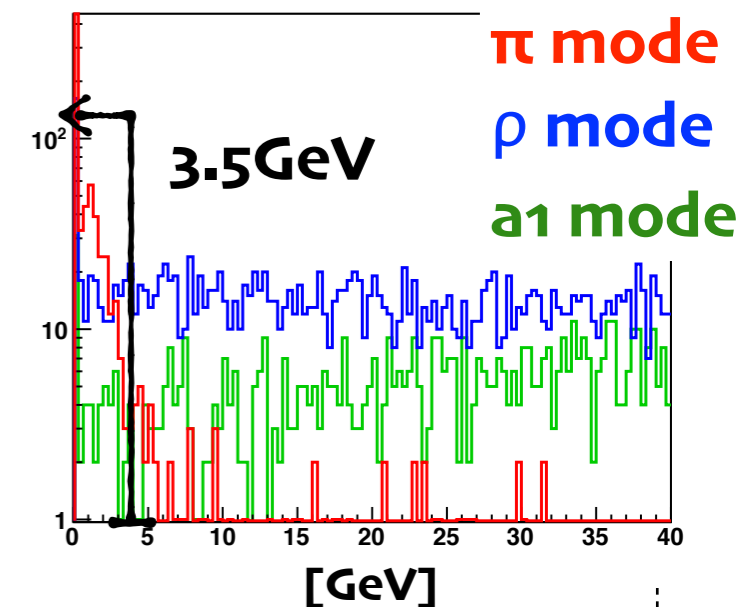
Mass of gammas (  $\text{PiO}$  ) is less than 0.45GeV.  $\rightarrow$   $\rho$  mode.

Mass of gammas (  $\text{PiO}$  ) is more than 0.45GeV.  $\rightarrow$   $a_1$  mode.

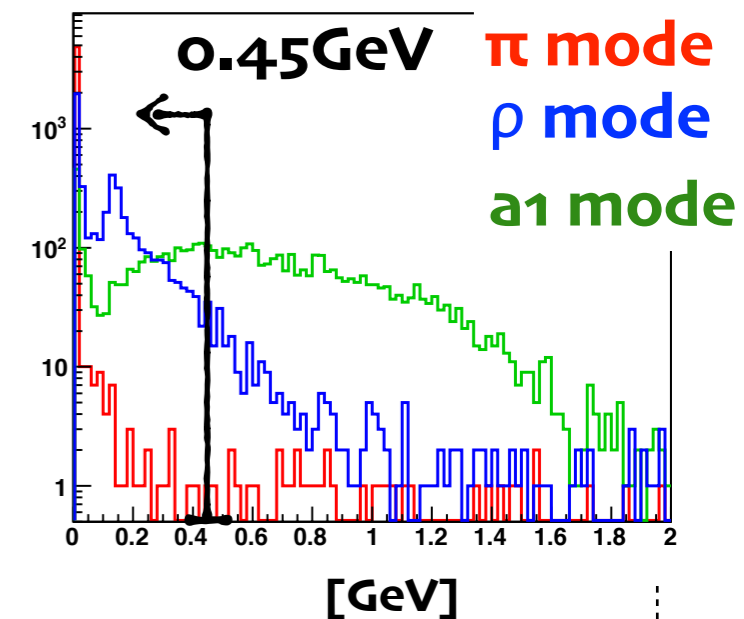
- MVA Cut : based on MVA method

$\rightarrow$  Distinguish from MVA response on each ECAL.

Energy of Gammas  
single tau 250GeV  
Si ECAL Reconstruction



Mass of gammas  
single tau 250GeV  
Si ECAL Reconstruction



# Efficiency & purity with Loose Cut

## - Comparison of Detectors

-  $\sqrt{500\text{GeV}}$  e-Le+R  $\rightarrow$  tau-tau+

## - Detectors

Si ECAL,

DoubleLayer Hybrid

Sci ECAL w/SSA

## - Cut

**Loose Cut**

## - Efficiency & Purity

- In reconstruction of leptonic decay, efficiency and purity are almost same.

- In reconstruction of hadronic decay, efficiency and purity are difference.

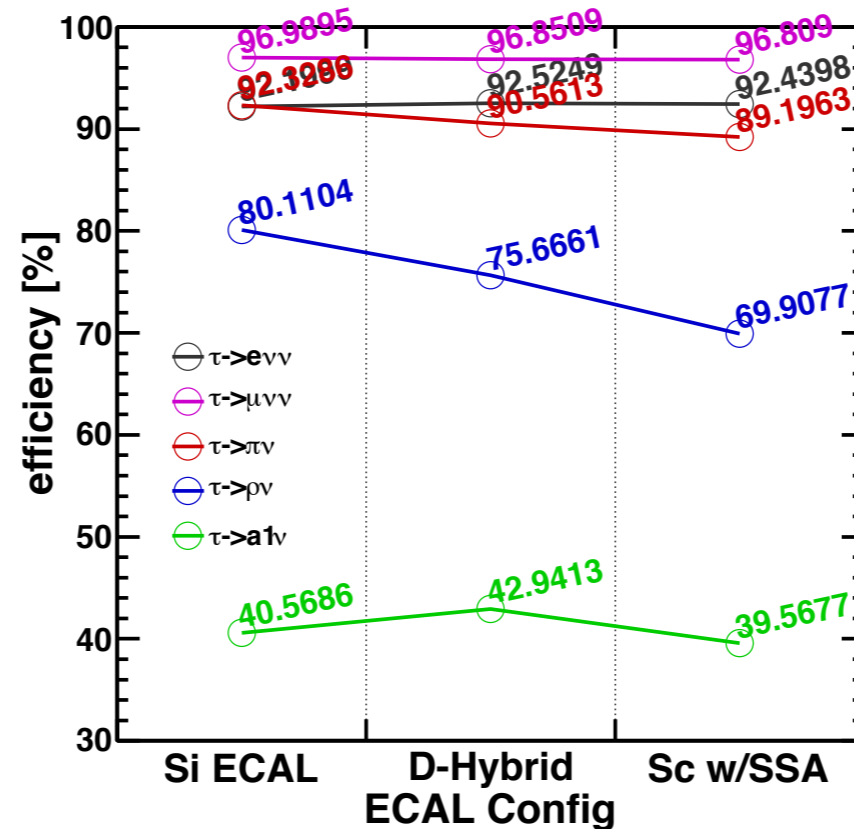
( Good ) Si ECAL > DoubleLayer Hybrid > Sci w/SSA ( Not good )

## - Miss Selection

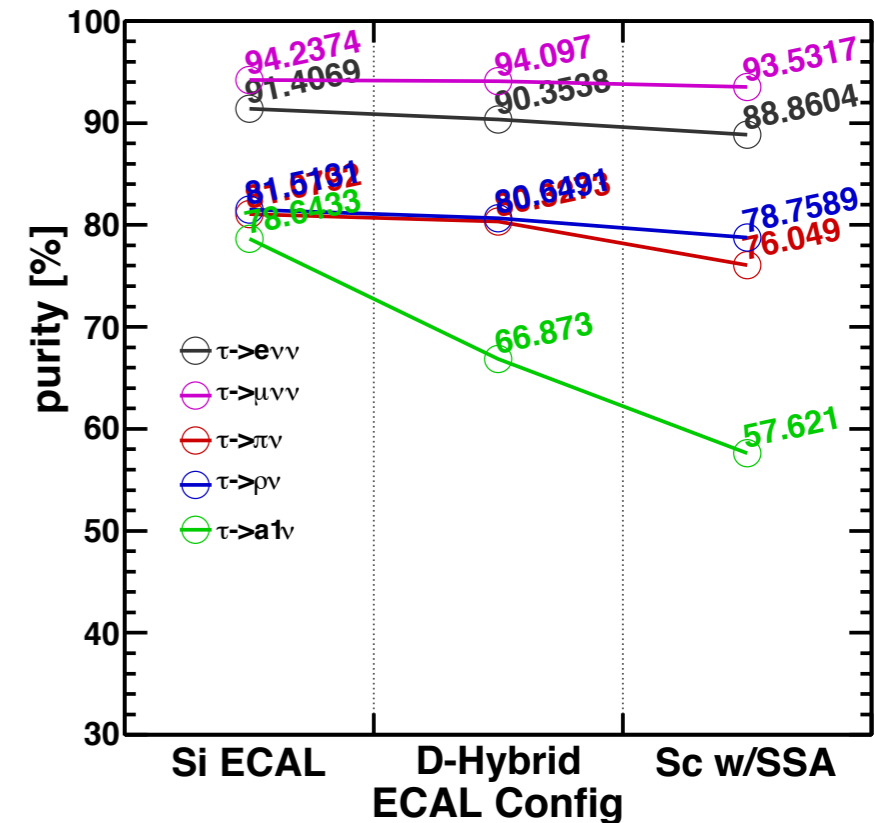
- Also miss selection is difference.

( Less ) Si ECAL 16.54% > DoubleLayer Hybrid 18.97% > Sci w/SSA 20.39% ( Not less )

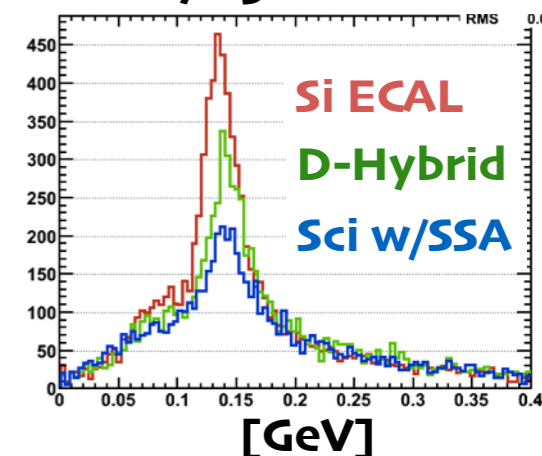
## efficiency



## purity



## pi0 Mass at tau -> rho exactly 2gammas





# Efficiency & Purity with Loose Cut @ $\sqrt{s} = 250, 500 \text{ \& } 1000 \text{ GeV}$

- Also simulated at some energy points 250, 500, 1000GeV.
- In e decay (leptonic decay), efficiency and purity are almost same.
- In pi decay, compared with Si ECAL,  $\tau$ ECALs get a little bit worse.
- In rho and a1, with increasing energy they get worse, even Si ECAL.

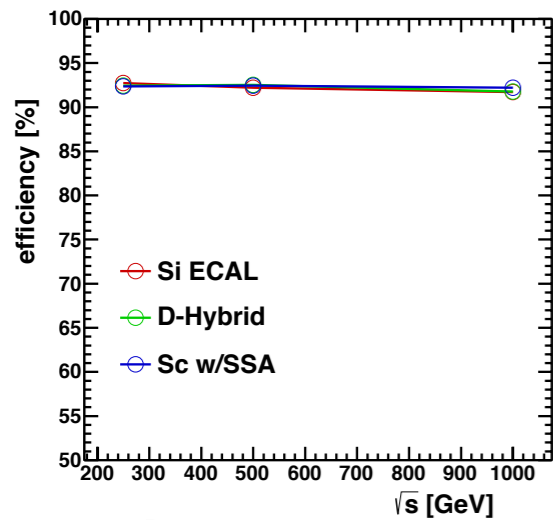
e-mode

pi-mode

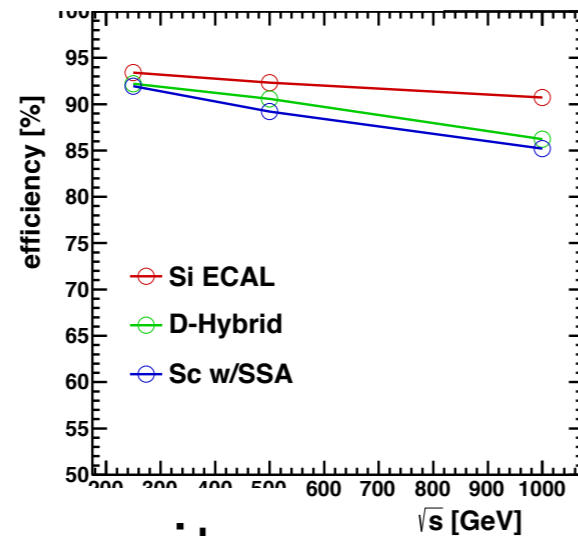
rho-mode

a1-mode

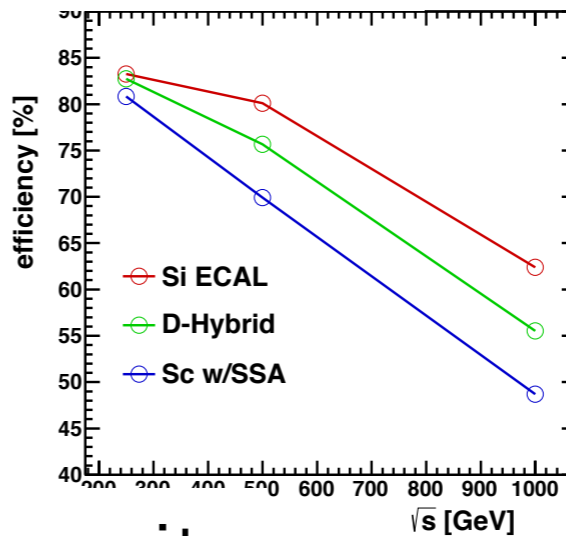
efficiency



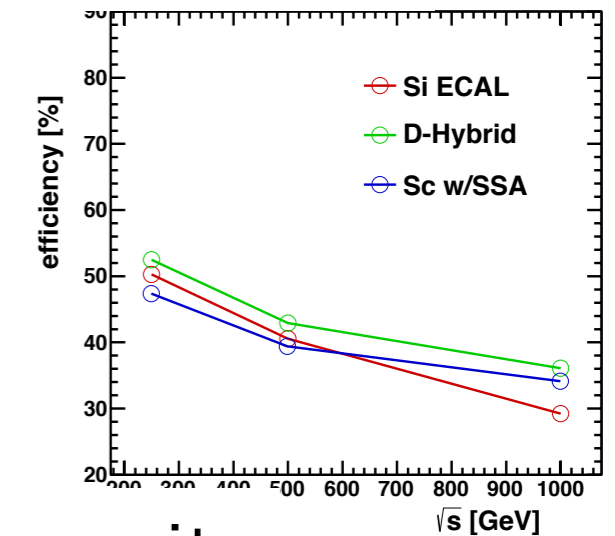
$\tau$  efficiency



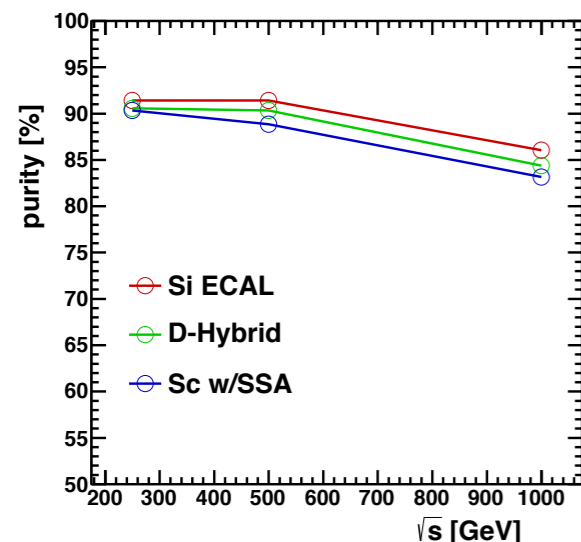
efficiency



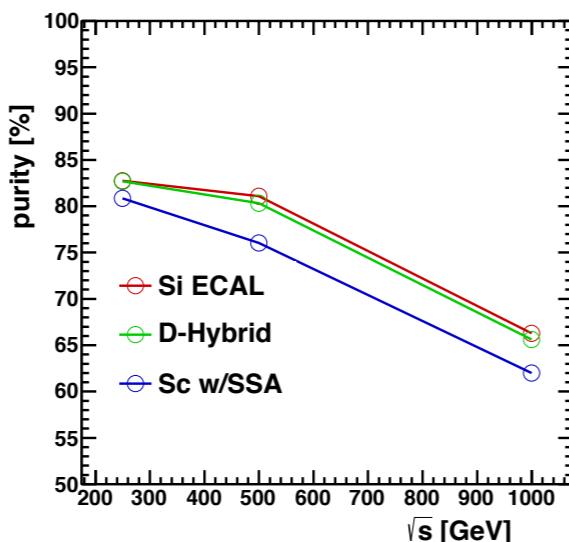
efficiency



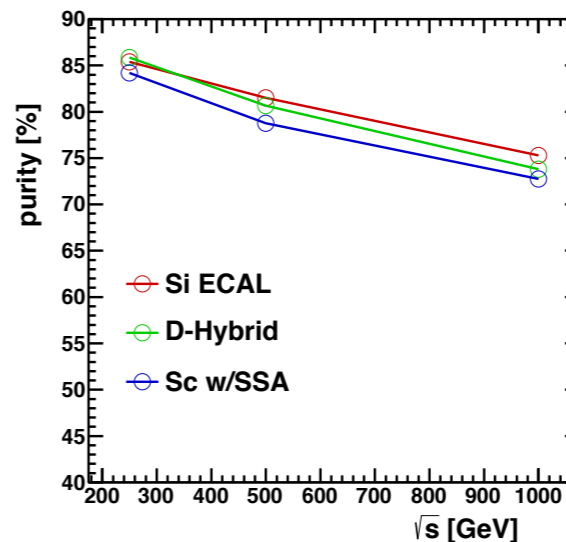
purity



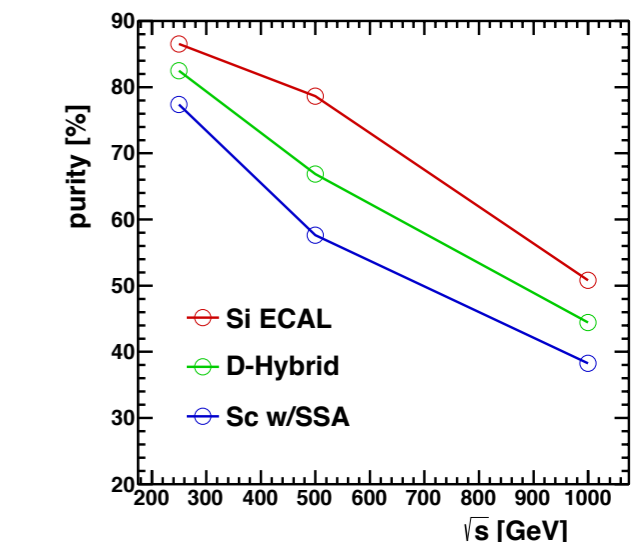
purity



purity



purity

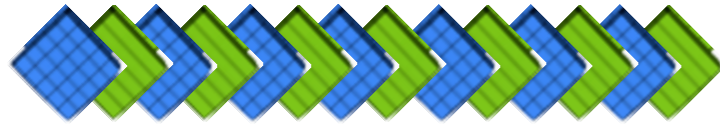




# Further Configurations

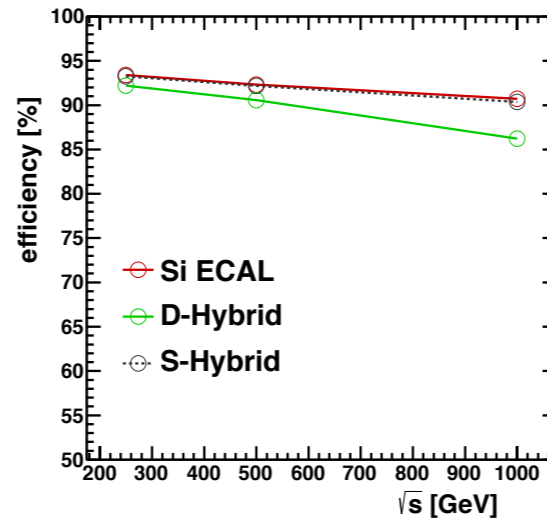
## - Configurations.

- SingleLayer Hybrid

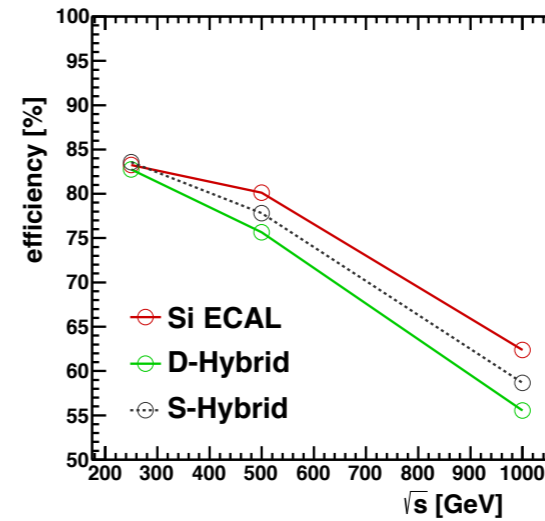


- Use Si 1-layer Sc 1-layer alternatively
- Can use precise information of Si layer and prevent ghost hit.
- Can expect almost the same performance of Si ECAL.

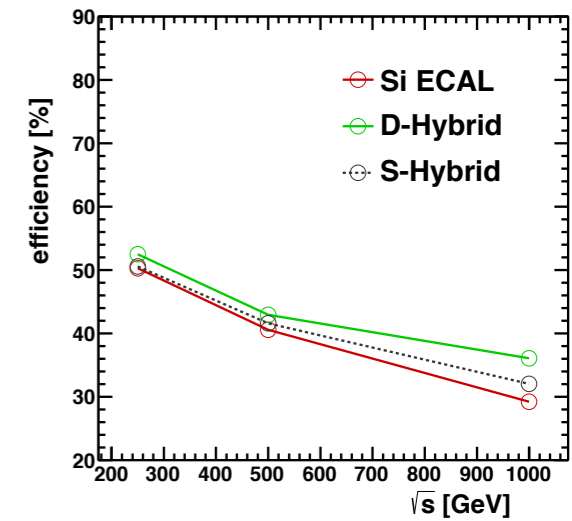
pi-mode efficiency



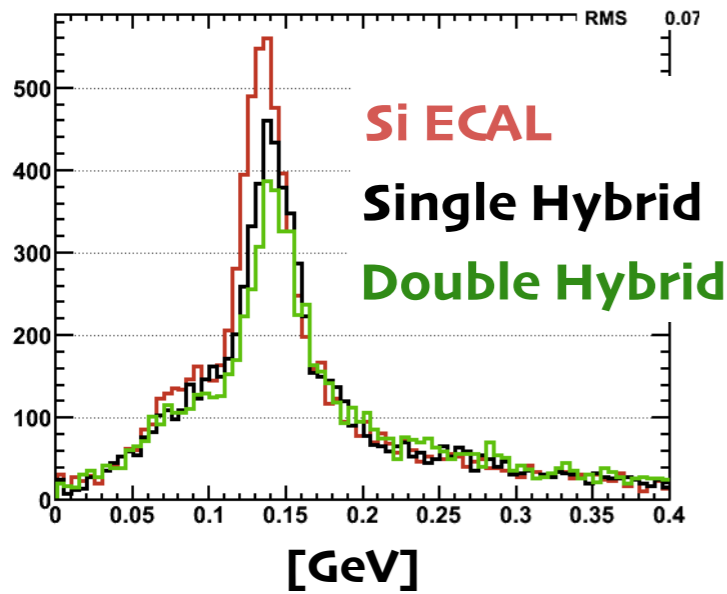
rho-mode efficiency



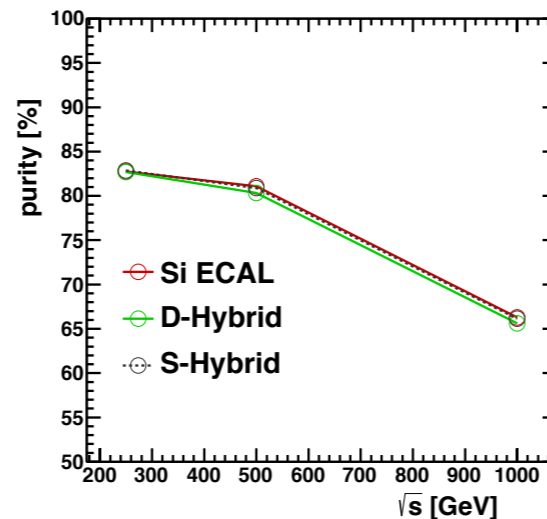
a1-mode efficiency



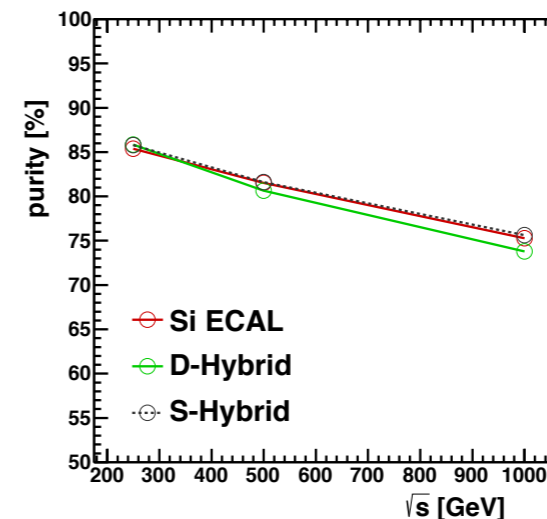
pi0 Mass at tau->rho exactly 2gammas



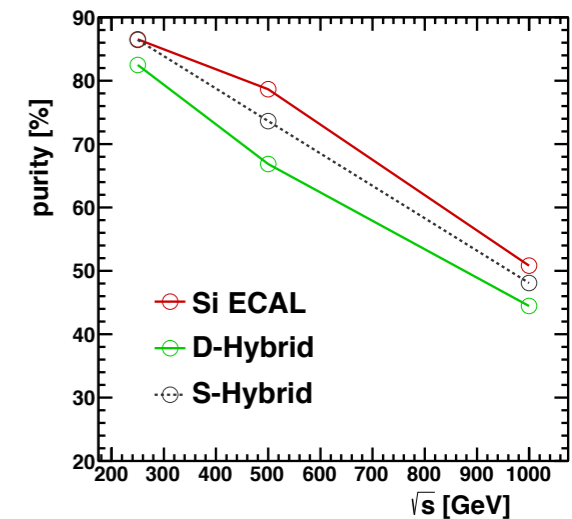
purity



purity



purity



## - Under progress.

- Scinti 45x5 + Scinti 10x10

# Polarization and Optimal observable $\omega$

- we can measure a polarization from the angular distribution of decay daughters.
  - the precise information of decay daughters is important
- The main observable are energies and angles of/between daughters in  $\tau$  rest-frame.
  - ( - Since the neutrino is not observed,  $E$  and  $\theta$  cannot be reconstructed completely. )
- Polarization calculation varies by decay modes.
- We can estimate by using optimal observable  $\omega$ .

- Leptonic decay :

$$\omega_l = \frac{1 + x - 8x^2}{5 + 5x - 4x^2}$$

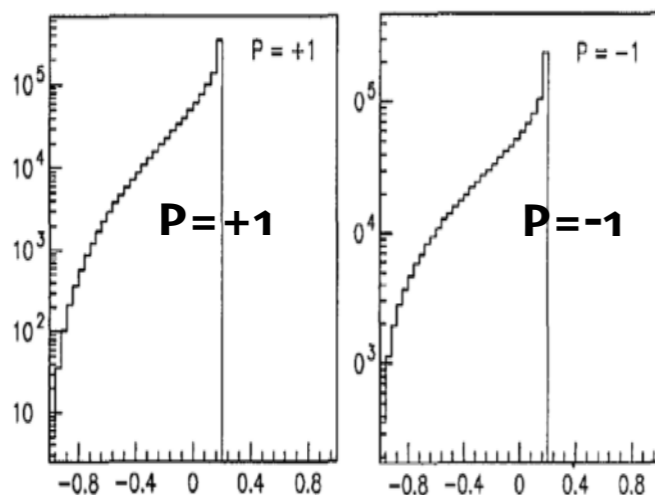
- Hadronic decay :

$$\omega_\pi = 2x - 1$$

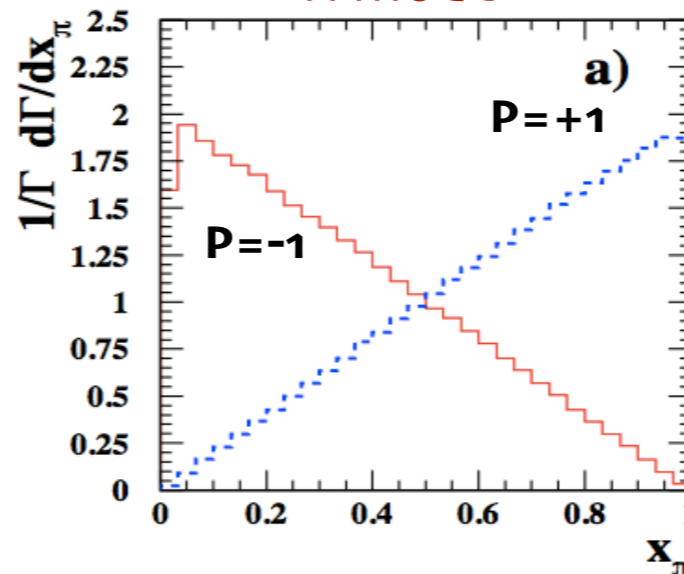
$$\omega_\rho = \frac{(-2 + \frac{m_\tau^2}{Q^2} + 2(1 + \frac{m_\tau^2}{Q^2}) \frac{3 \cos \psi - 1}{2} \frac{3 \cos^2 \beta - 1}{2}) \cos \theta + 3 \sqrt{\frac{m_\tau^2}{Q^2} \frac{3 \cos^2 \beta - 1}{2}} \sin 2\psi \sin \theta}{2 + \frac{m_\tau^2}{Q^2} - 2(1 - \frac{m_\tau^2}{Q^2}) \frac{3 \cos \psi - 1}{2} \frac{3 \cos^2 \beta - 1}{2}}$$

$$\cos \psi = \frac{x(m_\tau^2 + Q^2) - 2Q^2}{(m_\tau^2 - Q^2) \sqrt{x^2 - 4Q^2/s}}$$

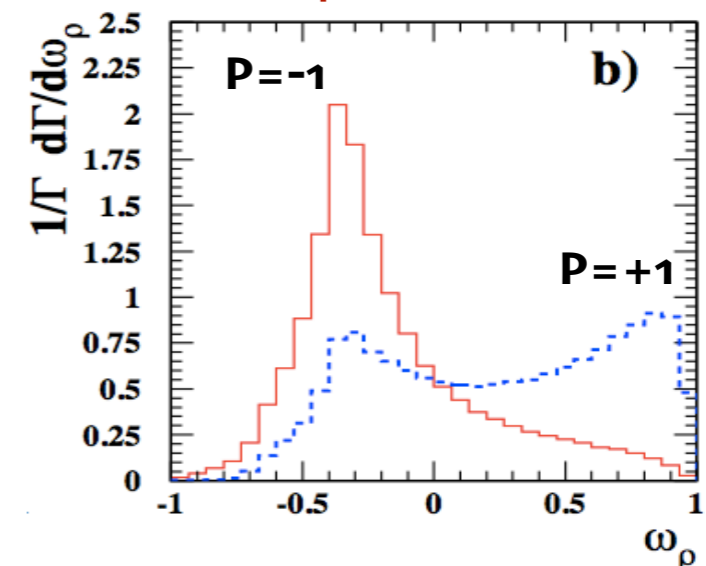
Leptonic



$\pi$  mode



$\rho$  mode



- So far, i do not consider a1 mode.

# Polarization with 3 Detectors

- Compared with 3 ECALs :  
Si ECAL, D-Hybrid, Sci w/SSA.

- Apply  $\omega$  formula on sample after some cut applied.

- Loose cut is used for mode selection.

- Initial beam polarization.

Beam polarized :  $e^-, e^+ = -80\%, +30\%$

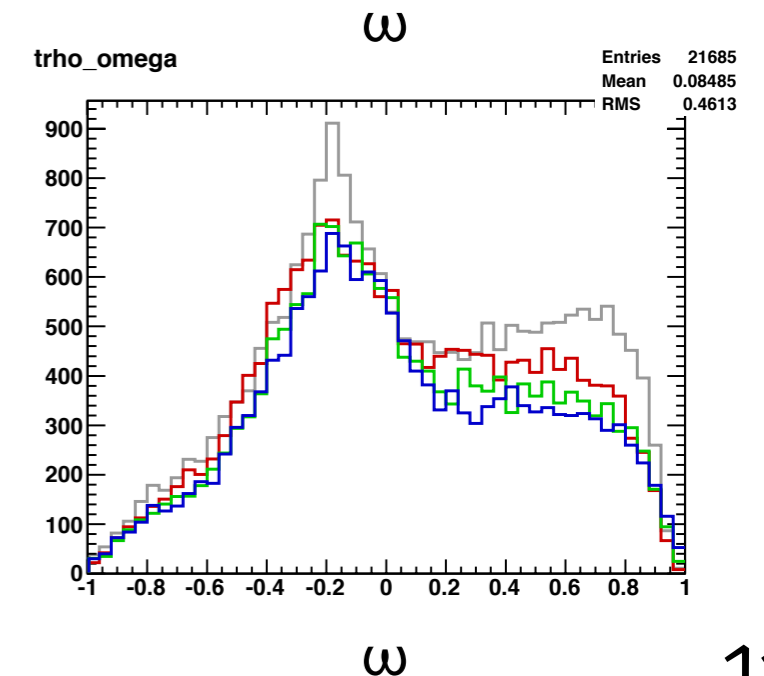
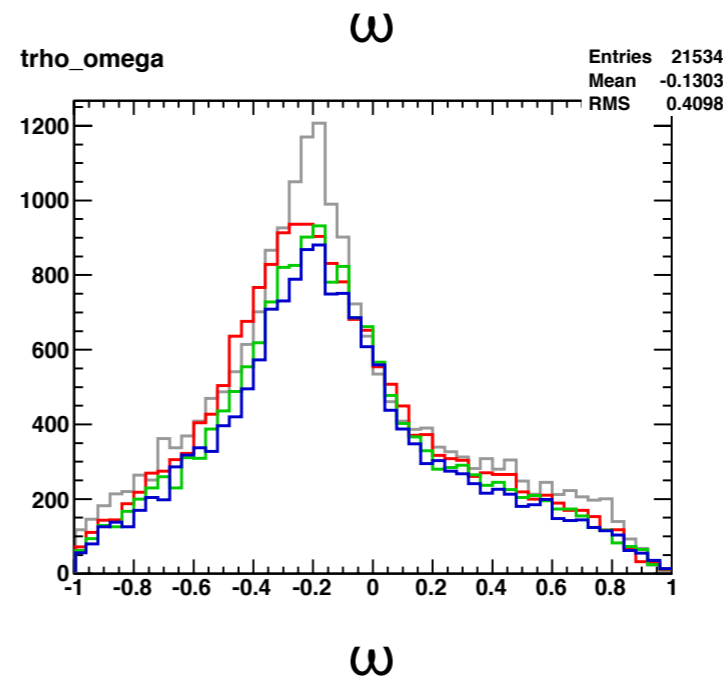
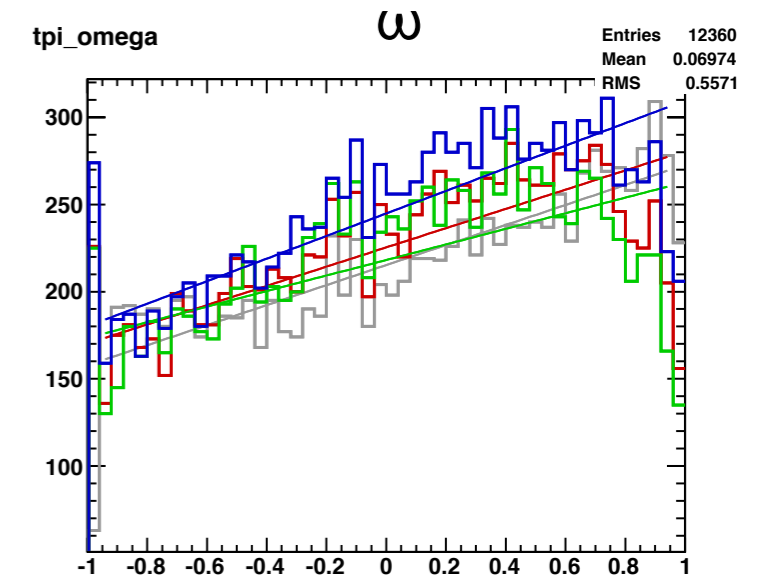
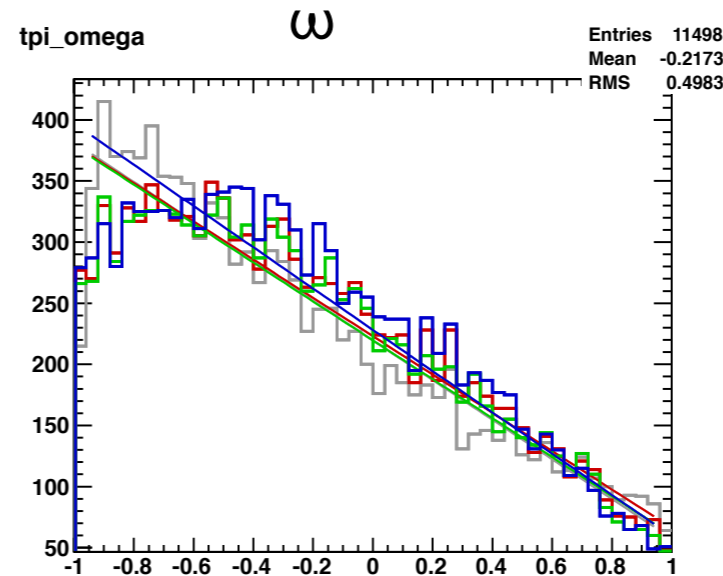
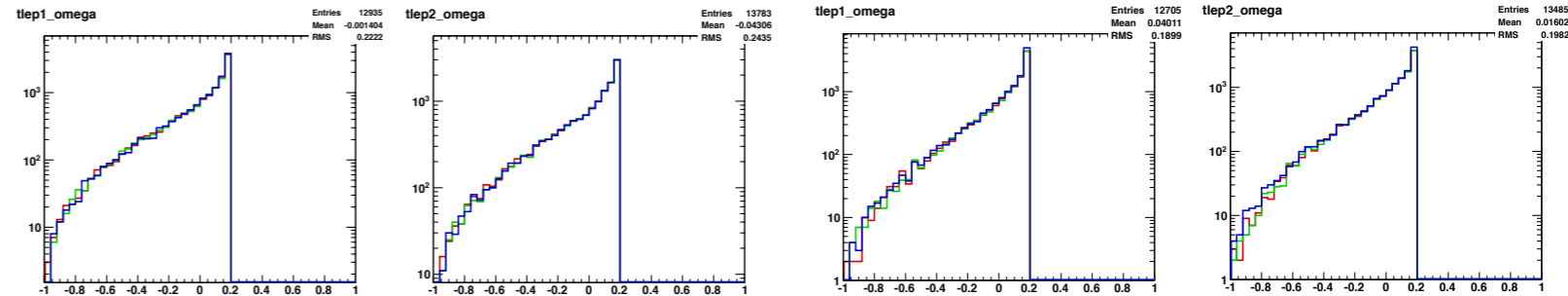
$e^-, e^+ = +80\%, -30\%$

Mtrue ———  
Si ECAL ———  
D-Hybrid ———  
Sci w/SSA ———

- difference appears at  $e^-, e^+ = +80\%, -30\%$

$e^-, e^+ = -80\%, +30\%$

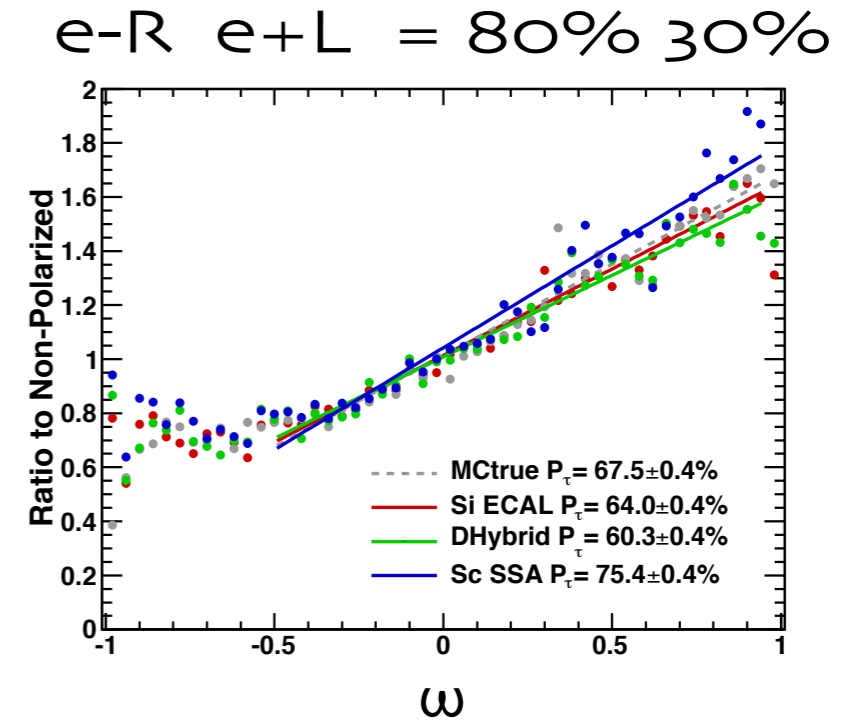
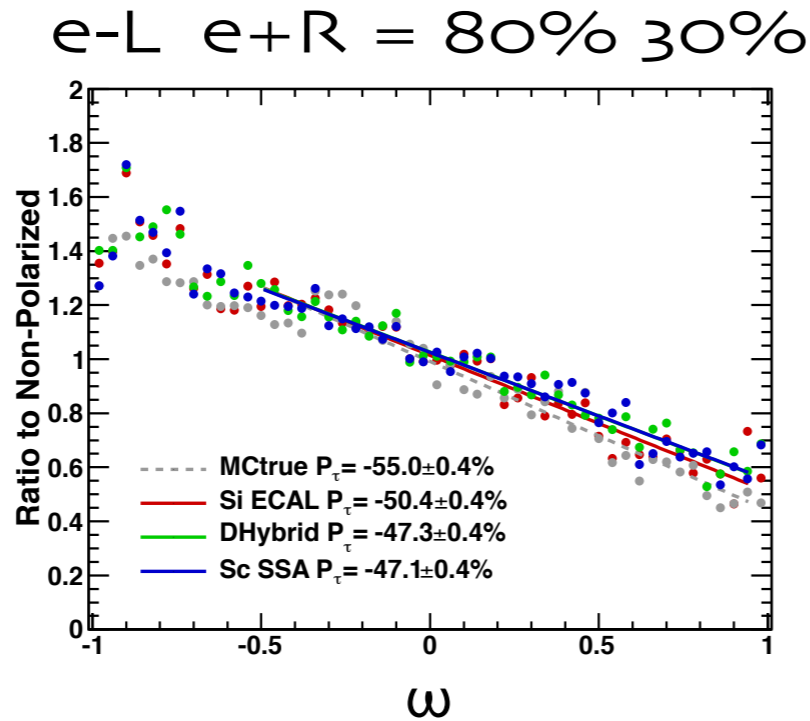
$e^-, e^+ = +80\%, -30\%$



# Polarization combined $\omega$ with 3Detectors

- Formula of  $\omega$  differs by decay modes,  
but  $\omega$  can be summed up through all decay modes.

→ Ratio to non-polarized sample.



- Obtained P( $\tau$ )
  - MC true : 55.0%
  - Si ECAL : 50.4%
  - DHybrid : 47.3%
  - Sc w/SSA : 47.1%

- MC true : 67.5%
- Si ECAL : 64.0%
- DHybrid : 60.3%
- Sc w/SSA : 75.4%

- estimated tau polarization and compared with 3ECALs.
- do not include error and need to analysis more precisely.

## Summary & Outlook

- I simulated tau-pair events with some ILD ECAL candidates to test ECAL performance.
- Decay mode identified with Cut base.
  - For leptonic decay, performance is almost same between 3ECALs.
  - For hadronic decay mainly rho and a1 mode, performance is different between 3ECALs.
    - rho mode : Efficiency of D-Hybrid and Sc w/SSA decrease 5% by 5% from one of Si ECAL.
    - a1 mode : **Efficiency of D-Hybrid and Sc w/SSA is almost same with one of Si ECAL.**  
**but purity decrease 10% by 10% from one of Si ECAL.**
- With increasing  $\sqrt{s}$  the gammas are closer and it is more difficult for even Si ECAL to reconstruct them.
- Simulation with further configuration is under progress.
  - Efficiency and purity of S-Hybrid is improved.
    - we can expect S-Hybrid will be almost the same performance of Si ECAL**
- And also, we compared tau polarization and the difference appears.
  - Including systematic error and need to analysis more precisely.

# Backup

# Comparison of Performance on Tau with ILD ECAL candidates

- we want to estimate the performance of ECALs with the ILD bench mark process  $ee \rightarrow \tau\tau$ .
  - Identifying and measuring gammas (from  $\pi^0$ s) in jets is already an important/crucial requirement.
  - Also, the full reconstruction of taus may be yet more challenging and the physics opportunities are potentially crucial. (Taus appear in many New Physics signatures)
  - At high energy, daughters of  $\tau$  decay are concentrated in a very narrow angle and a narrow area due to the Lorentz boost.
- it is difficult to separate particles with PFA (). → ILD demands well segmented ECAL. .

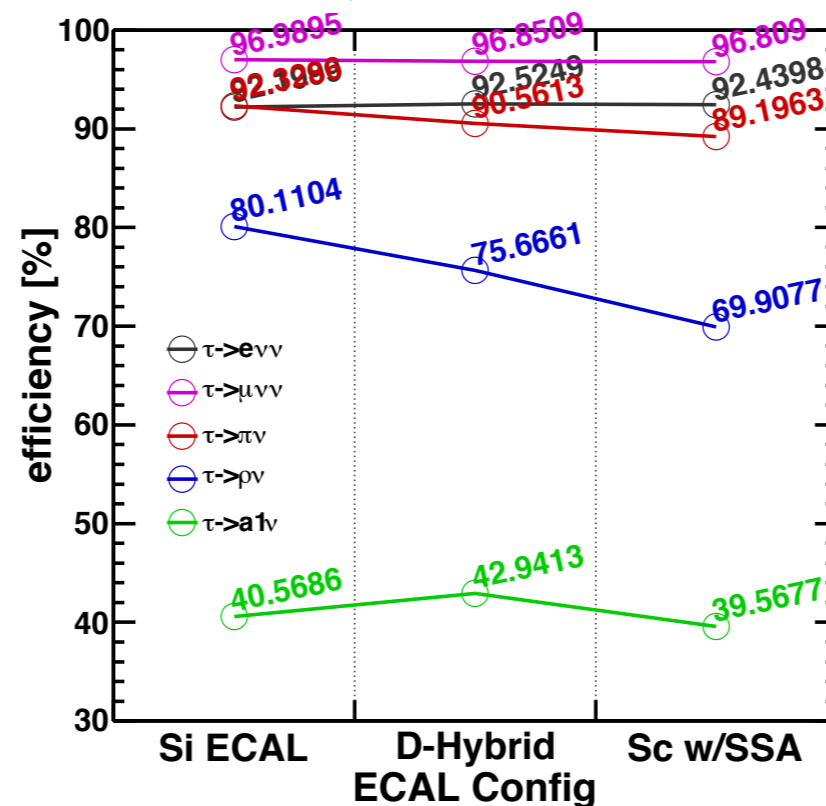
I compared tau reconstruction

1-prong decay  
e, mu, pi, rho, a1

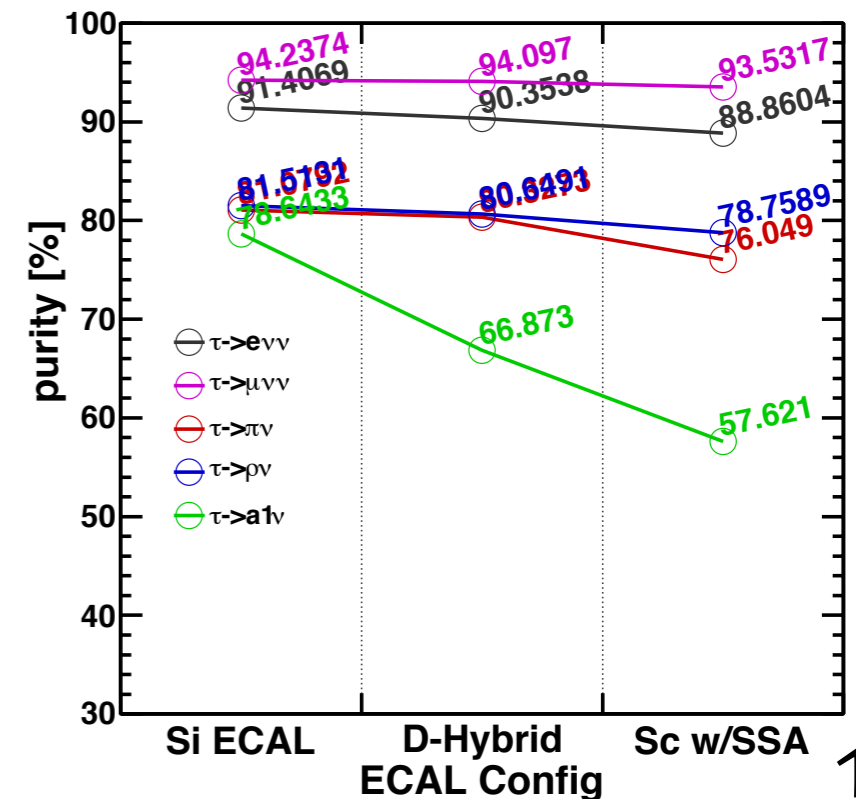
with some ECALs

Si ECAL, Hybrid, Sci ECAL

efficiency



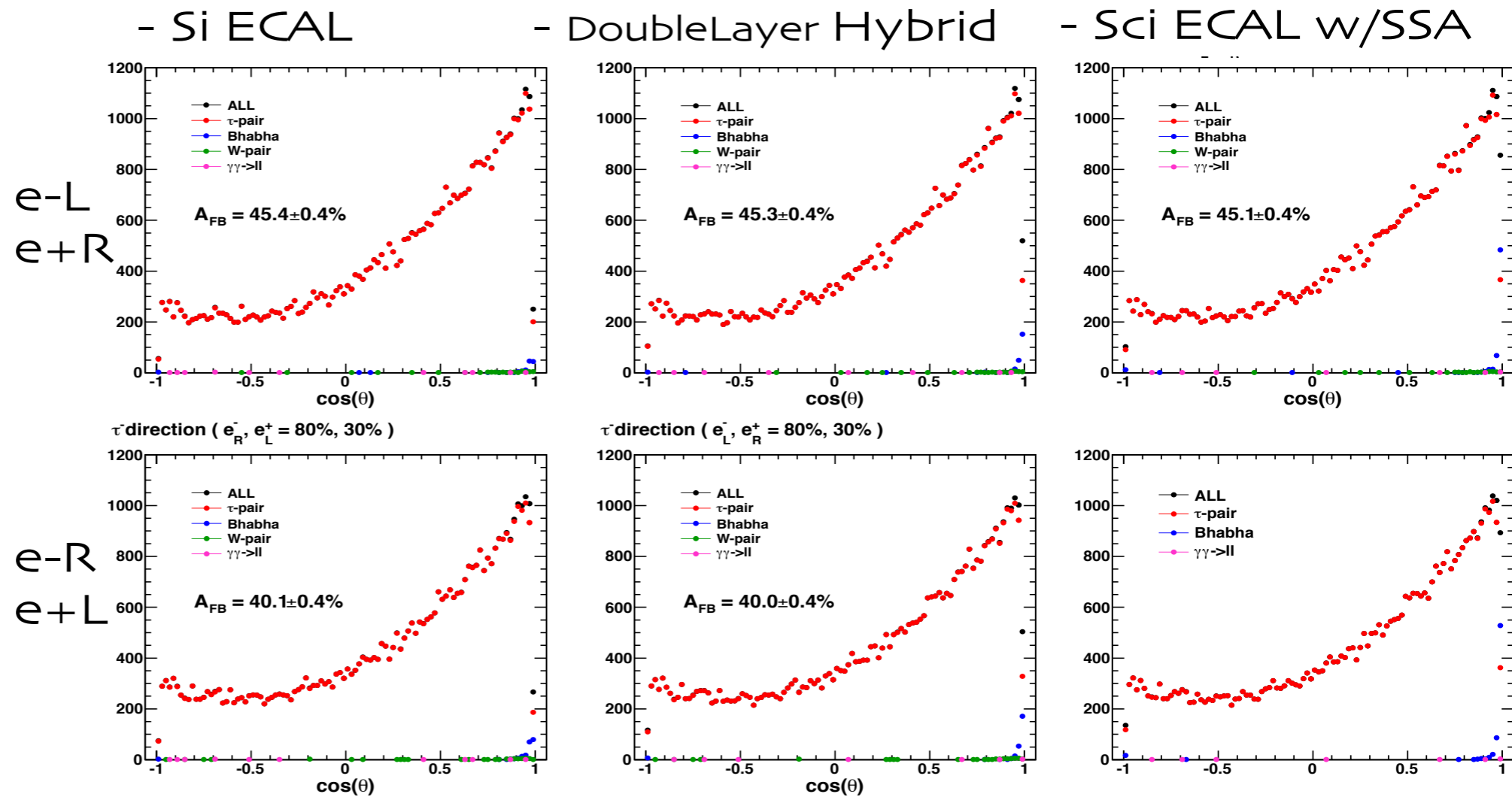
purity





# Forward-Backward Asymmetry

- Angular distribution of tau- ( $-0.99 < \cos\theta < 0.99$ )



→ Afb does not depend on ECAL geometries.

But need to consider BG properly.

	e-L, e+R	e-R, e+L
Si Ecal	$45.4 \pm 0.4\%$	$40.1 \pm 0.4\%$
Hybrid	$45.3 \pm 0.4\%$	$40.0 \pm 0.4\%$
Sc SSA	$45.1 \pm 0.4\%$	$40.4 \pm 0.2\%$

# Miss Selection with **Loose Cut**

## - Comparison of Detectors in each decay

### - Si ECAL

Reconstructed mode

decay mode

(%)	$\pi$	$\rho$	a1
e	1.27	2.53	3.98
$\mu$	1.03	1.67	2.51
$\pi$	<b>92.30</b>	5.65	2.89
$\rho$	3.74	<b>80.11</b>	38.61
a1	0.30	3.49	<b>40.57</b>
x	1.36	6.55	11.47

### - DoubleLayer Hybrid

Reconstructed mode

decay mode

(%)	$\pi$	$\rho$	a1
e	1.25	3.05	4.21
$\mu$	0.98	1.55	2.30
$\pi$	<b>90.56</b>	6.04	3.18
$\rho$	5.41	<b>75.67</b>	35.25
a1	0.44	6.98	<b>42.94</b>
x	1.36	6.71	12.12

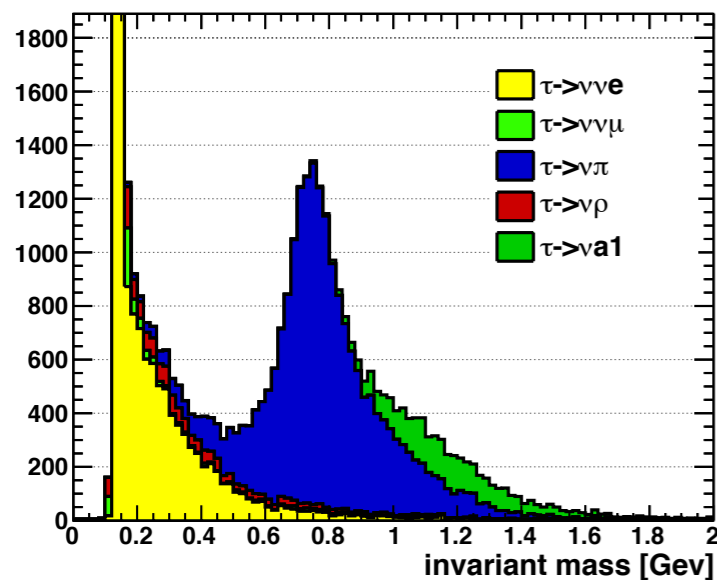
### - Sci ECAL w/SSA

Reconstructed mode

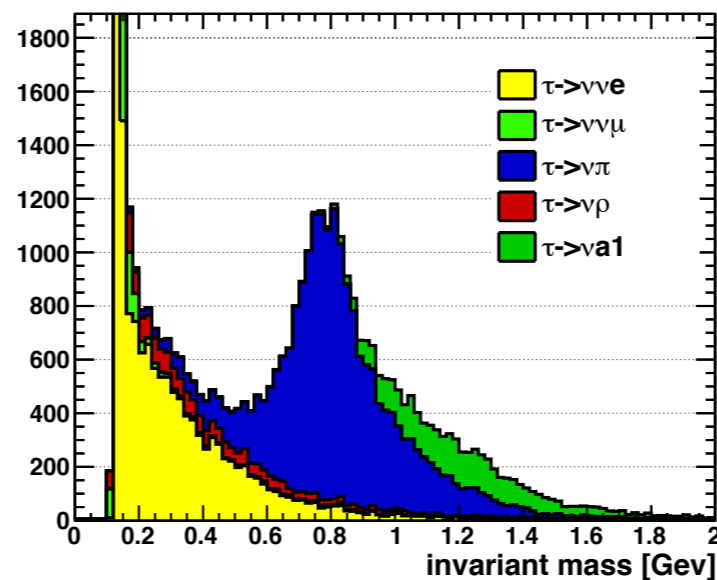
decay mode

(%)	$\pi$	$\rho$	a1
e	1.53	3.45	4.90
$\mu$	1.11	1.65	2.35
$\pi$	<b>89.19</b>	8.52	4.06
$\rho$	6.03	<b>69.90</b>	36.35
a1	0.76	9.68	<b>39.57</b>
x	1.38	6.80	12.77

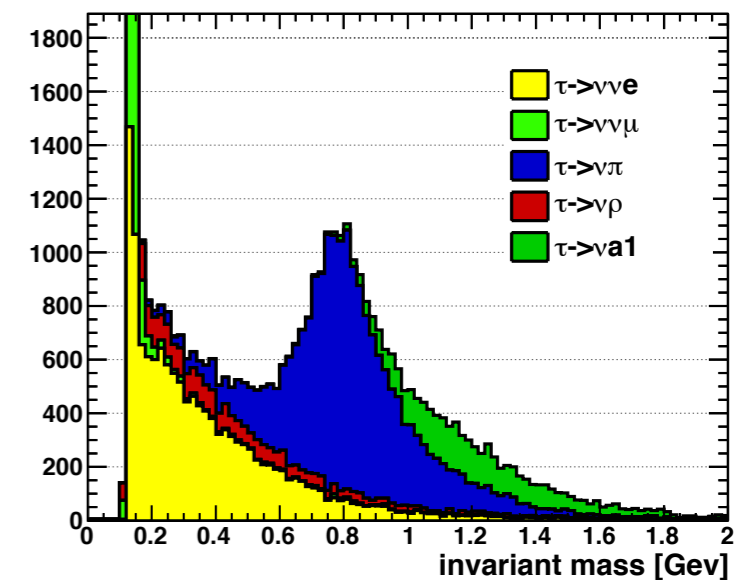
1-Prong Mass Dist



1-Prong Mass Dist



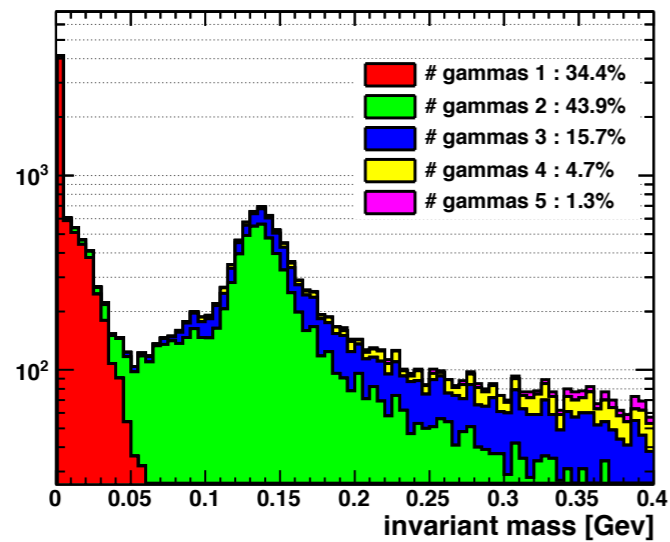
1-Prong Mass Dist



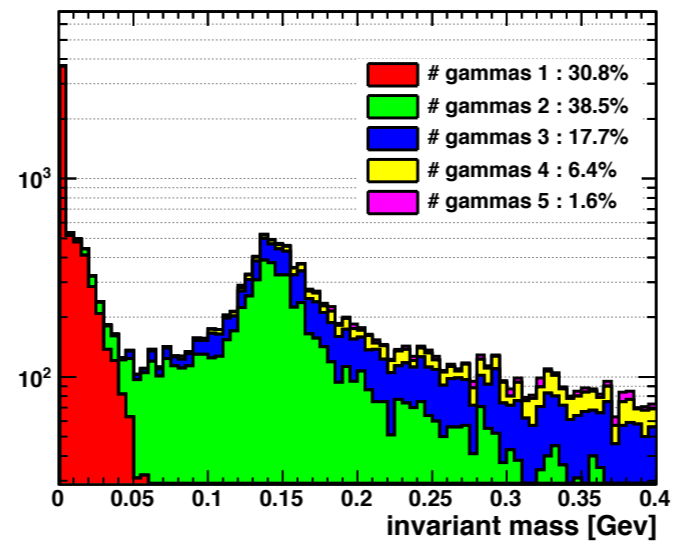
# PiO at Rho mode with **Loose Cut**

## - Comparison of Detectors.

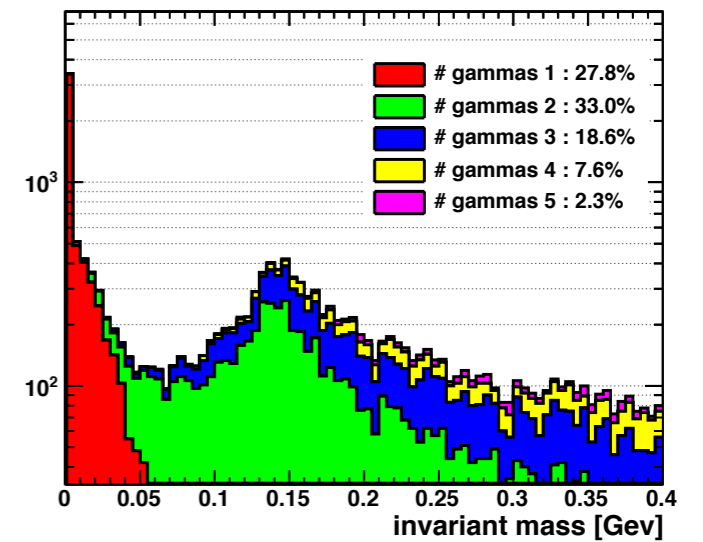
- Si ECAL



- DoubleLayer Hybrid

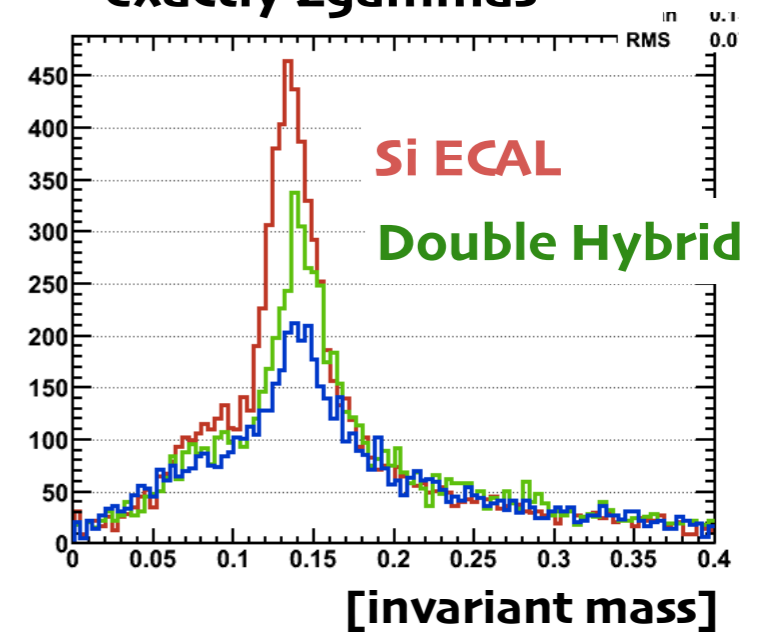


- Sci ECAL w/SSA



## - Exactly 2-gammas.

piO Mass at tau->rho  
exactly 2gammas



# MVA input Variables

## - Training sample

Training on each mode

$\sqrt{500\text{GeV}}$  e-Le+R  $\rightarrow$  tau-tau+

tau  $\rightarrow$  only e decay (mu, pi, rho, a1p1)

## - MVA input variables.

1. #of gamma clusters.
2. Sum of gamma energy.
3. Mass of gamma clusters.
4. #of calorimeter Hits.
5. Sum of neutron energy.
6. Track energy.
7. ECAL E / Total E.
8. Hit E / Track E.
9. Mass of track+gammas.

## - Method is BDT

Response : 0 ( false )  $\sim$  1 ( true )

e mode Response  $>$  0.7

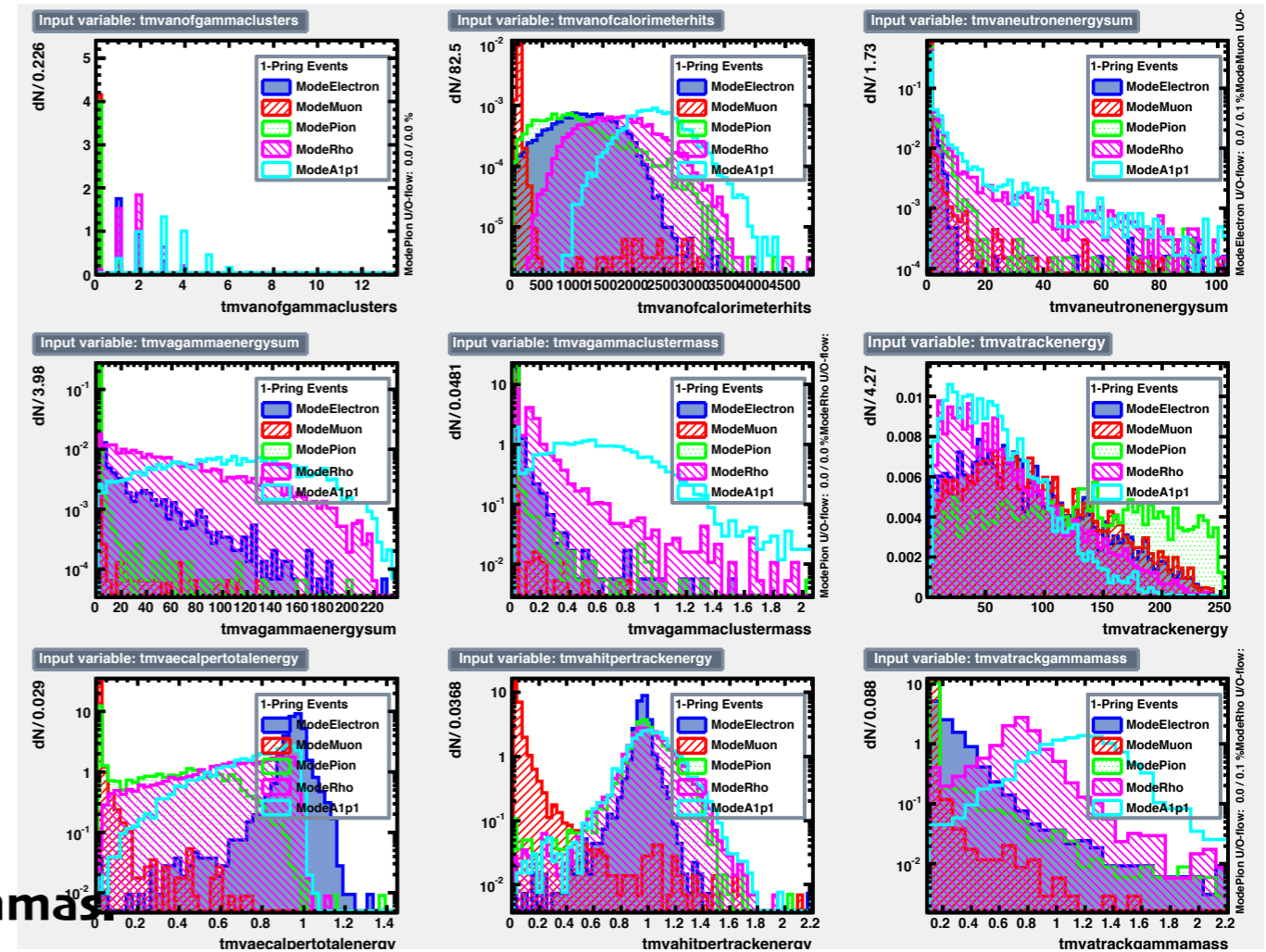
$\mu$  mode Response  $>$  0.7

$\pi$  mode Response  $>$  0.3

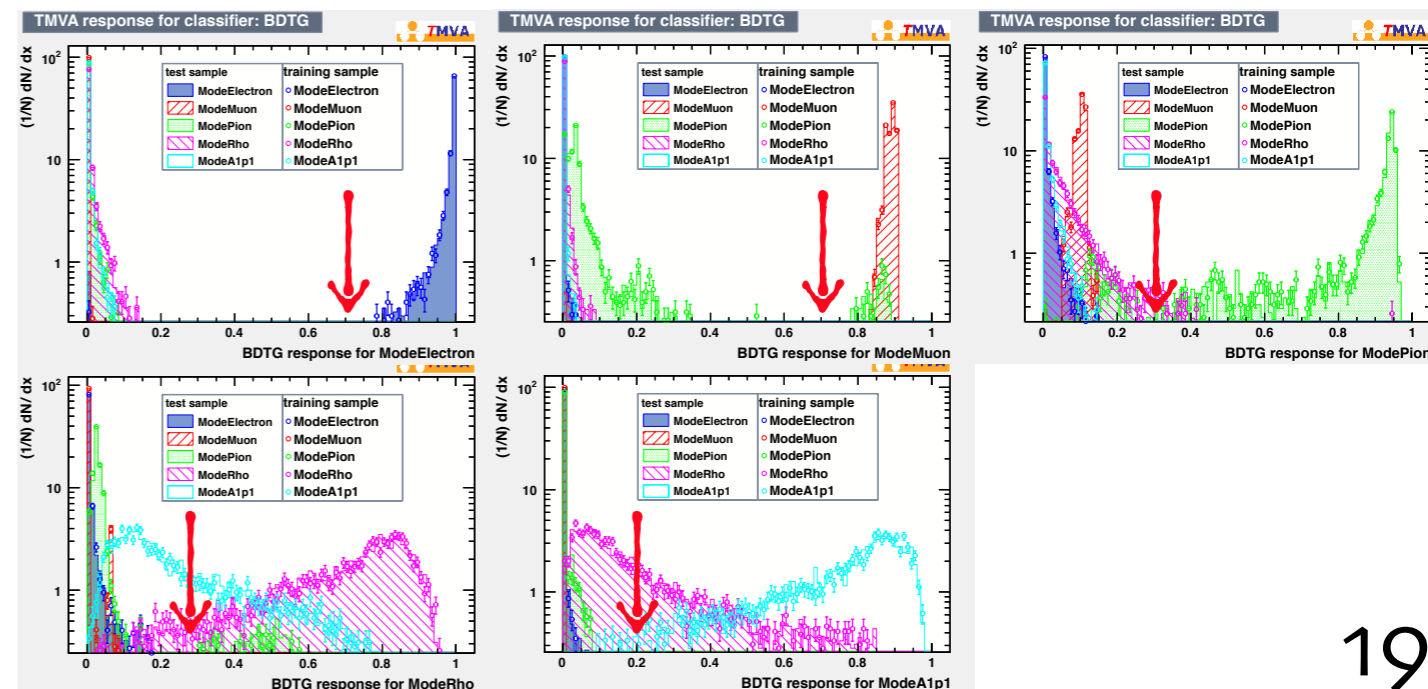
$\rho$  mode Response  $>$  0.28

a1p1 mode Response  $>$  0.2

## Distribution of input variables ( in case of Si ECAL )



## MVA response ( in case of Si ECAL )



# Comparison of Cut Method in Si ECAL

## - Comparison of Cut Method

-  $\sqrt{500\text{GeV}}$  e-Le+R  $\rightarrow$  tau-tau+

- Detector

In case of Si ECAL.

- Only 1-prong decay

e, mu, pi, rho, a1p1

- Cut

Loose Cut, MVA Cut.

- MVA Cut

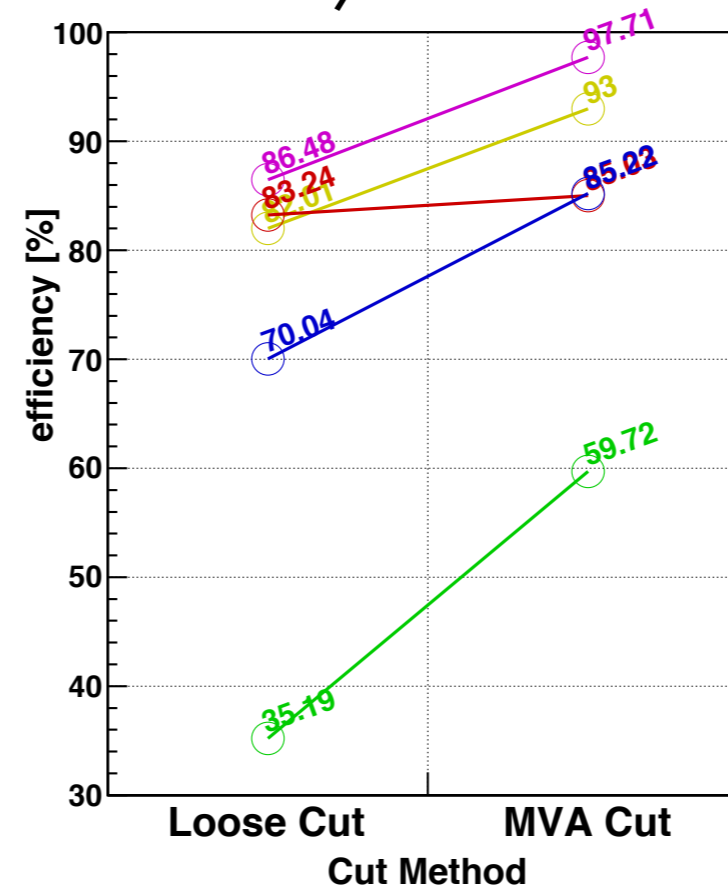
is over 80% on both efficiency and purity ( except a1p1 decay ).

- Miss Selection

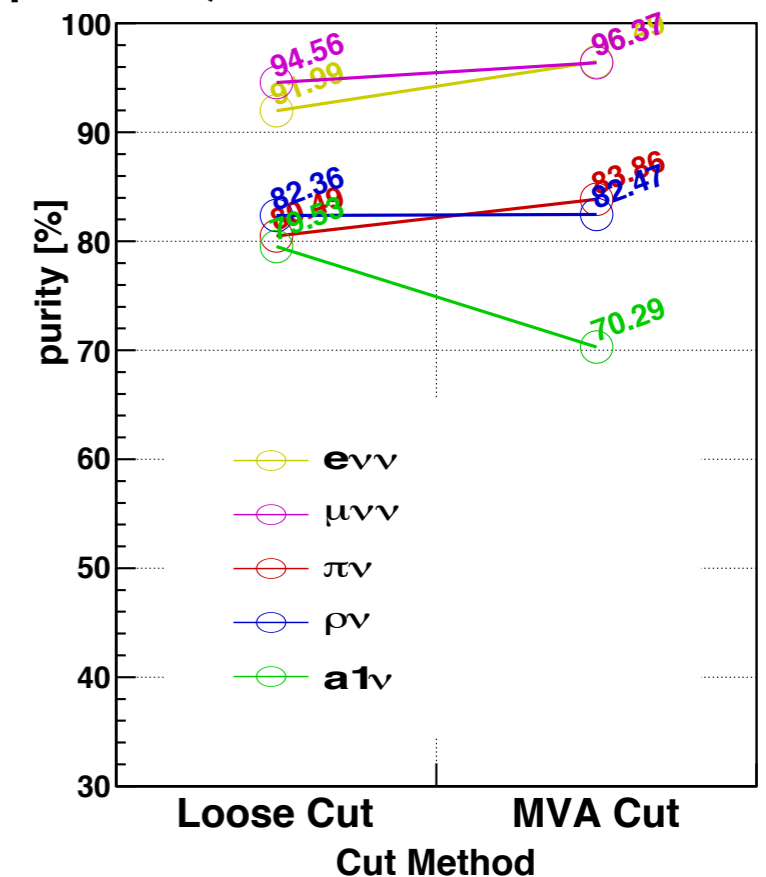
In case of Loose Cut, ratio is 16.54%.

In case of MVA Cut, ratio is 13.34%.

### efficiency



### purity



# Efficiency & purity with **MVA Cut**

## - Comparison of Detectors

-  $\sqrt{500\text{GeV}}$  e-Le+R  $\rightarrow$  tau-tau+

## - Detectors

Si ECAL,

DoubleLayer Hybrid

Sci ECAL w/SSA

## - Cut

**MVA Cut**

## - Efficiency & Purity

- Improved generally by MVA
- In reconstruction of leptonic decay, efficiency and purity are almost same.
- In reconstruction of hadronic decay, efficiency and purity are difference.

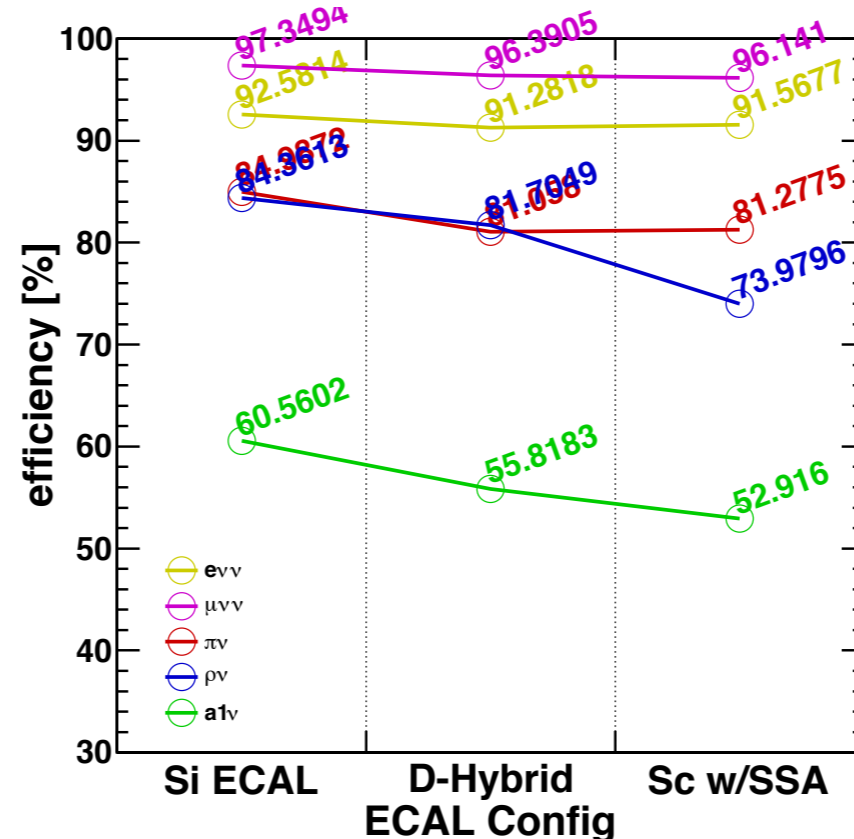
( Good ) Si ECAL > DoubleLayer Hybrid > Sci w/SSA ( Not good )

## - Miss Selection

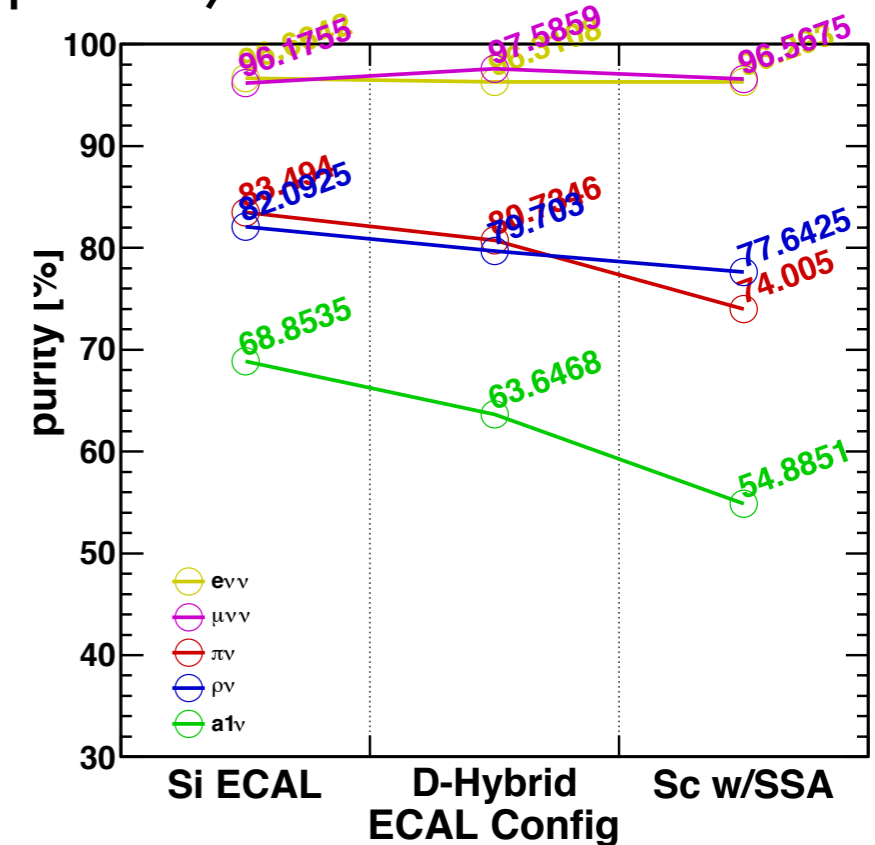
- Also miss selection is difference.

( Less ) Si ECAL **13.34%** > DoubleLayer Hybrid **15.19%** > Sci w/SSA **18.23%** ( Not less )

efficiency



purity





# Miss Selection with **MVA** Cut

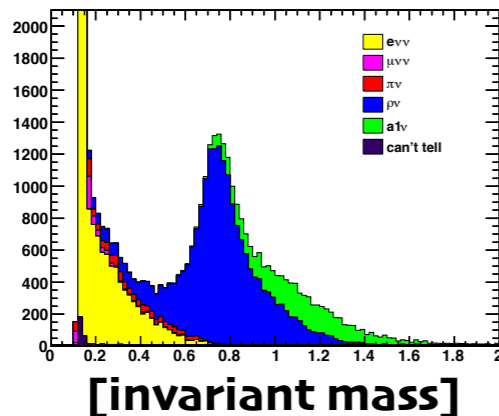
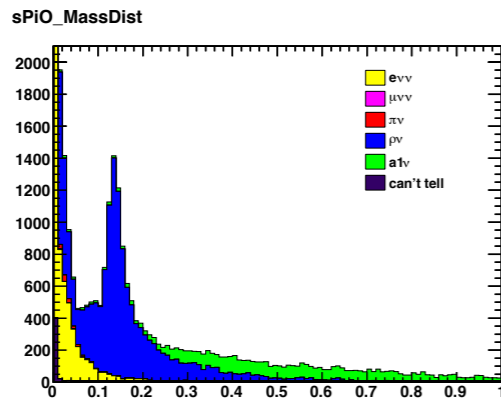
## - Comparison of Detectors in each decay

### - Si ECAL

#### Reconstructed mode

decay mode

(%)	$\pi$	$\rho$	a1
e	1.25	0.95	0.74
$\mu$	4.09	0.14	0.09
$\pi$	<b>84.99</b>	<b>5.53</b>	<b>1.20</b>
$\rho$	<b>5.98</b>	<b>84.36</b>	<b>37.24</b>
a1	<b>1.41</b>	<b>8.45</b>	<b>60.56</b>
x	2.28	0.57	0.17

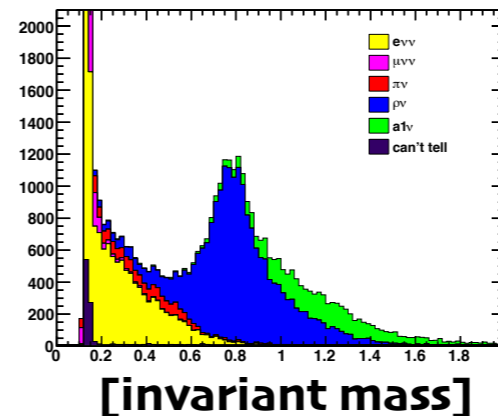
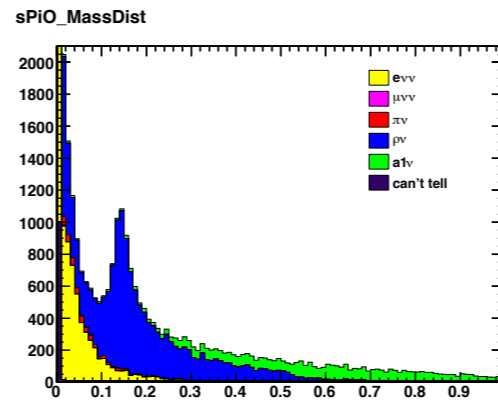


### - DoubleLayer Hybrid

#### Reconstructed mode

decay mode

(%)	$\pi$	$\rho$	a1
e	1.52	1.01	0.65
$\mu$	2.11	0.07	0.07
$\pi$	<b>81.06</b>	<b>6.96</b>	<b>1.27</b>
$\rho$	<b>6.95</b>	<b>81.70</b>	<b>42.02</b>
a1	<b>1.72</b>	<b>9.57</b>	<b>55.82</b>
x	6.11	0.69	0.17

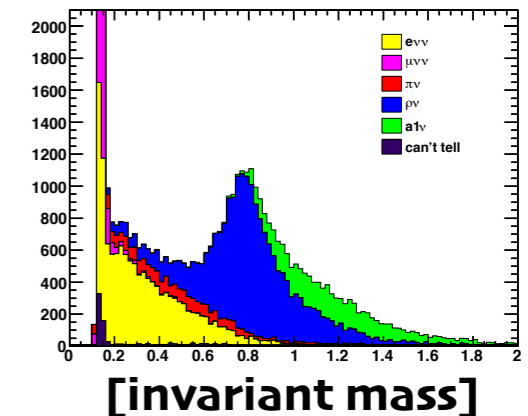
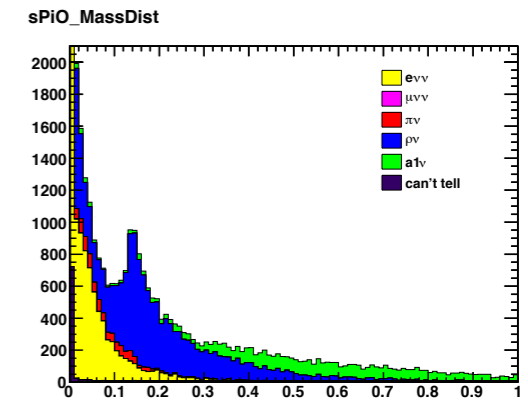


### - Sci ECAL w/SSA

#### Reconstructed mode

decay mode

(%)	$\pi$	$\rho$	a1
e	1.71	0.97	0.60
$\mu$	3.12	0.14	0.11
$\pi$	<b>81.28</b>	<b>10.76</b>	<b>2.54</b>
$\rho$	<b>7.35</b>	<b>73.98</b>	<b>43.71</b>
a1	<b>2.34</b>	<b>13.24</b>	<b>52.96</b>
x	4.2	0.91	0.08





# 3 Detectors @ tautau with Loose Cut

## Si ECAL thick 0.5mm

Efficiency, Purity & Acceptance  
( with **Loose Cut** )

Lepton1Mode Efficiency = 81.21  
Lepton1Mode Purity = 91.99  
Lepton1Mode Acceptance = 88.27

Lepton2Mode Efficiency = 86.48  
Lepton2Mode Purity = 94.56  
Lepton2Mode Acceptance = 91.46

PionMode Efficiency = 83.24  
PionMode Purity = 80.49  
PionMode Acceptance = 103.4

RhoMode Efficiency = 70.04  
RhoMode Purity = 82.36  
RhoMode Acceptance = 85.04

A1p1Mode Efficiency = 35.19  
A1p1Mode Purity = 79.53  
A1p1Mode Acceptance = 44.25

MissSelectionRatio = 16.54

## A Double Layer Sci-thick 1.0mm

Efficiency, Purity & Acceptance  
( with **Loose Cut** )

Lepton1Mode Efficiency = 80.98  
Lepton1Mode Purity = 91.13  
Lepton1Mode Acceptance = 88.86

Lepton2Mode Efficiency = 86.05  
Lepton2Mode Purity = 95.15  
Lepton2Mode Acceptance = 90.44

PionMode Efficiency = 80.02  
PionMode Purity = 78.47  
PionMode Acceptance = 101.9

RhoMode Efficiency = 66.30  
RhoMode Purity = 81.20  
RhoMode Acceptance = 81.65

A1p1Mode Efficiency = 37.37  
A1p1Mode Purity = 69.18  
A1p1Mode Acceptance = 54.01

MissSelectionRatio = 18.97

## Sci w/ SSA Sci-thick 1.0mm

Efficiency, Purity & Acceptance  
( with **Loose Cut** )

Lepton1Mode Efficiency = 81.10  
Lepton1Mode Purity = 90.31  
Lepton1Mode Acceptance = 89.79

Lepton2Mode Efficiency = 86.39  
Lepton2Mode Purity = 94.78  
Lepton2Mode Acceptance = 91.15

PionMode Efficiency = 79.29  
PionMode Purity = 77.77  
PionMode Acceptance = 101.9

RhoMode Efficiency = 63.58  
RhoMode Purity = 80.25  
RhoMode Acceptance = 79.22

A1p1Mode Efficiency = 36  
A1p1Mode Purity = 59.28  
A1p1Mode Acceptance = 60.74

MissSelectionRatio = 20.39

# 3 Detectors @ tautau with MVA Cut

## Si ECAL thick 0.5mm

Efficiency, Purity & Acceptance  
( with **MVA Cut** )

Lepton1Mode Efficiency = 93.00  
Lepton1Mode Purity = 96.49  
Lepton1Mode Acceptance = 96.38

Lepton2Mode Efficiency = 97.71  
Lepton2Mode Purity = 96.37  
Lepton2Mode Acceptance = 101.4

PionMode Efficiency = 85.03  
PionMode Purity = 83.86  
PionMode Acceptance = 101.4

RhoMode Efficiency = 85.22  
RhoMode Purity = 82.47  
RhoMode Acceptance = 103.3

A1p1Mode Efficiency = 59.72  
A1p1Mode Purity = 70.29  
A1p1Mode Acceptance = 84.96

MissSelectionRatio = 13.34

## ADoubleLayer Sci-thick 1.0mm

Efficiency, Purity & Acceptance  
( with **MVA Cut** )

Lepton1Mode Efficiency = 92.22  
Lepton1Mode Purity = 96.42  
Lepton1Mode Acceptance = 95.64

Lepton2Mode Efficiency = 96.76  
Lepton2Mode Purity = 97.77  
Lepton2Mode Acceptance = 98.97

PionMode Efficiency = 81.53  
PionMode Purity = 80.59  
PionMode Acceptance = 101.2

RhoMode Efficiency = 82.96  
RhoMode Purity = 80.56  
RhoMode Acceptance = 102.9

A1p1Mode Efficiency = 56.36  
A1p1Mode Purity = 65.63  
A1p1Mode Acceptance = 85.88

MissSelectionRatio = 15.19

## Sci w/ SSA Sci-thick 1.0mm

Efficiency, Purity & Acceptance  
( with **MVA Cut** )

Lepton1Mode Efficiency = 92.78  
Lepton1Mode Purity = 96.73  
Lepton1Mode Acceptance = 95.92

Lepton2Mode Efficiency = 96.42  
Lepton2Mode Purity = 97.02  
Lepton2Mode Acceptance = 99.38

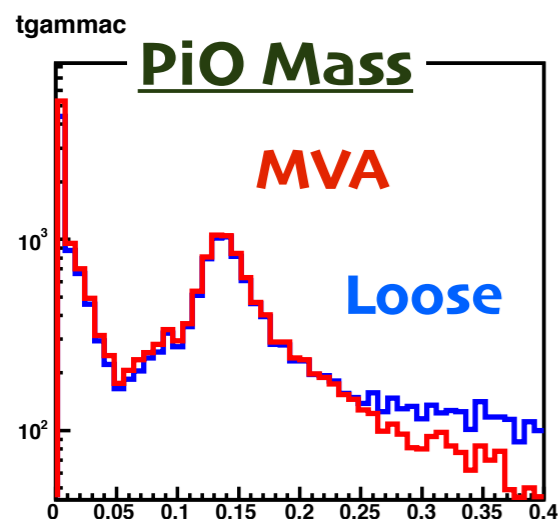
PionMode Efficiency = 81.24  
PionMode Purity = 74.28  
PionMode Acceptance = 109.38

RhoMode Efficiency = 74.33  
RhoMode Purity = 77.98  
RhoMode Acceptance = 95.32

A1p1Mode Efficiency = 53.16  
A1p1Mode Purity = 54.96  
A1p1Mode Acceptance = 96.70

MissSelectionRatio = 18.23

# Si ECAL @ tautau



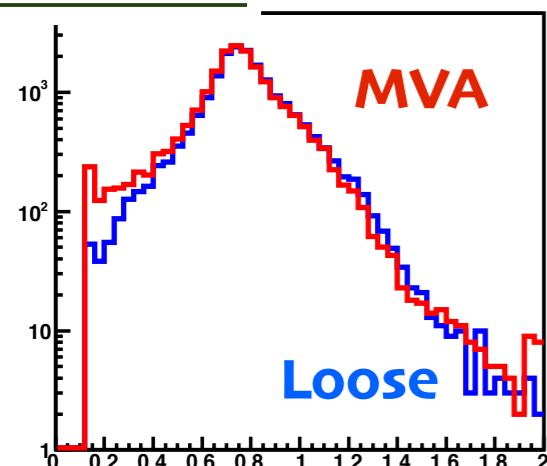
Efficiency, Purity & Acceptance  
( with **Loose Cut** )

Lepton1Mode Efficiency = 81.21  
Lepton1Mode Purity = 91.99  
Lepton1Mode Acceptance = 88.27

Efficiency, Purity & Acceptance  
( with **MVA Cut** )

Lepton1Mode Efficiency = 93.00  
Lepton1Mode Purity = 96.49  
Lepton1Mode Acceptance = 96.38

## Rho Mass



Lepton2Mode Efficiency = 86.48  
Lepton2Mode Purity = 94.56  
Lepton2Mode Acceptance = 91.46

Lepton2Mode Efficiency = 97.71  
Lepton2Mode Purity = 96.37  
Lepton2Mode Acceptance = 101.4

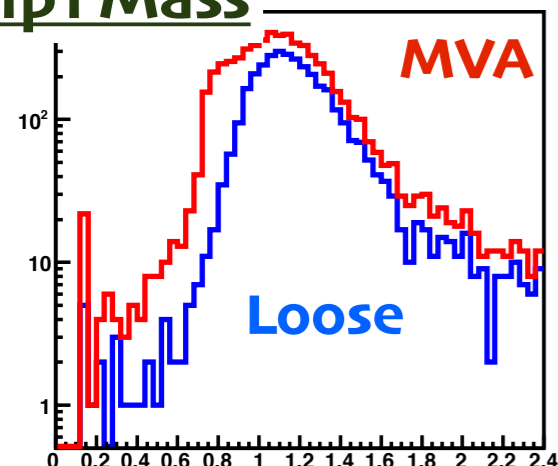
PionMode Efficiency = 83.24  
PionMode Purity = 80.49  
PionMode Acceptance = 103.4

PionMode Efficiency = 85.03  
PionMode Purity = 83.86  
PionMode Acceptance = 101.4

RhoMode Efficiency = 70.04  
RhoMode Purity = 82.36  
RhoMode Acceptance = 85.04

RhoMode Efficiency = 85.22  
RhoMode Purity = 82.47  
RhoMode Acceptance = 103.3

## a1p1 Mass



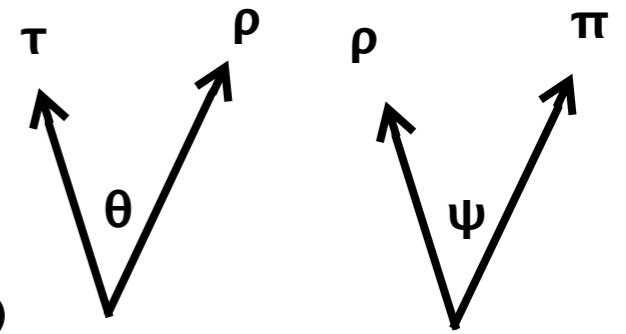
A1p1Mode Efficiency = 35.19  
A1p1Mode Purity = 79.53  
A1p1Mode Acceptance = 44.25

A1p1Mode Efficiency = 59.72  
A1p1Mode Purity = 70.29  
A1p1Mode Acceptance = 84.96

MissSelectionRatio = 16.54

MissSelectionRatio = 13.34

# Polarization observables $\omega$



Recover optimal observable  $\omega$  with  $\cos\psi^*$  in  $\rho$  mode. ( BackUp Slides )

A lot of sensitivity of the polarization is lost compared to the  $\pi$  decay.

→ due to the mixing of longitudinally and transversely polarized vector states.

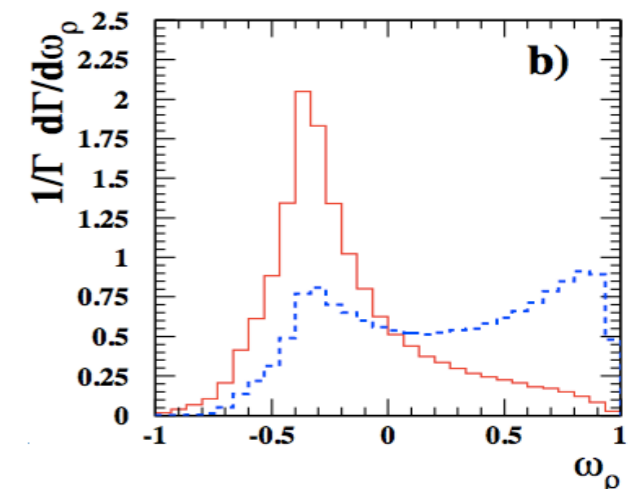
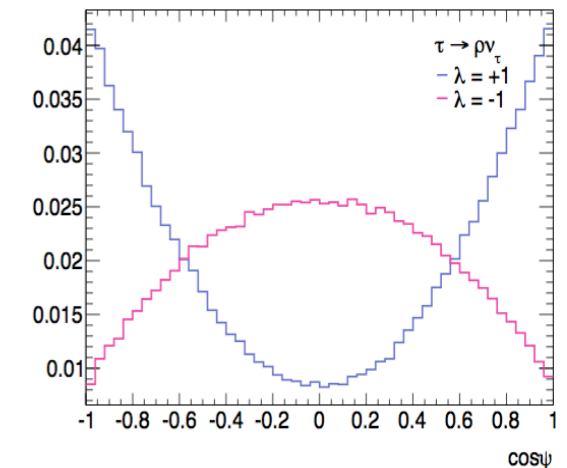
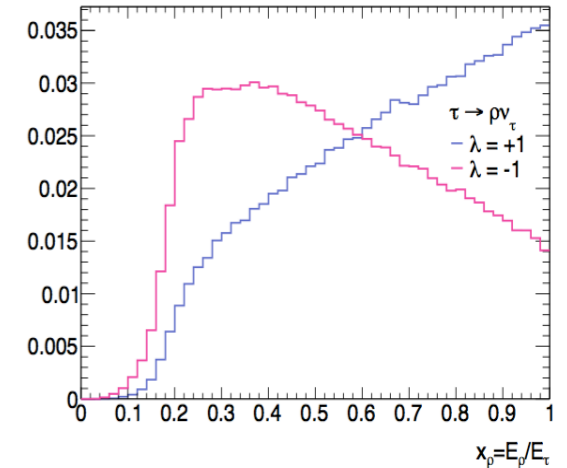
Some of the sensitivity can be regained by considering other variables are sensitive to the tau helicity.

- If one uses information of helicity of intermediate resonance, most of lost sensitivity can be regained.

→ Define  $\psi$  as the angle between the charged  $\pi$  and the  $\rho$  initial direction

- In terms of the laboratory frame

$$\cos\psi^* = (E_{\pi^\pm} - E_{\pi^0}) / E_\rho$$



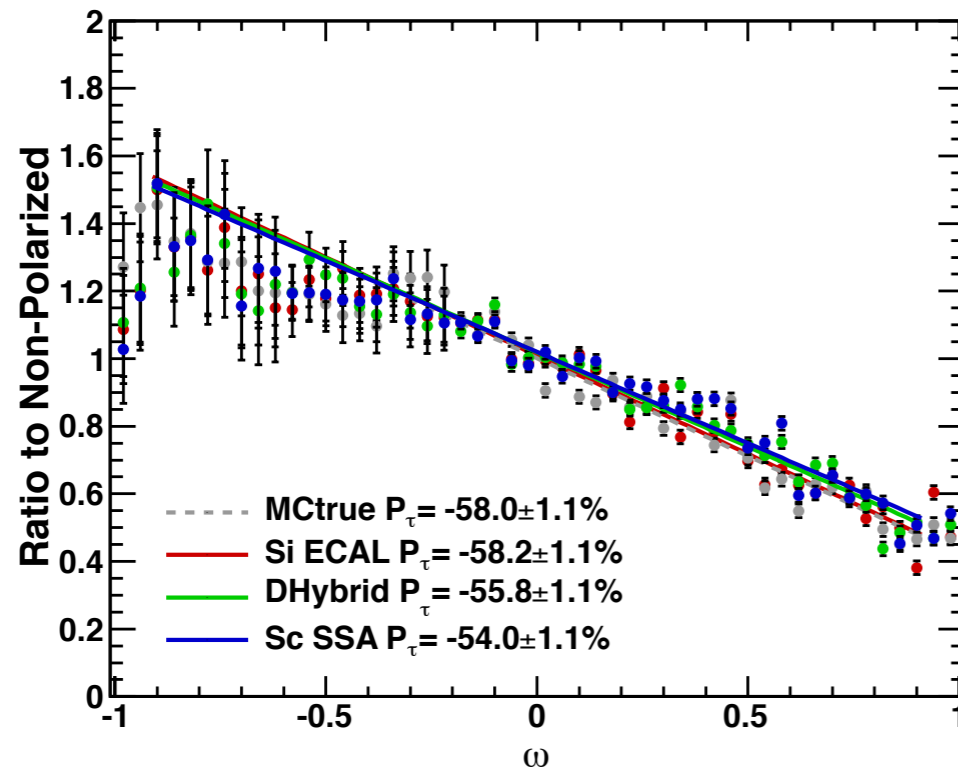
# Polarization combined $\omega$ with 3 Detectors

- Formula of  $\omega$  differs by decay modes, but  $\omega$  can be summed up through all decay modes.

※ Include error forcibly

e-L e+R

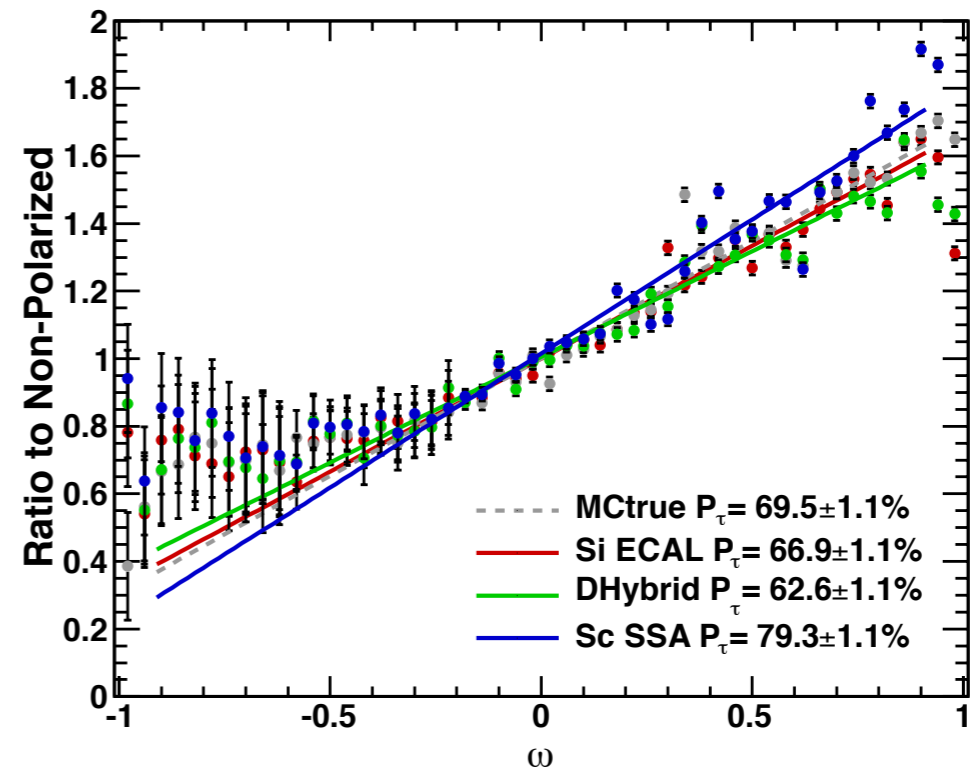
e  $\mu$   $\pi$   $\rho$  combined  $\omega$  (  $e_L^-, e_R^+ = 80\%, 30\%$  )



- MC true : 58.0%
- Si ECAL : 58.2%
- DHybrid : 55.8%
- Sc w/SSA : 54.0%

e-R e+L

e  $\mu$   $\pi$   $\rho$  combined  $\omega$  (  $e_R^-, e_L^+ = 80\%, 30\%$  )



- MC true : 69.5%
- Si ECAL : 66.9%
- DHybrid : 62.6%
- Sc w/SSA : 79.3%