

# UV complete theory of SUSY radiative seesaw scenarios

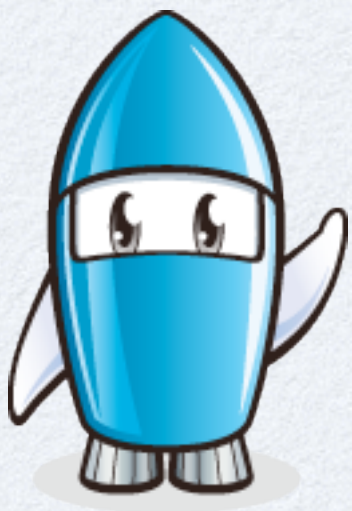
Tetsuo Shindou (Kogakuin University)

S. Kanemura, T.S, and T. Yamada, PRD86,055023

S. Kanemura, E. Senaha, T.S, T. Yamada, JHEP1305,066

S. Kanemura, N. Machida, T.S, T. Yamada, arXiv:1309.3207

14/11/2013 LCWS2013 @ Univ. of Tokyo Japan





# Physics beyond the SM

Discovery of a Higgs boson & measurements of properties



Essence of the electroweak symmetry breaking



New Physics at TeV scale

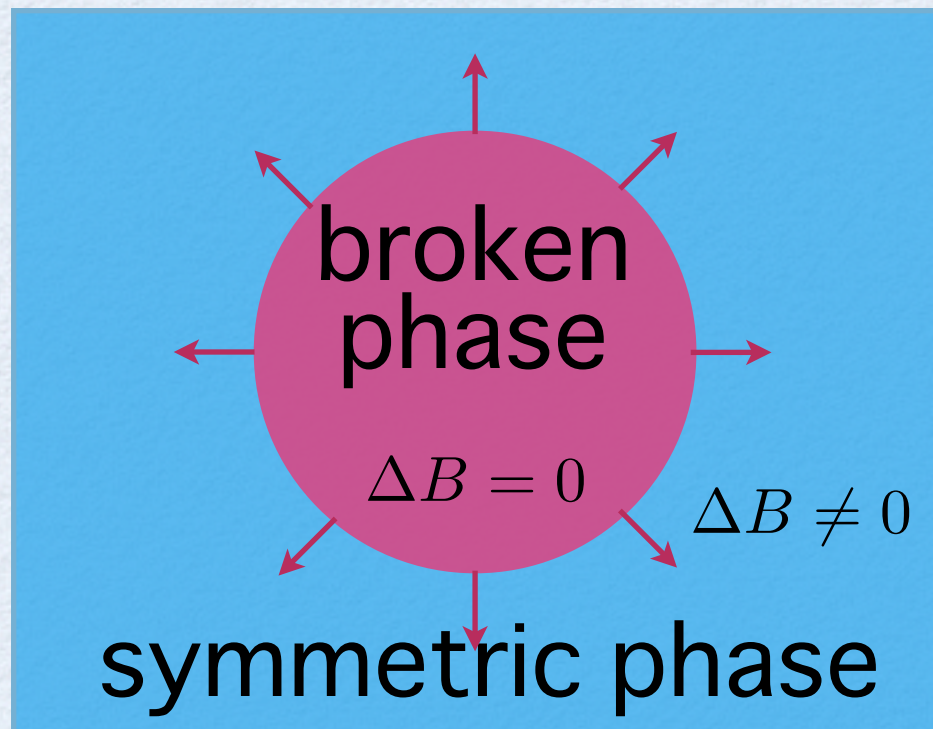
It's quite interesting,  
if **the NP** provides solutions on  
the problems in the SM:

- Baryon asymmetry of the Universe
- Origin of the neutrino mass
- DM candidate



# Electroweak Baryogenesis

Electroweak Baryogenesis  $\longleftrightarrow$  essence of EWSB



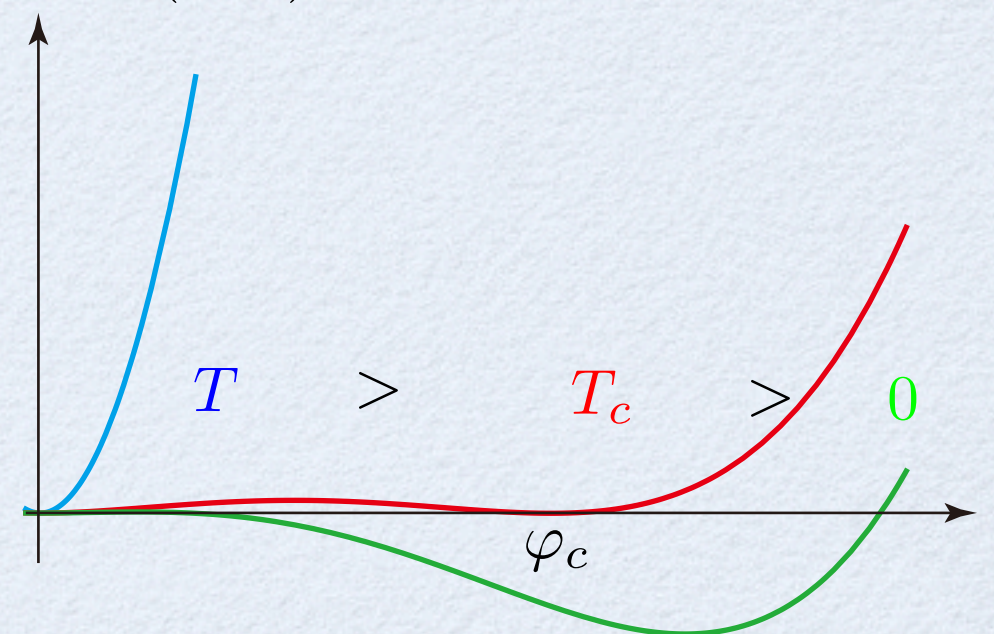
1st order electroweak transition  
+  
Sphaleron

To avoid too strong washout

The strong enough first order electroweak phase transition is necessary

$$\underline{\varphi_c/T_c > 1}$$

$$V_{\text{eff}}(v; T) - V_{\text{eff}}(0, T)$$



Higgs potential@EW scale



# To get strong 1st order EWT

Strong 1st order EWPT requires extension of the SM

In the SM, the condition is satisfied only when  $m_h < 50\text{GeV}$

( $\varphi_c/T_c$  is suppressed by  $m_h$ )

↑  
conflict with LHC data

Extra boson loop can enhance  $\varphi_c/T_c$

Extended Higgs sector!

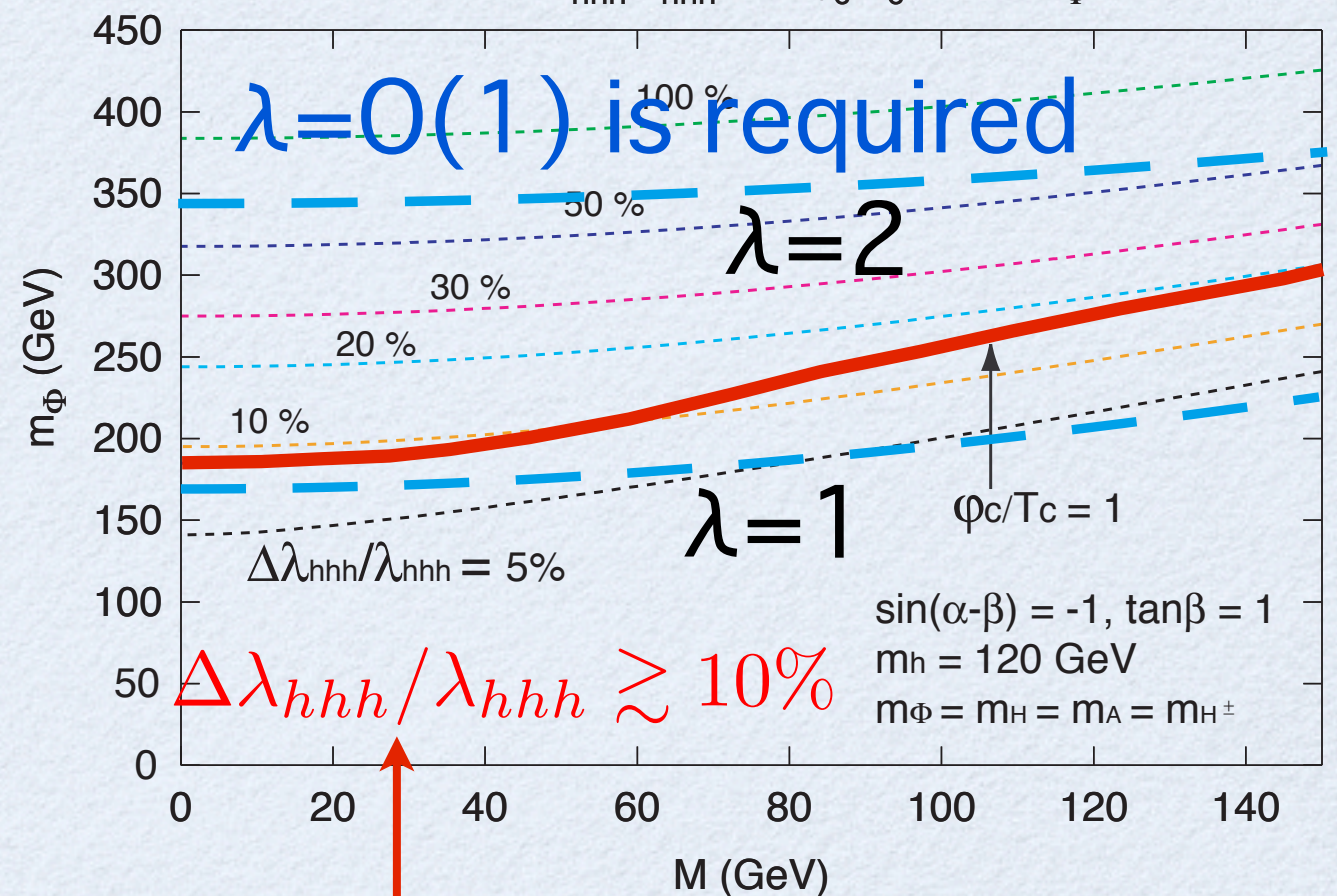
e.g. 2HDM

$$\mathcal{L} = \frac{\lambda_i}{2} h^2 |\Phi_i|^2$$

$$m_{\Phi}^2(\varphi) = M^2 + \lambda_i \varphi^2$$

Extra Higgs bosons as H, A, H $^{\pm}$

Contour plot of  $\Delta\lambda_{hhh}/\lambda_{hhh}$  and  $\varphi_c/T_c$  in the  $m_{\Phi}$ -M plane



Kanemura, Okada, Senaha, PLB606,361

Testable@Collider exp.



# In SUSY case

In the MSSM, there is no such a large coupling with SM-like Higgs

(The light stop scenario is the only possibility but it's almost dead)

The simplest example of **strong but light Higgs** scenario is **SUSY 4HD+charged singlets**

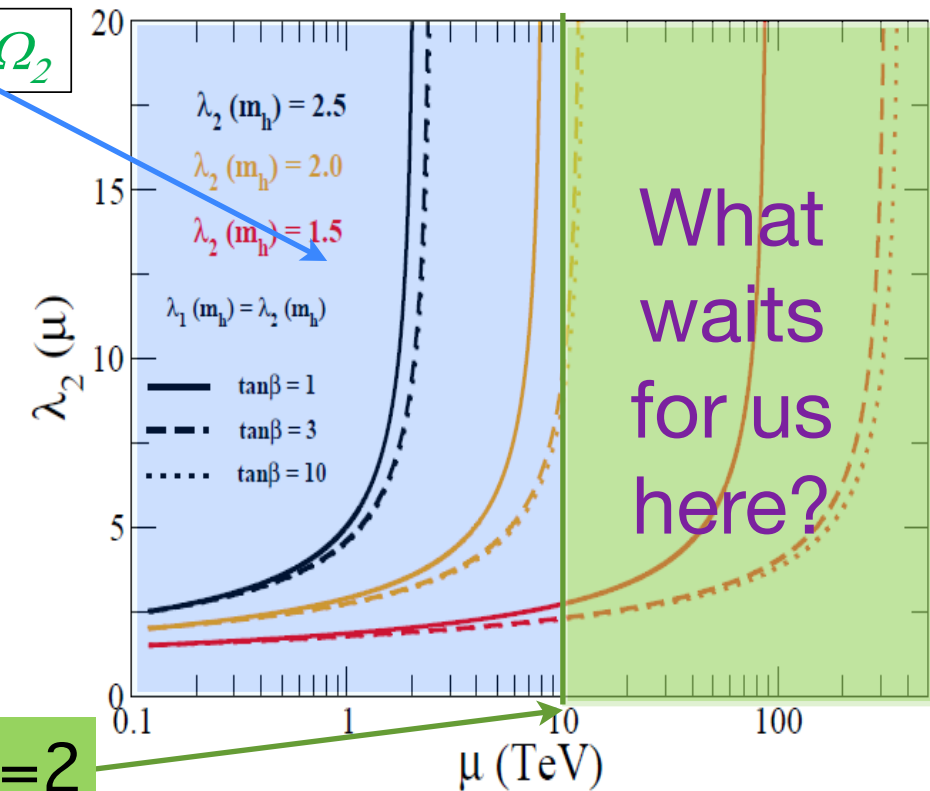
S.Kanemura, E. Senaha, T.S, PLB706,40

$\phi_c/T_c > 1$  with  $m_h=126\text{GeV}$

$\lambda > 1.6$

$$W = \lambda_1 H_u H_u' \Omega_1 + \lambda_2 H_d H_d' \Omega_2$$

$\lambda_2$	$\Lambda_{\text{cutoff}}$
2.5	2 TeV
2.0	10 TeV
1.5	100 TeV



cutoff for  $\lambda=2$

Kanemura, T.S, Yagyu, 2010

EW baryogenesis can be realized in a SUSY model @TeV



# Fundamental theory?

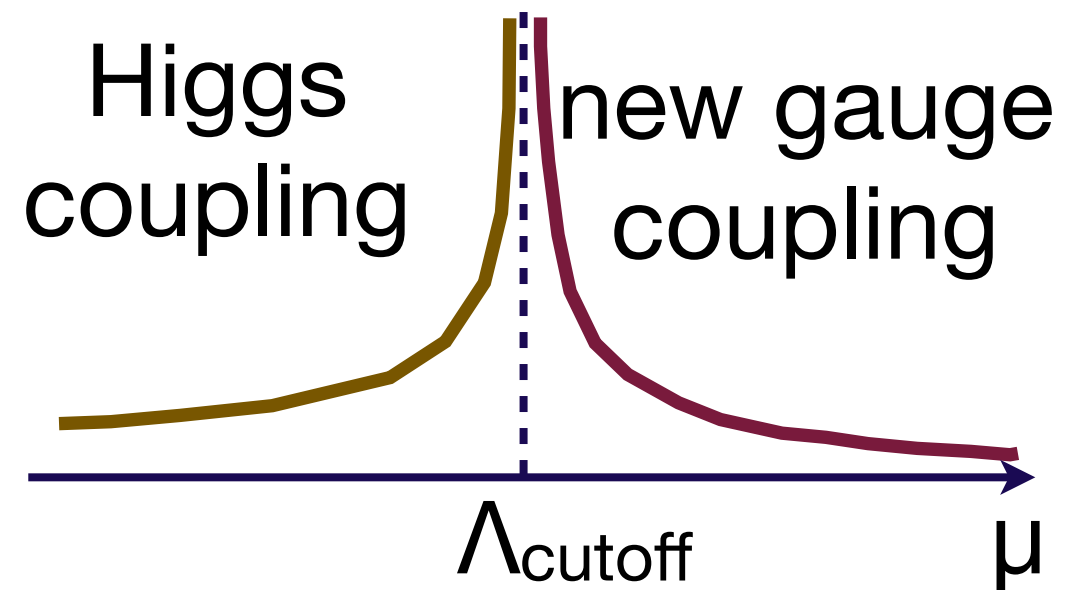
- Electroweak baryogenesis
  - Enhancement of EWPT by bosonic loop requires **strong** Higgs coupling ( $> 1$ ) **but light** (125 GeV) Higgs
- What is the fundamental theory of such models?
  - Large coupling constant  $\rightarrow$  Landau pole (cutoff)
  - What is the origin of Higgs force?



# Fundamental theory?

- Electroweak baryogenesis
  - Enhancement of EWPT by bosonic loop requires **strong** Higgs coupling ( $> 1$ ) **but light** (125 GeV) Higgs
- What is the fundamental theory of such models?
- Large coupling constant
- What is the origin of Higgs

Our expectation:





# SUSY SU(2)<sub>H</sub> model

In SUSY QCD:  $N_f = N_c + 1 \Rightarrow$  confinement

See e.g. Intriligator, Seiberg, hep-th/9509006

Let us consider the simplest case ( $N_c = 2 \& N_f = 3$ )

**SUSY SU(2)<sub>H</sub> × SU(2)<sub>L</sub> × U(1)<sub>Y</sub>** S.Kanemura, T.S, and T. Yamada, PRD86,055023

It's asymptotic free!

It's the same setup as **the minimal SUSY fat Higgs**  
R Harnik, et al., PRD70, 015002

Fields	SU(2) <sub>L</sub>	U(1) <sub>Y</sub>
$\begin{pmatrix} T_1 \\ T_2 \end{pmatrix}$	2	0
$T_3$	1	+1/2
$T_4$	1	-1/2
$T_5$	1	+1/2
$T_6$	1	-1/2



Field	SU(2) <sub>L</sub>	U(1) <sub>Y</sub>
$H_u = \begin{pmatrix} H_{13} \\ H_{23} \end{pmatrix}$	2	+1/2
$H_d = \begin{pmatrix} H_{14} \\ H_{24} \end{pmatrix}$	2	-1/2
$N = H_{56}, N_\Phi = H_{34}, N_\Omega = H_{12}$	1	0
$\Phi_u = \begin{pmatrix} H_{15} \\ H_{25} \end{pmatrix}$	2	+1/2
$\Phi_d = \begin{pmatrix} H_{16} \\ H_{26} \end{pmatrix}$	2	-1/2
$\Omega_+ = H_{35}$	1	+1
$\Omega_- = H_{46}$	1	-1
$\zeta = H_{36}, \xi = H_{45}$	1	0

Below the confinement scale  $\Lambda_H$ ,  
the effective theory is described  
by  $H_{ij} \sim T_i T_j$

cf. In the minimal SUSY fat Higgs, only  $H_u, H_d$ , and  $N$  are made light  
(The effective theory is “minimal”)



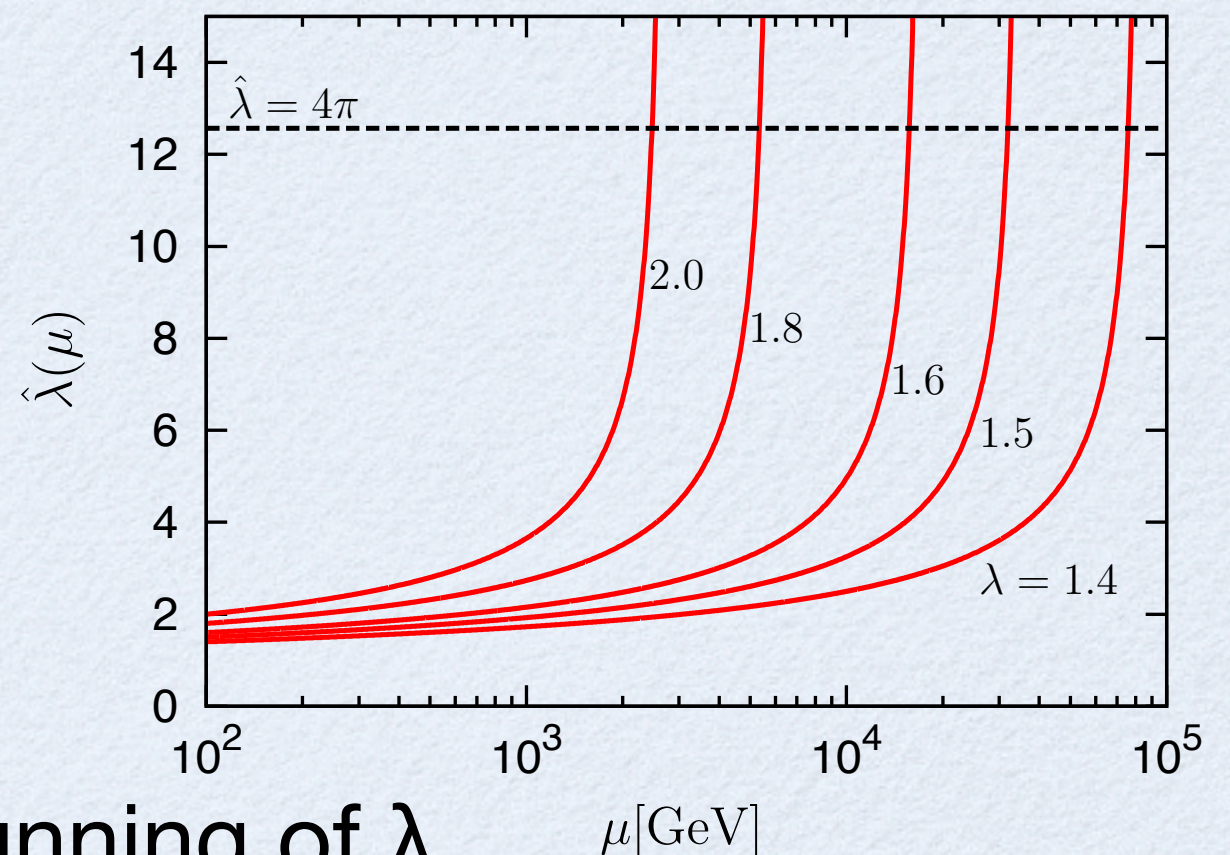
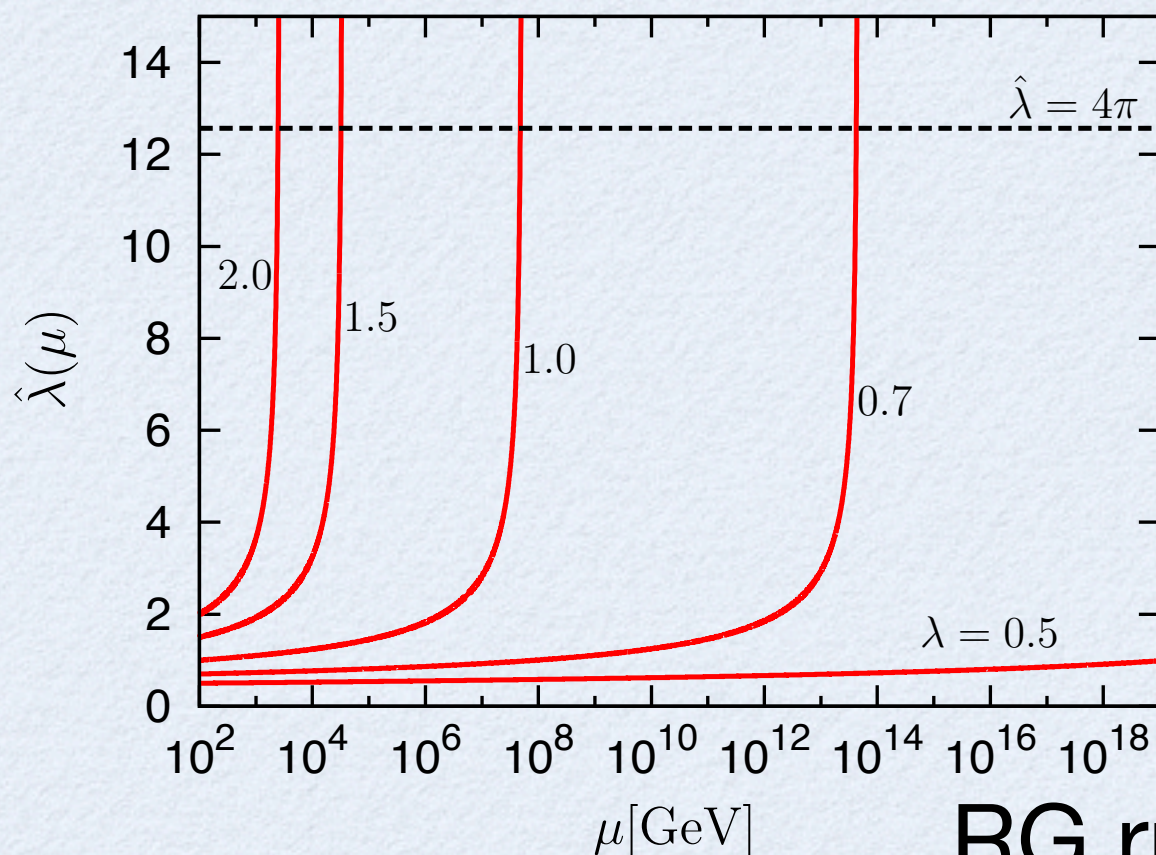
# Effective theory of $SU(2)_H$ model

S.Kanemura, E. Senaha, T.S, T.Yamada, JHEP1305,066

MSSM-like Higgs doublets

$$W = -\mu H_u H_d - \mu_\Phi \Phi_u \Phi_d - \mu_\Omega (\Omega_+ \Omega_- - \zeta \eta) \\ + \hat{\lambda} \{ H_d \Phi_u \zeta + H_u \Phi_d \eta - H_u \Phi_u \Omega_- - H_d \Phi_d \Omega_+ \}$$

$$\hat{\lambda}(\Lambda_H) \simeq 4\pi \text{ (Naive dimensional analysis)}$$



RG running of  $\lambda$

$\lambda = \lambda(\mu_{EW})$  determines the cutoff scale



# 1st order EWPT

S.Kanemura, E. Senaha, T.S, T.Yamada, JHEP1305,066

$m_h = 126 \text{ GeV}$

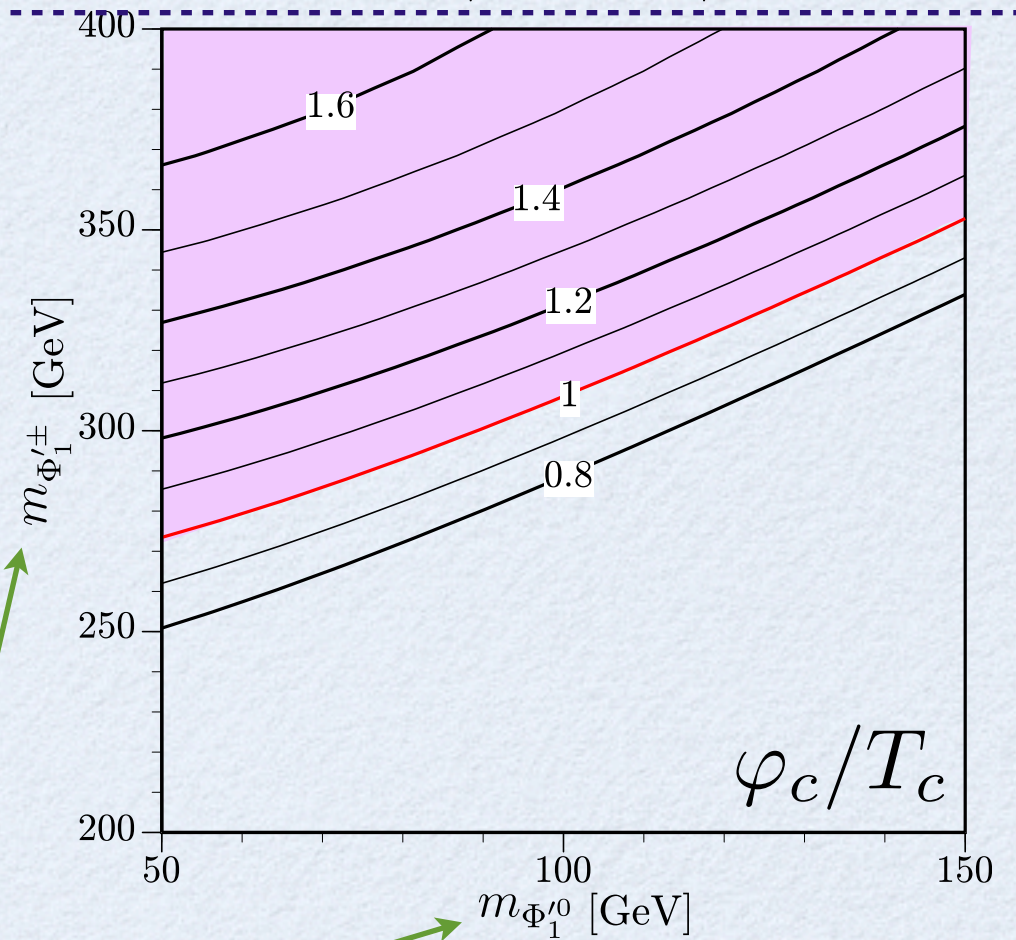
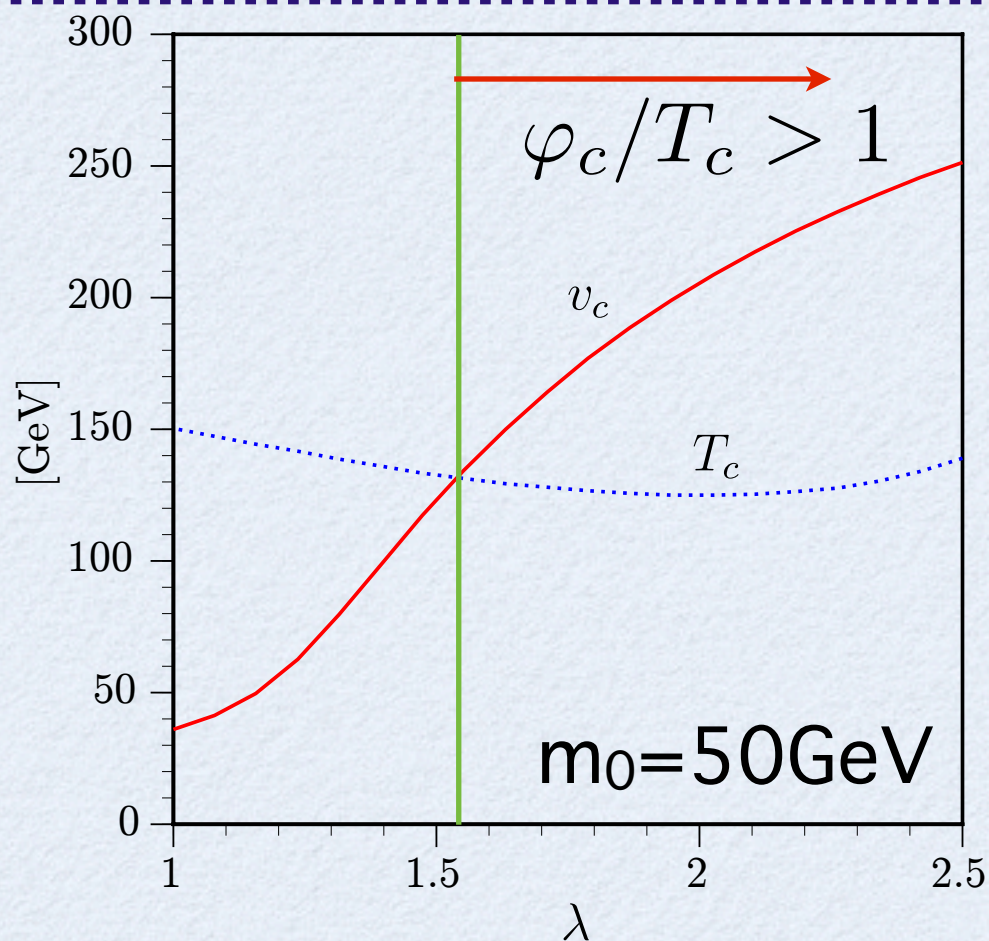
Benchmark:

$$\tan \beta = 15, m_{H^+} = 350 \text{ GeV}, \mu = 200 \text{ GeV}, M_{\tilde{t}} = M_{\tilde{q}} = 2000 \text{ GeV}$$

$$\bar{m}_{\Omega^+}^2 = \bar{m}_{\Phi_d}^2 = \bar{m}_{\zeta}^2 = (1500 \text{ GeV})^2, \bar{m}_{\eta}^2 = (2000 \text{ GeV})^2, \mu_{\Phi} = \mu_{\Omega} = 550 \text{ GeV}$$

$$m_0^2 \equiv \bar{m}_{\Phi_u}^2 = \bar{m}_{\Omega^-}^2 \quad (\text{Scanned})$$

$$(m_{\phi}^2 = \bar{m}_{\phi}^2 + c_{\phi} \lambda^2 v^2)$$



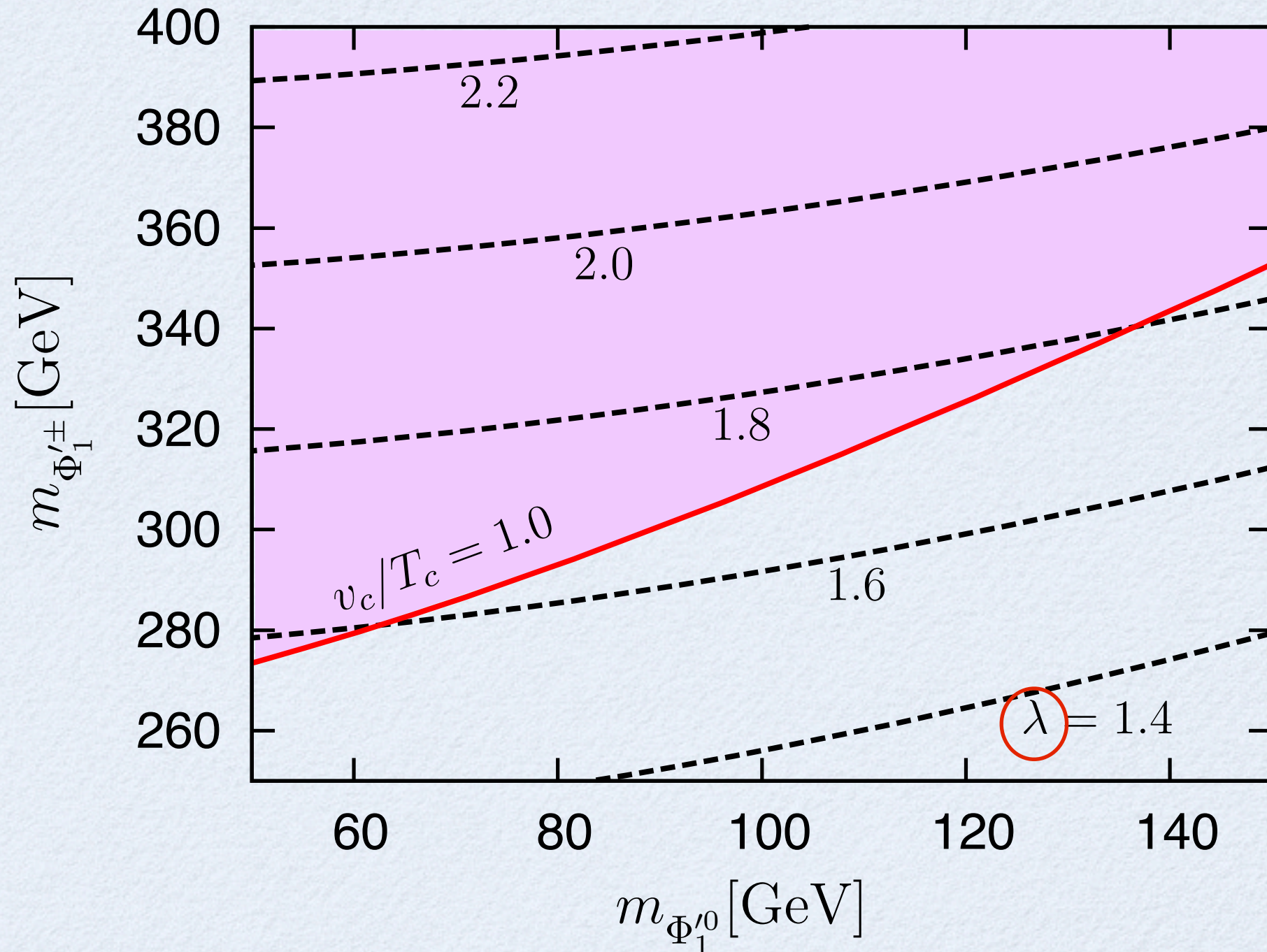
$\varphi_c/T_c > 1$  can be satisfied!!

Lightest  $Z_2$  odd masses



# 1st order EWPT

S.Kanemura, E. Senaha, T.S, T.Yamada, JHEP1305,066

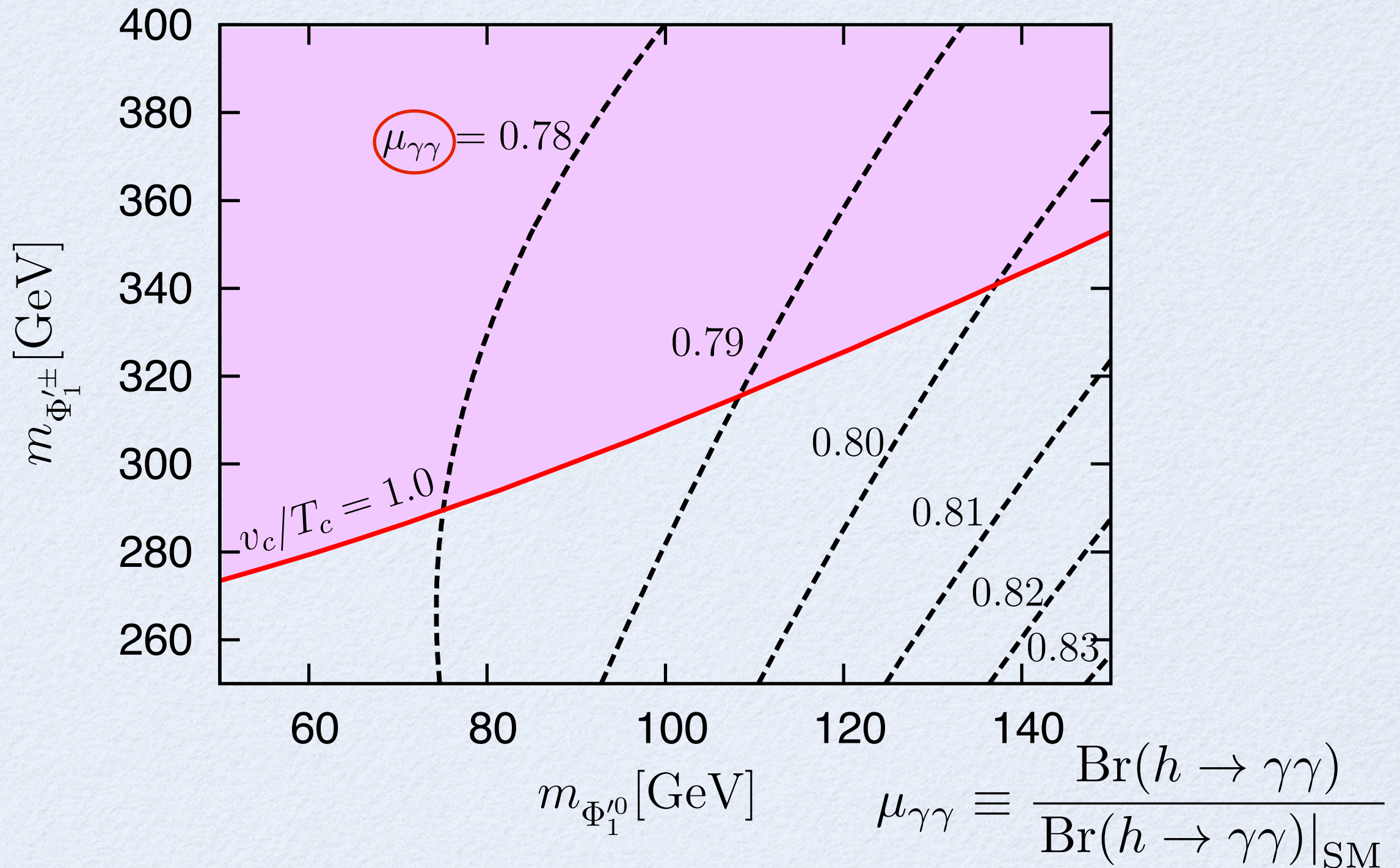


$$\varphi_c/T_c > 1 \implies \lambda \gtrsim 1.5 \quad (\Lambda_H \lesssim 20\text{TeV})$$



# Contribution to $h\gamma\gamma$

S.Kanemura, E. Senaha, T.S. T. Yamada, JHEP1305,066

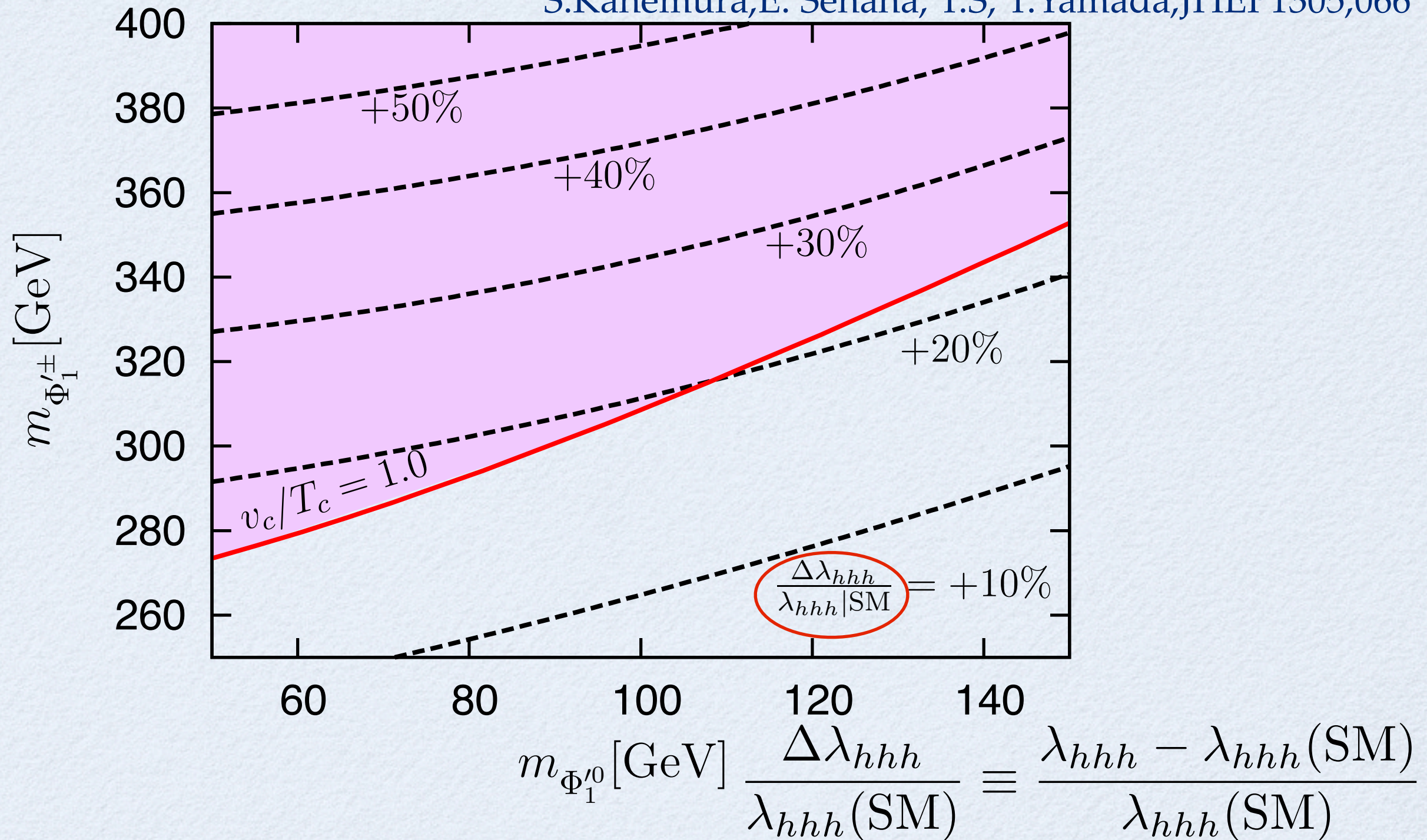


**~20% deviation is possible in the region of  $v_c/T_c > 1$**



# hhh coupling

S.Kanemura, E. Senaha, T.S. T. Yamada, JHEP1305,066



~20% deviation is possible in the region of  $v_c/T_c > 1$



# How about neutrino mass?

Origin of the neutrino mass at TeV scale

Alternative to the well-known seesaw model:

Idea of loop induced neutrino mass

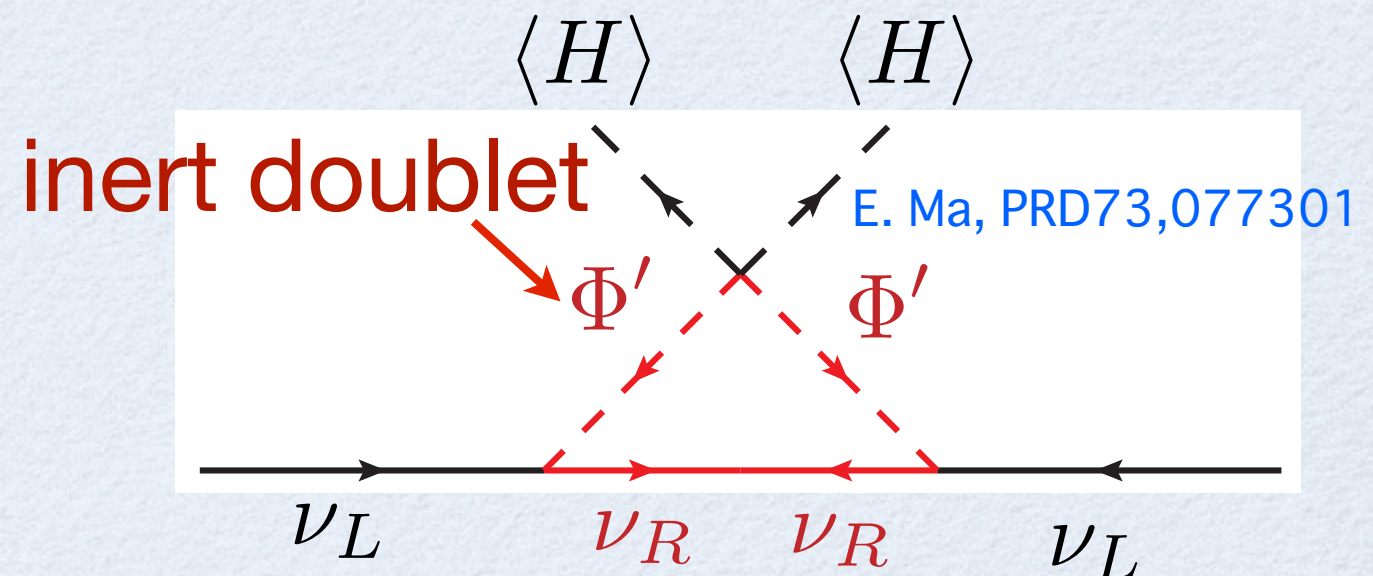
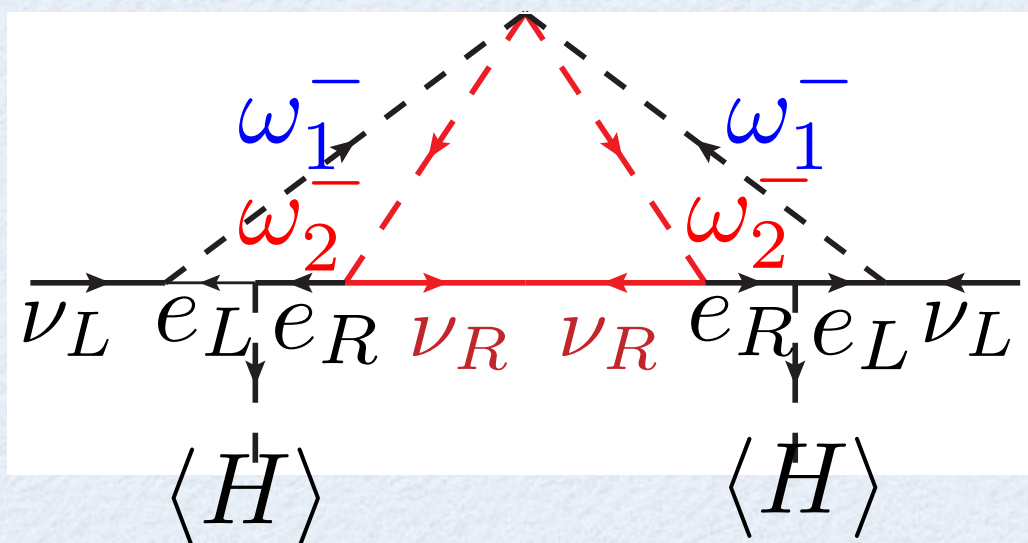
Especially, radiative seesaw scenarios are interesting

Loop diagram with RH neutrinos give tiny neutrino mass

( $Z_2$ -odd) ← To avoid tree level contribution

Some new scalars are introduced!

L.M.Krauss, S.Nasri, M.Trodden, PRD67,085002



Lightest  $Z_2$ -odd neutral particle can be a DM

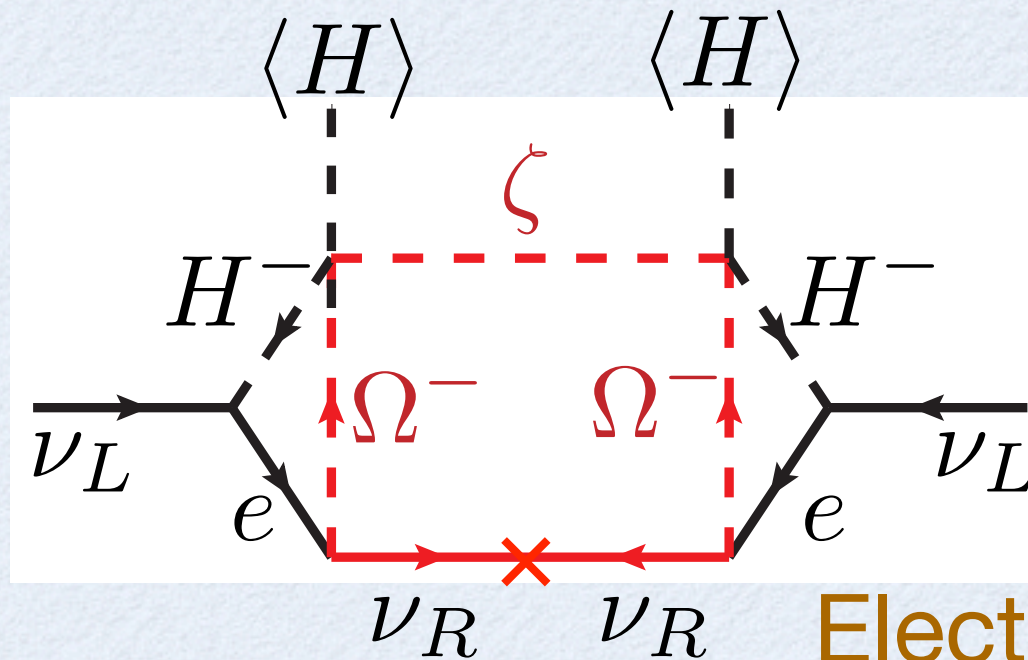


# AKS model

Aoki-Kanemura-Seto model

Aoki, Kanemura, Seto, PRL102, 051805

(2HD+ $Z_2$ -odd charged and neutral singlet+ $Z_2$ -odd RHN)



Lighter one can be a DM

neutrino mass

Electroweak baryogenesis also can work

As a phenomenological model, this is quite interesting

But ...

Large couplings  $\longrightarrow$  Landau pole at low energy scale

Many extra scalars  $\longrightarrow$  It seems artificial

What is the fundamental theory of this model?



# For radiative seesaw

S.Kanemura, N. Machida, T.S, T.Yamada, arXiv:1309.3207

We can use the  $SU(2)_H$  model

Fields	$SU(2)_L$	$U(1)_Y$	$Z_2$
$\begin{pmatrix} T_1 \\ T_2 \end{pmatrix}$	2	0	+
$T_3$	1	+1/2	+
$T_4$	1	-1/2	+
$T_5$	1	+1/2	-
$T_6$	1	-1/2	-



Field	$SU(2)_L$	$U(1)_Y$	$Z_2$
$H_u = \begin{pmatrix} H_{13} \\ H_{23} \end{pmatrix}$	2	+1/2	+
$H_d = \begin{pmatrix} H_{14} \\ H_{24} \end{pmatrix}$	2	-1/2	+
$N = H_{56}, N_\Phi = H_{34}, N_\Omega = H_{12}$	1	0	+
$\Phi_u = \begin{pmatrix} H_{15} \\ H_{25} \end{pmatrix}$	2	+1/2	-
$\Phi_d = \begin{pmatrix} H_{16} \\ H_{26} \end{pmatrix}$	2	-1/2	-
$\Omega_+ = H_{35}$	1	+1	-
$\Omega_- = H_{46}$	1	-1	-
$\zeta = H_{36}, \xi = H_{45}$	1	0	-

Then,  $Z_2$ -odd RH neutrinos are introduced as  $SU(2)_H$  singlet fields

In the low energy effective theory,

$$W_N = (y_N)_i N_i^c L_j \Phi_u + (h_N)_{ij} N_i^c E_j^c \Omega^- + \frac{M_i}{2} N_i^c N_i^c$$

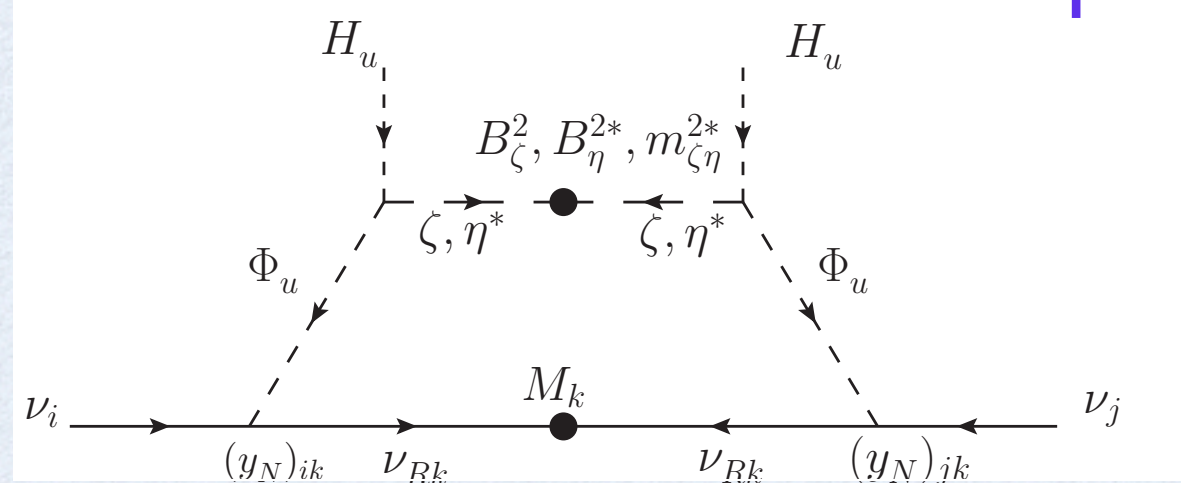


# Neutrino mass generation

S.Kanemura, N. Machida, T.S, T.Yamada, arXiv:1309.3207

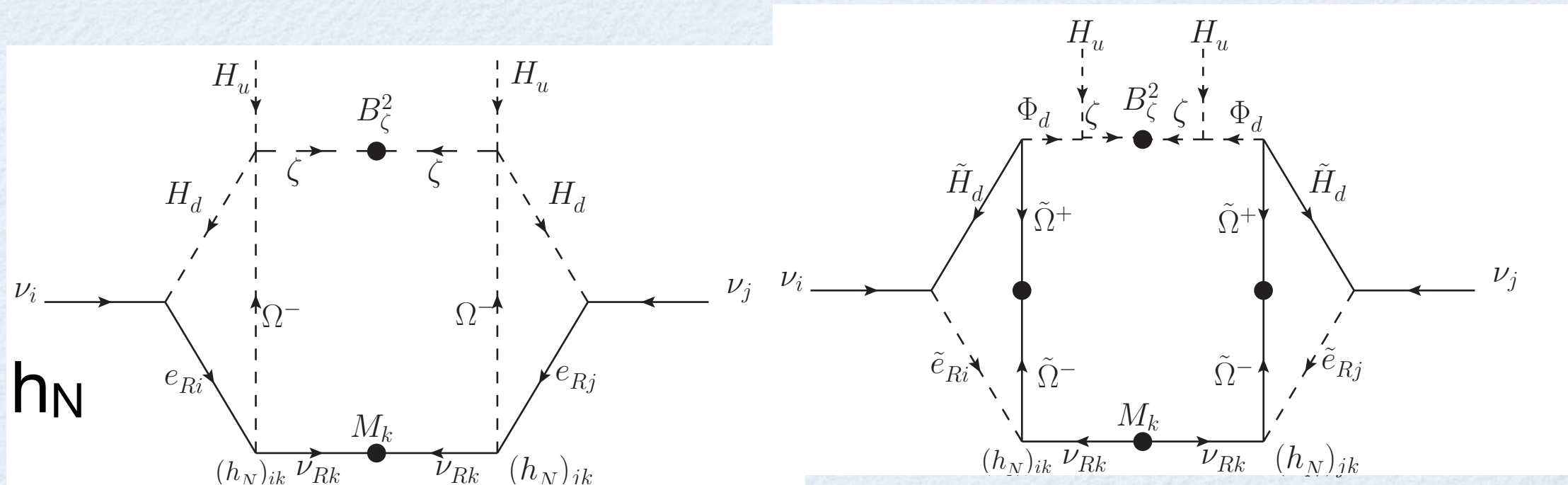
Two different types of contributions are possible

1-loop  
driven by  $y_N$



It corresponds to SUSY Ma model

3-loop  
driven by  $h_N$



They correspond to SUSY AKS model



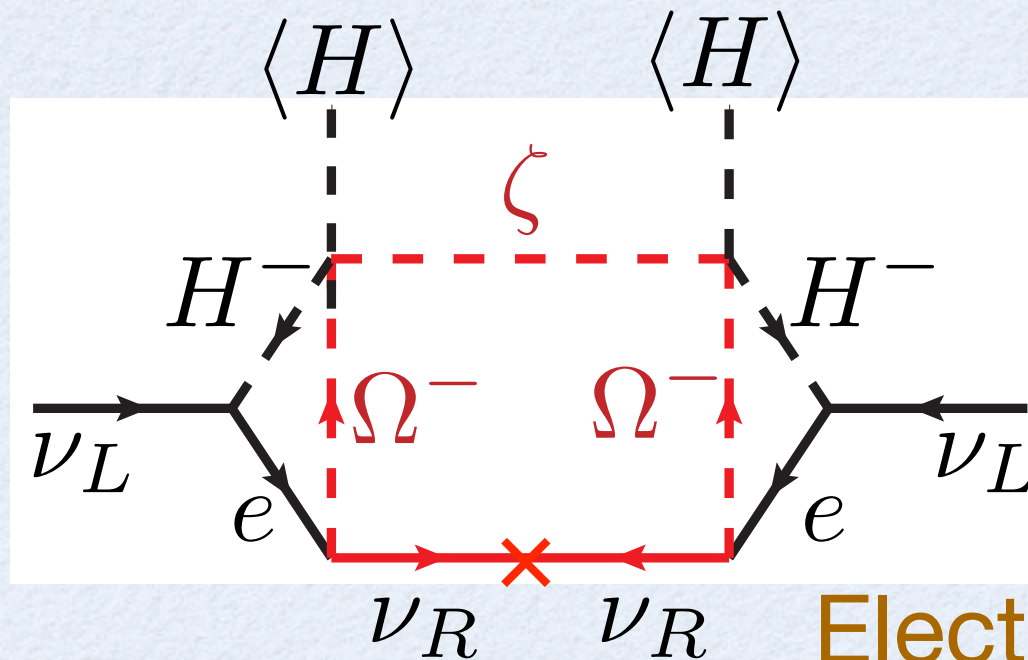
# Comment on SUSY AKS

S.Kanemura, N. Machida, T.S, T.Yamada, arXiv:1309.3207

e.g. Aoki-Kanemura-Seto model

Aoki, Kanemura, Seto, PRL102, 051805

(2HD+ $Z_2$ -odd charged and neutral singlet+ $Z_2$ -odd RHN)



→ neutrino mass

Lighter one can be a DM

Electroweak baryogenesis also can work

In SUSY version,

$H_u, H_d$  (MSSM-like Higgs)

$\Omega^+, \Omega^-$

$\phi_u, \phi_d$

$\zeta$

$N^c$  (RHN)

Many new fields are required

$SU(2)_H$  model automatically provides all the fields in the Higgs sector!!



# Benchmark points

(A): 1-loop dominant point  
(B): 3-loop dominant point

Case	$\lambda$	$\tan\beta$	$m_{H^\pm}$	$m_{\tilde{W}}$	$\mu$	$\mu_\Phi$	$\mu_\Omega$
(A)	1.8	15	350GeV	500GeV	100GeV	550GeV	-550GeV
(B)	1.8	30	350GeV	500GeV	100GeV	550GeV	-550GeV

Case	$\bar{m}_{\Phi_u}^2$	$\bar{m}_{\Phi_d}^2$	$\bar{m}_{\Omega^+}^2$	$\bar{m}_{\Omega^-}^2$	$\bar{m}_\zeta^2$	$\bar{m}_\eta^2$
(A)	$(100\text{GeV})^2$	$(1500\text{GeV})^2$	$(1500\text{GeV})^2$	$(100\text{GeV})^2$	$(1500\text{GeV})^2$	$(2000\text{GeV})^2$
(B)	$(1500\text{GeV})^2$	$(1500\text{GeV})^2$	$(1500\text{GeV})^2$	$(30\text{GeV})^2$	$(1410\text{GeV})^2$	$(30\text{GeV})^2$

Case	$B_\zeta^2$	$B_\eta^2$	$m_{\zeta\eta}^2$
(A)	$(100\text{GeV})^2$	$(100\text{GeV})^2$	$(100\text{GeV})^2$
(B)	$(1400\text{GeV})^2$	0	0

Case	$M_1$	$M_2$	$M_3$	$m_{\tilde{\nu}_{R1}}$	$m_{\tilde{\nu}_{R2}}$	$m_{\tilde{\nu}_{R3}}$	$m_{\tilde{e}_{Ri}} (i=1,2,3)$
(A)	60GeV	120GeV	180GeV	60GeV	120GeV	180GeV	6000GeV
(B)	100GeV	2000GeV	4000GeV	100GeV	4000GeV	8000GeV	6000GeV

Case	$(y_N)_{ij}$	$(h_N)_{ij}$
(A)	$\begin{pmatrix} -0.45 & -0.44 & 0.51 \\ 0.23 & 0.23 & -0.26 \\ 0.19 & 1.37 & 1.37 \end{pmatrix} \times 10^{-4}$	$\sim \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix}$
(B)	$\sim \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix}$	$\begin{pmatrix} 0.001 & 0 & 0 \\ -0.0624 + 0.16i & -0.0314 - 0.0016i & -0.0022 + 0.000297i \\ 0.902 + 2.46i & 0.000681 - 0.00126i & -0.000755 - 0.00161i \end{pmatrix}$

Case	$m_1$	$m_2$	$m_3$	$\sin^2 \theta_{12}$	$\sin^2 2\theta_{23}$	$ \sin \theta_{13} $
(A)	0.0eV	0.0090eV	0.050eV	0.31	1.0	0.1
(B)	0.0eV	0.0089eV	0.050eV	0.31	1.0	0.1

The neutrino mass and angles are reproduced

Case	$B(\mu \rightarrow e\gamma)$	$B(\mu \rightarrow eee)$
(A)	$4.6 \times 10^{-19}$	$7.2 \times 10^{-21}$
(B)	$5.2 \times 10^{-14}$	$4.7 \times 10^{-13}$

$\phi_c/T_c > 1$  is realized!

Serious LFV constraints are also satisfied



# Comments on direct detection

Our model is characterized by the  $Z_2$  odd sector

$Z_2$ -odd particle search is important  
colorless  $\rightarrow$  ILC

Case (A): light inert doublet

$$\begin{aligned} e^+ e^- &\rightarrow H' A' \rightarrow Z H' H' \\ e^+ e^- &\rightarrow H^{+'} H^{-'} \rightarrow W^+ W^- H' H' \end{aligned} \quad @ILC$$

Mass determination can be done with a few GeV accuracy

M. Aoki, S. Kanemura and H. Yokoya, PLB725,302.

Case (B): Singlet-like charged particle  $\Omega^+$

$$e^+ e^- \rightarrow \Omega_1^+ \Omega_1^-$$

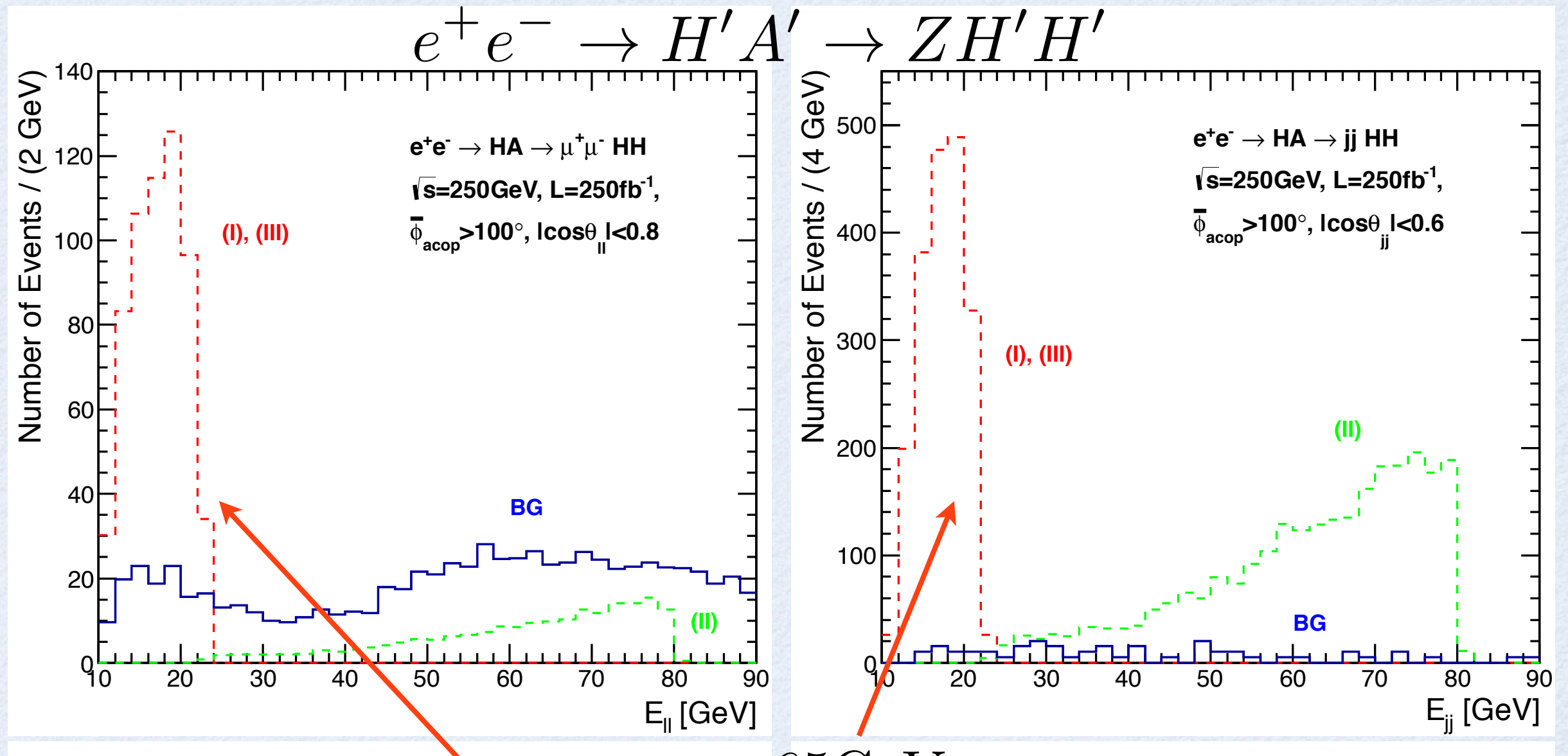
$$e^- e^- \rightarrow \Omega_1^- \Omega_1^- \leftarrow \text{Strong evidence of the model}$$

Aoki&Kanemura&Seto, PRD80,033007; Aoki&Kanemura, PLB689,28.



# Light inert doublet @ ILC

M. Aoki, S. Kanemura and H. Yokoya, PLB725,302.



$$m_{H'} = 65\text{GeV}$$

$$m_{A'} = 73\text{GeV}$$

$$m_{H^{\pm'}} = 120\text{GeV}$$

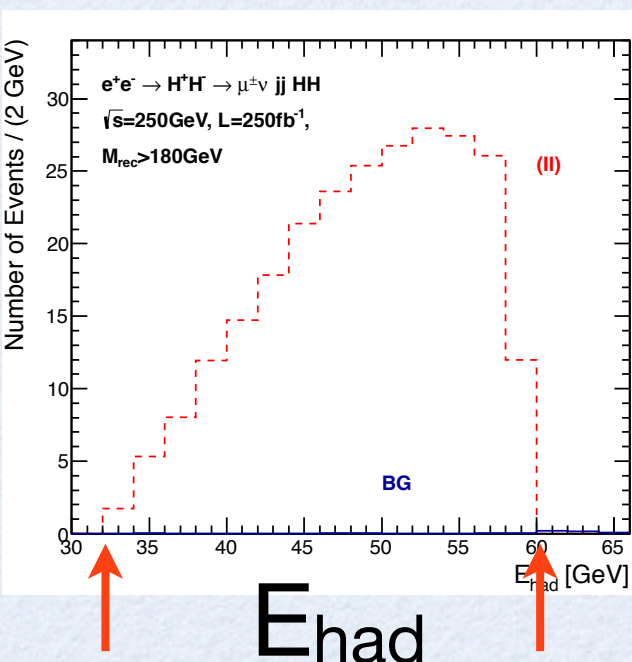
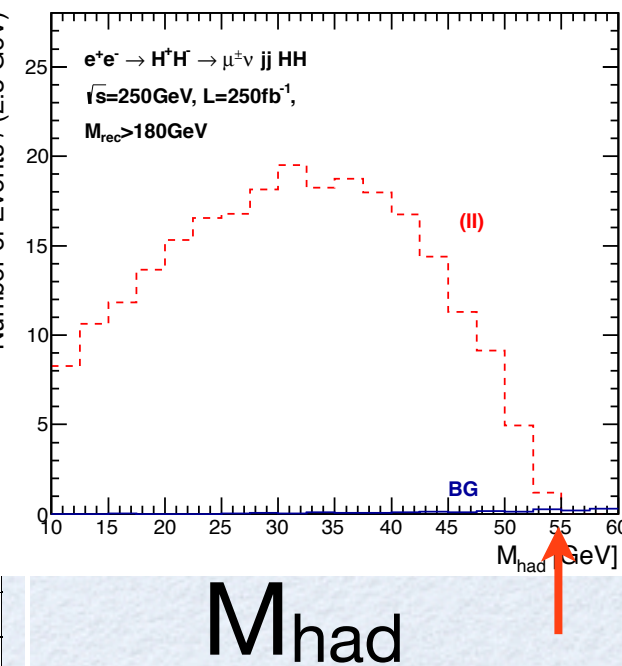
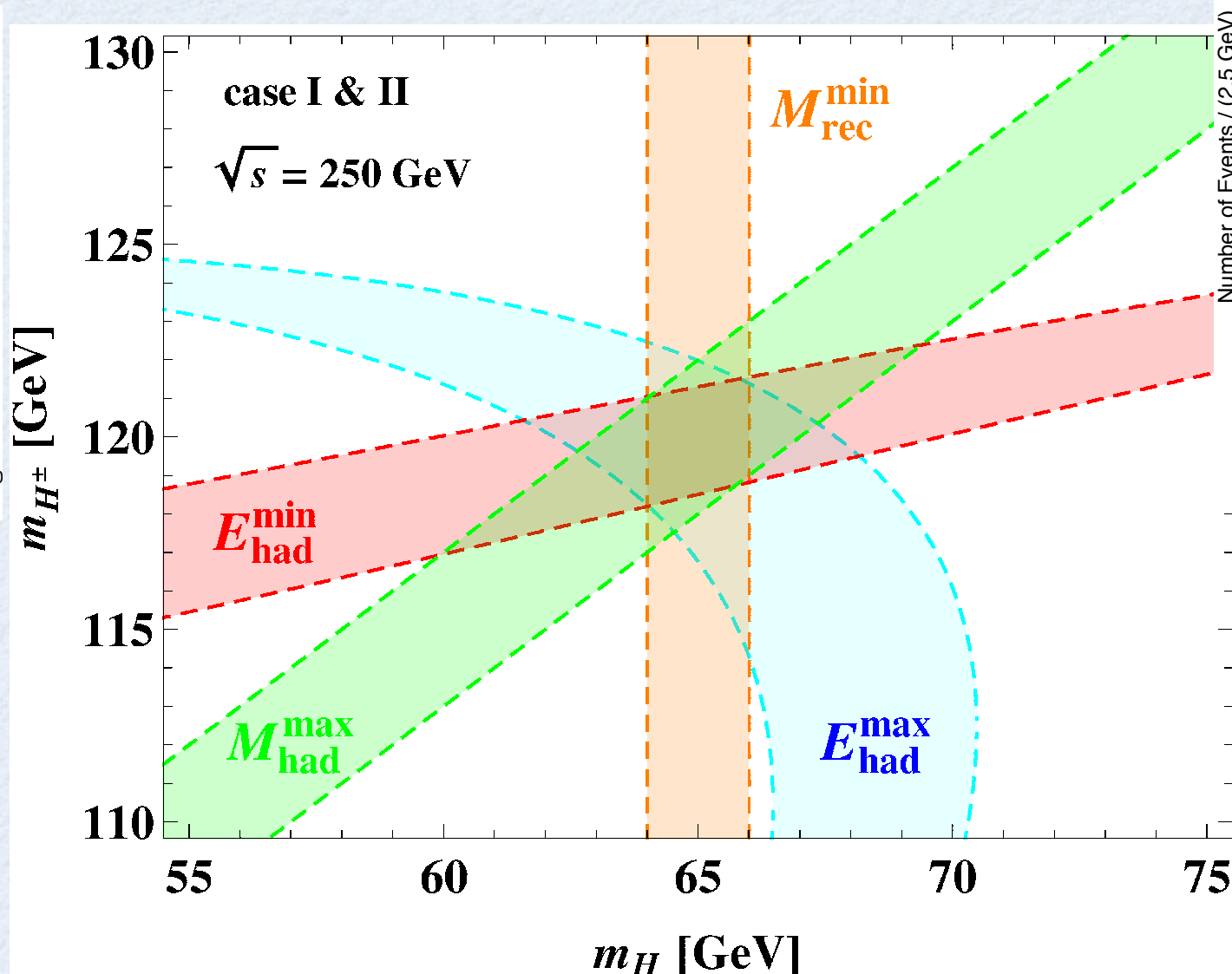
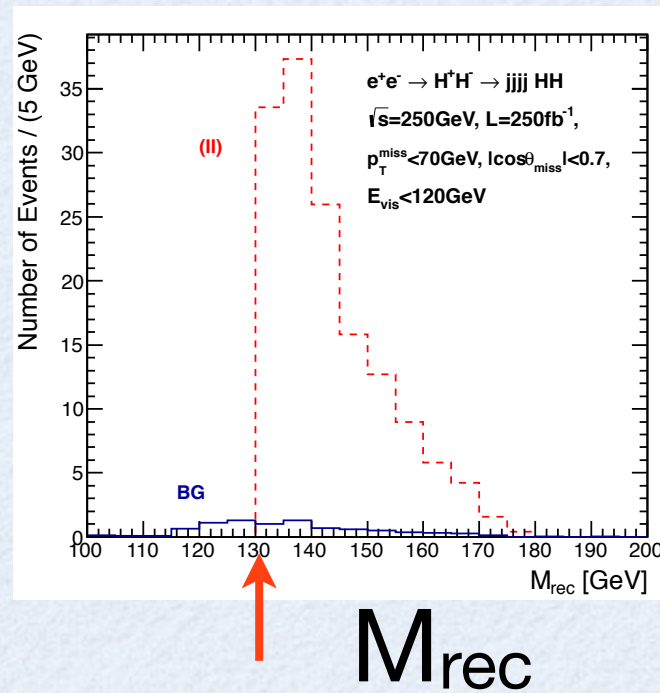
(Similar to Case (A))



# Light inert doublet @ ILC

M. Aoki, S. Kanemura and H. Yokoya, PLB725,302.

$$e^+e^- \rightarrow H^{+'}H^{-'} \rightarrow W^+W^-H'H'$$



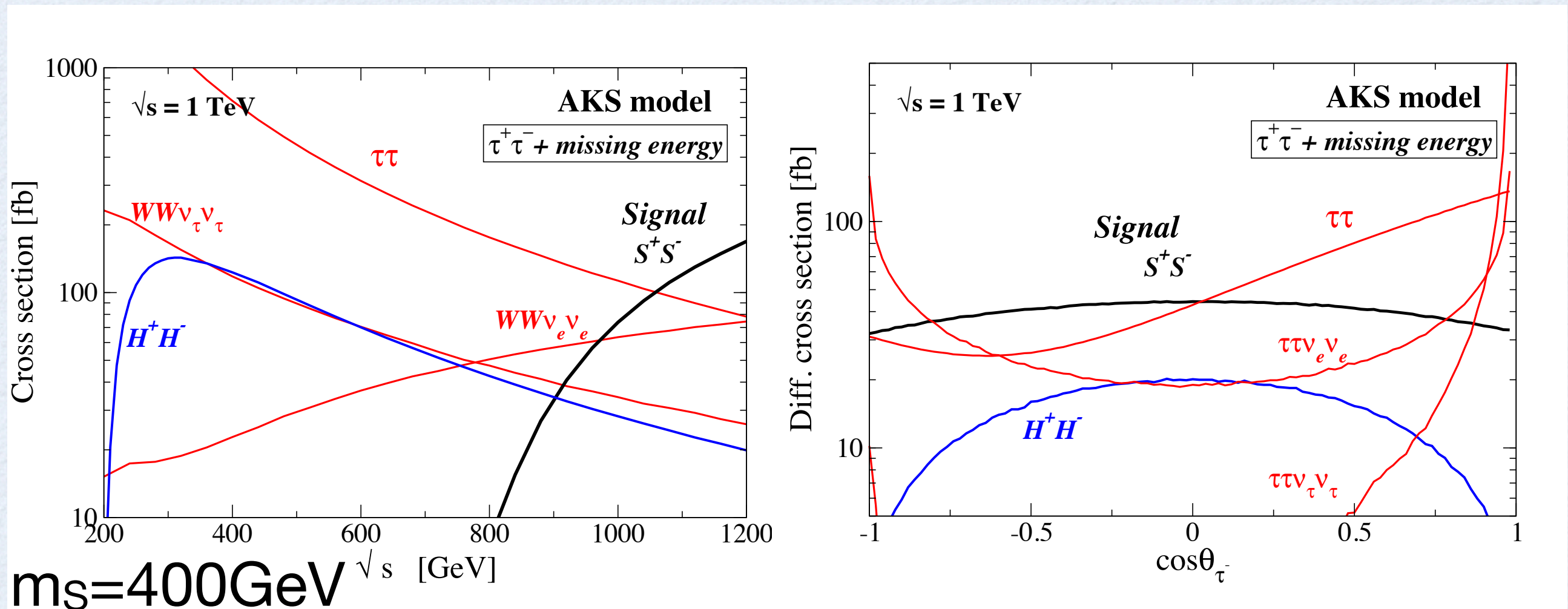
The masses can be precisely determined



# Singlet-like scalar @ ILC

Aoki&Kanemura, PLB689,28.

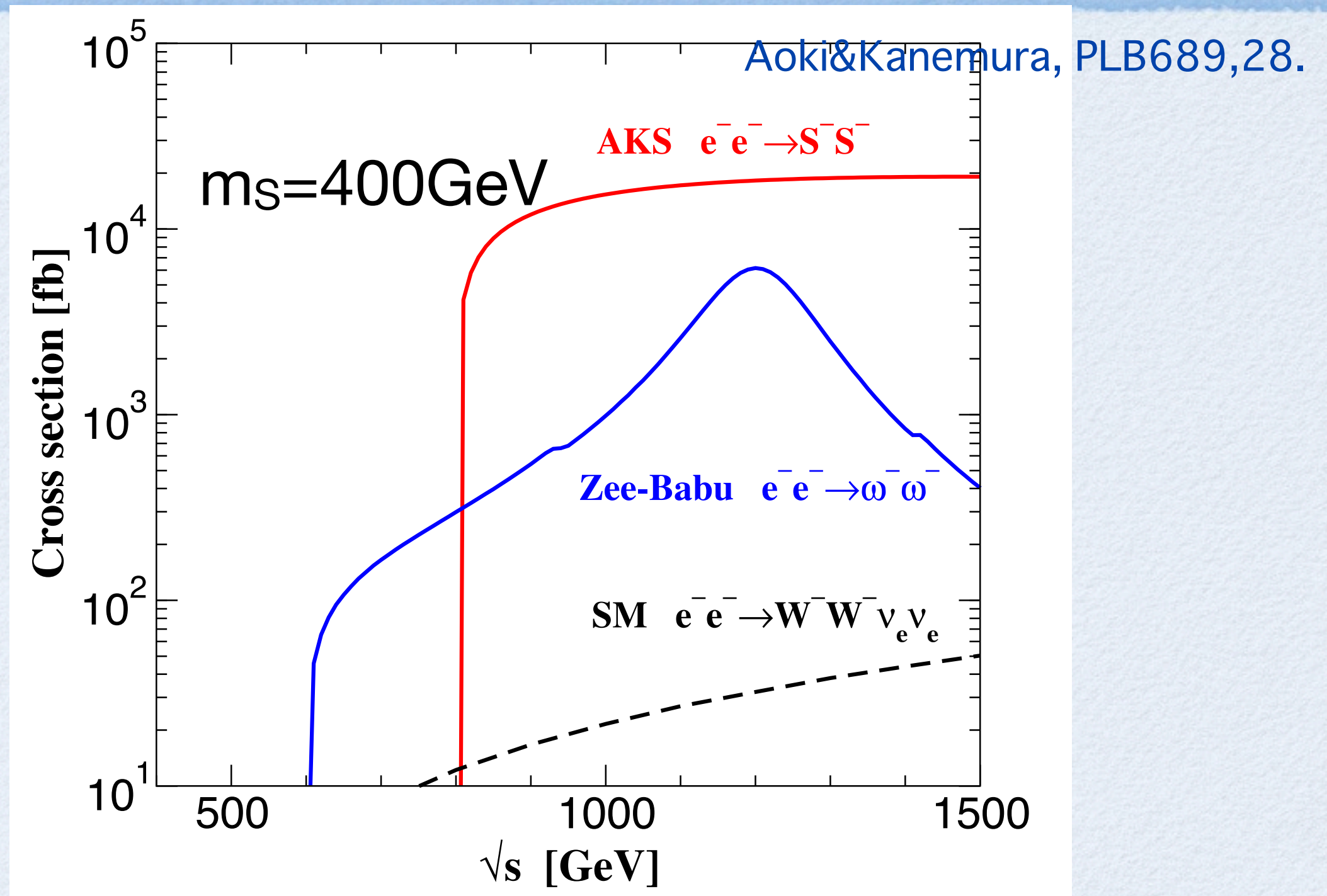
$$e^+e^- \rightarrow S^+S^- \rightarrow \tau^+\tau^- + \text{missing}$$



A signal can be seen at the ILC@1TeV



# Singlet-like scalar @ILC- $e^-e^-$



The signal is quite clear evidence of the Majorana nature and the scenario



# Summary

- It is quite interesting, NP in the Higgs sector provides solutions for baryogenesis, neutrino mass, DM.
  - Electroweak baryogenesis, radiative generation of neutrino mass,...
  - It can be tested at collider experiments
  - Many models have been considered but they have been developed purely phenomenologically
- We have succeeded to provide a candidate of fundamental theory of such models
- SUSY  $SU(2)_H$  with  $N_f=3 + Z_2$ -odd RHN is attractive simple candidate  
It provides new DM candidate
- It's very different from GUT beyond the grand desert  
Rich field will be there!



Back up



# Top Yukawa coupling

Introducing several new fields ( $SU(2)_H$  singlets) as

$$W_f = M_f(\varphi_u \bar{\varphi}_u + \bar{\varphi}_d \varphi_d) + \bar{\varphi}_d T T_4 + \bar{\varphi}_u T T_3$$

$$+ h_u^{ij} Q_i u_j \varphi_u + h_d^{ij} Q_i d_j \varphi_d + h_e^{ij} L_i e_j \varphi_d$$

$$T = \begin{pmatrix} T_1 \\ T_2 \end{pmatrix}$$

conformal enhancement

$Q, L, u, d, e$ : Matter fields in the SM

$\varphi_{u,d}$  and  $\bar{\varphi}_{u,d}$  are integrated out

$$W = \frac{4\pi}{M_f} \{ h_u^{ij} Q_i u_j (T T_3) + h_d Q_i d_j (T T_4) + h_e L_i e_j (T T_4) \}$$

Below  $\Lambda_H$

$$(T T_3) \rightarrow \frac{\Lambda_H}{4\pi} H_u \quad (T T_4) \rightarrow \frac{\Lambda_H}{4\pi} H_d$$

$$W = h_u^{ij} Q_i u_j H_u + h_d^{ij} Q_i d_j H_d + h_e^{ij} L_i e_j H_d$$

for  $M_f \sim \Lambda_H$



# EWBG in the SM

In the high temperature approximation,

$$V(\varphi, T) \simeq D(T^2 - T_0^2)\varphi^2 - ET\varphi^3 + \frac{\lambda_T}{4}\varphi^4 + \dots$$

$$\varphi_c/T_c = 2E/\lambda_{T_c}$$

1st order PT is possible due to the cubic term

$$E = \frac{1}{12\pi v^3}(6m_W^3 + 3m_Z^3)$$

$$\lambda_T = \frac{m_h^2}{2v^2} + \log \text{ corrections}$$

$$\varphi_c/T_c \propto 1/m_h^2$$

Light Higgs is required !!

In SM, Higgs should be lighter than 50GeV

excluded by

NEW CP phases are also necessary for successful baryogenesis

LEP data

Extension of the SM at TeV scale is necessary

It can be tested by experiments

- New bosonic loop contribution
- Higher dim. term in the potential
- ...



# EWBG in the MSSM

Carena et al., PLB380,81;...

Lighter **stop** loop can contribute

enhance

large top Yukawa coupling

$$E \simeq \frac{1}{12\pi v^3} (6m_W^3 + 3m_Z^3) + \frac{m_t^3}{2\pi v^3} \left( 1 - \frac{|A_t + \mu \cot \beta|^2}{M_{\tilde{q}}^2} \right)^{3/2}$$

$$\varphi_c/T_c = 2E/\lambda_{T_c} > 1$$

where the maximal contribution case is considered;

$$m_{\tilde{t}_1}^2(\varphi, \beta) = M_{TR}^2 + \frac{y_t^2 s_\beta^2}{2} \left( 1 - \frac{|A_t + \mu \cot \beta|^2}{M_{\tilde{q}}^2} \right) \varphi^2$$

For larger  $M_{TR}$ , the effect is smaller

Light stop is necessary

↔ No new coloured particles at LHC...

Even with such a maximal case, it's not easy to get  $\varphi_c/T_c > 1$

Carena et al., NPB812,243; Funakubo, Senaha, PRD79,115024

MSSM should be also modified at TeV scale for EWBG



# What kind of modification?

$$\varphi_c/T_c \propto 1/m_h^2$$

Small  $m_h$  is preferable

$m_h = 126 \text{ GeV @ LHC}$   
support

We want to keep it!

A Good point of MSSM :  $h^4$  coupling is from gauge coupling  $\rightarrow$  Light Higgs

strong but light!

Large bosonic loop contribution

- A strong Higgs coupling with additional bosons ( $h-\Phi'-\Phi'$ )
- Mass of  $\phi'$  is dominated by vev  $m_{\Phi'}^2 = M^2 + \lambda^2 v^2$

A natural realization of “strong but light” in SUSY model:

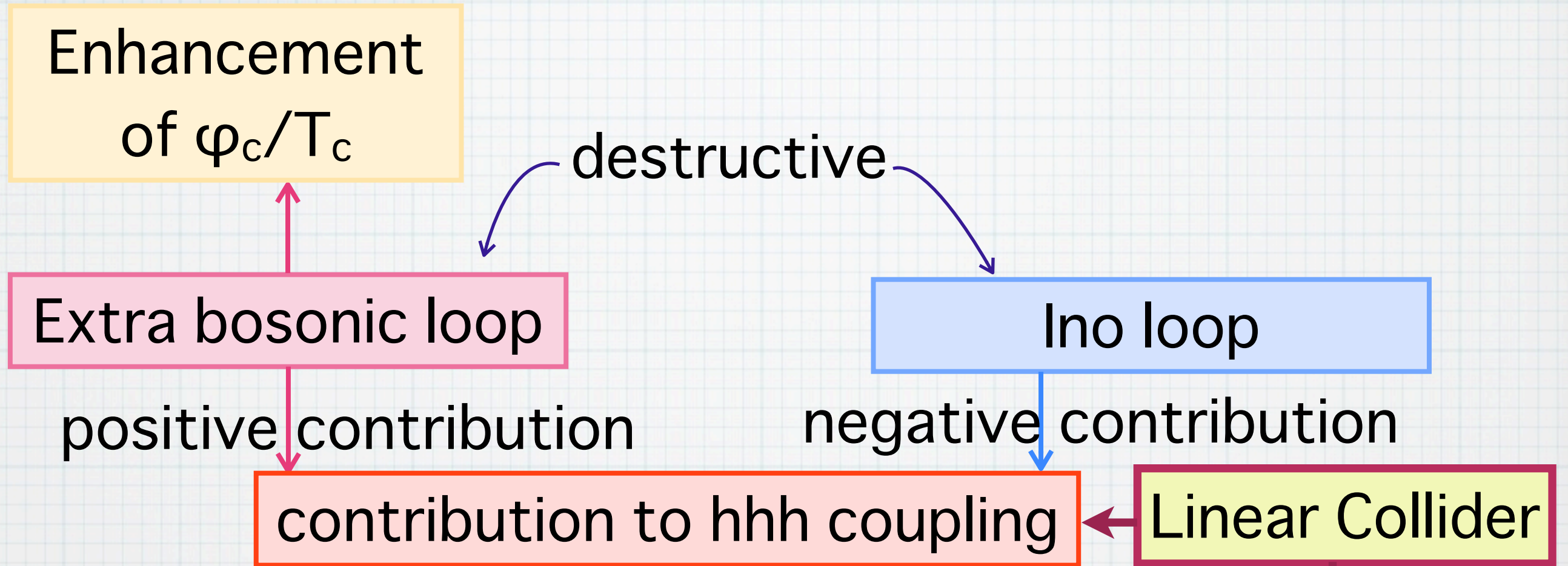
MSSM Higgs       $Z_2$  odd new fields

$$W = \lambda \Phi_{u,d} \Phi'_1 \Phi'_2 \rightarrow \Delta V = |\lambda|^2 h^2 \varphi'_{1,2} \varphi'_{1,2}$$

It provides strong coupling but  $m_h$  is kept small!



# Tests of the scenario



Inert scalar mass:  $m_{\Phi'}^2 = M'^2 + \lambda^2 v^2$

Inert ino mass:  $m_{\tilde{\Phi}'} = \mu' + \lambda v$

The loop contributions are significant when  $\lambda v$  dominates the masses.

$Z_2$  odd scalars as light as  $\sim \lambda v$

Large  $\mu'$  and small  $M'^2$  provides large deviation in hhh and large  $\varphi_c/T_c$