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Review of α_s determinations from e+e- annihilation

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••• Outline

- Introduction: event shapes in e⁺e⁻ collisions
- α_s from event shapes
- Electroweak corrections and radiative return
- Prospects for the ILC
- Further strong coupling determinations
- Conclusions & Outlook



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• Consider a tipical jet event at LEP:





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Is it possible to extract usefull information from the shape of an event?





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• Various proposals to measure shape of events finding ways to parametrize the geometry of hadronic final states:

• Thrust:
$$T = \max_{\vec{n}} \left(\frac{\sum_i |\vec{p_i} \cdot \vec{n}|}{\sum_i |\vec{p_i}|} \right)$$



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• Various proposals to measure shape of events finding ways to parametrize the geometry of hadronic final states:



- From theoretical point of view:
 - Many are Infra-Red and collinear safe (-> suitable for computations)
 - Perturbative picture:

 γ/Z^{o}

Deviation from 2-jet configuration proportional to α_s

von Humbold

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e⁺

e

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3 jets NLO EW

[Denner, Dittmaier, Gehrmann, Kurz; Carloni-Calame; Moretti, Piccinini, Ross]



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- From theoretical point of view:
 - Many are Infra-Red and collinear safe (-> suitable for computations)
 - Perturbative picture:



• Precise extraction of α_s requires precise description of each "step"



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- Further event shapes usually used:
 - Heavy jet mass: $\rho = \frac{1}{E_{\text{tot-vis.}}^2} \max\left(M_L^2, M_R^2\right); \qquad M_{L/R}^2 = \left(\sum_{n \in H_{L/R}} |\vec{p_n}|\right)$
 - Total/Wide Broadenings: $B_i = \frac{\sum_{k \in H_i} |\vec{p}_k \times \vec{n}_T|}{2\sum_j |\vec{p}_j|}$;

• Total:
$$B_T = B_1 + B_2$$

• Wide:
$$B_W = \max(B_1, B_2)$$

• C-parameter:
$$\Theta^{\alpha\beta} = \frac{1}{\sum_{i} |\vec{p_i}|} \sum_{i} \frac{p_i^{\alpha} p_i^{\beta}}{|\vec{p_i}|}$$

tensor with EV
$$\lambda_1, \lambda_2, \lambda_3$$

$$C = 3(\lambda_1\lambda_2 + \lambda_2\lambda_3 + \lambda_3\lambda_1)$$

 $y_{ij} = \frac{2\min(E_i^2, E_j^2)(1 - \cos\theta_{ij})}{E_{\text{vis}}^2}$

• 2 \rightarrow 3 jet resolution parameter (Durham alg.): Y_3

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•• Data sources

- Data on event shapes available at several CM energies and from several experiments:
 - PETRA:
 - TASSO data from 14 to 44 GeV
 - JADE data for 35 and 44 GeV: still maintained and analyzed [Bethke, Kluth, Pahl]
 - TRISTAN:
 - AMY data at 55 GeV
 - SLAC:
 - SLC data at 91.2 GeV
 - LEP:
 - ALEPH / OPAL / DELPHI / L3 data from 91.2 to 207 GeV
 - DELPHI / L₃ data with radiated photon and Q < M_Z



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Impact of QED effects in these sets?



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••• Event shapes: theory vs data

• How well are data described by theory predictions?



[Gehrmann, GL, Monni]





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[Gehrmann, GL, Monni]





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••• Extracting α_s from data



- Main open issues
 - NNLL+NNLO is becoming state-of-the-art for (almost) all observables
 - Analytical vs. Monte Carlo hadronization corrections?
 - Which observables and which data sets?



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•• NNLO(+NLL) fits to 6 event-shapes



- From NLO to NNLO: decrease in uncertainties and central value
- From NNLO to NLLA+NNLO: increase in uncertainty
 - → NLLA resummation does not cancel NNLO running of coupling in the matching



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MC hadronization This approach is problematic if parton level predictions in MC and pQCD are very different **Detector** level Hadron level parameters Hadronization corr. Parton level Leeeeeeeee Resummation **ME** level (NLL, NNLL,...) Fit Parton level MC (EVENT₂, EERAD₃,...) MC generator Fixed order calculation

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Stiftung/Found

•• MC hadronization



• Pythia parameters tuned such that missing higher order terms are overcompensated and hadronization corrections are effectively too small



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MC hadronization



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•• NNLO(+NLL) global fits



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Stiftung/Foun

• Analytical Hadronization Models

• Dispersive model

[Dokshitzer, Marchesini, Webber; Dokshitzer et al.]

• NP corrections by means of a physical coupling:

$$\tilde{\alpha}_s(k_{\perp}^2) = \alpha_s^{\rm PT}(k_{\perp}^2) + \alpha_s^{\rm NP}(k_{\perp}^2)$$

• Introduce matching scale μ_I and $\alpha_0(\mu_I) = \frac{1}{\mu_I} \int_0^{\mu_I} dk_\perp \tilde{\alpha}_s(k_\perp^2)$

• NP correction amounts to a shift:

$$\frac{\mathrm{d}\sigma}{\mathrm{d}y}(y) = \frac{\mathrm{d}\sigma_{\mathrm{pt}}}{\mathrm{d}y} \left(y - a_y P \right)$$

• Shape function

[Korchemsky, Sterman, Tafat; Abbate, Fickinger, Hoang, Mateu, Stewart]

• Split soft function into PT and NP contribution:

$$S(\nu, Q) = \int_0^1 \frac{\mathrm{d}\alpha}{\alpha} \left(1 - e^{-\nu\alpha}\right) \left[\int_{\alpha^2 Q^2}^{\alpha Q^2} \frac{\mathrm{d}k_{\perp}^2}{k_{\perp}^2} \Gamma\left(\alpha_s(k_{\perp}^2)\right) + B\left(\alpha_s(\alpha Q^2)\right)\right]$$
$$\equiv S_{PT}(\nu, Q, \mu) + S_{NP}(\nu, Q, \mu)$$

• Again NP corrections amount to a shift:

$$\frac{\mathrm{d}\sigma_{\mathrm{PT}}(\tau)}{\mathrm{d}\tau} \longrightarrow \frac{\mathrm{d}\sigma_{\mathrm{PT}}(\tau)}{\mathrm{d}\tau} + \mathcal{O}\left(1/(\tau Q)^2\right) \quad \text{where } \int \mathrm{d}\epsilon \,\epsilon \, f_T\left(\epsilon;\mu\right) = \lambda_1$$

2.8 von Humboldt Stiftung/Found



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$\mathbf{\alpha}_{s}$ from moments

Alternative to distributions: moments of event shapes

$$\langle y^n
angle = rac{1}{\sigma_{
m had}} \int_0^{y_{
m max}} y^n rac{{
m d}\sigma}{{
m d}y} {
m d}y$$



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- Higher moments more sensitive to multiparticle region
- Perturbative and non-perturbative contributions additive:

 $\langle y^n \rangle = \langle y^n \rangle_{\rm pt} + \langle y^n \rangle_{\rm np}$

• Can add NP corretions either form Monte Carlo or from analytical description



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α_{s} from moments

[Gehrmann, Jaquier, GL, 0911.2422]

- With JADE/OPAL data:
 - Fit to first 5 moments of τ , ρ , C, Y₃
 - Broadenings not included in final average since analytical power correction was not fully extended at NNLO
 - No hadron mass corrections

 $\alpha_s(M_Z) = 0.1153 \pm 0.0017 \pm 0.0023$ $\alpha_0(2 \text{GeV}) = 0.5132 \pm 0.0115 \pm 0.0381$



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$\mathbf{\alpha}_{s}$ from moments

• Global fit for 1st moment of thrust



••• NLL+NNLO+PC with thrust

[Davison, Webber., 0809.3326]

- A first analysis with NNLO thrust distributions:
 - global fit for thrust distributions for energies between 14 GeV and 207 GeV.
 - power corrections within dispersive model
 - scale variation using factor $\sqrt{2}$

 $\alpha_s(M_Z) = 0.1164^{+0.0028}_{-0.0026}$ $\alpha_0(2 \text{GeV}) = 0.59 \pm 0.03$





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••• NNLL+NNLO+PC with thrust

[Gehrmann, GL, Monni, 1210.6945]

• Fit using TASSO/ALEPH/L3 data

- NP corrections within dispersive model extended to account for NNLL+NNLO corrections
- b-mass corrections included to NLO
- Random scan can over theoretical parameters
- Result stable by varying boundaries:





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••• NN(N)LL+NNLO+PC with thrust (SCET)

[Abbate, Fickinger, Hoang, Mateu, Stewart, 1006.3080]

Global fit using thrust

- Analytical hadronization with shape function
- Renormalon subtraction
- b-mass corrections and QED corrections





\mathbf{u}_{s} from jet rates

•
$$i^{\text{th}}$$
 jet rate: $R_i(y_{\text{cut}}) = \frac{\sigma_i(y_{\text{cut}})}{\sigma_{\text{tot}}}$

- From 3-jet rates:
 - ALEPH: [Dissertori et al., 0910.4283]
 - NNLO only
 - Stable up to $\ln(y_{cut}) = -4.5$
 - Small hadronization corrections

 $\alpha_s(M_Z) = 0.1175 \pm 0.0020 \pm 0.0015$

- JADE:
- [Schieck et al., 1205.3714]
- NNLO+NLLA+K + MC hadronization
- Impact of resummation important

 $\alpha_s(M_Z) = 0.1199 \pm 0.0023 \pm 0.0054$



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\mathbf{m}_{s} from jet rates

- From 5-jet rates: [Frederix et al., 1008.5313]
 - Using ALEPH data
 - Hadronization corrections estimated with Sherpa
 - → small, so **not** included

$$\alpha_s(M_Z) = 0.1156^{+0.0041}_{-0.0034}$$

	LEP1, hadr. $\sigma_{\rm tot}^{-1} {\rm d}\sigma/{\rm d}y_{45}, R_5$	LEP1, no hadr. $\sigma_{\rm tot}^{-1} d\sigma/dy_{45}, R_5$
stat.	+0.0002 -0.0002	+0.0002 -0.0002
syst.	+0.0027 -0.0029	+0.0027 -0.0029
pert.	+0.0062 -0.0043	+0.0068 -0.0047
fit range	+0.0014 -0.0014	+0.0005 -0.0005
hadr.	$+0.0012 \\ -0.0012$	_
$\alpha_s(M_Z)$	$0.1159 +0.0070 \\ -0.0055$	$0.1163 {+0.0073 \\ -0.0055}$

Table 2: Values of the strong coupling constant $\alpha_s(M_Z)$ obtained from fits to ALEPH LEP1 data for $\sigma_{\text{tot}}^{-1} d\sigma/dy_{45}$ and R_5 . NLO QCD predictions are used. Hadronization corrections are estimated with SHERPA. Default fit ranges are $3.8 \leq -\ln y_{45} \leq 5.2$, and $4.0 \leq -\ln y_{\text{cut}} \leq 5.6$. See the text for details.



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••• EW corrections & radiative return

[Denner, Dittmaier, Gehrmann, Kurz]

- NLO electroweak effect is potentially as large as NNLO QCD: $\alpha \approx \alpha_s^2$
 - Strong cancellation between event-shape distribution and hadronic cross section
 - ISR cancels

 M_7

- Weak loop corrections below per-mille
- corrections depend on final state photon cuts
- contribution from photon fragmentation
- α_s determination with EW corrections non trivial:
 - LEP data corrected for photonic effects
 - At LEP₂ radiative return not fully supressed



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Perspective for ILC

• Hadronization corrections proportional to Q⁻¹:



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• Perspective for ILC



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Recent fits of the strong coupling

• NNLO/NLL+NNLO with MC hadronization:

1. a/b ALEPH: [Dissertori at al. `o7, 'o9] $\alpha_s(M_Z) = 0.1240 \pm 0.0013 \pm 0.0031$ $\alpha_s(M_Z) = 0.1224 \pm 0.0013 \pm 0.0037$

2. a/b JADE: [Bethke at al. `08] $\alpha_s(M_Z) = 0.1210 \pm 0.0022 \pm 0.0057$ $\alpha_s(M_Z) = 0.1172 \pm 0.0021 \pm 0.0046$

3. a/b OPAL: [OPAL collaboration `11] $\alpha_s(M_Z) = 0.1201 \pm 0.0015 \pm 0.0026$ $\alpha_s(M_Z) = 0.1189 \pm 0.0018 \pm 0.0037$

• NN(N)LL+NNLO without hadronization:

4. ALEPH/OPAL (T): [Becher, Schwartz `08] $\alpha_s(M_Z) = 0.1172 \pm 0.0013 \pm 0.0017$

5. ALEPH/OPAL (ρ): [Chien, Schwartz `08] $\alpha_s(M_Z) = 0.1220 \pm 0.0019 \pm 0.0024$

[First error stati+syst., second error theo+had]

• NLL+NNLO with dispersive model:

6. Global fit (T): [Davison, Webber `o8] $\alpha_s(M_Z) = 0.1164^{+0.0028}_{-0.0026} \quad \alpha_0(2 \text{GeV}) = 0.59 \pm 0.03$

• NNLL+NNLO with dispersive model

7. Global fit (T): [Gehrmann, GL, Monni. '12] $\alpha_s(M_Z) = 0.1131^{+0.0028}_{-0.0022} \quad \alpha_0(2 \text{GeV}) = 0.538^{+0.102}_{-0.047}$

• NN(N)LL+NNLO with shape function

8. Global fit (T): [Abbate et al. `10]

 $\alpha_s(M_Z) = 0.1135 \pm 0.0002 \pm 0.0010$

• Jet rates extraction

9. ALEPH (R₃): no hadronization [Dissertori et al. `10] $\alpha_s(M_Z) = 0.1175 \pm 0.0020 \pm 0.0015$

10. JADE (R₃): NNLO+NLL [Schieck et al. `12] $\alpha_s(M_Z) = 0.1199 \pm 0.0023 \pm 0.0054$

11. ALEPH (R₅): [Frederix et al. `10] $\alpha_s(M_Z) = 0.1156^{+0.0041}_{-0.0034}$



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Recent fits of the strong coupling 2

• NNLO moments:



α_s from DIS and Hadron Collider

- On their way to precision ...
 - From PDF's and jet observables





D0 jet angular correlations, NLO D0, Phys. Lett. B718, 56 (2012)

ATLAS incl. jets, NLO B. Malaescu et al., EPJC 72, 2041 (2012)

CMS R3/2, NLO CMS QCD-11-003 (2012)

World average S. Bethke et al (PDG), Phys. Rev. D86, 010001 (2012)

0.11 0.12 [ATLAS, CMS, CDF, Do, H1 and Zeus Colls., 1302.4652]



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0.13

α_<(M_)

-

Determination of α_s (NLO)

- Comparison to other hadron O collider experiments
- Extraction also performed for three subranges in Q
- Small exp. uncertainty
- Dominated by th. uncertainty:
- asymmetric scale uncertainty
- PDF uncertainty

 $\begin{array}{c} \text{exp} \\ \hline \textbf{NNPDF21:} \quad \alpha_s(M_z) = 0.1148 \pm 0.0014 \\ \text{CT10:} \quad \alpha_s(M_z) = 0.1135 \pm 0.0019 \\ \text{MSTW2008:} \quad \alpha_s(M_z) = 0.1141 \pm 0.0022 \\ \textbf{(ABM11:} \quad \alpha_s(M_z) = 0.1214 \pm 0.0020) \end{array}$



PDF uncertainty: Repeat fit for each NNPDF replica \rightarrow get estimators for μ and σ Scale uncertainty: Repeat fit for six variations of $(\mu_r, \mu_r) \rightarrow$ get maximal deviation



Further determinations of α_{s}





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Conclusions & Outlook

- Many new determinations!!
 - e⁺e⁻ now with NNLL+NNLO

• Fit to full standard set soon?

Hadronization corrections are now the challenge

Further refinement in analytical models?
What about new MC tools?

- ILC can help since hadronization corrections get smaller!
- Learning how to perform precise extractions also from Tevatron and LHC data!

Further new results from different sources are on their way, stay tuned!!



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