# $m_{c}, m_{b}$, and $\alpha_{s}$ Lattice status and prospects 

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## Parametric uncertainties in BSM searches

| Channel | $M_{\mathrm{H}}[\mathrm{GeV}]$ | $\Gamma[\mathrm{MeV}]$ | $\Delta \alpha_{\text {s }}$ | $\Delta m_{\mathrm{b}}$ | $\Delta m_{\text {c }}$ | $\Delta m_{\mathrm{t}}$ | THU |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{H} \rightarrow \mathrm{bb}$ | 122 | 2.30 | -2.3\% | $+3.2 \%$ | +0.0\% | +0.0\% | $\begin{aligned} & +2.0 \% \\ & -2.0 \% \end{aligned}$ |
|  | 126 | 2.36 | $+2.3 \%$ $-2.3 \%$ | $-3.2 \%$ $+3.3 \%$ | $-0.0 \%$ $+0.0 \%$ | -0.0\% | +2.0\% |
|  | 126 |  | $\begin{aligned} & +2.3 \% \\ & -2.4 \% \\ & +2.3 \% \end{aligned}$ | $-3.2 \%$ | -0.0\% | -0.0\% | -2.0\% |
|  | 130 | 2.42 |  | $\begin{aligned} & +3.2 \% \\ & -3.2 \% \end{aligned}$ | $+0.0 \%$ | $\begin{aligned} & +0.0 \% \\ & { }_{-0.0 \%}^{+0} \end{aligned}$ | $\begin{aligned} & +2.0 \% \\ & { }_{-2.0 \%} \end{aligned}$ |
| $\mathrm{H} \rightarrow \tau^{+} \tau^{-}$ | 122 | $2.51 \cdot 10^{-1}$ | +0.0\% | +0.0\% | ${ }_{-0.0 \%}^{+0.0 \%}$ | $\begin{gathered} +0.0 \% \\ { }_{-0.1 \%}^{+0} \end{gathered}$ | +2.0\% |
|  | 122 | $2.51 \cdot 10^{-1}$ | $\begin{aligned} & +0.0 \% \\ & +0.0 \% \\ & \hline \end{aligned}$ | -0.0\% |  |  | +2.0\% |
|  | 126 | $2.59 \cdot 10^{-1}$ | $+0.0 \%$ $+0.0 \%$ | ${ }_{-0.0 \%}^{+0.0 \%}$ | ${ }_{-0.0 \%}$ | ${ }_{-0.1 \%}^{+0.1 \%}$ | -2.0\% |
|  | 130 | $2.67 \cdot 10^{-1}$ | $\begin{array}{r} +0.0 \% \\ +0.0 \% \\ \hline \end{array}$ | $\begin{array}{r} +0.0 \% \\ { }_{-0.0 \%} \\ \hline \end{array}$ | $\begin{array}{r} +0.0 \% \\ { }_{-0.0 \%} \\ \hline \end{array}$ | $\begin{aligned} & +0.1 \% \\ & { }_{-0.1 \%}^{+0} \end{aligned}$ | $\begin{aligned} & +2.0 \% \\ & -2.0 \% \\ & \hline \end{aligned}$ |
|  | 130 |  |  |  |  |  |  |
| $\mathrm{H} \rightarrow \mu^{+} \mu^{-}$ | 122 | $8.71 \cdot 10^{-4}$ | +0.0\% | +0.0\% | $\begin{aligned} & +0.0 \% \\ & -0.0 \% \end{aligned}$ | $\begin{aligned} & +0.1 \% \\ & { }_{-0.1 \%}^{+0} \end{aligned}$ | $\begin{aligned} & +2.0 \% \\ & -2.0 \% \end{aligned}$ |
|  | 126 | $8.99 \cdot 10^{-4}$ | $\begin{aligned} & +0.0 \% \\ & +0.0 \% \end{aligned}$ | $\begin{aligned} & +0.0 \% \\ & { }_{-0.0 \%} \end{aligned}$ | $\begin{aligned} & -0.1 \% \\ & -0.0 \% \end{aligned}$ | $+0.0 \%$ | $\begin{array}{r} 2.0 \% \end{array}$ |
|  |  |  | $\begin{aligned} & +0.0 \% \\ & +0.1 \% \\ & +0.0 \% \end{aligned}$ |  |  | $\begin{aligned} & -0.1 \% \\ & +0.1 \% \\ & -0.0 \% \end{aligned}$ | $\begin{aligned} & -2.0 \% \\ & +2.0 \% \end{aligned}$ |
|  | 130 | $9.27 \cdot 10^{-4}$ |  | $\begin{array}{r} +0.0 \% \\ { }_{-0.0 \%} \\ \hline \end{array}$ | $\begin{aligned} & -0.0 \% \\ & +0.0 \% \\ & -0.0 \% \end{aligned}$ |  |  |
| $\mathrm{H} \rightarrow \mathrm{c} \overline{\mathrm{c}}$ | 122 | $1.16 \cdot 10^{-1}$ | $\begin{aligned} & -7.1 \% \\ & +7.0 \% \end{aligned}$ | -0.1\% | $\begin{aligned} & +6.2 \% \\ & -60 \% \end{aligned}$ | ${ }_{-0.0 \%}^{+0.0 \%}$ | $\begin{aligned} & +2.0 \% \\ & -2.0 \% \end{aligned}$ |
|  |  | $1.19 \cdot 10^{-1}$ |  | $\begin{aligned} & -0.1 \% \\ & -0.1 \% \end{aligned}$ |  |  |  |
|  | 126 |  | $\begin{aligned} & +7.0 \% \\ & -7.1 \% \\ & +7.0 \% \end{aligned}$ |  | ${ }^{+6.2 \%}$ | $\begin{aligned} & +0.0 \% \\ & { }_{-0.1 \%} \end{aligned}$ | $\begin{aligned} & +2.0 \% \\ & { }_{-2.0 \%}^{+} \end{aligned}$ |
|  | 130 | $1.22 \cdot 10^{-1}$ | $\begin{aligned} & +7.0 \% \\ & -7.1 \% \\ & +7.0 \% \\ & \hline \end{aligned}$ | $\begin{aligned} & -0.1 \% \\ & -0.1 \% \\ & -0.1 \% \end{aligned}$ | +6.3\% | $\begin{aligned} & +0.1 \% \\ & { }_{-0.1 \%}^{+0} \end{aligned}$ | $\begin{aligned} & +2.0 \% \\ & -2.0 \% \\ & \hline \end{aligned}$ |
|  |  |  |  |  | -6.0\% |  |  |
| $\mathrm{H} \rightarrow \mathrm{gg}$ | 122 | $3.25 \cdot 10^{-1}$ | +4.2\% | -0.1\% | ${ }^{+0.0 \%}$ | $\begin{aligned} & -0.2 \% \\ & +0.2 \% \end{aligned}$ | +3.0\% |
|  | 126 | $3.57 \cdot 10^{-1}$ | $\begin{aligned} & -4.1 \% \\ & +4.2 \% \end{aligned}$ | $-0.1 \%$$-0.1 \%$ | $\begin{aligned} & +0.0 \% \\ & { }_{-0.0 \%}^{+0} \end{aligned}$ | $\begin{aligned} & -0.2 \% \\ & +0.2 \% \end{aligned}$ | $+3.0 \%$ |
|  |  |  | $\begin{aligned} & -4.1 \% \\ & +4.2 \% \\ & -4.1 \% \end{aligned}$ |  |  |  |  |
|  | 130 | $3.91 \cdot 10^{-1}$ |  | $-0.1 \%$ $-0.2 \%$ | $\begin{array}{r} +0.0 \% \\ { }_{-0.0 \%} \\ \hline \end{array}$ | $\begin{aligned} & -0.2 \% \\ & +0.2 \% \\ & \hline \end{aligned}$ | $\begin{array}{r} +3.0 \% \\ -3.0 \% \\ \hline \end{array}$ |
| $\mathrm{H} \rightarrow \gamma \gamma$ | 122 |  | -4.1\% | $\begin{aligned} & +0.0 \% \\ & { }_{-0}^{+0 \%} \end{aligned}$ | $+0.0 \%$ | $\begin{aligned} & +0.0 \% \\ & { }_{-0.0 \%}^{+0} \end{aligned}$ | $\begin{aligned} & +1.0 \% \\ & -10 \% \end{aligned}$ |
|  |  | $8.37 \cdot 10^{-3}$ | ${ }_{-0.0 \%}^{+0.0 \%}$ |  |  |  |  |
|  | 126 | $9.59 \cdot 10^{-3}$ | $\begin{aligned} & +0.0 \% \\ & { }_{-0.0 \%}^{+0} \end{aligned}$ | $\begin{aligned} & +0.0 \% \\ & { }_{-0.0 \%}^{+0} \end{aligned}$ | $\begin{aligned} & +0.0 \% \\ & { }_{-0.0 \%}^{+0} \end{aligned}$ | $\begin{aligned} & +0.0 \% \\ & { }_{-0.0 \%}^{+0} \end{aligned}$ | $\begin{aligned} & +1.0 \% \\ & { }_{-1.0 \%}^{+} \end{aligned}$ |
|  | 130 | $1.10 \cdot 10^{-2}$ | $\begin{array}{r} +0.1 \% \\ { }_{-0.0 \%} \\ \hline \end{array}$ | $\begin{aligned} & +0.0 \% \\ & { }_{-0.0 \%}^{+0} \end{aligned}$ | $\begin{aligned} & +0.0 \% \\ & -0.0 \% \end{aligned}$ | $\begin{aligned} & +0.0 \% \\ & { }_{-0.0 \%} \\ & \hline \end{aligned}$ | $\begin{aligned} & +1.0 \% \\ & -1.0 \% \\ & \hline \end{aligned}$ |
|  | 130 |  |  |  |  |  |  |
| $\mathrm{H} \rightarrow \mathrm{Z} \gamma$ | 122 | $4.74 \cdot 10^{-3}$ | +0.0\% | +0.0\% | +0.0\% | -0.1\% | $-5.0 \%$ |
|  |  | $6.84 \cdot 10^{-3}$ | $\begin{aligned} & -0.1 \% \\ & +0.0 \% \\ & -0.0 \% \end{aligned}$ | $\begin{aligned} & -0.0 \% \\ & +0.0 \% \\ & -0.0 \% \end{aligned}$ | $\begin{aligned} & -0.0 \% \\ & +0.0 \% \end{aligned}$ |  |  |
|  | 126 |  |  |  | -0.1\% | -0.1\% | -5.0\% |
|  | 130 | $9.55 \cdot 10^{-3}$ | $\begin{array}{r} +0.0 \% \\ { }_{-0.0 \%} \\ \hline \end{array}$ | $\begin{array}{r} +0.0 \% \\ +0.0 \% \\ \hline \end{array}$ | $\begin{aligned} & +0.0 \% \\ & { }_{-0.0 \%}^{+0.0} \end{aligned}$ | $\begin{aligned} & +0.0 \% \\ & -0.0 \% \end{aligned}$ | $\begin{array}{r} +5.0 \% \\ { }_{-5.0 \%} \\ \hline \end{array}$ |
|  |  |  |  |  |  |  |  |
| $\mathrm{H} \rightarrow \mathrm{WW}$ | 122 | $6.25 \cdot 10^{-1}$ | +0.0\% |  | -0.0\% | ${ }_{-0.0 \%}$ | ${ }^{+0.5 \%}$ |
|  | 126 | $9.73 \cdot 10^{-1}$ | $\begin{aligned} & -0.0 \% \\ & +0.0 \% \\ & -0.0 \% \\ & +0.0 \% \\ & +0.0 \% \\ & \hline \end{aligned}$ | $+0.0 \%$ | +0.0\% | +0.0\% | +0.5\% |
|  | 126 |  |  | $-0.0 \%$ | -0.0\% | -0.0\% | -0.5\% |
|  | 130 | 1.49 |  | $+0.0 \%$ | +0.0\% | +0.0\% | +0.5\% |
|  |  | 1.49 |  | $-0.0 \%$ | -0.0\% | -0.0\% | -0.5\% |
|  | 122 | $7.30 \cdot 10^{-2}$ | +0.0\% | +0.0\% | +0.0\% | +0.0\% | +0.5\% |
|  | 122 |  | -0.0\% | -0.0\% | -0.0\% | -0.0\% | -0.5\% |
| $\mathrm{H} \rightarrow \mathrm{ZZ}$ | 126 | $1.22 \cdot 10^{-1}$ | ${ }_{-0.0 \%}^{+0.0 \%}$ | ${ }_{-0.0 \%}^{+0.0 \%}$ | ${ }_{-0.0 \%}^{+0.0 \%}$ | $+0.0 \%$ | $+0.5 \%$ |
|  | 130 | $1.95 \cdot 10^{-1}$ | +0.0\% | +0.0\% | +0.0\% | +0.0\% | +0.5\% |
|  |  |  | -0.0\% | -0.0\% | -0.0\% | -0.0\% | -0.5\% |

Uncertainties in standard model parameters limit possible precision in searches for new physics.

Partial widths into $b \bar{b}, c \bar{c}$, and $g g$ are more dependent on parametric uncertainties than on other theory.

LHC Higgs Cross Section Working Group A. Denner et al. arXiv:1307.1347v1

Table 1: SM Higgs partial widths and their relative parametric (PU) and theoretical (THU) uncertainties for a selection of Higgs masses. For PU, all the single contributions are shown. For these four columns, the upper percentage value (with its sign) refers to the positive variation of the parameter, while the lower one refers to the negative variation of the parameter.

| Channel | $M_{\mathrm{H}}[\mathrm{GeV}]$ | BR | $\Delta m_{\text {c }}$ | $\Delta m_{\mathrm{b}}$ | $\Delta m_{\mathrm{t}}$ | $\Delta \alpha_{\text {s }}$ | PU | TU | Total |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{H} \rightarrow \mathrm{b} \overline{\mathrm{b}}$ | 120 | $6.48 \mathrm{E}-01$ | $\begin{aligned} & -0.2 \% \\ & +0.2 \% \end{aligned}$ | $\begin{aligned} & +1.1 \% \\ & -1.2 \% \end{aligned}$ | $\begin{aligned} & \hline+0.0 \% \\ & -0.0 \% \end{aligned}$ | $\begin{aligned} & -1.0 \% \\ & +0.9 \% \end{aligned}$ | $\begin{aligned} & \hline+1.5 \% \\ & -1.5 \% \end{aligned}$ | $\begin{aligned} & \hline{ }_{-1.3 \%}^{+1.3 \%} \end{aligned}$ | $\begin{aligned} & \hline+2.8 \% \\ & -2.8 \% \end{aligned}$ |
|  | 150 | $1.57 \mathrm{E}-01$ | $-0.1 \%$ | $\begin{aligned} & +2.7 \% \\ & +2.7 \% \end{aligned}$ | ${ }_{-0.1 \%}^{+0.1 \%}$ | $-2.2 \%$ | ${ }_{-3.5 \%}^{+3.4 \%}$ | ${ }_{-0.6 \%}^{+0.6 \%}$ | ${ }^{+4.0 \%}$ |
|  | 200 | $2.40 \mathrm{E}-03$ | ${ }_{-0.0 \%}^{+0.1 \%}$ | $-2.7 \%$ $+3.2 \%$ | ${ }^{-0.1 \%}$ | ${ }_{-2.5 \%}^{+2.1 \%}$ | ${ }^{-3.5 \%}$ | $-0.6 \%$ $+0.5 \%$ | $-4.0 \%$ $+4.6 \%$ |
|  |  |  | +0.0\% | $-3.2 \%$ | -0.1\% | +2.5\% | $-4.1 \%$ | -0.5\% | $-4.6 \%$ |
|  | 500 | $1.09 \mathrm{E}-04$ | $\begin{aligned} & -0.0 \% \\ & +0.0 \% \\ & \hline \end{aligned}$ | $\begin{aligned} & +3.2 \% \\ & \\ & -3.2 \% \end{aligned}$ | ${ }_{-0.1 \%}^{+0.1 \%}$ | $\begin{aligned} & -2.8 \% \\ & +2.8 \% \end{aligned}$ | $\begin{aligned} & +4.3 \% \\ & { }_{-}^{4.3 \%} \end{aligned}$ | $\begin{aligned} & +3.0 \% \\ & { }_{-1.1 \%} \end{aligned}$ | $\begin{aligned} & +7.2 \% \\ & -5.4 \% \end{aligned}$ |
| $\mathrm{H} \rightarrow \tau^{+} \tau^{-}$ | 120 | $7.04 \mathrm{E}-02$ | $\begin{aligned} & -0.2 \% \\ & +0.2 \% \end{aligned}$ | $\begin{aligned} & -2.0 \% \\ & +2.1 \% \end{aligned}$ | $\begin{aligned} & \hline+0.1 \% \\ & { }_{-0.1 \%} \end{aligned}$ | $\begin{aligned} & { }_{-1.3 \%}^{+1.4 \%} \end{aligned}$ | $\begin{aligned} & \hline+2.5 \% \\ & -2.4 \% \end{aligned}$ | $\begin{aligned} & { }_{-3.6 \%}^{+3.6 \%} \end{aligned}$ | ${ }_{-6.0 \%}^{+6.1 \%}$ |
|  | 150 | $1.79 \mathrm{E}-02$ | $\begin{aligned} & -0.1 \% \\ & +0.1 \% \end{aligned}$ | $\begin{aligned} & -0.5 \% \\ & +0.5 \% \end{aligned}$ | ${ }_{-0.1 \%}^{+0.1 \%}$ | ${ }_{-0.3 \%}^{+0.3 \%}$ | ${ }_{-0.6 \%}^{+0.6 \%}$ | ${ }_{-2.5 \%}^{+2.5 \%}$ | ${ }_{-3.1 \%}^{+3.0 \%}$ |
|  | 200 | 2.87E-04 | -0.0\% $+0.0 \%$ | -0.0\% $+0.0 \%$ $+0.0 \%$ | ${ }_{-0.1 \%}^{+0.0 \%}$ | ${ }_{-0.0 \%}^{+0.0 \%}$ | ${ }_{-0.1 \%}^{+0.0 \%}$ | ${ }_{-2.5 \%}^{+2.5 \%}$ | ${ }_{-2.6 \%}^{+2.5 \%}$ |
|  |  |  | ${ }_{-0.0 \%}^{+0.0 \%}$ | ${ }_{-0.0 \%}^{+0.0 \%}$ | ${ }^{-0.1 \%}$ | ${ }^{-0.0 \%}$ | $-0.1 \%$ $+0.1 \%$ | $-2.5 \%$ $+5.0 \%$ | $-2.6 \%$ $+5.0 \%$ |
|  | 500 | $1.53 \mathrm{E}-05$ | +0.0\% | +0.0\% | -0.1\% | +0.0\% | -0.1\% | -3.1\% | -3.2\% |
| $\mathrm{H} \rightarrow \mu^{+} \mu^{-}$ | 120 | $2.44 \mathrm{E}-04$ | $\begin{aligned} & -0.2 \% \\ & +0.2 \% \end{aligned}$ | $\begin{aligned} & -2.0 \% \\ & +2.1 \% \end{aligned}$ | ${ }_{-0.1 \%}^{+0.1 \%}$ | $\begin{aligned} & { }_{-1.3 \%}^{+1.4 \%} \end{aligned}$ | ${ }_{-2.5 \%}^{+2.5 \%}$ | ${ }_{-3.9 \%}^{+3.9 \%}$ | ${ }_{-6.3 \%}^{+6.4 \%}$ |
|  | 150 | $6.19 \mathrm{E}-05$ | $\begin{aligned} & -0.0 \% \\ & +0.0 \% \end{aligned}$ | $\begin{aligned} & -0.5 \% \\ & +0.5 \% \end{aligned}$ | ${ }_{-0.1 \%}^{+0.1 \%}$ | ${ }_{-0.3 \%}^{+0.3 \%}$ | $\begin{array}{r} +0.6 \% \\ +0.6 \% \end{array}$ | $\begin{array}{r} +2.5 \% \\ +2.5 \% \end{array}$ | ${ }_{-3.2 \%}^{+3.1 \%}$ |
|  | 200 | 9.96E-07 | ${ }_{-0.0 \%}^{-0.0 \%}$ | ${ }_{-}^{-0.0 \%}$ | ${ }_{-0.1 \%}^{+0.1 \%}$ | ${ }_{-0.0 \%}^{+0.0 \%}$ | ${ }_{-0.1 \%}^{+0.1 \%}$ | ${ }^{+2.5 \%}$ | ${ }_{-2.6 \%}^{+2.6 \%}$ |
|  | 500 | $5.31 \mathrm{E}-08$ | -0.0\% | $-0.0 \%$ | $+0.1 \%$ | -0.0\% | $+0.1 \%$ | +5.0\% | +5.1\% |
|  | 500 | 5.31E-08 | +0.0\% | +0.0\% | -0.1\% | +0.0\% | -0.1\% | -3.1\% | -3.1\% |
| $\mathrm{H} \rightarrow \mathrm{c} \overline{\mathrm{c}}$ | 120 | $3.27 \mathrm{E}-02$ | ${ }_{-5.8 \%}^{+6.0 \%}$ | $\begin{aligned} & -2.1 \% \\ & +2.2 \% \end{aligned}$ | ${ }_{-0.1 \%}^{+0.1 \%}$ | $\begin{aligned} & -5.8 \% \\ & +5.6 \% \end{aligned}$ | ${ }_{-8.5 \%}^{+8.5 \%}$ | ${ }_{-3.7 \%}^{+3.8 \%}$ | $\begin{gathered} { }_{-12.2 \%}^{+12.2 \%} \end{gathered}$ |
|  | 150 | 7.93E-03 | ${ }_{-6.2 \%}$ | ${ }^{-0.6 \%}$ | ${ }^{+0.1 \%}$ | ${ }^{-6.9 \%}$ | ${ }^{+9.2 \%}$ | ${ }^{+0.6 \%}$ | ${ }^{+9.7 \%}$ |
|  | 200 | $1.21 \mathrm{E}-04$ | -6.2\% | ${ }_{-0.2 \%}^{+0.6 \%}$ | ${ }_{+}^{-0.1 \%}$ | ${ }_{-7.2 \%}^{+6.8 \%}$ | ${ }_{+}^{-9.2 \%}$ | ${ }^{-0.6 \%}$ | $-9.7 \%$ $+10.0 \%$ |
|  | 200 | $1.21 \mathrm{E}-04$ | ${ }_{-6.1 \%}$ | +0.1\% | $-0.2 \%$ | +7.2\% | -9.5\% | -0.5\% | -10.0\% |
|  | 500 | $5.47 \mathrm{E}-06$ | ${ }_{-6.0 \%}^{+6.2 \%}$ | $\begin{aligned} & -0.1 \% \\ & +0.1 \% \end{aligned}$ | ${ }_{-0.1 \%}^{+0.1 \%}$ | $\begin{aligned} & -7.6 \% \\ & +7.6 \% \end{aligned}$ | ${ }_{-9.7 \%}^{+9.8 \%}$ | ${ }_{-1.1 \%}^{+3.0 \%}$ | $\begin{aligned} & +12.8 \% \\ & { }_{-10.7 \%} \end{aligned}$ |
| $\mathrm{H} \rightarrow \mathrm{t} \overline{\mathrm{t}}$ | 350 | $1.56 \mathrm{E}-02$ | $\begin{aligned} & +0.0 \% \\ & +0.0 \% \end{aligned}$ | $\begin{aligned} & -0.0 \% \\ & +0.0 \% \end{aligned}$ | $\begin{array}{r} -78.6 \% \\ +120.9 \% \end{array}$ | ${ }_{-0.9 \%}^{+0.9 \%}$ | $\begin{aligned} & +120.9 \% \\ & { }_{-78.6 \%} \end{aligned}$ | $\begin{aligned} & { }_{-12.7 \%}^{+6.9 \%} \end{aligned}$ | $\begin{aligned} & \hline+127.8 \% \\ & { }_{-91.3 \%}^{+8} \end{aligned}$ |
|  | 360 | 5.14E-02 | ${ }_{-0}^{-0.0 \%}$ | ${ }^{-0.0 \%}$ | -36.2\% | ${ }^{+0.7 \%}$ | ${ }_{-36 \%}+3.6$ | ${ }^{+6.6 \%}$ | +42.2\% |
|  |  | $1.48 \mathrm{E}-01$ | $-0.0 \%$ $+0.0 \%$ | ${ }_{-0.0 \%}^{+0.0 \%}$ | ${ }^{+35.8 \%}$ | $-0.7 \%$ $+0.4 \%$ | $-36.2 \%$ $+6.2 \%$ | ${ }^{-12.2 \%}$ | $-48.4 \%$ $+12.2 \%$ |
|  | 400 | $1.48 \mathrm{E}-01$ | +0.0\% | +0.0\% | +6.2\% | -0.3\% | -6.8\% | -11.1\% | -17.8\% |
|  | 500 | $1.92 \mathrm{E}-01$ | $\begin{aligned} & -0.0 \% \\ & +0.0 \% \\ & \hline \end{aligned}$ | $\begin{aligned} & -0.0 \% \\ & +0.0 \% \\ & \hline \end{aligned}$ | $\begin{aligned} & -0.3 \% \\ & +0.1 \% \\ & \hline \end{aligned}$ | $\underset{-0.2 \%}{+0.1 \%}{ }_{-{ }_{-0.2}}$ | ${ }_{-0.3 \%}^{+0.1 \%}$ | $\begin{gathered} +9.5 \% \\ { }_{-9.5 \%}^{4 .} \end{gathered}$ | $\begin{aligned} & +4.6 \% \\ & { }_{-9.8 \%}^{+4} \end{aligned}$ |
| $\mathrm{H} \rightarrow \mathrm{gg}$ | 120 | 8.82E-02 | $\begin{aligned} & -0.2 \% \\ & +0.2 \% \end{aligned}$ | $\begin{aligned} & -2.2 \% \\ & +2.2 \% \end{aligned}$ | $\begin{aligned} & -0.2 \% \\ & +0.2 \% \end{aligned}$ | ${ }_{-5.4 \%}^{+5.7 \%}$ | ${ }_{-5.8 \%}^{+6.1 \%}$ | $\begin{aligned} & { }_{-4.5 \%}^{+4.5 \%} \end{aligned}$ | $\begin{aligned} & { }_{-10.3 \%}^{10.6 \%} \end{aligned}$ |
|  | 150 | $3.46 \mathrm{E}-02$ | ${ }^{-0.1 \%}$ | ${ }^{-0.7 \%}$ | $-0.3 \%$ | ${ }^{+4.4 \%}$ | ${ }^{+4.4 \%}$ | ${ }^{+3.5 \%}$ | +7.9\% |
|  |  |  | ${ }_{-0.0 \%}^{+0.1 \%}$ | ${ }_{-0.1 \%}^{+0.6 \%}$ | ${ }_{-0.6 \%}^{+0.3 \%}$ | $-4.2 \%$ $+3.9 \%$ | $-4.3 \%$ $+3.9 \%$ | ${ }^{-3.5 \%}+3.7 \%$ | -7.8\% |
|  | 200 | $9.26 \mathrm{E}-04$ | ${ }_{-0.0 \%}$ | ${ }^{-0.1 \%}$ | ${ }^{-0.6 \%}$ | ${ }_{-3.8 \%}^{+3.9 \%}$ | ${ }_{-3.9 \%}^{+3.9 \%}$ | ${ }_{-3.7 \%}^{+3.75}$ | ${ }_{-7.6 \%}^{+7.6 \%}$ |
|  | 500 | $6.04 \mathrm{E}-04$ | $\begin{aligned} & -0.0 \% \\ & +0.0 \% \end{aligned}$ | $\begin{aligned} & -0.0 \% \\ & +0.0 \% \\ & + \end{aligned}$ | $\begin{aligned} & +1.6 \% \\ & -1.6 \% \\ & \\ & \hline \end{aligned}$ | $\begin{aligned} & +.4 \% \\ & { }_{-3.3 \%} \end{aligned}$ | $\begin{aligned} & +3.7 \% \\ & { }_{-3.7} \end{aligned}$ | $\begin{aligned} & +6.2 \% \\ & { }_{-}^{+6.3 \%} \end{aligned}$ | ${ }_{-7.9 \%}^{+9.9 \%}$ |
| $\mathrm{H} \rightarrow \gamma \gamma$ | 120 | $2.23 \mathrm{E}-03$ | $\begin{aligned} & -0.2 \% \\ & +0.2 \% \end{aligned}$ | $\begin{aligned} & -2.0 \% \\ & +2.1 \% \end{aligned}$ | $\begin{aligned} & +0.0 \% \\ & +0.0 \% \end{aligned}$ | $\begin{aligned} & { }_{-1.3 \%}^{+1.4 \%} \end{aligned}$ | $\underset{-2.4 \%}{+2.5 \%}$ | $\begin{aligned} & { }_{-2.9 \%}^{+2.9 \%} \end{aligned}$ | $\underset{-5.3 \%}{+5.4 \%}$ |
|  | 150 | $1.37 \mathrm{E}-03$ | ${ }^{+0.0 \%}$ | ${ }^{-0.5 \%}$ | ${ }_{-0.1 \%}^{+0.10 \%}$ | ${ }_{-0.3 \%}^{+0.3 \%}$ | ${ }_{-0.6 \%}^{+0.6 \%}$ | ${ }^{+1.6 \%}$ | + ${ }^{2.1 \%}$ |
|  |  | $5.51 \mathrm{E}-05$ | ${ }_{-0.0 \%}^{+0.1 \%}$ | ${ }_{-0.0 \%}^{+0.5 \%}$ | ${ }_{+}^{+0.0 \%}$ | $-0.3 \%$ $+0.0 \%$ | ${ }_{+}^{-0.6 \%}$ | ${ }^{-1.5 \%}+1.5 \%$ | - $+1.1 \%$ $+1.6 \%$ |
|  | 200 | 5.51E-05 | -0.0\% | +0.0\% | $-0.1 \%$ | -0.0\% | $-0.1 \%$ | $-1.5 \%$ | $-1.6 \%$ |
|  | 500 | $3.12 \mathrm{E}-07$ | $\begin{aligned} & -0.0 \% \\ & +0.0 \% \\ & \hline \end{aligned}$ | $\begin{aligned} & -0.0 \% \\ & +0.0 \% \\ & \hline \end{aligned}$ | $\begin{aligned} & +8.0 \% \\ & \hline-6.5 \% \end{aligned}$ | $\begin{aligned} & -0.7 \% \\ & +0.7 \% \end{aligned}$ | ${ }_{-6.6 \%}^{+8.0 \%}$ | $\begin{aligned} & +2.1 \% \\ & { }_{-2.15}^{+4 .} \end{aligned}$ | $\begin{array}{r} +11.9 \% \\ \quad-8.7 \% \end{array}$ |
| $\mathrm{H} \rightarrow \mathrm{Z} \gamma$ | 120 | $1.11 \mathrm{E}-03$ | $\begin{aligned} & -0.3 \% \\ & +0.2 \% \end{aligned}$ | $\begin{aligned} & -2.1 \% \\ & +2.1 \% \end{aligned}$ | ${ }_{-0.1 \%}^{+0.0 \%}$ | $\begin{aligned} & { }_{-1.4 \%}^{+1.4 \%} \end{aligned}$ | ${ }_{-2.5 \%}^{+2.5 \%}$ | ${ }_{-6.8 \%}^{+6.9 \%}$ | $\underset{-9.3 \%}{+9.4 \%}$ |
|  | 150 | $2.31 \mathrm{E}-03$ | $-0.1 \%$ $+0.0 \%$ | $-0.6 \%$ $+0.5 \%$ | ${ }_{-0.1 \%}^{+0.0 \%}$ | ${ }_{-0.3 \%}^{+0.2 \%}$ | ${ }_{-0.6 \%}^{+0.5 \%}$ | ${ }_{-5.5 \%}^{+5.5 \%}$ | ${ }_{-6.2 \%}^{+6.0 \%}$ |
|  |  |  | ${ }_{-0.0 \%}^{+0.0 \%}$ | ${ }_{-0.0 \%}^{+0.5 \%}$ | ${ }_{+}^{-0.1 \%}$ | $-0.3 \%$ $+0.0 \%$ | ${ }_{+}^{-0.6 \%}$ | ${ }^{-5.5 \%}$ | ${ }^{-6.2 \%}$ |
|  | 200 | $1.75 \mathrm{E}-04$ | -0.0\% | +0.0\% | ${ }_{-0.1 \%}$ | ${ }^{-0.0 \%}$ | ${ }_{-0.1 \%}$ | ${ }_{-5.5 \%}$ | ${ }_{-5.6 \%}$ |
|  | 500 | 7.58E-06 | $\begin{aligned} & -0.0 \% \\ & +0.0 \% \\ & \hline \end{aligned}$ | $\begin{aligned} & -0.0 \% \\ & +0.0 \% \\ & \hline \end{aligned}$ | ${ }_{-0.6 \%}^{+0.8 \%}$ | $\begin{aligned} & -0.0 \% \\ & +0.0 \% \\ & \hline \end{aligned}$ | ${ }_{-0.6 \%}^{+0.8 \%}$ | ${ }_{-6.1 \%}^{+8.0 \%}$ | $\begin{gathered} +8.7 \% \\ { }_{-6.7}^{+8 \%} \end{gathered}$ |
| $\mathrm{H} \rightarrow \mathrm{WW}$ | 120 | $1.41 \mathrm{E}-01$ | $\begin{aligned} & -0.2 \% \\ & +0.2 \% \end{aligned}$ | $\begin{aligned} & -2.0 \% \\ & +2.1 \% \end{aligned}$ | $\begin{aligned} & -0.0 \% \\ & +0.0 \% \end{aligned}$ | $\begin{aligned} & { }_{-1.4 \%}^{+1.4 \%} \end{aligned}$ | ${ }_{-2.5 \%}^{+2.5 \%}$ | ${ }_{-2.2 \%}^{+2.2 \%}$ | $\begin{aligned} & { }_{-4.7 \%}^{+4.8 \%} \end{aligned}$ |
|  | 150 | 6.96E-01 | $-0.1 \%$ $+0.1 \%$ | -0.5\% | -0.0\% | ${ }_{-0.3 \%}^{+0.3 \%}$ | ${ }_{-0.6 \%}^{+0.6 \%}$ | ${ }_{-0.3 \%}^{+0.3 \%}$ | ${ }_{-0.8 \%}^{+0.9 \%}$ |
|  | 200 | 7.41E-01 | ${ }^{-0.0 \%}$ | ${ }_{-0.0 \%}$ | ${ }^{-0.0 \%}$ | ${ }^{+0.0 \%}$ | ${ }^{+0.0 \%}$ | ${ }^{+0.0 \%}$ | ${ }^{+0.0 \%}$ |
|  |  | 7.415-01 | -0.0\% | +0.0\% | +0.0\% | -0.0\% | -0.0\% | -0.0\% | -0.0\% |
|  | 500 | $5.46 \mathrm{E}-01$ | $\begin{aligned} & -0.0 \% \\ & +0.0 \% \\ & \hline \end{aligned}$ | $\begin{aligned} & -0.0 \% \\ & +0.0 \% \\ & \hline \end{aligned}$ | $\begin{array}{r} -0.0 \% \\ +0.1 \% \end{array}$ | $\begin{aligned} & -0.0 \% \\ & +0.0 \% \\ & \hline \end{aligned}$ | ${ }_{-0.1 \%}^{+0.1 \%}$ | ${ }_{-1.1 \%}^{+2.3 \%}$ | ${ }_{-1.1 \%}^{+2.4 \%}$ |
| $\mathrm{H} \rightarrow \mathrm{ZZ}$ | 120 | $1.59 \mathrm{E}-02$ | $\begin{aligned} & -0.2 \% \\ & +0.2 \% \end{aligned}$ | $\begin{aligned} & -2.0 \% \\ & +2.1 \% \end{aligned}$ | $\begin{aligned} & -0.0 \% \\ & +0.0 \% \end{aligned}$ | $\begin{aligned} & { }_{-1.4 \%}^{+1.4 \%} \end{aligned}$ | ${ }_{-2.5 \%}^{+2.5 \%}$ | $\begin{aligned} & { }_{-2.2 \%}^{+2.2 \%} \end{aligned}$ | $\begin{aligned} & { }_{-4.7 \%}^{+4.8 \%} \end{aligned}$ |
|  | 150 | $8.25 \mathrm{E}-02$ | ${ }^{-0.1 \%}$ | ${ }^{-0.5 \%}$ | ${ }^{+0.0 \%}$ | ${ }_{-0.3 \%}^{+0.3 \%}$ | ${ }_{-0.6 \%}^{+0.6 \%}$ | ${ }_{-0.3 \%}^{+0.3 \%}$ | ${ }_{-0.8 \%}^{+0.9 \%}$ |
|  | 200 | $2.55 \mathrm{E}-01$ | ${ }^{-0.0 \%}$ | ${ }^{-0.0 \%}$ | +0.0\% | +0.0\% | +0.0\% | ${ }^{+0.0 \%}$ | ${ }^{-0.0 \%}$ |
|  |  | $2.55 \mathrm{E}-01$ | +0.0\% | +0.0\% | -0.0\% | -0.0\% | -0.0\% | -0.0\% | -0.0\% |
|  | 500 | $2.61 \mathrm{E}-01$ | ${ }_{-0.0 \%}^{+0.0 \%}$ | $\begin{aligned} & -0.0 \% \\ & +0.0 \% \end{aligned}$ | ${ }_{+}^{+0.0 \%}$ | $\begin{aligned} & -0.0 \% \\ & +0.0 \% \end{aligned}$ | ${ }_{-0.0 \%}^{+0.1 \%}$ | ${ }_{-1.1 \%}^{+2.3 \%}$ | ${ }_{-1.1 \%}^{+2.3 \%}$ |

Branching ratios.

Since the total width is dominated by the $b \bar{b}$ channel, almost all branching fractions are strongly dependent on $m_{b}$, as well.

Lattice QCD can provide the most precise determinations of the parameters $\alpha_{s}, m_{c}$, and $m_{b}$.

Handbook of LHC Higgs cross sections: 3. Higgs properties
S. Heinemeyer et al.
arXiv:1307.1347v1 (with its sign) refers to the positive variation of the parameter, while the lower one refers to the negative variatio parameter. Results for the full mass range, including the total uncertainties, are listed in Tables at the end of the doc

## Lattice in the 21st century



Phys.Rev.Lett. 92 (2004) 022001
Lattice/experiment without (L) and with (R) quark-antiquark pairs.

For the past ~ten years, it has been possible to use lattice QCD Monte Carlo methods to calculate simple quantities with understood error budgets that are complete, including the effects of quarkantiquark pairs.

## What is "simple"?

- Simplest: stable mesons.
- Over the last ten years, many key quantities. Hadronically stable mesons, especially:
- Heavy and light meson decay constants,
- Semileptonic decays,
- Meson-antimeson mixing.
- Make possible important determinations of 8 CKM matrix elements, 5 quark masses, the strong coupling constant.
- Now: $\pi \pi$ systems, nucleons


## Coming US experimental program

- Next five years: lattice calculations are needed throughout the entire future US experimental program.
- g-2
- mu2e, LBNE, Nova: nucleon matrix elements.
- Underground LBNE: proton decay matrix elements.
- LHCb, Belle-2: continued improvement of CKM results
- LHC, Higgs decays: lattice provides the most accurate $\alpha_{s}$ and $m_{c}$ now, and $m_{b}$ in the future


## How?



$$
\left\langle\bar{\psi} \gamma_{5} \psi(t=0) \mid \bar{\psi} \gamma_{5} \psi(t)\right\rangle=C \exp (-M t)+\text { excited states. }
$$

If the two quarks were a $u$ and a $\bar{u}$, the slope would give $M_{\pi}, C$ would be proportional to $F_{\pi}{ }^{2}$.

## To obtain $\alpha_{s}, m_{c}$, or $m_{b}$ via the lattice

- In principle,
- can get $m_{\overline{M s}}$ from $m_{\text {latt }}$ by equating Green's functions calculated in perturbation theory in the two regulators:

- In practice,
- Calculating short-distance quantities to third order perturbation theory is hard and messy.
- Calculating some short-distance quantities nonperturbatively is easy and clean.
- The art of determining $\alpha_{s}$ or $m_{q}$ via the lattice is finding a quantity as easy to calculate as possible
- with continuum perturbation theory, and
- nonperturbatively with the lattice.


PDG, Beringer et al., 2013.

The most precise nonlattice determinations of $m_{c}$ use $e^{+} e^{-}$annihilation $m_{c}$ use $e^{+} e^{-}$annihilation
data and ITEP sum rules. (Karlsruhe group, Chertyrkin et al.)

Recent lattice determination of HPQCD uses the same type of perturbation theory, but lattice QCD to supply the correlation functions rather than experiment.

## $e+e-\rightarrow m_{c}$



$$
\mathcal{M}_{n} \equiv \int \frac{d s}{s^{n+1}} R_{Q}(s)
$$

Moments of the heavy quark production cross section in $\mathrm{e}^{+} \mathrm{e}^{-}$annihilation can be related to the derivatives of the vacuum polarization at $q^{\wedge} 2=0$.


$$
\mathcal{M}_{n}=\left.\frac{12 \pi^{2}}{n!}\left(\frac{d}{d q^{2}}\right)^{n} \Pi_{Q}\left(q^{2}\right)\right|_{q^{2}=0}
$$

Can be calculated in perturbation theory. Known to $\mathrm{O}\left(\alpha_{s}{ }^{3}\right)$ (Chetyrkin et. al.)

## Lattice QCD

can also compute such correlation functions with high accuracy.



Correlation functions of all currents can be calculated in perturbation theory (and with the lattice). The most precise $m_{c}$ can be obtained by choosing the one that is most precise on the lattice: the pseudoscalar correlator.

$$
\begin{aligned}
& G(t)=a^{6} \sum_{\mathbf{x}}\left(a m_{0 h}\right)^{2}\langle 0| j_{5}(\mathbf{x}, t) j_{5}(0,0)|0\rangle, \\
& G_{n} \equiv \sum_{t}(t / a)^{n} G(t),
\end{aligned}
$$

Perturbation theory to $\alpha_{s}{ }^{3}$ from the Karlsruhe group.

## Technical tricks to make the lattice calculation more precise

Choose pseudoscalar (easiest) current correlator. (Easier to calculate than a pion or charmonium mass.)


In matching perturbative and nonperturbative results, divide both by the tree level correlator. (Removes leading discretization errors.)

In the lattice calculation of, for example, the charm correlator, use $M \eta_{c}$ as experimental input to set the energy scale. (Removes sensitivity to the tuning of the lattice mass used.)

$$
R_{n} \equiv \begin{cases}G_{4} / G_{4}^{(0)} & \text { for } n=4 \\ \frac{a m_{n_{h}}}{2 a m_{0 n}}\left(G_{n} / G_{n}^{(0)}\right)^{1 /(n-4)} & \text { for } n \geq 6\end{cases}
$$

## $m_{c}$ results



PDG, Beringer et al., 2013.

|  | $m_{c}(3)$ |
| :--- | :---: |
| $a^{2}$ extrapolation | $0.2 \%$ |
| Perturbation theory | 0.5 |
| Statistical errors | 0.1 |
| $m_{h}$ extrapolation | 0.1 |
| Errors in $r_{1}$ | 0.2 |
| Errors in $r_{1} / a$ | 0.1 |
| Errors in $m_{\eta_{c}}, m_{\eta_{b}}$ | 0.2 |
| $\alpha_{0}$ prior | 0.1 |
| Gluon condensate | 0.0 |
| Total | $0.6 \%$ |

$m_{c}\left(m_{c}, n_{f}=4\right)=1.273(6) \mathrm{GeV}$.

HPQCD, McNeile et al.
Uncertainty is dominated by the same perturbation theory used in all of the most precise results.

# Why can lattice determinations of $m_{c}$ from correlation functions be more precise than those from $e^{+} e^{-}$? 



Moments of correlation functions are even easier than what I earlier told you have been considered the easiest quantities for the last ten years.
We need the correlation functions at finite $T$, and not their asymptotic form at large $T$.


PDG, Beringer et al., 2013.

The most precise nonlattice determinations of $m_{c}$ use $e^{+} e^{-}$annihilation data and ITEP sum rules. (Karlsruhe group, Chertyrkin et al.)

Recent lattice determination uses the same type of perturbation theory, but lattice QCD to supply the correlation functions rather than experiment.

For $m_{b}$, perturbative errors are tiny. $\left(\alpha\left(m_{b}\right)^{4} \ll \alpha\left(m_{c}\right)^{4}\right.$.)

## $m_{b}$ results

For $m_{b}$, these lattice correlator methods are just barely working at $a=0.045 \mathrm{fm}$.
(They treat the $b$ as light compared with 1/a.)
Need $a=0.03 \mathrm{fm}$ to be comfortable.
Discretization errors and statistics dominate current uncertainties. Both can be attacked with brute force computing power.
Needed configurations are projected to be generated in the next few years.


## $m_{b}$ results

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Need $a=0.03 \mathrm{fm}$ to be comfortable.
Discretization errors and statistics dominate current uncertainties. Both can be attacked with brute force computing power.
Needed configurations are projected to be generated in the next few years.

The three most precise determinations of mb using moments of $e^{+} e^{-}$data arrive at different estimates of the precision.

Coming lattice calculations should be able to confirm (or not) the more more precise claims.
Unlike $m_{c}$, where the lattice and $e^{+} e^{-}$ determinations share the same perturbation theory, perturbative uncertainties are neglible and the lattice and $e^{+} e-$ determinations will have totally independent uncertainties.


There are multiple ways of determining $\alpha_{s}$, both with and without the lattice.

There are several lattice determinations equal to or more precise than all the non-lattice determinations together.

## $\alpha_{s}$ results: correlator method




Results are dominated by perturbation theory. May by hard to improve without next term in perturbation theory.

## $\alpha_{s}$ results: Wilson loops

$\alpha_{s}$ can be determined with lattice calculations of many other quantities, e.g., the heavy quark potential.


Lattice calculates the heavy quark potential from Wilson loops.


HPQCD has determined $\alpha_{s}$ directly from Wilson loops.
Result compatible with their correlator result, similar precision: $\alpha_{s}=0.1184(6)$, but
totally different uncertainties, heavy use of lattice perturbation theory.

## $\alpha_{s}$, other lattice results

There are numerous good ways of determining $\alpha_{s}$ using lattice QCD.

- The Adler function, JLQCD. Phys.Rev. D82 (2010) 074505.
- $\alpha_{s}=0.1181 \pm 0.0003+0.0014-0.0012$
- The Schrödinger functional, PACS-CS. JHEP 0911:053,2009.
- $\alpha_{s}=0.1205(8)(5)(+0 /-17)$
- The ghost-gluon vertex, European Twisted Mass Collaboration (ETM). Phys.Rev.Lett. 108 (2012) 262002.
- $\alpha_{s}=0.1200(14)$


## PDG

2012, combined the lattice numbers in a weighted average. It takes a combined error of the most precise of the inputs.


## PDG

2012, combined the lattice numbers in a weighted average. It takes a combined error of the most precise of the inputs.


The lattice results (2013) are dominated by the two most precise results from HPQCD, but there are several other lattice results from Europe and Japan, all of which agree with each other and each which is more precise than any non-lattice result.

## Prospects: $m_{c}$ and $m_{b}$

- Correlator methods are currently the most precise, both with
- $\mathrm{e}^{+} \mathrm{e}^{-}$and with lattice methods.
- For $m_{c}$, correlator moments are simple to calculate on the lattice
- Should be checkable by many lattice groups.
- Results should be of comparable precision to determinations from e+e-
- Uncertainty will be dominated by perturbation theory.
- For $m_{b}$, most precise lattice determination relies on treating $b$ quark as light compared to $1 / a$.
- Possible with HISQ fermions, may be hard for other lattice methods.
- The lattice result should catch up to the most precise of the $\mathrm{e}^{+} \mathrm{e}^{-}$results with more CPU power.
- The resulting uncertainties in the $\mathrm{e}^{+} \mathrm{e}^{-}$determinations and the lattice determinations will be totally independent of each other (unlike the case for $m_{c}$ ); perturbative uncertainty is negligible.


## Prospects: $\alpha_{s}$

- The uncertainties of the Wilson loop and correlator determinations of $\alpha_{s}$ are dominated by perturbation theory and will improve somewhat, but probably not dramatically.
- $\alpha_{s}$ can be determined well from lattice calculations of many different quantities. There is likely to be continued improvement in the apparent robustness of the lattice results as more quantities are calculated with increasing precision.
- As of now there are results from
- five different quantities,
- four different groups on three continents,
- four different fermion discretizations.
- Results are completely independent and consistent, and each is more precise than the most precise non-lattice determination.


## Treatment of parametric uncertainties in Higgs physics

Current discussions of Higgs branching fractions and partial widths use very conservative estimates of parametric precisions.

Table 1: Input parameters and their relative uncertainties, as used for the uncertainty estimation of the branching ratios. The masses of the central values correspond to the 1-loop pole masses, while the last column contains the corresponding $\overline{\mathrm{MS}}$ mass values.

| Parameter | Central value | Uncertainty | $\overline{\mathrm{MS}}$ masses $m_{\mathrm{q}}\left(m_{\mathrm{q}}\right)$ |
| :---: | :---: | :---: | :---: |
| $\alpha_{\mathrm{s}}\left(M_{\mathrm{Z}}\right)$ | 0.119 | $\pm 0.002$ |  |
| $m_{\mathrm{c}}$ | 1.42 GeV | $\pm 0.03 \mathrm{GeV}$ | 1.28 GeV |
| $m_{\mathrm{b}}$ | 4.49 GeV | $\pm 0.06 \mathrm{GeV}$ | 4.16 GeV |
| $m_{\mathrm{t}}$ | 172.5 GeV | $\pm 2.5 \mathrm{GeV}$ | 165.4 GeV |

arXiv:1201.3084v1 [hep-ph] 15 Jan 2012

|  | Higgs X- <br> Section WG | PDG | lattice | Karlsruhe <br> $\left(\mathrm{e}^{+} \mathrm{e}^{-}\right)$ | world <br> non-lattice |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\delta \alpha_{s}$ | 0.002 | 0.0007 | 0.0007 |  | 0.0012 |
| $\delta m_{c}(\mathrm{GeV})$ | 0.03 | 0.025 | 0.006 | 0.013 |  |
| $\delta m_{b}(\mathrm{GeV})$ | 0.06 | 0.03 | 0.023 | 0.016 |  |

$90 \% \mathrm{CL}, 2 \sigma$, and $2 \sigma$ errors.
$1 \sigma$ errors.

Level of conservatism in assumed uncertainties that is appropriate depends on circumstances, e.g., on whether you're discussing with a postdoc where something funny might be going on or whether you're discussing with the New York Times.

## What to expect

- $m_{c}$ : Uncertainty in leading lattice result will improve somewhat. Correlator moments will be calculated by a number of lattice groups with competing methods. Uncertainty will be dominated by perturbation theory.
- $\alpha_{s}$ : Uncertainty in leading lattice result will improve somewhat.
$\alpha_{s}$ will be determined by a number of lattice groups using competing methods. Each will be more precise than all the nonlattice determinations put together.
- $m_{b}$ : The precision of the best lattice result will improve by a factor of two or more, matching the most precise claimed uncertainties from $\mathrm{e}^{+} \mathrm{e}^{-}$. Uncertainties from lattice and $\mathrm{e}^{+} \mathrm{e}^{-}$will have nothing to do with each other.


## What to expect

| P | $\begin{aligned} & \text { PDG } \\ & 2013 \end{aligned}$ | $\begin{gathered} \text { Lattice } \\ 2013 \end{gathered}$ | $\begin{gathered} \delta \mathrm{P} \\ 2018 \end{gathered}$ | $\begin{gathered} \text { Corroboration } \\ 2018 \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: |
| $m_{c}$ | $\begin{gathered} 1.275(25) \\ \mathrm{GeV} \end{gathered}$ | $\begin{gathered} 1.273(6) \\ \mathrm{GeV} \end{gathered}$ | $\begin{gathered} 0.004 \\ \mathrm{GeV} \end{gathered}$ | Many lattice calculations of the charm moments will exist with completely independent uncertainties. |
| $\alpha_{s}$ | 0.1184(7) | 0.1184(6) | 0.0004 | Many lattice calculations of the charm moments will exist with completely independent uncertainties. <br> Many different lattice determinations using different quantities will exist with precisions approaching this value and completely independent uncertainties. |
| $m_{b}$ | $4.18(3)$ $\mathrm{GeV}$ | $\begin{gathered} 4.164(23) \\ \mathrm{GeV} \end{gathered}$ | $\begin{gathered} 0.011 \\ \mathrm{GeV} \end{gathered}$ | Lattice result and the most precise e+e- results will agree (?) within stated precisions, with completely independent uncertainties. |

## Conclusion

- Lattice calculations now provide the most precise determinations of $\alpha_{s}$ and $m_{c}$. They soon will also provide the most precise determination of $m_{b}$.
- People who wish to really be serious about understanding the partial widths of the Higgs will have to try to understand them


## Backup slides

## Perturbative coefficients for moments

TABLE III. Perturbation theory coefficients $\left(n_{f}=3\right)$ for $r_{n}$ [2-6]. Coefficients are defined by $r_{n}=1+\sum_{j=1} r_{n j} \alpha_{\overline{\mathrm{MS}}}^{j}(\mu)$ for $\mu=m_{h}(\mu)$. The third-order coefficients are exact for $4 \leq n \leq$ 10. The other coefficients are based upon estimates; we assign conservative errors to these.

| $n$ | $r_{n 1}$ | $r_{n 2}$ | $r_{n 3}$ |
| :--- | ---: | ---: | ---: |
| 4 | 0.7427 | -0.0577 | 0.0591 |
| 6 | 0.6160 | 0.4767 | -0.0527 |
| 8 | 0.3164 | 0.3446 | 0.0634 |
| 10 | 0.1861 | 0.2696 | 0.1238 |
| 12 | 0.1081 | 0.2130 | $0.1(3)$ |
| 14 | 0.0544 | 0.1674 | $0.1(3)$ |
| 16 | 0.0146 | 0.1293 | $0.1(3)$ |
| 18 | -0.0165 | 0.0965 | $0.1(3)$ |

HPQCD take uncalculated coefficients in series for moments $r_{n j} \sim \mathrm{O}\left(0.5 \alpha_{s}\left(m_{q}\right)\right)^{i}$;
further constrain the possible sizes for coefficients by comparing nonperturbative results for many quark masses with perturbation theory using Baysian priors for higher order terms.

