



# HIGGS SELF COUPLING ANALYSIS USING THE EVENTS CONTAINING $H \rightarrow WW^*$ DECAY

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# INTRODUCTION

- Measuring the Higgs self coupling is the key point to prove the electroweak symmetry breaking mechanism
  - Higgs potential in SM:

$$V = \lambda v^2 H^2 + \lambda v H^3 + \frac{1}{4} \lambda H^4$$

Mass term

Trilinear coupling

Quartic coupling

→ difficult to measure

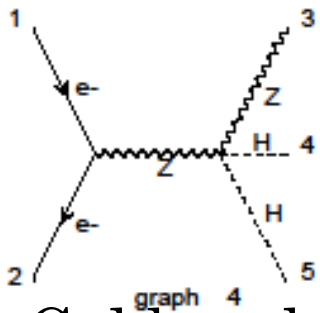
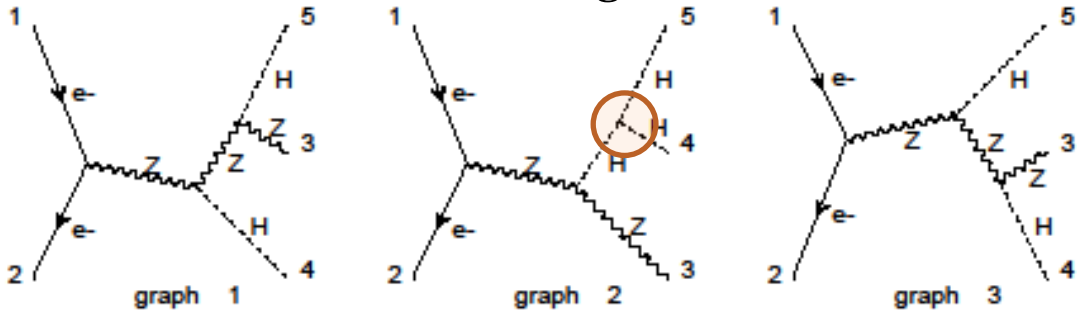
$$SM: \lambda = \frac{m_H^2}{2v^2} \quad v \sim 246 GeV$$

- Observing two Higgs bosons in the event is the only way to measure the self coupling
- Accurate test of the coupling may lead to the extended nature of Higgs sector → may go to new physics
- Our goal is to observe and measure the Higgs self coupling first

# SIGNAL EVENTS

Signal:  $e^+e^- \rightarrow Z^* \rightarrow ZH \rightarrow ZHH$  is used for the analysis

- Cross section is largest @ 500 GeV for the self coupling analysis



Signal: 2  
Irreducible B.G.: 1, 3, 4

Golden channel:  $Z(bb)(bb)$

- b-tagging is important

Requirement of  $H \rightarrow WW^*$  decay

- Contribution of the total sensitivity
- Need to reduce the backgrounds using kinematics of the events

		H1		
H2	Br	bb		WW
	bb			
	WW			

# BACKGROUNDS AND SIMULATION

## ○ Backgrounds considered:

B.G. Process	Feature	Basic idea for rejection
<b>ttbar</b> <b>ZWW</b>	Huge number of events	Flavor tagging Kinematics topology Difference of the final states
<b>ttbar + X</b>	b-jet rich in the final states Similar final states	Kinematics topology
<b>Triple boson</b> • ZZ + H • ZZZ	Small cross section b-jet rich in the final states	Kinematics topology Difference of the final states

- S/B ~ 1/3000

## ○ Simulation

- Polarization: (e, p)=(-0.8, +0.3)
- Higgs mass is set @125GeV/c<sup>2</sup>
- Using the full simulation with DBD detector configuration

process	$\sigma(\text{fb})$
Signal(inclusive)	0.2
ttbar & ZWW	581.8
ttbar + QQ	0.83
ttbar + Z	0.98
ttbar + H	0.14
ZZ + H	0.77
ZZZ	1.83

# ANALYSIS STRATEGY FOR $HH \rightarrow (BB)(WW)$

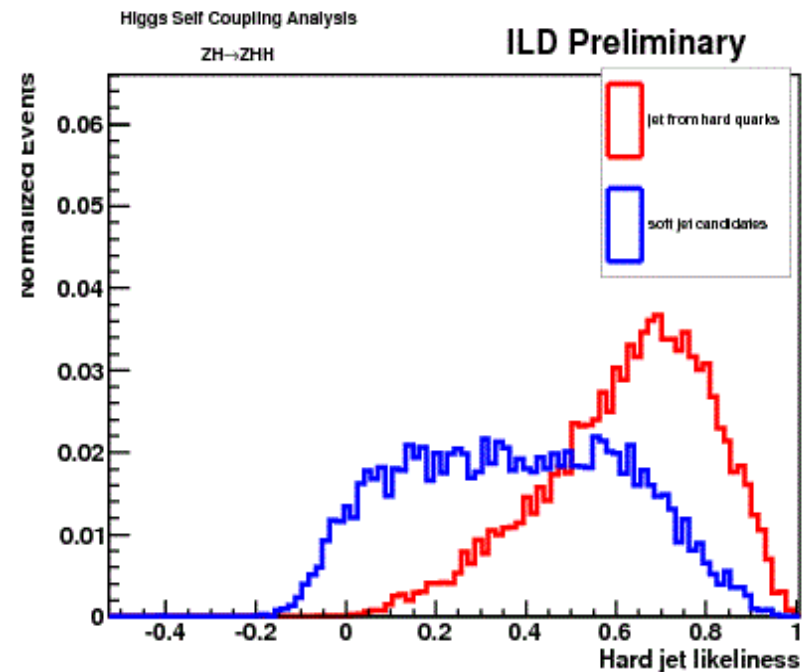
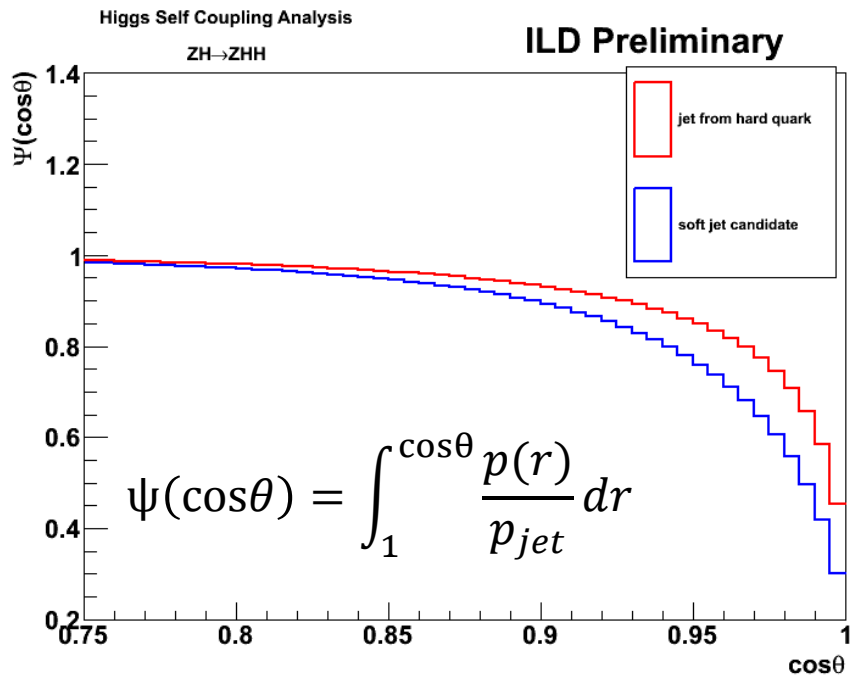
- Classify the events with Z and W decays:

	$WW \rightarrow (qq)(qq)$	$WW \rightarrow (qq)(lv)$
$Z \rightarrow bb$	8jets	Lepton+6jets
$Z \rightarrow cc$	8jets	Lepton+6jets
$Z \rightarrow ll$	Dilepton+6jets	Trilepton+4jets

- **Z decays into heavy flavor pair or lepton pair mainly**
  - Need flavor tagger or clean Z mass distribution to reject huge backgrounds
- **Number of b jet candidates in the event and number of leptons can form exclusive samples**
  - Number of b-tagging available: up to 4
    - Basically, 2 or 4 b-tagged jets events can be used
    - c-tagging is also available
  - Number of leptons: from 0 to 3

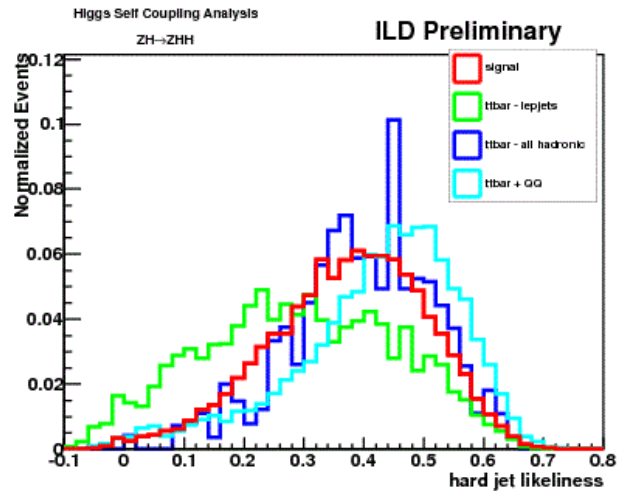
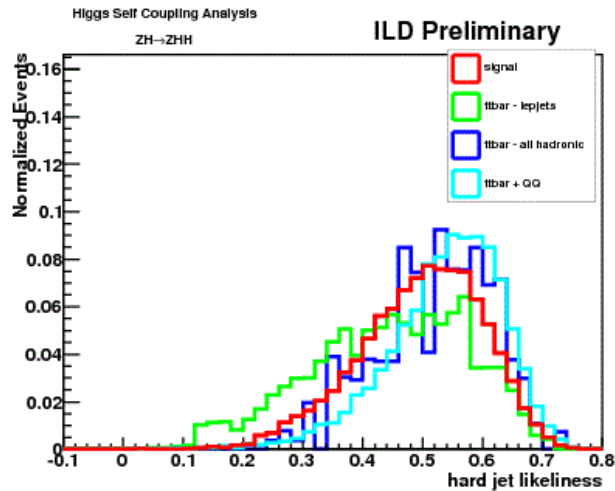
# SOFT JET FINDING

- Tracks in the gluon jets spread wider than those in quark jets(e.g. analyses on hadron collider)
  - Traditional jet shape can be a good estimator
- Using Multivariate Analysis and estimating the hard jet likeliness for each jet

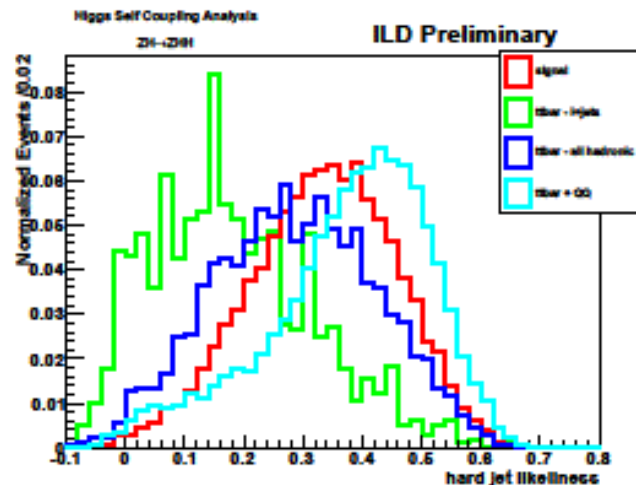
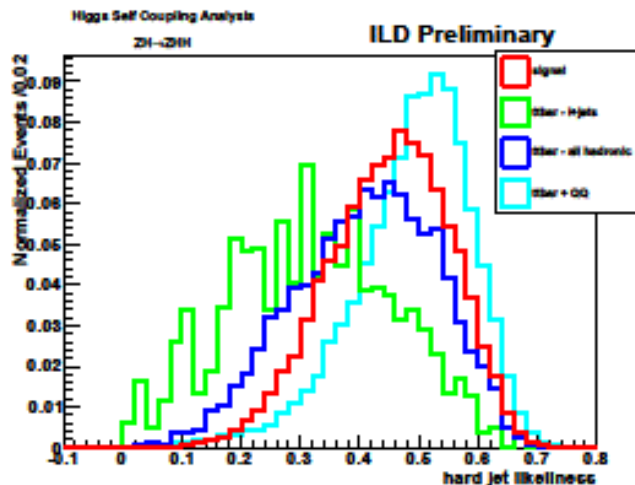


# CHECK THE PERFORMANCE

- Check the jets with small hard jet likelihood – signal vs.  $t\bar{t}$
- For 6jets



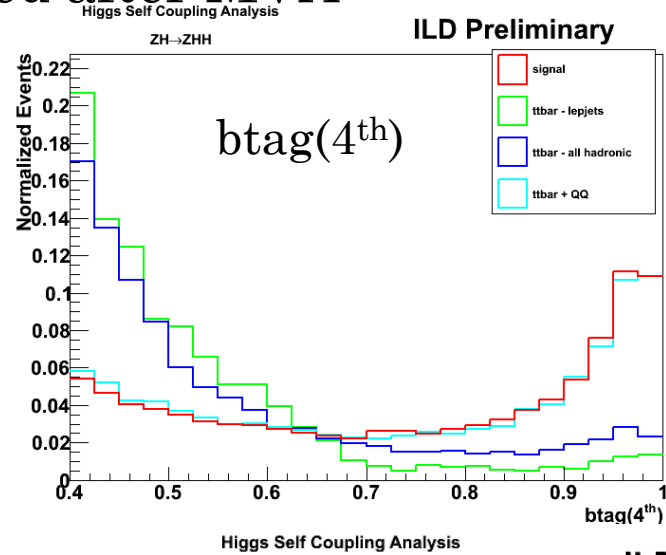
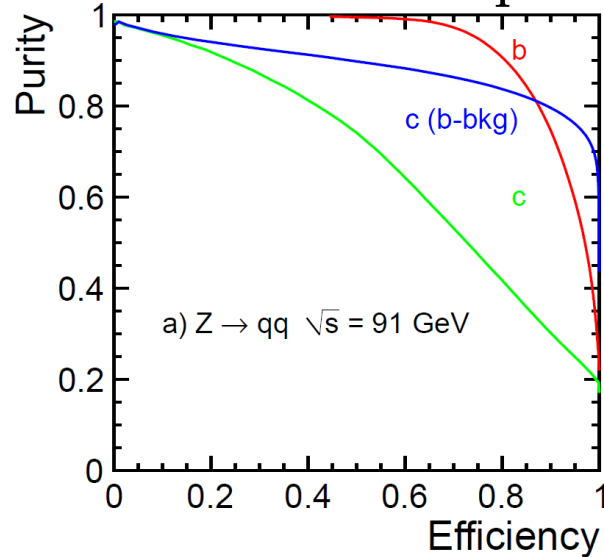
- For 8jets



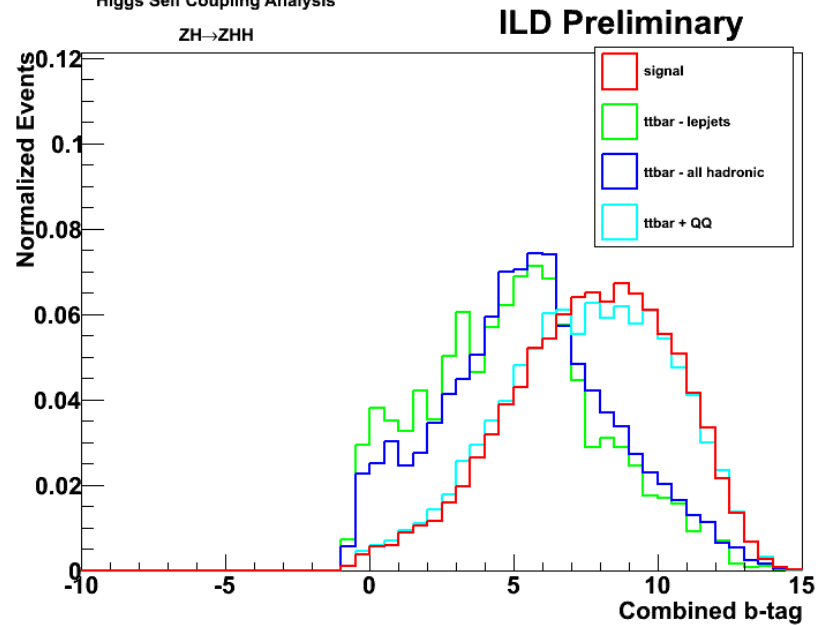
# FLAVOR TAGGING

## Using LCFIPlus

- b candidate is set  $>0.4$
- Final b-likeliness is optimized after MVA



- Introduce combined b-tagging
  - After solving the jet pairing
  - $b(\text{Combined}) = \frac{b_1 b_2}{(1-b_1)(1-b_2)}$
  - Use as an input variable for MVA

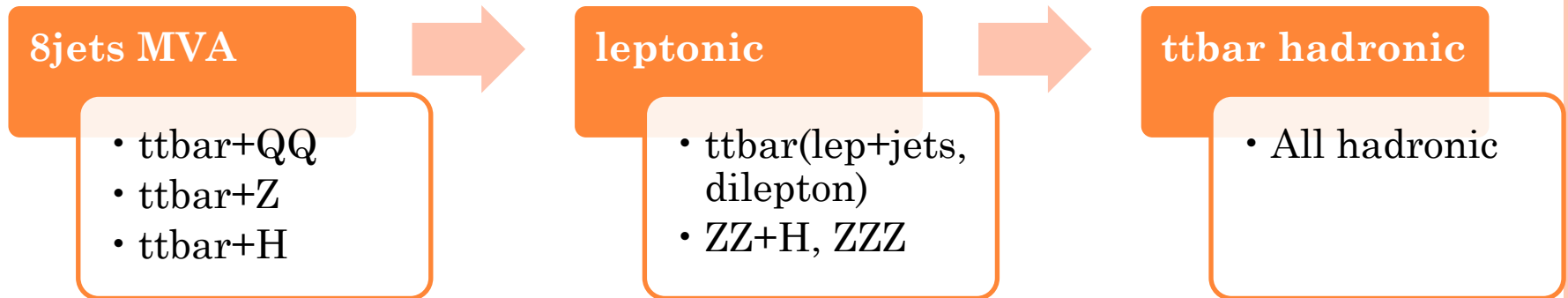




# BACKGROUND REJECTION

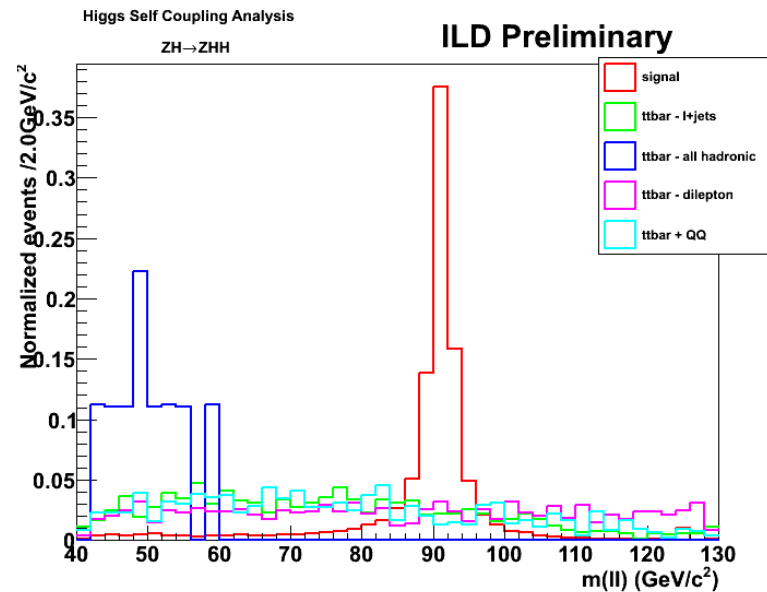
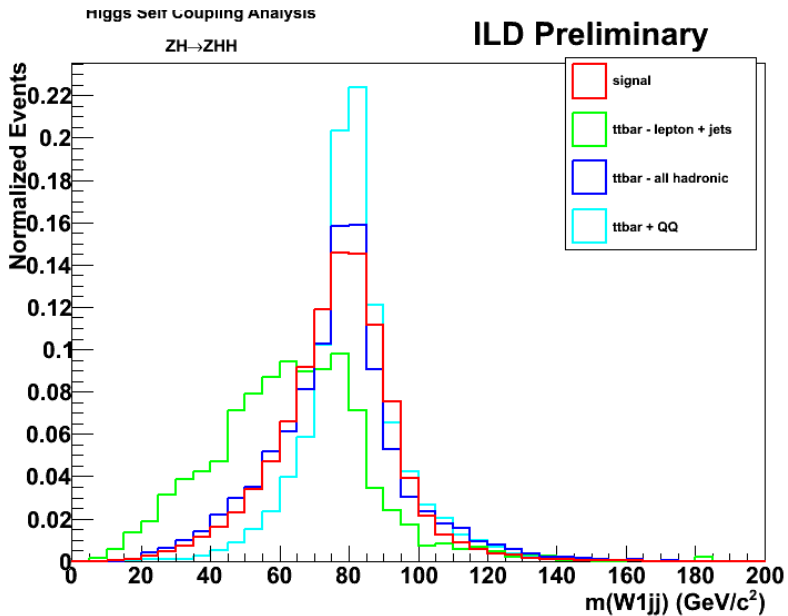
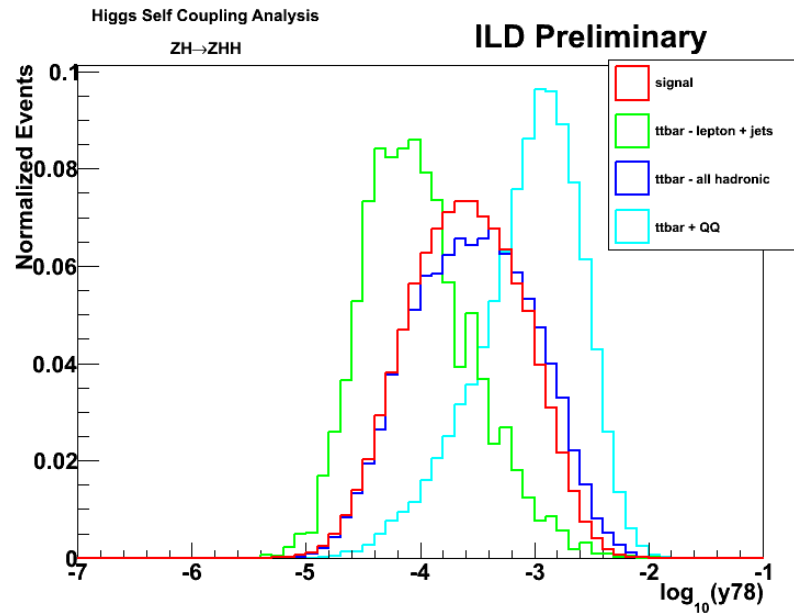
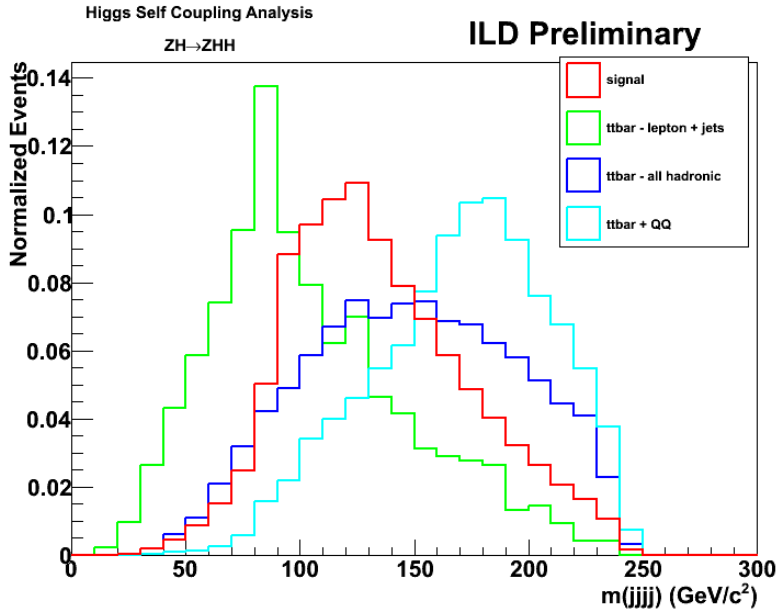
## Using Multi Variate Analysis

- Some cuts are implemented before MVA to tighten the input variable space – jet energy,  $\chi^2$ , visible energy, (Z mass)
- Background rejection strategy : rejecting small backgrounds first and then rejecting main background
  - Tighten the variable space when rejecting main backgrounds
- e.g. all hadronic case:



# SOME KINEMATIC VARIABLES USED FOR MVA

Very powerful variable:  $m(jjjj)$ ,  $m(lvjj)$



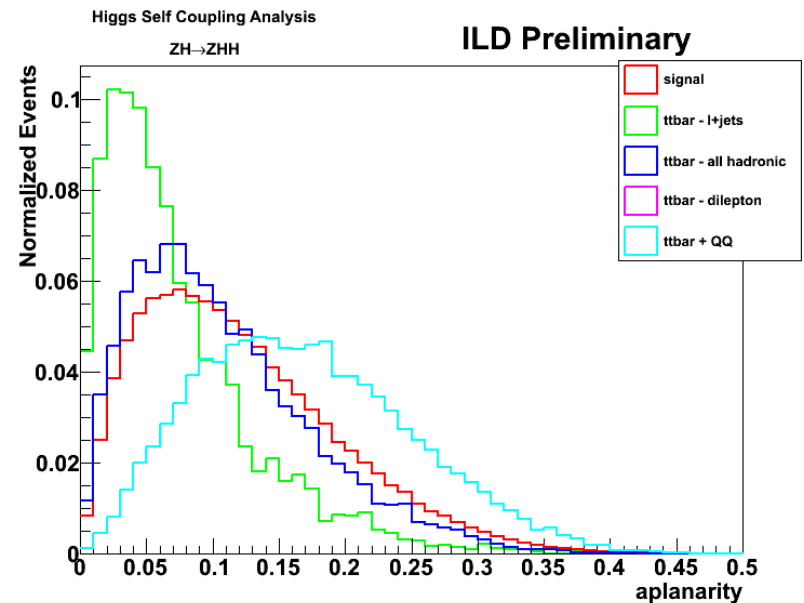
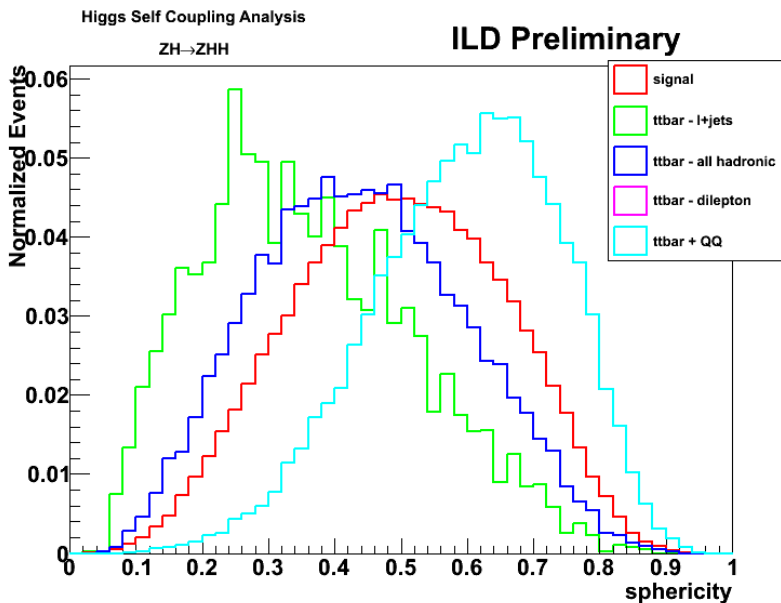
# NON-SIMPLE VARIABLES USED FOR MVA

## ○ Sphericity and aplanarity

- Eigenvalue combinations of sphericity tensor:

$$S^{\alpha\beta} = \frac{\sum_i p_i^\alpha p_i^\beta}{\sum_i |\mathbf{p}_i|^2}, \quad \text{eigenvalues: } \lambda_1 > \lambda_2 > \lambda_3$$

- Sphericity:  $S = \frac{3}{2}(\lambda_2 + \lambda_3)$
- Aplanarity:  $A = \frac{3}{2}\lambda_3$
- Indicates whether the event is 2-jets like or isotropic

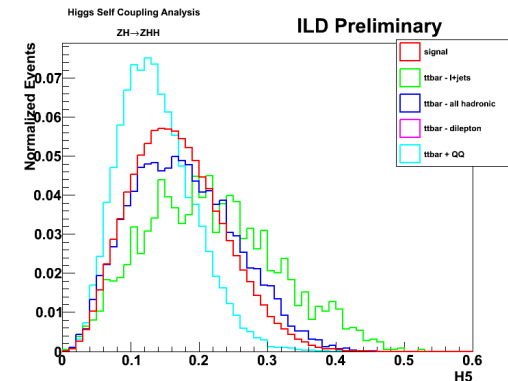
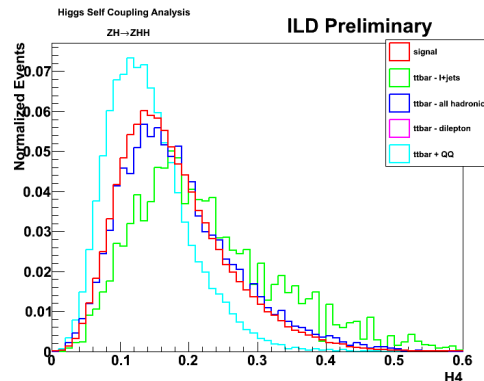
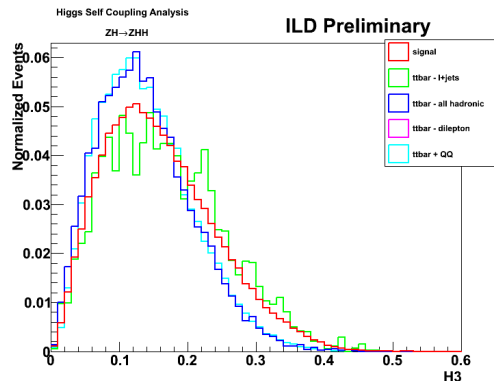
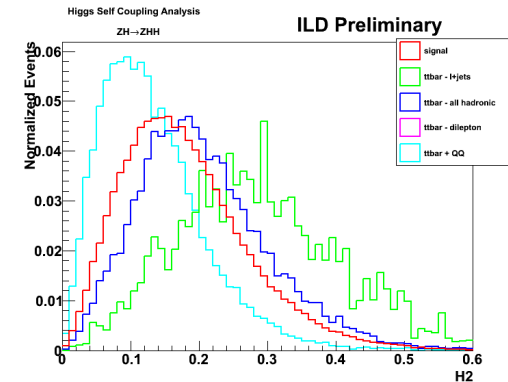
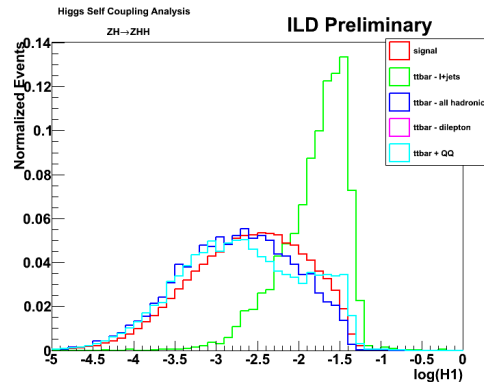
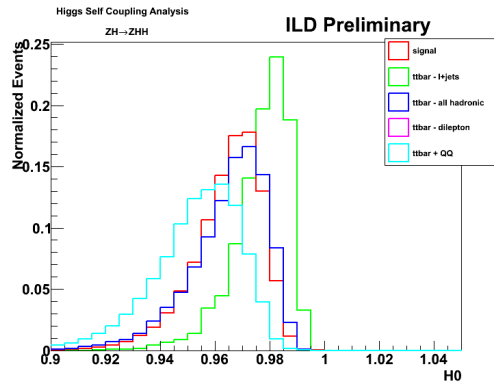


# NON-SIMPLE VARIABLES USED FOR MVA

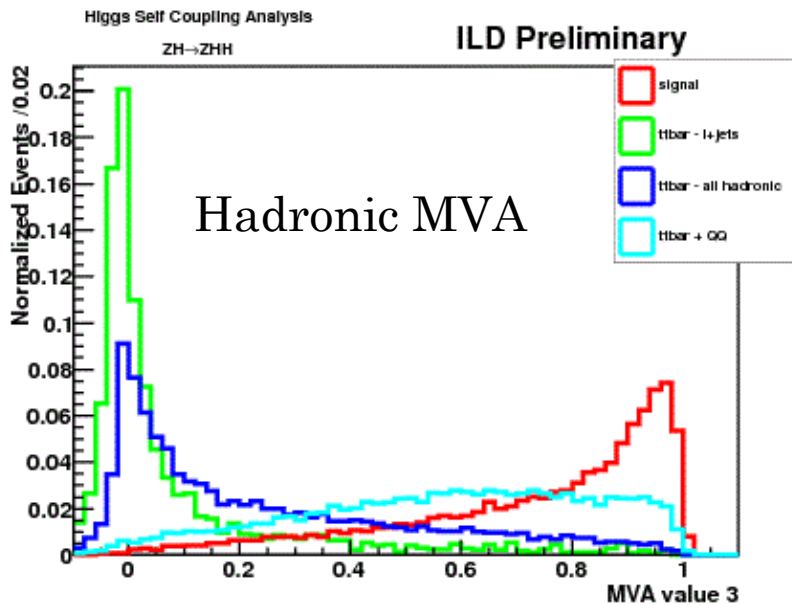
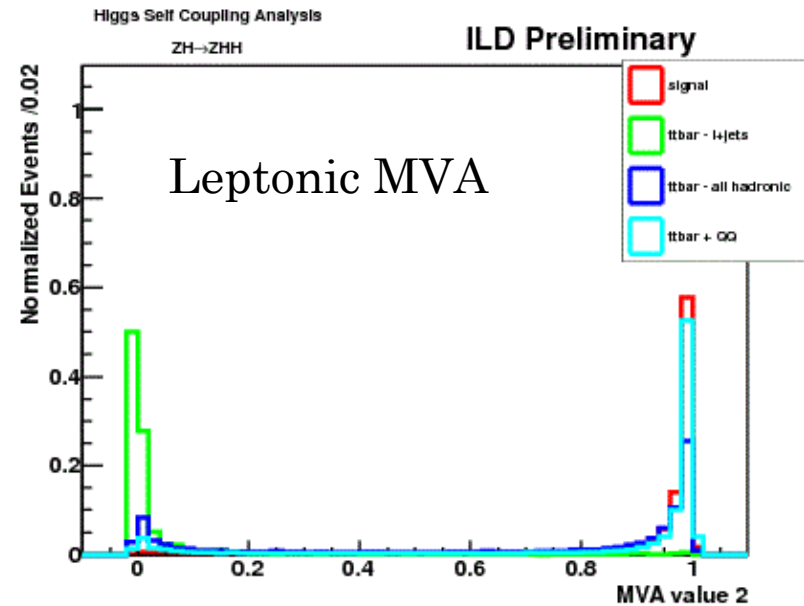
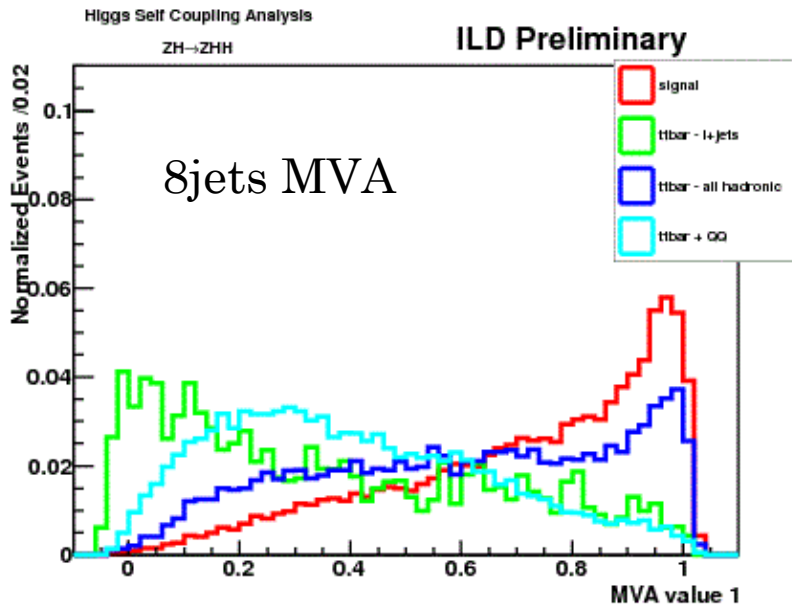
## ○ Fox-wolfram moments

$$H_l = \sum_{i,j} \frac{|\mathbf{p}_i| |\mathbf{p}_j|}{E_{\text{vis}}^2} P_l(\cos \theta_{ij}) ,$$

- $P_l$  is Legendre polynomials
- Those moments characterize the structures of 2jets, 3jets, or isotropic events



# MVA OUTPUTS EXAMPLES(ALLHADRONIC)



cut of MVA:  
 $MVA_{8jets} > 0.08$   
 $MVA_{lep} > 0.02$   
 $MVA_{had} > 0.74$

# SENSITIVITY

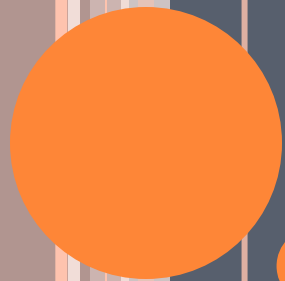
## ○ $HH \rightarrow (bb)(WW)$

- As mentioned, categorized with decay types of Z and W boson
  - $Z \rightarrow bb, cc$  or  $ll$
- b-tagging strategy – introduce looser b-tag category
  - 4-btag & 3-btag
- $E_{CM} = 500 \text{ GeV}$ ,  $L = 2 \text{ ab}^{-1}$
- **Significance  $\sim 1.91\sigma$**

Modes	Z decay	b tag	Signal	Background	Significance
All hadronic	$Z \rightarrow bb$	4btag	15.20	87.52	$1.50\sigma$
		3btag	19.43	3099.49	$0.35\sigma$
	$Z \rightarrow cc$		11.29	366.13	$0.58\sigma$
Lepton + jets	$Z \rightarrow bb$		1.65	17.62	$0.38\sigma$
	$Z \rightarrow cc$		1.50	819.61	$0.05\sigma$
Dilepton	$Z \rightarrow ll$		2.24	8.44	$0.69\sigma$
Trilepton	$Z \rightarrow ll$		1.05	2.60	$0.55\sigma$
Combined					<b><math>1.91\sigma</math></b>

# SUMMARY AND PLAN

- Higgs self coupling analysis using the events with  $H \rightarrow WW^*$  is ongoing.
  - Multi variate analysis to reject the backgrounds
  - Total sensitivity is  $\sim 1.91\sigma$
- **Plan:**
  - Optimize b-tagging strategy
    - Fewer number of b-tagging sample
  - Analysis@1TeV
  - Improvement of basic components for the analysis
    - Lepton ID
    - b-tagging
    - Jet energy resolution
    - Jet clustering



# BACKUPS



# EVENT SELECTION

## ○ Lepton selection

- Lepton ID: The isolated lepton coming from the primary vertex

lepton	electron	muon
cut	$0.65 < E/p < 1.25$ $E(\text{EM}) / (E(\text{EM}) + E(\text{HAD})) > 0.90$ $ d_0  < 0.02$ $ z_0  < 0.02$ Cone Energy $< 61.10 - 0.28P$	$E/p < \min(0.5, 10.0/E)$ $E(\text{EM}) / (E(\text{EM}) + E(\text{HAD})) < 0.45$ $ d_0  < 0.02$ $ z_0  < 0.02$ Cone Energy $< 52.45 - 0.28P$

- Detection efficiency of Lepton ID  $\sim 98.4\%$  for lep+jets signal events

	Signal	ttbar – lep+jets	ttbar - allhad
Efficiency(%)	98.4	71.4	7.9

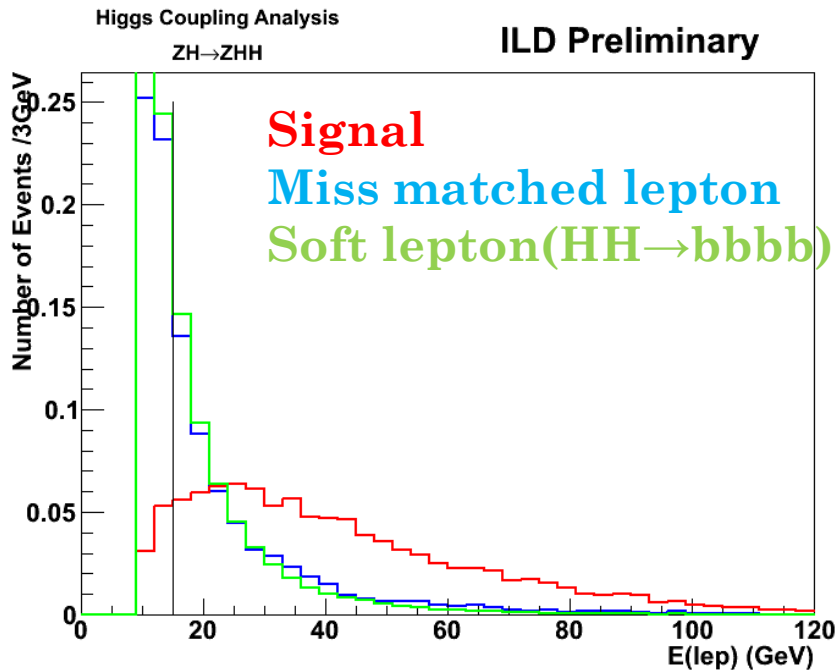
- For dilepton events  $\sim 83.8\%$  of signal events

	Signal	ttbar – dilepton
Efficiency(%)	83.8	84.5

# EVENT SELECTION

## ○ Lepton selection

- $E(\text{lep}) > 15\text{GeV}$  is required to suppress soft leptons
- Dividing into 3 samples:
  - one lepton for **lepton + jets**
  - two leptons for **dilepton** → opposite charge & same flavor
  - three leptons for **trilepton** → looking for the lepton pair from Z
  - tight lepton veto for **all hadronic**



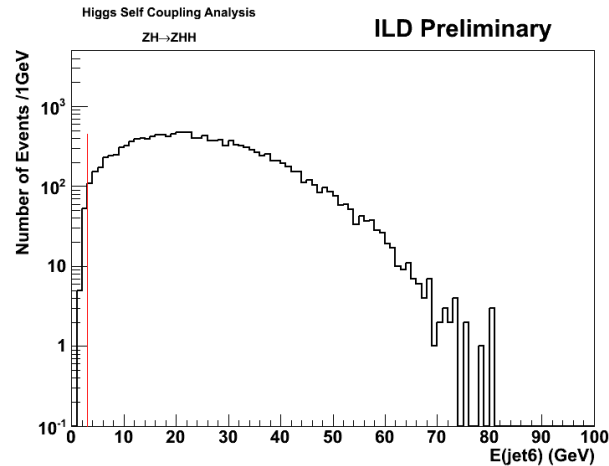
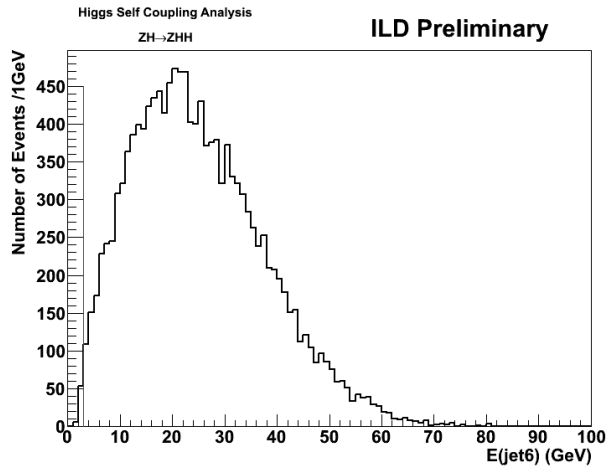
Lepton matching is required:  
 $\cos\theta > 0.9$

# EVENT SELECTION

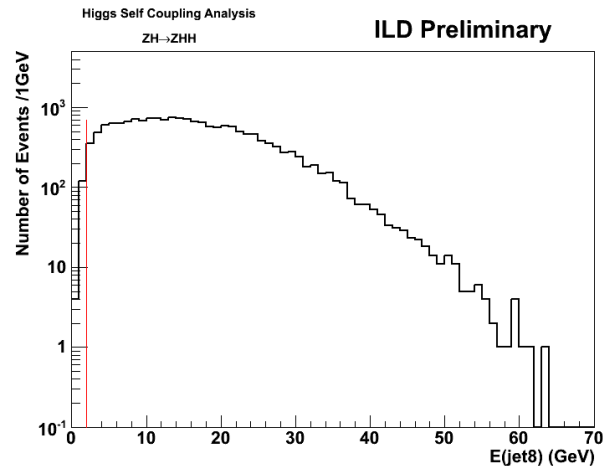
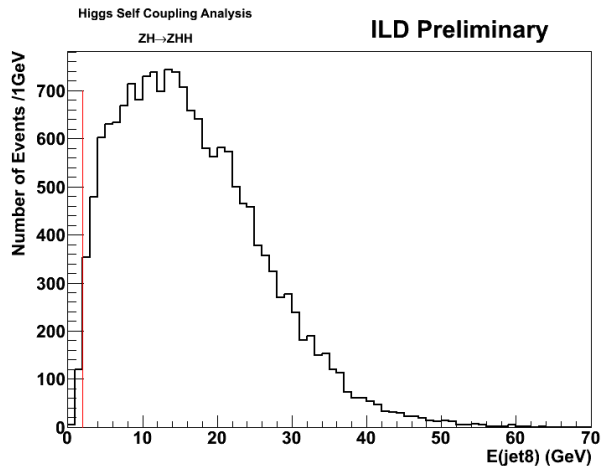
## ○ jet selection

- requiring 4jets, 6 jets or 8 jets using LCFIPlus & Durham
- $E(\text{jet}) > 3\text{GeV}$  is required to care the lowest energy jet for **6 jets** case

•



- $E(\text{jet}) > 2\text{GeV}$  is required to care the lowest energy jet for **8 jets** case



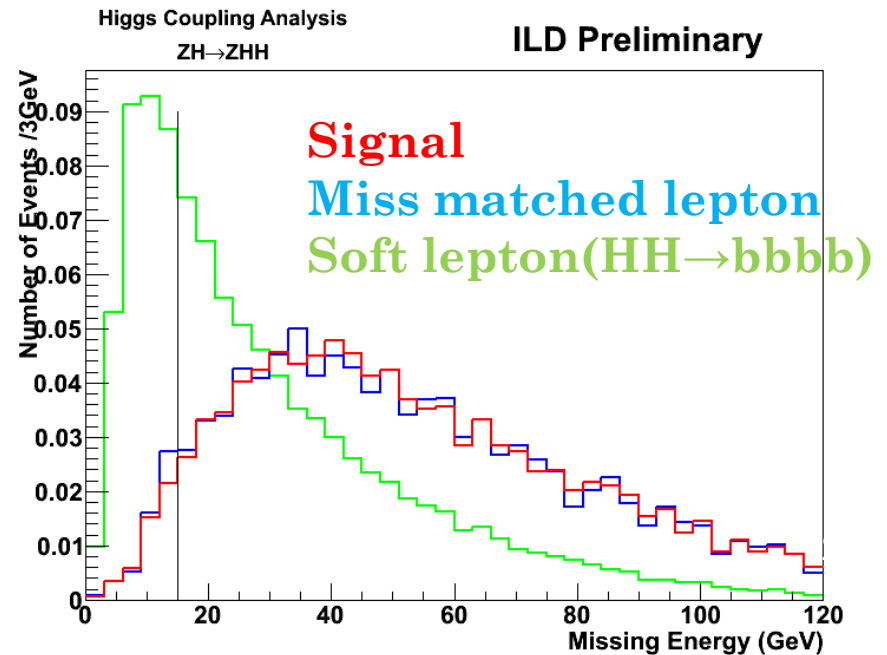
# EVENT SELECTION

- Detection efficiency after the jet energy cut:

signal	4jets requirement	6jets requirement	8jets requirement
Efficiency(%)	99.0	99.4	99.6

- Missing momentum

- **lepton + jets**:  $P(\text{Miss}) > 15 \text{ GeV}/c$  to suppress  $\text{HH} \rightarrow \text{bbbb}$  events
- **All hadronic & dilepton**:  $P(\text{Miss}) < 80 \text{ GeV}/c$  required
- **Trilepton**:  $P(\text{Miss}) < 150 \text{ GeV}/c$  to gain the acceptance



# EVENT SELECTION & MAKING SAMPLES

## ○ preselection

- lepton selection – looking for isolated leptons
  - Electron and muon from primary vertex
  - Lepton energy cut –  $E > 15 \text{ GeV}$  to reject soft leptons
  - **Divide into orthogonal samples based on the lepton number in the events**
    - From 0 to 3
    - For 2 and 3 lepton samples, looking for a lepton pair from Z boson
- Jet selection – jet clustering
  - Require proper number of jets for each sample – 4, 6, or 8 jets
  - Minimum jet energy cut is required to reject trivial backgrounds

	4jets	6jets	8jets
Min. Energy(GeV)	1.0	3.0	2.0

- $b$  likeliness  $> 0.4$  is required for  $b$  jet candidates
- Missing momentum

Category(Lep. Num.)	0	1	2	3
P(Miss) (GeV/c)	$P < 80$	$P > 15$	$P < 80$	$P < 150$

# SOLVING THE COMBINATION OF JETS

- Jets should be assigned to their parent particles correctly to obtain good kinematic variables

- **Jet pairing is based on the  $\chi^2$  technique**

- b jet assignment to Higgs and Z boson:

$$\chi^2 = \frac{(m_1 - m_Z)^2}{\sigma_Z^2} + \frac{(m_2 - m_H)^2}{\sigma_H^2}$$

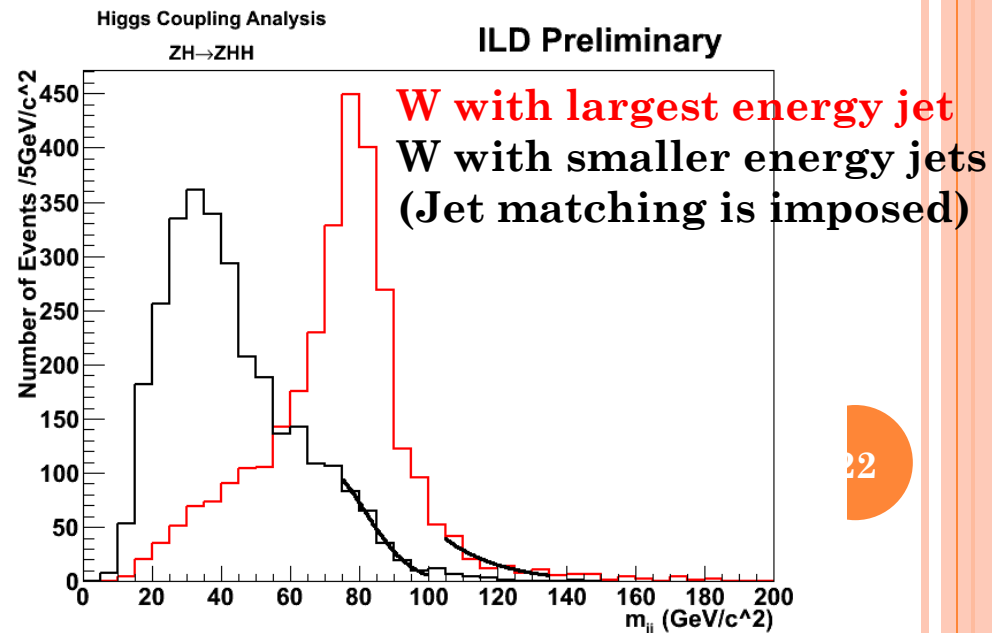
- Light flavor jet assignment to 2 W bosons:

- Mass constraint is imposed only to the W boson with largest energy jets

- Breit-Wigner is assumed

for W mass shape

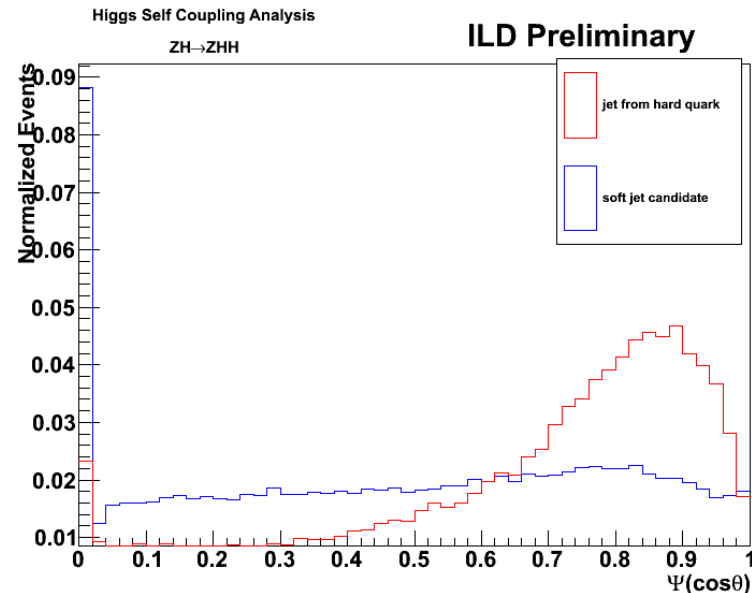
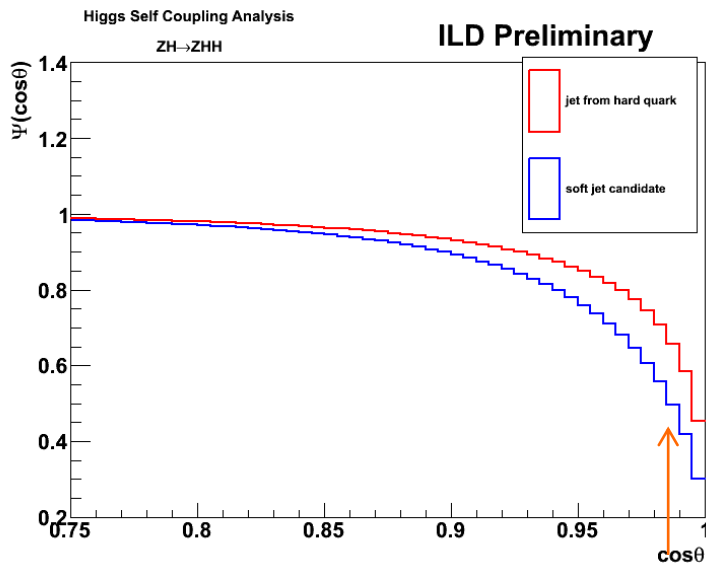
- $\chi^2 = -2\text{Log}(\text{BW}(m_{W1}|m_W, \Gamma_W))$



# SOFT JET FINDING

- Soft jet finding may be available for the events with extra jets not coming from hard process quarks
  - e.g. 8 jets requirement to  $t\bar{t}$  hadronic events (6 jets from hard quarks)
- Traditional jet shape indicates the same tendency as hadron collider analysis

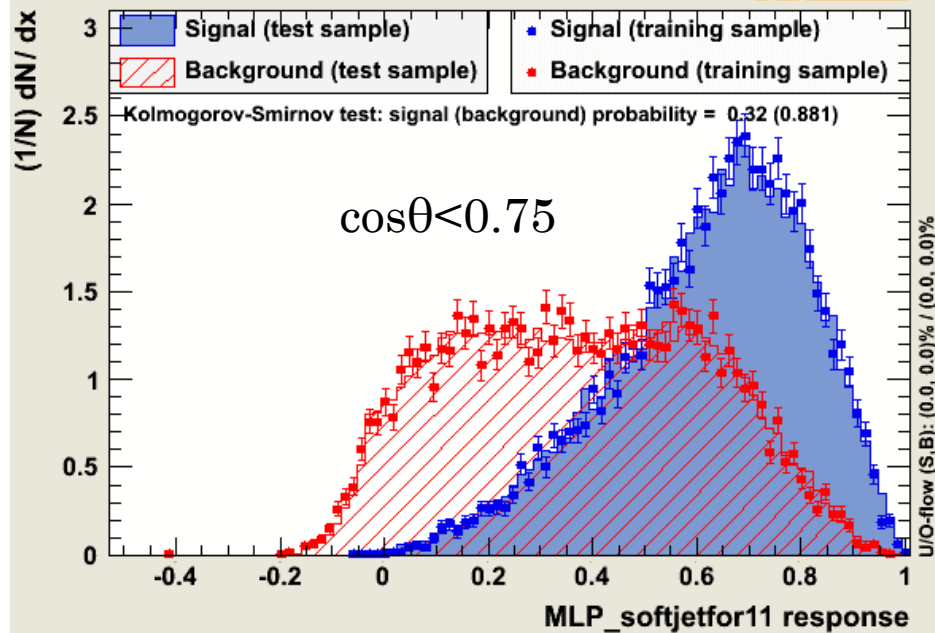
$$\psi(\cos\theta) = \int_1^{\cos\theta} \frac{p(r)}{p_{jet}} dr$$



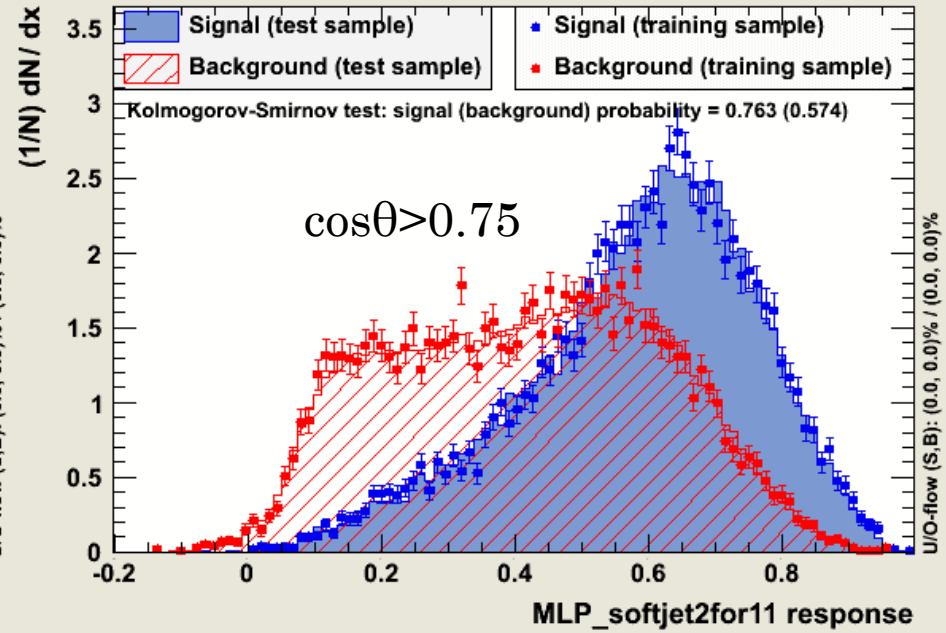
# SOFT JET FINDING

- Hard jet likeliness is introduced
  - Using MVA to form it
  - Analysis samples are divided into 2 based on the angle with the nearest jet
    - large shared area for both jets deteriorate the traditional jet shape
- Use the likeliness for the input of background rejection MVA or simple cut of backgrounds

TMVA overtraining check for classifier: MLP\_softjetfor11



TMVA overtraining check for classifier: MLP\_softjet2for11





# REDUCTION TABLE

## All hadronic

- Final b-tagging:  $\text{btag}(3) > 0.92$  &&  $\text{btag}(4) > 0.44$
- $\text{HH} \rightarrow \text{bbbb}$  contamination is 5.41 events

process	signal	ttbar	tt + QQ	tt+Z	tt + H	ZZ + H	ZZZ
expected	354.00	$1.16 \times 10^6$	1660.00	3307.00	280.00	1540.00	3660.00
preselection	49.47	2462.09	79.11	76.25	38.32	87.22	70.72
Jet energy	47.92	1970.58	77.62	74.98	37.96	72.88	57.28
$\chi^2$	44.32	1353.38	64.57	62.41	34.02	61.60	48.16
Visible energy	44.23	1326.19	64.31	62.00	33.92	61.18	47.90
NN for 8 jets	36.51	1011.92	36.37	34.37	16.38	51.59	47.90
NN for ttbar	20.53 (9.85)	302.59	26.44	25.17	13.07	21.71	9.00
b-tagging	14.92 (5.41)	87.54	17.54	16.42	9.13	16.10	6.03