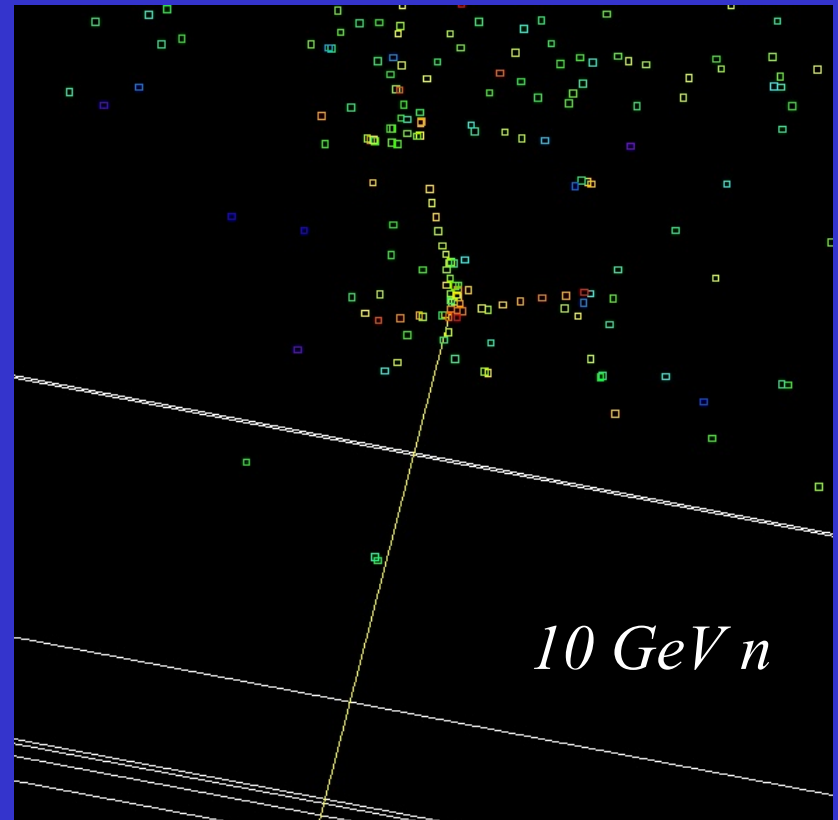
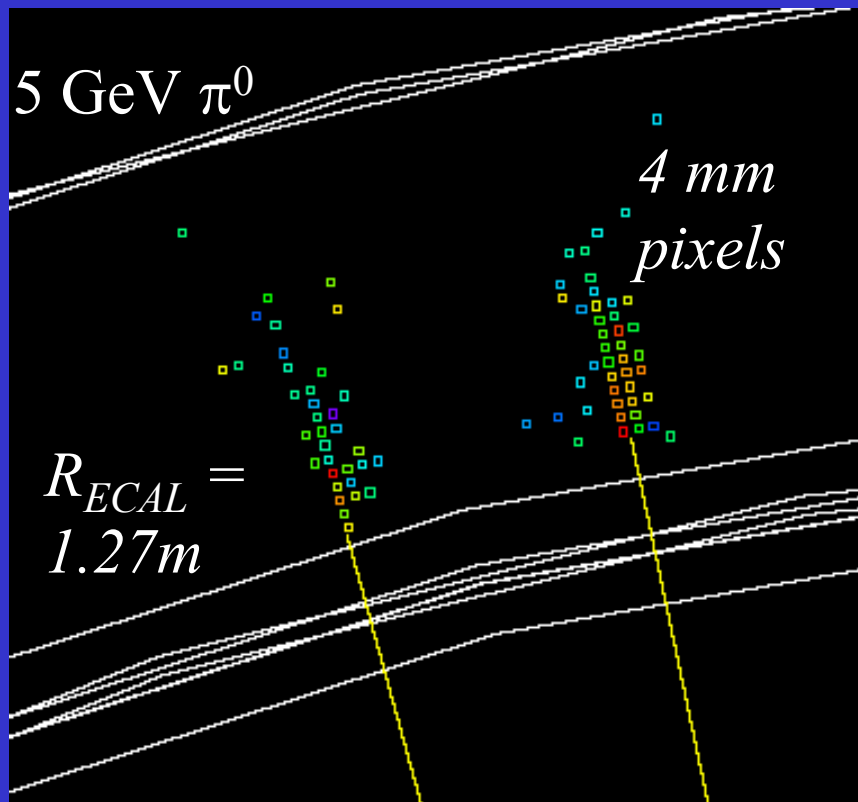


# Impact of $\pi^0$ Reconstruction on PFA and Neutral-hadron TOF possibilities



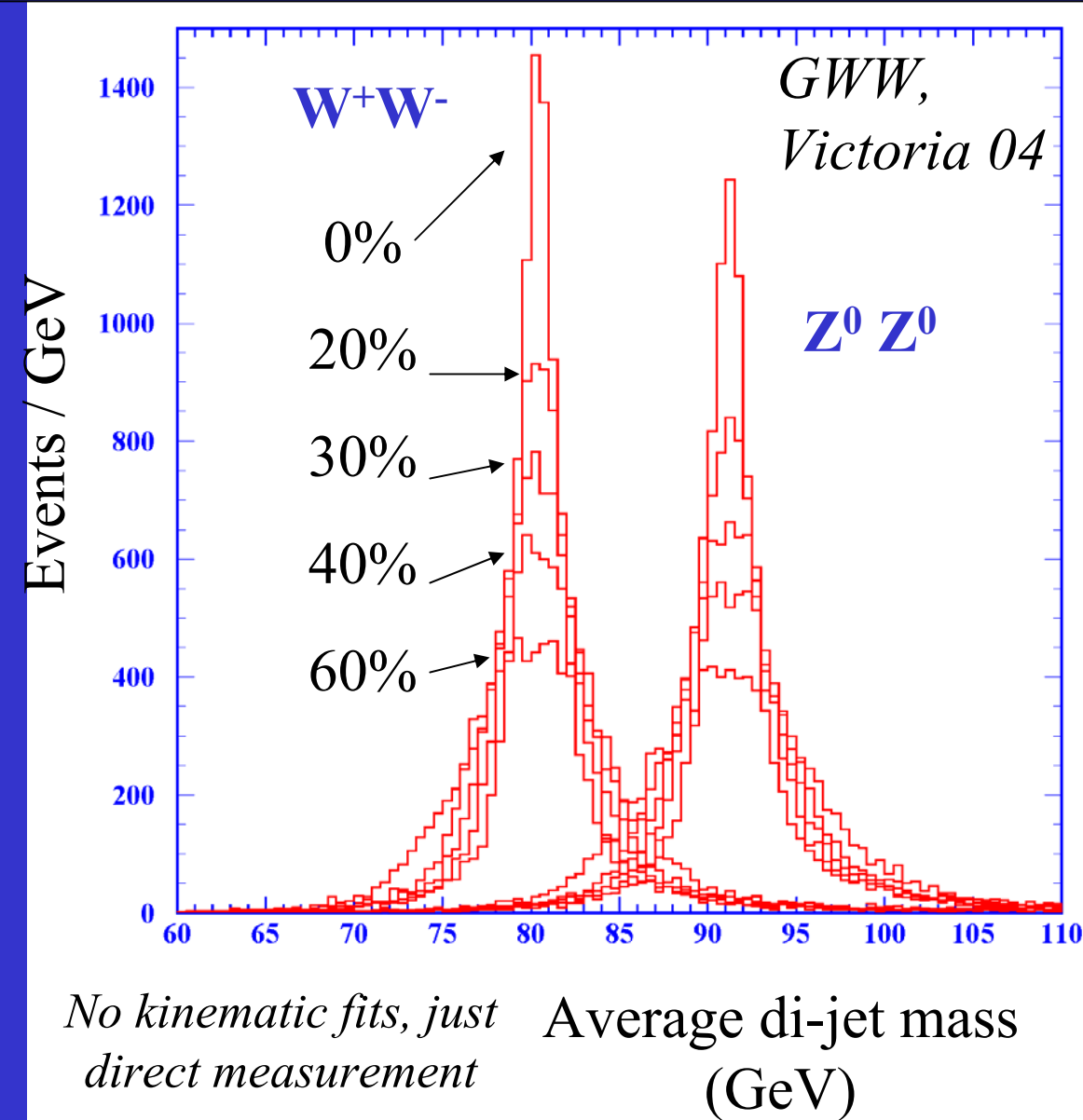
Graham W. Wilson, University of Kansas

*LCWS07, Sim/reco session DESY Hamburg, June 2007*

# Outline

- Big picture on jet energy resolution potential
- Big detector
- Fast-timing ideas
- Applying  $\pi^0$  mass constraint to hadronic events.

# Di-jet mass distribution vs $E_{\text{jet}}$ resolution



Comparing  $e^+e^- \rightarrow WW$   
and

$e^+e^- \rightarrow ZZ$  at  $\sqrt{s}=300$  GeV  
 $\langle E_{\text{jet}} \rangle = 75$  GeV  
 (hadronic decays only,  
 assume  $WW:ZZ = 1:1$   
 for illustration)

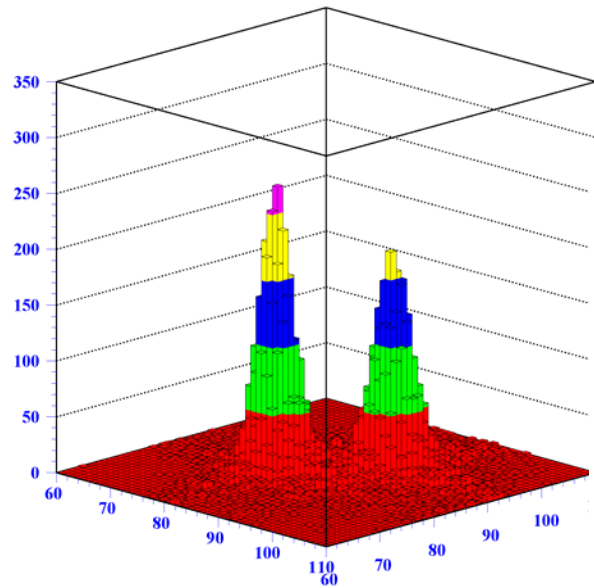
*Reality = 7:1 !*

$$\sigma(E_{\text{jet}}) =$$

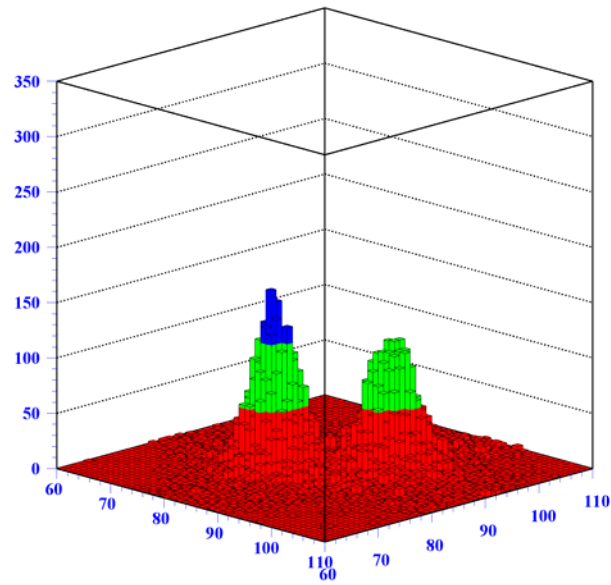
$$xx\% \sqrt{E_{\text{jet}}}(\text{GeV})$$

**$30\% \sqrt{E_{\text{jet}}}$  is a good target.**  
**Physics ( $\Gamma_w=2$  GeV) may**  
**demand even more !**

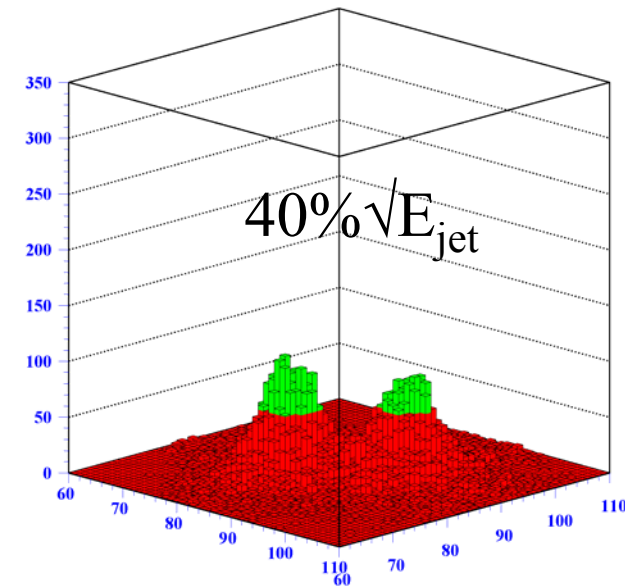
Wouldn't 20% be really something !



$20\% \sqrt{E_{\text{jet}}}$



$30\% \sqrt{E_{\text{jet}}}$



$40\% \sqrt{E_{\text{jet}}}$

# Example detector model which should be able to achieve the $\pi^0$ performance indicated here.

A radially staggered buildable analog calorimeter with exquisite granularity, with no cost optimization using Tungsten.  $B = 3T$ .

With M. Thomson.

Acknowledgements to N. Graf

*frankyaug05*

R(m) Nlayers X0 Active Cell-size (mm)

EM Barrel 1: 2.10 10 0.5 Si  $2.5 \times 2.5 \times 0.32$

EM Barrel 2: 2.13 10 0.5 Si  $10 \times 10 \times 0.32$

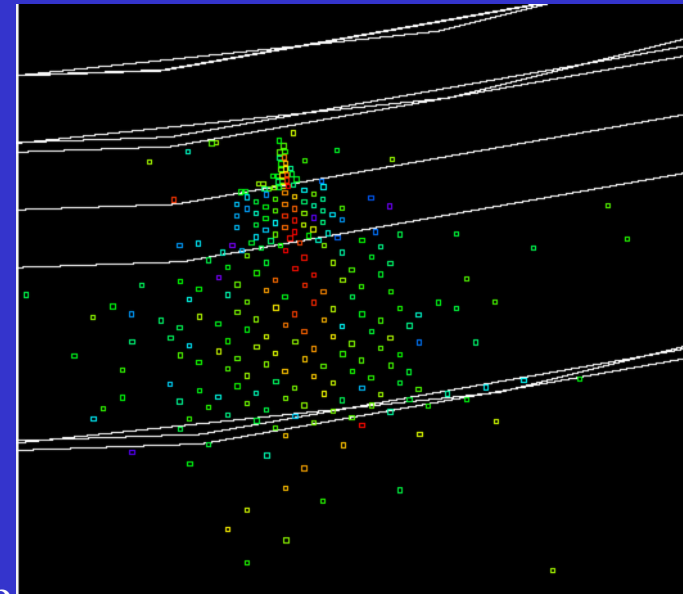
EM Barrel 3: 2.16 20 0.5 Sc  $20 \times 20 \times 2$

HCAL: 2.255 50 2.0 Sc  $40 \times 40 \times 2$

Choices made based on then current R&D work, driven by making a sensible, robust design with aggressive performance and minimizing Silicon area in a GLD-scale detector.

Expect:  $\sigma_E/E = 11\%/\sqrt{E}$  at low energy

(W was cheaper in 05..)

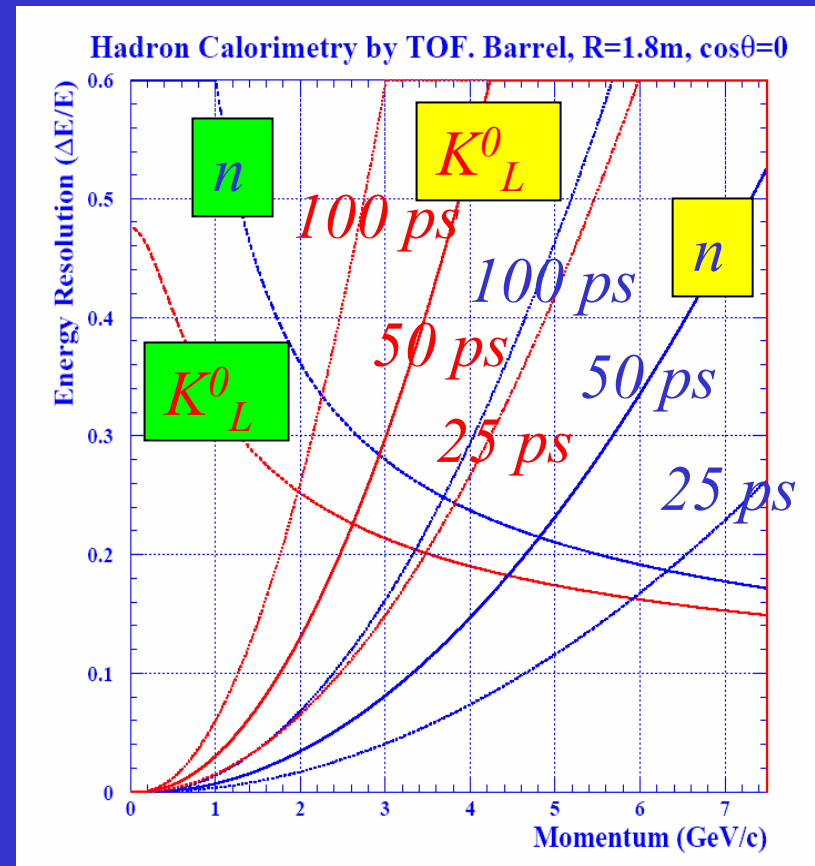
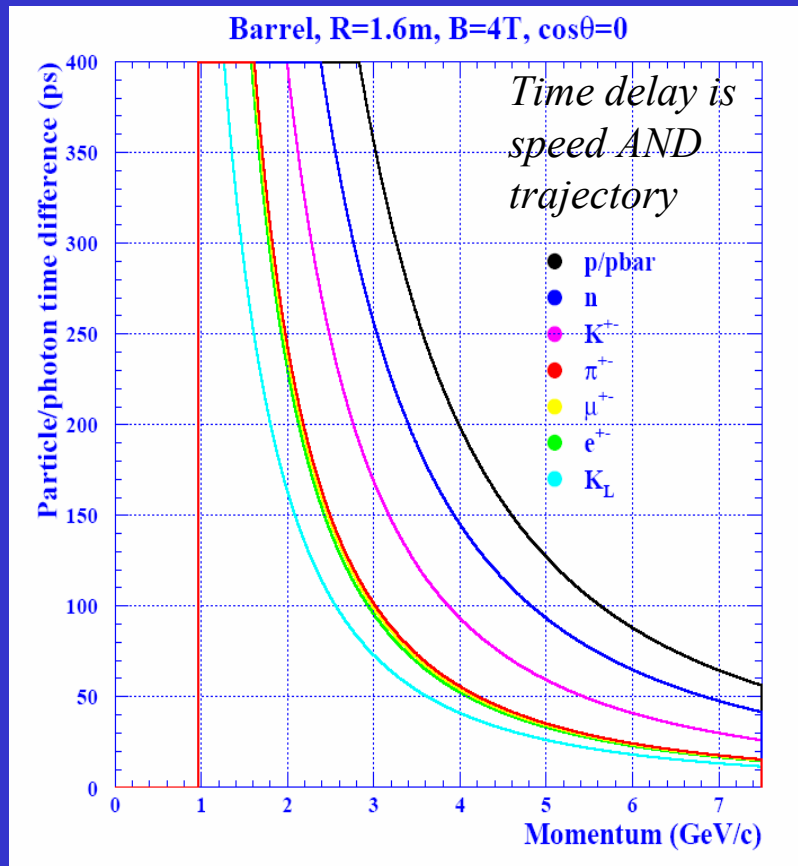


50 GeV photon

# Fast Timing / Temporal Calorimetry

*Idea: time resolution at below the 100 ps level is easily achievable with dedicated detectors. Can it be applied in a useful way in an ILC detector ?*

*Can TOF help measure neutral hadrons at low  $p$  ?*



*Can help resolving  $\gamma/\pi$ . (PID by TOF possible – but redundant with  $dE/dx$  in a TPC-based detector).*

*Resolve confusion.*

*HCAL (LDC DOD) TOF*

Interaction Picking Settings

Shape

Actions / Settings

Zoom into Region

Translate to Picked Object

☒ Pick while Moving/Dragging

Picked objects (0):

Type	Points	Code
------	--------	------

Attributes of picked object (0):

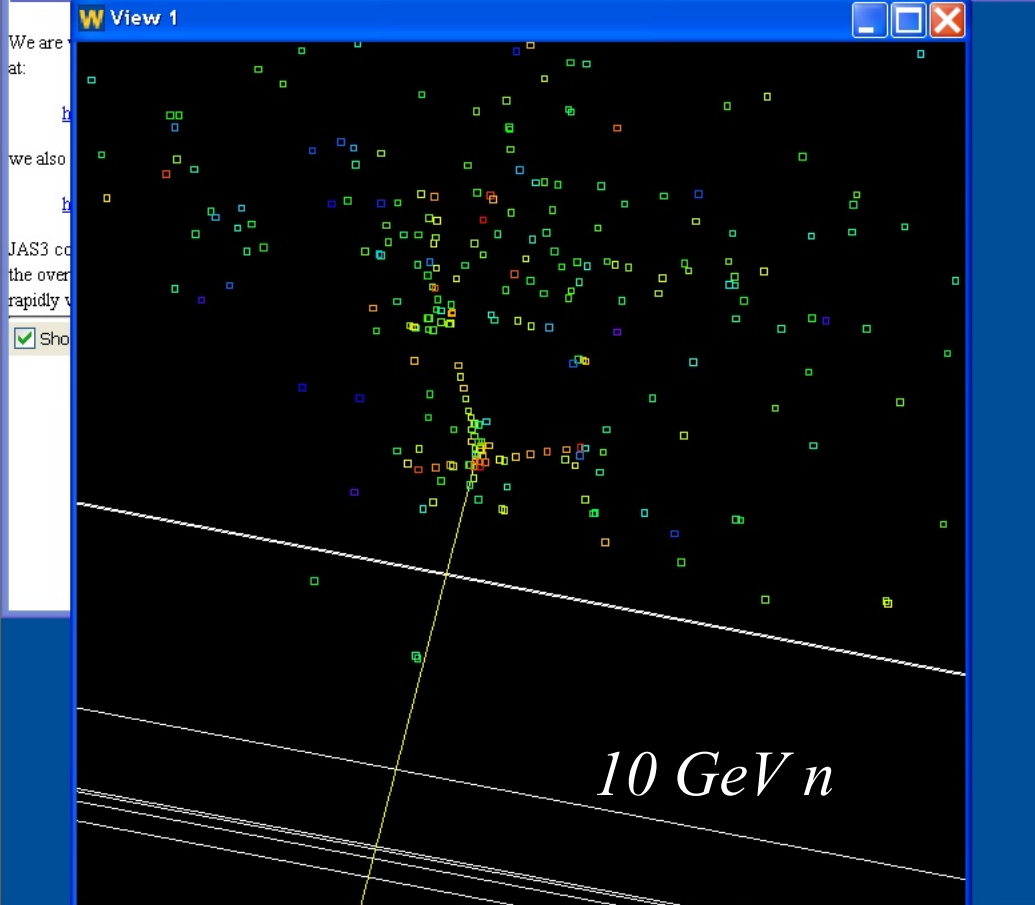
Name	Value	Unit	Node
------	-------	------	------

LCSim Event

Run:0 Event: 0

Collection: EcalBarrHits size:131 flags:e0000000

id: sy...	id: ...	id:...	id:...	id: z	raw en...	corrected e...	x (mm)	y (mm)	z (mm)	tim...
2	11	0	639	-1	.0010073	.063037	-174.51	1302.0	-1.7500	4.4064
2	11	0	639	0	.0011621	.072726	-174.51	1302.0	1.7500	4.4137
2	10	0	636	-1	7.0932E-4	.044391	-170.19	1298.9	-1.7500	4.4181
2	10	0	637	-1	.0013573	.084945	-173.66	1298.4	-1.7500	4.4183
2	11	0	639	1	.0011043	.069108	-174.51	1302.0	5.2500	4.4222
2	12	0	641	-1	2.6792E-4	.016767	-176.29	1305.5	-1.7500	4.4281
2	10	0	636	1	.0022967	.14373	-170.19	1298.9	5.2500	4.4442
2	13	0	643	-2	2.1419E-4	.013405	-177.14	1309.2	-5.2500	4.4499
2	12	0	642	-2	5.1488E-4	.032223	-179.76	1305.1	-5.2500	4.4520



# Possible Detectors ?

- State-of-the-art: MCP-PMT,  $\sigma_t = 5$  ps measured using Cerenkov light in 10mm quartz, K. Inami et al, NIM A 560 (2006) 303.
  - Also see emerging “fast-timing” initiatives. (Fritsch, LeDu)
- Cerenkov layers – also designed for C-based compensation.
- Ultra-fast scintillator pads with direct-coupled thin B-field tolerant photo-detectors tiled in a few layers through the calorimeter ??
  - Eg. quenched scintillators with FWHM of 400 ps per  $\gamma$ . (BC-422Q)
  - Will do time resolution studies with this.
- RPCs, Pestov
- Scintillating fibers.



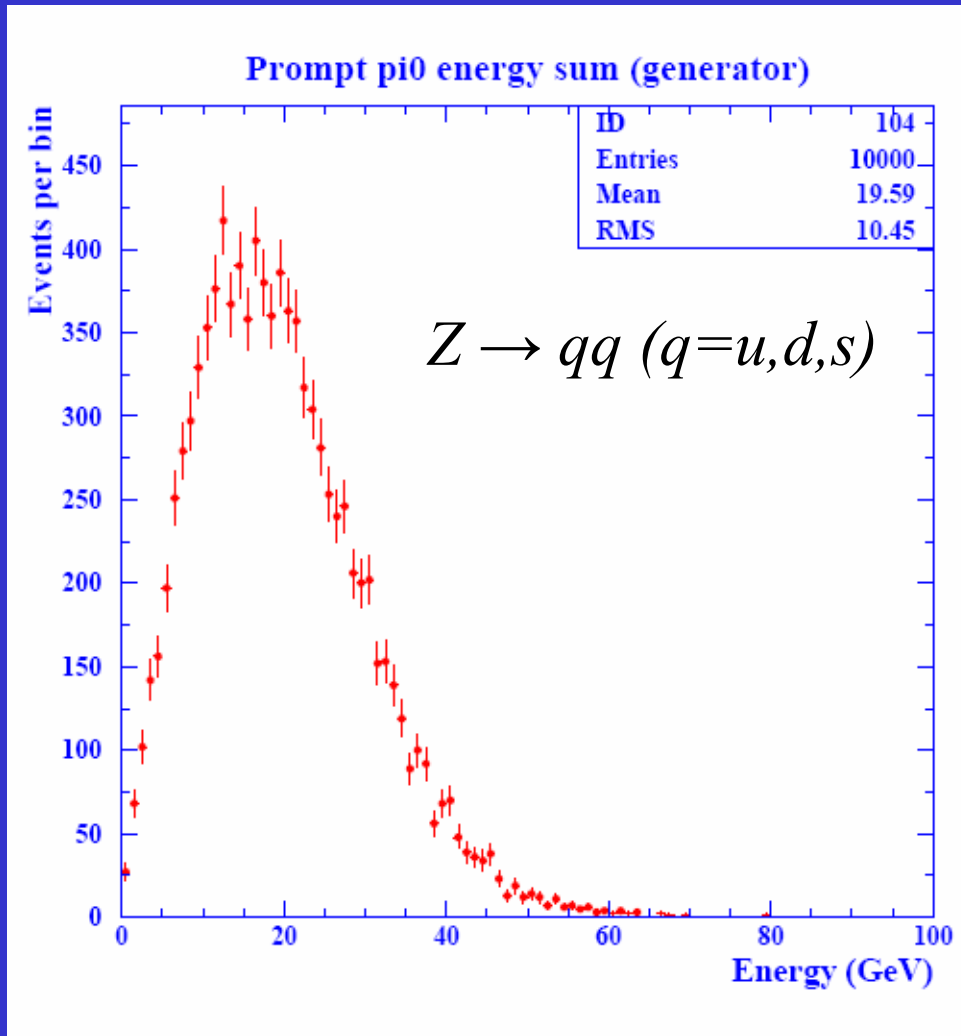
# Prompt EM energy component of jets

*Dominated by  $\pi^0$ 's.*

*Defined as prompt if they are produced within 10 cm of the IP.*

*On average, with  $16\%/\sqrt{E}$  EM energy resolution, the intrinsic EM resolution contribution to the jet energy is 0.71 GeV corresponding to  $7.4\%/\sqrt{E_{\text{jet}}}$ .*

*Can potentially reduce this contribution using  $\pi^0$  mass constraint. May drive ultra-fine position resolution (eg. MAPS) and/or lead to an option of saving some Silicon layers.*



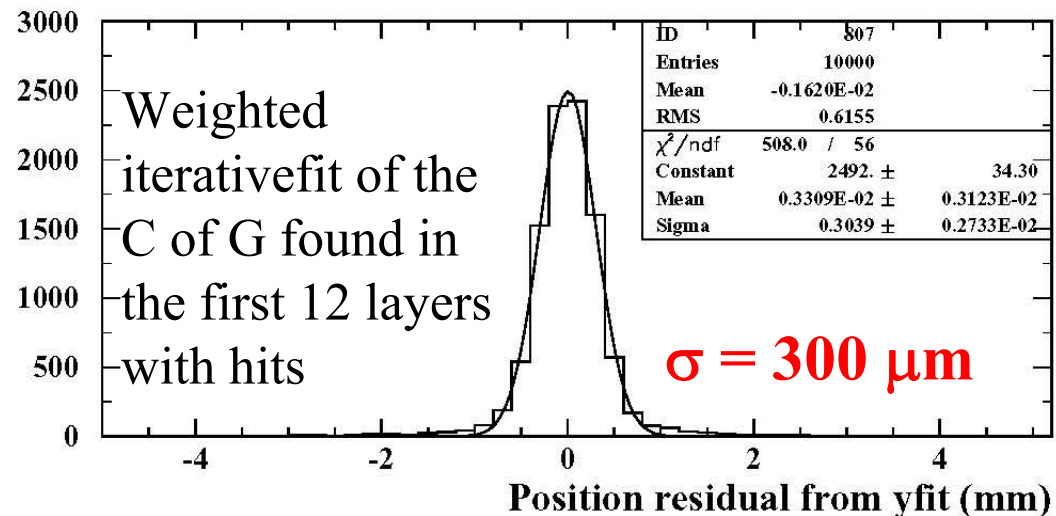
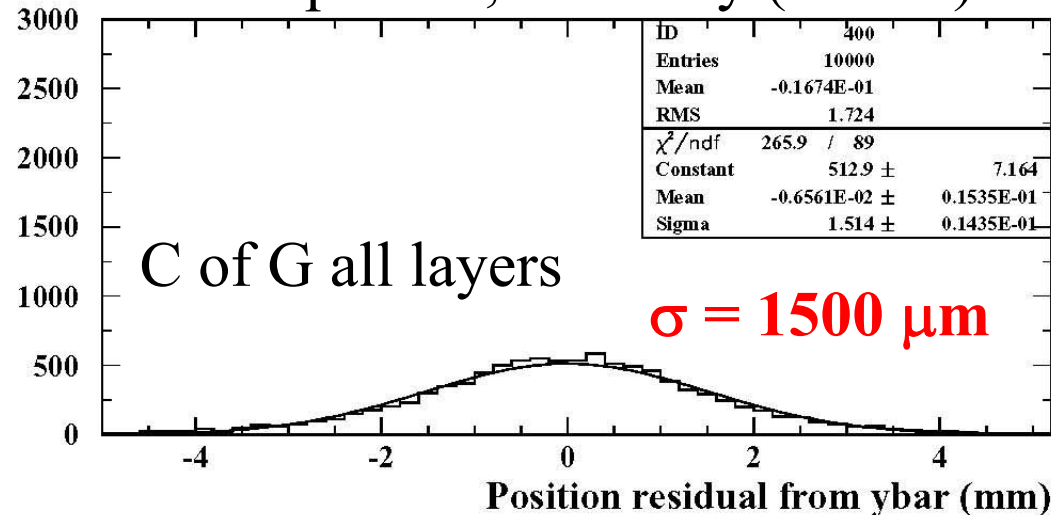
# Position resolution from simple fit

*Key: measure the shower really well near the conversion point ( $\gamma \rightarrow e^+e^-$ )*

*2004 study with 1mm\*1mm Si pixels (pre-MAPS I thought this was unbuildable ...) and 42 layers with sampling every  $5/7 X_0$*

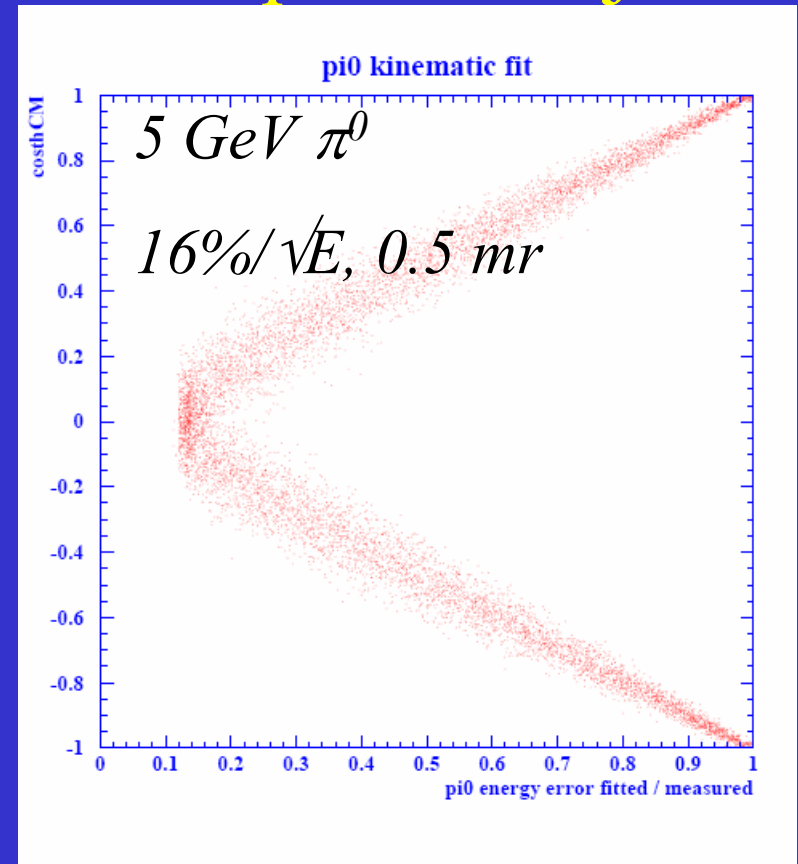
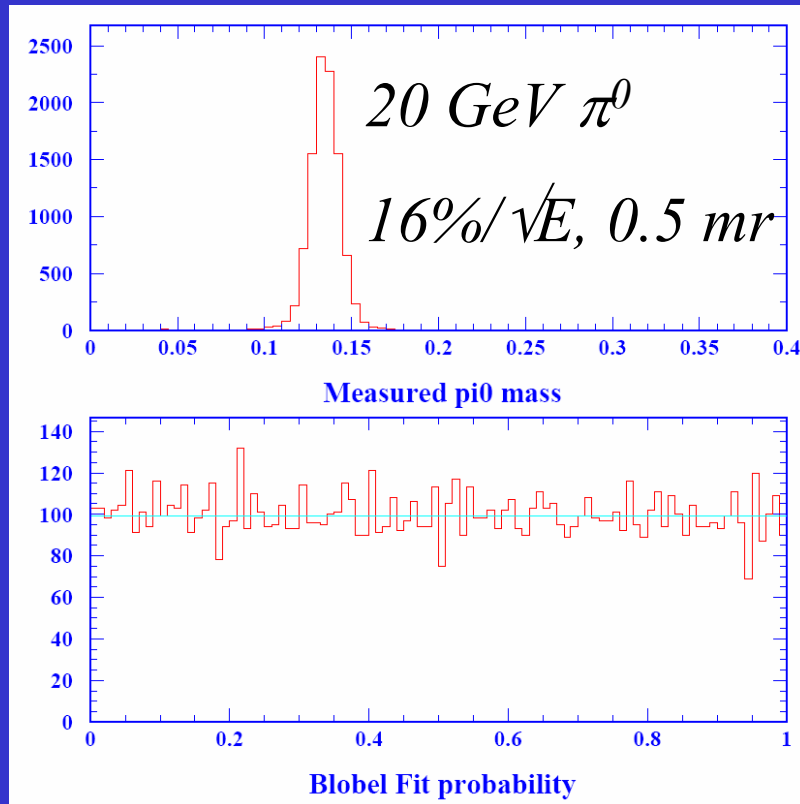
*Position resolution does indeed improve by a factor of 5 in a realistic 100% efficient algorithm!*

1 GeV photon, G4 study (GWW)



Still just  $d/\sqrt{12}$  !

# Comprehensive study of applying mass-constrained fit for $\pi^0$ 's to improve the energy resolution of the *prompt* EM component of jets



*See talk at Valencia meeting for more details. Proof of principle of the intrinsic potential per  $\pi^0$ .*

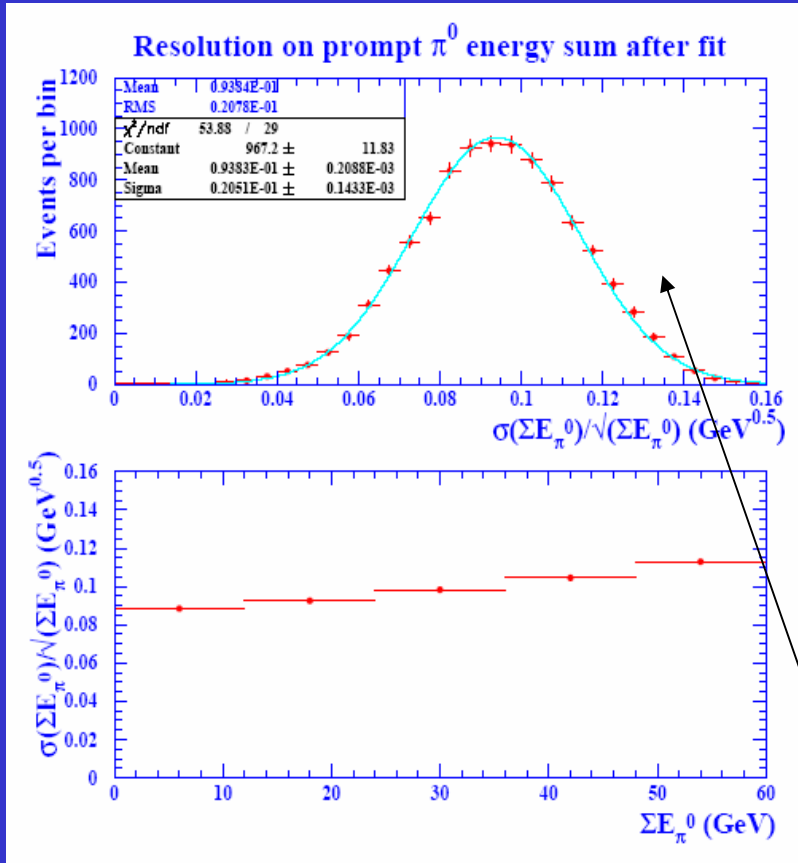
*NOTE: Not only does the resolution improve, the resolution is known per pair*

# Practical Implementation for Hadronic Events

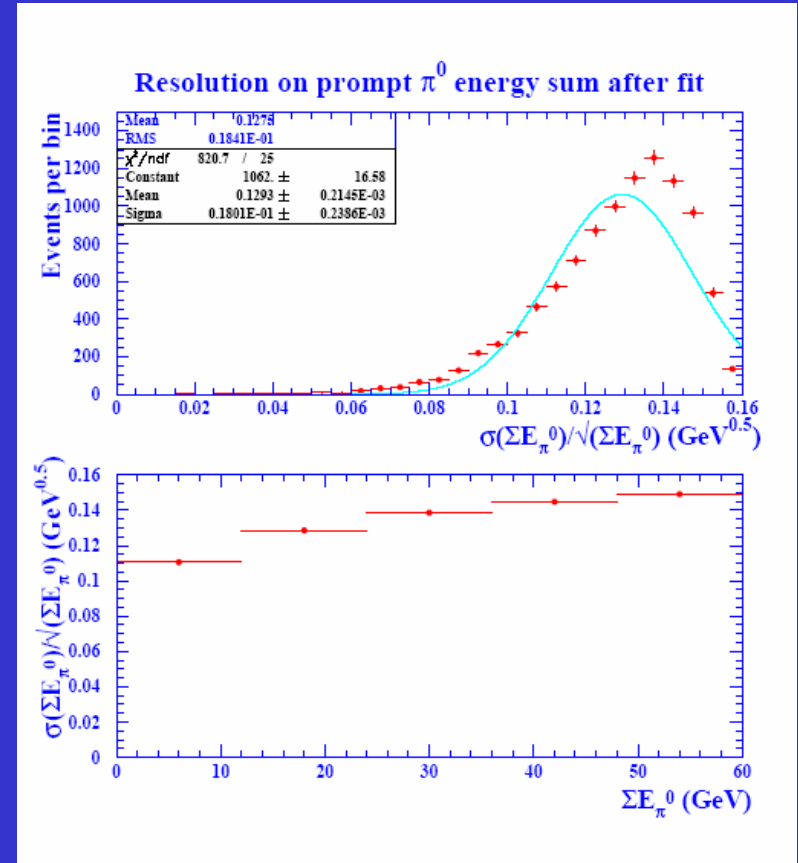
- 1. Assume perfect pairing of photons to  $\pi^0$ s.
  - Estimate improvement.
  - Study implications for detector.
- 2. Implement an assignment algorithm which associates sibling photon pairs to parent  $\pi^0$ s.
  - Now have a first implementation which can probably be improved considerably. Lots of work still to do here.
- 3. Implement in the context of full simulation of a particular detector model.
  - Need to care about photon calibration, resolution functions, purity, efficiency etc. (Clermont-Ferrand group, is working on this aspect for LDC). See P. Gris talk, work by C. Carloganu.

# Applying mass-constraint to $Z \rightarrow \text{hadrons}$

*Assumes perfect pairing of sibling photons to parent  $\pi^0$   
(currently restrict to prompt  $\pi^0$ s defined as originating within 10 cm of IP)*



$16\%/\sqrt{E}$ ,  $\Delta\psi_{12}=0.5mr$



$16\%/\sqrt{E}$ ,  $\Delta\psi_{12}=8mr$

*Potential to improve resolution on average to  $9.4\%/\sqrt{E}$*

# Summary on potential with perfect pairing

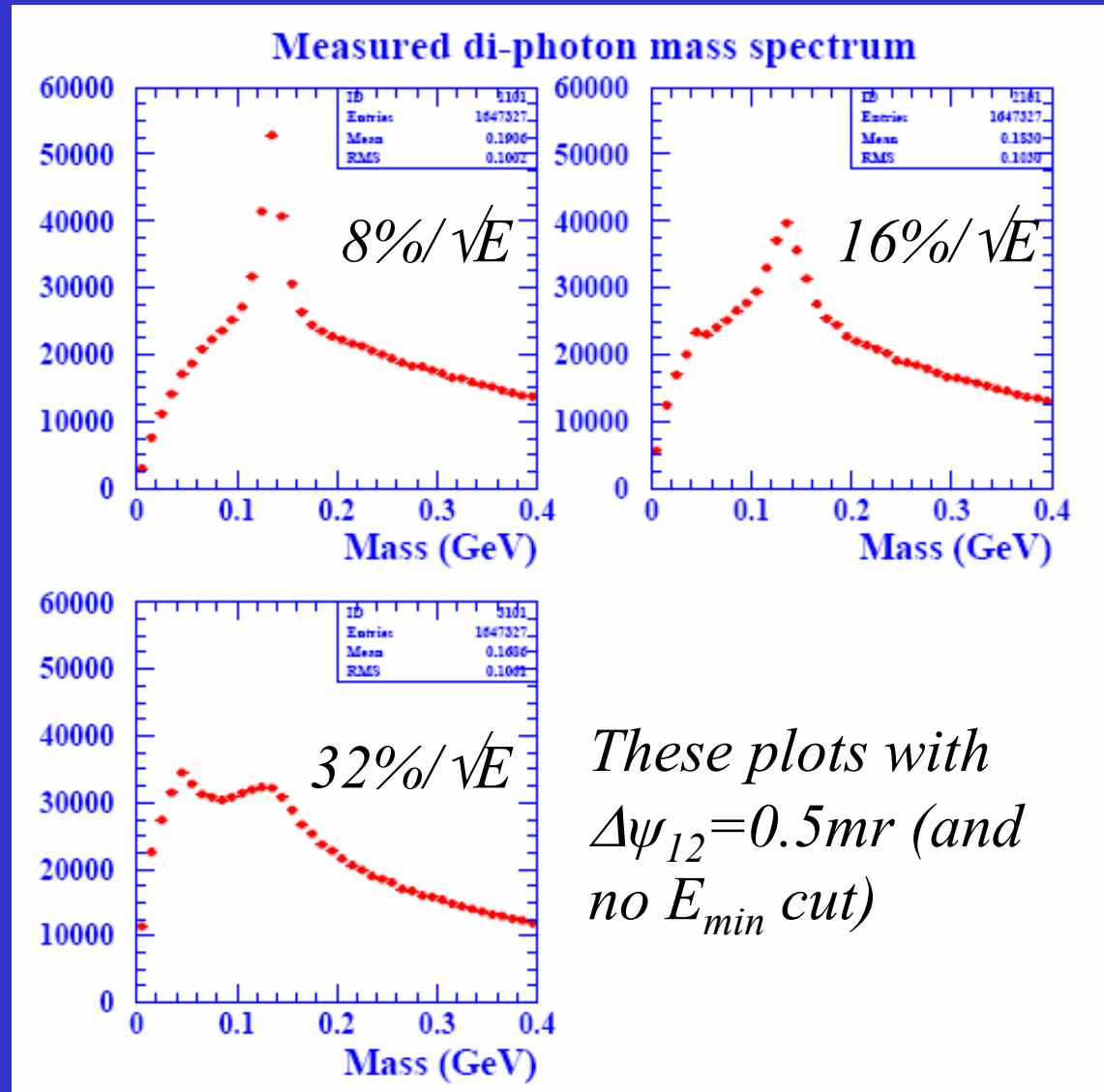
ECAL Energy Resolution (%)	No fit	Fit (0.5 mrad)	Fit (2 mrad)	Fit (8 mrad)
8.0	8.0	4.9	5.8	6.8
16.0	16.0	9.4	10.7	12.7
32.0	32.0	18.3	19.9	23.4

Table 1: *Average normalized fractional energy resolution (%) on the total prompt  $\pi^0$  energy in light-quark Z events with and without kinematic fitting for different assumptions on the ECAL energy resolution stochastic term, and the di-photon opening angle resolution assuming perfect pairing in the kinematic fit. Errors are less than 0.1%.*

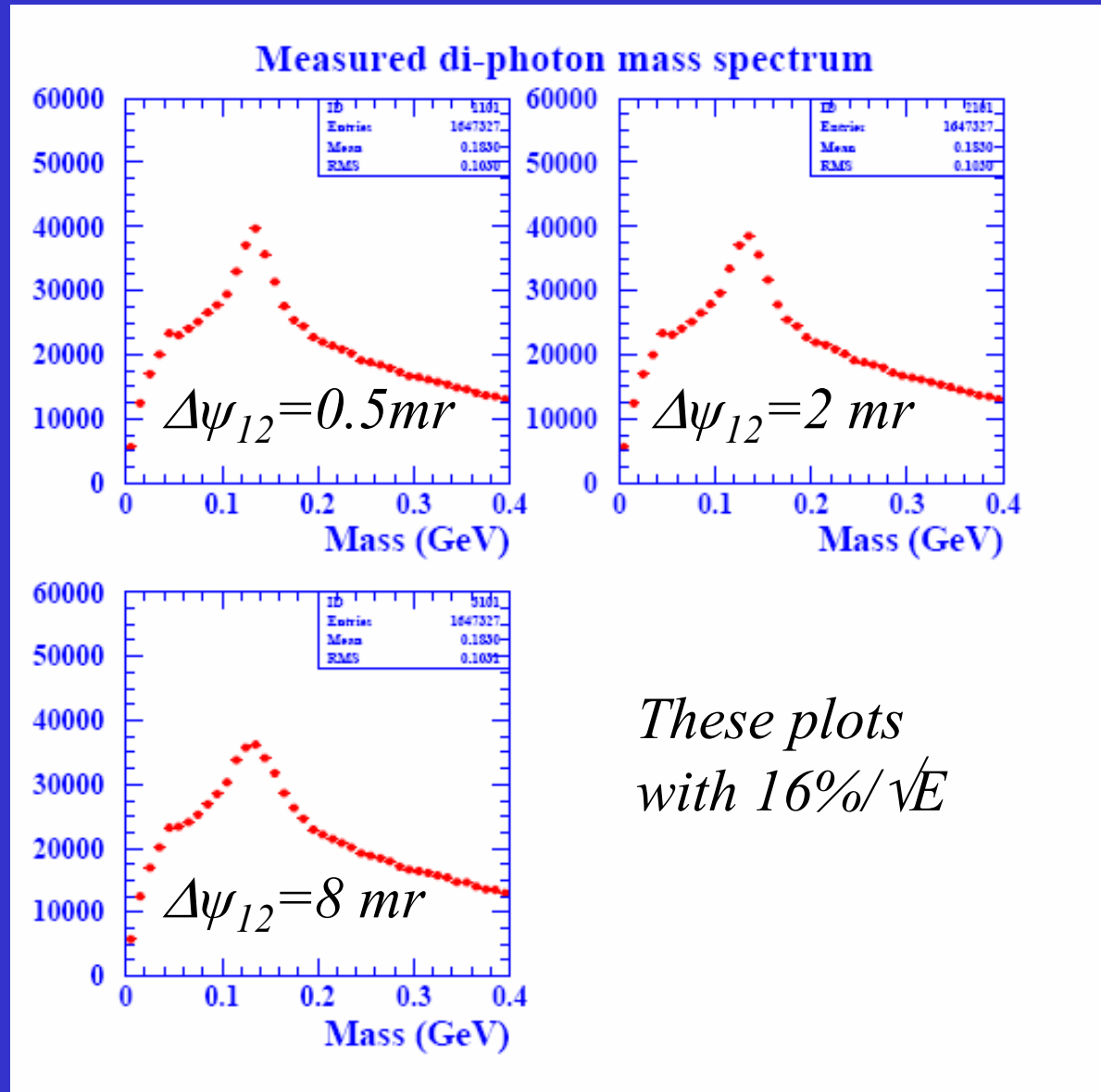
*(will pause to digest this later in talk)*

# Include (vast) combinatorics

$$\langle n_{\pi^0} \rangle = 8.6$$



# Same, but vary opening angle resolution





# Assignment Algorithm

- Very basic so far. (Snap-shot)
- $E_\gamma > 0.1 \text{ GeV}$
- $p_{\text{fit}} > 1\%$
- Form  $\chi^2_{\text{mass}} = [(m - m(\pi^0))/0.07]^2 \rightarrow p_{\text{mass}}$
- Use a discriminant,  $D = p_{\text{fit}} p_{\text{mass}} E_{\pi^0} / \sigma_m$
- Using energy sorted photons, assign photons to pairings if they have the highest D for both photons.
- Unassigned photons, contribute with their normal measured energy.
- Performance may be strongly dependent on the actual combinatorics.
- Have also looked into a more global method of assignment using assignment problem methodology. Currently pondering how to enforce one-to-one assignment, while taking advantage of  $N^3$  rather than  $N!$  scaling of standard techniques.

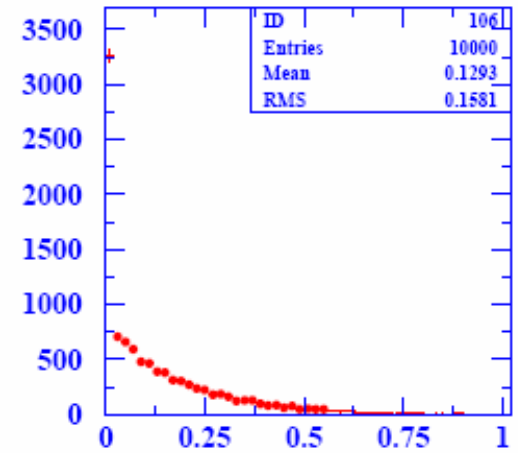
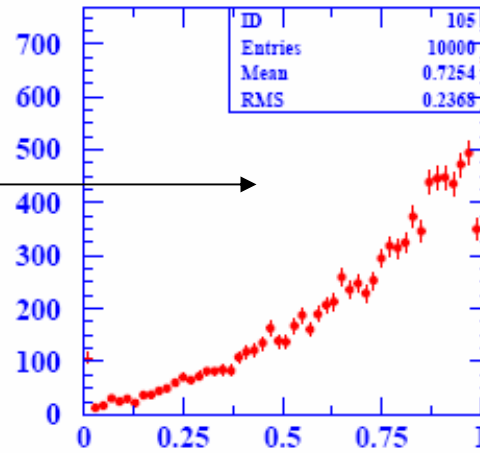
# Performance

*Fraction of prompt  $\pi^0$   
energy correctly fitted,  $\varepsilon_c$*

*Fraction of prompt  $\pi^0$   
energy wrongly fitted,  $\varepsilon_W$*

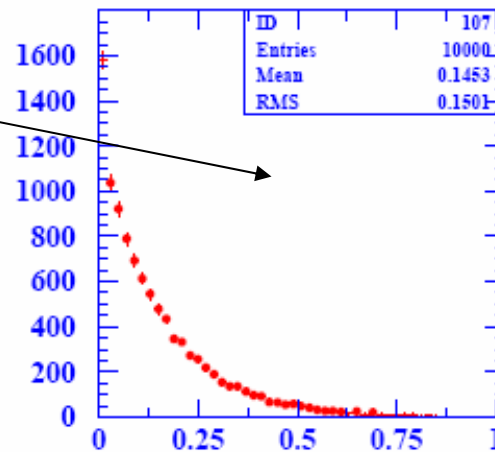
*Fraction of prompt  $\pi^0$   
energy unfitted,  $\varepsilon_{UF}$*

V1.67 Performance 16%, 0.5mr

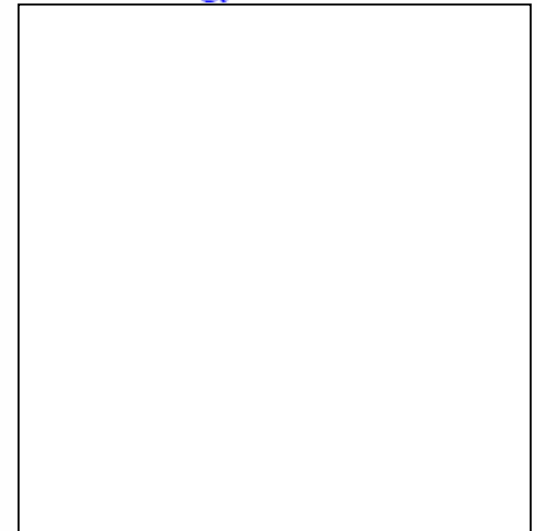


Energy efficiency

Energy contamination



Energy inefficiency



# Typical Event

(selected as having performance similar to the average).

This one has  $\Sigma E_{\pi^0} = 28 \text{ GeV}$ ,  $n_{\pi^0} = 14$ , so  $n_\gamma = 28$ ,  $n_{\gamma\gamma} = 378$ , and in total 107  $\gamma\gamma$  combinations passing the kinematic fit cuts.

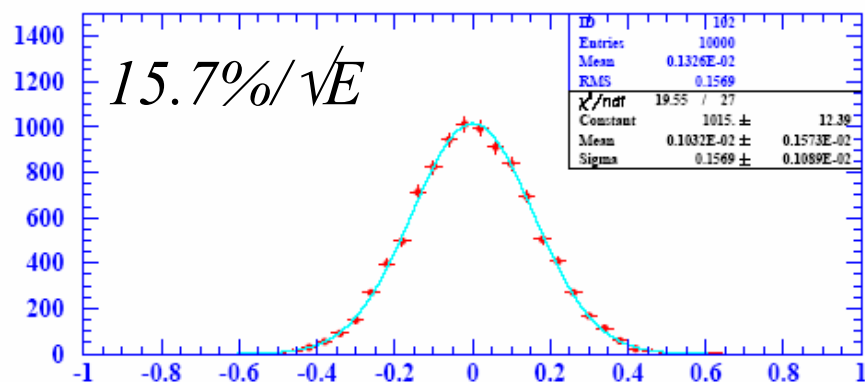
The stochastic deviation in this particular event improves from  $+9.9\%/\sqrt{E}$  to  $-0.07\%/\sqrt{E}$

Number of viable pairings for this photon

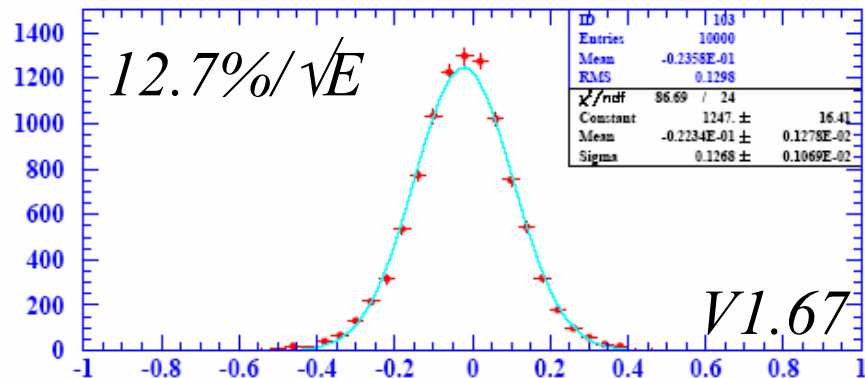
```
analyse_example.output - XEmacs
File Edit View Cmds Tools Options Buffers
Open Dired Save Print Cut Copy Paste Undo Spell Replace Mail Info Compile Debug News
analyse_example.output
Dumping the configuration
gamma 1np = 12 config = 0 1 3 1
gamma 2np = 0 config = 0 0 0 0
gamma 3np = 5 config = 63 1 13 2
gamma 4np = 0 config = 0 0 0 0 ← unassigned
gamma 5np = 22 config = 104 1 7 3
gamma 6np = 4 config = 131 1 12 3
gamma 7np = 6 config = 104 2 5 4
gamma 8np = 6 config = 0 2 7 4
gamma 9np = 4 config = 0 1 13 5
gamma 10np = 0 config = 0 0 0 0
gamma 11np = 0 config = 0 0 0 0
gamma 12np = 22 config = 131 2 6 6
gamma 13np = 22 config = 63 2 3 7
gamma 14np = 0 config = 0 0 0 0
gamma 15np = 7 config = 288 1 16 8 ← mis-
gamma 16np = 6 config = 288 2 15 8 ← assigned
gamma 17np = 9 config = 313 1 18 9 ← Correctly
gamma 18np = 7 config = 313 2 17 9 ← assigned
gamma 19np = 7 config = 334 1 20 10
gamma 20np = 6 config = 334 2 19 10
gamma 21np = 6 config = 351 1 22 11
gamma 22np = 13 config = 351 2 21 11
gamma 23np = 22 config = 364 1 24 12
gamma 24np = 5 config = 364 2 23 12
gamma 25np = 6 config = 373 1 26 13
gamma 26np = 6 config = 373 2 25 13
gamma 27np = 5 config = 378 1 28 14
gamma 28np = 6 config = 378 2 27 14
nviabale = 107
etotg: 27.8106766 etotm: 28.3339062 etotf: 27.7744846
Kinematic fit energy efficiency : 0.727168024
Kinematic fit energy contamination : 0.192166701
Kinematic fit inefficiency : 0.0806652158
Kinematic fit F-O-M : 0.587430477
stochastic deviations: 0.0992171019 -0.00686287507
Raw-----XEmacs: analyse_example.output (Fundamental)-----43%-----
Loading efs-cu...done
```

# Current Results (10k Z events)

16%, 0.5mr

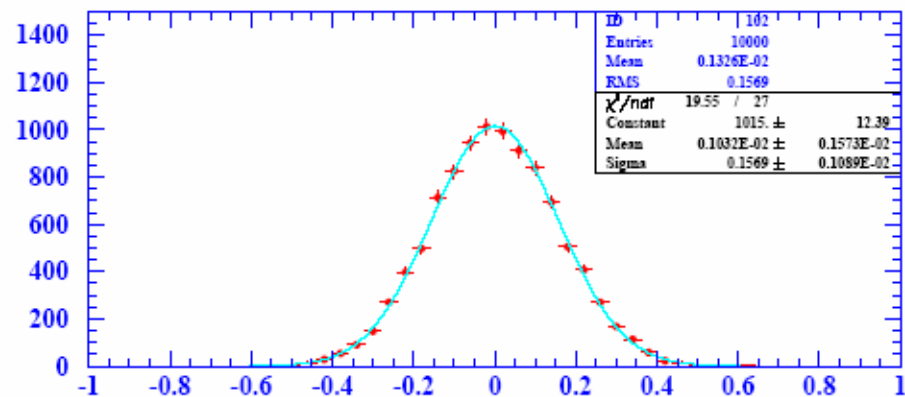


Measured stochastic deviation

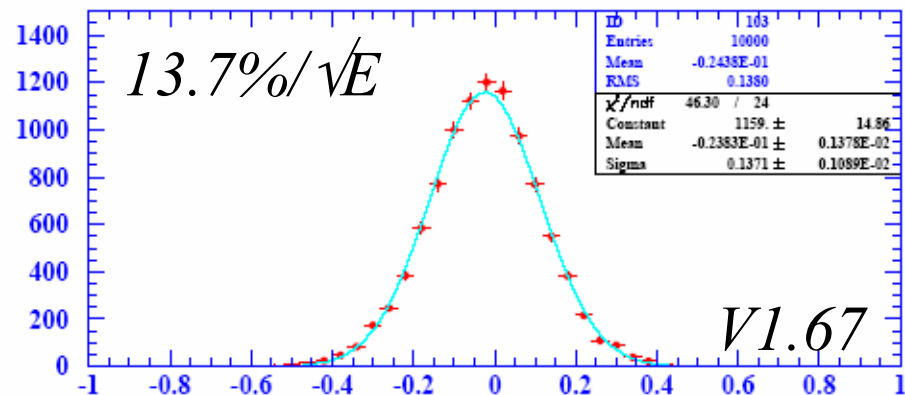


Fitted stochastic deviation

16%, 2.0mr



Measured stochastic deviation



Fitted stochastic deviation

*I believe this can still be improved substantially*

# Summary on potential of $\pi^0$ mass-constraint in hadronic events ( $\sqrt{s}=m_Z$ )

## 1. Perfect pairing

ECAL Energy Resolution (%)	No fit	Fit (0.5 mrad)	Fit (2 mrad)	Fit (8 mrad)
8.0	8.0	4.9	5.8	6.8
16.0	16.0	9.4	10.7	12.7
32.0	32.0	18.3	19.9	23.4

Table 1: Average normalized fractional energy resolution (%) on the total prompt  $\pi^0$  energy in light-quark Z events with and without kinematic fitting for different assumptions on the ECAL energy resolution stochastic term, and the di-photon opening angle resolution assuming perfect pairing in the kinematic fit. Errors are less than 0.1%.

*(uses fit to the error distribution from the fit)*

## 2. Assignment algorithm 1.67

<i>Using fitted <math>\sigma</math> of</i>	<i>7.9</i>	<i>6.3</i>	<i>6.9</i>	<i>7.5</i>
<i>deviation on same</i>	<i>15.7</i>	<b><i>12.7</i></b>	<i>13.7</i>	<i>14.8</i>
<i>10k events</i>	<i>31.0</i>	<i>25.9</i>	<i>27.0</i>	<i>29.0</i>

# Summary

- EM calorimeter contribution to the jet energy resolution can plausibly be considerably improved using  $\pi^0$  mass constraint in detector designs with fine granularity ECAL.
- Fast-timing has a lot of potential.
  - Particle ID, confusion mitigation, neutral hadron reconstruction.
  - Worthwhile to evaluate performance/feasibility of some of the possible approaches. Are you interested ?

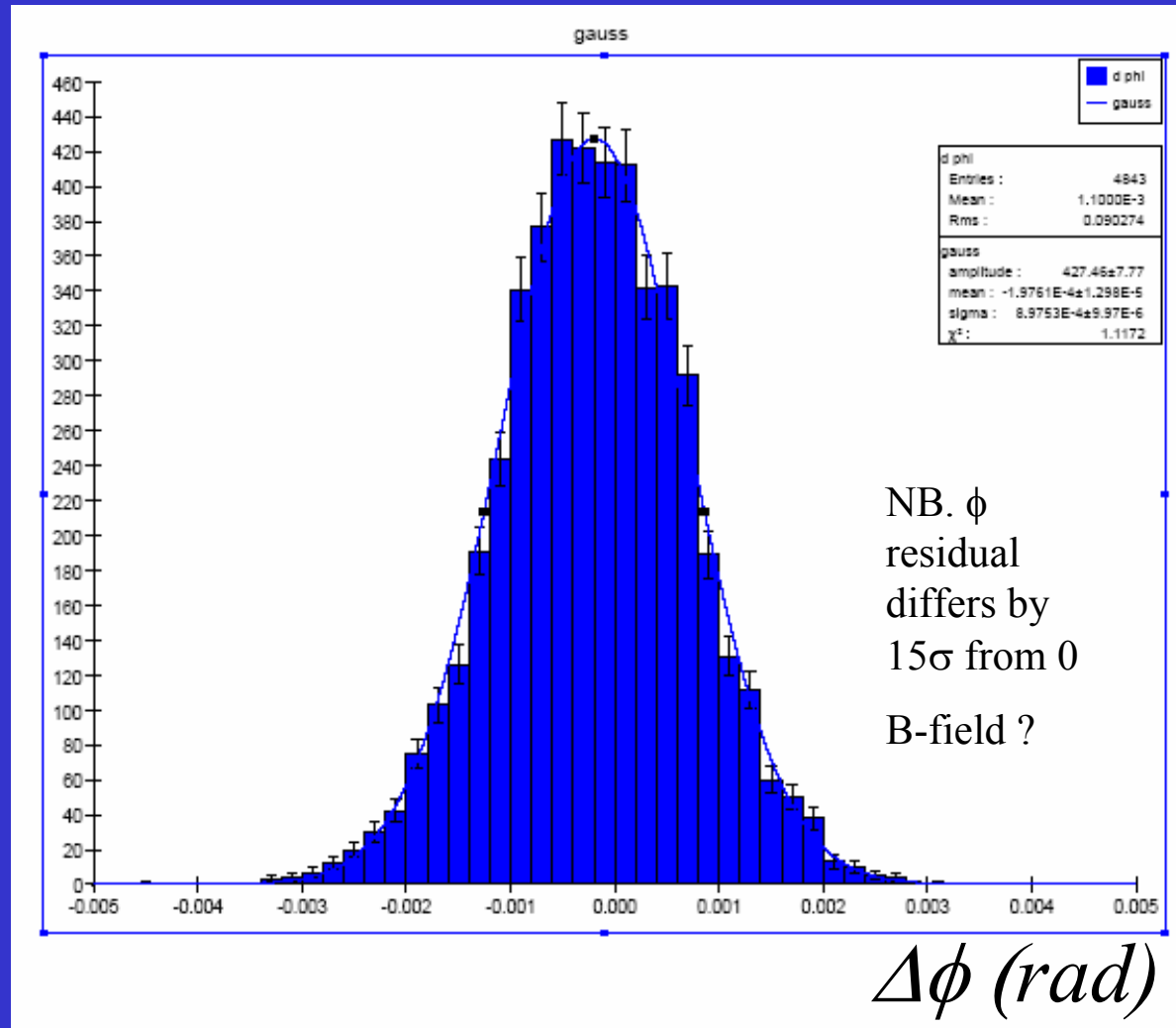
# Backup Slides

# Angular Resolution Studies

5 GeV photon at  $90^\circ$ ,  
sidmay05 detector (4 mm  
pixels,  $R=1.27\text{m}$ )

Phi resolution of 0.9 mrad  
*just* using cluster CoG.

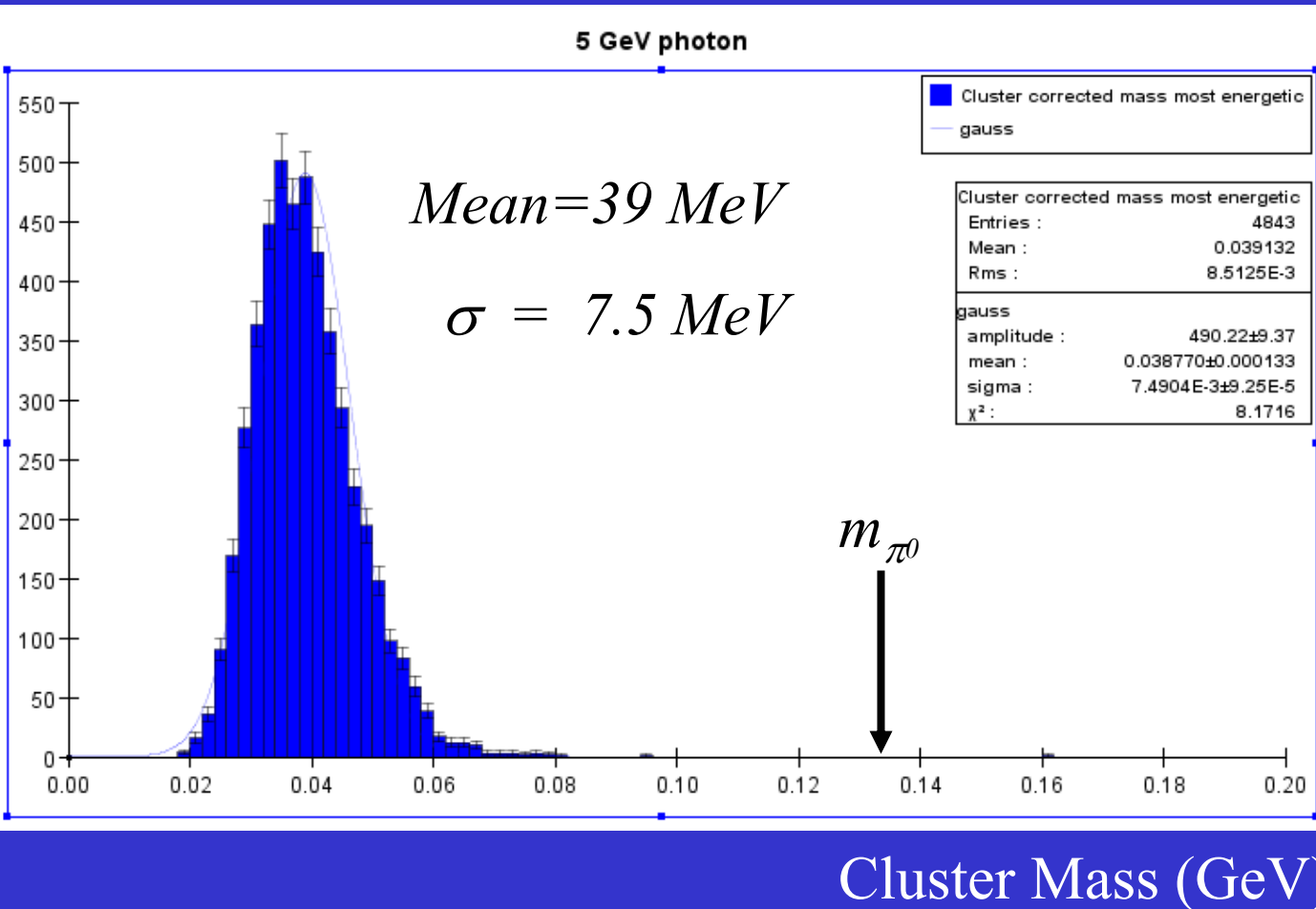
$\Rightarrow \theta_{12}$  resolution of 2  
mrad is easily achievable  
for spatially resolved  
photons.



NB. Previous study (see backup slide), shows that a factor of 5 improvement in resolution is possible at fixed  $R$  using longitudinally weighted “track-fit”.



# Cluster Mass for Photons



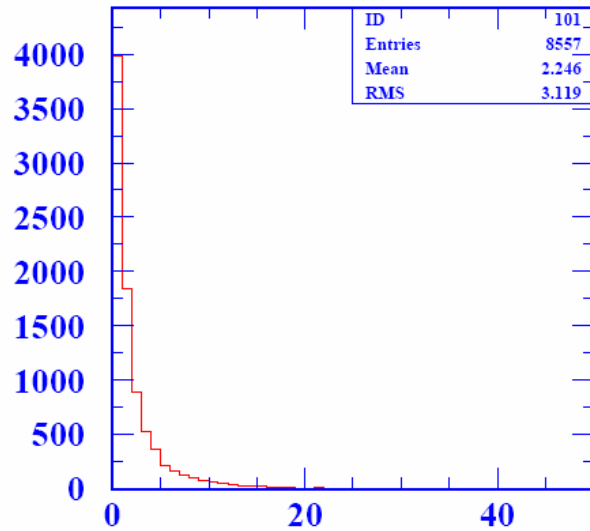
*Of course, photons actually have a mass of zero.*

*The transverse spread of the shower leads to a non-zero cluster mass calculated from each cell.*

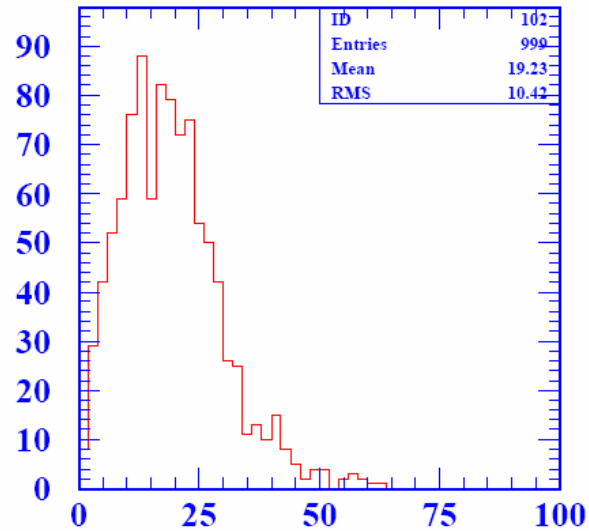
*Use to distinguish single photons from merged  $\pi^0$ 's.*

*Performance depends on detector design ( $R$ ,  $R_M$ ,  $B$ , cell-size, ...)*

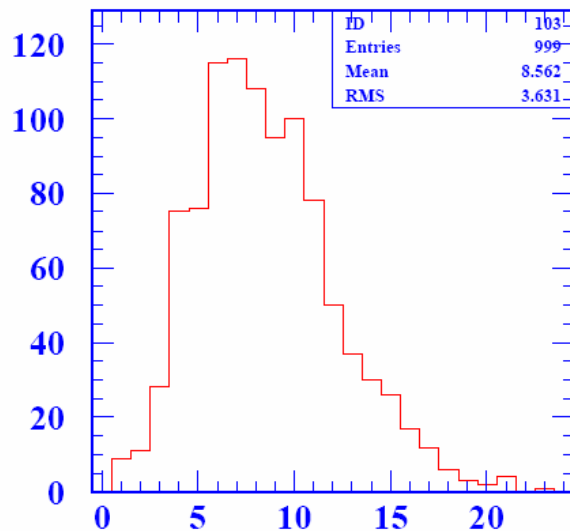
## Z to uu, dd, ss at 91 GeV



Prompt pi0 energy spectrum



Prompt pi0 event energy



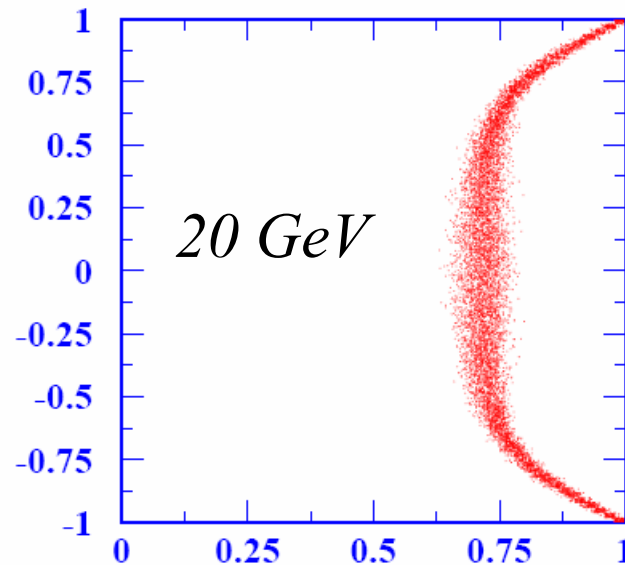
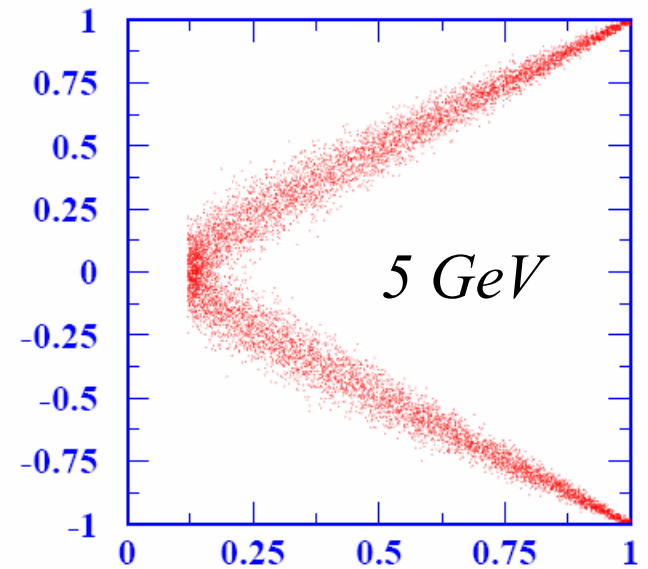
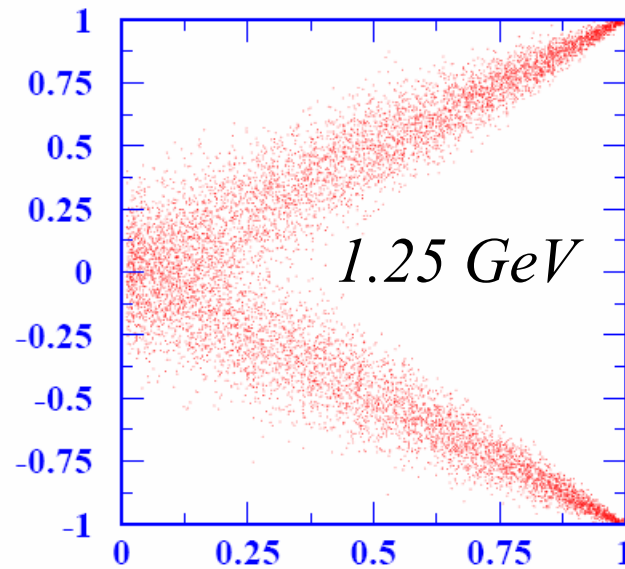
Prompt pi0 count

On average 19.2 GeV  
(21.0%)

NB generator has  
ISR and  
beamsstrahlung  
turned off.

*Dependence  
on  $\pi^0$  energy*

Boomerangs: 16 per cent, 0.5mr

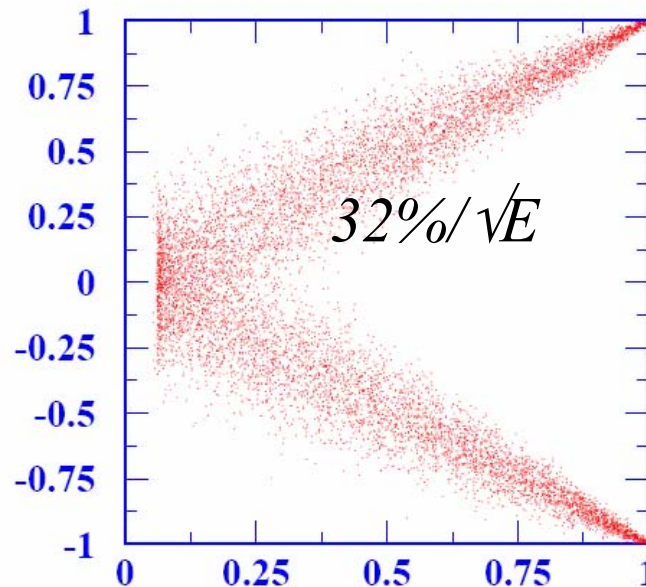
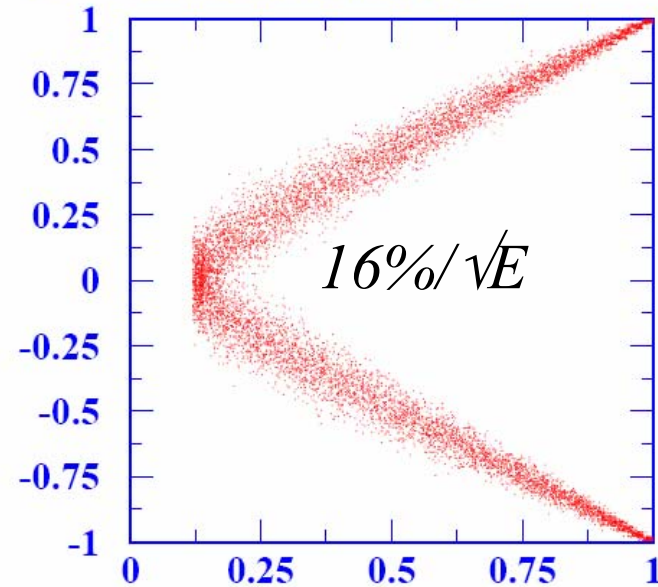
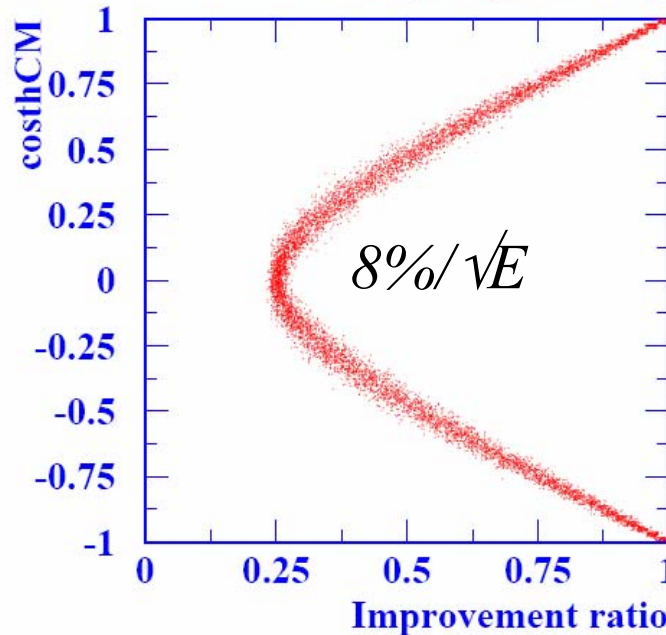


$x$ : improvement ratio

$y$ :  $\cos\theta^*$

$5\text{ GeV } \pi^0$

## Varying Energy Resolution 11,21,31



*Improvement ratio (x-projection) **DOES** depend on Energy resolution (for this  $\pi^0$ )*

*- But on average the dependence is only weak (see next slide)*

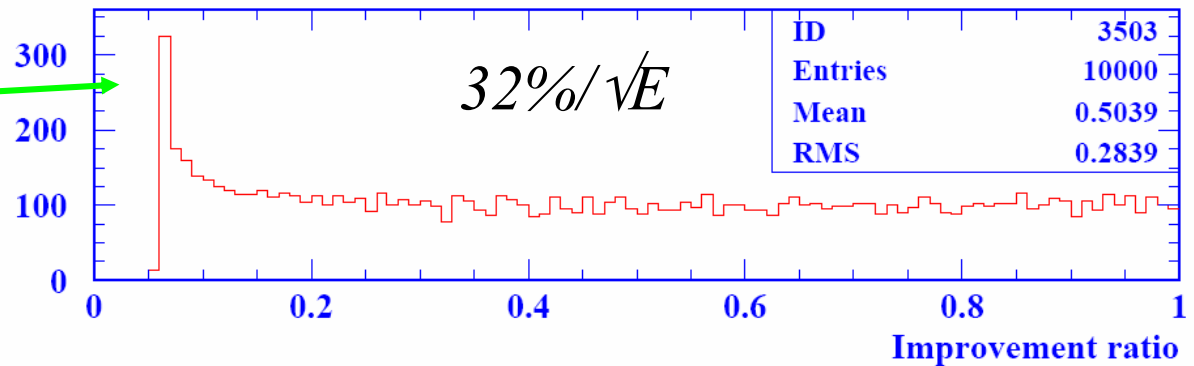
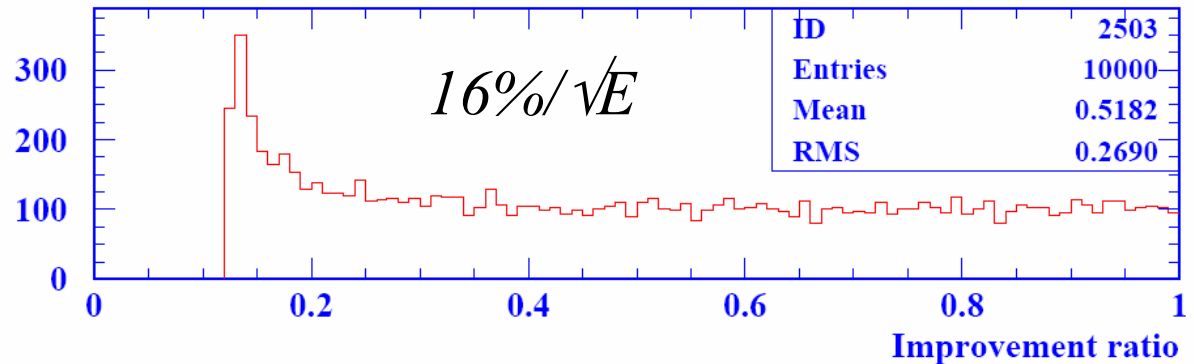
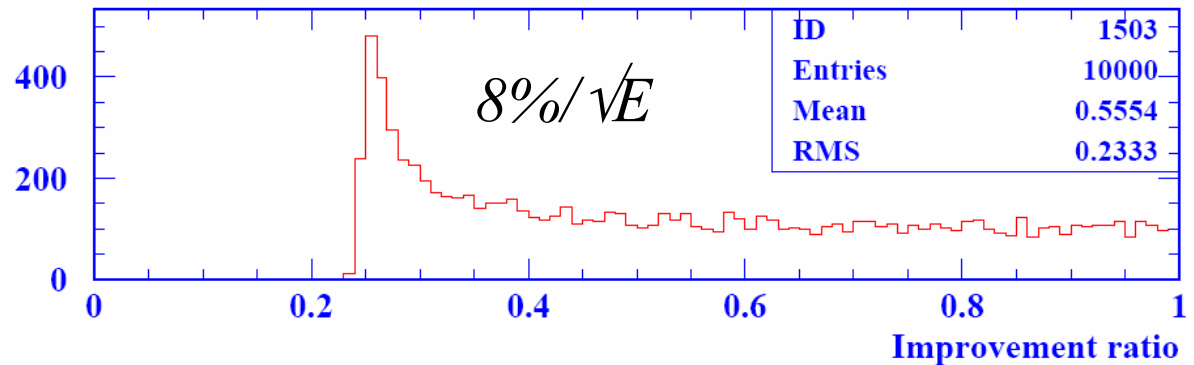
This slide has been corrected from that presented at Vancouver

## 5 GeV $\pi^0$

*Average improvement factor not highly dependent on energy resolution.*

*BUT the maximum possible improvements increase as the energy resolution is degraded.*

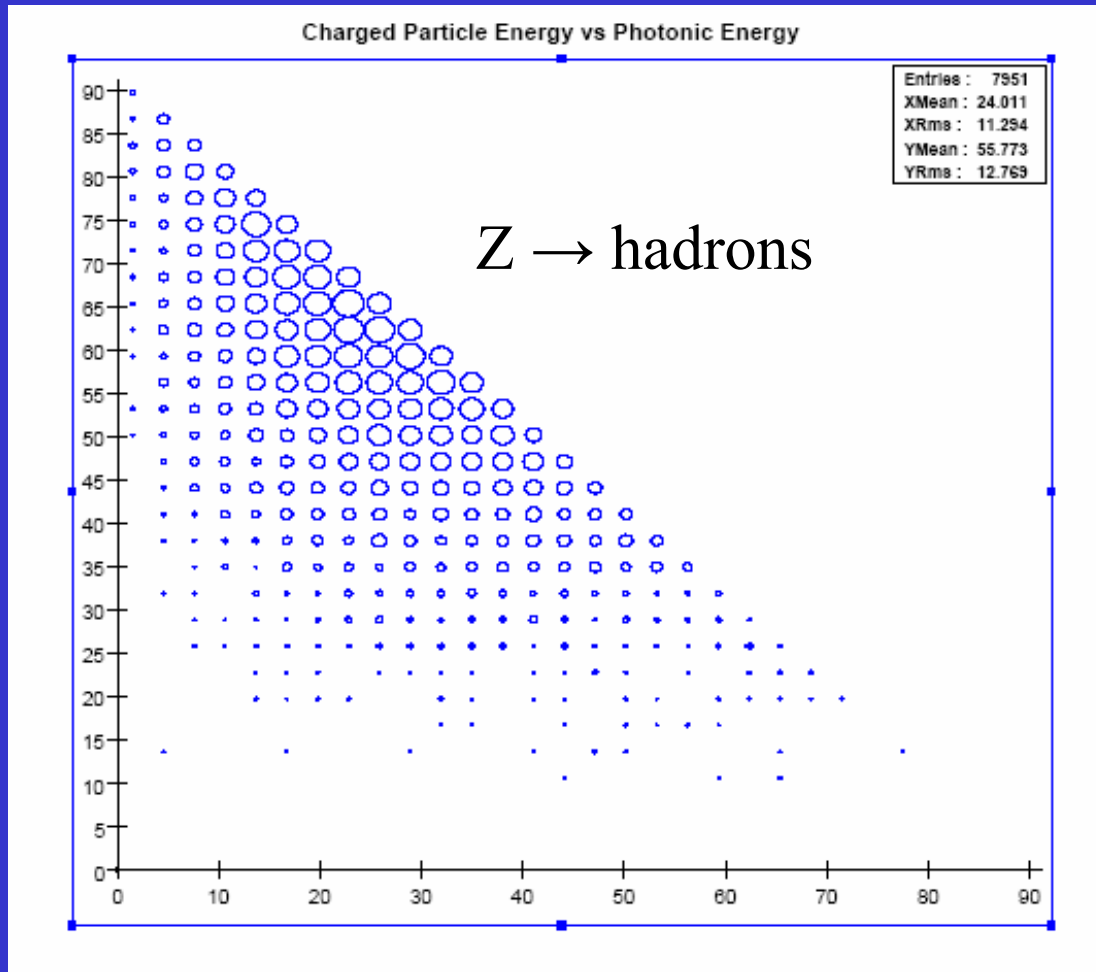
### Improvement Ratio Dependence on Energy Resolution



# PFA “Dalitz” Plot

Also see: [http://heplx3.phsx.ku.edu/~graham/lcws05\\_slacconf\\_gwwilson.pdf](http://heplx3.phsx.ku.edu/~graham/lcws05_slacconf_gwwilson.pdf)

“On Evaluating the Calorimetry Performance of Detector Design Concepts”, for an alternative detector-based view of what we need to be doing.



On average,  
photonic energy  
only about 30%, but  
often much greater.

# $\gamma, \pi^0, \eta^0$ rates measured at LEP

	Experimental results				JETSET 7.4	HERWIG 5.9
	OPAL	ALEPH [6]	DELPHI [9]	L3 [10-12]		
photon						
$x_E$ range	0.003-1.000	0.018-0.450				
$N_\gamma$ in range	$16.84 \pm 0.86$	$7.37 \pm 0.24$				
$N_\gamma$ all $x_E$	$20.97 \pm 1.15$				20.76	22.65
$\pi^0$						
$x_E$ range	0.007-0.400	0.025-1.000	0.011-0.750	0.004-0.150		
$N_{\pi^0}$ in range	$8.29 \pm 0.63$	$4.80 \pm 0.32$	$7.1 \pm 0.8$	$8.38 \pm 0.67$		
$N_{\pi^0}$ all $x_E$	$9.55 \pm 0.76$	$9.63 \pm 0.64$	$9.2 \pm 1.0$	$9.18 \pm 0.73$	9.60	10.29
$\eta$						
$x_E$ range	0.025-1.000	0.100-1.000		0.020-0.300		
$N_\eta$ in range	$0.79 \pm 0.08$	$0.282 \pm 0.022$		$0.70 \pm 0.08$		
$N_\eta$ all $x_E$	$0.97 \pm 0.11$			$0.91 \pm 0.11$	1.00	0.92
$N_\eta$ $x_p > 0.1$	$0.344 \pm 0.030$	$0.282 \pm 0.022$			0.286	0.243

Consistent with JETSET  
tune where 92% of  
photons come from  $\pi^0$ 's.

Some fraction is non-  
prompt, from  $K_S^0, \Lambda$  decay  
9.6  $\pi^0$  per event at Z pole

## 2. $\pi^0$ Kinematic Fitting

- For simplicity used the following measured experimental quantities:

$E_1$  (Energy of photon 1)

$E_2$  (Energy of photon 2)

$\psi_{12}$  (3-d opening angle of photons 1 and 2)

- Fit uses

- 3 variables,  $\mathbf{x} = ( E_1, E_2, 2(1 - \cos\psi_{12}) )$

- a diagonal error matrix

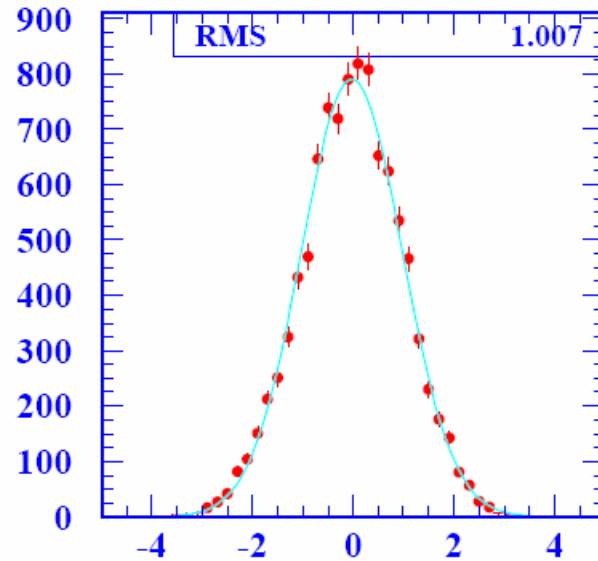
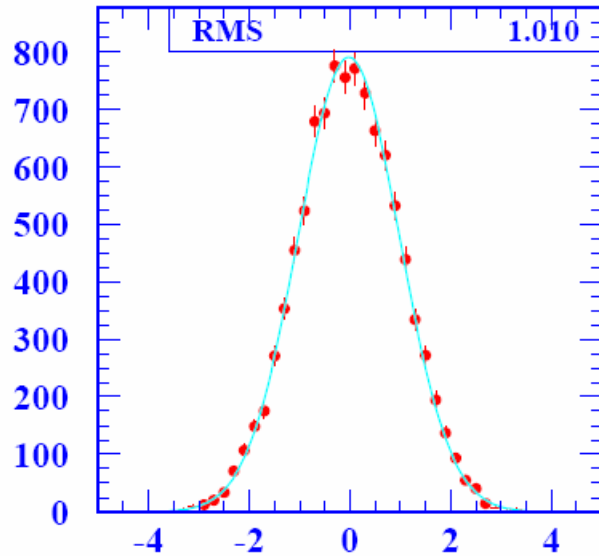
(assumes individual  $\gamma$ 's are completely resolved and measured independently)

- and the constraint equation

$$m_{\pi^0}^2 = 2 E_1 E_2 (1 - \cos\psi_{12}) = \mathbf{x}_1 \mathbf{x}_2 \mathbf{x}_3$$

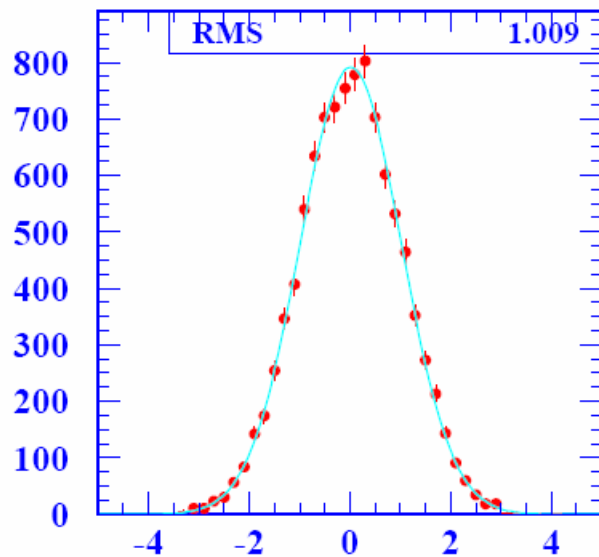


## Pull distributions



Measured  $\pi^0$  energy pull cf gen

Fitted  $\pi^0$  energy pull cf gen



*=> You should also  
be able to believe the  
errors on the fitted  
energies of each  $\pi^0$*

Fitted  $\pi^0$  energy Pull cf measured