

Physics potential of Higgs pair production at a $\gamma\gamma$ collider

Shinya KANEMURA (Univ. of Toyama)

On behalf of

E. Asakawa (Meiji-Gakuin), D. Harada (Sokendai), S.K.,
Y. Okada (Sokendai, KEK), K. Tsumura (ICTP)

TILC08@Sendai March. 05. 2008

Higgs

- Picture for the origin of Mass= **Spontaneous EWSB**
- Higgs sector remains unknown.
 - No Higgs found yet
 - Mass and couplings are unknown yet
- SM Higgs: a scalar iso-doublet
 - Problematic
 - Motivation for various new physics models

Identify Higgs sector = Determination of New Physics

Higgs potential

$$V = \frac{1}{2}m_h^2 h^2 + \frac{1}{3!}\lambda_{hhh}h^3 + \frac{1}{4!}\lambda_{hhhh}h^4 + \dots$$

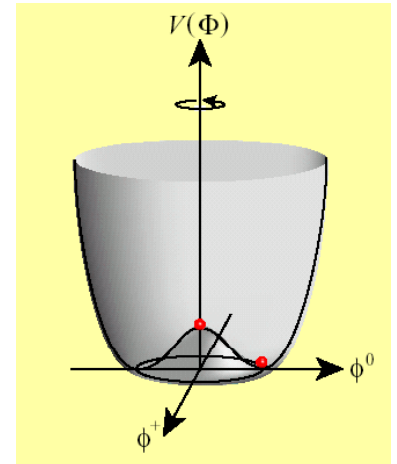
- SM Higgs potential
 - Electroweak Symmetry Breaking

$$V(\Phi) = -\mu^2|\Phi|^2 + \lambda|\Phi|^4$$

- Free parameter of the SM λ

$$m_h^2 = \lambda v^2, \quad \lambda_{hhh} = \lambda v, \quad \lambda_{hhhh} = \lambda$$

- It is important to measure both the mass m_h and hhh (and hhhh) coupling
 - Test for the SM Higgs potential
 - Nature of the EWSB
 - New physics determination



New Physics effect on HHH

- Non-decoupling effects

hhh coupling

$$\lambda_{hhh} \simeq \frac{3m_h^2}{v} \left(1 - \frac{N_c m_t^4}{3\pi^2 v^2 m_h^2} + \dots \right)$$

A m_t^4 term appears in the 1-loop correction.
loop effect $\sim 10\%$

Similarly, by new physics loops, HHH can easily receive large deviation from the SM value.

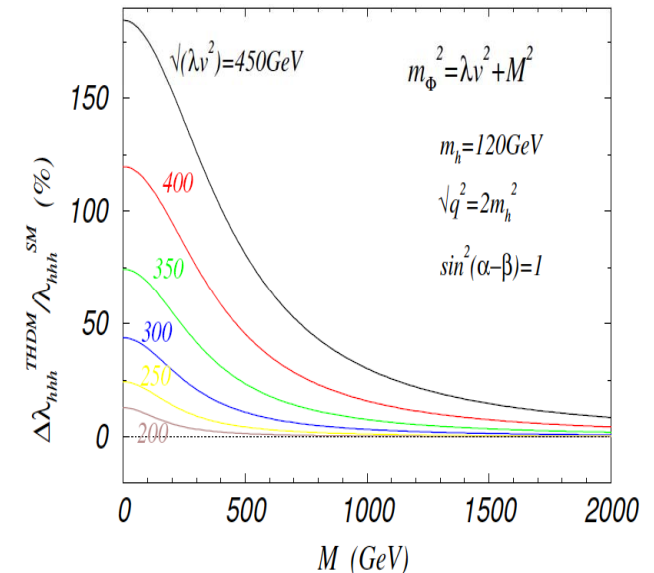
- Pure dim-6 operators

$$\mathcal{L}' = \sum_i \frac{f_i}{\Lambda^2} \mathcal{O}_i$$

$$\mathcal{O}_1 = \frac{1}{2} \partial_\mu (\Phi^\dagger \Phi) \partial^\mu (\Phi^\dagger \Phi) \quad \mathcal{O}_2 = -\frac{1}{3} (\Phi^\dagger \Phi)^3$$

$$\mathcal{L}_{H^3} = -\frac{m_H^2}{2v} \left(\left(1 - \frac{a_1}{2} + \frac{2a_2}{3} \frac{v^2}{m_H^2} \right) H^3 - \frac{2a_1 H \partial_\mu H \partial^\mu H}{m_H^2} \right)$$

2HDM



SK, Kiyoura, Okada, Senaha, Yuan

Tsumura's talk

Cosmological Connections

- Higgs Effective Potential
- Electroweak Phase Transition at Early Universe

SM λ_{HHH}
2nd Order

\Leftrightarrow

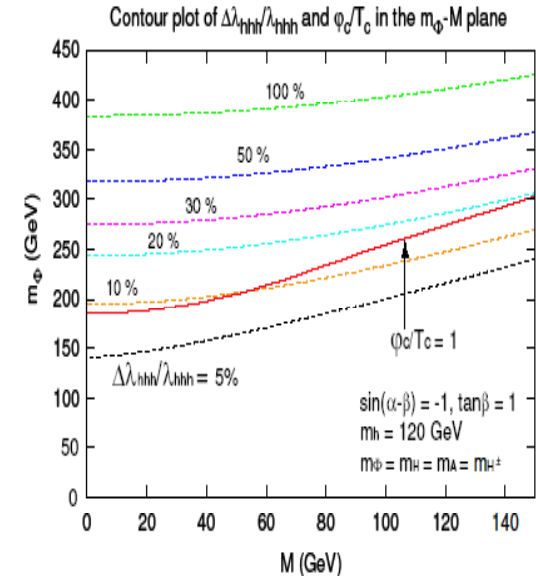
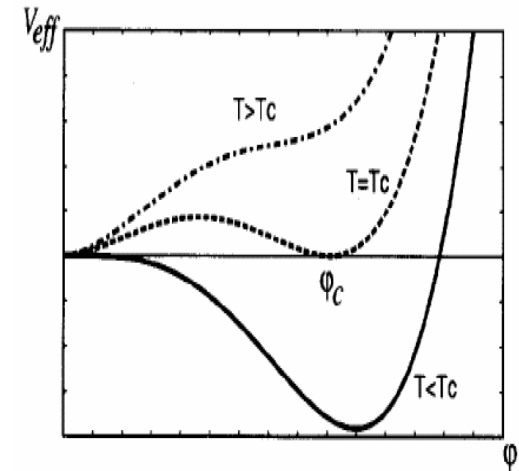
A large $\delta\lambda_{HHH}$
Strong 1st Order

- Electroweak Baryogenesis requires a strong 1st Order PT (For avoiding sphaleron smearing in broken phase)

$$\frac{\varphi_c}{T_c} > 1 \quad \Rightarrow \quad \frac{\Delta\lambda_{hhh}}{\lambda_{hhh}^{SM}} > \mathcal{O}(10)\%$$

- 2HDM
- Dim-6 Operator (Grogan, Sevant, Wells)
- MSSM (Nelson et al; Carena et al,

Noble, Pelestein



SK, Okada, Senaha

In this talk

- We discuss a possibility to measure the Higgs tri-linear coupling via the process of

$$\gamma\gamma\rightarrow HH$$

at the ILC **photon collider** option.

- Alternative or better as compared to e^+e^- collision?
Jikia, Jikia and Belusevic HHZ, HH $\nu\nu$
- Can new physics effects drastically change SM predictions?
- Valuable for a simulation study?

Measurement of the HHH coupling

- Higgs self-coupling (HHH)

- Direct information to the Higgs potential
- Effect on the New Physics
- Cosmological Connection

Required accuracy $\frac{\Delta\lambda_{hhh}}{\lambda_{hhh}^{SM}} < \mathcal{O}(10)\%$

- Measurement at collider experiments

- LHC $gg \rightarrow HH$

- ILC $e^+e^- \rightarrow ZHH$ $e^+e^- \rightarrow HH\nu\bar{\nu}$

- ILC ($\gamma\gamma$ collider)

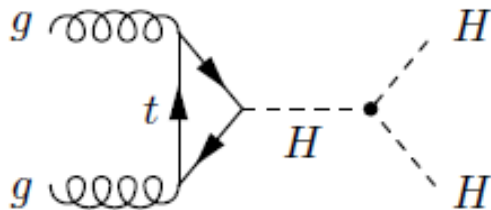
$$\gamma\gamma \rightarrow HH \quad \text{This is our subject.}$$

- Sensitivity to anomalous deviations of λ

$$\lambda = \lambda_{SM} + \delta\lambda = \lambda_{SM} (1 + \delta\kappa)$$

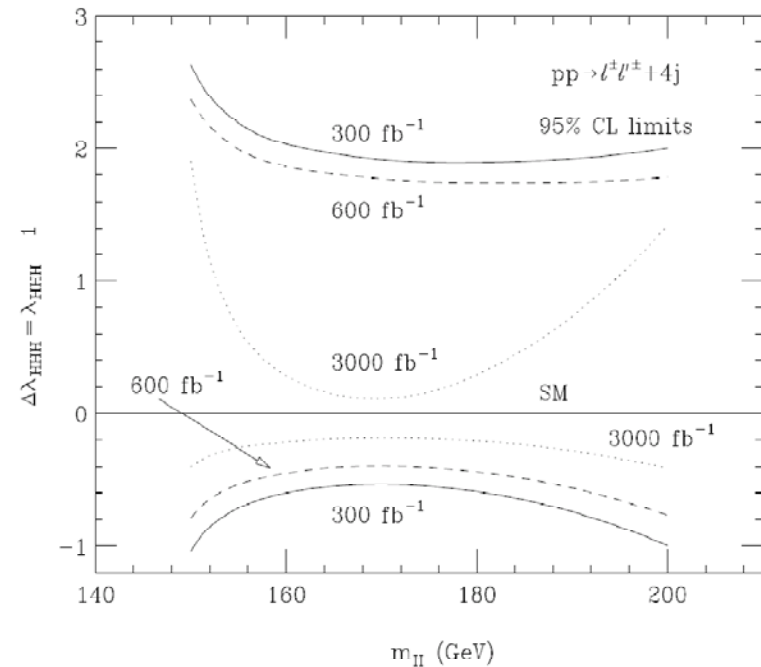
HHH measurement at LHC

- Decays into gauge boson pairs
- Hopeless for a light H
- Intermediate masses:
Non-vanishing of λ can be established at the LHC.



Precision measurement of the HHH coupling is business of the ILC.

$$pp \rightarrow HH \rightarrow W^+W^-W^+W^- \rightarrow \ell^\pm \ell'^\pm + 4j$$

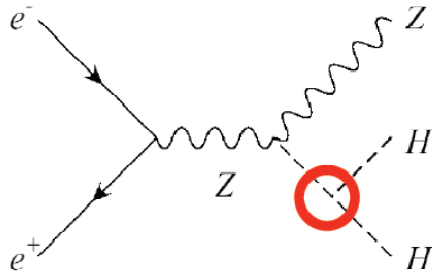


Bauer, Plehn, Rainwater

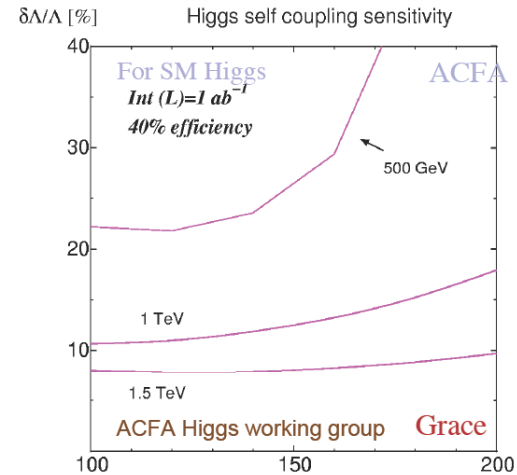
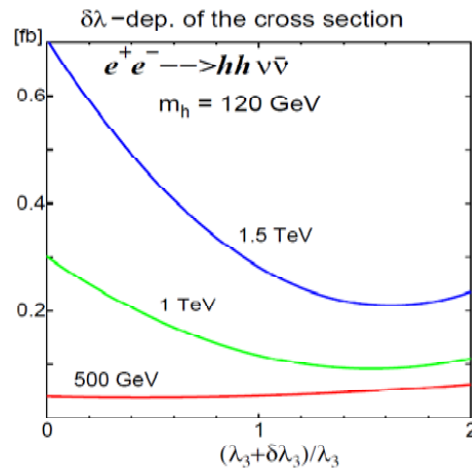
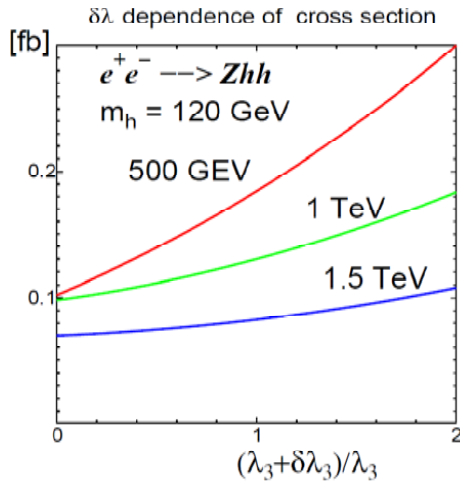
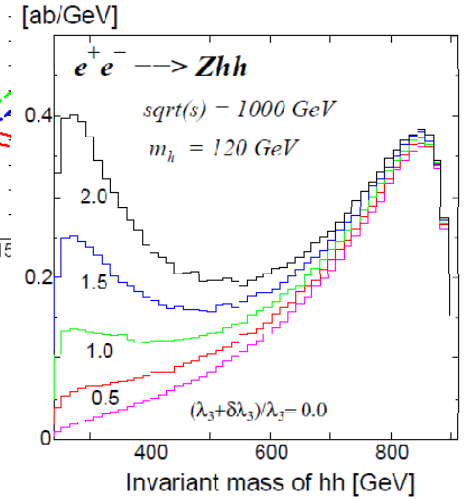
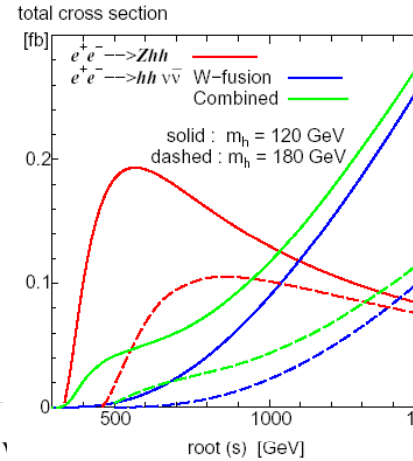
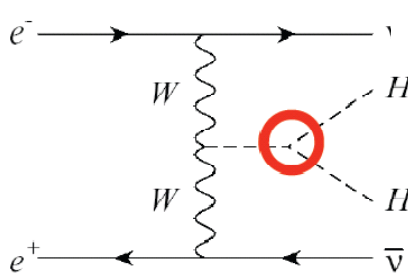
Measurement at the ILC

1st stage $\sqrt{s} = 500$ GeV
 2nd stage $\sqrt{s} = 1$ TeV
 $\int \mathcal{L} = 0.5 - 1 \text{ ab}^{-1}$

HH-strahlung



HH-fusion



ACFA Higgs Working Group 2002

$\mathcal{O}(10 - 20)\%$

Study HHH at a photon collider

$$\gamma\gamma \rightarrow HH$$

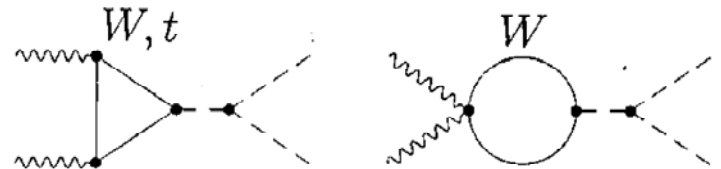
Difference from ZHH and HH $\nu\nu$ production at ILC

– Two body final state

- There is kinematical advantage, even though a loop suppression and also even though $L_{\gamma\gamma} \sim L_{e^+e^-}/3$

– Loop induced process

- New physics loop correction to the $\gamma\gamma H$ (loop induced) couplings can be $O(1)$.
- Different $\delta\lambda$ dependences from e^+e^- collision \Rightarrow different sensitivity property

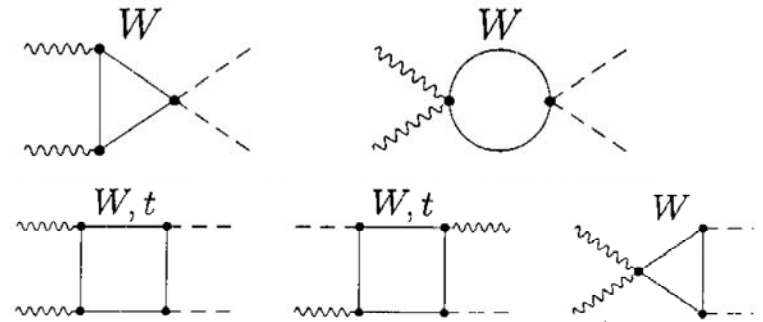
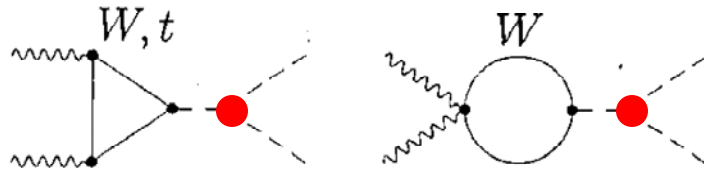


– Helicity amplitude

We can select a best helicity set to measure HHH.

Process $\gamma\gamma \rightarrow HH$

SM diagrams



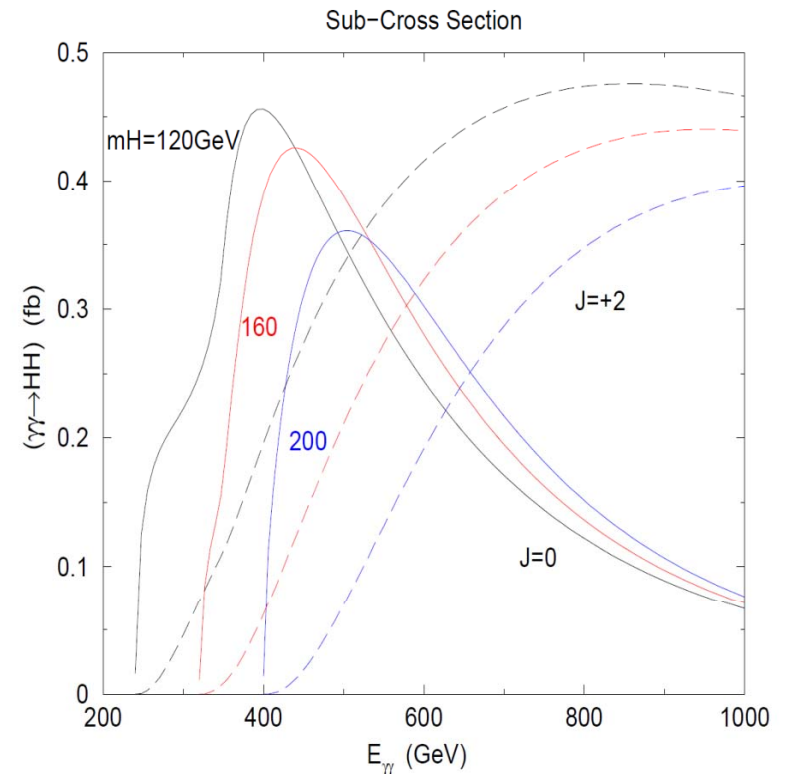
Helicity amplitudes

$$\mathcal{M}(\lambda_1, \lambda_2) = \mathcal{M}(-\lambda_1, -\lambda_2)$$

$$\mathcal{M}(+, +) = \text{pole} + \text{box}(+, +) \quad J_z = 0$$

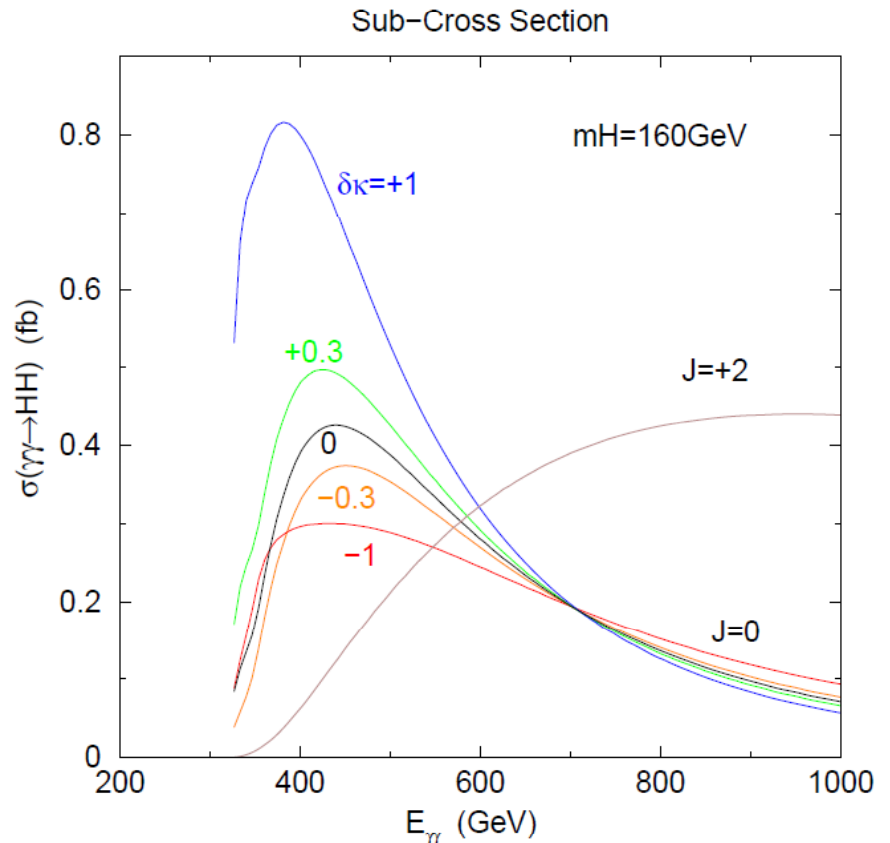
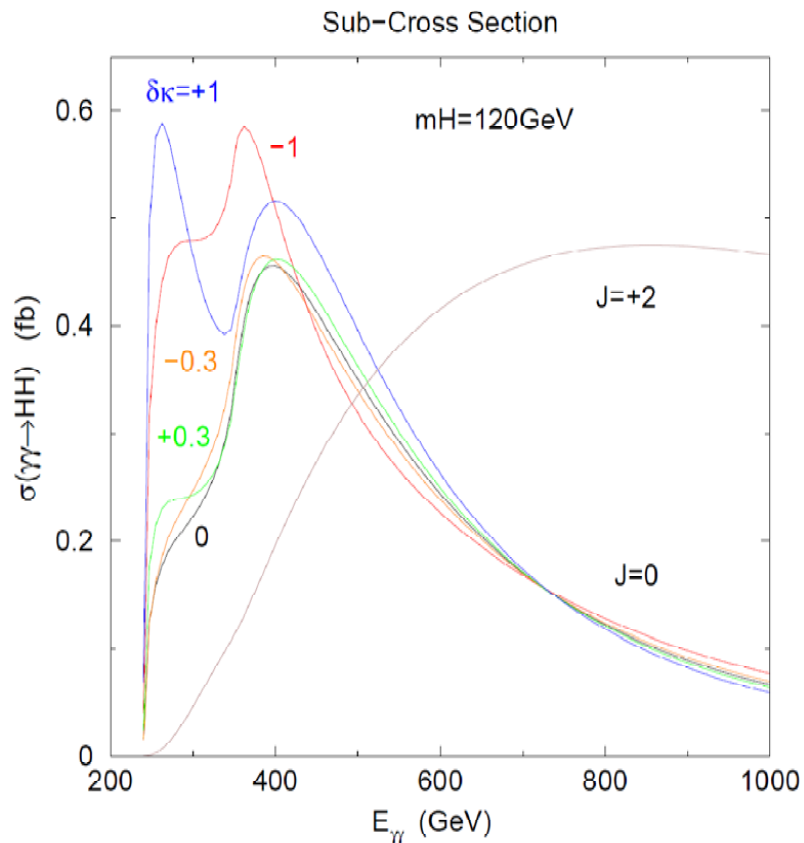
$$\mathcal{M}(+, -) = \text{box}(+, -) \quad J_z = +2$$

$$\frac{d\sigma(\lambda_1, \lambda_2)}{dt} = \frac{\alpha^2 \alpha_W^2}{32\pi s^2} |\mathcal{M}(\lambda_1, \lambda_2)|^2$$



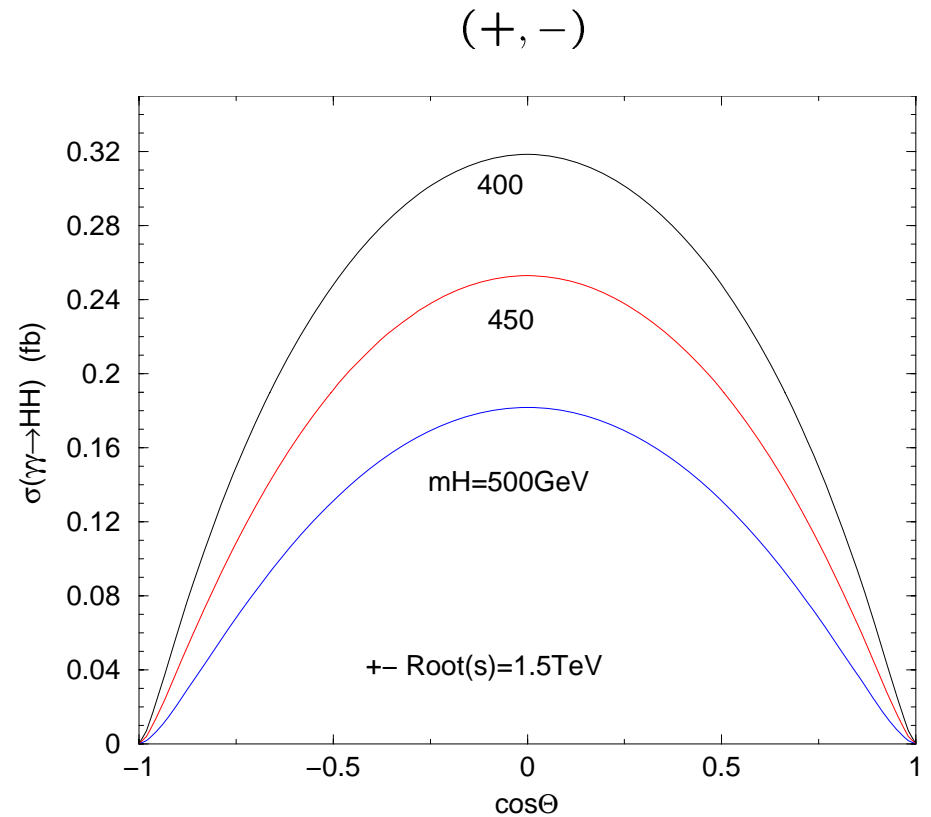
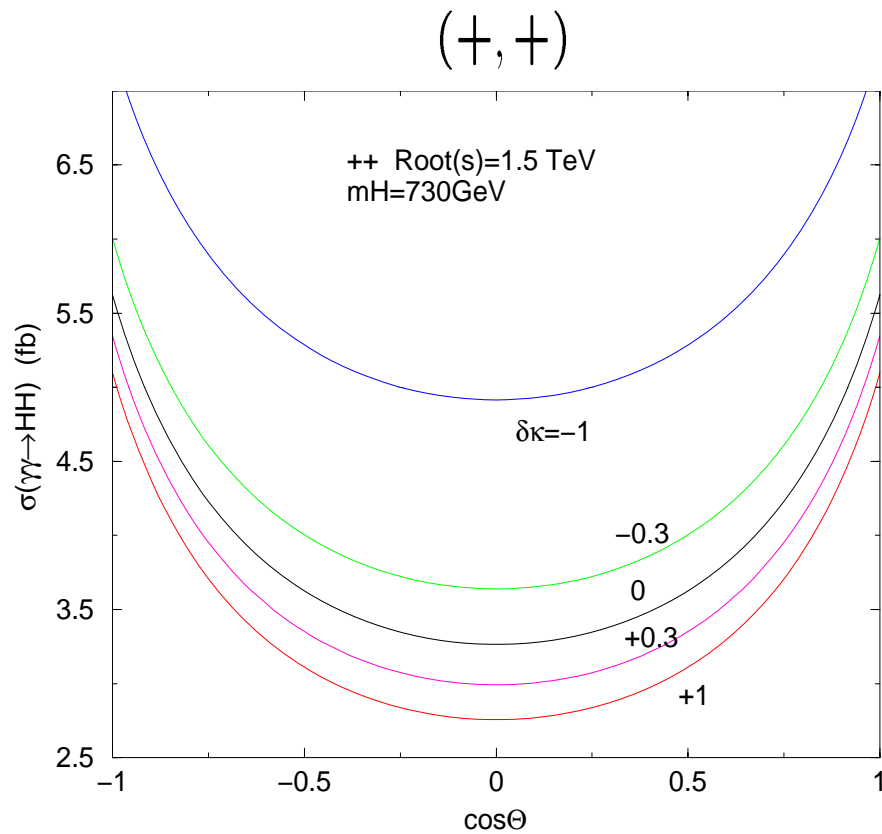
Anomalous HHH coupling

$$\lambda = \lambda^{\text{SM}}(1 + \delta\kappa)$$



Sub cross section is more sensitive to $\delta\kappa$ for heavier H.

Sub-Process



Anomalous coupling parameter $\delta\kappa$

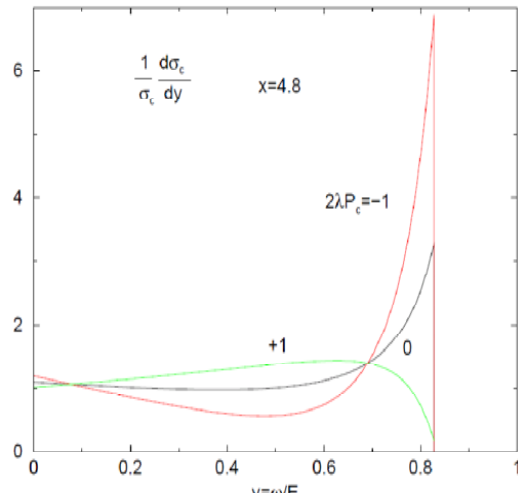
$$\lambda = \lambda^{\text{SM}} (1 + \delta\kappa)$$

$\delta\kappa$ changes cross sections, but
does not affect angular distribution

Full Cross Section

Photon structure function

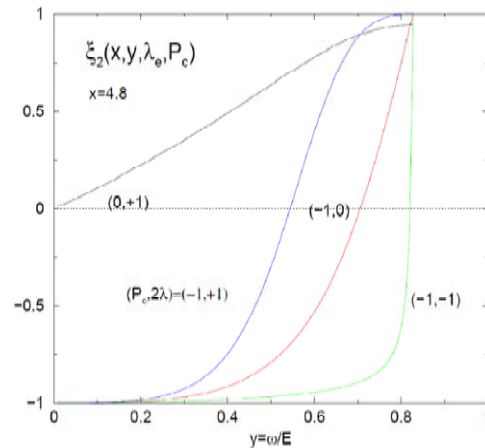
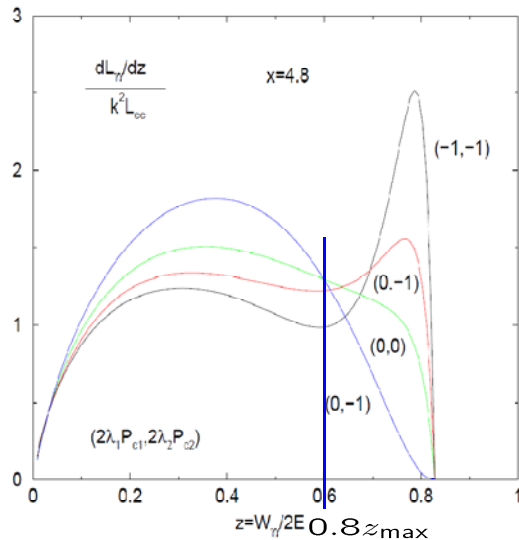
Ginzburg, et. al



$$d\sigma = \int_{\tau/y_m}^{y_m} d\tau \frac{dL_{\gamma\gamma}}{d\tau} \left(\frac{1 + \langle \xi_2^{(1)} \xi_2^{(2)} \rangle}{2} d\hat{\sigma}(+, +) + \frac{1 - \langle \xi_2^{(1)} \xi_2^{(2)} \rangle}{2} d\hat{\sigma}(+, -) \right)$$

$$\frac{L_{\gamma\gamma}}{d\tau} = \int_{\tau/y_m}^{y_m} \frac{dy}{y} f_\gamma(x, y) f_\gamma(x, \tau/y)$$

$$\tau = \hat{s}/s, y = E_\gamma/E_e \quad y_m = \frac{x}{1+x}, x = \frac{4E_e\omega_0}{m_e^2}$$



$\langle \xi_2 \rangle$: mean polarization of the γ beam

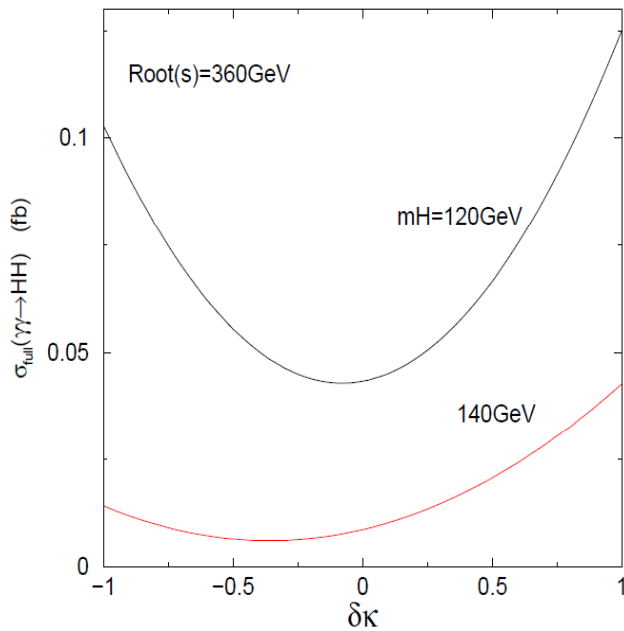
λ_e : electron helicity

P_c : laser photon

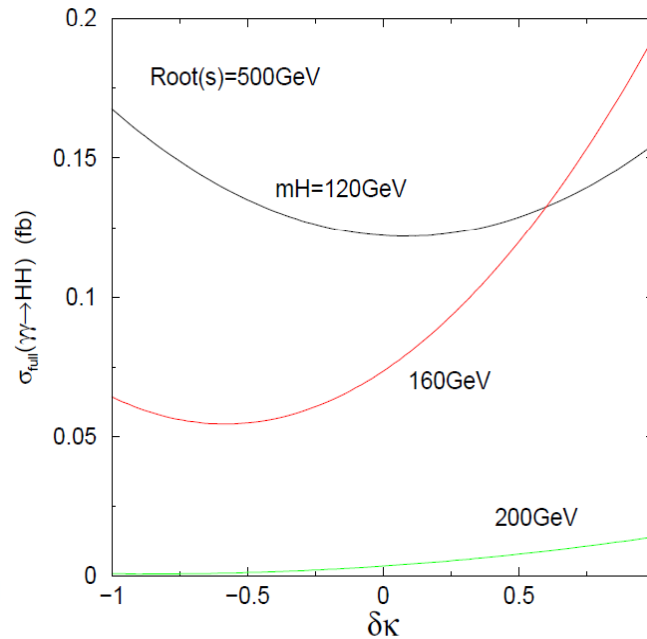
mean helicity

Full cross section ($\delta\kappa$ dependences)

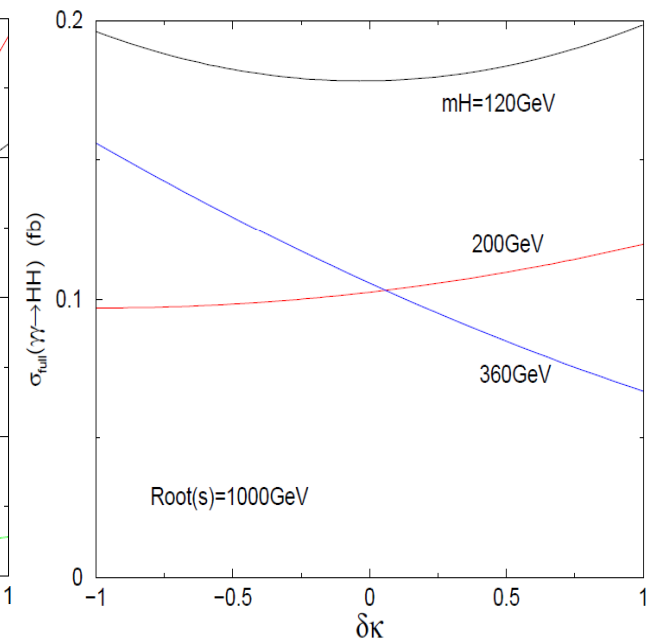
$$\sqrt{s_{ee}} = 360\text{GeV}$$



$$\sqrt{s_{ee}} = 500\text{GeV}$$



$$\sqrt{s_{ee}} = 1000\text{GeV}$$



pole > box

pole < box

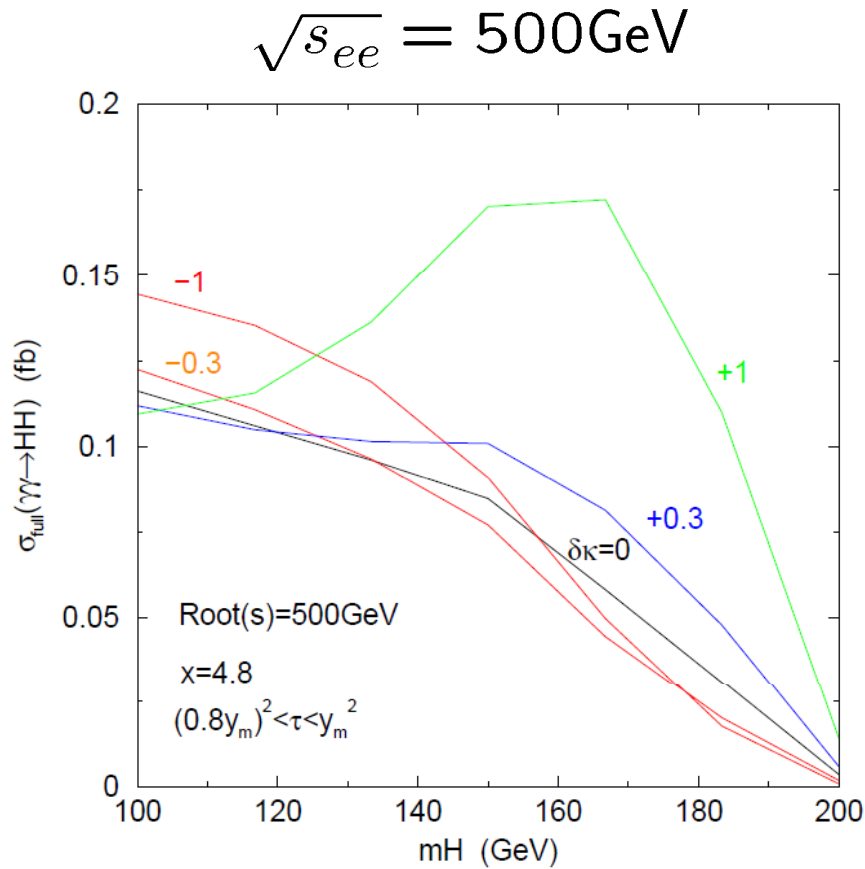
Anomalous coupling parameter $\delta\kappa$

$$\lambda = \lambda^{\text{SM}}(1 + \delta\kappa)$$

Sensitivity to $\delta\kappa$ can be large depending on parameters

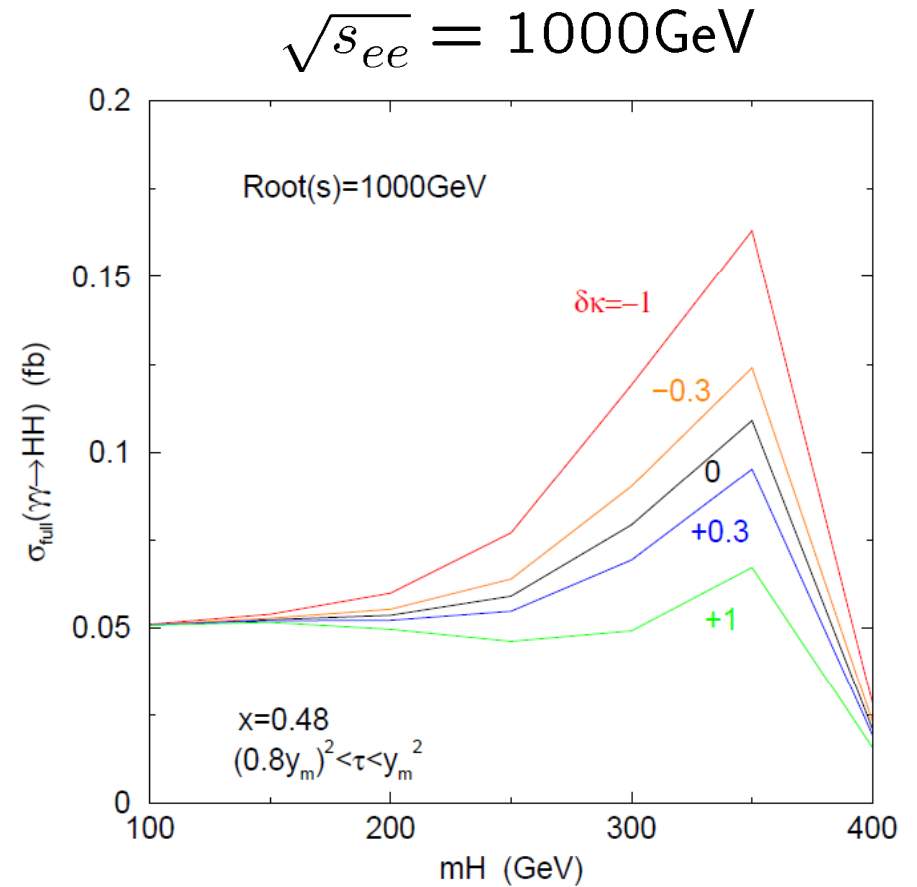
$$\begin{aligned} \lambda_{e_1} &= \lambda_{e_2} = 0.45 \\ \lambda_{\gamma_1} &= \lambda_{\gamma_2} = -1 \end{aligned}$$

Full Cross Section 2

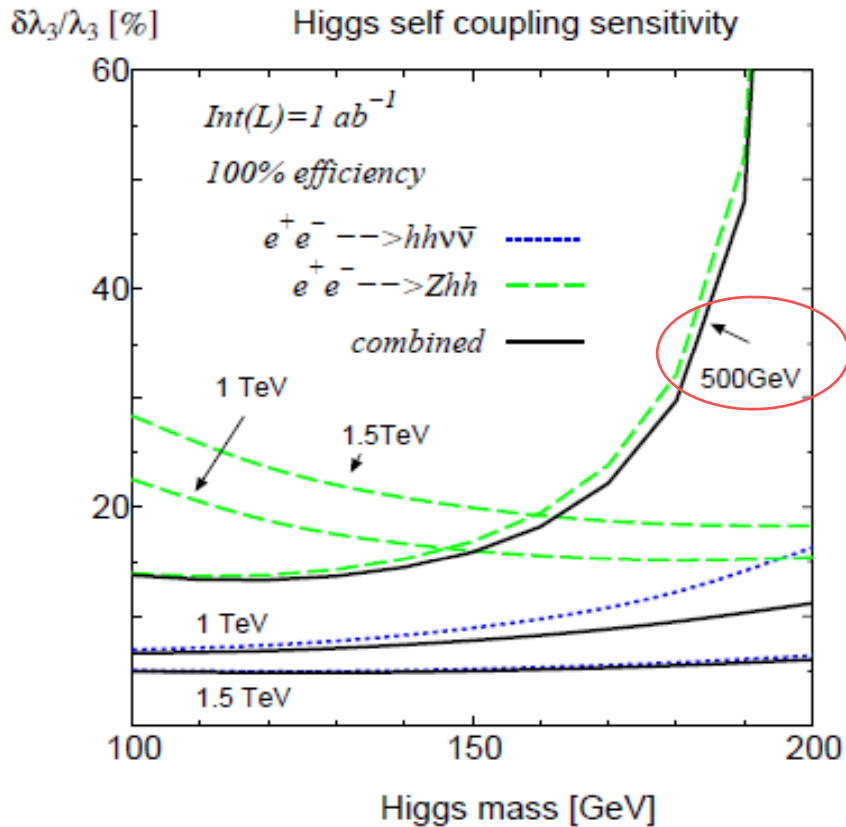


$$\lambda_{e_1} = \lambda_{e_2} = 0.45$$

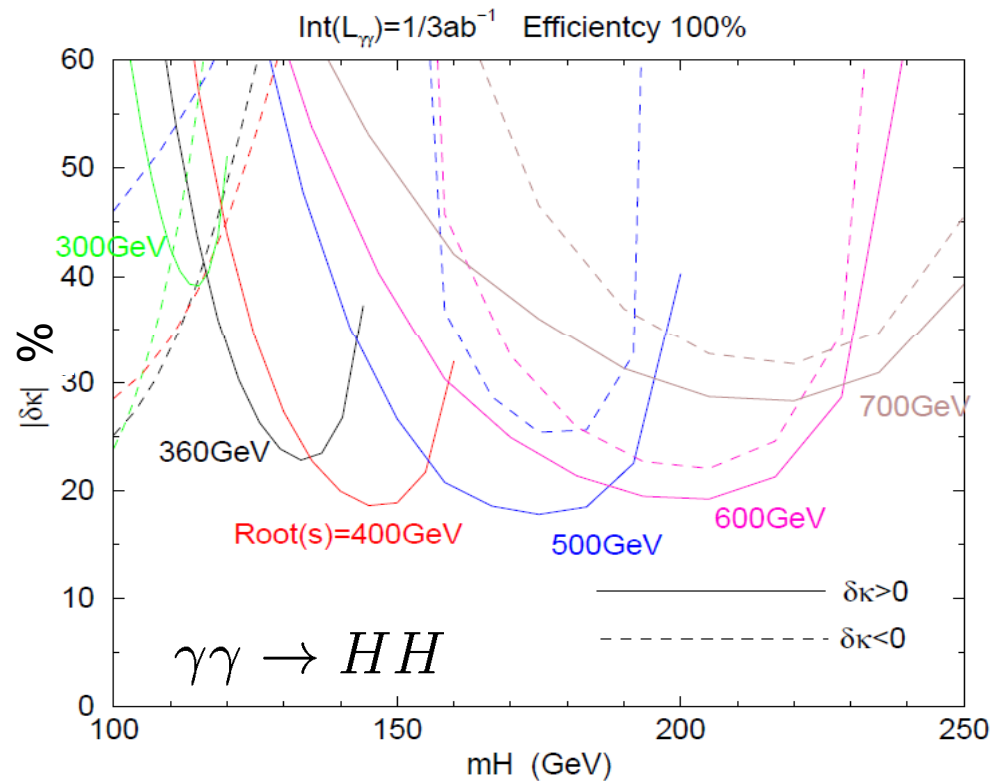
$$\lambda_{\gamma_1} = \lambda_{\gamma_2} = -1$$



Estimation of HHH sensitivity



Higgs self coupling sensitivity



For relatively low e^+e^- (e^-e^-) energies ($\sqrt{s} < 500$ GeV), sensitivity is larger in e^+e^- process for $m_H < 150$ GeV, but $\gamma\gamma \rightarrow HH$ can be useful for higher values of m_H .

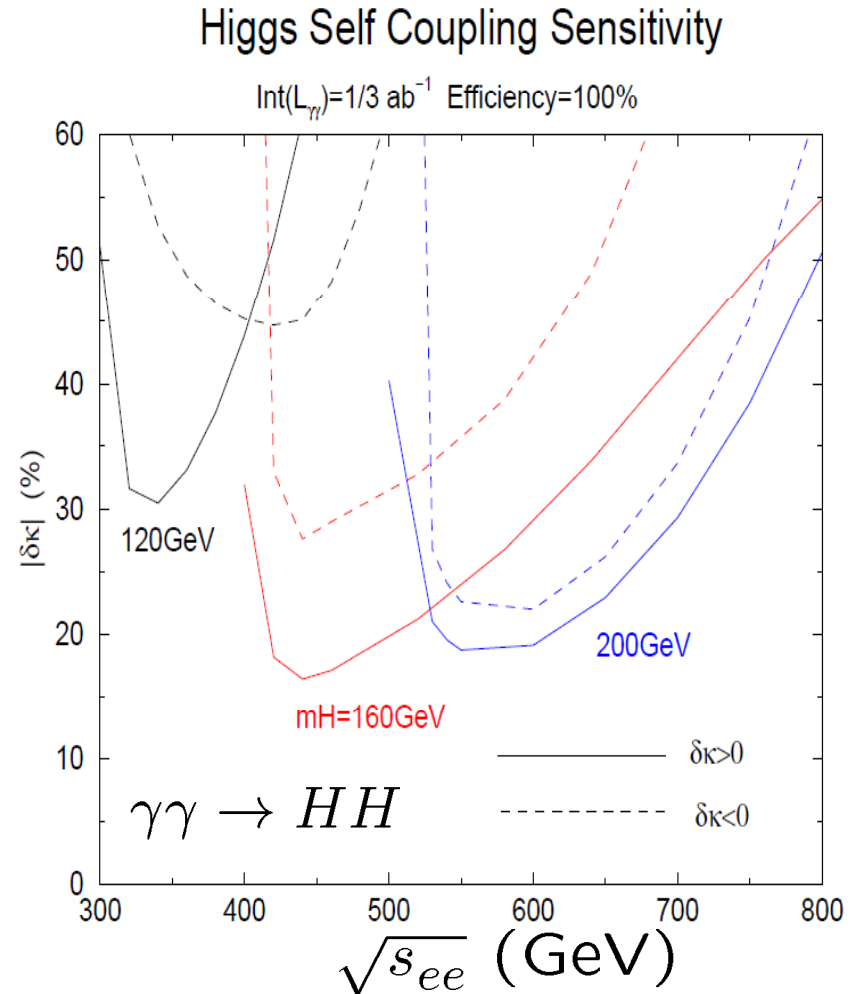
$$\lambda_{e_1} = \lambda_{e_2} = 0.45$$

$$\lambda_{\gamma_1} = \lambda_{\gamma_2} = -1$$

Estimation of HHH sensitivity

- At the ILC, energies of initial electron and laser can be changed.
- After H is found, m_H is known. Then we can examine the HHH coupling by selecting the best E_{ee} .

$$m_H \approx \frac{x}{x+1} \sqrt{s_{ee}} \times 0.8 = 0.33 \times \sqrt{s_{ee}}$$



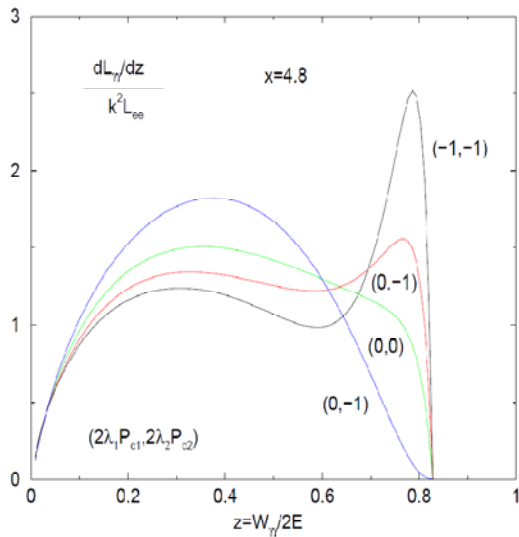
Summary

- Higgs self-coupling (HHH)
 - Nature of SSB (Higgs potential)
 - Probe of new physics, EWPT
- HHH measurements
 - LHC: Difficult
 - ILC: ZHH (better for lighter H), $\nu\nu$ HH (better for lighter E)
- HHH at $\gamma\gamma$ collider $\gamma\gamma \rightarrow HH$
 - Result is consistent with previous works in the SM. [Jikia, Belusevic](#)
 - Sensitivity study
 - A $\gamma\gamma$ collider ($E_{ee} < 500\text{GeV}$) may be useful to measure the HHH coupling especially for $m_H = 150\text{-}200\text{GeV}$.
 - Simulation

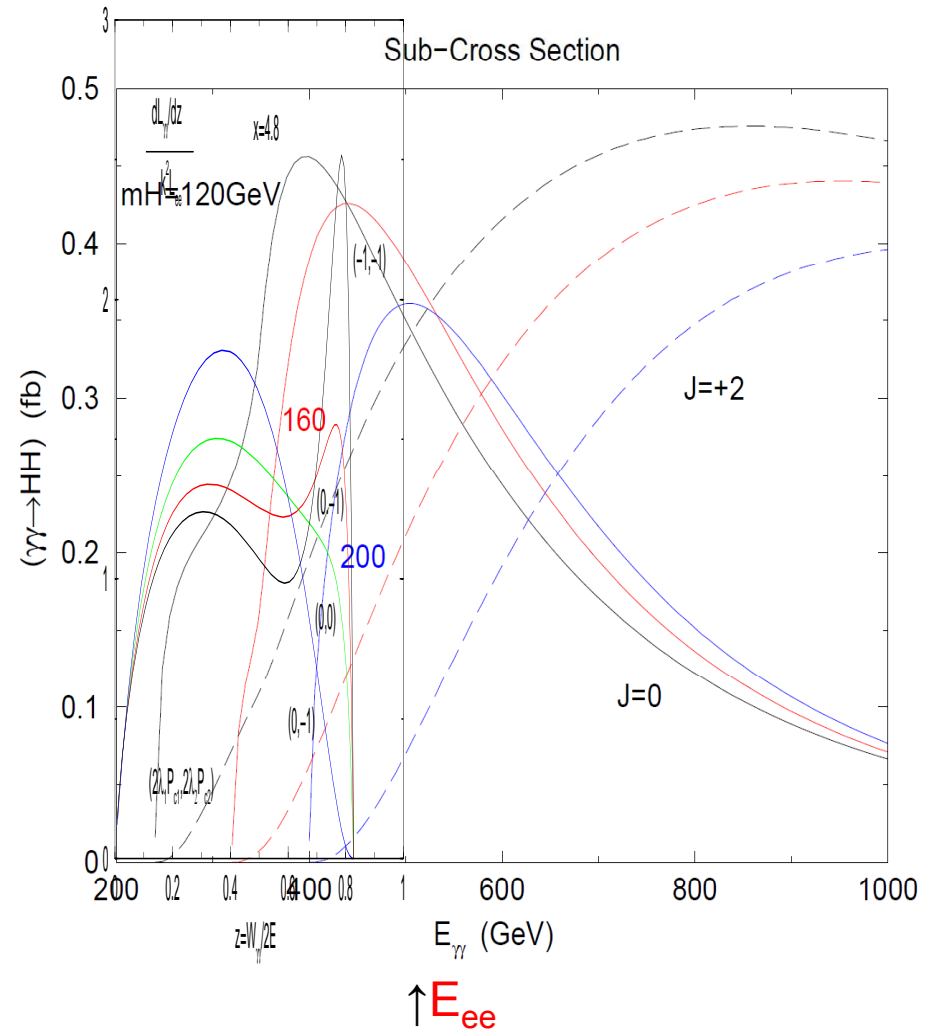
The best E_{ee} for each m_H

$m_H=160$ GeV

Full Cross Section becomes large for $E_{ee}=450-500$ GeV



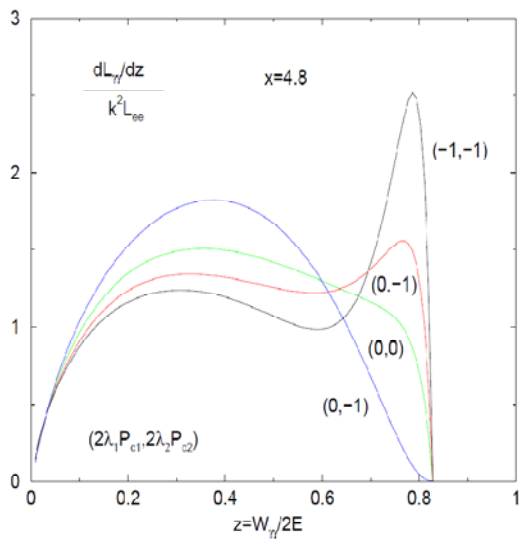
Photon Structure Function



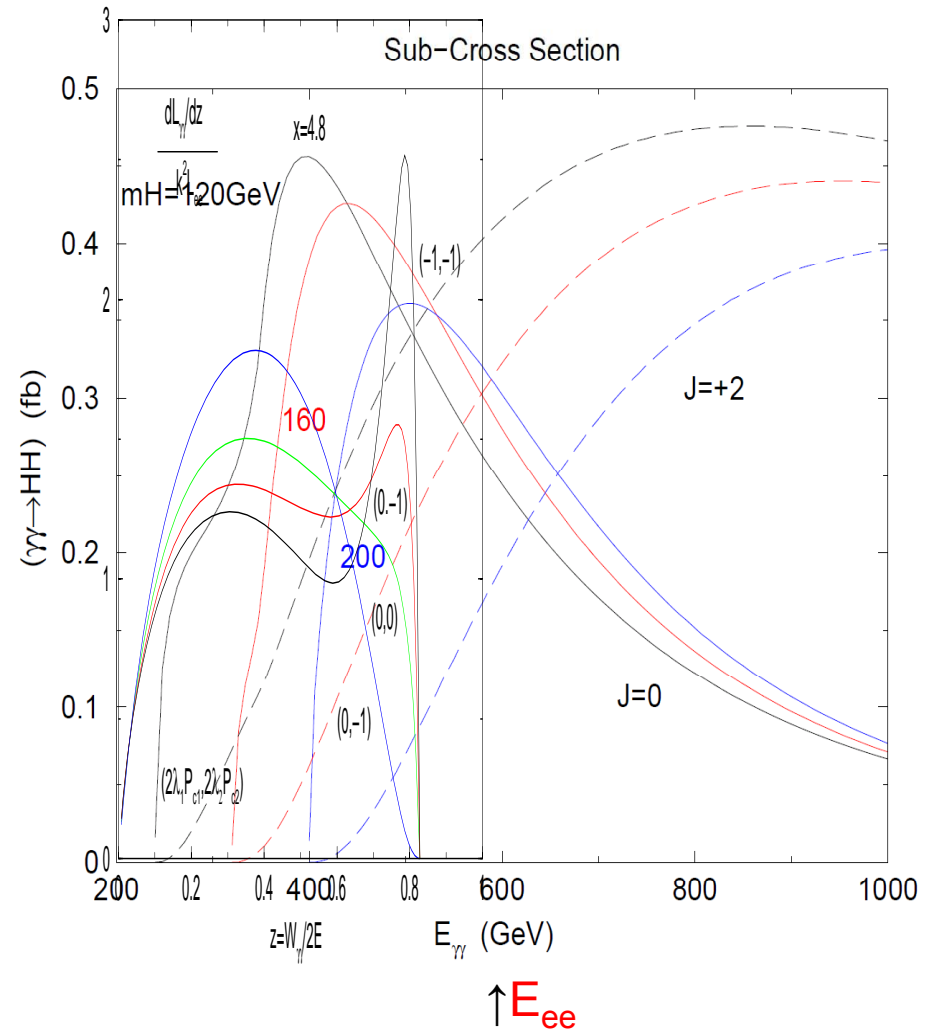
The best E_{ee} for each m_H

$m_H=200\text{GeV}$

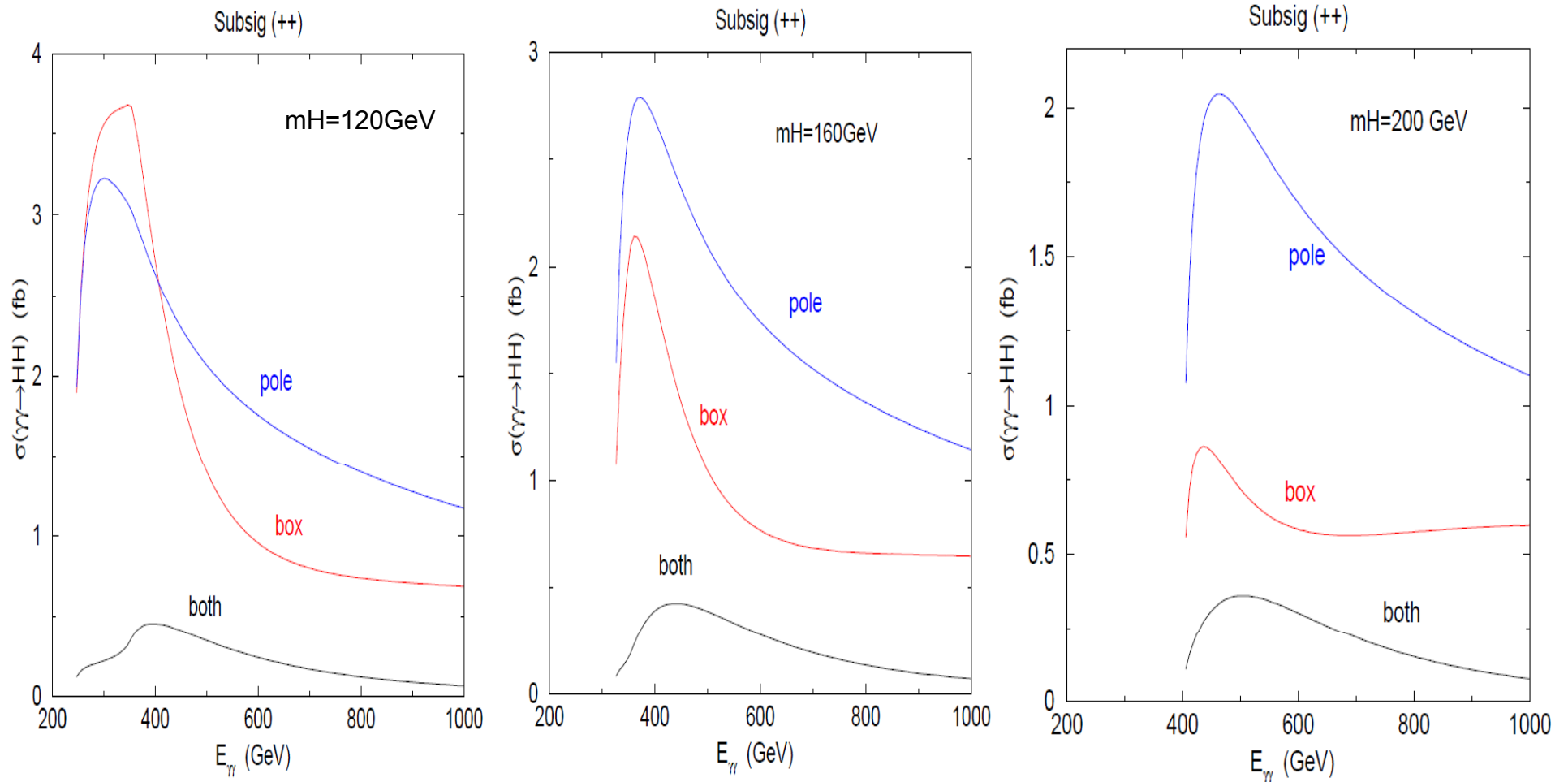
Full Cross Section becomes large for $E_{ee}=550\text{-}600\text{ GeV}$



Photon Structure Function



Pole vs Box (J=0)



Large destructive cancellation between pole and box contributions.
Pole contribution becomes dominant for larger M_H values.

New Physics effects on

$$\gamma\gamma \rightarrow HH$$

- New physics loop effect can be large, because the SM contributions are also loop-induced.

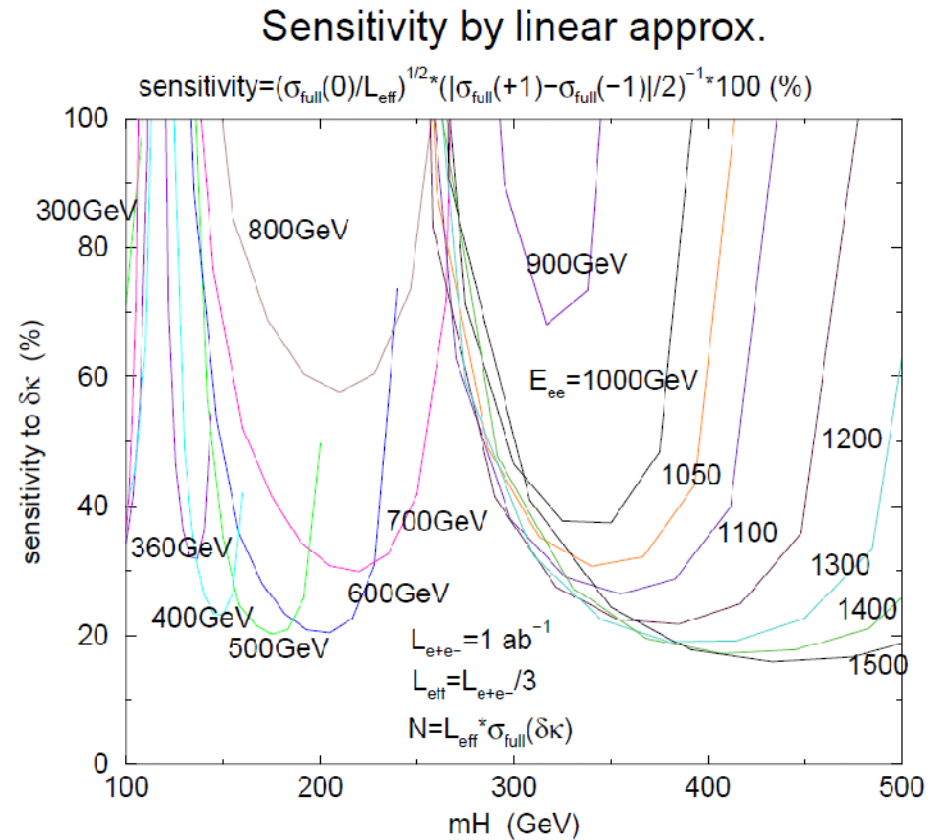
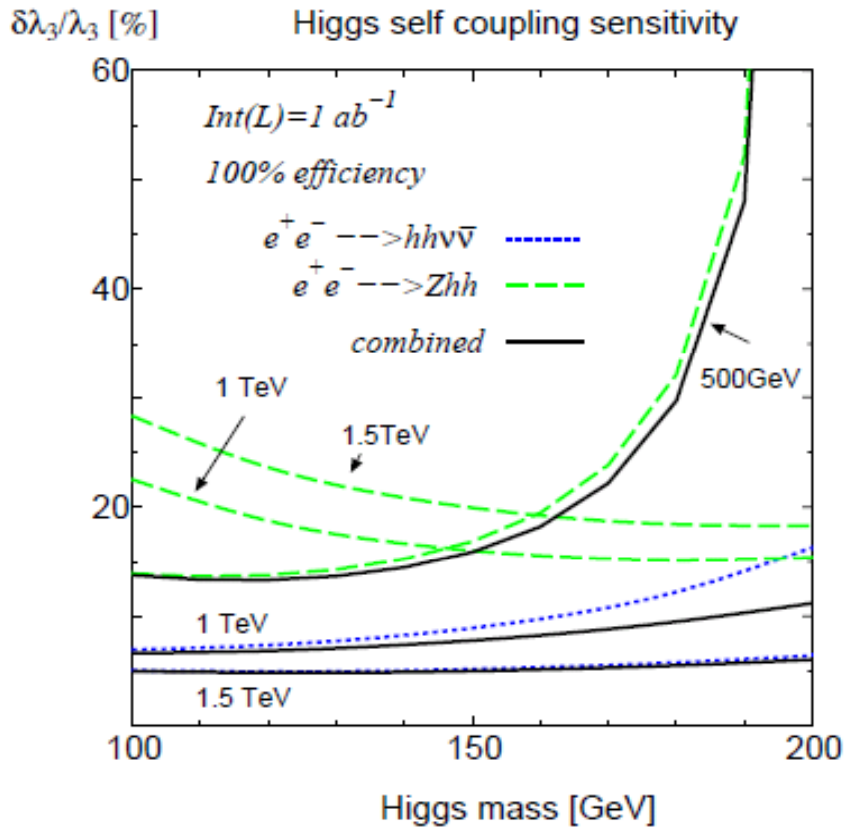
$$\mathcal{M}(\text{pole}) = (\mathcal{M}_{\text{SM}}^{\text{loop}} + \mathcal{M}_{\text{NEW}}^{\text{loop}}) \frac{1}{\hat{s} - m_H^2} (\lambda + \delta\lambda)$$

- New Physics contribution changes not only the size of the cross section but also (delicate) balance between the pole and the box diagrams.

$$\begin{aligned} |\mathcal{M}(+, +)|^2 &= |A(\lambda + \delta\lambda) + B|^2 \\ &= |A| \delta\lambda^2 + 2|A| |A\lambda + B| \delta\lambda + |A\lambda + B|^2 \end{aligned}$$

HHH sensitivity could greatly depend on the model

Backup Slide 1



For relatively low e^+e^- (e^-e^-) energies ($\sqrt{s} < 500-600$ GeV), sensitivity is larger in e^+e^- process for $m_H < 150$ GeV, but $\gamma\gamma \rightarrow HH$ can be useful for higher values of m_H .

Backup Slide 2

- Sensitivity

$$N = L_{\gamma\gamma}\sigma(0)$$

$$N \pm \sqrt{N} = L_{\gamma\gamma}\sigma(\Delta\kappa)$$

$L_{\gamma\gamma}\sigma(\delta\kappa)$

