

# Discriminating Spin Through Quantum Interference

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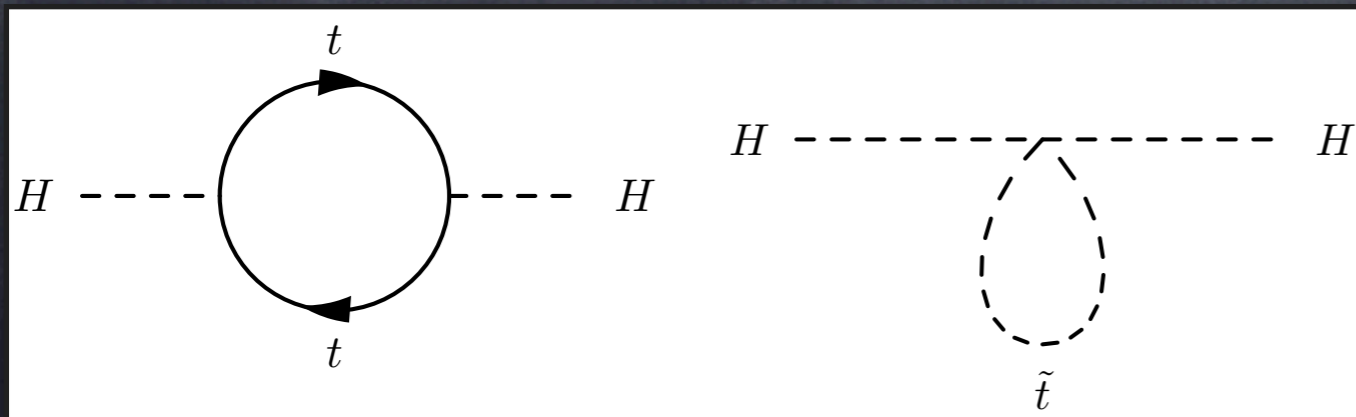


# Beyond the SM

- Naturalness and hierarchy problems
  - Suggest some new physics at  $\sim 1$  TeV

## Supersymmetry? Technicolor? Extra Dimensions?

- Supersymmetry solves naturalness problem by introducing new-particles with opposite spin statistics to cut off loop corrections.
- Universal Extra Dimensions solves the problem by having a TeV-scaled extra dimension. That is, the Planck scale is the EW scale



$$M_{Pl}^2 = M^{2+d} (2\pi R)^d$$



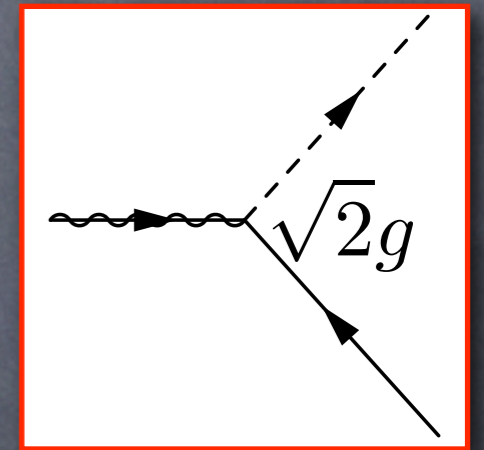
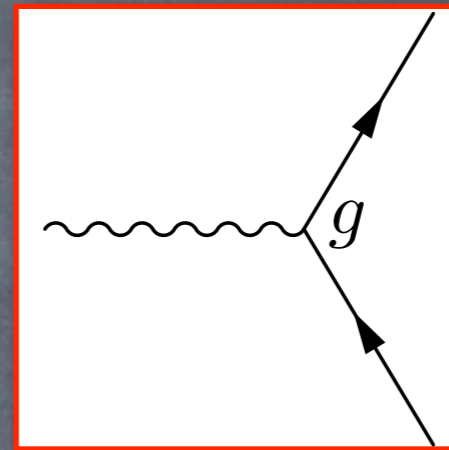
# SUSY vs. UED

- Both spectra contain 'copies' of SM

- SUSY has superpartners

- UED has tower of Kaluza-Klein modes

- New particles have similar interaction strengths:



$$\begin{aligned}
 W^\pm, Z, A &\rightarrow \tilde{W}^\pm, \tilde{Z}, \tilde{A} \quad (\tilde{\chi}_i^\pm, \tilde{\chi}_i^0) && \text{(SUSY)} \\
 &\rightarrow W_1^\pm, Z_1, A_1, W_2^\pm, Z_2, A_2, \dots && \text{(UED)}
 \end{aligned}$$

Spin measurements may be the defining experimental difference



# Spin at LHC/ILC

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- Most methods attempt to distinguish specific models
  - Comparison of total cross sections:  $\sigma_{SUSY} < \sigma_{UED}$ 
    - Not a measurement of spin
  - Can look for  $KK > 1$  towers
    - Could be too heavy for colliders, could be seeing non-minimal SUSY states
- Threshold scans at ILC
  - Both spinors and vector bosons have  $\sigma \propto \beta$
- Production or decay angular dependence
  - Assumptions about t-channel, chiral couplings



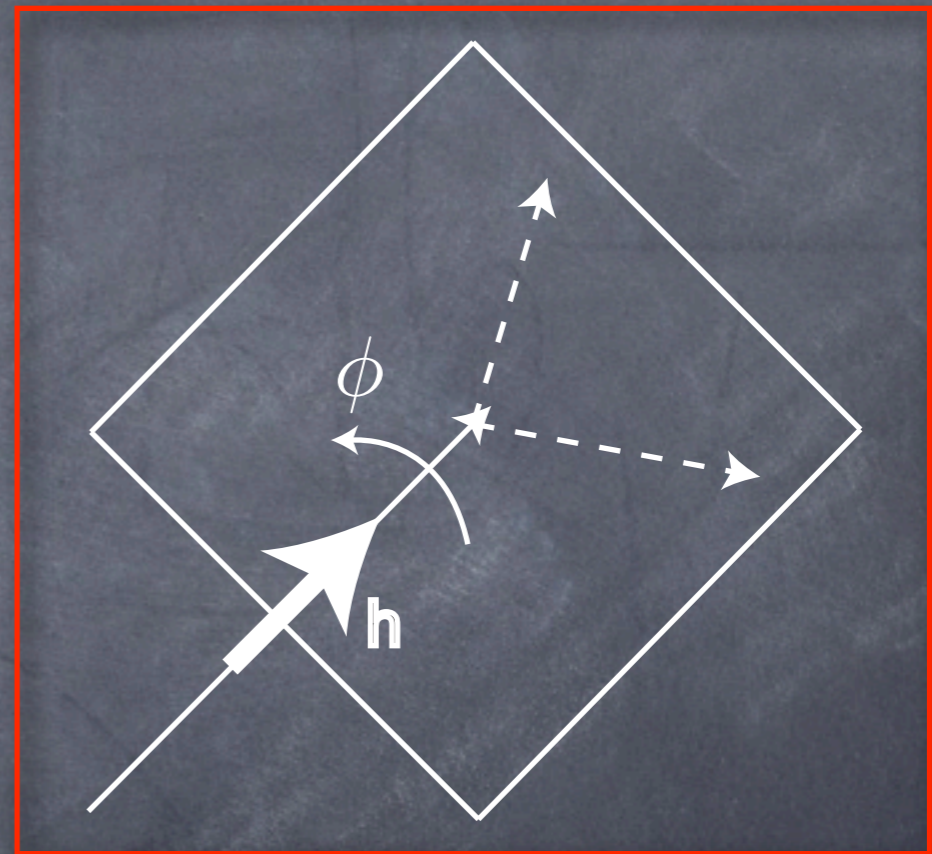
# Spin and Quantum Interference

- Decay of particle with helicity  $h$ :
- Rotation about z-axis of decay plane implies

$$\mathcal{M} \propto e^{iJ_z \phi}$$

$$J_z = \frac{(\vec{s} + \vec{x} \times \vec{p}) \cdot \vec{p}}{|\vec{p}|}$$

$$= \frac{\vec{s} \cdot \vec{p}}{|\vec{p}|} = h$$





# Spin and Quantum Interference

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- If particle produced in multiple helicities, then

$$\sigma \propto \left| \sum \mathcal{M}_{prod.} \mathcal{M}_{decay} \right|^2$$

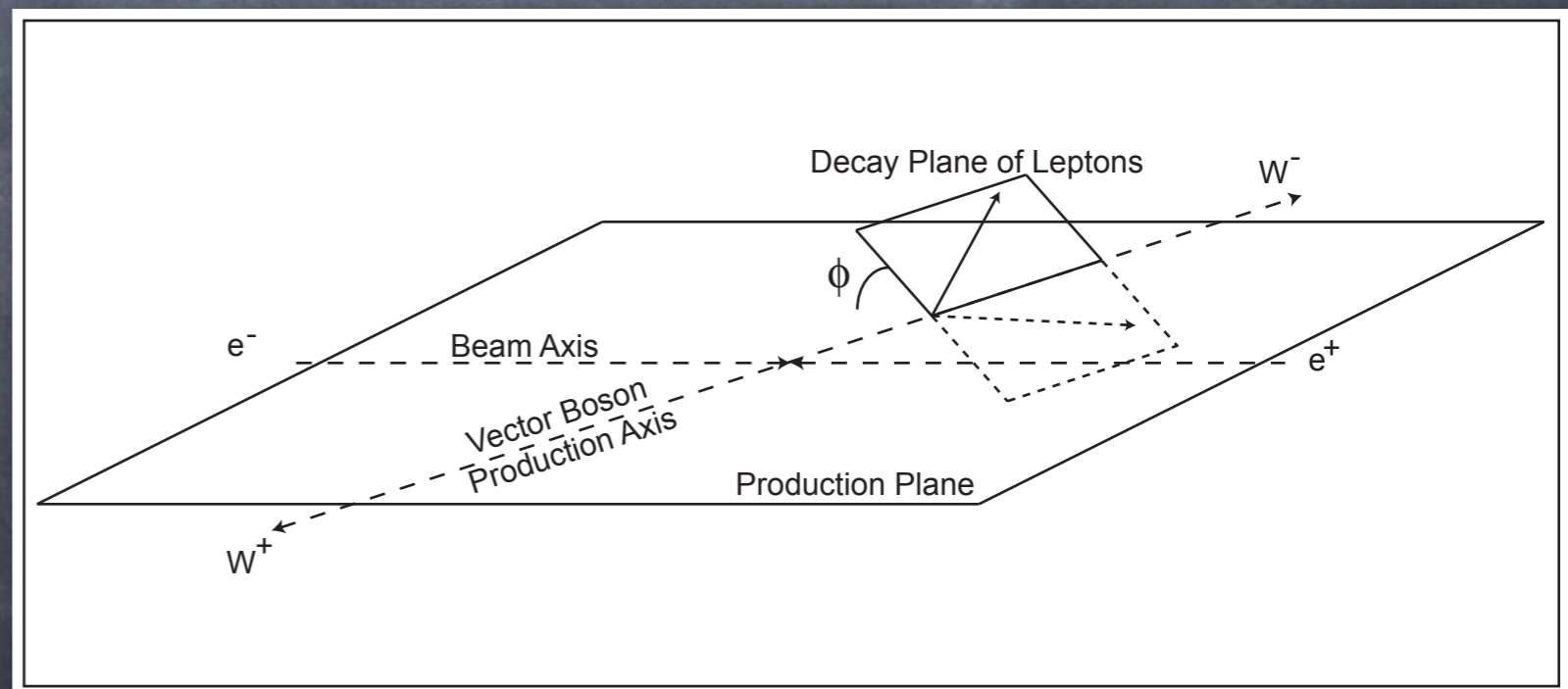
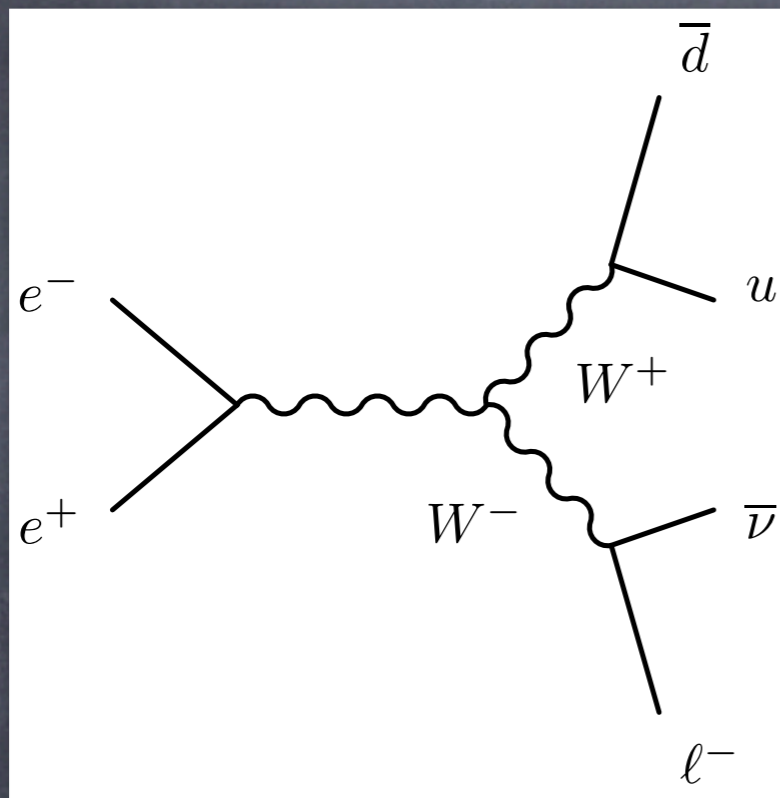
$$\mathcal{M}_{decay} = e^{ih\phi} \mathcal{M}_{decay}(h, \phi = 0)$$

- Different helicity states interfere as they decay
- The  $\phi$  dependence of cross section allows us to determine what helicities interfered.

$$\sigma = A_0 + A_1 \cos(\phi) + \cdots + A_n \cos(n\phi), \quad n = 2 \times \text{spin}$$



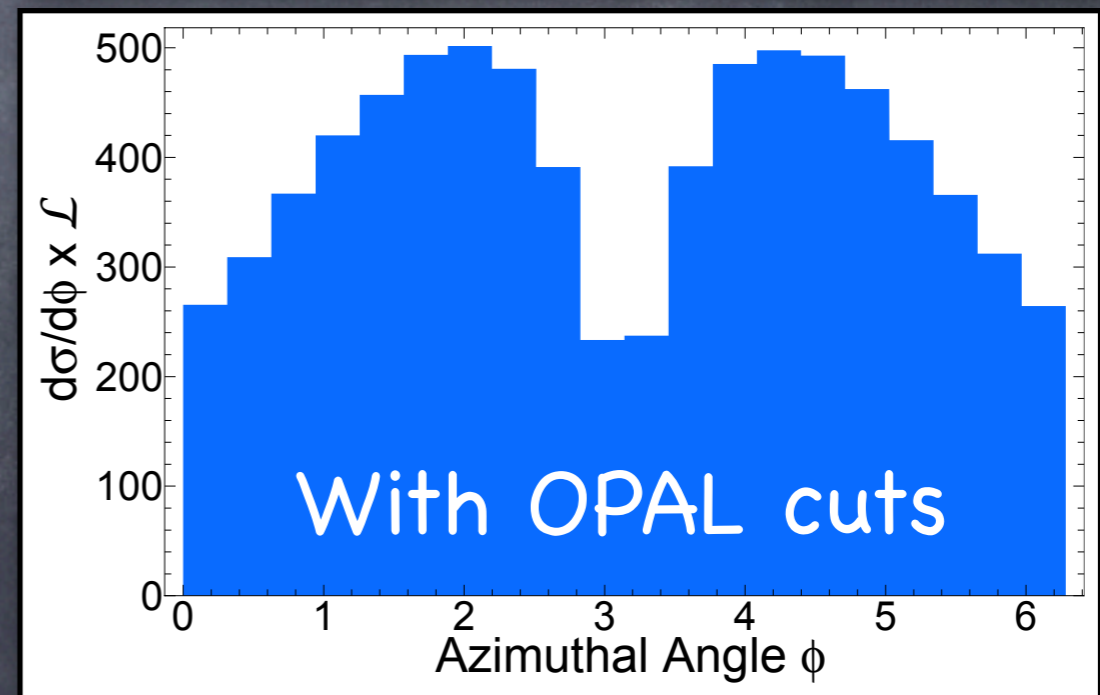
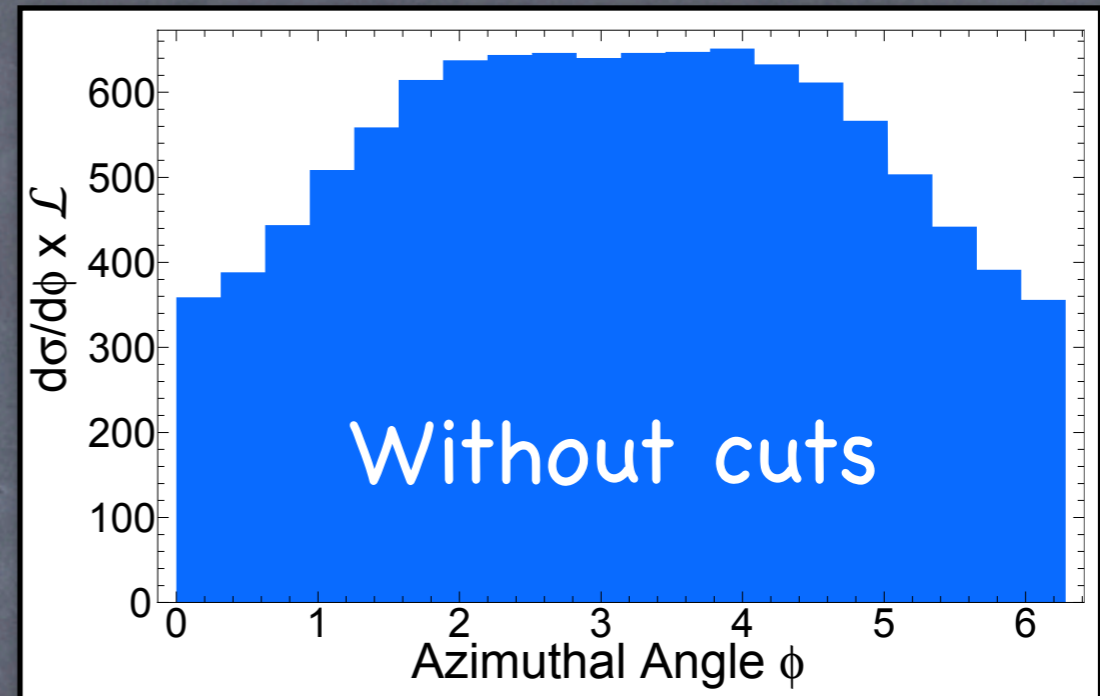
# Coherent Sums and Kinematics





# LEP II $W$ Pair Production

- Semi-leptonic decays, fully reconstructable
- Simulated OPAL data from 1997–2000:
  - $\mathcal{L} = 682 \text{ pb}^{-1}$
  - Before cuts have 3400 events available
  - 2450 events after cuts





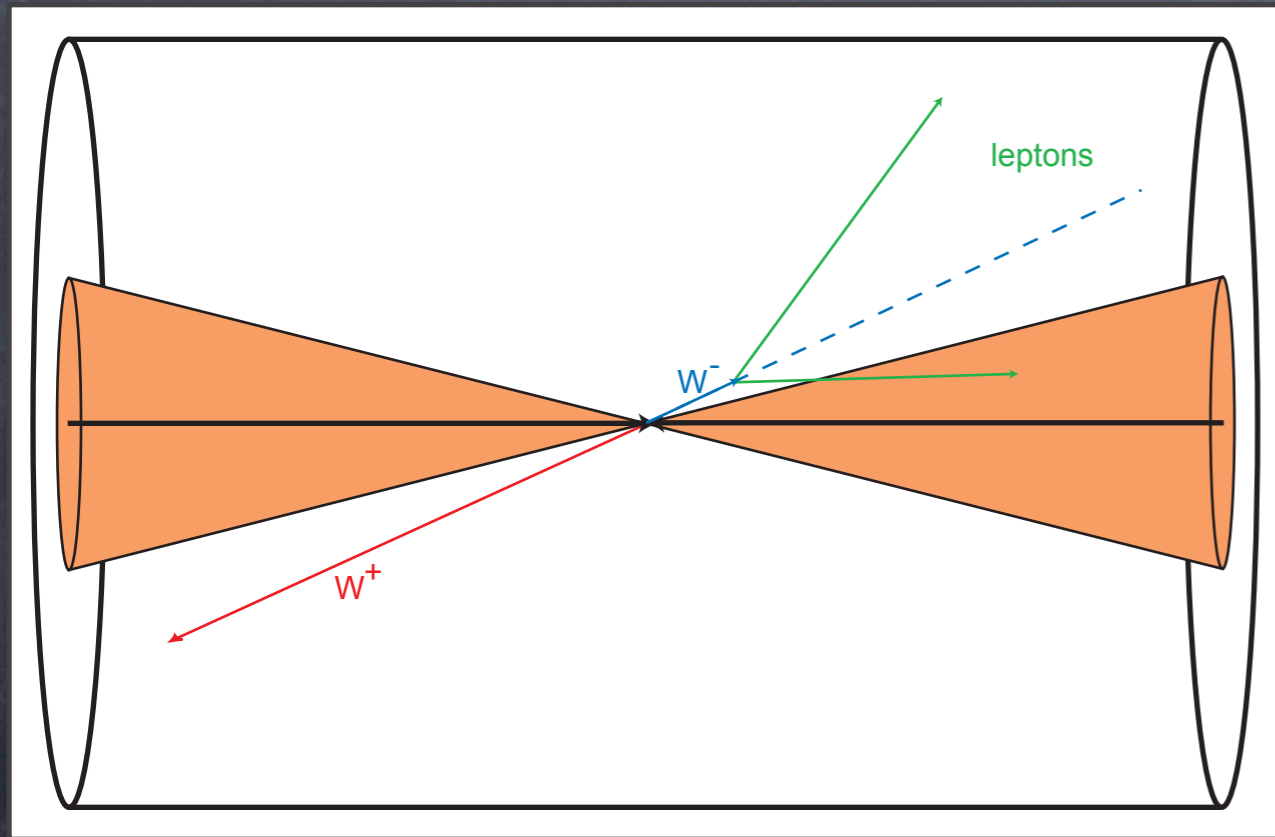
# LEP II $W$ Pair Production

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Problem is that  $E_T, \eta$  cuts are not azimuthally symmetric about  $W$ -boson axis

Rotationally invariant cuts: require that leptons pass acceptance cuts for all rotations about the  $W$ -boson axis

This cut is  $\sim 15\%$  efficient

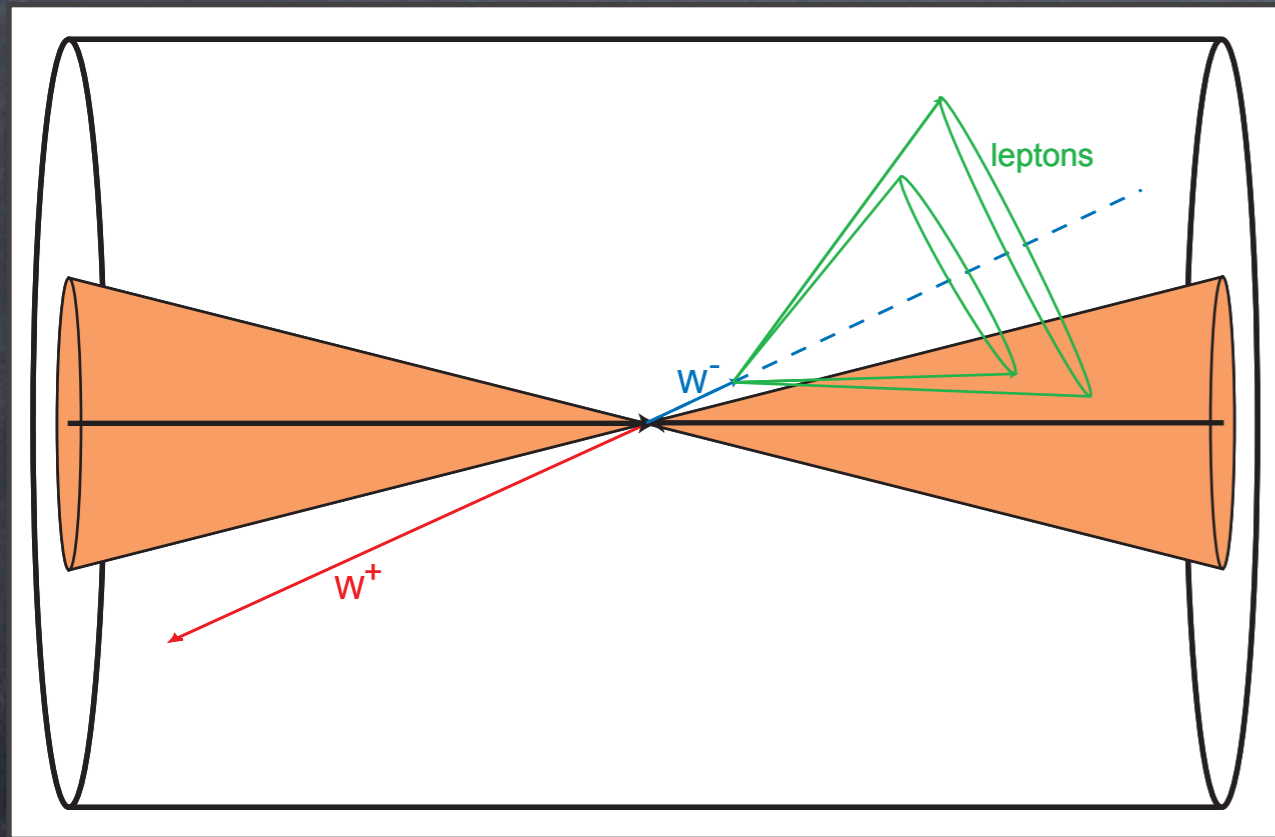




# LEP II $W$ Pair Production

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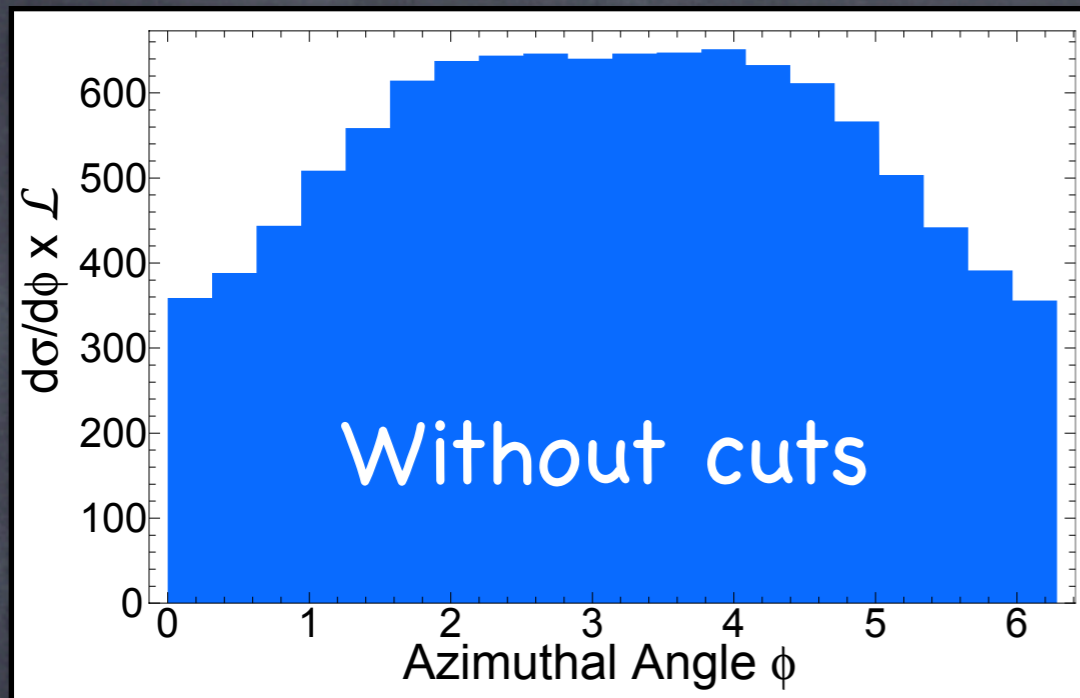


Rotationally invariant cuts: require that leptons pass acceptance cuts for all rotations about the  $W$ -boson axis

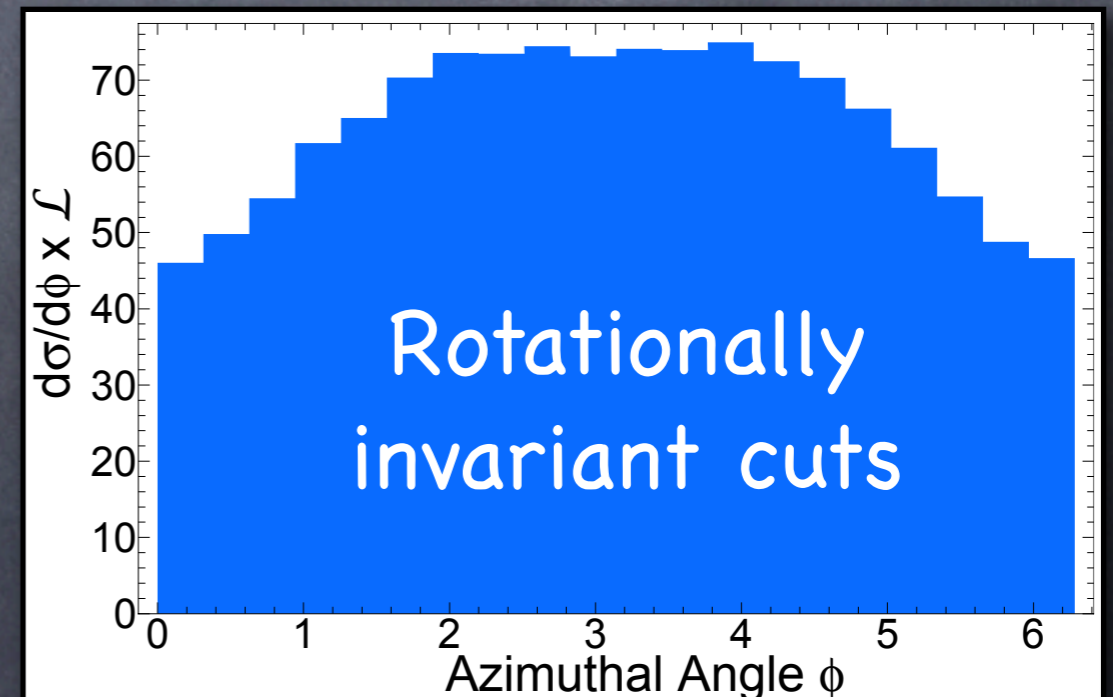
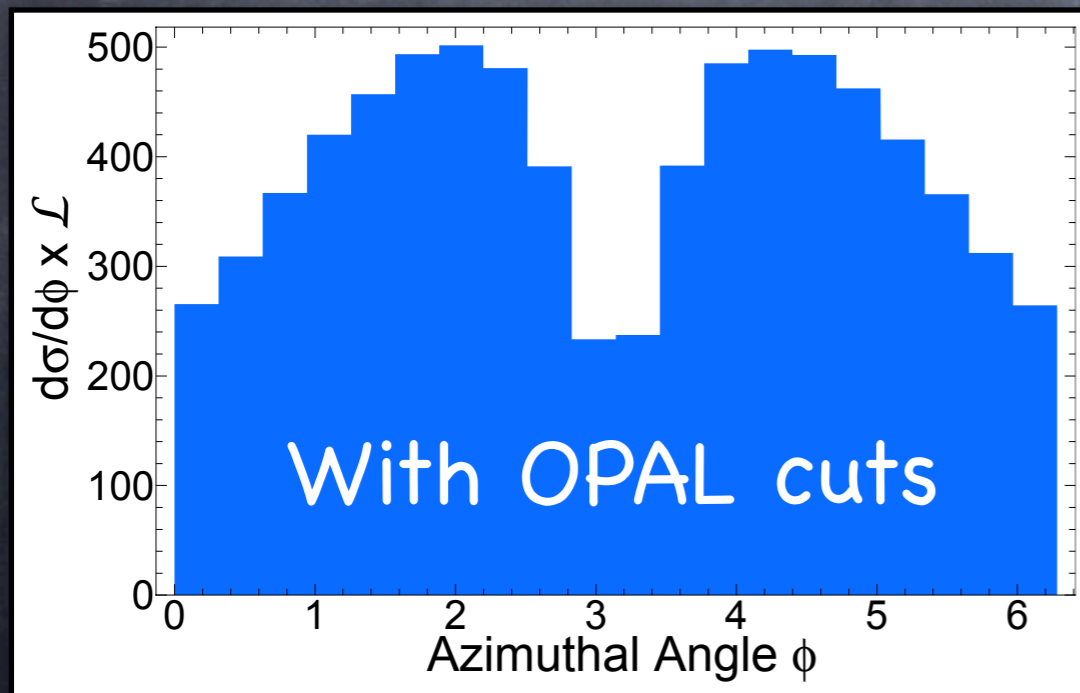
This cut is  $\sim 15\%$  efficient



# LEP II $W$ Pair Production



$A_1/A_0$	$-0.211 \pm 0.050$
$A_2/A_0$	$-0.081 \pm 0.049$
$A_3/A_0$	$0.000 \pm 0.057$
$A_4/A_0$	$0.000 \pm 0.057$





# Scalar vs. Spinor at ILC

$$\begin{aligned} e^- e^+ &\rightarrow \tilde{\mu}_R^+ \tilde{\mu}_R^- \rightarrow \mu^+ \mu^- \tilde{\chi}_0^1 \tilde{\chi}_0^1 \\ e^- e^+ &\rightarrow \mu_{1R}^+ \mu_{1R}^- \rightarrow \mu^+ \mu^- B_1 B_1 \end{aligned}$$

- Many SM extensions have new particles charged under additional symmetry (R-parity for SUSY, T-parity for Little Higgs,  $Z_2$  parity in extra-dim).
- Lightest charged particle a good DM candidate but weakly interacting, stable, and invisible in detectors.

$$\rightarrow \cancel{E}_T, \cancel{p}_T$$

Need to reconstruct  $\phi_{1/2}$  distributions  
to measure  $A_0, A_1$  parameters



# Minimal UED

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- One extra dimension of radius  $R$ , compactified to  $S^1/Z_2$
- Quantized 5th dimension momentum provides tree level mass for KK modes:

$$m_n^2 = \frac{n^2}{R^2} + m_0^2$$

- Requiring  $\psi_R, A_5$  odd and  $\psi_L$  even under the  $Z_2$  provides chiral fermions in the KK=0 level.
- Flavor universal boundary terms set to zero at scale  $\Lambda$
- Lightest KK=1 state stable: LKP (usually  $B_1$ )

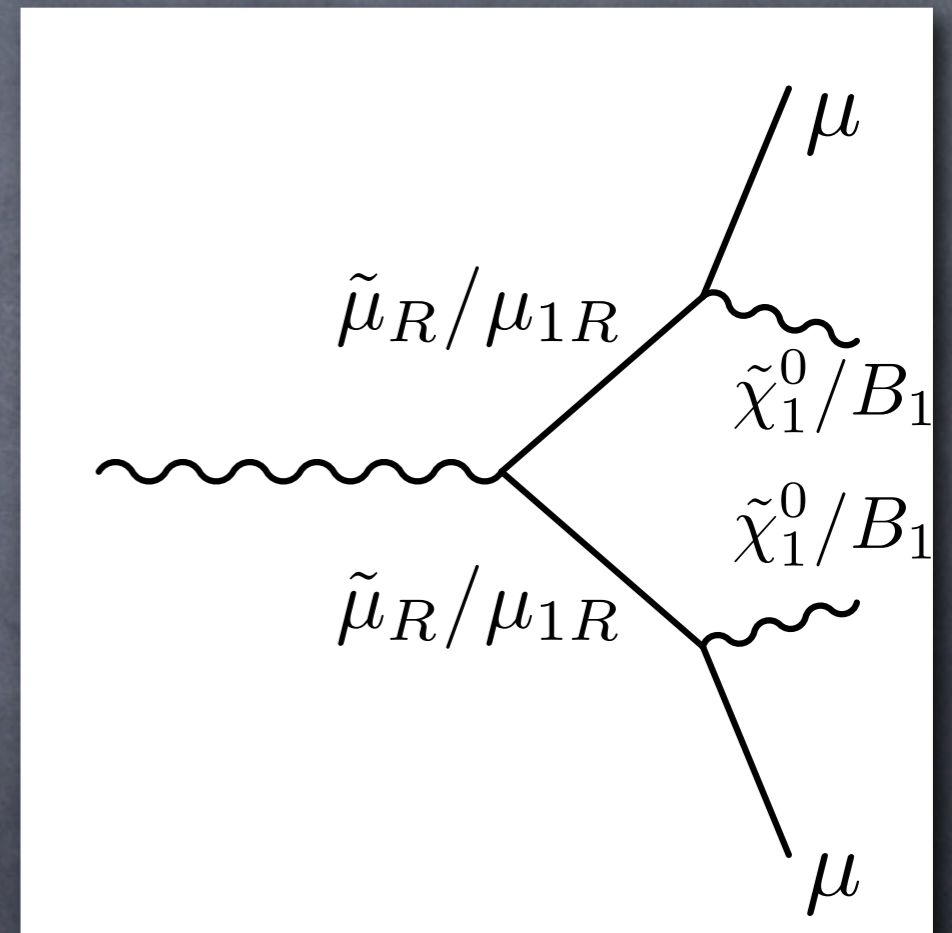


# Reconstruction of $\phi_{1/2}$

- Assume masses of  $\mu/B$  partners known.

4+4 unknown momenta  
-4 measured  $\not{p}$   
-4 mass relations

- system specified up to a 2-fold ambiguity
- Use both solutions: true/false  $\vec{p}_{\tilde{\mu}_R}$  to derive true and false values for  $\phi_i$





# Mass Measurements at ILC

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- Reconstruction assumes no mass/momentum measurement errors.
  - Known mass allows effective background cut via successful reconstruction
- Tracking resolution at ILC expected to have error  $\Delta p_T/p_T = 5 \times 10^{-5} (p_T/\text{GeV})$

	$\Delta m_{cont.}$ (GeV)	$\Delta m_{thres}$ (GeV)
$\tilde{e}_R$	0.2	0.05
$\tilde{e}_L$	0.2	0.18
$\tilde{\nu}_e$	0.1	0.07
$\tilde{\chi}_1^0$	0.1	0.05



# Scalar vs. Spinor at ILC

- Assume  $\sqrt{s} \leq 1 \text{ TeV}$ ,  $L = 500 \text{ fb}^{-1}$
  - Cut on lepton and missing energy  $\eta \leq 2.5$
  - Take two possible spectra: a typical SUSY and a typical MUED spectrum.
    - Since mass of SM partners assumed known, we 'fake' a MUED model with SUSY spectrum, and vice versa.
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## SUSY SPS3

$m_0$	90 GeV
$m_{1/2}$	400 GeV
$A_0$	0
$\tan \beta$	10
$\mu$	$> 0$

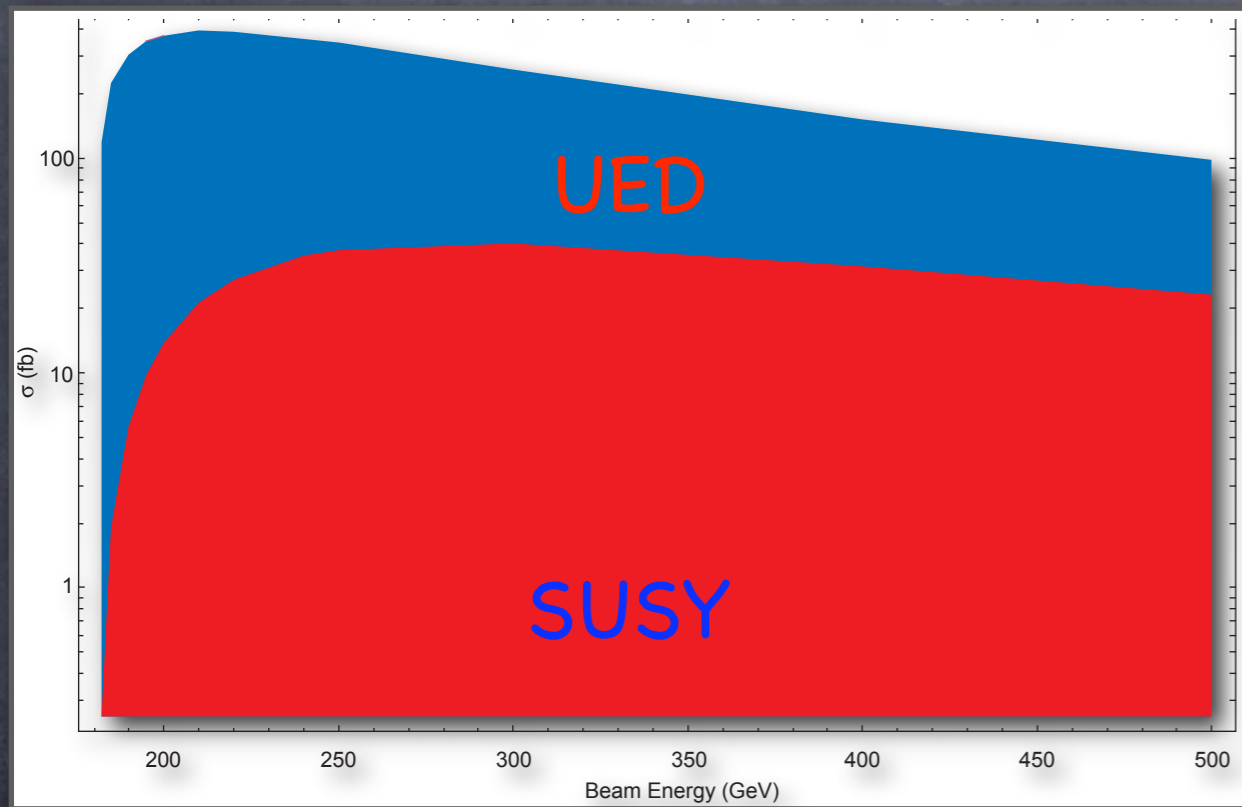
## MUED

$R^{-1}$	300 GeV
$\Lambda$	$20R^{-1}$
$m_H$	120 GeV

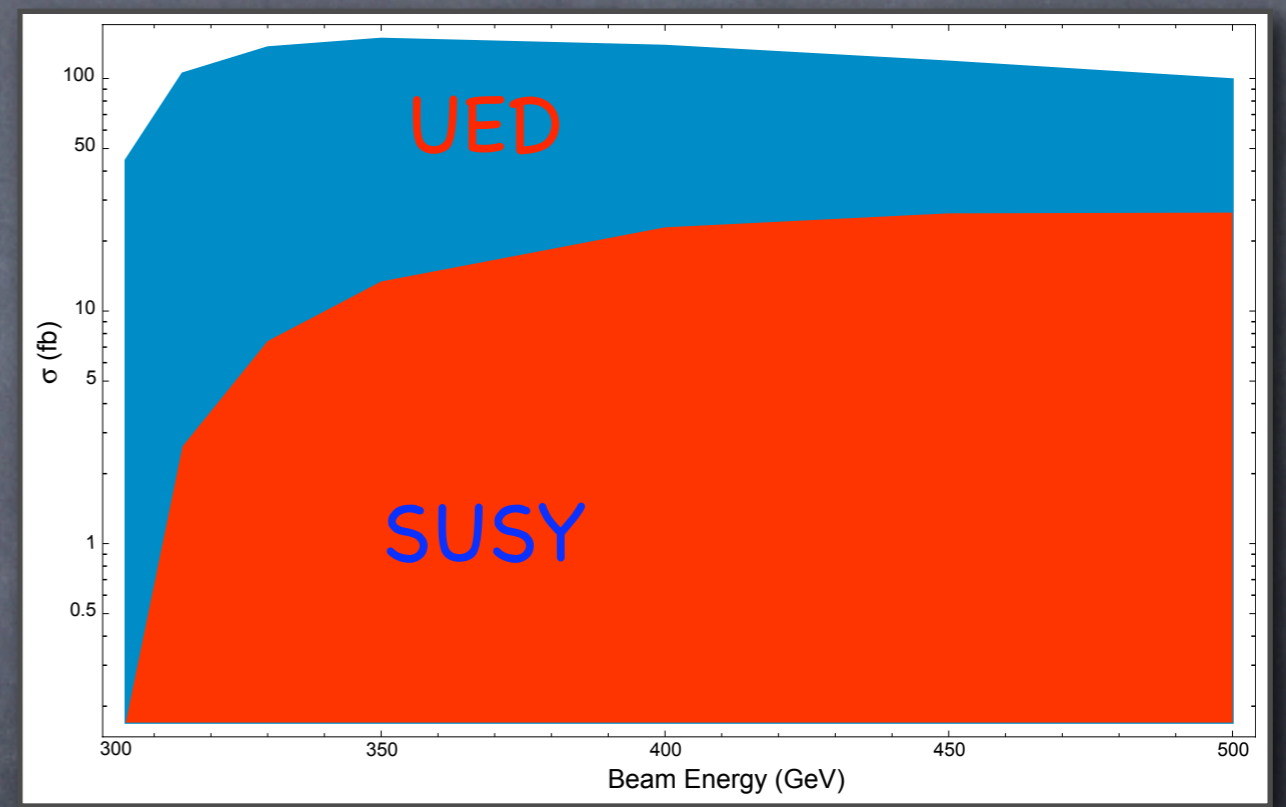


# Scalar vs. Spinor at ILC

SPS3



MUED



$\tilde{\chi}_1^0/B_1$	161 GeV
$\tilde{\mu}_R/\mu_{1R}$	181 GeV
$\tilde{\mu}_L/\mu_{1L}$	289 GeV

$\tilde{\chi}_1^0/B_1$	301.5 GeV
$\tilde{\mu}_R/\mu_{1R}$	303.3 GeV
$\tilde{\mu}_L/\mu_{1L}$	309.0 GeV



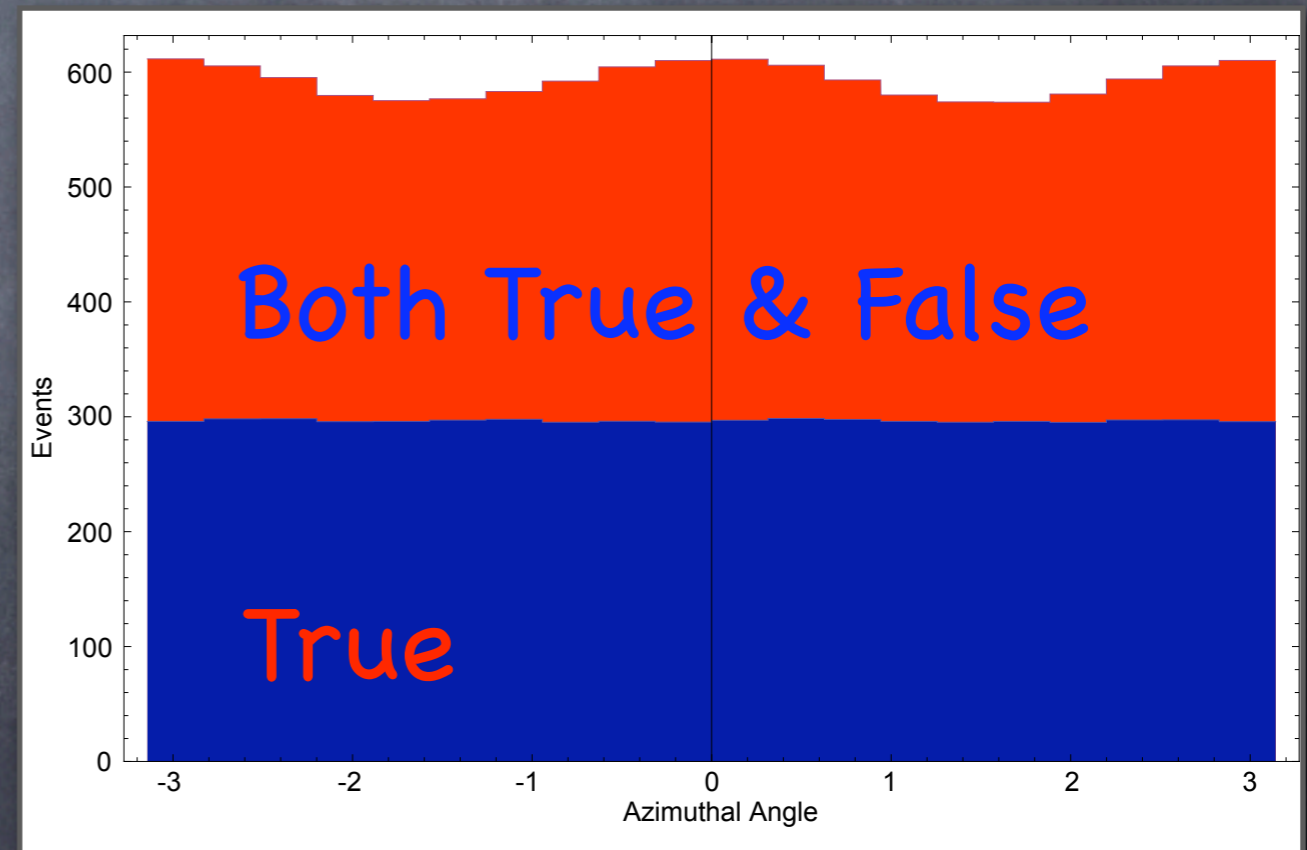
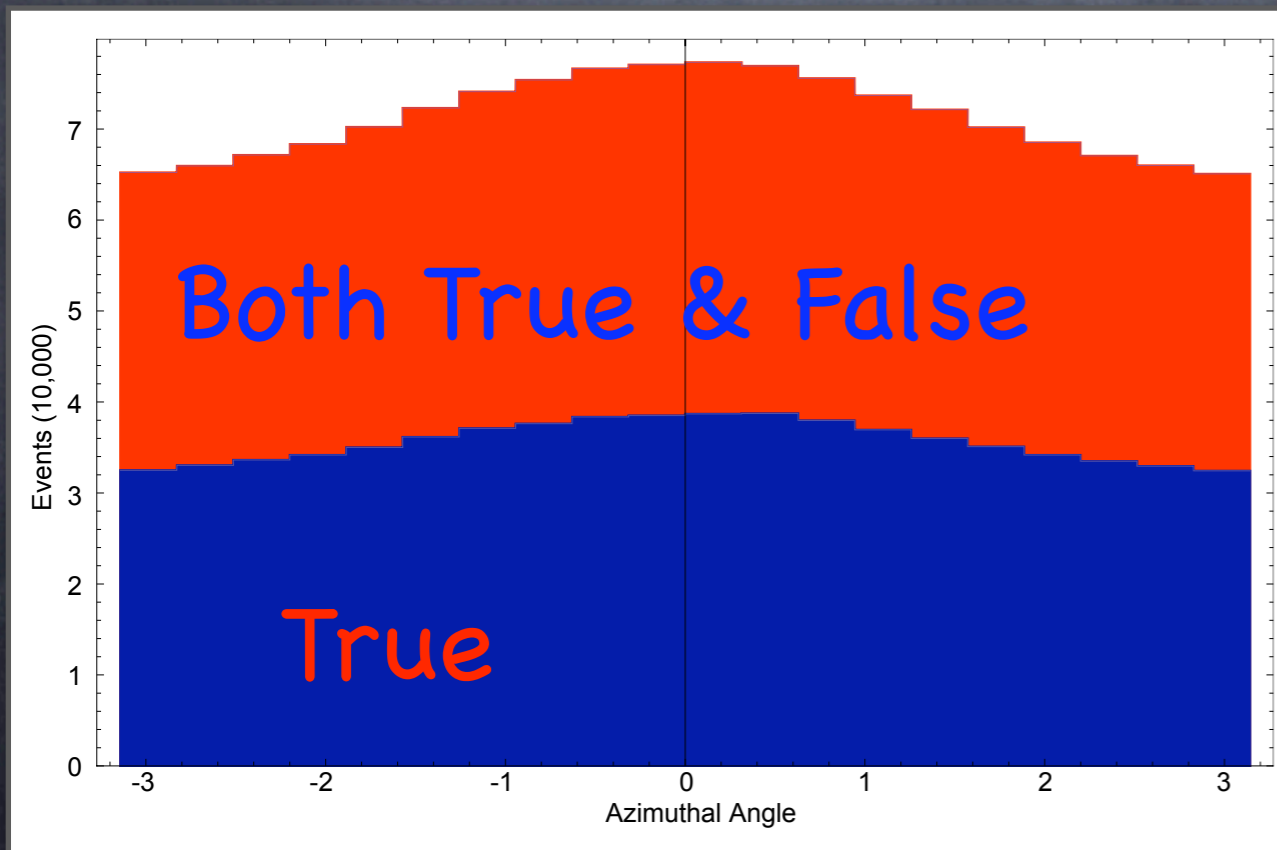
# Azimuthal Distributions

- Sum  $\phi_1$  and  $\phi_2$  distributions.

$$\sqrt{s} = 370 \text{ GeV}$$

UED distribution

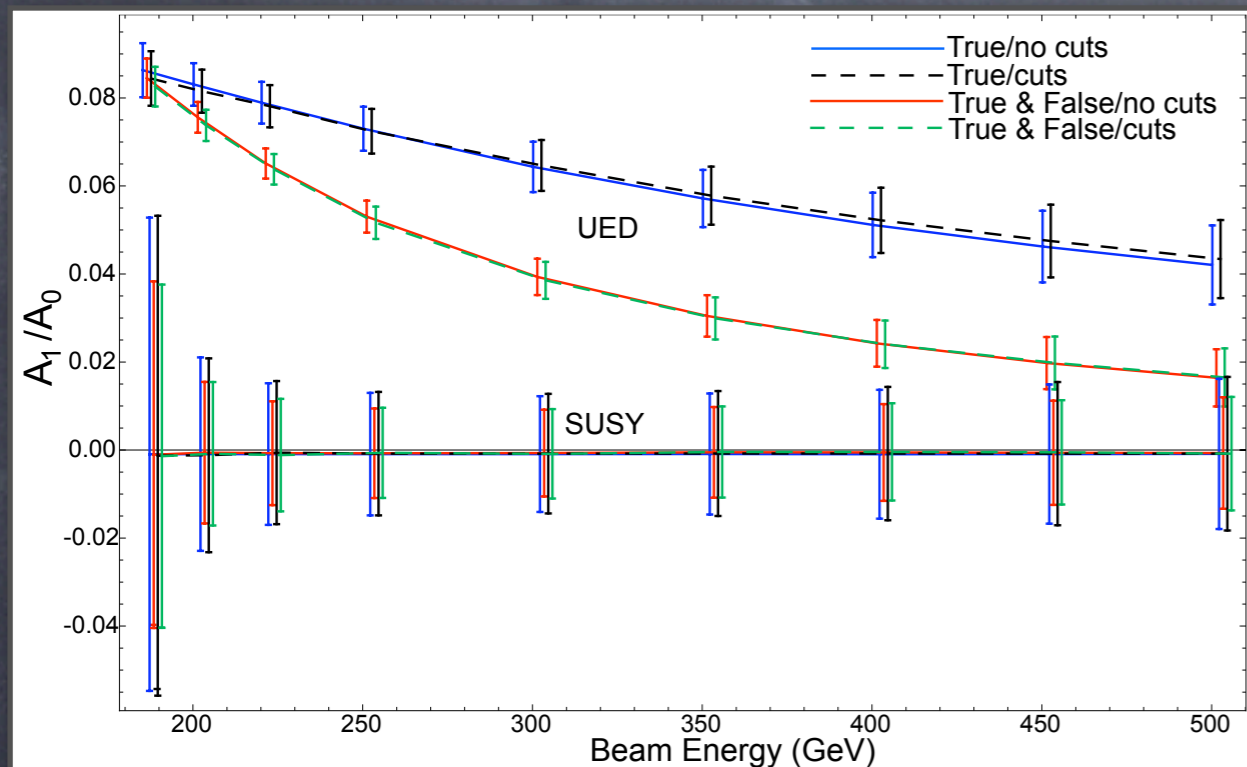
SUSY distribution



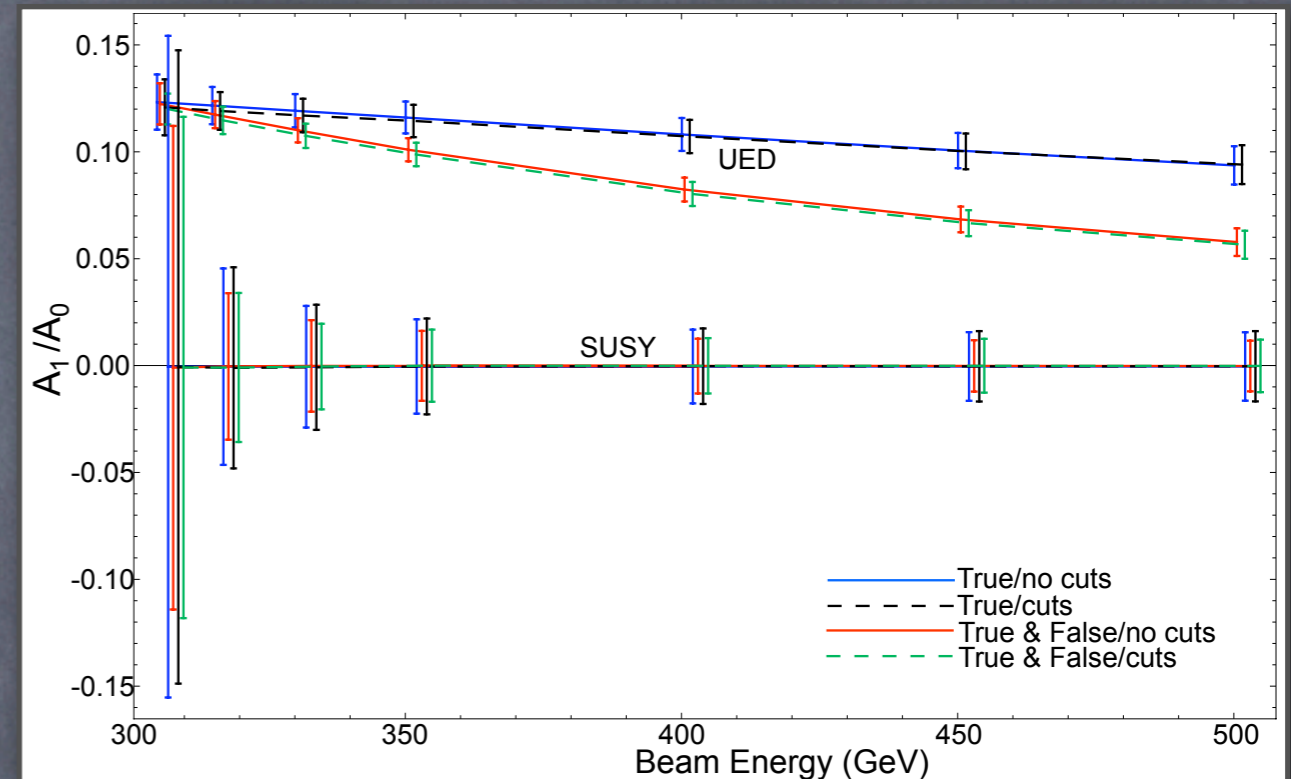


# Azimuthal Distributions

SPS3



MUED



Fit to

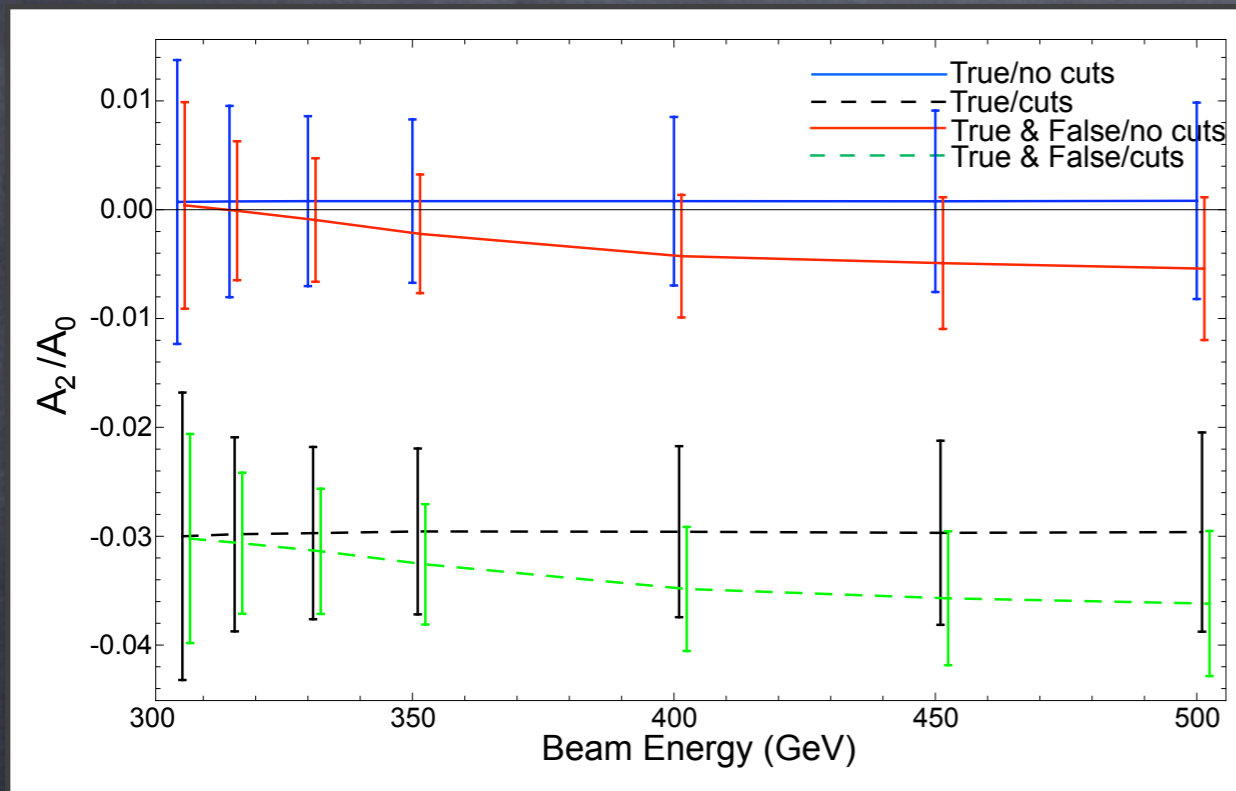
$$\sigma = A_0 + A_1 \cos \phi + A_2 \cos 2\phi$$



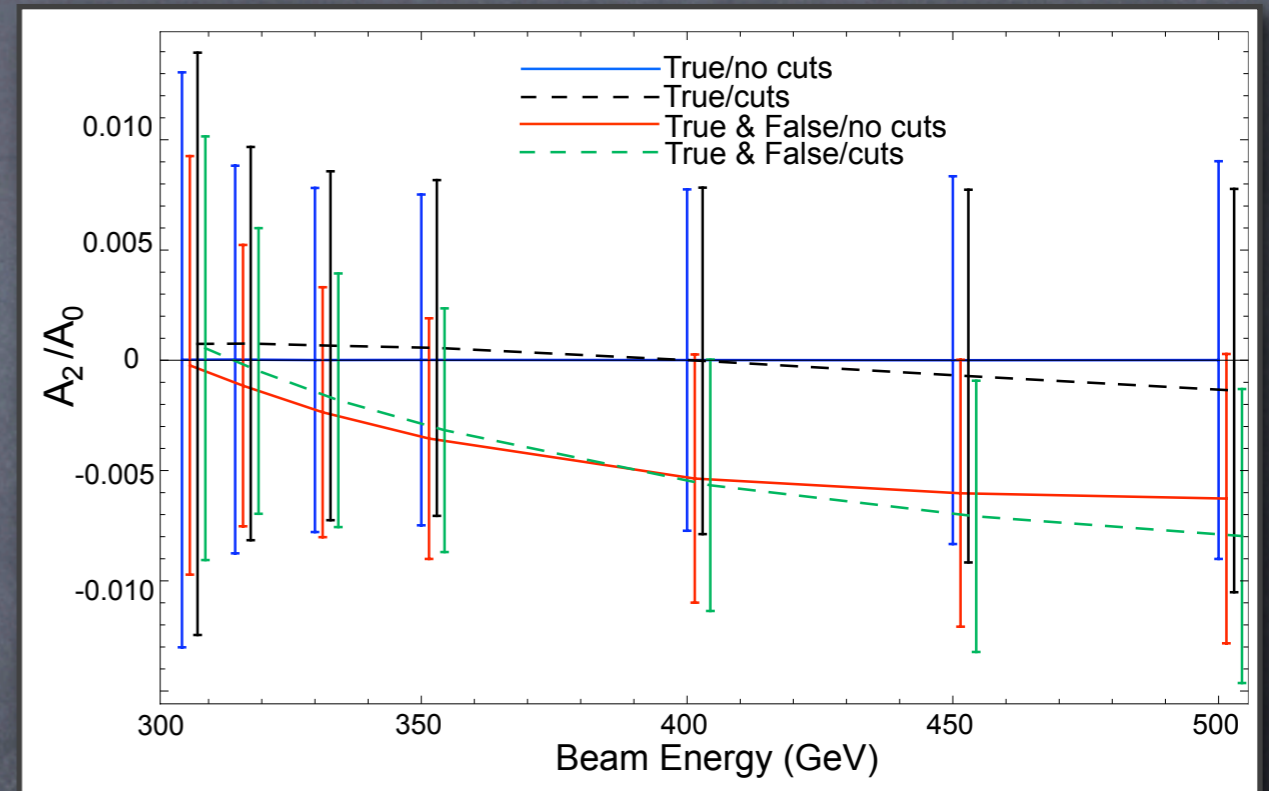
# Effects of Cuts on

$$e^-e^+ \rightarrow \mu_{1R}^+\mu_{1R}^- \rightarrow \mu^+\mu^- B_1 B_1$$

MUED uncorrected



MUED corrected



- Subtract off effect of cuts on flat distribution to correct for detector effects



# Conclusions

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- Quantum interference between helicity/polarization states can serve as a fully model independent probe of spin in an event
- We can use this method right now with data already on tape.
- A linear collider should be capable of distinguishing scalars from higher spins



# Conclusions

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- Need better understanding of how to correct for cuts and false solutions
  - Necessary to distinguish higher spin states
  - Longer decay chains may remove 2-fold ambiguity.
- At LHC, long decay chains would allow for 2-fold reconstruction; large # of events should allow for direct spin measurements.