

summary Loopverein & Generators

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- Tools and Automatization
 - Alternative 1-loop calculations: OPP vs generalized unitarity
 - SloopS
 - Photos Monte Carlo
 - Whizard
- EW corrections in the TeV region
- MSSM
 - renormalization in the complex MSSM
 - SUSY Higgs Yukawa couplings to bottom quarks at NNLO

Alternative 1-loop Calculations

new methods

- 1-loop amplitude

$$\mathcal{M} = \sum \text{Coeff} \times \text{loop integral}$$

- idea: “direct” construction of coefficients
⇒ loop amplitude known

Alternative 1-loop Calculations


The OPP Method (Ossola, Papadopoulos, Pittau, 2007)

Working at the *integrand* level

$$A = \int d^n \bar{q} \left[\mathcal{A}(q) + \tilde{A}(q, \tilde{q}, \epsilon) \right]$$

$$\left(\begin{array}{l} \bar{q} = q + \tilde{q} \\ n = 4 + \epsilon \end{array} \right)$$

- For example, in the case of $2 \rightarrow 6$

$$\mathcal{A}(q) = \sum \underbrace{\frac{N_i^{(6)}(q)}{\bar{D}_{i_0} \bar{D}_{i_1} \cdots \bar{D}_{i_5}}}_{\text{hexagon}} + \underbrace{\frac{N_i^{(5)}(q)}{\bar{D}_{i_0} \bar{D}_{i_1} \cdots \bar{D}_{i_4}}}_{\text{pentagon}} + \underbrace{\frac{N_i^{(4)}(q)}{\bar{D}_{i_0} \bar{D}_{i_1} \cdots \bar{D}_{i_3}}}_{\text{square}} + \underbrace{\frac{N_i^{(3)}(q)}{\bar{D}_{i_0} \bar{D}_{i_1} \bar{D}_{i_2}}}_{\text{triangle}} + \cdots$$


Alternative 1-loop Calculations

The function to be sampled *numerically*
to extract the coefficients of the scalar 1-loop functions

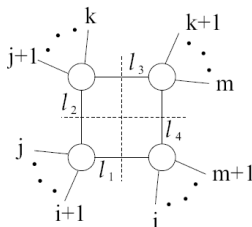
$$\begin{aligned} N_i^{(6)}(q) &= \sum_{i_0 < i_1 < i_2 < i_3}^5 \left[\textcolor{red}{d}(i_0 i_1 i_2 i_3) + \textcolor{blue}{\tilde{d}}(q; i_0 i_1 i_2 i_3) \right] D_{i_4} D_{i_5} \\ &+ \sum_{i_0 < i_1 < i_2}^5 \left[\textcolor{red}{c}(i_0 i_1 i_2) + \textcolor{blue}{\tilde{c}}(q; i_0 i_1 i_2) \right] D_{i_3} D_{i_4} D_{i_5} \\ &+ \sum_{i_0 < i_1}^5 \left[\textcolor{red}{b}(i_0 i_1) + \textcolor{blue}{\tilde{b}}(q; i_0 i_1) \right] D_{i_2} D_{i_3} D_{i_4} D_{i_5} \\ &+ \sum_{i_0}^5 \left[\textcolor{red}{a}(i_0) + \textcolor{blue}{\tilde{a}}(q; i_0) \right] D_{i_1} D_{i_2} D_{i_3} D_{i_4} D_{i_5} \\ &+ \textcolor{blue}{\tilde{P}}(q) D_{i_0} D_{i_1} D_{i_2} D_{i_3} D_{i_4} D_{i_5} \end{aligned}$$

Alternative 1-loop Calculations

Generalized Unitarity: more Cutting (more Gluing)

Bern, Dixon, Dunbar, Kosower, hep-ph/9403226; Ellis, Giele, Kunszt, Melnikov, 0806.3467; Berger et al. (BlackHat), 0803.4180

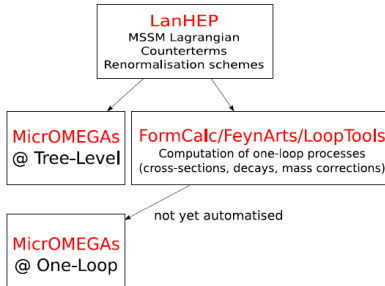
- 1 Quadruple cuts \Leftrightarrow gluing 4 tree-level, *gauge invariant*, amplitudes (Britto, Cachazo, Feng, hep-th/0412103)



- 2 q integration frozen \Rightarrow *coefficient d_i of the box extracted*
- 3 3 bubbles are connected together, the box contributions subtracted and the *coefficients c_i of the triangles extracted*

Conclusions

- ① New techniques and ideas allowed an impressive progress in the field of 1-loop calculations:
 - I (briefly) discussed and compared the OPP method and the GU techniques;
 - They have been successfully applied in QCD to compute at NLO $pp \rightarrow t\bar{t}b\bar{b}$, $pp \rightarrow t\bar{t}j\bar{j}$, $pp \rightarrow W + 3 \text{ jets}$, $pp \rightarrow W + 4 \text{ jets}$, \dots ;
 - Computing R in both OPP and GU still unsatisfactory;
 - Wave function renormalization problem unsolved in GU. In OPP put by hand (but gauge dependent!).
- ② No complete EW calculation is available so far with these new techniques.
- ③ They will be needed for ILC Physics.
- ④ The final goal should be delivering public 1-loop codes.



SLOOPS

A code for calculation of **loops** diagrams in the MSSM with application to **colliders**, **astrophysics** and **cosmology**.

- Evaluation of one-loop diagrams including a **complete** and **coherent** renormalisation of **each sector** of the MSSM with an **OS** scheme.
- Modularity between different renormalisation schemes.
- **Non-linear** gauge fixing.
- Checks : results **UV,IR** finite and **gauge** independent.

<http://code.sloops.free.fr/>



SLOOPS applications

application examples

- Higgs and neutralino masses
- Higgs and Chargino decays
- $\tilde{\chi}^\pm, \tilde{\tau}, W/Z$ production at ILC
- cosmology, $\Omega_\chi h^2 @ 1 - 2\%$
 \Rightarrow 1-loop corrections needed

THERMAL RELIC

- $\Omega_\chi h^2 \propto 1/(\sigma(\chi\chi \rightarrow \text{SM}))$
- Relic density calculated through the interface of **SloopS** with **micrOMEGAs** (Bélanger *et al.*)

BUNCH OF FULL ONE-LOOP PROCESSES CALCULATED

Baro, Boudjema, Semenov, *Phys. Lett B* **660**

Baro, Boudjema, G.C, Sun Hao, *Phys. Rev. D* **81** 015005 (2010) (2008) 550

- $\tilde{\chi}_1^0 \tilde{\chi}_1^0 \rightarrow f \bar{f}$ (bino)
- $\tilde{\chi}_1^0 \tilde{\tau}_1^+ \rightarrow \tau^+ \gamma (Z^0)$ (bino)
- $\tilde{\tau}_1^+ \tilde{\tau}_1^+ \rightarrow \tau^+ \tau^+$ (bino)
- $\tilde{\chi}_1^0 \tilde{\chi}_1^0 \rightarrow W^+ W^-, Z^0 Z^0$ (bino-wino, bino-higgsino, higgsino, higgsino-bino, wino)
- $\tilde{\chi}_1^0 \tilde{\chi}_1^+ \rightarrow u \bar{d}, t \bar{b}$ (bino-wino, higgsino, higgsino-bino, wino)
- $\tilde{\chi}_1^+ \tilde{\chi}_1^- \rightarrow W^+ W^-, Z^0 Z^0$ (wino)

First and second order spin amplitudes for precision of PHOTOS Monte Carlo

Z. Was^{*}, A. van Hameren, G. Nanava, T. Przedzinski, P. Roig, Q. Xu

^{*}speaking, Institute of Nuclear Physics, Krakow and CERN PH-TH, Geneva

- (1) From semileptonic B and K mesons decays (measurements of quark mixing), properties of W and Z decays at LHC, to signatures for discovery and properties of New Physics particles bremsstrahlung must be taken into account.
- (2) PHOTOS Monte Carlo is used in such studies. **Essential:** Input from spin calculations was necessary for design of the program and for tests of its physical precision.
- (3) *I will mention:* phase space parametrization, crude distribution in single photon emission, double photon emission, and multiple emission; all modes needed for tests.
- (4) *Technical points like:* event record type HEPEVT, HepMC; intermediate particles explicitly stored in it or not; numerical tests for user installation will be skipped.
- (5) *At which precision QED FSR can be separated from the rest, that is:* genuine weak corrections, ISR, ISR \times PS, ISR-FSR interference. This important point will be skipped too.

Summary

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1. PHOTOS Monte Carlo is for simulation of multiphoton FSR bremsstrahlung.
2. Program is designed to help generate correlated samples: events with and without FSR bremsstrahlung.
3. For processes mediated by Z/γ' and W 's high precision is investigated.
4. Important for program construction were presented here studies of spin amplitudes. Structure of their gauge invariant parts is used in definition of photon emission kernel.
5. Remaining parts of amplitudes are needed for discussion of systematic errors, for optimization of program performance or for construction correcting weights.
6. For some processes eg. where matrix element is obtained from scalar QED introduction of data constrained form factors may be necessary.
7. New version of program, using HepMC event record of C++ is available for tests.

Whizard 2.x: Monte Carlo Generator for ILC

- ▶ **O'Mega** matrix element compiler:
 - ▶ **maximally factorized** matrix elements
 - ▶ exponential, not factorial, complexity (**recursion relations**)
 - ▶ **model independent** algorithm
- ▶ **VAMP** adaptive multi channel sampling:
 - ▶ multiple independent **VEGAS** grids
 - ▶ efficient integration of complicated phase spaces
 - ▶ **unweighted** event generation
- ▶ **WHIZARD** core:
 - ▶ phase space parametrization
 - ▶ unstable particle decays with **spin correlations**
 - ▶ interfaces, I/O
 - ▶ supervisor
 - ▶ scripting language

Whizard 2.x: Monte Carlo Generator for ILC

- ▶ QED
- ▶ QCD
- ▶ Standard Model
- ▶ SM with anomalous top and gauge couplings
- ▶ Z'
- ▶ Supersymmetry: MSSM (cross checked with MadGraph and Sherpa), NMSSM, PSSSM
- ▶ Extra Dimensions, UED
- ▶ 3-Site Higgsless Model
- ▶ Little Higgs: Littlest, Simplest
- ▶ all FeynRules models
- ▶ your own ...

Whizard 2.x: Monte Carlo Generator for ILC

- ▶ efficient and **complete** implementations of the Fortran 2003 standard
 - ▶ **procedure pointers** (required for dynamic linking) only correctly implemented by NAG and gfortran 4.5
- ▶ use more symmetries to reduce the code size
 - ▶ compiled code for multi jet cross sections at LHC can become larger than a **giga[sic!]byte**
- ▶ allow completely general vertex structures (**MadGraph** is working on this too)
- ▶ **loops** (**proof-of-principle** implementations by other groups exist, but completely **general** and fully **automatic** implementations are still science fiction ...)
- ▶ get it from

<http://projects.hepforge.org/whizard/>

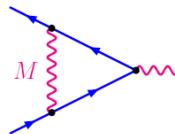
EW corrections in the TeV region

"Typical" size of electroweak corrections: $\frac{\alpha_{\text{weak}}}{\pi} \approx 10^{-2}$

new aspects at LHC: $\sqrt{s} \approx 1\text{-}2\text{TeV} \gg M_{W,Z}$

strong enhancement of negative corrections

one-loop example: massive U(1)



$$\Rightarrow \text{Born} * \left[1 + \frac{\alpha}{4\pi} \left(-\ln^2 \frac{s}{M^2} + 3 \ln \frac{s}{M^2} - \frac{7}{2} + \frac{\pi^2}{3} \right) \right]$$

$\frac{s}{M^2}$	$-\ln^2 \frac{s}{M^2}$	$+3 \ln \frac{s}{M^2}$	$-\frac{7}{2} + \frac{\pi^2}{3}$	Σ	$* 4 \frac{\alpha_{\text{weak}}}{4\pi}$
$\left(\frac{1000}{80}\right)^2$	-25.52	+15.15	-0.21	-10.6	-13%
$\left(\frac{2000}{80}\right)^2$	-41.44	+19.31	-0.21	-22.3	-27%

EW corrections in the TeV region

observations

- subleading terms important
- 2-loop may be relevant

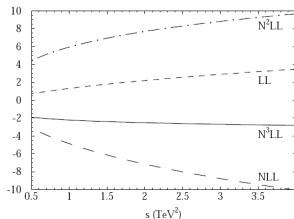
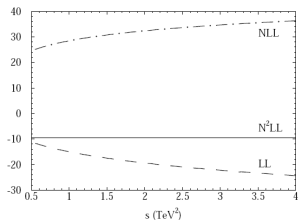
higher loops needed

(recent) 2-loop results in high energy limit for [\[Kuehn et al '03-'10\]](#)

- fermion-fermion-vector form factor. up to N^4LL .
- 4f scattering, $e^+e^- \rightarrow q\bar{q}$. up to N^3LL
- W pair production at linear collider and LHC. up to N^2LL .

EW corrections in the TeV region

Separate **logarithmic contributions** to $R(e^+e^- \rightarrow q\bar{q})$ in % to the Born approximation



one-loop LL ($\ln^2(s/M^2)$), NLL ($\ln^1(s/M^2)$)
and $N^2\text{LL}$ ($\ln^0(s/M^2)$)

two-loop LL ($\ln^4(s/M^2)$), NLL ($\ln^3(s/M^2)$),
 $N^2\text{LL}$ ($\ln^2(s/M^2)$) and $N^3\text{LL}$ ($\ln^1(s/M^2)$)

Large cancellations!

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real W/Z radiation will compensate these effects.

can real radiation be separated?

Renormalization in the complex MSSM

Effects of complex parameters in the Higgs sector:

Complex parameters enter via loop corrections:

- μ : Higgsino mass parameter
- $A_{t,b,\tau}$: trilinear couplings $\Rightarrow X_{t,b,\tau} = A_{t,b} - \mu^* \{\cot \beta, \tan \beta\}$ complex
- $M_{1,2}$: gaugino mass parameter (one phase can be eliminated)
- $m_{\tilde{g}}$: gluino mass

\Rightarrow can induce \mathcal{CP} -violating effects

Result:

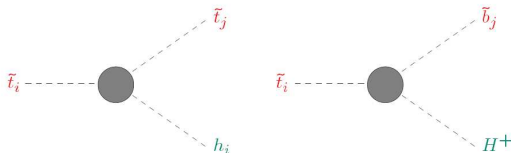
$$(A, H, h) \rightarrow (h_3, h_2, h_1 (= \phi))$$

with

$$M_{h_3} > M_{h_2} > M_{h_1}$$

Renormalization in the complex MSSM

Examples for processes with (external) stops and Higgs bosons:



- important decay modes of stops
- A_t and A_b directly enter the vertex **incl. complex phases!**
- possible source of Higgs bosons at the LHC/ILC
- ...

⇒ **higher-order corrections important!**

⇒ **simultaneous renormalization of stop and sbottom sector required!**

⇒ **including complex phases!**

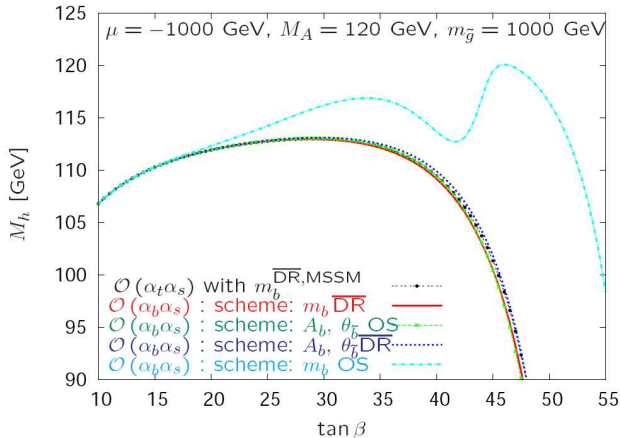
want BR ⇒ need all decays

⇒ (nearly) all sectors of the cMSSM have to be renormalized simultaneously

Renormalization in the complex MSSM

studied several renormalization schemes to find best scheme
effect of bad renormalization scheme

“OS” scheme: $\delta A_b = \frac{1}{m_b} [-(A_b - \mu^* \tan \beta) \delta m_b + \dots]$



⇒ fails already for Higgs boson self-energies

5. Conclusions & Outlook

- \tilde{t} and \tilde{b} sector important for collider phenomenology
- Simultaneous renormalization of both sectors crucial for higher-order corrections – on-shell properties for external squarks!

⇒ \tilde{t}/\tilde{b} renormalization in the cMSSM

⇒ simultaneous renormalization of all sectors in the cMSSM

- Sbottom sector: six (+X) schemes defined and tested
analytical deficiencies found in all schemes
most “robust”: RS2: “ $m_b, A_b \overline{\text{DR}}$ ” ← preferred scheme
RS6: “ A_b vertex, $\text{Re}Y_b$ OS”
- Numerical analysis: RS2: “ $m_b, A_b \overline{\text{DR}}$ ” shows very robust and stable behavior over nearly all (tested) cMSSM parameter space

Evaluation of $\Gamma(\tilde{t}_2 \rightarrow \tilde{t}_1 h_i)$ and $\text{BR}(\tilde{t}_2 \rightarrow \tilde{t}_1 h_i)$

⇒ sizable effects in Γ and BR

⇒ have to be included for ILC analyses (and possibly for LHC)

SUSY Higgs Yukawa couplings at NNLO

bottom Yukawa couplings in MSSM for large $\tan\beta$

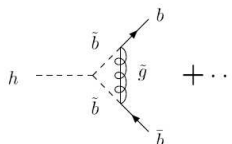
- dominate Higgs boson production & decay processes

$gg \rightarrow \phi$ dominant for $\tan\beta \lesssim 10$

$gg \rightarrow \phi b\bar{b}$ dominant for $\tan\beta > 10$

- large NLO SUSY corrections to bottom Yukawa couplings

- large SUSY-QCD corrections to $\phi^0 \rightarrow b\bar{b}$ ($\Delta\Gamma/\Gamma \sim 10\%$)



$$h \rightarrow b\bar{b} \text{ via } g \text{ loop} + \dots \propto \frac{\alpha_s}{\pi} \frac{M_{\tilde{g}} \mu \tan\beta}{M_{\tilde{SUSY}}^2}$$

Hall, ...
Carena, ...
Nierste, ...
Guasch, ...
etc.

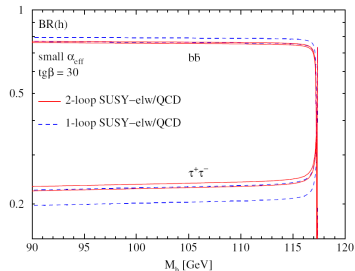
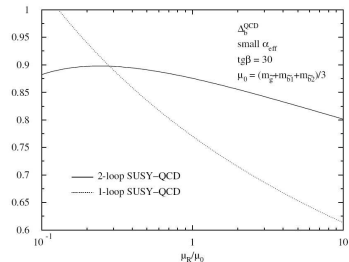
resummation possible [Carena, Garcia, Nierste, Wagner] [Guasch, Haefliger, Spira]

$$\mathcal{L}_{eff} = -\lambda_b \bar{b}_R \left[\phi_1^0 + \frac{\Delta_b}{\tan\beta} \phi_2^{0*} \right] b_L + h.c. \quad \text{valid to all orders in } \Delta_b$$

SUSY Higgs Yukawa couplings at NNLO

- 2-loop SUSY QCD corrections to Δ_b [Noth, Spira]
- need 2-loop self energies at zero momentum
- impact
scale dependence reduced
BR uncertainty reduced
- applications $e^+e^- \rightarrow b\bar{b}\phi, t\bar{t}H^-$

Noth, Spira



Conclusions

- for ILC to reach full potential higher order corrections mandatory
- fully automated NLO generators for ILC desirable
significant recent progress in new methods
well underway for QCD/LHC, first steps taken for EW/ILC
will be available
- potentially large radiative corrections in MSSM
careful treatment of all effects needed