

Measurement of Top-Yukawa coupling at the early stage ILC

R. Yonamine, K. Ikematsu^A, T. Tanabe^B
K. Fujii^C, Y. Kiyo^C, Y. Sumino^D, H. Yokoya^E

Sokendai(KEK), Siegen U.^A, Tokyo U.^B, KEK^C, Tohoku U.^D, CERN^E

$$\mathcal{L}_{BSM}$$

$$\mathcal{L}_{Gauge} + \mathcal{L}_{Higgs} + \mathcal{L}_{Yukawa}$$

Gauge
Principle

Symmetry
Breaking
&
Mass
Generation

Relativistic Quantum Field Theory

Two pillars of SM

Standard model consists of two pillars:

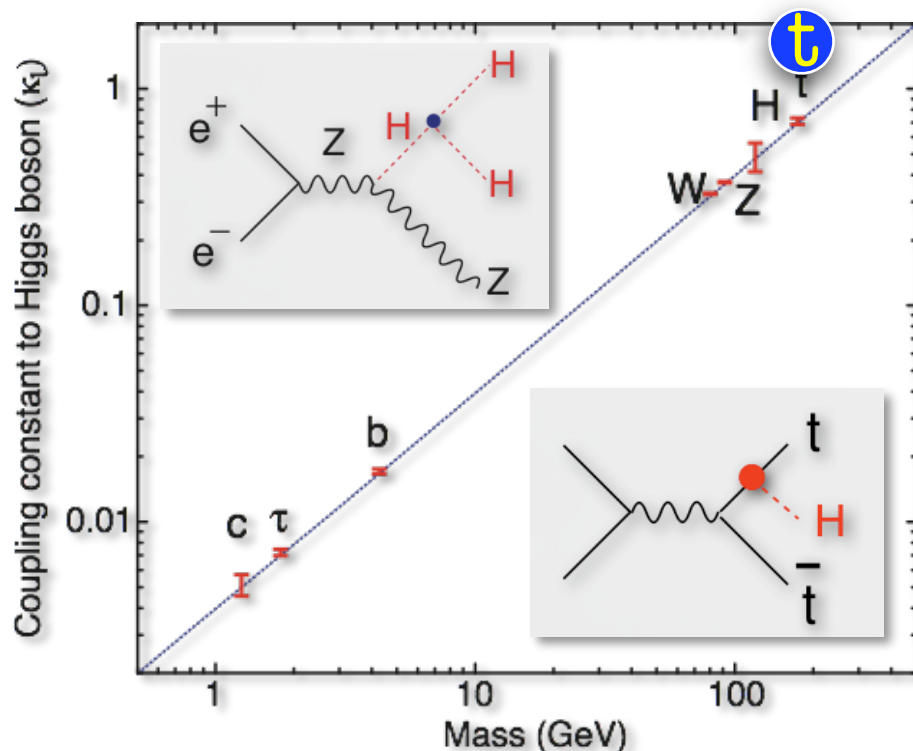
- One pillar, gauge symmetry, has been established by precision EW studies.
- Another one, higgs mechanism, is still untested.

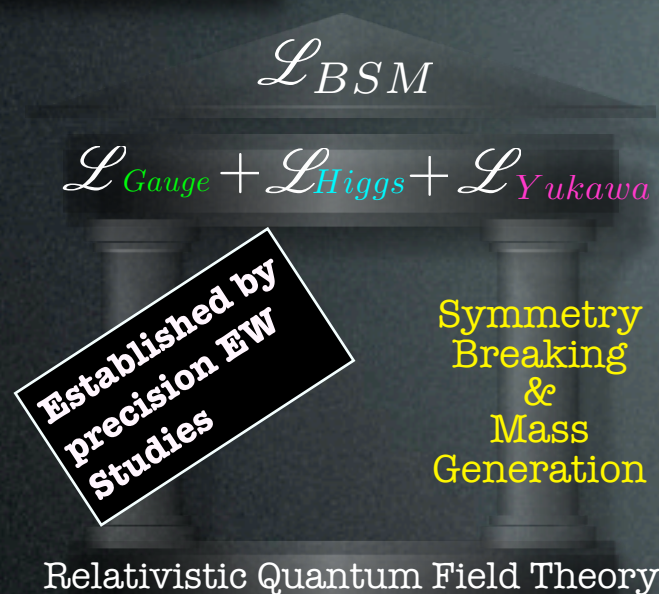
A critical mission for the ILC is the Higgs coupling measurement !

Higgs self coupling will be tested at ~ 500 GeV where $e^+e^- \rightarrow ZHH$ cross section attains its maximum.

Our motivation is to confirm the untested pillar by measuring Top-Yukawa coupling at 500 GeV (1st stage of ILC) concurrently to measuring Higgs self coupling.

Relation between mass and coupling constant with Higgs





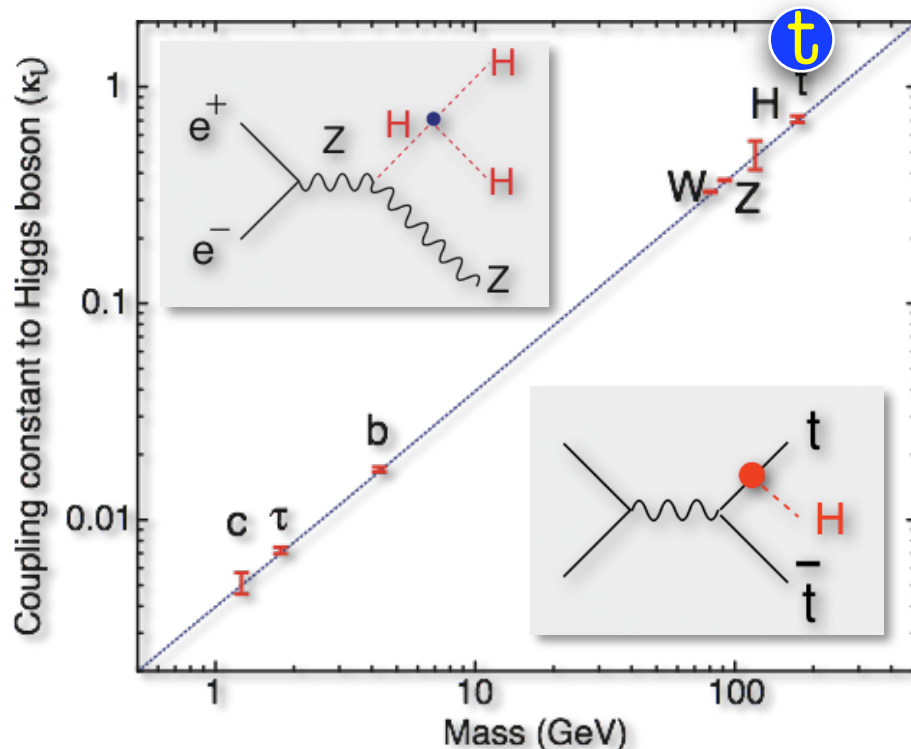
Two pillars of SM

Standard model consists of two pillars:

- One pillar, gauge symmetry, has been established by precision EW studies.
- Another one, higgs mechanism, is still untested.

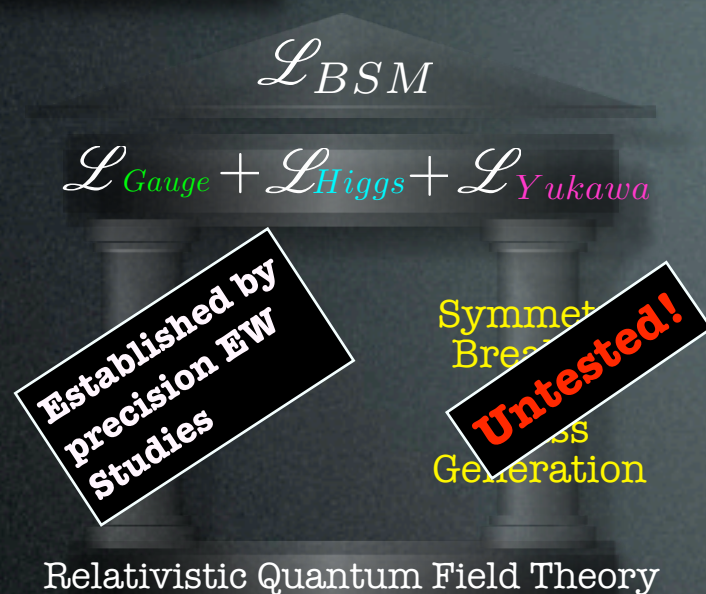
A critical mission for the ILC is the Higgs coupling measurement !

Relation between mass and coupling constant with Higgs



Higgs self coupling will be tested at ~ 500 GeV where $e^+e^- \rightarrow ZHH$ cross section attains its maximum.

Our motivation is to confirm the untested pillar by measuring Top-Yukawa coupling at 500 GeV (1st stage of ILC) concurrently to measuring Higgs self coupling.



Two pillars of SM

Standard model consists of two pillars:

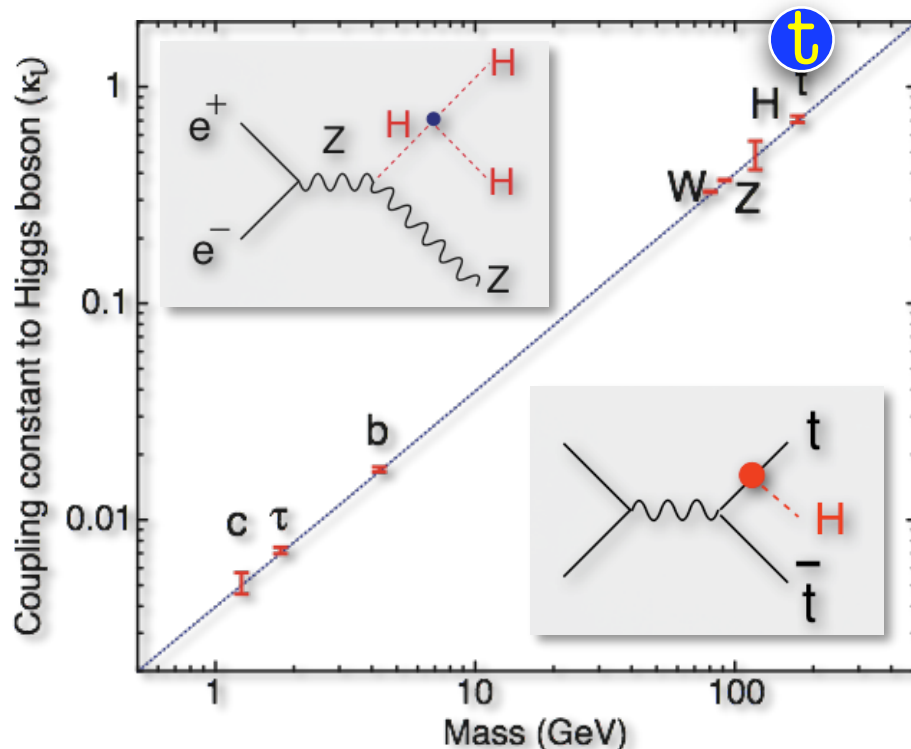
- One pillar, gauge symmetry, has been established by precision EW studies.
- Another one, higgs mechanism, is still untested.

A critical mission for the ILC is the Higgs coupling measurement !

Higgs self coupling will be tested at ~ 500 GeV where $e^+e^- \rightarrow ZHH$ cross section attains its maximum.

Our motivation is to confirm the untested pillar by measuring Top-Yukawa coupling at 500 GeV (1st stage of ILC) concurrently to measuring Higgs self coupling.

Relation between mass and coupling constant with Higgs



\mathcal{L}_{BSM}
 $\mathcal{L}_{Gauge} + \mathcal{L}_{Higgs} + \mathcal{L}_{Yukawa}$

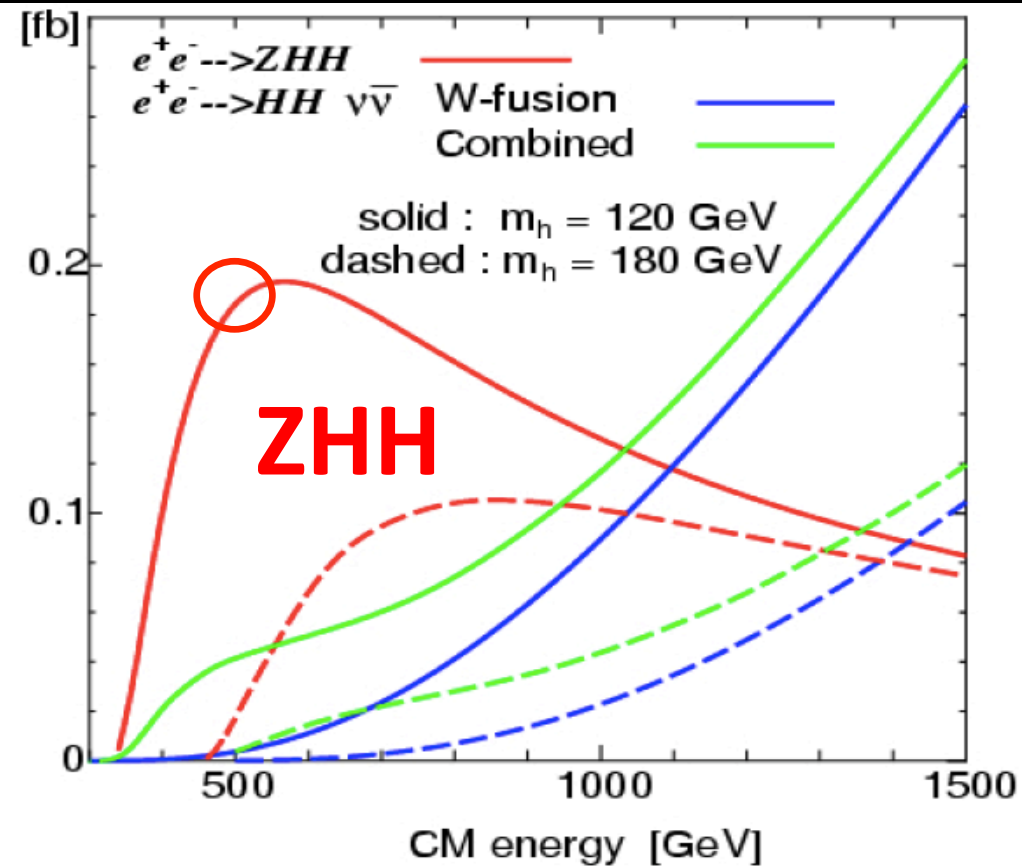
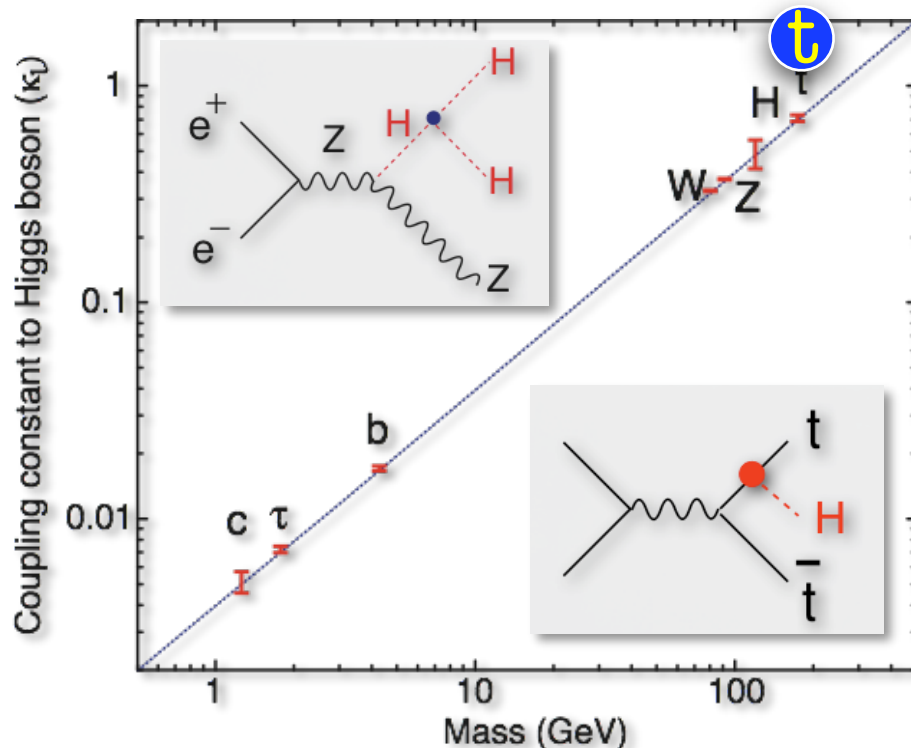
Established by
precision EW
Studies

Symmet
Break
Mass
Generation

Untested!

Relativistic Quantum Field Theory

Relation between mass and coupling constant with Higgs



Higgs self coupling will be tested at ~ 500 GeV where $e^+e^- \rightarrow ZHH$ cross section attains its maximum.

Our motivation is to confirm the untested pillar by measuring Top-Yukawa coupling at 500 GeV (1st stage of ILC) concurrently to measuring Higgs self coupling.

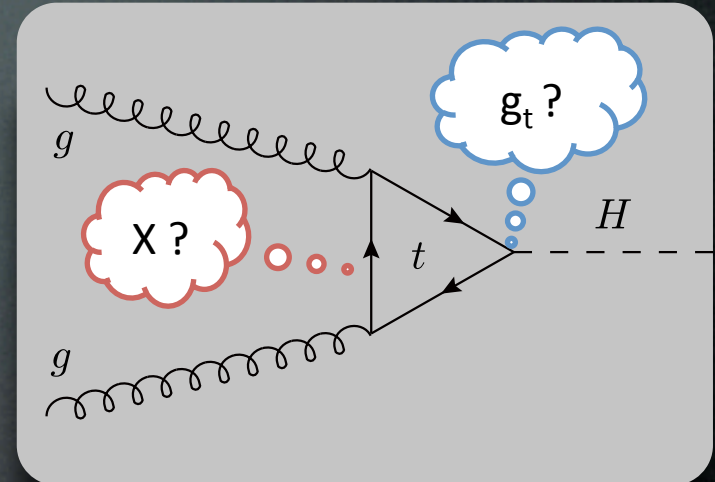
Top-Yukawa coupling $\begin{cases} \text{indirect measurement} \\ \text{direct measurement} \end{cases}$

• indirect measurement

The Higgs sector offers a broad range of possibilities for new physics ...

There is a possibility of a new particle X being in the loop.

difficult to distinguish X loop and top loop!

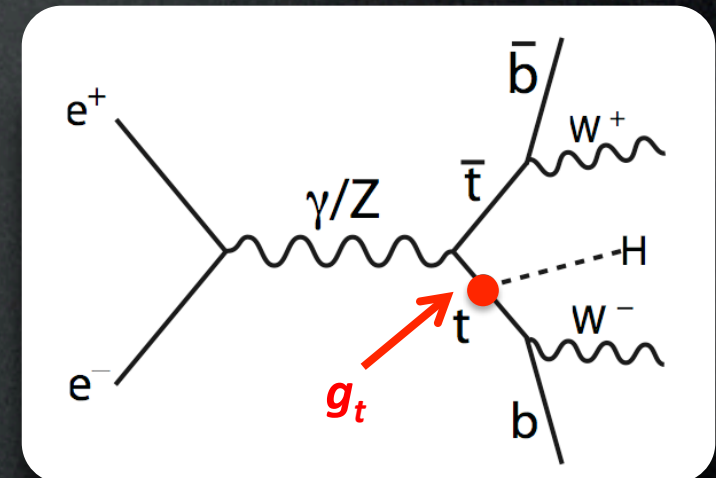


$gg \rightarrow ttH$ @ LHC

• direct measurement

promising at ILC !!

main decay mode ($H \rightarrow b\bar{b}$ 68%) can be used



$e^+e^- \rightarrow ttH$ @ ILC

Measurement of top-Yukawa coupling at 500 GeV

Past work estimated the measurement accuracy around $E_{\text{cm}} = 700 - 800$ GeV where the cross section reaches maximum.

500 GeV is nearly threshold of ttH.

Cross section is smaller than 1 fb!

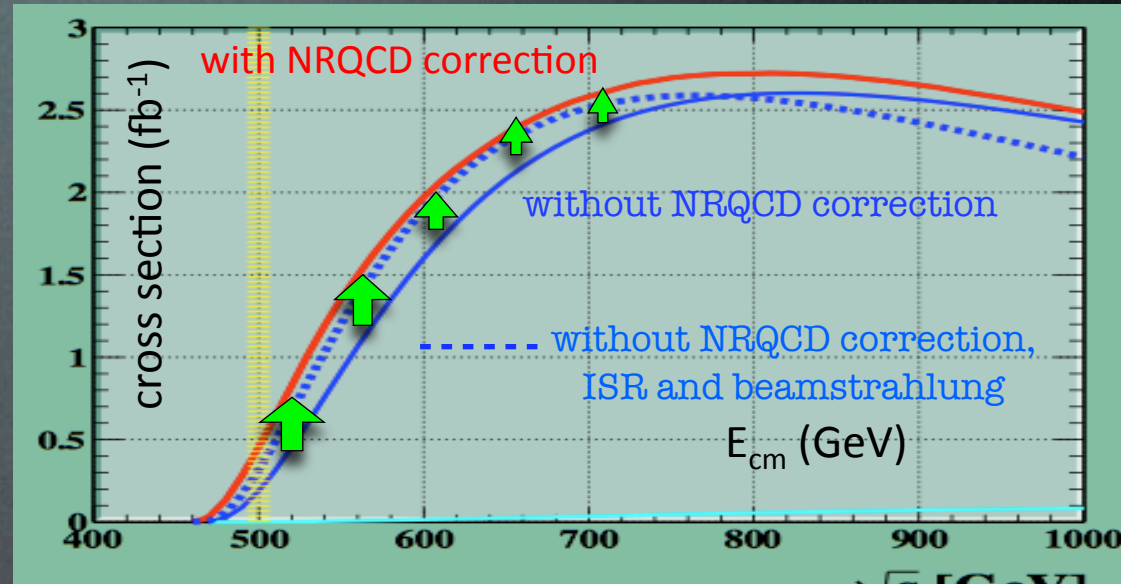
But ...

tt threshold correction enhances ttH production (and also ttZ)

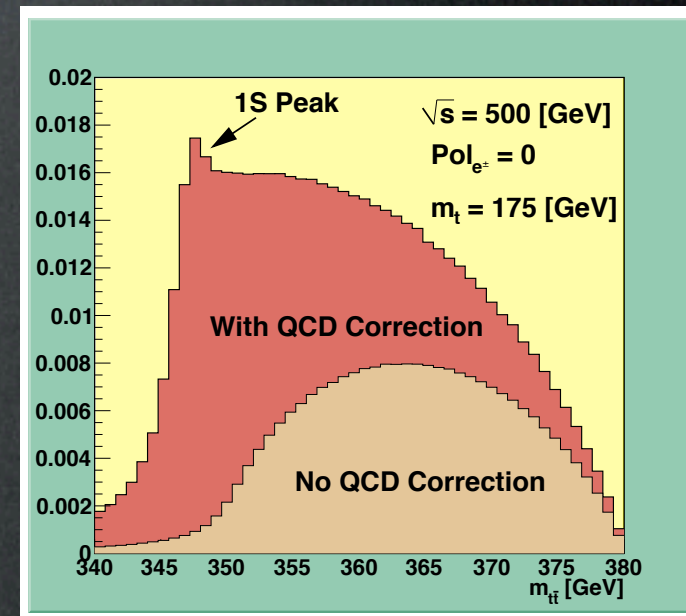
This makes it possible to perform the direct g_t measurement at 500 GeV

Cross section of ttH

enhancement



Invariant mass dist. for tt system



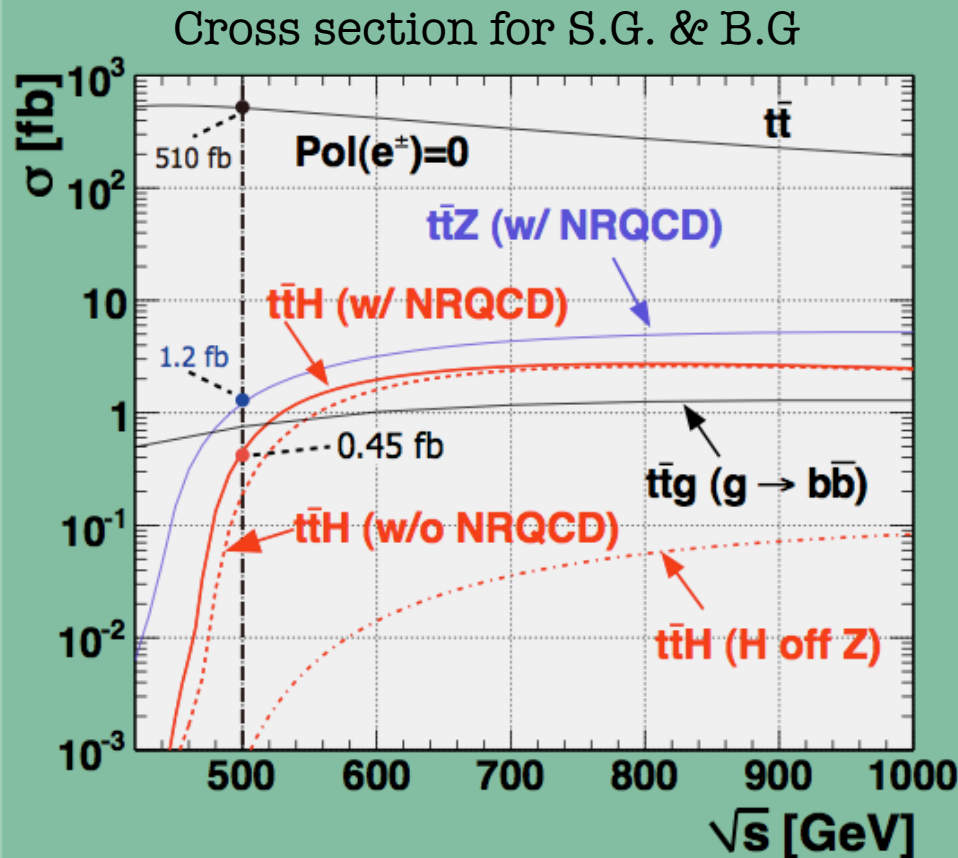
Feature of signal process ($e^+e^- \rightarrow ttH$)

event signature in our study

$ttH \rightarrow bWbWbb$ ($H \rightarrow bb$: 68%)

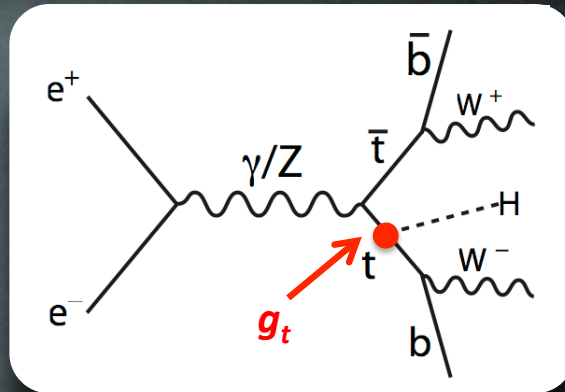
8jet, 1-lepton + 6jet, and 2 lepton + 4-jet

At $E_{cm} = 500$ GeV, ttH production is dominated by s-channel γ / Z exchange.

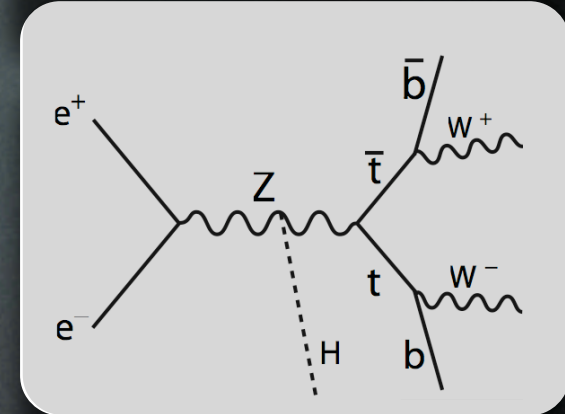


5

$e^+e^- \rightarrow ttH$



contains
 g_t



does NOT
contains
 g_t

There is contribution to ttH from Higgs-strahlung. This diagram doesn't contain top-Yukawa coupling. But its contribution is negligible because of small cross section.

The cross section for ttH , tt , ttZ and $ttg^*(g \rightarrow b\bar{b})$ are shown in left plot, which includes NRQCD correction to ttH and ttZ .

$\sigma_{ttH} = 0.45 \text{ fb}$ without beam pol.

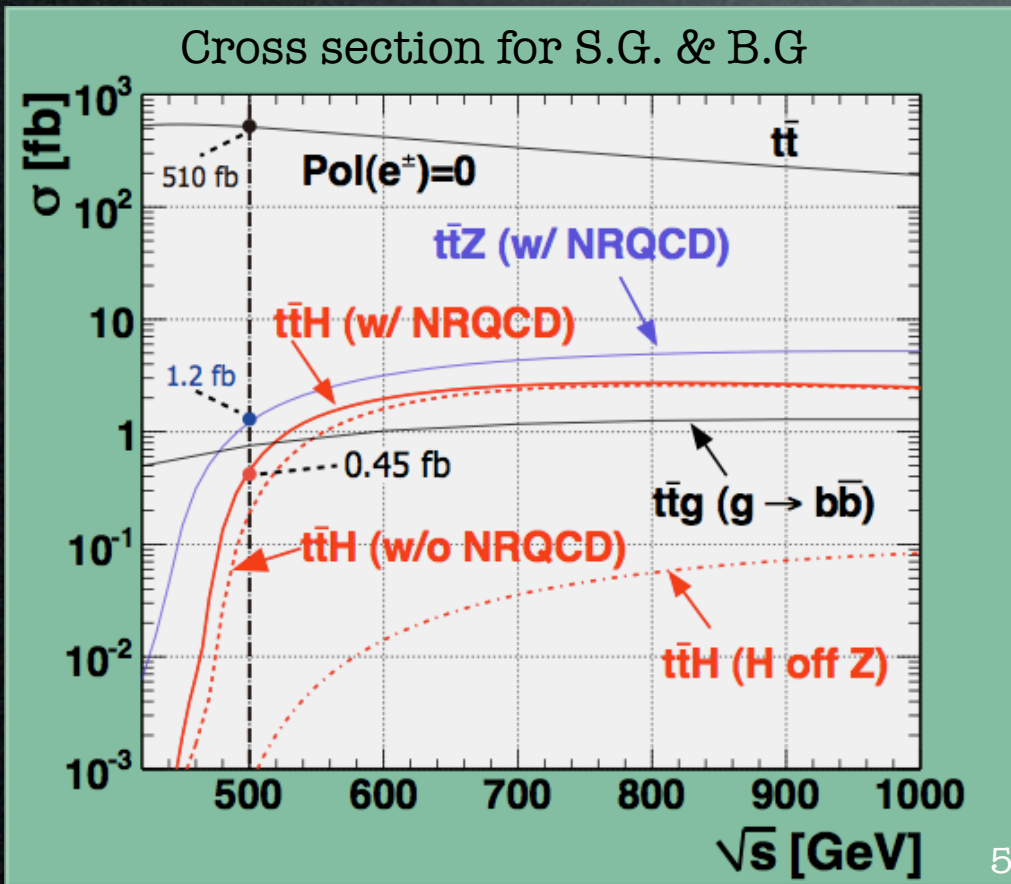
Feature of signal process ($e^+e^- \rightarrow ttH$)

event signature in our study

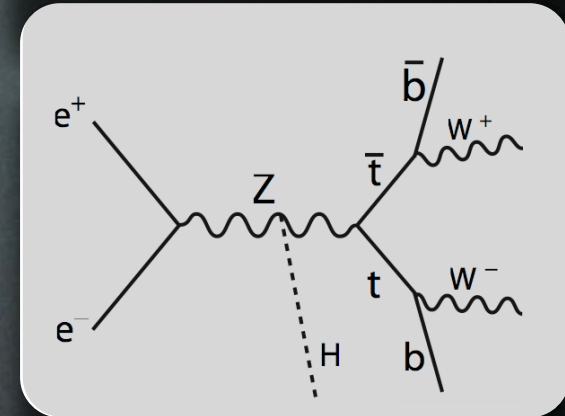
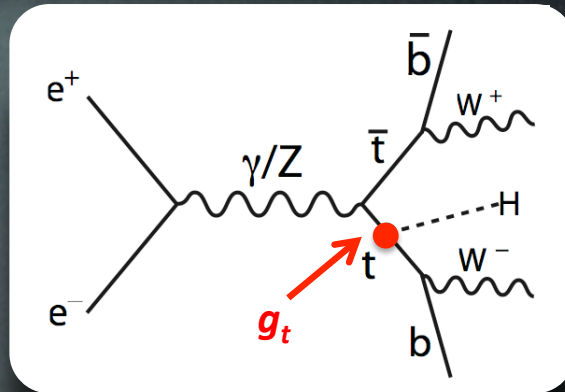
$ttH \rightarrow bWbWbb$ ($H \rightarrow bb$: 68%)

8jet, 1-lepton + 6jet, and 2 lepton + 4-jet

At $E_{cm} = 500$ GeV, ttH production is dominated by s-channel γ / Z exchange.



$e^+e^- \rightarrow ttH$



There is contribution to ttH from Higgs-strahlung. This diagram doesn't contain top-Yukawa coupling. But its contribution is negligible because of small cross section.

The cross section for ttH , tt , ttZ and $ttg^*(g \rightarrow b\bar{b})$ are shown in left plot, which includes NRQCD correction to ttH and ttZ .

$$\sigma_{ttH} = 0.45 \text{ fb without beam pol.}$$

Backgrounds

Main backgrounds

ttZ followed by $Z \rightarrow bb$ (15%) same final state ($t\bar{t}Z \rightarrow bW bW b\bar{b}$)

└─→ irreducible background

tt threshold correction enhances σ_{ttZ} from 0.7fb to 1.3fb

ttg^* followed by $g^* \rightarrow b\bar{b}$ same final state ($t\bar{t}g^* \rightarrow bW bW b\bar{b}$)

└─→ irreducible background

tt

- huge cross section (500fb)
- hard gluon emission from bottom quarks mimic signal
- even a tiny fraction of mis-reconstruction or b-tagging failure leads to significant background contamination.

The other possible backgrounds ?

$W^*W^*/Z^*Z \rightarrow ttbb$ small contribution (< 0.01 fb)

qq (5 flavors), WW , ZZ , ZH have different signature from ttH signal.

- can be separated with 4×b tagging, event shape cut and mass cut

We generated signal(ttH) and main backgrounds (ttZ , ttg^* , tt).

Basic idea to reduce backgrounds

backgrounds	$t\bar{t}$	$t\bar{t}Z$	$t\bar{t}g^*$
event shape compared to $t\bar{t}H$	Effective ! different	same	same
maximum number of b-jets	2	4	4
Higgs candidate(Z, g^*) mass compared to H	none	Effective ! different	Effective ! different

Analysis Framework

- Event generator : physsim

- full helicity amplitude calculation by HELAS
- MC phase space integration by BASES/SPRING

ISR & beamstrahlung are included

NRQCD correction for ttH and ttZ is included

Dedicated ttg generator with correct color strings

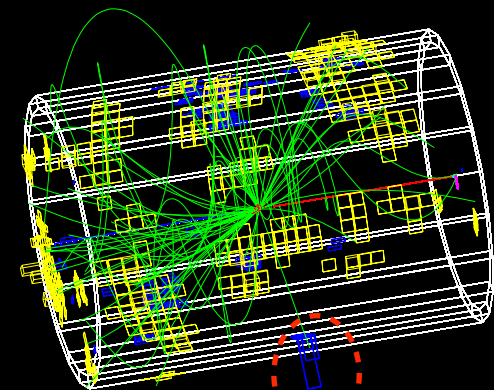
- Parton shower & hadronization: pythia

- Fast detector simulation: JSF

Detector parameters

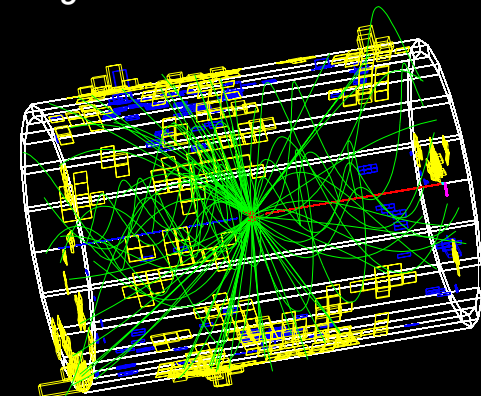
Detector	Performance	Coverage
Vertex detector	$\sigma_b = 7.0 \oplus (20.0/p) / \sin^{3/2} \theta \mu m$	$ \cos \theta \leq 0.90$
Central drift chamber	$\sigma_{P_T}/P_T = 1.1 \times 10^{-4} p_T \oplus 0.1\%$	$ \cos \theta \leq 0.95$
EM calorimeter	$\sigma_E/E = 15\%/\sqrt{E} \oplus 1\%$	$ \cos \theta \leq 0.90$
Hadron calorimeter	$\sigma_E/E = 40\%/\sqrt{E} \oplus 2\%$	$ \cos \theta \leq 0.90$

ttH L+6-jet mode event display



Isolated lepton(electron)

ttH 8-jet mode event display



Charged particle tracks

Signals on H-Cal.

Signals on E-Cal.

Cut values

the following values were chosen to yield optimized value of measurement significance.

6-Jet + lepton	8-Jet
# of isolated lepton = 1	# of isolated lepton = 0
$Y_{5 \rightarrow 4} = 0.005$	$Y_{8 \rightarrow 7} = 0.00082$
thrust > 0.85	thrust > 0.8
b-tagging (at least 4 b-jet)	b-tagging (at least 4 b-jet)
140 GeV < top mass < 205 GeV	136 GeV < top mass < 205 GeV
90 GeV < higgs mass < 150 GeV	85 GeV < higgs mass < 150 GeV

Cut flow (**6Jet + lepton**, lumi. = 1 ab⁻¹, unpolarized beams)

Cut	ttH(6J+L)	ttH (8J, 4J+2L)	tt	ttZ	ttg* (g* -> bb)	significance
no cut	167	212	514076	1340	697	0.23
Single isolated lepton	106.1	28.6	180112	441	242	0.25
thrust < 0.85	104	27.2	147518	423	225	0.27
$Y_{5 \rightarrow 4} > 0.005$	86.1	17.4	10407	264	84.8	0.82
4×b-tagging	33.9	2.9	137	34.2	28.3	2.21
mass cut	28.5	1.0	27.4	23.6	11.3	2.97

H -> bb (68%) Z->bb (15%)

Cut flow (**8Jet**, lumi. = 1 ab⁻¹, unpolarized beams)

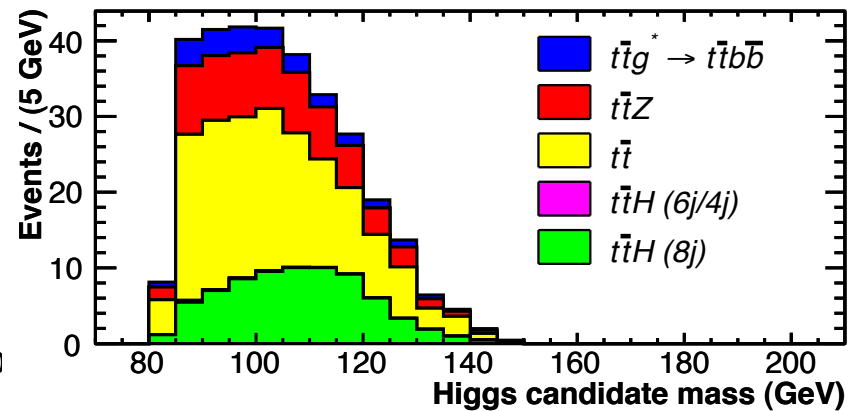
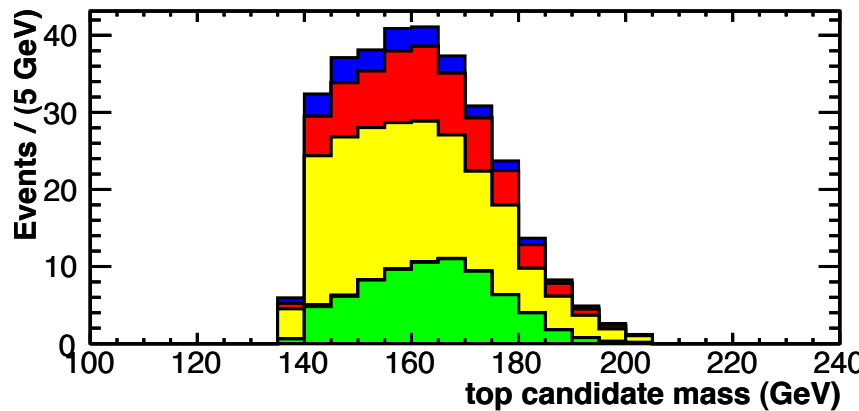
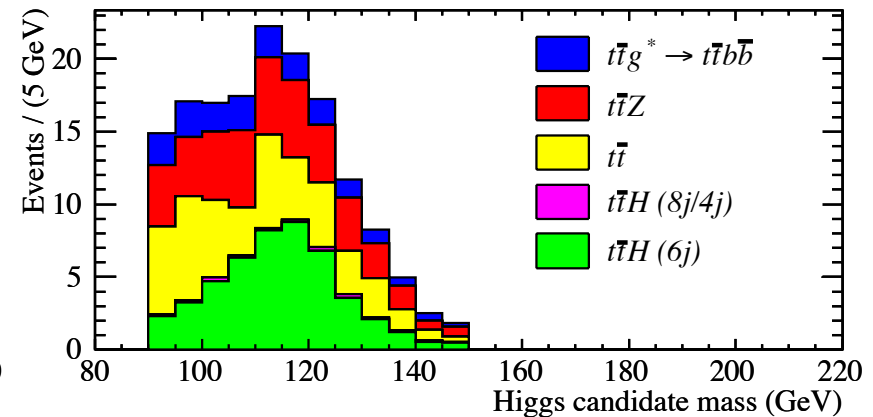
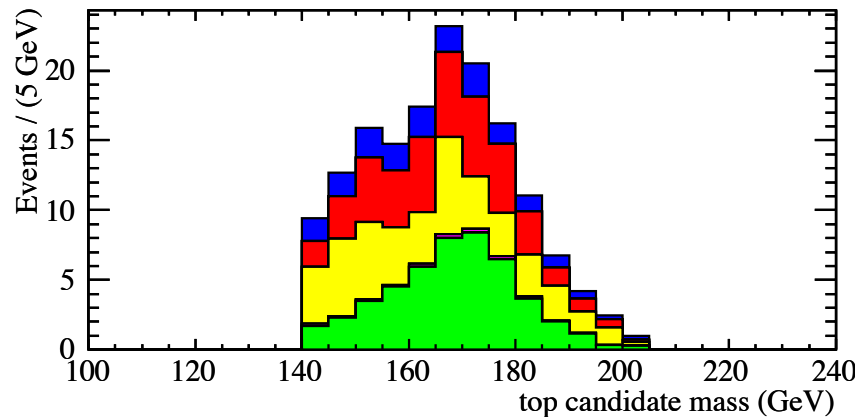
Cut	ttH(8J)	ttH (6J+L, 4J+2L)	tt	ttZ	ttg* (g* -> bb)	significance
no cut	172	207	514076	1340	697	0.24
Isolated lepton veto	158	54	306582	752	418	0.28
thrust < 0.8	153	49.4	240148	716	377	0.31
$Y_{8 \rightarrow \gamma} > 0.00082$	104	13.5	9651	296	79.1	1.03
4×b-tagging	61.3	7.0	357	63.4	46.2	2.65
mass cut	43.8	0.4	93.4	34.5	13.8	3.21

H -> bb (68%) Z->bb (15%)

Mass plot

6-jet + lepton

8-jet



Top Mass

Higgs Mass

Beam polarization (P_{e^-}, P_{e^+}) = (-0.8, +0.3)

Integrated luminosity 1ab^{-1}

Result summary

 1ab^{-1}

Beam pol. (e^- , e^+)	6Jet+lepton		8Jet	
	S / N	significance	S / N	significance
(0, 0)	28.5 / 63.3	2.97	43.8 / 142.1	3.21
(-0.8, +0.3)	48.2 / 107.3	3.87	73.6 / 244.4	4.13

Combined results

 1ab^{-1}

Beam pol. (e^- , e^+)	Combined significance	Combined $\Delta g_t/g_t$
(0, 0)	4.37	11.4%
(-0.8, +0.3)	5.66	8.8%

(stat. error only)

Summary & Plan

We assumed **early stage ILC**

- $E_{\text{cm}} = 500 \text{ GeV}$
- luminosity 1 ab^{-1}
- polarized beams $(-0.8, +0.3)$

Fast simulation studies suggests

$\sim 10\%$ accuracy on top-Yukawa coupling is achievable.

We will move on to full simulation studies.

Backup

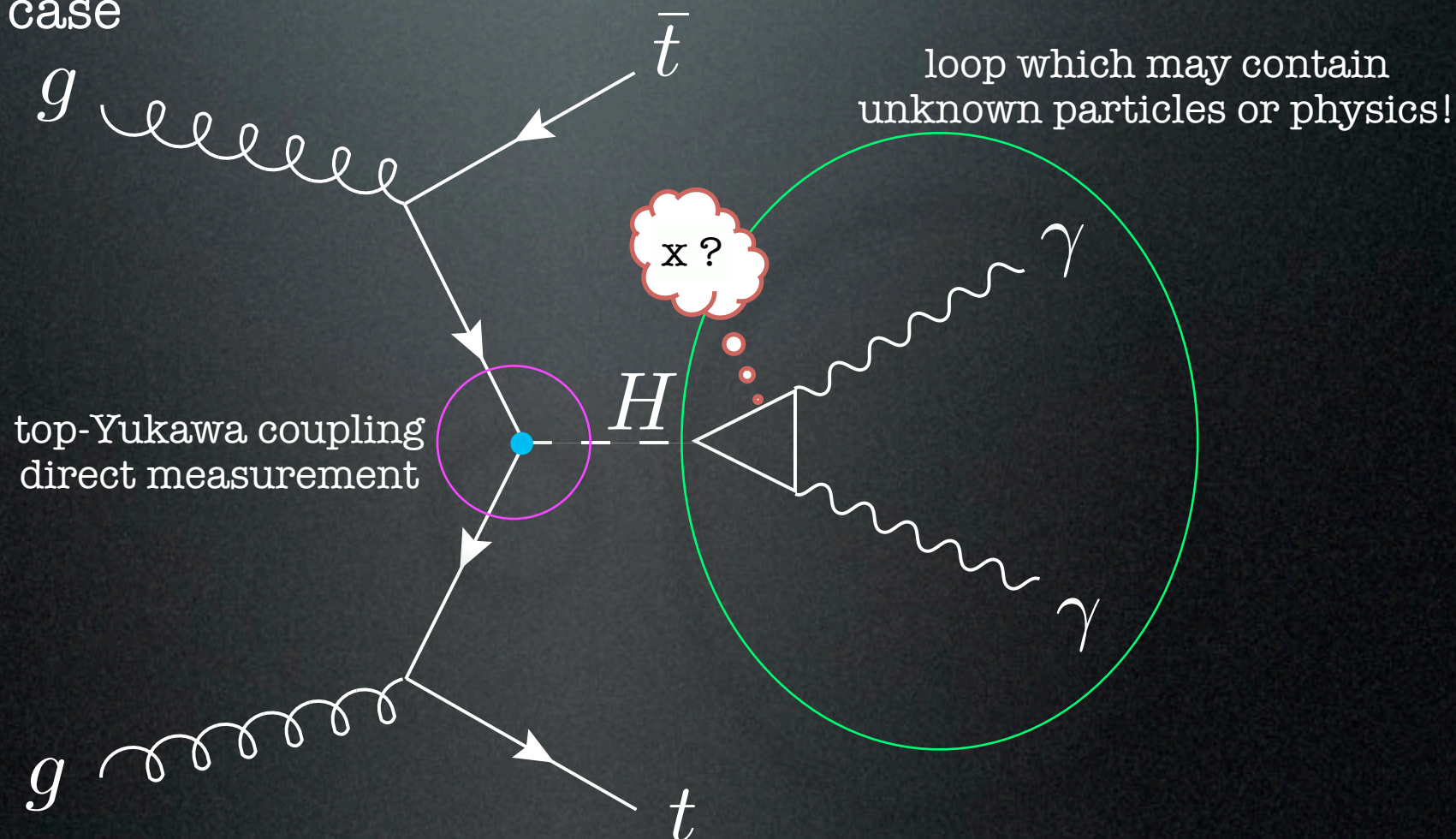
Direct measurement at LHC

may be possible at LHC using $H \rightarrow \gamma\gamma, \tau\tau$

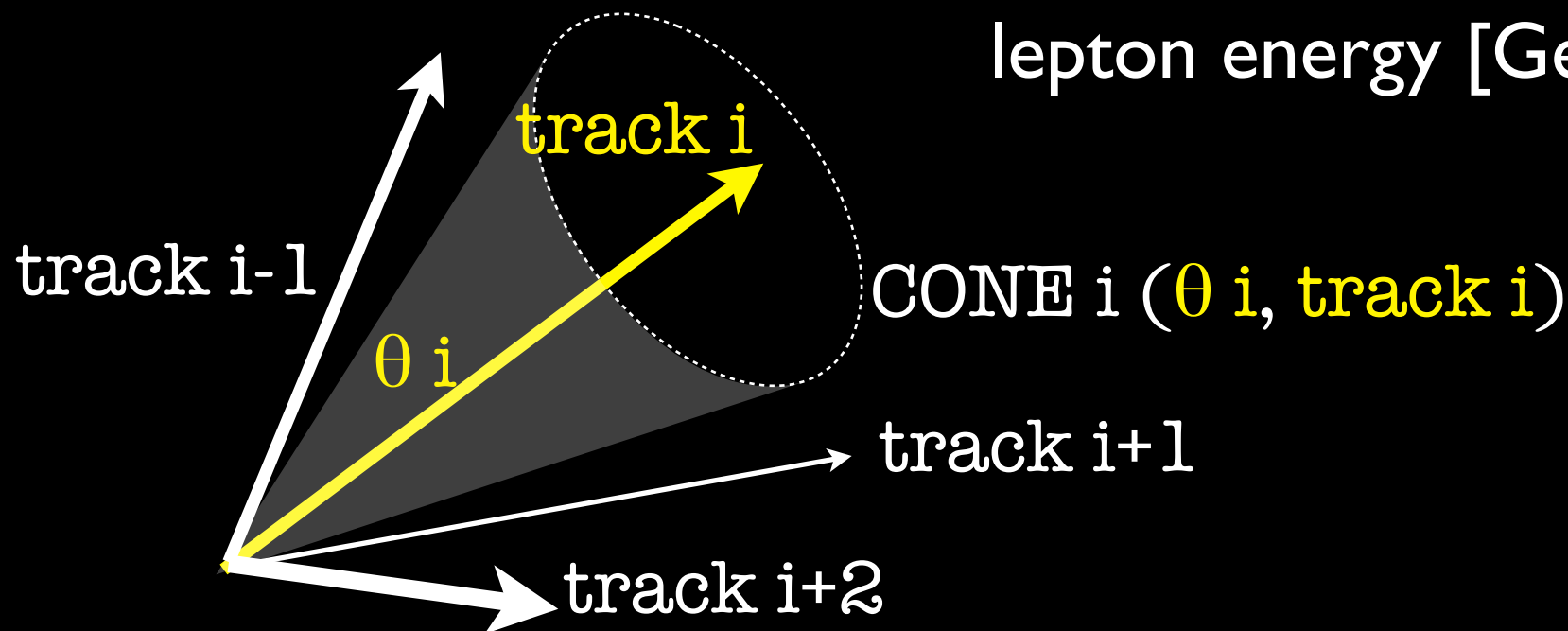
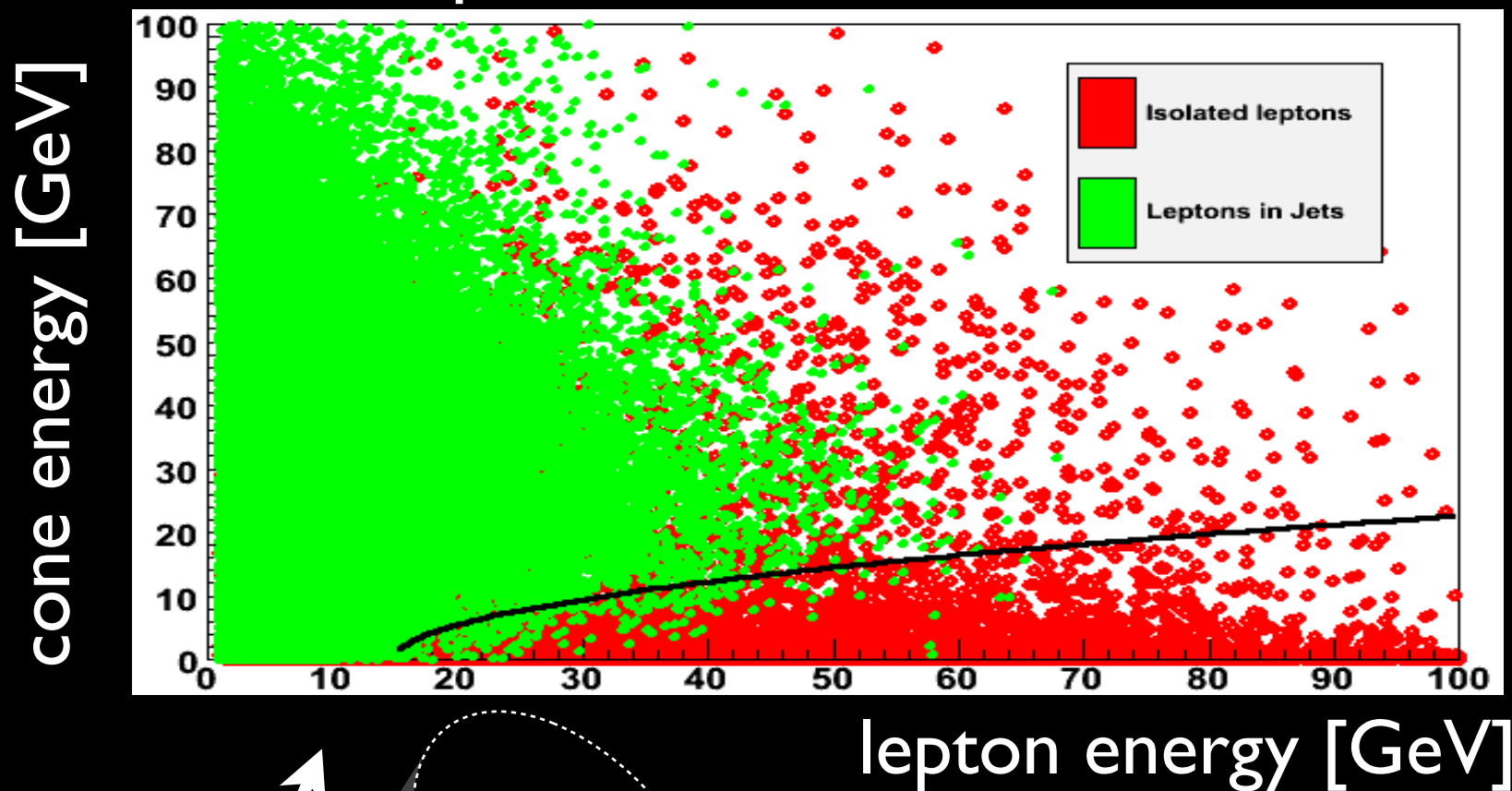
but in this case **needs accurate BR($H \rightarrow \gamma\gamma, \tau\tau$) information**

Or need to assume certain model .

$H \rightarrow \gamma\gamma$ case



Isolated lepton

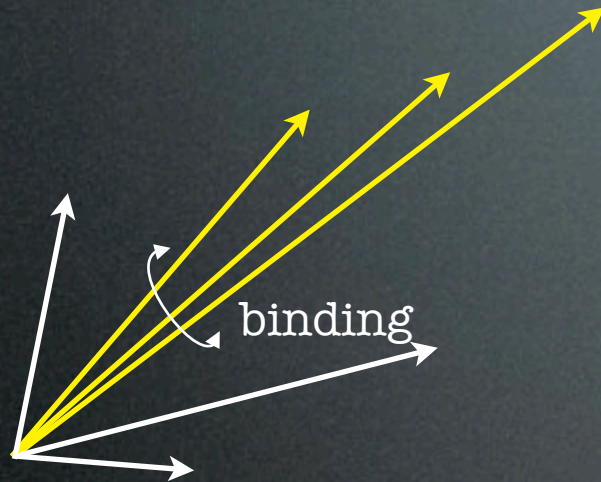


Jet Clustering

using Forced n-jet clustering

Forced n-jet clustering

1. Putting together tracks around a seed track until \mathcal{Y} reaches a certain value (Y_{cut}).



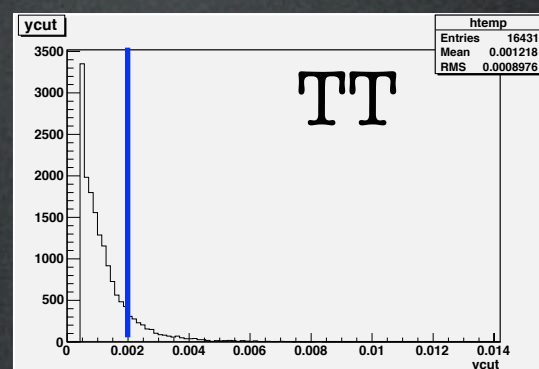
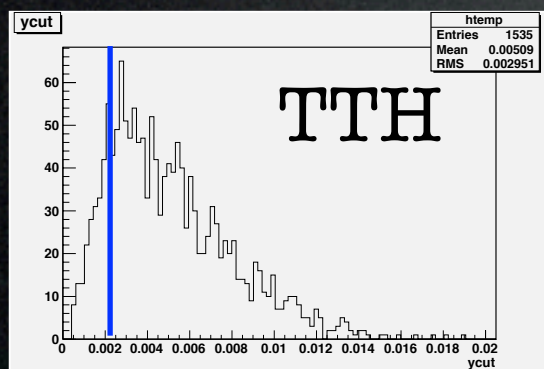
while ...

$$Y_{ij} = \frac{\min\{E_i^2, E_j^2\}(1 - \cos\theta_{ij})}{E_{\text{cm}}^2}$$

(Durham jet clustering)

2. Forced n-jet clustering always makes n jets by adjusting Y_{CUT} automatically for every event.

If we apply Forced 6-Jet Clustering for 4-Jet event, Y_{cut} will be small.



b-tag

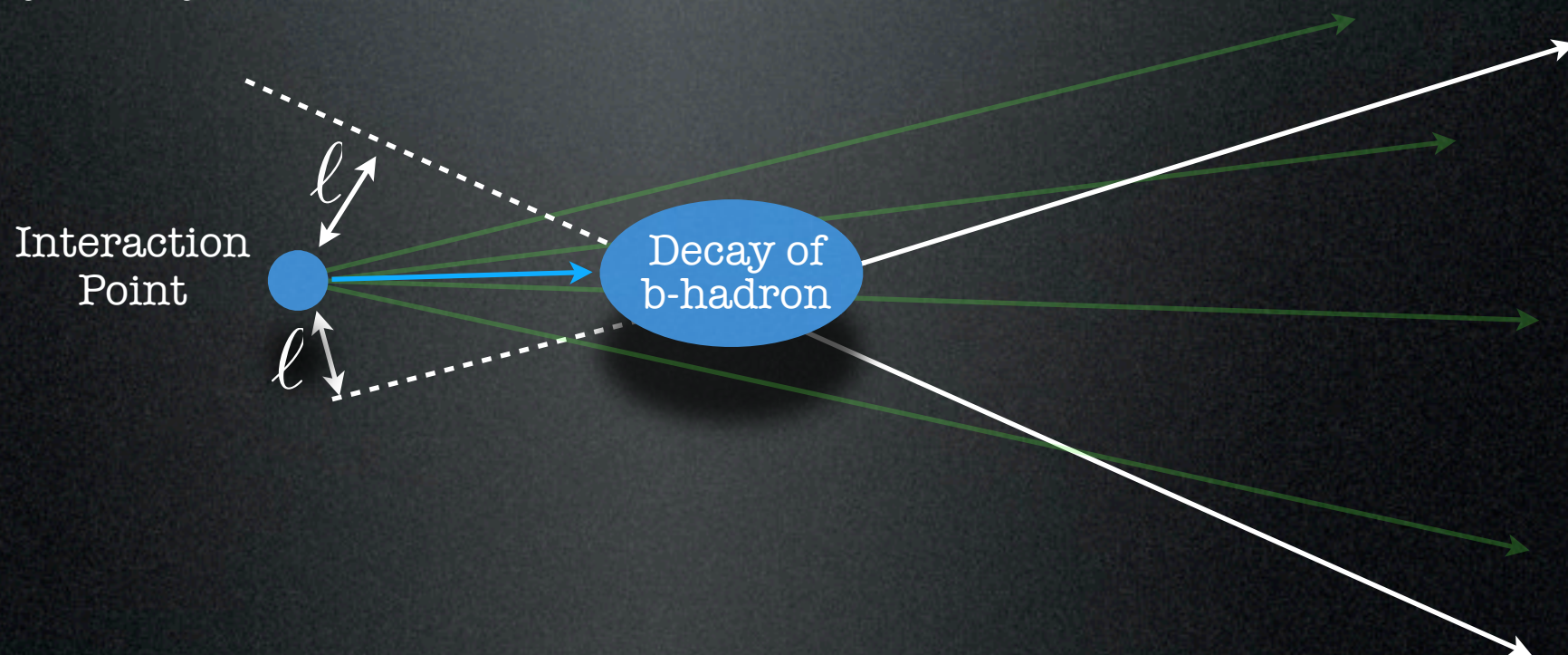
n-sig method

n-sig method

Given the distance between a tracks and IP, ℓ
and the measurement error, σ_ℓ

define the track as “off vertex track” if $\frac{\ell}{\sigma_\ell}$ is over a certain value

define the jet as b-jet if the number of “off vertex tracks” in a Jet is over a certain value.



Definition of polarization

$$P_-^e = - \frac{N_-^e - N_+^e}{N_+^e + N_-^e}$$

N_-^e : # of left handed electrons

$$P_+^p = \frac{N_+^p - N_-^p}{N_+^p + N_-^p}$$

N_+^p : # of right handed positrons

g_{tth} measurement accuracy

$$\frac{\Delta g_{tth}^2}{g_{tth}^2} = \frac{\Delta \sigma_{tth}}{\sigma_{tth}} = \frac{\Delta(N_{obs}/(\eta_{all} \cdot L))}{N_{tth}/(\eta_{all} \cdot L)} = \frac{\sqrt{(\sigma_{tth} \cdot \eta_{tth} + \sigma_{BG} \cdot \eta_{BG}) \cdot L}}{\sigma_{tth} \cdot \eta_{tth} \cdot L}$$

χ^2 definition

$$\chi^2 = \frac{(m2j - M_H)^2}{\sigma_H^2} + \frac{(m2j - M_{W_1})^2}{\sigma_{W_1}^2} + \frac{(m3j - M_{t_1})^2}{\sigma_{t_1}^2} + \frac{(m2j - M_{W_2})^2}{\sigma_{W_2}^2} + \frac{(m3j - M_{t_2})^2}{\sigma_{t_2}^2}$$

1 Lepton + 6Jet mode analysis

8Jet mode analysis

ttH analysis

6 jet + 1 lepton mode

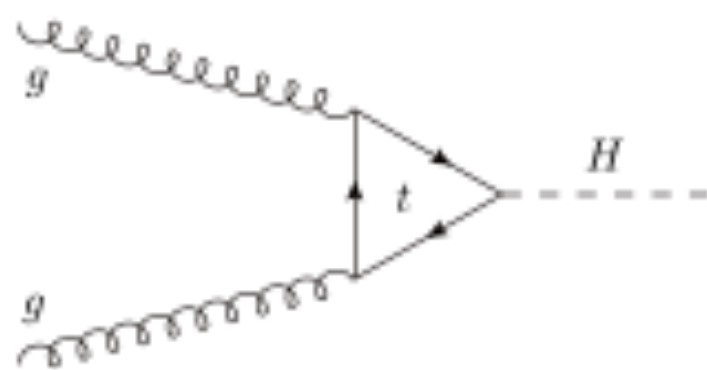
- Find isolated lepton from W (semileptonic decay)
- Jet clustering to be 6 jet (Durham algorithm)
- Event shape cut (thrust, jet clustering)
- Find 4 b jets.
- Invariant mass cut for top and higgs candidates.

8 jet mode

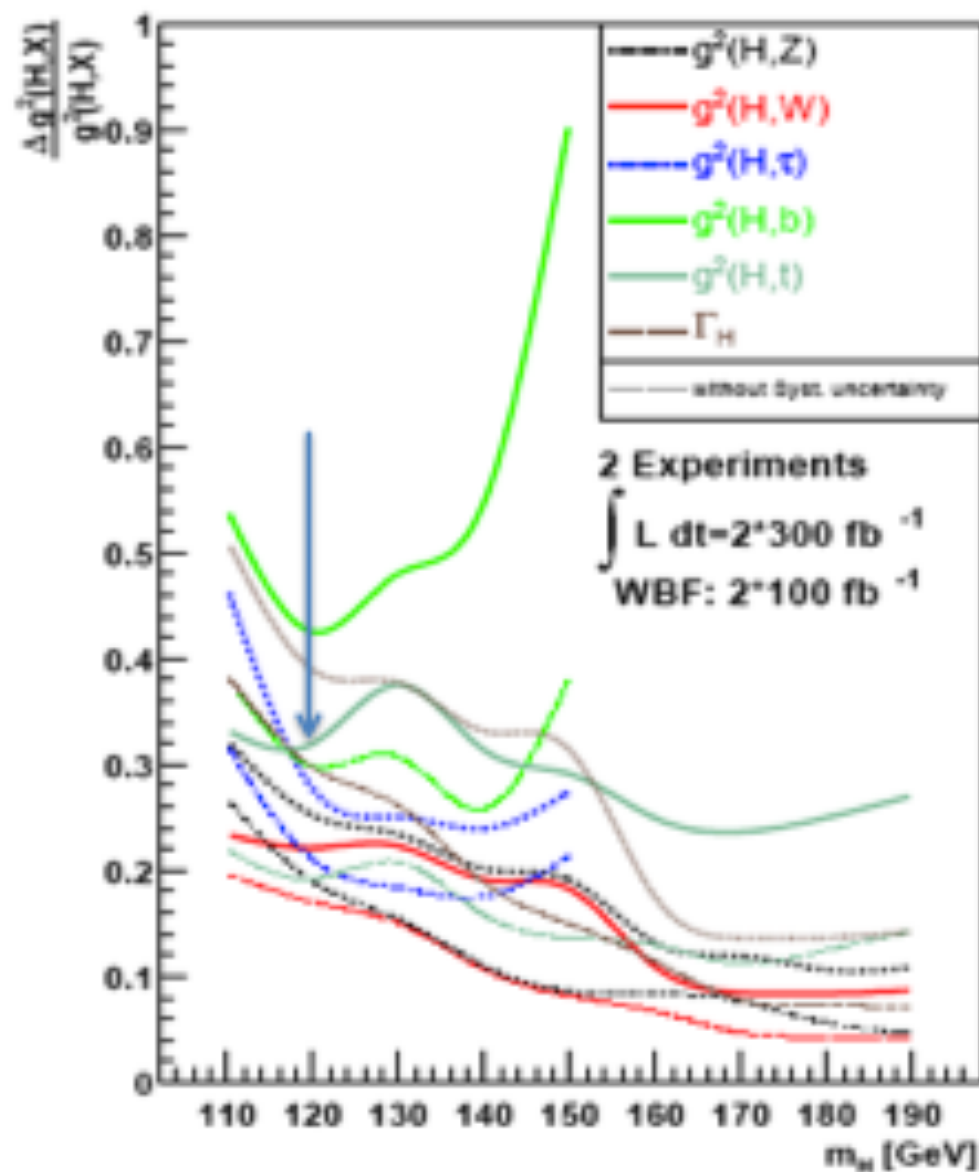
- Isolated lepton veto
- Jet clustering to be 8 jet (Durham algorithm)
- Event shape cut (thrust, jet clustering)
- Find 4 b jets.
- Invariant mass cut for top and higgs candidates.

situation at LHC

- at the LHC, **direct** measurement of the top Yukawa coupling ($pp \rightarrow ttH$) is thought to be impossible due to **too much background**
- through indirect measurement involving **gluon fusion** with a **top loop**,



g_t measurement precision is estimated to be **$\sim 15\%$** for $M_H = 120$ GeV with $2 \times 300 \text{ fb}^{-1}$ data at $E_{\text{cm}} = 14$ TeV



data samples

process	xsec (fb)	generated events	equivalent luminosity (ab ⁻¹)
ttH	1.24	50,000	40.3
ttZ	4.04	50,000	12.4
ttg (g->bb)	1.93	50,000	25.9
tt	1440.	7,000,000	4.9
ttH	0.540	50,000	92.6
ttZ	1.324	50,000	37.8
ttg (g->bb)	0.859	50,000	58.2
tt	618	5,000,000	8.1

e-/e+ polarization = (-1.0, +1.0)

e-/e+ polarization = (+1.0, -1.0)