Top-Quark Pair Production in Randall-Sundrum Models:

The Forward-Backward Asymmetry and Prospects at the ILC

Florian Goertz





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M. Bauer, FG, U. Haisch, T. Pfoh and S. Westhoff, arXiv:1008.0742[hep-ph],...

Outline



2 The Forward-Backward Asymmetry of the Top Quark

3 Other Observables and RS Signatures at a Linear Collider

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- ... is the only SM fermion with a Yukawa coupling of O(1)
- ... might be deeply connected to the mechanism of electroweak symmetry breaking
- ... has been detected thousands of times at the Tevatron, which allows for a determination of its mass, total production cross section and kinematic distributions with reasonable accuracy



The Top Quark in Warped Extra Dimensions...

... is even more special



Why wXD: Gauge Hierarchy Problem and Flavor Puzzle



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Just the Higgs boson has to be localized at (close to) the TeV brane in order to solve the hierarchy problem \Rightarrow Bulk-SM



Davoudiasl, Hewett, Rizzo, hep-ph/9911262, Grossman, Neubert, hep-ph/9912408

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gauge bosons have flat profiles only if gauge symmetry is not broken

 $m^{(1)}pprox 2.5~M_{
m KK}$ $M_{
m KK}=ke^{-L}\sim~TeV$

Non-trivial overlaps + doublet-singlet mixing

 \Rightarrow fields with same QN under unbroken symmetry have different couplings to gauge bosons of broken symmetry \Rightarrow tree FCNCs

RS as a Solution to the Flavor Puzzle

 RS offers an explanation for the fermion mass hierarchies and small CKM mixing angles with anarchic 5D Yukawa couplings Huber, Shafi, hep-ph/0010195; Huber, hep-ph/0303183; Casagrande, FG, Haisch, Neubert, Pfoh, 1005.4315



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Couplings of KK gauge bosons to **top quarks** enhanced by factor \sqrt{L}

The Top Quark in Warped Extra Dimensions

- Couplings involving third generation quarks could provide possibility to test the model
- Study top quark pair production, asymmetries

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The top-quark forward-backward asymmetry measured at CDF,

$$\left(A_{\rm FB}^t\right)_{\rm exp}^{p\bar{p}} = (15.0 \pm 5.0_{\rm stat.} \pm 2.4_{\rm syst.}),$$

is about 1.7 σ larger than the (robust) SM prediction

$$(A_{\rm FB}^t)_{\rm SM}^{p\bar{p}} = (5.1 \pm 0.6)$$
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 $\mathsf{D} \varnothing$ finds a value comparably above the theoretical prediction.

CDF/ANAL/TOP/PUBLIC/10224 Antunano, Kühn, Rodrigo, 0709.1652 DØ6062-CONF

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Expect to see RS signatures in 3rd generation observables
 → anomaly due to warped extra dimensions?

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- s-channel exchange of heavy particles with axial-vector couplings to fermions, g^q_Ag^t_A < 0, Candidates of models that can lead to a positive shift:
 - warped extra dimensions Djouadi, Moreau, Richard, Singh: 0906.0604
 - chiral color Frampton, Shu, Wang, 0911.2955

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Important constraints: reproduction of SM-like $\sigma_{t\bar{t}}$ and $d\sigma_{t\bar{t}}/dM_{t\bar{t}}$

The Forward-Backward Asymmetry of the Top Quark

$$A_{\rm FB}^{t} \equiv \frac{\int_{0}^{1} d\cos\theta \, \frac{d\sigma^{p\bar{p}\to t\bar{t}X}}{d\cos\theta} - \int_{-1}^{0} d\cos\theta \, \frac{d\sigma^{p\bar{p}\to t\bar{t}X}}{d\cos\theta}}{\int_{0}^{1} d\cos\theta \, \frac{d\sigma^{p\bar{p}\to t\bar{t}X}}{d\cos\theta} + \int_{-1}^{0} d\cos\theta \, \frac{d\sigma^{p\bar{p}\to t\bar{t}X}}{d\cos\theta}}$$

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$$\frac{d\sigma_{a(s)}}{d\cos\theta} \equiv \frac{1}{2} \left[\frac{d\sigma^{p\bar{p}\to t\bar{t}X}}{d\cos\theta} - \frac{d\sigma^{p\bar{p}\to t\bar{t}X}}{d\cos\theta} \right]$$

used C-symmetry of QCD:
$$\frac{d\sigma^{p\bar{p} \to ttX}}{d\cos\theta}\Big|_{\cos\theta=c} = \frac{d\sigma^{p\bar{p} \to ttX}}{d\cos\theta}\Big|_{\cos\theta=-c}$$

Charge asymmetric contribution to cross section given by convolution of parton luminosity functions with charge-asymmetric hard scattering kernels

$$\sigma_{a} = \frac{\alpha_{s}}{m_{t}^{2}} \sum_{i,j} \int_{4m_{t}^{2}}^{s} \frac{d\hat{s}}{s} f_{ij}(\hat{s}/s, \mu_{f}) A_{ij}\left(\frac{4m_{t}^{2}}{\hat{s}}\right) \qquad (\sigma_{s} : A_{ij} \to S_{ij})$$

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- In SM the LO coefficients $A_{q\bar{q}}^{(0)}$ and $A_{gg}^{(0)}$ both vanish identically
- At NLO non zero coefficient $A_{q\bar{q}}^{(1)}$ generated through interference of tree level gluon exchange with QCD box diagram and ISR/FSR





New Physics Contributions to A_{FB}^t

Consider effective dim-6 Lagrangian

$$\begin{split} \mathcal{L}_{\text{eff}} = \sum_{q,u} \sum_{A,B=L,R} \Big[\ C_{q\bar{q},AB}^{(V,8)} \ Q_{q\bar{q},AB}^{(V,8)} + C_{t\bar{u},AB}^{(V,8)} \ Q_{t\bar{u},AB}^{(V,8)} \\ + C_{t\bar{u},AB}^{(V,1)} \ Q_{t\bar{u},AB}^{(V,1)} + C_{t\bar{u},AB}^{(S,1)} \ Q_{t\bar{u},AB}^{(S,1)} \Big] \end{split}$$

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 $\begin{aligned} Q_{q\bar{q},AB}^{(V,8)} &= (\bar{q}\gamma_{\mu} T^{a} P_{A} q) (\bar{t}\gamma^{\mu} T^{a} P_{B} t) \quad Q_{t\bar{u},AB}^{(V,8)} &= (\bar{u}\gamma_{\mu} T^{a} P_{A} t) (\bar{t}\gamma^{\mu} T^{a} P_{B} u) \\ Q_{t\bar{u},AB}^{(V,1)} &= (\bar{u}\gamma_{\mu} P_{A} t) (\bar{t}\gamma^{\mu} P_{B} u) \qquad Q_{t\bar{u},AB}^{(S,1)} &= (\bar{u}P_{A} t) (\bar{t}P_{B} u) , \end{aligned}$

appropriate for broad class of BSM models

New Physics Contributions to A_{FB}^t : LO

Corrections to LO asymmetric/symmetric kernels given by interference between SM-gluon exchange and s- and t-channel new physics contributions

$$\begin{split} \mathcal{A}_{u\bar{u},\mathrm{NP}}^{(0)} &= \frac{\beta^2 \rho}{144} \,\hat{s} \, \left[C_{u\bar{u},\parallel}^{(V,8)} - C_{u\bar{u},\perp}^{(V,8)} + \frac{1}{3} \, C_{t\bar{u},\parallel}^{(V,8)} \right] + \mathrm{EW} \text{ contributions} \,, \\ \mathcal{S}_{u\bar{u},\mathrm{NP}}^{(0)} &= \frac{\beta \rho}{216} \, (2+\rho) \,\hat{s} \, \left[C_{u\bar{u},\parallel}^{(V,8)} + C_{u\bar{u},\perp}^{(V,8)} + \frac{1}{3} \, C_{t\bar{u},\parallel}^{(V,8)} \right] + \mathrm{EW} \text{ contributions} \,, \\ \mathcal{C}_{ij,\parallel}^{(V,8)} &= \mathrm{Re} \left[C_{ij,LL}^{(V,8)} + C_{ij,RR}^{(V,8)} \right] \,, \quad \mathcal{C}_{ij,\perp}^{(V,8)} = \mathrm{Re} \left[C_{ij,LR}^{(V,8)} + C_{ij,RL}^{(V,8)} \right] \,, \\ \beta = \sqrt{1-\rho} \,, \quad \rho = \frac{4m_t^2}{\hat{s}} \end{split}$$

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RS Contributions to A_{FB}^t : LO

RS contributions to the Wilson coefficients introduced before:



RS Contributions to A_{FB}^t : LO

Axial-vector couplings of quarks to gluons arise in the RS model due to the different profiles of right- and left-handed (singlet/doublet) quark zero modes



RS Contributions to A_{FB}^t : LO

Expansion in $v^2/M_{\rm KK}^2$ and small difference of light quark bulk mass parameters leads to

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• Positive shift in σ_a possible, but LO contributions tiny due to elementary nature (UV localization: $c_a < -1/2$) and nearly vector like couplings of **light quarks** (keep in mind: still has to divide by σ_s)

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- Given the smallness of the LO contribution: look at NLO

New Physics Contributions to A_{FB}^t : NLO

At NLO: σ_a gets contributions from vector-currents

$$\left[d_{abc}^{2}=\left(2\mathrm{Tr}\left(\left\{T^{a},\,T^{b}\right\}T^{c}\right)\right)^{2}\,\mathrm{terms}\right]$$

Kühn, Rodrigo, hep-ph/9802268, hep-ph/9807420



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 In models with small axial-vector couplings to light quarks and no significant FCNC effects in the t-channel, e.g. models which solve the flavor puzzle by (geometrical) sequestering, the NLO corrections often exceed the LO ones

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- RS condition:

$$rac{lpha_{s}}{4\pi}\left(1+c_{t_{L}}+c_{t_{R}}
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• For typical bulk masses: $\sigma_a^{(1)}/\sigma_a^{(0)}\sim 25$ (IR localization of top)

RS Contributions to A_{FB}^t : NLO

c _{tL}		$\tilde{C}_{u\bar{u}}^V/\alpha_s$	$\tilde{C}^{A}_{u\bar{u}}/\alpha_{s}$	$\tilde{C}_{d\bar{d}}^{V}/\alpha_{s}$	$\tilde{C}^{A}_{d\bar{d}}/\alpha_{s}$	$\tilde{C}_{t\bar{u}}^V/\alpha_s$	$\tilde{C}_{t\bar{u}}^{S}$
-0.41	0.09	4.50	$0.71 \cdot 10^{-2}$	0.68	$-1.40 \cdot 10^{-3}$	$-1.35 \cdot 10^{-4}$	$8.2 \cdot 10^{-7}$
-0.47	0.48	4.95	$0.22 \cdot 10^{-2}$	0.27	$-0.03 \cdot 10^{-3}$	$-0.70 \cdot 10^{-4}$	$4.1 \cdot 10^{-7}$
-0.49	0.90	5.31	$1.79 \cdot 10^{-2}$	0.08	$-0.64 \cdot 10^{-3}$	$-2.45 \cdot 10^{-4}$	$122 \cdot 10^{-7}$

$$(A_{\rm FB}^t)_{\rm RS}^{p\bar{p}} = \left[\frac{1 + 0.22\,\tilde{C}_{u\bar{u}}^A + 0.034\,\tilde{C}_{u\bar{u}}^V + \dots}{1 + 0.053\,\tilde{C}_{u\bar{u}}^V + \dots}\right] \left(5.6^{+0.8}_{-1.0}\right)\%,$$

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RS Contributions to A_{FB}^t : NLO



- Red: excluded by $Z \rightarrow b\bar{b}$
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Outline

The Top Quark (in Warped Extra Dimensions)

2 The Forward-Backward Asymmetry of the Top Quark

3 Other Observables and RS Signatures at a Linear Collider

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De Pree, Sher, hep-ph/0603105

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Rare Top Decays

Significant effects possible in $t \rightarrow c Z$ and $t \rightarrow ch$



Summary

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Summary

Thank you for your attention!

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Backup: RS as a Solution to the Flavor Puzzle



one-to-one correspondence to Froggatt-Nielsen mechanism

Froggatt, Nielsen, Nucl. Phys. B 147, 277 (1979)

S. Casagrande, FG, U. Haisch, M. Neubert, T. Pfoh, 1005.4315

Backup: Custodial Protection

Implement custodial protection by extending the SM gauge group

 $SU(3)_c \times SU(2)_L \times SU(2)_R \times U(1)_X \times P_{LR}$

•
$$SU(2)_R \times U(1)_X \xrightarrow{\mathrm{UV}} U(1)_Y$$

- P_{LR} : interchange $SU(2)_L \leftrightarrow SU(2)_R$
- T parameter protected

•
$$b_L \in (2,2)_{2/3}
ightarrow Zb_L ar{b}_L$$
 protected

Agashe, Delgado, May, Sundrum, hep-ph/0308036,

Agashe, Contino, Da Rold, Pomarol, hep-ph/0605341

alternative option: heavy Higgs, Casagrande, FG, Haisch, Neubert, Pfoh, 0807.4937

Backup: Rare Decays $t \rightarrow cZ^0$ and $t \rightarrow ch$

• Expect sizable efects due to IR localization of top quark

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