# CLIC FFS New Tuning Techniques 

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- Alignment procedure
- Basic equations
- CLIC case
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- Summary and conclusions


## Alignment Procedure

Four steps:

- With the multipole magnets switched Off

1) Orbit Correction (1-to-1)
2) Orbit + Target Dispersion Steering

- Beam-based centering of the multipole magnets

3) Multipole-shunting, one by one

- With the multipole magnets On

4) Orbit + Target Dispersion-Coupling-Beta-Beating Steering
$\Rightarrow$ A more detailed explanation of this method can be found in the Proceedings of LINAC10:
A. Latina, MOP026, LINAC10.

## Basic Equations

Given a system:

$$
\begin{equation*}
\mathbf{y}=\mathbf{f}(\mathrm{x}) \tag{1}
\end{equation*}
$$

its Taylor expansion around $\mathbf{x}_{\mathbf{0}}, \mathbf{y}_{\mathbf{0}}=\mathbf{f}\left(\mathbf{x}_{\mathbf{0}}\right)$ is

$$
\begin{equation*}
\mathbf{y}=\mathbf{y}_{\mathbf{0}}+\left.\frac{\partial \mathbf{f}}{\partial \mathbf{x}}\right|_{\mathbf{x}_{\mathbf{0}}}\left(\mathbf{x}-\mathbf{x}_{\mathbf{0}}\right)+\ldots \tag{2}
\end{equation*}
$$

$\mathbf{A}=\left.\frac{\partial \mathbf{f}}{\partial \mathbf{x}}\right|_{\mathbf{x}_{\mathbf{0}}}$ is the Jacobian, or response matrix, of the system.

The linear approximation of eq. (1) around $\left(\mathbf{x}_{\mathbf{0}}, \mathbf{y}_{\mathbf{0}}\right)$ is therefore:

$$
\begin{equation*}
\mathbf{y} \approx \mathbf{y}_{\mathbf{0}}+\mathbf{A}\left(\mathbf{x}-\mathbf{x}_{\mathbf{0}}\right) \tag{3}
\end{equation*}
$$

## Linear Approximation and Least Squares Method

This is our "model":

$$
\mathbf{y}=\mathrm{y}_{0}+\mathbf{A}\left(\mathrm{x}-\mathrm{x}_{\mathbf{0}}\right)
$$

Where, in our case:
$\mathrm{x}: \quad$ is the vector of the correctors
y : is the vector of the observables
A: is the response matrix
$\mathrm{x}_{\mathbf{0}}, \mathrm{y}_{\mathbf{0}}$ : is the central point :
correctors to zero $\rightarrow$ observables for the reference trajectory
$\Rightarrow$ the observables we will use are: orbit, dispersion, beta-beating and coupling.

Given an arbitrary system configuration, $\mathbf{y}=\mathbf{y}_{\text {Measured }}$, the corresponding correctors, x , that match this status, can be found solving the least squares minimization of the function:

$$
\chi^{2}=\left\|\mathbf{y}_{\text {Measured }}-\left[\mathbf{y}_{0}+\mathbf{A}\left(\mathbf{x}_{\text {Unknown }}-\mathbf{x}_{0}\right)\right]\right\|^{2}
$$

## Least Squares Method and Singular Value Decomposition

The solution, $\mathbf{x}$, of the previous equation is given by $\frac{\partial \chi^{2}}{\partial \mathbf{x}}=\mathbf{0}$ :

$$
\mathbf{y}_{\mathrm{M}}-\mathbf{y}_{0}=\mathbf{A}\left(\mathbf{x}-\mathbf{x}_{0}\right)
$$

Being $\mathbf{x}_{0}=0$,

$$
\mathbf{y}_{\mathrm{M}}-\mathbf{y}_{\mathbf{0}}=\mathbf{A x}
$$

The matrix A is likely not squared, having usually more observables than correctors $\rightarrow$ the system is overdetermined. One way to solve overdetermined systems is to use the Singular Value Decomposition of this matrix.

The solution is:

$$
\mathbf{x}=\mathbf{A}^{\dagger}\left(\mathbf{y}_{\mathbf{M}}-\mathbf{y}_{\mathbf{0}}\right)
$$

where $\mathbf{A}^{\dagger}$ is the pseudo-inverse of $\mathbf{A}$ in the SVD-sense.

## Beam Delivery System

In this context the correctors, x , are called
$\theta_{x} \quad$ horizontal correctors
$\theta_{y} \quad$ vertical correctors
whereas the observables, $\mathbf{y}$, are:
$\mathbf{b}_{x} \quad$ horizontal bpm readings
$\mathbf{b}_{y} \quad$ vertical bpm readings
$\boldsymbol{\eta}_{x} \quad$ horizontal dispersion at each bpm
$\boldsymbol{\eta}_{y} \quad$ vertical dispersion at each bpm
$\boldsymbol{\beta}_{x} \quad$ horizontal beta - beating at each bpm
$\boldsymbol{\beta}_{y} \quad$ vertical beta - beating at each bpm
$\mathrm{C}_{x}$ horizontal coupling at each bpm
$\mathbf{C}_{y} \quad$ vertical coupling at each bpm

## How to Measure Dispersion, Coupling and Beta-Beating (1/2)

To measure the dispersion, it is necessary to use one or more test-beams with different energies. We used two test beams with energy difference $\delta= \pm 0.005$ :

$$
\boldsymbol{\eta}=\frac{b_{+\delta}-b_{-\delta}}{2 \delta}
$$

To measure the horizontal beta-beating, it is necessary to have the first corrector kicking in $x= \pm 1$, then measure the horizontal response of the system:

$$
\boldsymbol{\beta}_{x}=\frac{b_{x \mid \theta_{1, x=+1}}-b_{x \mid \theta_{1, x=-1}}}{2 \Delta \theta_{1, x}}
$$

To measure the vertical beta-beating, it is necessary to have the first corrector kicking in $y= \pm 1$, then measure the vertical response of the system:

$$
\boldsymbol{\beta}_{y}=\frac{b_{y \mid \theta_{1, y=+1}}-b_{y \mid \theta_{1, y=-1}}}{2 \Delta \theta_{1, y}}
$$

## How to Measure Dispersion, Coupling and Beta-Beating (2/2)

To measure the horizontal coupling, it is necessary to have the first corrector kicking in $y= \pm 1$, then measure the horizontal response of the system:

$$
\mathbf{C}_{x}=\frac{b_{x \mid \theta_{1, y=+1}}-b_{x \mid \theta_{1, y=-1}}}{2 \Delta \theta_{1, y}}
$$

To measure the vertical coupling, it is necessary to have the first corrector kicking in $x= \pm 1$, then measure the vertical response of the system:

$$
\mathbf{C}_{y}=\frac{b_{y \mid \theta_{1, x=+1}}-b_{y \mid \theta_{1, x=-1}}}{2 \Delta \theta_{1, x}}
$$

$\Rightarrow$ Notice that to obtain these 6 quantities,

$$
\underbrace{\boldsymbol{\eta}_{x}, \boldsymbol{\eta}_{y}}_{\delta= \pm 0.5 \%}, \underbrace{\boldsymbol{\beta}_{x}, \mathbf{C}_{x}}_{\theta_{1, x= \pm 1}}, \underbrace{\boldsymbol{\beta}_{y}, \mathbf{C}_{y}}_{\theta_{1, y= \pm 1}}
$$

a total of six measurements is required.

## Alignment Algorithm (1/2)

Multipoles OFF

1) Orbit correction

$$
\binom{\mathbf{b}_{x}}{\mathbf{b}_{y}}=\left(\begin{array}{cc}
R_{x x} & 0 \\
0 & R_{y y}
\end{array}\right)\binom{\boldsymbol{\theta}_{x}}{\boldsymbol{\theta}_{y}}
$$

2) Target Dispersion Steering

$$
\left(\begin{array}{c}
\mathbf{b}_{x} \\
\mathbf{b}_{y} \\
\boldsymbol{\eta}_{x}-\boldsymbol{\eta}_{0, x} \\
\boldsymbol{\eta}_{y}-\boldsymbol{\eta}_{0, y}
\end{array}\right)=\left(\begin{array}{cc}
R_{x x} & 0 \\
0 & R_{y y} \\
D_{x x} & 0 \\
0 & D_{y y}
\end{array}\right)\binom{\boldsymbol{\theta}_{x}}{\boldsymbol{\theta}_{y}}
$$

$\Rightarrow$ it requires one or two test beams, with $E=E_{0}(1 \pm 0.005)$, to measure the dispersion.

## Alignment Algorithm (2/2)

Multipoles ON
3) Beam-based centering of each individual multipolar element (see later for details)
4) Coupling and Beta-Beating Steering

$$
\left(\begin{array}{c}
\mathbf{b}_{x} \\
\mathbf{b}_{y} \\
\boldsymbol{\eta}_{x}-\boldsymbol{\eta}_{0, x} \\
\boldsymbol{\eta}_{y}-\boldsymbol{\eta}_{0, y} \\
\boldsymbol{\beta}_{x}-\boldsymbol{\beta}_{0, x} \\
\boldsymbol{\beta}_{y}-\boldsymbol{\beta}_{0, y} \\
\mathbf{C}_{x} \\
\mathbf{C}_{y}
\end{array}\right)=\left(\begin{array}{cc}
R_{x x} & 0 \\
0 & R_{y y} \\
D_{x x} & 0 \\
0 & D_{y y} \\
B_{x x} & 0 \\
B_{y x} & 0 \\
0 & C_{x y} \\
0 & C_{y y}
\end{array}\right)\binom{\boldsymbol{\theta}_{x}}{\boldsymbol{\theta}_{y}}
$$

$\Rightarrow$ it requires four shots -nominal energy- with the first corrector $\mathrm{ON}, \Delta \theta_{1, x \mid y}= \pm$ small kick, to measure beta-beating and coupling.

## Orbit Response Matrix

Jacobian of the system:

$$
\mathbf{R}=\frac{\partial \mathbf{b}}{\partial \theta} ; \quad \mathbf{R}_{i j}=\frac{b_{i ;+\Delta \theta_{j}}-b_{i ;-\Delta \theta_{j}}}{2 \Delta \theta_{j}}
$$

Response matrices: $R_{x x}, R_{y y}$



Target Responses:



## Dispersion Response Matrix

Jacobian of the system:

$$
\mathbf{D}=\frac{\partial \eta}{\partial \theta}=\frac{\eta_{i ;+\Delta \theta_{j}}-\eta_{i ;-\Delta \theta_{j}}}{2 \Delta \theta_{j}}=\frac{\partial}{\partial \theta} \frac{\partial \mathbf{b}}{\partial \mathbf{E}}
$$

Response matrices: $D_{x x}, D_{y y}$



Target Responses:



## Beta-Beating Response Matrix

Jacobian of the system:

$$
\mathbf{B}_{\mathbf{x} \mid \mathbf{y}}=\frac{\partial \beta}{\partial \theta}=\frac{\partial}{\partial \theta} \frac{\partial \mathbf{b}_{\mathbf{x} \mid \mathbf{y}}}{\partial \theta_{1, \mathbf{x} \mid \mathbf{y}}}
$$

Response matrices: $B_{x x}, B_{y x}$



Target Responses:


## Coupling Response Matrix

Jacobian of the system:

$$
\mathbf{C}_{\mathbf{x} \mid \mathbf{y}}=\frac{\partial \mathbf{c}}{\partial \theta}=\frac{\partial}{\partial \theta} \frac{\partial \mathbf{b}_{\mathbf{x} \mid \mathbf{y}}}{\partial \theta_{\mathbf{1 , \mathbf { y }} \mid \mathbf{x}}}
$$




Target Responses:



## The Actual Systems of Equations

For simplicity I did not mention that we have also:

- the $\omega$-terms, ie. the weights
- the SVD-term $\beta$ to control and limit the amplitude of the correction

So the actual systems of equations are the following:

1) Target Dispersion Steering

$$
\left(\begin{array}{ll} 
& \mathbf{b} \\
\omega_{1} & \binom{\left.\boldsymbol{\eta}-\boldsymbol{\eta}_{0}\right)}{\mathbf{0}}=\left(\begin{array}{rl} 
& \mathbf{R} \\
\omega_{1} & \cdot \\
\mathbf{D}^{2} \\
\beta & \mathbf{I}
\end{array}\right)\binom{\boldsymbol{\theta}_{x}}{\boldsymbol{\theta}_{y}} .
\end{array}\right.
$$

2) Coupling and Beta-Beating Steering:

$$
\left(\begin{array}{ll} 
& \mathbf{b} \\
\omega_{2} & \cdot\left(\boldsymbol{\eta}-\boldsymbol{\eta}_{0}\right) \\
\omega_{3} & \cdot\left(\boldsymbol{\beta}-\boldsymbol{\beta}_{0}\right) \\
\omega_{3} & \cdot \mathbf{C} \\
& \mathbf{0}
\end{array}\right)=\left(\begin{array}{rl} 
& \mathbf{R} \\
\omega_{2} & \cdot \\
\mathbf{D} \\
\omega_{3} & \cdot \\
\omega_{3} \\
\omega_{3} & \cdot \mathbf{C} \\
\beta & \cdot \mathbf{I}
\end{array}\right)\binom{\boldsymbol{\theta}_{x}}{\boldsymbol{\theta}_{y}}
$$

$\Rightarrow$ We have four degrees of freedom to tune: $\omega_{1}, \omega_{2}, \omega_{3}$ and $\beta$.

## Beam-Based Centering of the Multipoles

Sextupoles, Octupoles and Decapoles can strongly deflect the beam when they are off-centered.

The kick that they induce depends on the difference between the beam position and the magnetic center of the magnet: $\mathrm{dx}, \mathrm{dy}$.

We scan, horizontally and vertically, the position of each multipole and register the change in beam position at the downstream bpms. We scan in the range $\mathrm{dx}, \mathrm{dy} \in[-0.5,0.5] \mathrm{mm}$.

1) Sextupoles

$$
\begin{aligned}
\Delta \mathrm{x}^{\prime} & =-\frac{1}{2} \frac{\mathrm{~S}_{\mathrm{N}}}{\mathrm{~B} \rho}\left(\mathrm{dx}^{2}-\mathrm{dy}^{2}\right) \\
\Delta \mathrm{y}^{\prime} & =+\frac{\mathbf{S}_{\mathrm{N}}}{\mathrm{~B} \rho} \mathrm{dx} \mathrm{~d} \mathbf{y}
\end{aligned}
$$


a parabolic fit in $x$ and $y$ gives $\mathrm{d} \mathbf{x}$ and $\mathrm{d} \mathbf{y}$

## Beam-Based Centering of the Multipoles

2) Octupoles

$$
\begin{aligned}
& \Delta \mathrm{x}^{\prime}=-\frac{1}{6} \frac{\mathrm{~S}_{\mathrm{N}}}{\mathrm{~B} \rho}\left(\mathrm{dx}^{3}-3 \mathrm{dxd} \mathrm{y}^{2}\right) \\
& \Delta \mathrm{y}^{\prime}=+\frac{1}{6} \frac{\mathrm{~S}_{\mathbf{N}}}{\mathrm{B} \rho}\left(\mathrm{dx}{ }^{2} \mathrm{dy}-\mathrm{dy}^{3}\right)
\end{aligned}
$$



This curve is a cubic, therefore its first derivative is a parabola. A parabolic fit of its derivative, in $x$ and $y$, gives $\mathrm{d} \mathbf{x}$ and $\mathrm{d} \mathbf{y}$
3) Decapoles

$$
\begin{aligned}
& \Delta \mathrm{x}^{\prime}=-\frac{1}{24} \frac{\mathrm{~S}_{\mathrm{N}}}{\mathrm{~B} \rho}\left(\mathrm{dx} \mathrm{x}^{4}-6 \mathrm{dx}^{2} \mathrm{dy}^{2}+\mathrm{dy}^{4}\right) \\
& \Delta \mathrm{y}^{\prime}=+\frac{1}{6} \frac{\mathrm{~S}_{\mathrm{N}}}{\mathrm{~B} \rho}\left(\mathrm{dx} \mathrm{x}^{3} \mathrm{~d} \mathbf{y}-\mathrm{dxd} \mathrm{y}^{3}\right)
\end{aligned}
$$



This curve is a parabola squared. A parabolic fit of its square root, in $x$ and $y$, gives dx and $\mathrm{d} \mathbf{y}$

## Multipoles Response Matrix

Jacobian of the system:

$$
\mathbf{S}=\frac{\partial \mathbf{b}}{\partial \theta}
$$




Target Responses:



## Simulation Setup

- CLIC BDS, $L^{*}=3.5 \mathrm{~m}$
- Misalignment $10 \mu \mathrm{~m}$ RMS for:
- quadrupoles: $x$ and $y$
- multipoles: $x$ and $y$
- bpms: $x$ and $y$
- Added two BPMs:
- one at the IP
- one 3.5 meters downstream the IP (might this be the same used for the IP-Feedback?)
-bpm resolution:
- 10 nm
- Apertures are not taken into account / synchrotron radiation emission is not taken into account
$\Rightarrow$ All simulations have been carried out using placet-octave


## Parameters Optimization (No Synrad)

- Each point is the average of 100 seeds; $\sigma_{\mathrm{bpm}}=10 \mathrm{~nm}$

$\Rightarrow$ The minimum is for $\beta=11.45$ at $\sigma_{y}=3.49 \mathrm{~nm}$
$\Rightarrow$ The omegas are: $\omega_{1}=9.5, \omega_{2}=1.0, \omega_{3}=1370.0$


## Results for 1000 seeds (No Synrad)

- Histograms of final vertical beamsizes for a 1000 seeds, $\sigma_{\mathrm{bpm}}=10 \mathrm{~nm}$

- Final beamsize after each stage of optimization:
- Orbit Correction $=455.2 \mathrm{~nm}$
- Target Dispersion Steering $=102.0$ nm
- Full Alignment Procedure $=4.38 \mathrm{~nm}$


## Results for 1000 seeds (No Synrad)

- Histograms of final horizontal beamsizes for a 1000 seeds, $\sigma_{\mathrm{bpm}}=10 \mathrm{~nm}$

- Final beamsize after each stage of optimization:
- Orbit Correction $=2500$ nm
- Target Dispersion Steering $=392.0$ nm
- Full Alignment Procedure $=40.0 \mathrm{~nm}$


## Results for 1000 seeds (No Synrad)

- Average final vertical emittance along the line for a 1000 seeds, $\sigma_{\mathrm{bpm}}=10 \mathrm{~nm}$

- Final emittances after each stage of optimization:
- Orbit Correction $=28.7 \mu \mathrm{~m}$
- Target Dispersion Steering $=2.6 \mu \mathrm{~m}$
- Full Alignment Procedure $=130.6 \mathrm{~nm}$


## Convergence of the algorithm

Standard misalignments, no SR emission in the final doublet, 100 seeds


- Final beamsize was $\sigma_{x}=(1635.0 \pm 1.0) \mathrm{nm}, \sigma_{y}=(20.0 \pm 1.0) \mathrm{nm}$
$\Rightarrow$ SEE: At the very minimum: $\sigma_{x}=876 \mathbf{n m}, \sigma_{y}=3.5 \mathbf{n m}$
$\Rightarrow$ Remark: with multipole-shunting, beamsize improves drastically.


## Improved Multipole-Shunting

$\Rightarrow$ the old version aligned 1 multipole at time (magnet turned ON - alignment - magnet turned OFF)
$\Rightarrow$ the new version turns them ON 1 by 1 , and keeps them ON, once they are powered (it does it in two passes)

## Convergence with the New Multipole-Shunting

Standard misalignments, no SR emission in the final doublet, 100 seeds


- Final beamsize is $\sigma_{x}=(96.0 \pm 1.0) \mathbf{n m}, \sigma_{y}=(7.25 \pm 0.50) \mathbf{n m}$
$\Rightarrow$ After multipole-shunting \#1: $\sigma_{x}=49.5 \mathbf{n m}, \sigma_{y}=6.4 \mathbf{n m}$
$\Rightarrow$ Remark: It is not so bad!


## Conclusions

- A new technique has been introduced:
- it takes into account additional observables, such as coupling and $\beta$-beating, and
- it implements a new multipole-shunting technique
- The results are promising even if, in CLIC, synrad emission in the final doublet is a very serious problem, that hasn't fully been addressed yet
- It seems that a good alignment of the multipoles is essential (sophisticated algorithms are needed - I have one, that perhaps can be improved)
$\Rightarrow$ More studies are required!

