

The Higgs boson mass

—

its meaning for the Standard Model?

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Outline

- 1 Introduction
 - Standard Model and the reality of the Universe
 - Minimal extension – still “Standard Model”
- 2 Higgs from EW scale up to Planck scale
 - Renormalization evolution of Higgs self coupling
 - Current Higgs boson results
 - Critical Higgs mass
- 3 “Standard” model examples
 - Asymptotic safety
 - Higgs inflation
 - R^2 inflation
- 4 Summary

Standard Model – describes **nearly** everything

Three Generations of Matter (Feynman) spin 1/2

	I	II	III	
quarks	u 2.4 MeV spin 1/2	c 1.577 GeV spin 1/2	t 173.2 GeV spin 1/2	g 8 MeV spin 1
quarks	d 4.8 MeV spin 1/2	s 95 MeV spin 1/2	b 4.18 GeV spin 1/2	γ 0 MeV spin 1
quarks	ν_u 0 MeV spin 1/2	ν_d 0 MeV spin 1/2	ν_t 0 MeV spin 1/2	Z 91.1876 GeV spin 1
leptons	e 0.511 MeV spin 1/2	μ 105.7 MeV spin 1/2	τ 1.777 GeV spin 1/2	H 125 GeV spin 0
leptons	ν_e 0 MeV spin 1/2	ν_μ 0 MeV spin 1/2	ν_τ 0 MeV spin 1/2	W 80.379 GeV spin 1

+

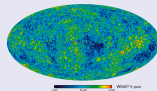
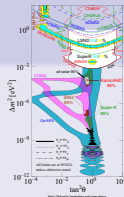
Einstein
gravity

Describes

- all laboratory experiments – electromagnetism, nuclear processes, etc.
- all processes in the evolution of the Universe after the Big Bang Nucleosynthesis ($T < 1 \text{ MeV}$, $t > 1 \text{ sec}$)

Experimental problems:

- Laboratory
 - ? Neutrino oscillations
- Cosmology
 - ? Baryon asymmetry of the Universe
 - ? Dark Matter
 - ? Inflation
 - ? Dark Energy



Can we describe everything with as small extension as possible?

- Minimal number of new particles
- No new scales before inflation/gravity

ν MSM+inflation – describes everything

Three Generations of Matter (fermions) spin 1/2

	I	II	III	
mass	2.4 MeV	1.27 GeV	171.2 GeV	171.2 GeV
charge	2/3	1/3	2/3	0
name	u up	c charm	t top	g gluon
Quarks	d down	s strange	b bottom	γ photon
	ν_u up	ν_c charm	ν_t top	Z boson
	ν_d down	ν_s strange	ν_b bottom	W boson
Leptons	e electron	μ muon	τ tau	H Higgs boson
	ν_e electron	ν_μ muon	ν_τ tau	spin 0
				W boson
				Z boson
				g gluon

+ Einstein gravity

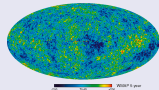
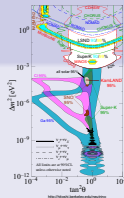
with ν MSM

- Right handed neutrinos
 - generation of active neutrino masses
 - keV scale DM
 - Baryogenesis via very low scale leptogenesis

+ cosmological constant

Experimental problems:

- Laboratory
 - ✓ Neutrino oscillations
- Cosmology
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SM everywhere?

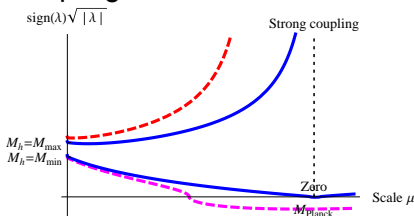
What happens if there is nothing else up to the Planck scales?
(or at least up to the scale of inflation)

Renormalization evolution of the Higgs self coupling λ

$$(4\pi)^2 \beta_\lambda = 24\lambda^2 - 6y_t^4 + \frac{3}{8}(2g_2^4 + (g_2^2 + g_1^2)^2) + (-9g_2^2 - 3g_1^2 + 12y_t^2)\lambda$$

- High M_h – strong coupling
- Low M_h – our (EW) vacuum is metastable.
- Boundary situation –
 $M_h = M_{\min}$

Coupling constant evolution:



$$\lambda(\mu_0) = 0, \quad \beta_\lambda(\mu_0) \equiv \mu \frac{d\lambda}{d\mu} = 0$$

Which case is realized?

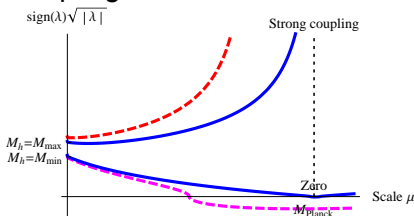
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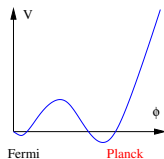
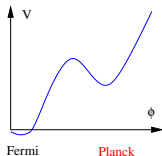
$$\lambda(\mu_0) = 0, \quad \beta_\lambda(\mu_0) \equiv \mu \frac{d\lambda}{d\mu} = 0$$

Coupling constant evolution:



Higgs effective potential

$$V(\varphi) \simeq \lambda(\varphi) \frac{\varphi^4}{4}$$



Which case is realized?

The boundary case defines both M_h and $\mu_0 \sim M_P$

Let us fix all the SM constants, except for the Higgs mass:

$$\alpha, M_W, M_Z, \alpha_S, M_t$$

Then *two* requirements:

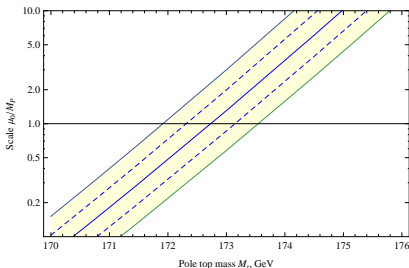
$$\lambda(\mu_0) = 0, \quad \beta_\lambda(\mu_0) \equiv \mu \frac{d\lambda}{d\mu} = 0$$

define *two* parameters:

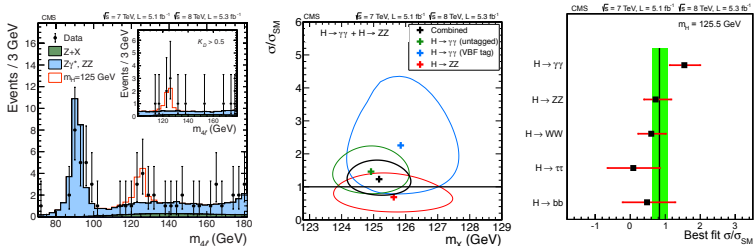
$$m_H, \quad \mu_0$$

Planck scale!

SM with $m_t \sim 173$ GeV leads to
 $\mu_0 \sim M_P$



CMS "new boson" results



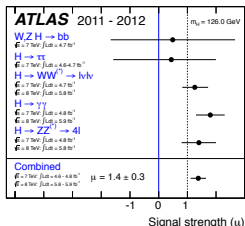
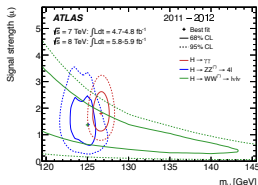
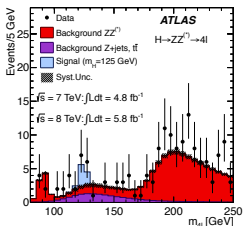
"New boson" mass

$$M_h = 125.3 \pm 0.4(\text{stat}) \pm 0.5(\text{syst}) \text{ GeV}$$

5.8 σ for SM Higgs boson of this mass

[CMS'12]

ATLAS "new particle" results



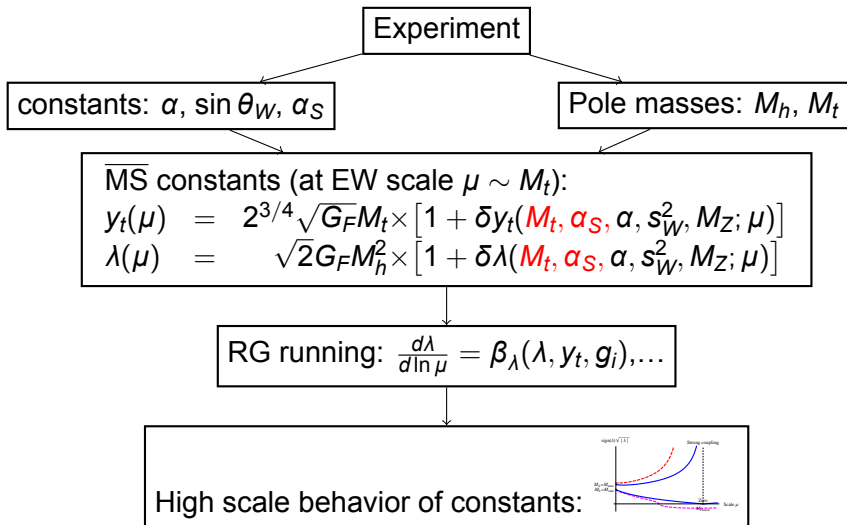
"New particle" mass

$$M_h = 126.0 \pm 0.4(\text{stat}) \pm 0.4(\text{syst}) \text{ GeV}$$

5.9 σ for SM Higgs boson of this mass

[ATLAS'12]

Calculation steps



Calculation steps: state of the art

- Convert to \overline{MS} constants $\lambda(\mu)$, $y_t(\mu)$ at a scale μ between M_Z and M_t

δy_t Up to $O(\alpha_s^2)$, $O(\alpha)$

$O(\alpha_s^3)$ [Chetyrkin, Steinhauser'99, Melnikov, Ritbergen'00]

$O(\alpha\alpha_s)$ [FB, Kalmykov, Kniehl, Shaposhnikov'12]

$\delta\lambda$ Up to $O(\alpha)$

$O(\alpha\alpha_s)$ [FB, Kalmykov, Kniehl, Shaposhnikov'12]

$O(y_t^4)$ (Yukawa part of $O(\alpha^2)$)

[Degrassi, Di Vita, Elias-Miro, Espinosa, Giudice, Isidori, Strumia'12]

- Evolve with RG up to Planck scales

β_{g_i} two loops

three loops [Mihaila, Salomon, Steinhauser'12]

$\beta_{y_t}, \beta_\lambda$ two loops

three loops (no EW gauge contributions)

[Chetyrkin, Zoller'12]

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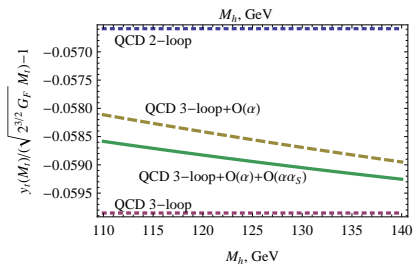
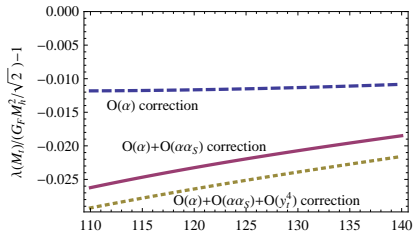
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[Degrassi, Di Vita, Elias-Miro, Espinosa, Giudice, Isidori, Strumia'12]
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 - $\beta_{y_t}, \beta_\lambda$ two loops
 - three loops (no EW gauge contributions)

[Chetyrkin, Zoller'12]

Size of contributions to M_{\min}

Contribution	ΔM_{\min} , GeV
Three loop beta functions	-0.23
$\delta y_t \propto O(\alpha_s^3)$	-1.15
$\delta y_t \propto O(\alpha\alpha_s)$	-0.13
$\delta\lambda \propto O(\alpha\alpha_s)$	0.62
$\delta\lambda \propto O(y_t^4)$	0.2



Error budget

Theoretical

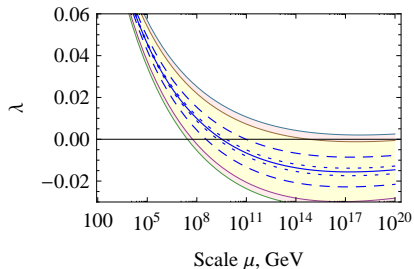
Source of uncertainty	Nature of estimate	$\Delta_{\text{theor}} M_{\text{min}}, \text{ GeV}$
3-loop matching λ	Sensitivity to μ	1.0
3-loop matching y_t	Sensitivity to μ	0.2
4-loop α_s to y_t	educated guess	0.4
confinement, y_t	educated guess	0.5
4-loop RG $M_W \rightarrow M_P$	educated guess	< 0.2
total uncertainty	sum of squares	1.2
total uncertainty	linear sum	2.3

Experimental

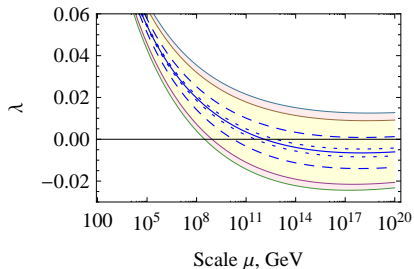
Source of uncertainty	$\Delta_{\text{exp}} M_{\text{min}}, \text{ GeV}$
M_t	~ 2
α_s	~ 0.6
total uncertainty	sum of squares 2.1

Scale for λ turning negative is high

Higgs mass $M_h=124$ GeV



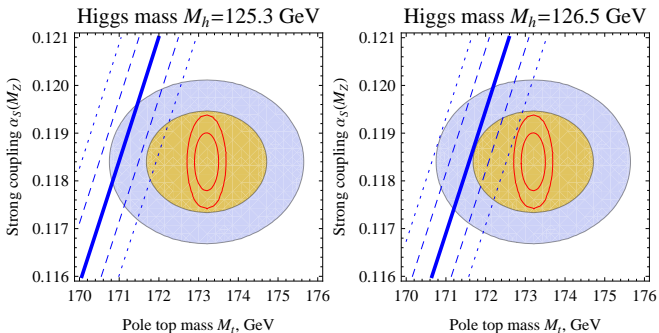
Higgs mass $M_h=127$ GeV



Critical Higgs mass is compatible with M_t and α_s

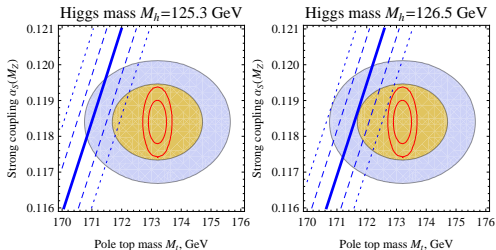
Tevatron value: $M_t = 173.2 \pm 0.6(\text{stat}) \pm 0.8(\text{syst}) \text{ GeV}$

$\alpha_s(M_Z) = 0.1184 \pm 0.0007$



$$M_{\min} = \left[129.5 + \frac{M_t - 173.2 \text{ GeV}}{0.9 \text{ GeV}} \times 1.8 - \frac{\alpha_s - 0.1184}{0.0007} \times 0.6 \pm 2 \right] \text{ GeV}$$

Is this coincidence really there?

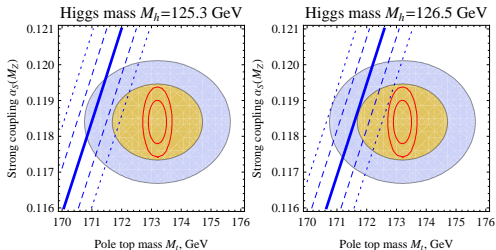


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We do not really know now! Yet to be done:

- Build a lepton collider at $\gtrsim 350$ GeV! (Higgs *and* top masses)
- Calculate higher order relations between $\overline{\text{MS}}$ parameters and masses

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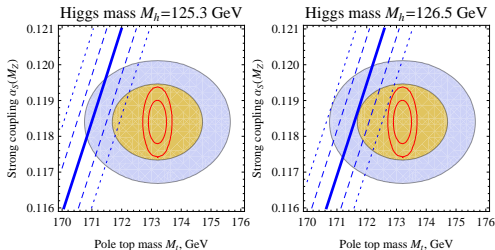


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Asymptotic safe model predicts M_h

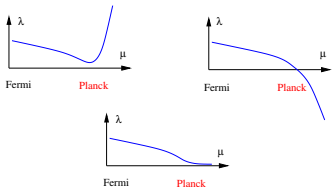
Above Planck scale beta functions for coupling constant $h \in \{g_1, g_2, g_3, \lambda, y_t\}$ get additional terms

$$\beta_h^{\text{grav}} = \frac{a_h}{8\pi M_P^2 + 2\xi_0\mu^2} h^2$$

leading to a *fixed point* at high energies

$a_\lambda > 0$ leads to the **prediction** $M_h = M_{\text{min}}$

(up to a difference of 0.1–0.2 GeV)



For other M_h no finite fixed point for λ

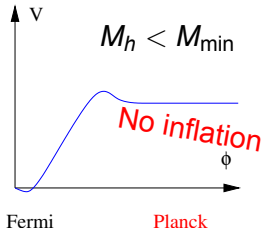
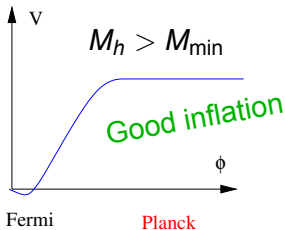
[Shaposhnikov, Wetterich'09]

There are other models predicting the same Higgs mass

- **Forggart, Nielsen'96** – Multiple point principle.
All the vacua should be degenerate – thus, the same prediction $M_h = M_{\min}$
- **Masina, Notari'11** – inflation from the decay of the metastable Planck scale vacuum – $M_h \simeq M_{\min}$
- ...

Higgs inflation works only for $M_h > M_{min}$

$$S_J = \int d^4x \sqrt{-g} \left\{ -\frac{M_P^2}{2} R - \xi \frac{h^2}{2} R + g_{\mu\nu} \frac{\partial^\mu h \partial^\nu h}{2} - \frac{\lambda}{4} (h^2 - v^2)^2 \right\}$$



Bound on the Higgs mass

$$M_h > M_{min}$$

Up to a difference of 0.1–0.2 GeV

[FB, Shaposhnikov'09]

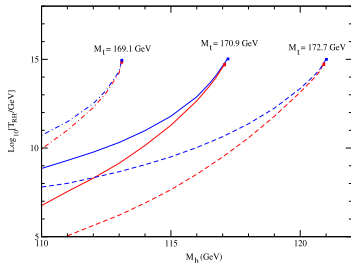
Modifying the gravity action gives inflation for any M_h

$$S_J = \int d^4x \sqrt{-g} \left\{ -\frac{M_P^2}{2} R + \frac{\zeta^2}{4} R^2 \right\} + S_{SM}$$

[Starobinsky'80]

The electroweak vacuum may decay at high temperature.
But reheating is due to M_P suppressed operators \Rightarrow
temperature is low

$$T_r \sim 10^7 - 10^9 \text{ GeV}$$



[Espinosa, Giudice, Riotto'07]

Higgs mass bounds in R^2 is weak

$$m_H > 116 \text{ GeV}$$

Summary

Coincidence in Standard Model

- $\lambda(M_P) = \left. \frac{d\lambda}{d\mu} \right|_{\mu=M_P} = 0$

Higgs self coupling is vanishing with its derivative at Planck scale

- for $M_h = M_{\min} =$

$$M_{\min} = \left[129.5 + \frac{M_t - 173.2 \text{ GeV}}{0.9 \text{ GeV}} \times 1.8 - \frac{\alpha_s - 0.1184}{0.0007} \times 0.6 \pm 2 \right] \text{ GeV}$$

- We may be learning about Planck scale physics!

To disprove/confirm this the following is needed

- e^+e^- collider up to $\gtrsim 350$ GeV
 - Higgs factory — M_H
 - top factory — M_t

-  FB, M. Kalmykov, B. Kniehl, M. Shaposhnikov, arXiv:1205.2893 [hep-ph]
-  G. Degrassi, S. Di Vita, J. Elias-Miro, J.R. Espinosa, G.F. Giudice, G. Isidori, A. Strumia arXiv:1205.6497 [hep-ph]
-  A.Starobinsky, Phys.Lett. B91 (1980) 99
-  J. R. Espinosa, G. F. Giudice and A. Riotto, JCAP **0805** (2008) 002
-  K. G. Chetyrkin and M. Steinhauser, *Phys. Rev. Lett.* **83** (1999) 4001
-  K. Melnikov and T. v. Ritbergen, *Phys. Lett.* **B482** (2000) 99
-  L. N. Mihaila, J. Salomon, and M. Steinhauser, *Phys. Rev. Lett.* **108** (2012) 151602
-  K. G. Chetyrkin and M. F. Zoller, arXiv:1205.2892.
-  FB, M. Shaposhnikov, Phys. Lett. B **659**, 703 (2008)
-  FB, M. Shaposhnikov, JHEP **0907** (2009) 089
-  M. Shaposhnikov and C. Wetterich, Phys. Lett. B **683** (2010) 196



CMS Collaboration, [arXiv:1207.7235 [hep-ex]]



ATLAS Collaboration, [arXiv:1207.7214 [hep-ex]]

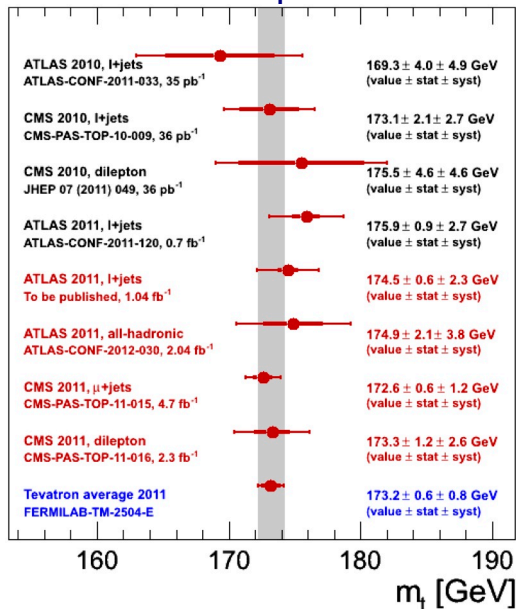
Exact effective potential definition

$$V(\varphi) = \lambda(\mu)\varphi^4 \left[1 + \sum \left(\frac{M_i^4(\varphi)}{64\pi} \log(M_i^2/\mu^2) \right) \right],$$

choosing μ to minimize logarithms

$$V(\varphi) \propto \lambda(\varphi)\varphi^4 \left[1 + \mathcal{O}\left(\frac{\alpha}{4\pi} \log(M_i/\varphi)\right) \right],$$

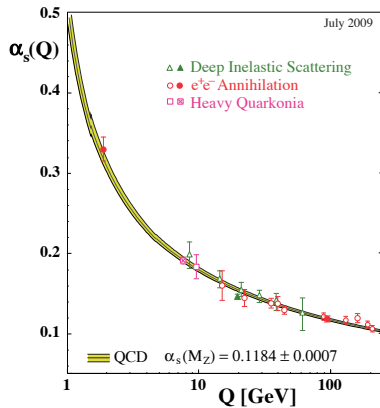
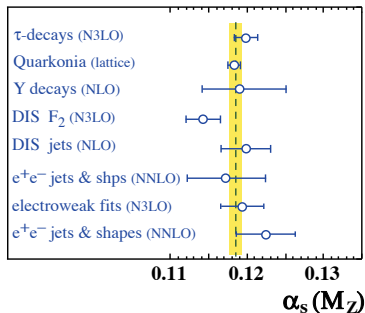
Top mass determination



In addition:

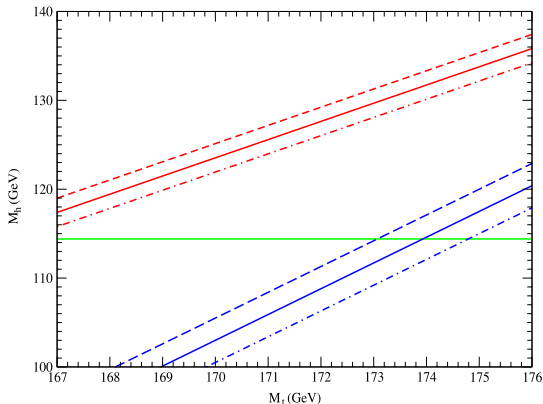
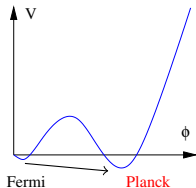
- Problems with relation of M_{Pythia} and M_{pole} – up to ~ 1 GeV

α_s determination



Even metastable EW vacuum overlives the Universe

Will the vacuum decay?



[Espinosa, Giudice, Riotto'07]

EW vacuum lifetime $> \tau_{\text{Universe}}$

$M_h > 111$ GeV

RG scale dependence

