Light Higgsino Precision Measurements at the ILC

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Motivated by naturalness which requires μ at the electroweak scale

Scenario contains

- \succ 3 light Gauginos, Higgsinos like: $\tilde{\chi}_1^\pm$ & $\tilde{\chi}_1^0$ & $\tilde{\chi}_2^0$
- > Almost mass degenerate: $\Delta M(\tilde{\chi}_1^{\pm}, \tilde{\chi}_1^0)$ & $\Delta M(\tilde{\chi}_2^0, \tilde{\chi}_1^0) \sim$ a few GeV
- All other supersymmetric particles are heavy up to a few TeV





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- > All other supersymmetric particles are heavy up to a few TeV

Mass Spectrum			
Particle	Mass (GeV)		
h	124		
$\tilde{\chi}_1^0$	164.17		
$\tilde{\chi}_1^{\pm}$	165.77		
$\tilde{\chi}_2^0$	166.87		
H's	$\sim 10^3$		
$ ilde{\chi}$'s	$\sim 2-3 imes 10^3$		

 $\Delta M(ilde{\chi}_1^\pm, ilde{\chi}_1^0) = 1.59 \; ext{GeV}$

Mas	Mass Spectrum				
Particle	Mass (GeV)				
h	127				
$\tilde{\chi}_1^0$	166.59				
$\tilde{\chi}_1^{\pm}$	167.36				
$\tilde{\chi}_2^0$	167.63				
H's	$\sim 10^3$				
$ ilde{\chi}$'s	$\sim 2-3 imes 10^3$				

 $\Delta M(ilde{\chi}_1^{\pm}, ilde{\chi}_1^0) = 0.77$ GeV

But also high scale models, for instance: "Hybrid Gauge-Gravity Mediated Supersymmetry Breaking Models" Ref: F. Brummer et al. hep-ph:1201.4338

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 Other combinations are kinematically allowed, but have negligible cross sections.





Decay Modes:







 Other combinations are kinematically allowed, but have negligible cross sections.

Decay Modes:





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Separation of the Processes

Chargino Process





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Ref: C.-H. Chen et al. hep-ph:9512230



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$m_h = 124 GeV$	$m_h = 127 GeV$
$\Delta M=1.59$ GeV	$\Delta M=0.77 \text{ GeV}$
$e/\mu + \pi^{\pm}(\pi^0)$	$e/\mu+\pi^{\pm}$
BR = 30.5%	BR = 35%

Neutralino Process







In the Final State

- > A few soft visible particles
- > A lot of missing energy (2 $\tilde{\chi}_1^0$)











It is extremely challenging for LHC to observe or resolve such a low energetic and degenerate particles





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It is also non-trivial for ILC





It is extremely challenging for LHC to observe or resolve such a low energetic and degenerate particles

It is also non-trivial for ILC

- ► It is very similar to some SM background final states, especially $\gamma\gamma \rightarrow f\bar{f}$.
- We have required hard ISR photon, to avoid this similarity.

 $\mathbf{e}^+ \mathbf{e}^-
ightarrow \widetilde{\chi}_1^+ \widetilde{\chi}_1^- \gamma$ $\mathbf{e}^+ \mathbf{e}^-
ightarrow \widetilde{\chi}_2^0 \widetilde{\chi}_1^0 \gamma$



	Introduction				
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Analysis Overview					

Software:

- Generate events with Whizard (ILC-Whizard by generator group) Ref: Wolfgang Kilian et al., hep-ph: 0708.4233v2
 - Branching ratios are calculated by Herwig++ Ref: M. Bahr et.al., Eur.Phys.J., C58:639–707, 2008
- DBD generated samples for SM backgrounds
- Apply fast detector simulation SGV (ILD DBD version of SGV)

Ref: M. Berggren, physics.ins-det: 1203.0217

- Track efficiency, which is obtained from full simulation including pair backgrounds, is applied for low P_t
 - Signals
 - Dominating SM background



Introduction						
Analysis Overview						

Data Set:

 $\blacktriangleright \sqrt{s} = 500 \text{ GeV}$

>
$$\int \mathcal{L} dt = 500 \text{ fb}^{-1}$$
 for each polarization

Polarization:

$$\blacktriangleright$$
 $P_{e^+}=+30\%$, $P_{e^-}=-80\%$

$$\blacktriangleright~P_{e^+}=-30\%$$
 , $P_{e^-}=+80\%$

Cross Sections are calculated by whizard

	$m_h = 124 GeV$		$m_h = 127 GeV$	
Processes	$ ilde{\chi}_1^+ ilde{\chi}_1^- \gamma$	$ ilde{\chi}_2^{0} ilde{\chi}_1^{0}\gamma$	$ ilde{\chi}_1^+ ilde{\chi}_1^- \gamma$	$ ilde{\chi}_2^{m 0} ilde{\chi}_1^{m 0}\gamma$
$\sigma(e_L^+e_R^- \to \tilde{\chi}\tilde{\chi}\gamma)$	26.83 ± 0.05	61.66 ± 0.10	26.28 ± 0.05	60.92 ± 0.10
$\sigma(e_R^+e_L^- \rightarrow \tilde{\chi}\tilde{\chi}\gamma)$	132.99 ± 0.23	80.12 ± 0.13	130.05 ± 0.22	79.16 ± 0.13

Aim of the Study: To measure

- > mass of the $\tilde{\chi}_1^+$ & $\tilde{\chi}_2^0$.
- > mass difference between $\tilde{\chi}_1^+$ & $\tilde{\chi}_1^0$.
- precision on the polarized cross section



$\tilde{\chi}_1^+$ & $\tilde{\chi}_2^0$ Mass Measurement ($M_{\tilde{\chi}_1^{\pm}}$ & $M_{\tilde{\chi}_2^0}$):

Recoil mass of hard ISR photon is used to measure mass of $\tilde{\chi}_1^+$ & $\tilde{\chi}_2^0$ Recoil Mass:

$$M_{recoil}^2 = s - 2\sqrt{s}E^{\gamma}$$

> $M_{recoil} = 2 \times M_{\tilde{\chi}}$ at the rest frame of $\tilde{\chi} = \tilde{\chi}_1^{\pm}$ or $\tilde{\chi}_2^0$.

> Fitting gives $M_{\tilde{\chi}}$.



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 at the rest frame of $\tilde{\chi} = \tilde{\chi}_1^{\pm}$ or $\tilde{\chi}_2^0$.

> Fitting gives $M_{\tilde{\chi}}$.

However; this method is an approximation, since

formula is obtained only after some assumptions

> \sqrt{s} is assumed 500 GeV

Hence,

> calibration is applied to the masses.



 $\tilde{\chi}_1^+$ & $\tilde{\chi}_2^0$ Mass Measurement ($M_{\tilde{\chi}_1^{\pm}}$ & $M_{\tilde{\chi}_2^0}$):

Recoil mass of hard ISR photon is used to measure mass of $ilde{\chi}_1^+$ & $ilde{\chi}_2^0$

Recoil Mass: $M_{recoil}^2 = s - 2\sqrt{s}E^{\gamma}$

Mass Difference Measurement ($\Delta M(\tilde{\chi}_1^{\pm}, \tilde{\chi}_1^0)$):

> Boost decay products to the rest frame of $\tilde{\chi}_1^{\pm}$

Boosted Energy:

$$E^*_{\pi} = rac{(\sqrt{s}-E^{\gamma})E^{\pi}+{f P}^{\pi}\cdot{f P}^{\gamma}}{2M_{ ilde{\chi}^\pm_1}}$$

At the rest frame of $\tilde{\chi}_1^{\pm}$;

>
$$\tilde{\chi}_1^0$$
 is produced at rest,

 $\succ E^*_{decays} = \Delta M(\tilde{\chi}_1^{\pm}, \tilde{\chi}_1^0)$







$\tilde{\chi}_1^+$ & $\tilde{\chi}_2^0$ Mass Measurement ($M_{\tilde{\chi}_1^{\pm}}$ & $M_{\tilde{\chi}_2^0}$):

Recoil mass of hard ISR photon is used to measure mass of $\tilde{\chi}_1^+ \& \tilde{\chi}_2^0$ Recoil Mass: $M_{recoil}^2 = s - 2\sqrt{s}E^{\gamma}$

Mass Difference Measurement ($\Delta M(\tilde{\chi}_1^{\pm}, \tilde{\chi}_1^0)$):

Boost decay products to the rest frame of $\tilde{\chi}_{1}^{\pm}$ ($E_{decays}^{*} = \Delta M(\tilde{\chi}_{1}^{\pm}, \tilde{\chi}_{1}^{0})$) Boosted Energy: $E_{\pi}^{*} = \frac{(\sqrt{s} - E^{\gamma})E^{\pi} + \mathbf{P}^{\pi} \cdot \mathbf{P}^{\gamma}}{\frac{2M_{\tilde{\chi}_{1}^{\pm}}}{\chi_{1}^{\pm}}}$

Polarized Cross Section Measurement ($\delta \sigma_{polarized} / \sigma_{polarized}$)

Statistical precision on polarized cross section

$$\begin{split} & \frac{<\delta\sigma_{meas}>}{<\sigma_{meas}>} = \frac{1}{\sqrt{\epsilon \cdot \pi \cdot \int \mathcal{L} dt \cdot \sigma_{signal}}} \\ & \sigma_{meas} = \sigma_{polarized} \times BR(\tilde{\chi}_1^+ \tilde{\chi}_1^- \to 2\tilde{\chi}_1^0, \pi, \mathbf{e}(\mu)) \end{split}$$

Estimated Precison is based on efficiency and purity



		Event Selection				
Event Selection						



Before Any Selection



			Event Selection		
		Event	Selection		
Preselect E_bea Nrec Req Esof Esof Emis cos	tion: $a_{mcal} < 40 \text{ GeV}$ $a_{sonstructed particles} < 15$ $a_{sonstructed particles} < 15$ a_{son	5	$m_{h} = 127 \text{ GeV}$ 10^{4} 10^{3} 10^{2} $0 \qquad 1 \qquad 2$	$\vec{x}_{1}^{\dagger} \vec{x}_{1}^{\dagger} \vec{\gamma}$ $\vec{x}_{1}^{\dagger} \vec{x}_{2}^{0} \vec{\gamma}$ $\vec{x}_{1}^{0} \vec{x}_{2}^{0} \vec{\gamma}$	1ta
				PT	/GeV

After PreSelection



			Event Selection		
		Event	Selection		
Selection E_{bec} N_{rec} Rec E_{sof} E_{sof} E_{sof} E_{sof} E_{sof} E_{sof} E_{sof} E_{sof} E_{sof}	n: amcal < 40 GeV constructed particles $<$ juire 1 photon with $E_{\gamma}^{max} > 10 \text{ GeV}$ $ \cos \theta_{\gamma}^{ISR} < 0.992$ is $\theta_{soft} < 0.9397$ t < 5 GeV as > 300 GeV is $\theta_{miss} < 0.992$ ext semi-leptonic 1π and (1 e or 1	15 th 3 decay modes μ)	$\begin{array}{c} \text{Steps} \\ \text{Homoson} \\ 10^3 \\ 10^2 \\ 10 \\ 10 \\ 0 \\ 1 \\ 2 \\ 1 \\ 0 \\ 1 \\ 2 \\ 1 \\ 1$	$\begin{array}{c c} \mathbf{x} & \mathbf{x}_{1}^{T} \mathbf{x}_{1}^{T} \mathbf{x}_{1}^{T} \mathbf{x}_{2}^{T} \mathbf{x}_{1}^{T} \mathbf{x}_{2}^{T} \mathbf{x}_{2}^{T} \mathbf{x}_{3}^{T} \mathbf{x}_{2}^{T} \mathbf{x}_{3}^{T} \mathbf{x}_{2}^{T} \mathbf{x}_{3}^{T} $	lata
	((**)			

 $\succ E_{\pi}^* < 3 \text{ GeV}$

After Chargino Selection



			Event Selection ○●		
		Event Se	election		
Selection F_{bec} N_{rei} Rec F_{sout}	$\begin{array}{l} \sum_{amcal} < 40 \ {\rm GeV} \\ \sum_{constructed particles} < \\ {\rm quire 1 photon with the second se$	15 th st 3	10^{3} m _h = 127 Ge	$\begin{array}{c} \mathbf{v} \\ $	ata
> Sel	ect semi-leptonic	decay modes	0 1 2	P ₁	₋/GeV

- > Select semi-leptonic decay modes
 - 1 π and (1 e or 1 μ)
- $E_{\pi}^{*} < 3 \text{ GeV}$
- Select photon decay mode
 - $\blacktriangleright 1 \gamma$



After Neutralino Selection



Event Selection

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Mass Measurement Procedure

Fitting Procedure

- Fitting is done in the following order:
 - SM background is fitted with a convenient function assuming that we can precisely predict SM background.
 - SM background is fixed.
 - SM background + Signal are fitted using linear function for signal.





Event Selection

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Mass Measurement Procedure

Calibration Procedure

- Choose different true masses (X-axis)
- Apply measurement and get fitted masses (Y-axis)
- > Obtain calibration curve





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$\tilde{\chi}_1^+$ Mass Measurement & Calibration







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$\tilde{\chi}_1^+$ Mass Measurement & Calibration







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$\tilde{\chi}_2^0$ Mass Measurement & Calibration







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$\tilde{\chi}_2^0$ Mass Measurement & Calibration



				Results
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Mass Difference Measurement







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Mass Difference Measurement





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Mass Difference Measurement



Polarized Cross Section Measurement

Efficiency, Purity and Precison on Polarized Cross Sections:

Polarizations	$P(e^+, e^-) = (+30\%, -80\%)$		${\sf P}({\sf e}^+,{\sf e}^-)=(-30\%,+80\%)$		
Processes	$\tilde{\chi}_1^+ \tilde{\chi}_1^- \gamma$	$ ilde{\chi}_2^{f 0} ilde{\chi}_1^{f 0} \gamma$	$ ilde{\chi}_1^+ ilde{\chi}_1^- \gamma$	$ ilde{\chi}_2^{0} ilde{\chi}_1^{0}\gamma$	
m _h =124 GeV					
Efficiency($\epsilon \times BR$)	24.1 %	28.8 %	24.1 %	28.8 %	
$Purity(\pi)$	62.8 %	50.9 %	32.4 %	49.6 %	
$\frac{\langle \delta \sigma_{meas} \rangle}{\langle \sigma_{meas} \rangle}$	2.3 %	3.4 %	6.5 %	3.8 %	
m _h =127 GeV					
Efficiency($\epsilon \times BR$)	41.4 %	29.7 %	41.4 %	29.7 %	
$Purity(\pi)$	90.7 %	74.7 %	67.9 %	73.9 %	
$\frac{\langle \delta \sigma_{meas} \rangle}{\langle \sigma_{meas} \rangle}$	1.4 %	1.6 %	3.2 %	1.8 %	

Polarized Cross Sections:





			Conclusion •
	Conclu	ision	

- Light Higgsinos are well motivated by naturalness
- It is a challenging scenario for LHC
- > Separation of Higgsinos at the reconstructed level is possible at the ILC
- Assumed
 - ▶ $\sqrt{s} = 500 \text{ GeV}$
 - ▶ $\int \mathcal{L}dt = 500 \ fb^{-1}$ with $P(e^+, e^-) = (+30\%, -80\%)$ and $P(e^+, e^-) = (-30\%, +80\%)$ each

> Statistical uncertainities for $P(e^+, e^-) = (+30\%, -80\%)$

 $m_h = 124 \text{ GeV}$

► $\delta(\sigma \times BR) \approx 3 \% \quad \delta M_{\tilde{\chi}_1^{\pm}}(M_{\tilde{\chi}_2^0}) \approx 2.1(3.7) \text{ GeV} \quad \delta \Delta M(\tilde{\chi}_1^{\pm}, \tilde{\chi}_1^0) = 70 \text{ MeV}$ m_b=127 GeV

• $\delta(\sigma \times BR) \approx 1.5 \,\% \, \delta M_{\tilde{\chi}_1^{\pm}}(M_{\tilde{\chi}_2^0}) \approx 1.5(1.6) \,\text{GeV} \, \delta \Delta M(\tilde{\chi}_1^{\pm}, \tilde{\chi}_1^0) = 20 \,\,\text{MeV}$



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Can this scenario be used to calculate μ parameter and predict $M_1 \& M_2$? Krzysztof's talk





Backup



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$\gamma\gamma \rightarrow f\bar{f} SM background$

 $\gamma\gamma
ightarrow far{f}$ SM background



 Outgoing particles go in the direction of the beampipe. So,

In the final state:

2 fermions with low energy, which is very similar to the signal > We have required hard ISR photon,

$$e^+e^-
ightarrow ilde{\chi}_1^+ ilde{\chi}_1^- \gamma \ e^+e^-
ightarrow ilde{\chi}_2^0 ilde{\chi}_1^0 \gamma$$

to avoid this similarity of the final states.

> For $\gamma \gamma \rightarrow f \bar{f}$ SM background



additional γ makes the beam electron visible in the detector.



realiser of events for two signals and an own background.	Number	of	events	for	two	signals	and	all	SM	background:
---	--------	----	--------	-----	-----	---------	-----	-----	----	-------------

Polarizations	$P(e^+, e^-) = (+30\%, -80\%)$			$P(e^+, e^-) = (-30\%, +80\%)$		
Processes	$\tilde{\chi}_1^+ \tilde{\chi}_1^- \gamma$	$\tilde{\chi}_2^0 \tilde{\chi}_1^0 \gamma$	All SM Bkg	$\tilde{\chi}_1^+ \tilde{\chi}_1^- \gamma$	$\tilde{\chi}_2^0 \tilde{\chi}_1^0 \gamma$	All SM Bkg
m _h =124 GeV						
nocut	38672	24250	1.37×10^{8}	9817	19071	$1.05 imes 10^8$
semi-lep sel	2872	82	906	712	62	893
photon sel	53	1733	1616	11	1414	1423
m _h =127 GeV						
nocut	38130	23940	1.37×10^{8}	9792	18773	1.05×10^{8}
semi-lep sel	5489	38	525	1408	32	634
photon sel	155	5224	1616	44	4128	1423

Measurement Results for Efficiency, Purity and Polarized Cross Sections:

Polarizations	$P_{e^+} = +30$	$0\%, P_{e^-} = -80\%$	$P_{e^+} = -30\%, P_{e^-} = +80\%$		
Processes	$ ilde{\chi}_1^+ ilde{\chi}_1^- \gamma$	$ ilde{\chi}_2^{0} ilde{\chi}_1^{0} \gamma$	$ ilde{\chi}_1^+ ilde{\chi}_1^- \gamma$	$ ilde{\chi}_2^{0} ilde{\chi}_1^{0}\gamma$	
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