

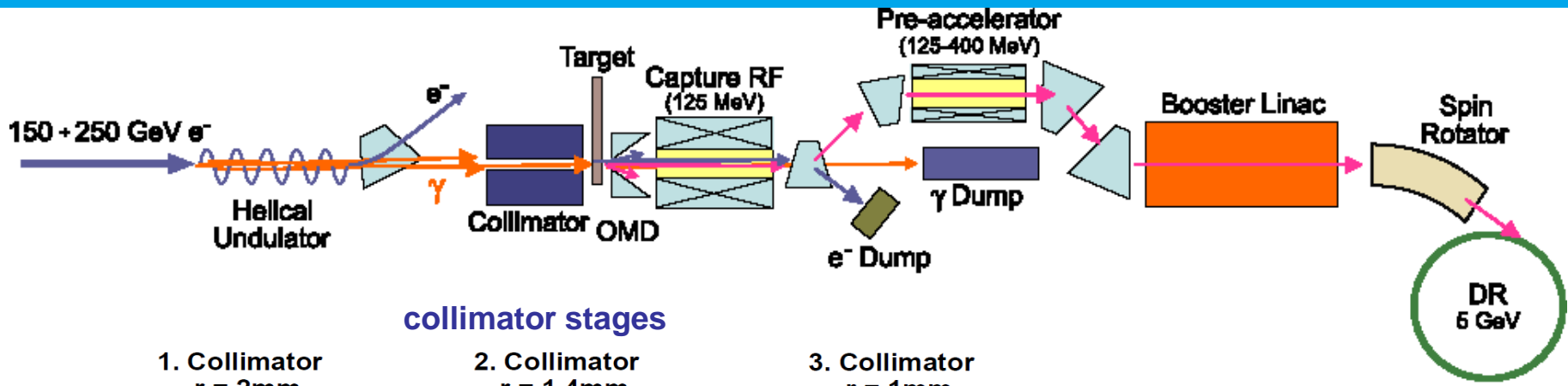
O. S. Adeyemi<sup>1</sup>, V. Kovalenko<sup>1</sup>, G. Moortgat-Pick<sup>1;2</sup>  
S. Riemann<sup>2</sup>, F. Staufenbiel<sup>2</sup>, A. Ushakov<sup>1</sup>

<sup>1</sup>University of Hamburg

<sup>2</sup>DESY

- ILC positron source unit
- Energy deposition in the collimators
- TDR parameter table with different collimator settings
- Dynamic evolution in the collimator
- Collimator cooling (average temperature)
- Conclusion

# ILC positron source unit

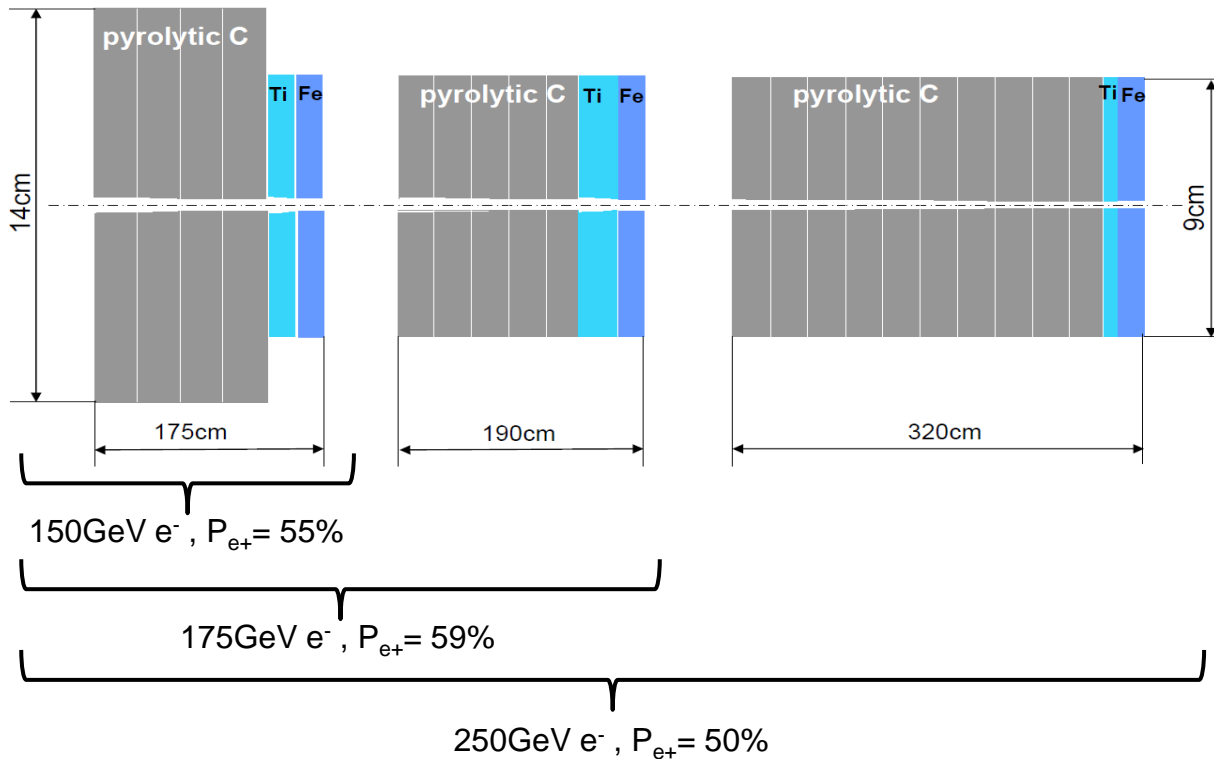


## collimator stages

1. Collimator  
 $r = 2\text{mm}$

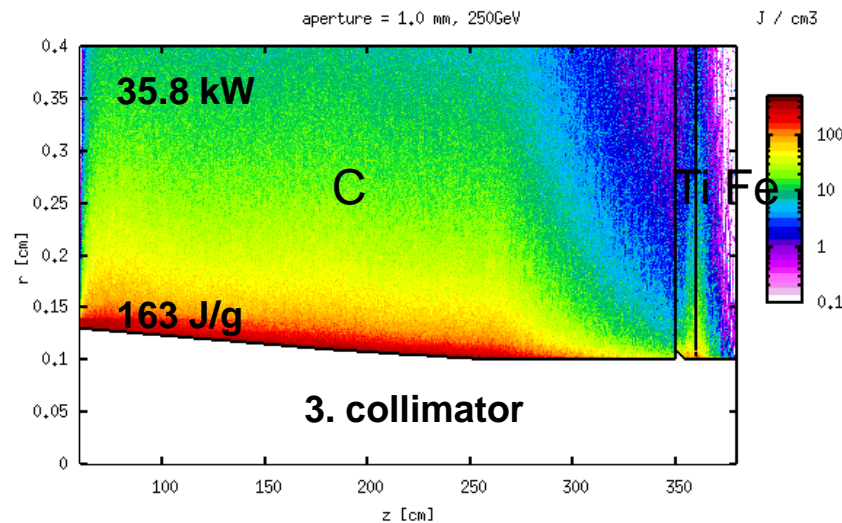
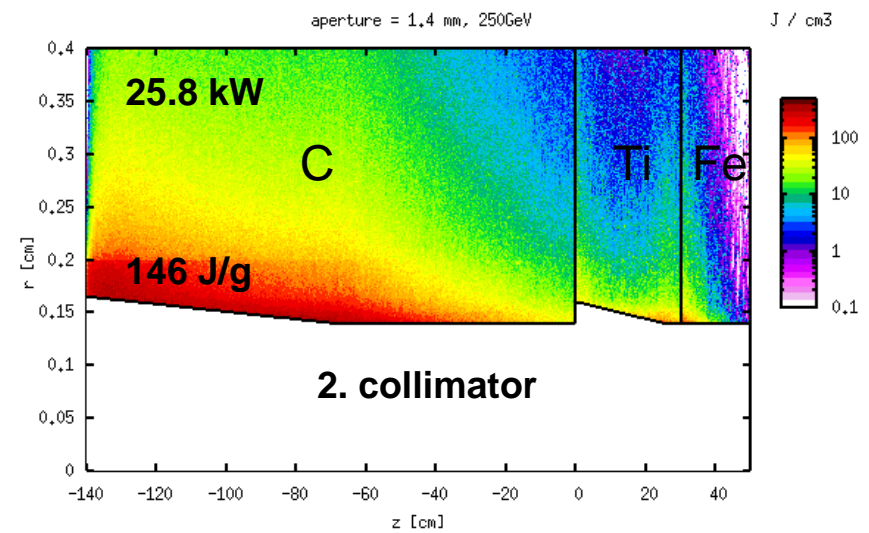
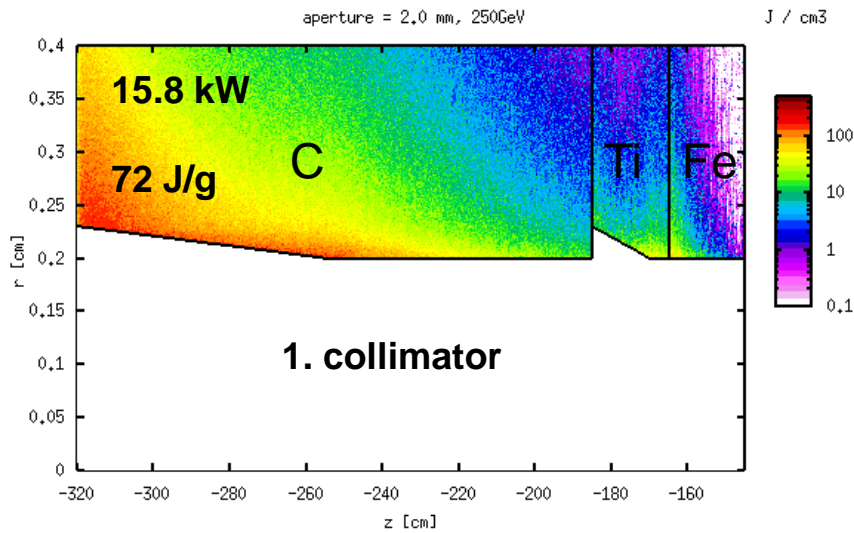
2. Collimator  
 $r = 1.4\text{mm}$

3. Collimator  
 $r = 1\text{mm}$



# Energy deposition in the collimators (high lumi)

drive beam 250GeV  $e^-$ ,  $P_{e^+} = 50\%$



Energy deposition  
scored with FLUKA  
[ $J/\text{cm}^3$ ]

# TDR parameter table with different collimator settings

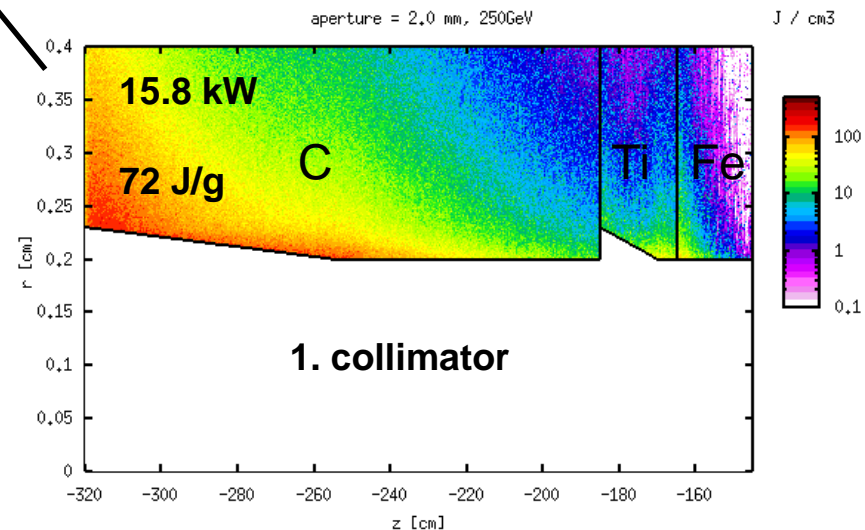
Photon Collimator Parameters			e- drive beam energy (GeV)			L upgrade
Parameter			150	175	250	250
Effective undulator field	$B_{und}$	T	0,86			0,86
			K=0.92			K=0.92
Active undulator length	$L_{und}$	m	231,0	196,0	70,0	70,0
Photons per bunch train	$n_{ph} / train$	$\times 10^{15}$	11,8	10,0	3,6	7,2
Average photon power	$P_{photon}$	kW	98,5	113,8	83,1	166,2
Abs.ph. power in collim.	$P_{collimator}$	kW	48,1	68,7	43,7	87,3
PEDD Ti target	$E_{max}$	J/g	61	61	31	63
Abs.ph. power in Ti target	$P_{target}$	kW	4,3	3,2	1,9	3,7
Collimator radius	$r$	mm	2,0	1,4	1,0	1,0
Positron Polarization	$P_+$	%	55,3	58,5	50,3	50,3
collimator r=2.0 / Pyr. C	$E_{max}$	J/g	177	144	36	72
collimator r=2.0 / Pyr. C	$P$	kW	44,8	36,3	7,9	15,8
collimator r=2.0 / Ti	$E_{max}$	J/g	16	18	6	11
collimator r=2.0 / Ti	$P$	kW	0,8	0,8	0,2	0,4
collimator r=2.0 / Fe	$E_{max}$	J/g	13	13	5	10
collimator r=2.0 / Fe	$P$	kW	0,2	0,3	0,1	0,2
cooling / Cu	$P$	kW	2,3	1,9	0,4	0,7
collimator r=1.4 / Pyr. C	$E_{max}$	J/g		183	73	146
collimator r=1.4 / Pyr. C	$P$	kW		25,9	12,9	25,8
collimator r=1.4 / Ti	$E_{max}$	J/g		22	30	32
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collimator r=1.0 / Ti	$P$	kW			0,2	0,4
collimator r=1.0 / Fe	$E_{max}$	J/g			9	19
collimator r=1.0 / Fe	$P$	kW			0,1	0,2
cooling / Cu	$P$	kW			1,8	3,6

		Pyr. C	Ti	Fe (ST70)	W (annealed)	W26Re (hardened)
Fatigue Temperature : (Ansys) $T$	°C	900	600	130	185	500
Fatigue Energy : (Ansys) $E_{fatigue}$	J/g	753	314	58	24	64
Fatigue Yield Strength : (Ansys) $P_{fatigue}$	MPa	40	340	280	440	600
Exp. Fatigue Yield Strength : $0.4 R_{max}$	MPa	36	356	280	440	600
Exp. Yield Strength : $R_{max} / R_{elastic}$	MPa	90	890 / 820	700 / 340	1100 / 800	1500 / 1200

$$\Delta T = E_{max} * c_v^{-1}$$

$$c_v^{-1} \text{ Carbon} \approx 1.2 \text{ [g}^* \text{K/J]}$$

$$c_v^{-1} \text{ Ti,Fe} \approx 2.0 \text{ [g}^* \text{K/J]}$$



# TDR parameter table with different collimator settings

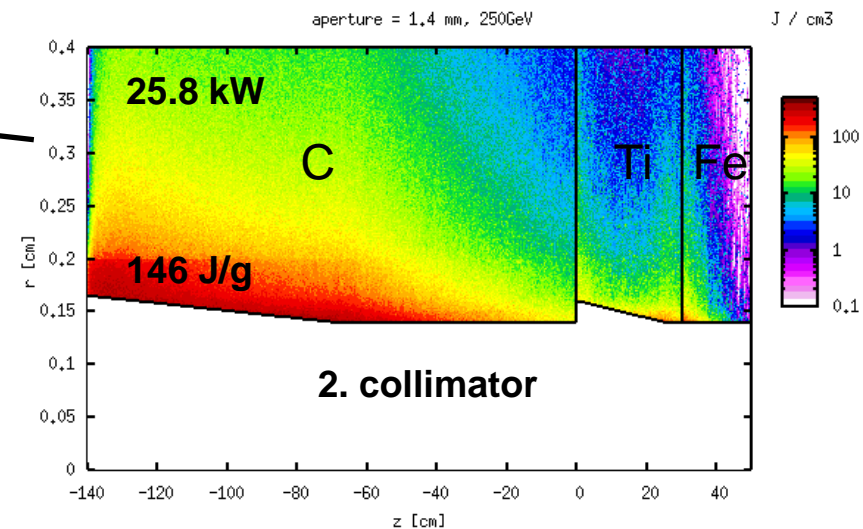
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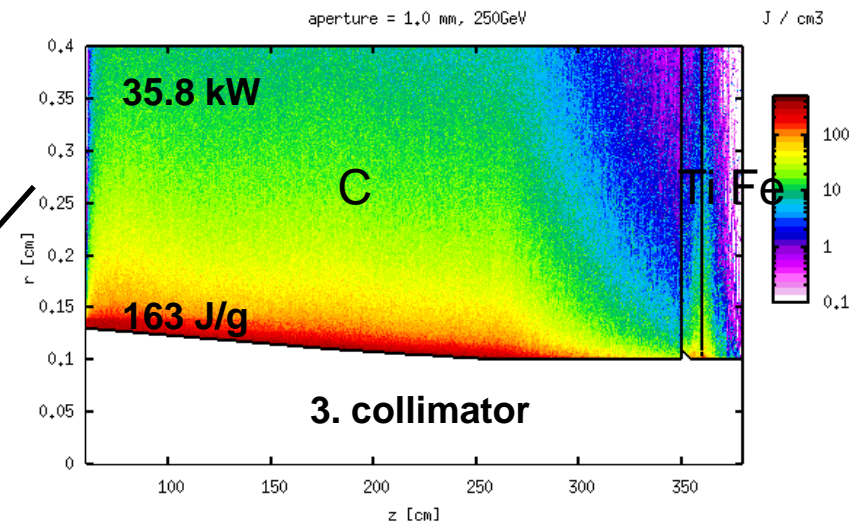
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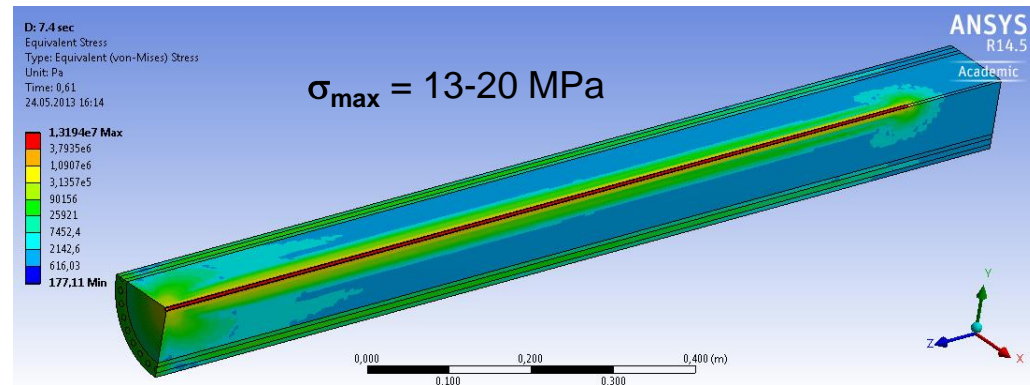
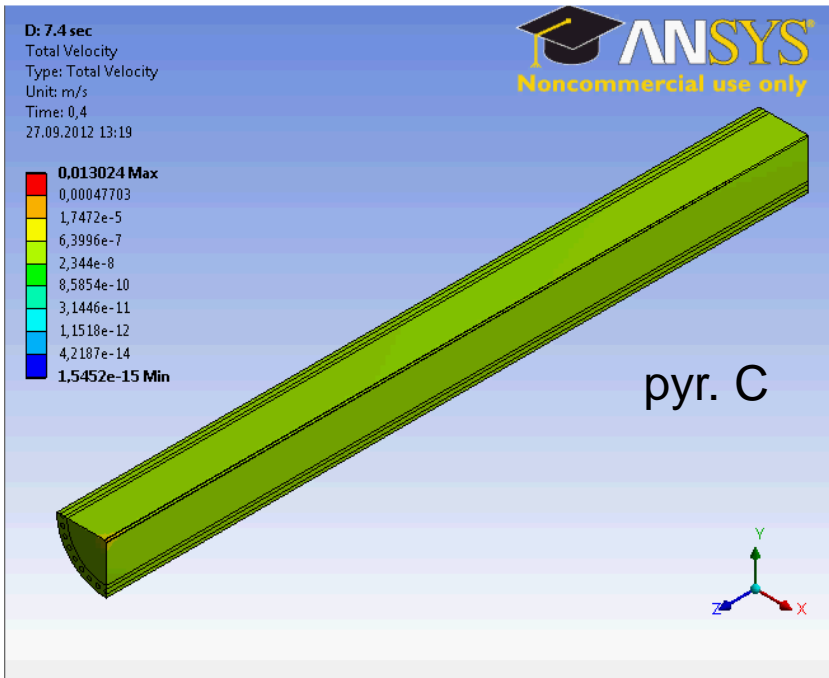
$$\Delta T = E_{max} * c_v^{-1}$$

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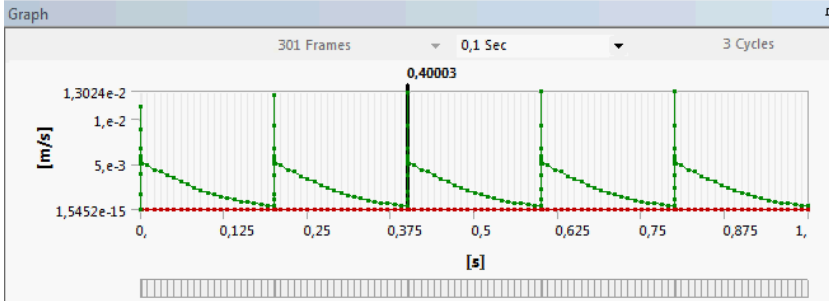
$$c_v^{-1} \text{ Ti,Fe} \approx 2.0 \text{ [g}^* \text{K/J]}$$



# Dynamic evolution in the 1. collimator (high lumi)



$\bar{\sigma} = 3 \text{ MPa}$

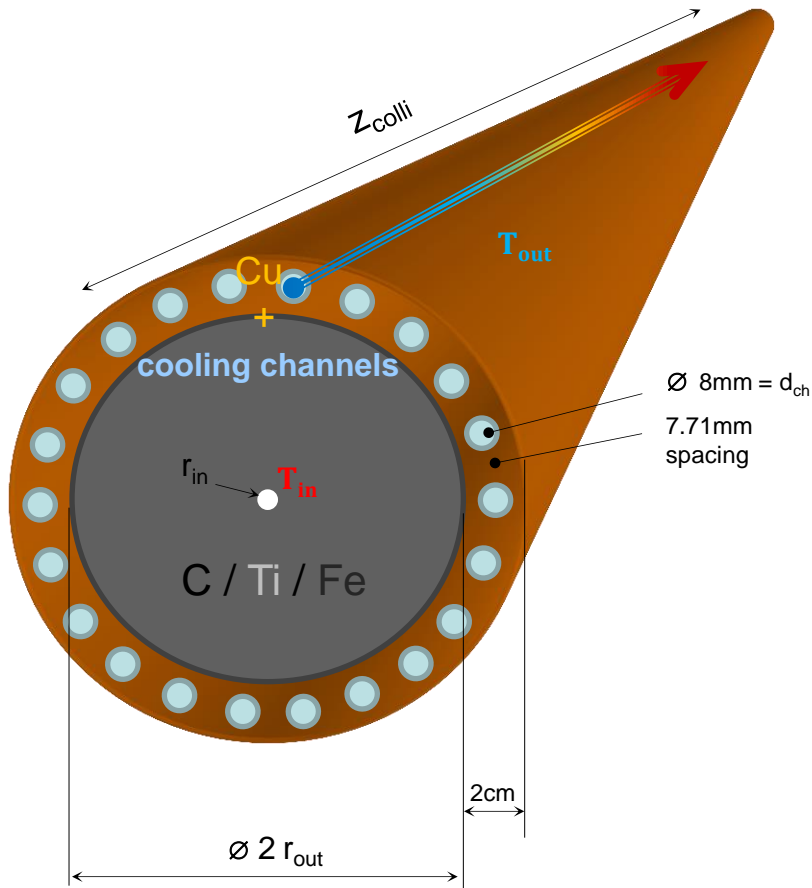


$2 \cdot 10^{10} \text{ e}^- / \text{ bunch}$   
 2625 bunch / train (0.97ms)  
 0.366  $\mu\text{s}$  bunch spacing  
 5 train / s

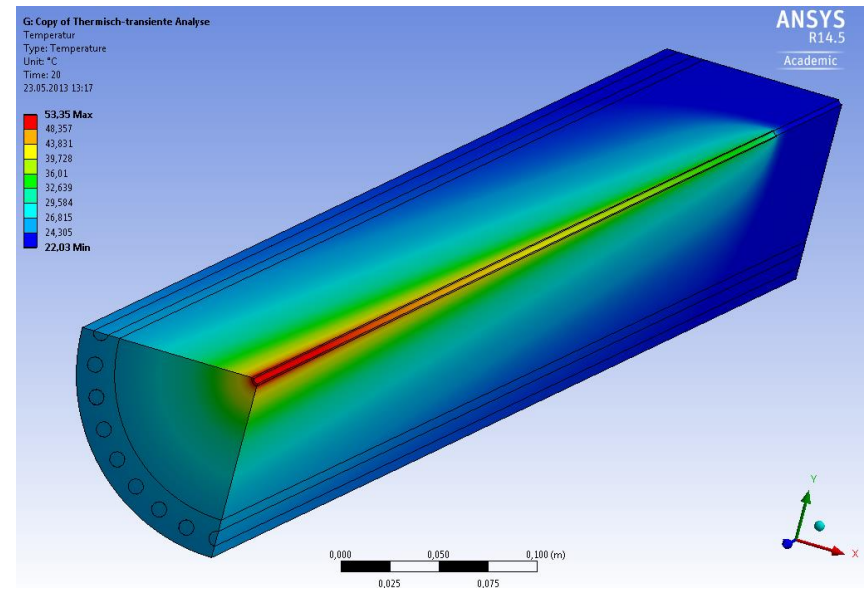
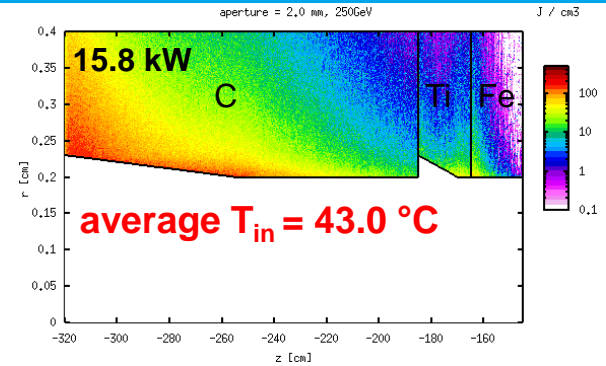
# Collimator cooling (average temperature)

$$\xrightarrow{\text{cyl.}} \dot{Q} = \frac{\lambda 2\pi z_{\text{colli}} \Delta T}{\ln(r_{\text{out}}/r_{\text{in}})}$$

radial heat flow



## 1. Collimator



$$T_{\text{in}} = \frac{\dot{Q}_0 \ln(r_{\text{out}}/r_{\text{in}})}{\lambda 2\pi z_{\text{colli}}} + T_{\text{water}} (22^\circ\text{C}) + \underbrace{\frac{\dot{Q}_0 \text{norm}}{d\dot{Q}_{\text{cool}}/dT} \cdot \frac{z}{z_{\text{colli}}}}_{\Delta T_{\text{water}}}$$

$\Delta T = 19.5 \text{ K}$ 
 $22^\circ\text{C}$ 
 $\Delta T = 1.5 \text{ K}$



# Cooling and temperature (high lumi)

drive beam 250GeV  $e^-$  ,  $P_{e^+} = 50\%$

<b>Carbon</b>	average T [°C]	$\Delta T$ peak [K]	$\Delta E$ peak [J/g]	fatigue Energy [J/g]
1. collimator	43	86	72	750
2. collimator	54	174	146	
3. collimator	46	194	163	

<b>Titanium</b>	average T [°C]	$\Delta T$ peak [K]	$\Delta E$ peak [J/g]	fatigue Energy [J/g]
1. collimator	67	21	11	350
2. collimator	123	61	32	
3. collimator	132	50	26	

<b>Iron (St70)</b>	average T [°C]	$\Delta T$ peak [K]	$\Delta E$ peak [J/g]	fatigue Energy [J/g]
1. collimator	30	22	10	50
2. collimator	31	49	22	
3. collimator	32	42	19	

# Cooling and temperature

drive beam 175GeV  $e^-$  ,  $P_{e^+} = 59\%$

<b>Carbon</b>	average T [°C]	$\Delta T$ peak [K]	$\Delta E$ peak [J/g]	fatigue Energy [J/g]
1. collimator	70	172	144	750
2. collimator	54	219	183	

<b>Titanium</b>	average T [°C]	$\Delta T$ peak [K]	$\Delta E$ peak [J/g]	fatigue Energy [J/g]
1. collimator	113	34	18	350
2. collimator	98	42	22	

<b>Iron (St70)</b>	average T [°C]	$\Delta T$ peak [K]	$\Delta E$ peak [J/g]	fatigue Energy [J/g]
1. collimator	34	29	13	50
2. collimator	32	29	13	

# Cooling and temperature

drive beam 150GeV  $e^-$  ,  $P_{e^+} = 55\%$

<b>Carbon</b>	average T [°C]	$\Delta T$ peak [K]	$\Delta E$ peak [J/g]	fatigue Energy [J/g]
1. collimator	81	140	177	750

<b>Titanium</b>	average T [°C]	$\Delta T$ peak [K]	$\Delta E$ peak [J/g]	fatigue Energy [J/g]
1. collimator	113	31	16	350

<b>Iron (St70)</b>	average T [°C]	$\Delta T$ peak [K]	$\Delta E$ peak [J/g]	fatigue Energy [J/g]
1. collimator	30	29	13	50

# Conclusion

- The collimator design achieved the fatigue stress limits of the materials for the proposed parameter sets (including safety factors)
- Dynamical calculations for the collimator shows not critical behavior
- Collimator cooling should be not difficult for this introduced design

to do: a material test experiment at a suitable accelerator have to be performed to verify (fatigue) stress limits with realistic beam conditions

# Material data

element $x_0[cm]$	$E [GPa]$	$\nu$	$\rho \left[ \frac{g}{cm^3} \right]$	$\alpha \left[ \frac{10^{-5}}{K} \right]$	$c_v \left[ \frac{J}{kg K} \right]$	$\lambda \left[ \frac{W}{m K} \right]$
<b>Au</b> 0.34	81	0.42	19.3	1.43	128	320
<b>Ag</b> 0.85	83	0.38	10.5	1.97	234	430
<b>Cu</b> 1.42	117	0.34	8.3	1.65	385	400
<b>W</b> 0.35	406	0.28	19.3	0.45	138	170
<b>Fe</b> 1.76	196	0.30	7.9	1.22	449	80
<b>Ti</b> 3.59	114	0.34	4.4	0.9	580	7-22
<b>C</b> 18.84	20	0	2.2	0.05 - 0.6	837	350

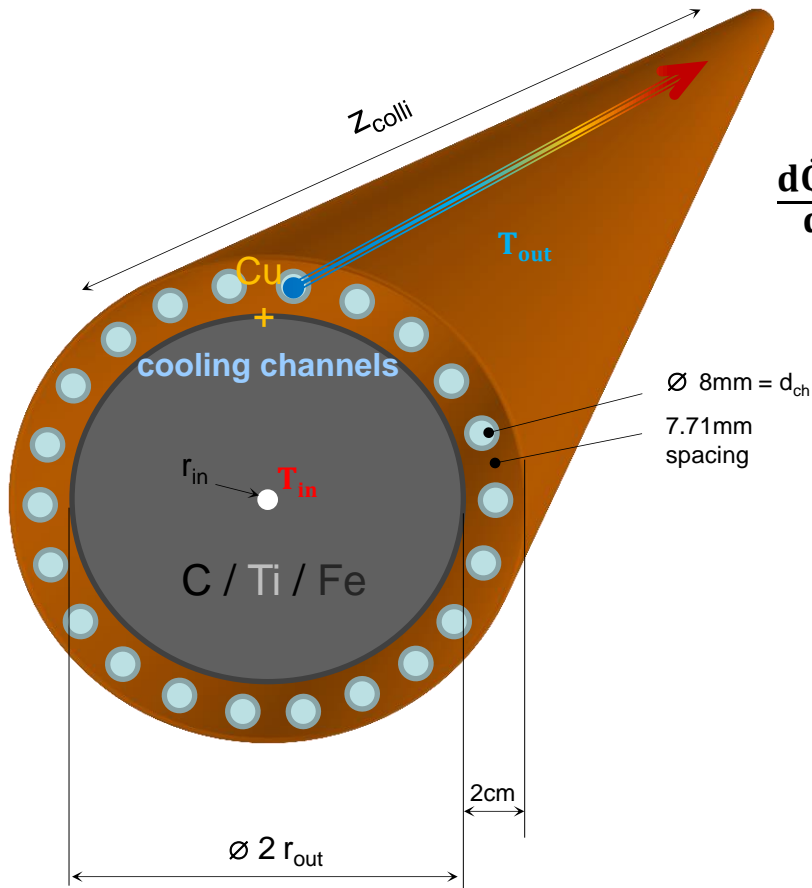
# Collimator cooling (average temperature)

## Reynolds number

$$Re = \frac{\bar{v}_{\text{water}} d_{\text{ch}}}{\nu(T = 30^\circ\text{C})_{\text{kin vis}}} = \frac{\bar{v}_{\text{water}} d_{\text{ch}} \rho}{\eta(T = 30^\circ\text{C})_{\text{dyn vis}}} \approx 2000 < 2300 = Re_{\text{krit, lamin}}$$

laminar flow of water !

$$\frac{d\dot{Q}_{\text{cool}}}{dT} / \text{chan.} \approx 0.3 \text{ kW}/\text{m}^2 \text{ K} \Leftrightarrow \bar{v}_{\text{water}} = 2 \text{ m/s} \xrightarrow{d_{\text{ch}}=8\text{mm}} 0.1 \text{ l/s}$$

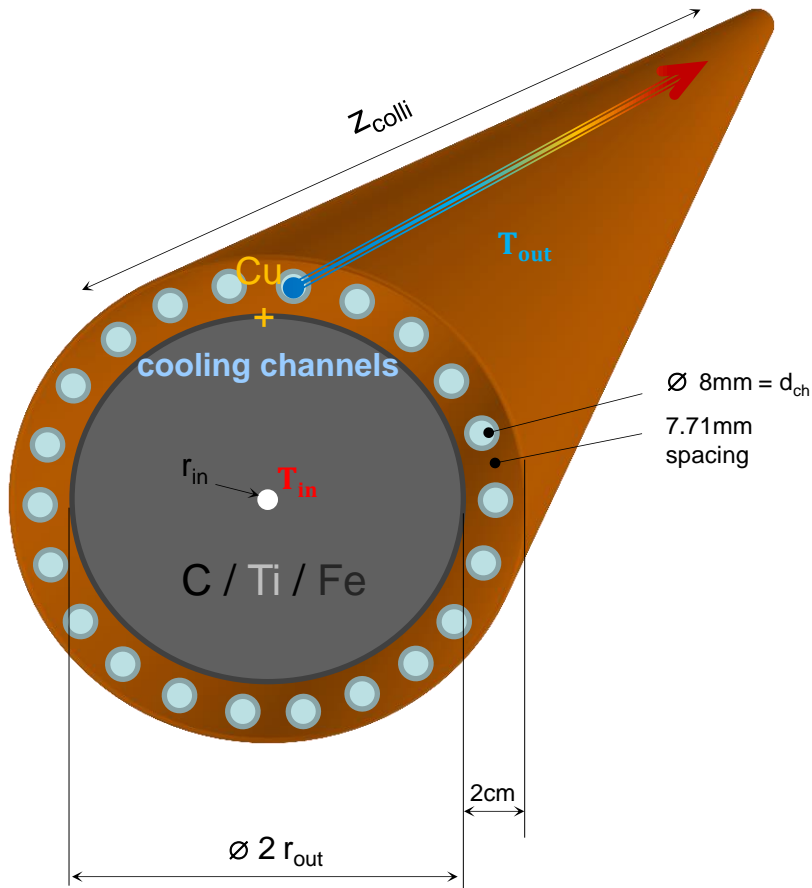


$$r_{\text{out}} = \begin{cases} 7.0\text{cm} \Rightarrow \frac{d\dot{Q}_{\text{cool}}}{dT} (32 \text{ ch}) \approx 9.6 \text{ kW}/\text{m}^2 \text{ K} \\ 4.5\text{cm} \Rightarrow \frac{d\dot{Q}_{\text{cool}}}{dT} (22 \text{ ch}) \approx 6.6 \text{ kW}/\text{m}^2 \text{ K} \end{cases}$$

# Collimator cooling (average temperature)

$$\xrightarrow{\text{cyl.}} \dot{Q} = \frac{\lambda 2\pi z_{\text{colli}} \Delta T}{\ln(r_{\text{out}}/r_{\text{in}})}$$

radial heat flow



$$\Delta T = T_{\text{in}} - T_{\text{out}} = \frac{\dot{Q}_0 \ln(r_{\text{out}}/r_{\text{in}})}{\lambda 2\pi z_{\text{colli}}}$$

$$\xrightarrow{\text{cooling}} T_{\text{out}}(z) = T_{\text{water}}(20^\circ\text{C}) + \frac{\dot{Q}_0 \text{norm}}{\underbrace{d\dot{Q}_{\text{cool}}/dT}_{\Delta T_{\text{water}}}} \cdot \frac{z}{z_{\text{colli}}}$$

$$\dot{Q}_0 \text{norm} = \frac{\dot{Q}_0}{A_{\text{cyl}}} = \frac{\dot{Q}_0}{2\pi r_{\text{out}} z_{\text{colli}}} \quad [\text{kW}/\text{m}_2]$$

$\xrightarrow{\text{cooling}}$

$$T_{\text{in}} = \frac{\dot{Q}_0 \ln(r_{\text{out}}/r_{\text{in}})}{\lambda 2\pi z_{\text{colli}}} + T_{\text{water}}(20^\circ\text{C}) + \frac{\dot{Q}_0 \text{norm}}{\underbrace{d\dot{Q}_{\text{cool}}/dT}_{\Delta T_{\text{water}}}} \cdot \frac{z}{z_{\text{colli}}}$$