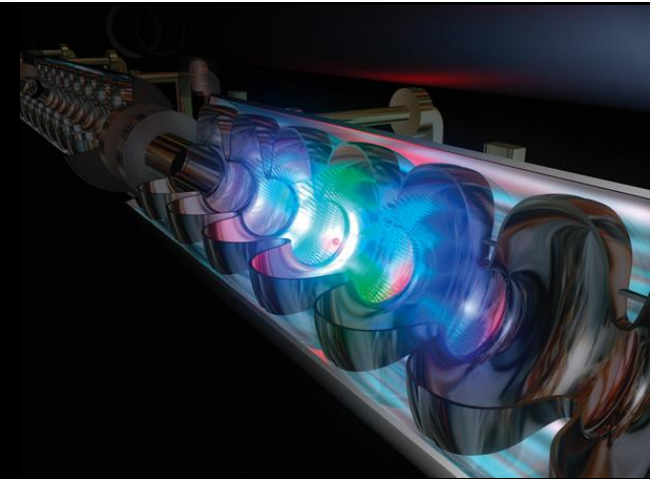


Bilinear R-Parity violation at the ILC.

Neutrino physics at colliders



[Benedikt Vormwald](#), Jenny List

ECFA Workshop 2013

Hamburg, 27.05.-31.05.2013



Universität Hamburg

DER FORSCHUNG | DER LEHRE | DER BILDUNG



- > Bilinear RPV – a motivation
- > Analysis strategy
- > Full Simulation
- > Precision estimation for measuring the neutrino atmospheric mixing angle
- > Conclusions



MSSM Superpotential

$$W = h_U^{ij} \hat{Q}_i \cdot \hat{H}_u \hat{U}_j + h_D^{ij} \hat{Q}_i \cdot \hat{H}_d \hat{D}_j + h_E^{ij} \hat{L}_i \cdot \hat{H}_u \hat{R}_j - \mu \hat{H}_d \cdot \hat{H}_u$$

additional allowed terms:

$$W_{\Delta L=1} = \lambda^{ijk} \hat{L}_i \cdot \hat{L}_j \hat{R}_k + \lambda'^{ijk} \hat{L}_i \cdot \hat{Q}_j \hat{D}_k + \mu^i \hat{L}_i \cdot \hat{H}_u \quad W_{\Delta B=1} = \lambda'^{ijk} U_i \hat{D}_j \hat{D}_k$$

→ most general gauge-invariant and renormalizable superpotential

Some facts of bilinear R-parity violation

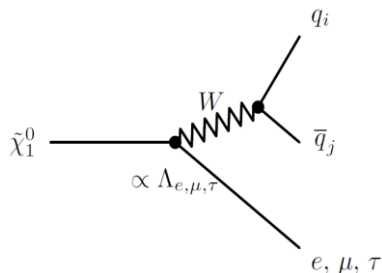
- largest neutrino mass at tree level
- 2 mixing angles at tree level
- remaining masses/angles at 1-loop-level
- correct scales of mass differences Δm_{ij}^2

$$m_\nu = \frac{M_1 g^2 + M_2 g'^2}{4 \det M_{\chi^0}} |\vec{\Lambda}|^2$$

$$\tan \theta_{23} = \frac{\Lambda_\mu}{\Lambda_\tau} \quad \tan \theta_{13} = -\frac{\Lambda_e}{\sqrt{\Lambda_\mu^2 + \Lambda_\tau^2}}$$

How is that connected to colliders?

dominant part of $\tilde{\chi}_1^0 - W - l_i$ coupling: $O_i^L = \Lambda_i \cdot f(M_1, M_2, \mu, \tan \beta, v_d, v_u) \propto \Lambda_i$



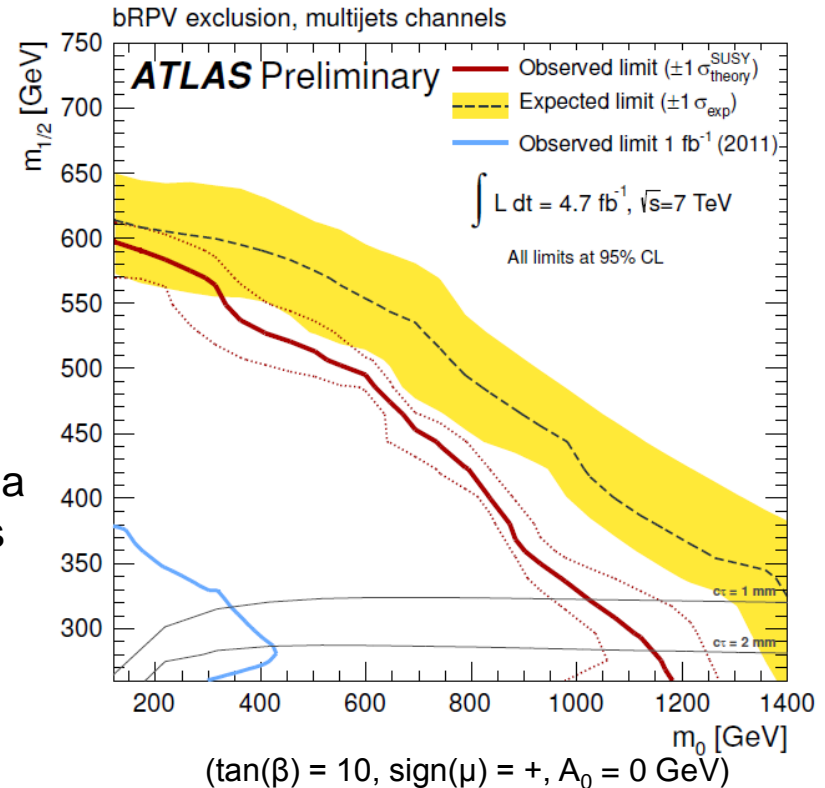
$$\tan^2 \theta_{23} = \left| \frac{\Lambda_\mu}{\Lambda_\tau} \right|^2 \cong \frac{BR(\tilde{\chi}_1^0 \rightarrow \mu W)}{BR(\tilde{\chi}_1^0 \rightarrow \tau W)}$$

→ Neutrino physics at collider experiments

Situation at LHC

One dedicated bRPV mSUGRA search from ATLAS (**ATLAS-CONF-2012-140**):

- large jet multiplicity
- 1 isolated lepton
- missing transverse momentum
- bRPV parameters fitted to neutrino data
- bRPV mSUGRA tested for $m_{1/2} > 240\text{GeV}$ ($\rightarrow c\tau < 15\text{ mm}$)
- analysis probes colored sector of theory via squark production and subsequent decays
- coupling of EW sector and colored sector



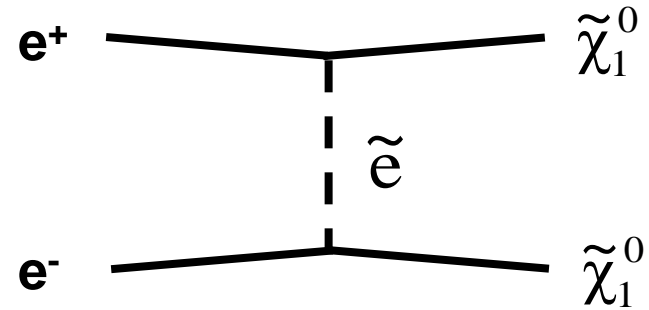
Situation at the ILC

- direct neutralino production \rightarrow direct access to EW sector
- need better parametrization than mSUGRA to study phenomenology of this model, especially decouple EW sector from colored one \rightarrow generic model

Generic SUSY model

Model definition

- high squark masses (~ 1.5 TeV)
- gaugino like LSP
- most relevant parameters for cross section:
 - selectron mass
 - neutralino mass

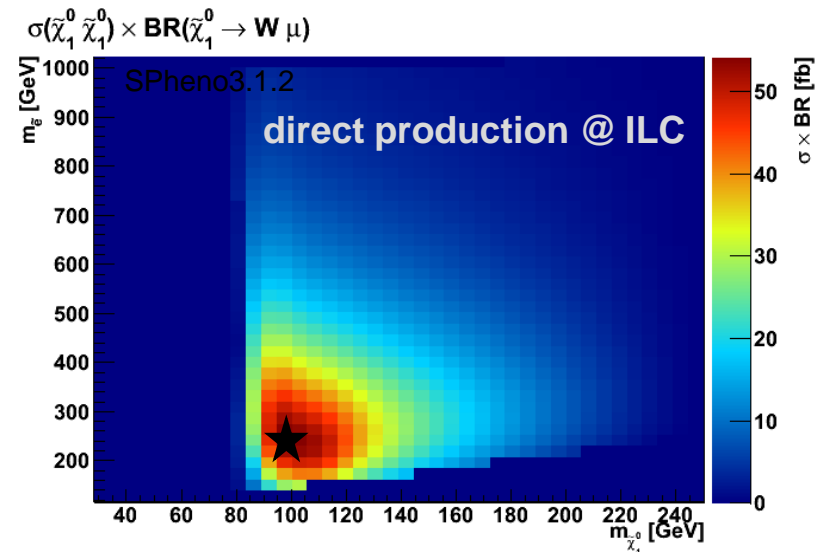


Example point

- $m(\tilde{\chi}_1^0) = 98.4$ GeV
- $c\tau = 4.55$ mm
- $BR(\tilde{\chi}_1^0 \rightarrow W \mu) = 0.28$
- $BR(\tilde{\chi}_1^0 \rightarrow W \tau) = 0.25$

beam polarization $\sqrt{s} = 500$ GeV:

$P(e^+)$	$P(e^-)$	$\sigma(ee \rightarrow \tilde{\chi}_1^0 \tilde{\chi}_1^0)$ [fb]
+0.3	-0.8	35
-0.3	-0.8	49
0	0	170
+0.3	+0.8	209
-0.3	+0.8	387



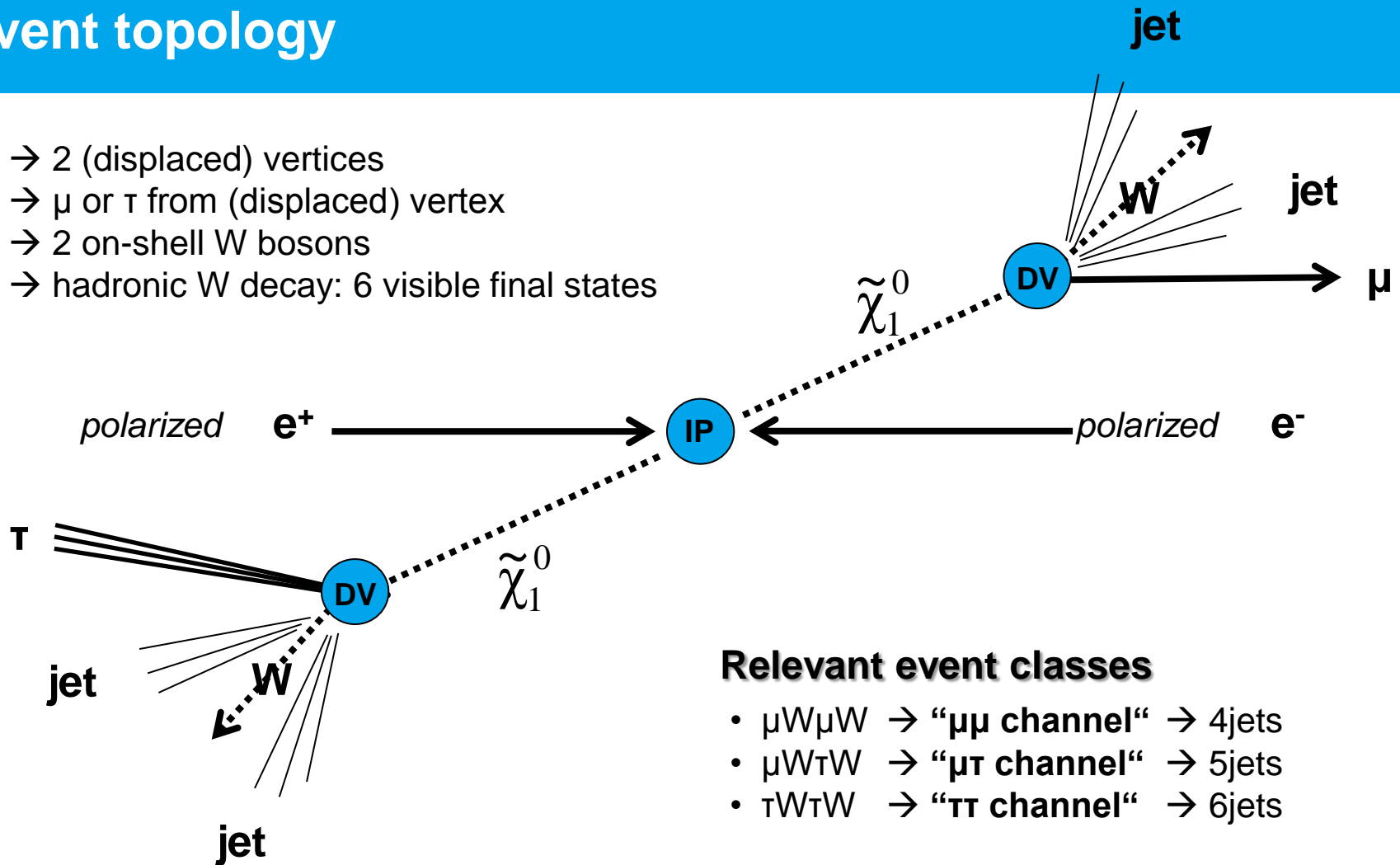
Expectations for $\int L dt = 500 \text{ fb}^{-1}$

- ~193500 events:
- ~15170 ($\mu W \mu W$) events
- ~12093 ($\tau W \tau W$) events



Event topology

- 2 (displaced) vertices
- μ or τ from (displaced) vertex
- 2 on-shell W bosons
- hadronic W decay: 6 visible final states



Relevant event classes

- $\mu W \mu W \rightarrow$ “ $\mu\mu$ channel” \rightarrow 4jets
- $\mu W \tau W \rightarrow$ “ $\mu\tau$ channel” \rightarrow 5jets
- $\tau W \tau W \rightarrow$ “ $\tau\tau$ channel” \rightarrow 6jets

Goals

- reconstruct neutralino mass
- count event classes in order to measure ratio of $BR(\chi_{10} \rightarrow W \mu)$ and $BR(\chi_{10} \rightarrow W \tau)$
- later step: measure decay length

Reconstruction strategy

events

$\gamma\gamma$ background removal
preselection

test for
 $\mu\mu$

- remove **2 leading muons** from PFO objects
- force rest of the event into **4 jets**
- find **two good W** candidates from jets
- try to combine **2 equal mass objects** from Ws and leptons



test for
 $\mu\tau$

- remove **leading muon** from PFO objects
- force rest of the event into **5 jets**
- consider jet with lowest multiplicity as tau
- find **two good W** candidates from remaining 4 jets
- try to combine **two equal mass objects** from Ws and leptons



test for
 $\tau\tau$

- force event into **6 jets**
- consider two jets with lowest multiplicity as taus
- find **two good W** candidates from remaining 4 jets
- try to combine **two equal mass objects** from Ws and leptons



Datasets and used software

Datasets

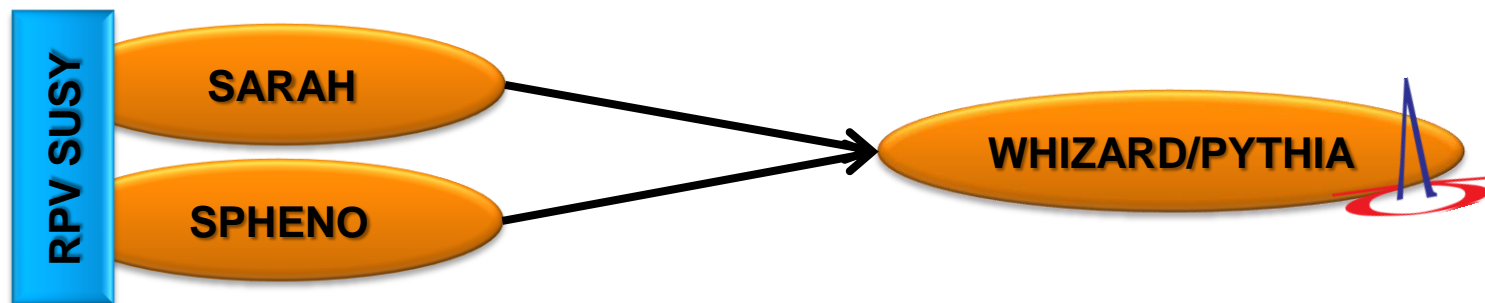
- 6f SM background: 500GeV DBD mass production (ILD_o1_v05)
- bRPV SUSY signal: private production with DBD software

Theory input

- *SARAH* for generating model files for event generator
- *SPheno* for SUSY parameter calculation and for fit of RPV parameters to neutrino data

Event generation

ILCWhizard (v1.95)
including ILC beam spectrum



Full Simulation

- simulated and reconstructed with ILCDIRAC system
- *reconstruction*: v01-16-p05_500
- *simulation*: v01-14-01-p00

data sample with:

100 fb⁻¹
500 GeV

Preselection

select only events with high multiplicity and small missing energy:

- reduce SM 6f background
- reduce leptonic W decay contribution

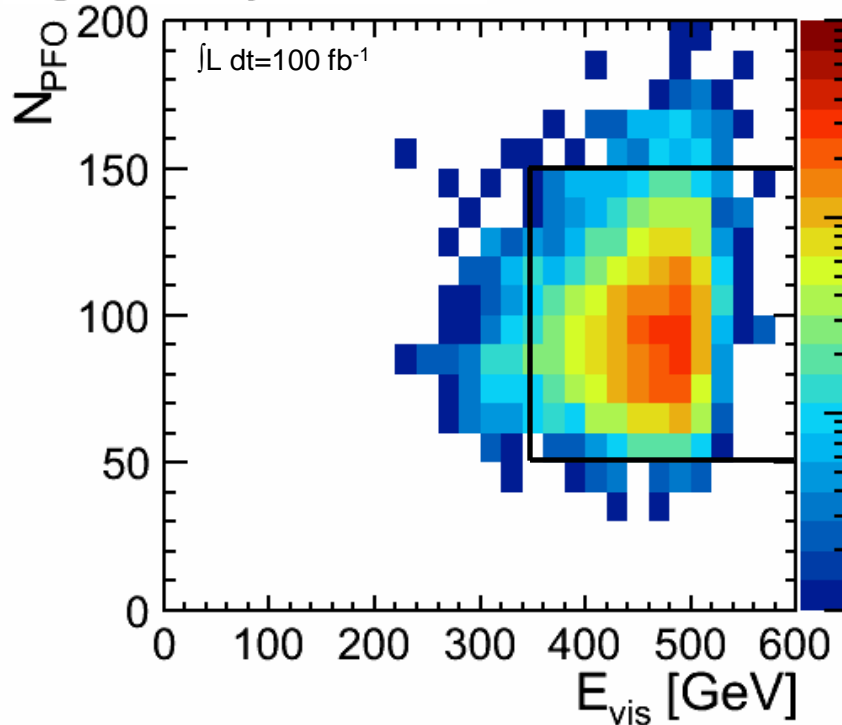
→ $E_{\text{vis}} > 350\text{GeV}$

→ $N_{\text{PFO}} > 50$

→ $N_{\text{PFO}} < 150$

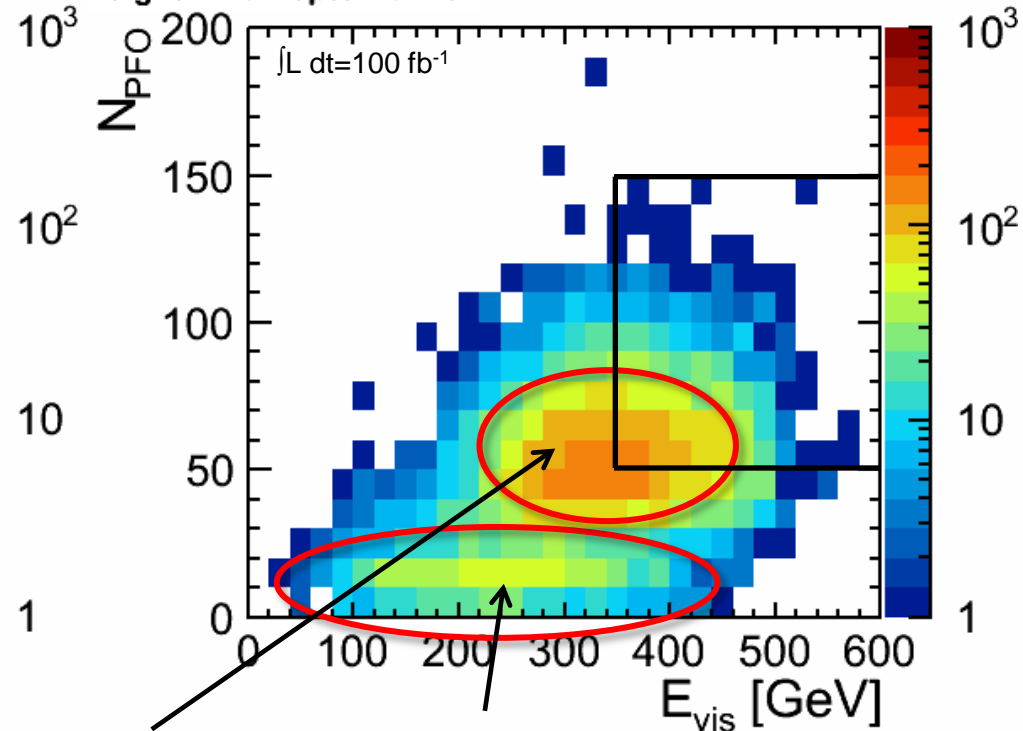
$IW_{\text{had}}IW_{\text{had}}$

signal with fully hadronic Ws



$IW_{\text{had,lep}}IW_{\text{lep}}$

signal with leptonic Ws

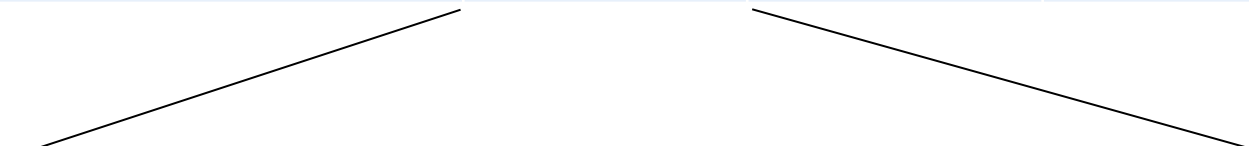


1 leptonic Ws

2 leptonic Ws

Preselection – cut flow

cut	SUSY signal	SUSY non-signal	SM 6f background
no cut	5641	32564	49461
excl. k_T converged	5641	32299	49453
$E_{\text{vis}} > 350 \text{ GeV}$	5483	11593	40224
$N_{\text{PFO}} > 50$	5468	8472	39927
$N_{\text{PFO}} < 150$	5390	8414	29825
efficiency	0.96	0.26	0.60



cut	$\mu\mu$ channel	$\mu\tau$ channel	$\tau\tau$ channel
no	1617	2783	1241
preselection	1561	2656	1173
efficiency	0.965	0.954	0.945

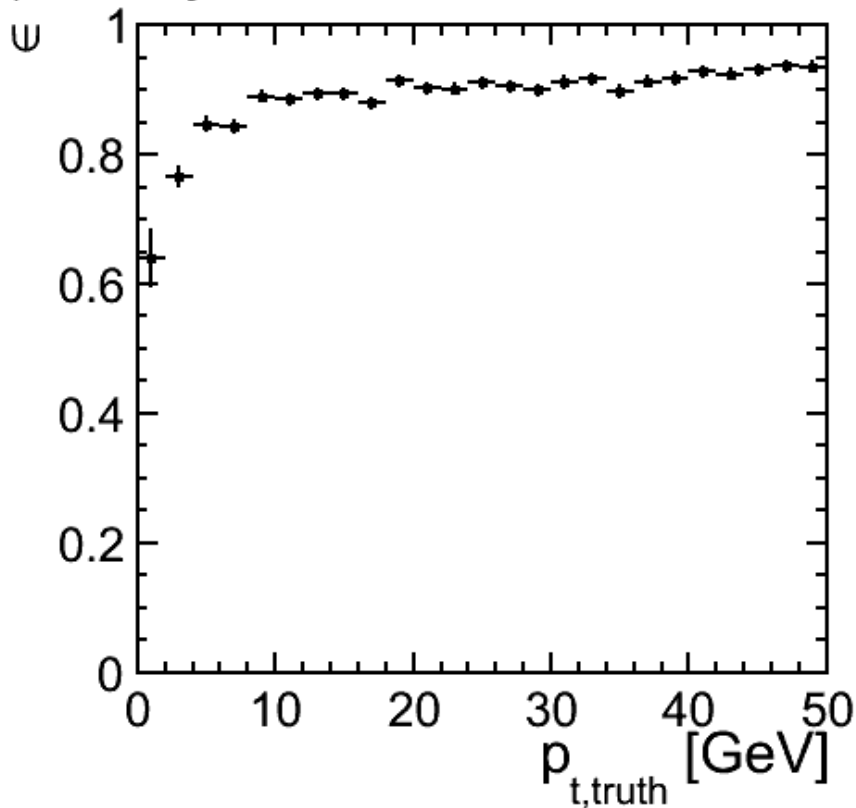


Muon reconstruction ($\mu\mu$ channel)

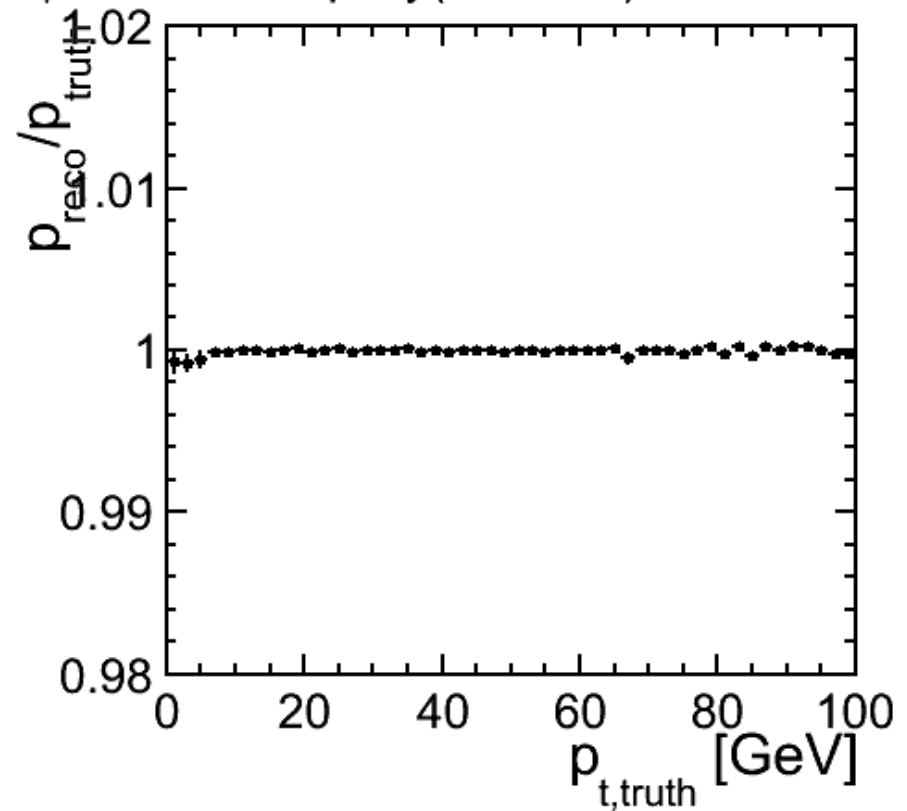
selection:

- Pandora PFO muons
- no isolation required \rightarrow depends on neutralino mass
- keep two most energetic muons as signal muons

μ efficiency vs. momentum



μ reconstruction quality (momentum)



\rightarrow overall efficiency of signal muon: 91%



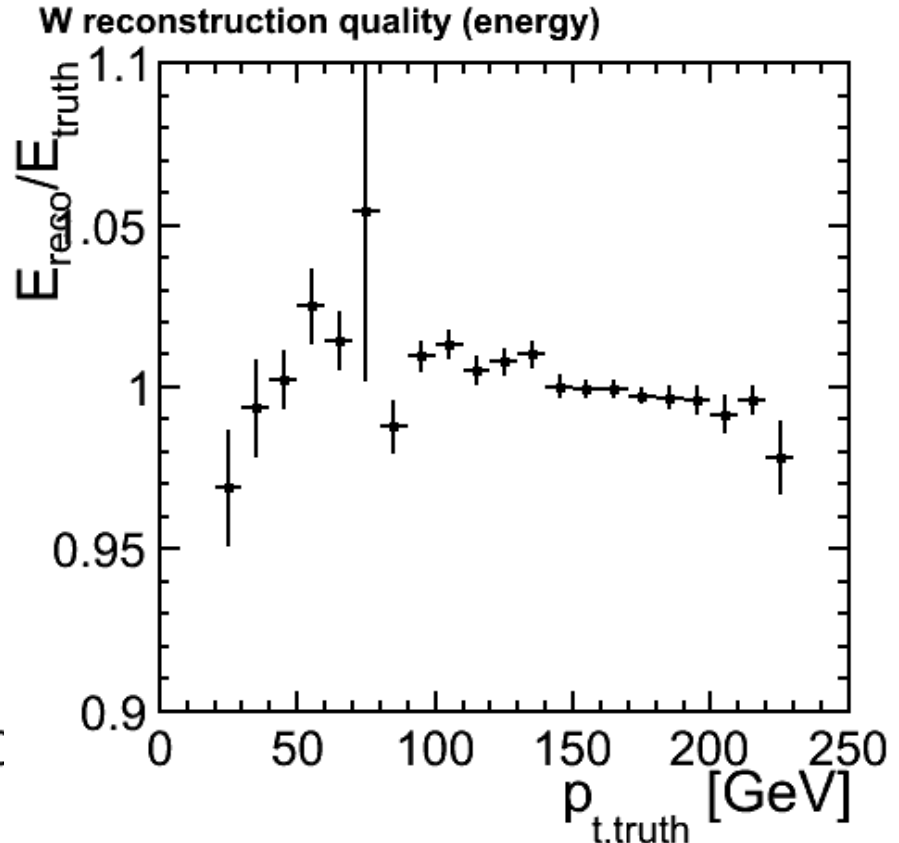
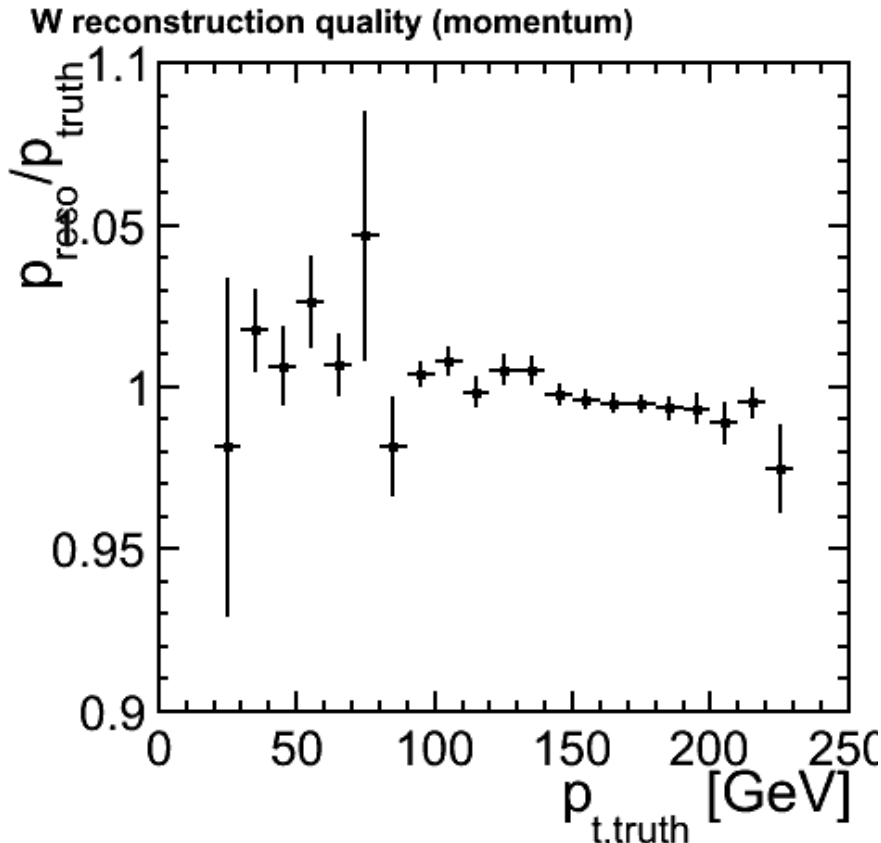
W reconstruction ($\mu\mu$ channel)

- remove leading muons from event
- force remaining objects into 4 jets (Durham)
- pair jets and test against W mass



$$\chi_W^2 = \frac{(m_{\text{reco}} - m_W)^2}{(5\text{GeV})^2}$$

best jet combination is considered as W



→ W efficiency: 64% for ($\chi_W^2 < 2$) and can be further increased with kinematic fitting

Full event reconstruction ($\mu\mu$ channel)

combine into two equal mass objects

2 μ

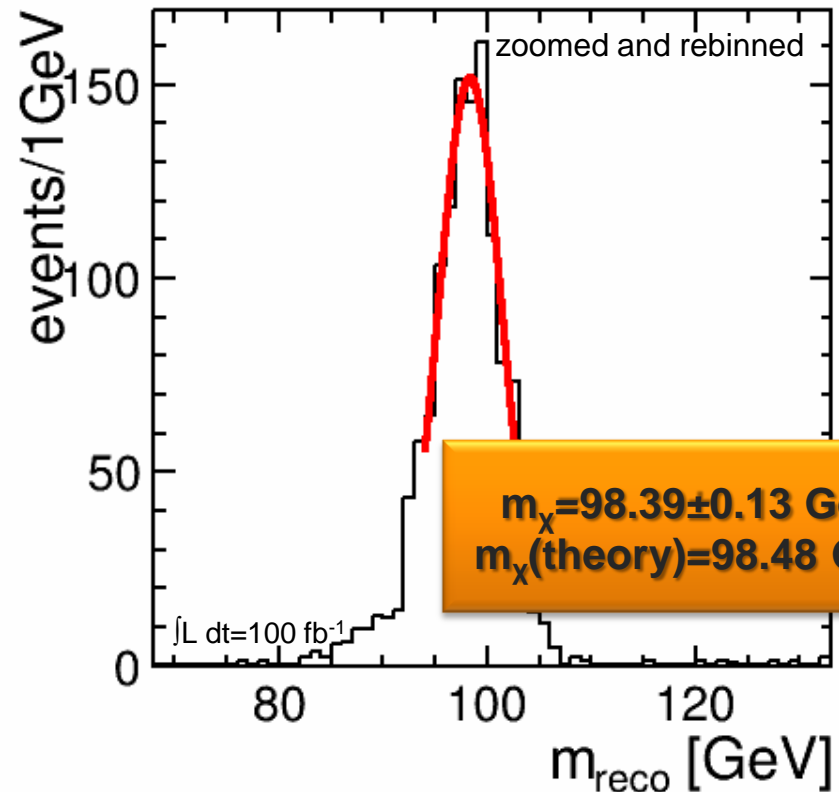
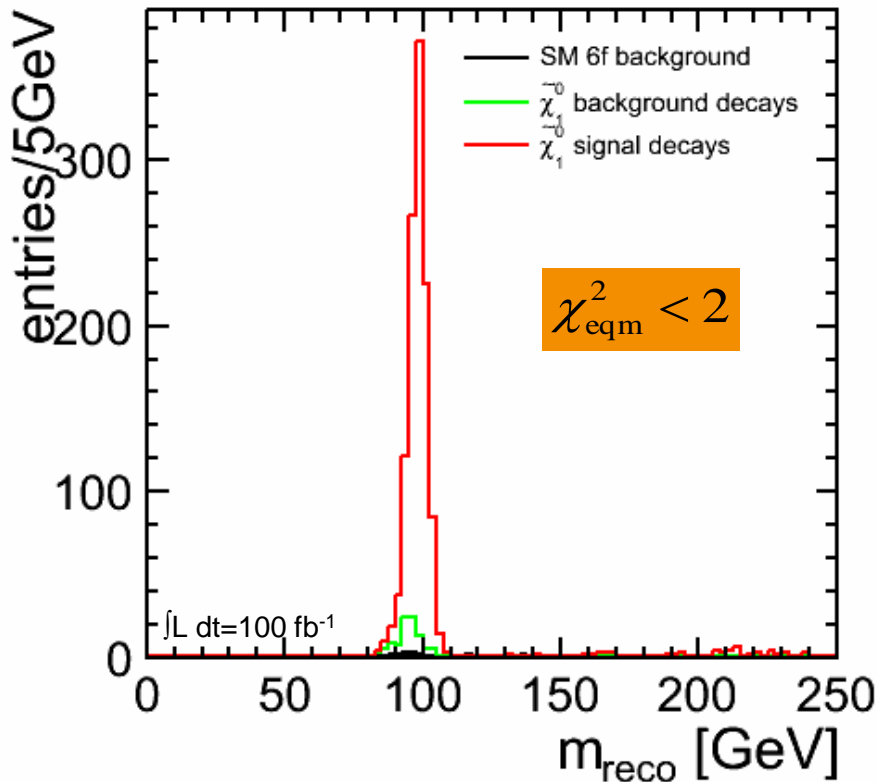


$$\chi_{\text{eqm}}^2 = \frac{(m_{p1} - m_{p2})^2}{(5\text{GeV})^2}$$

2 W



reconstructed mass in $W\mu W\mu$ channel



- very clean reconstruction of neutralino mass
- almost no 6f standard model background



Full event reconstruction (other channels)

test for
 $\mu\tau$

- remove **leading muon** from PFO objects
- force rest of the event into **5 jets**
- consider jet with lowest multiplicity as tau
- find **two good W** candidates from remaining 4 jets
- try to combine **two equal mass objects** from Ws and leptons

→ analog to $\mu\mu$ channel

test for
 $\tau\tau$

- force event into **6 jets**
- consider two jets with lowest multiplicity as taus
- find **two good W** candidates from remaining 4 jets
- try to combine **two equal mass objects** from Ws and leptons

- number of events after preselection in $\tau\tau$ channel ($\mu\mu$ channel): 1173 (1561)
- W selection similar to selection in $\mu\mu$ channel :

$$\chi_W^2 < 2 \quad \text{using} \quad \chi_W^2 = \frac{(m_{\text{reco}} - m_W)^2}{(5\text{GeV})^2}$$

- efficiency for full event reconstruction including taus is expected to be much less than in muonic channel



Full event reconstruction ($\tau\tau$ channel)

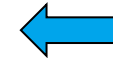
combine into two equal mass objects

2 τ



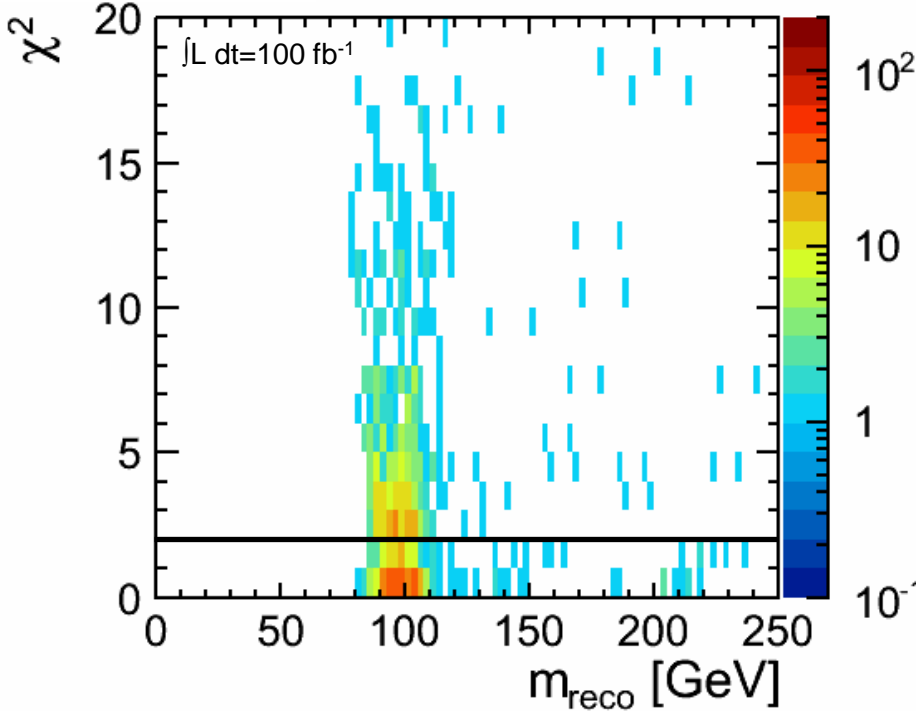
$$\chi_{\text{eqm}}^2 = \frac{(m_{p1} - m_{p2})^2}{(5\text{GeV})^2}$$

2 W

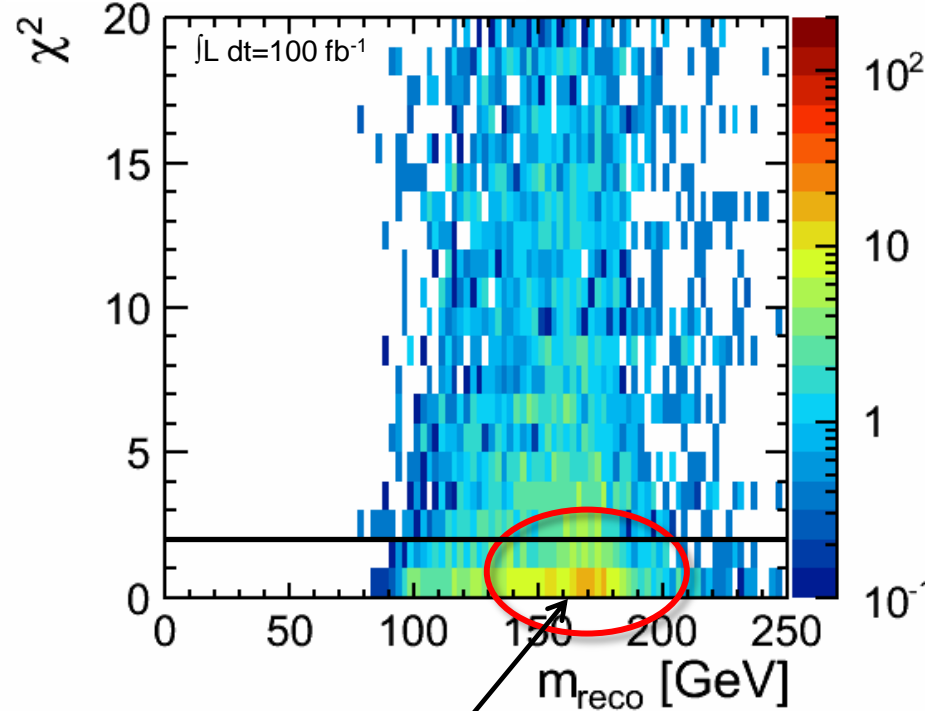


aka "2 jet with least components"

signal ($\tau\tau$ channel)



SM 6f background ($\tau\tau$ channel)



ttbar



Full event reconstruction ($\tau\tau$ channel)

combine into two equal mass objects

2 τ



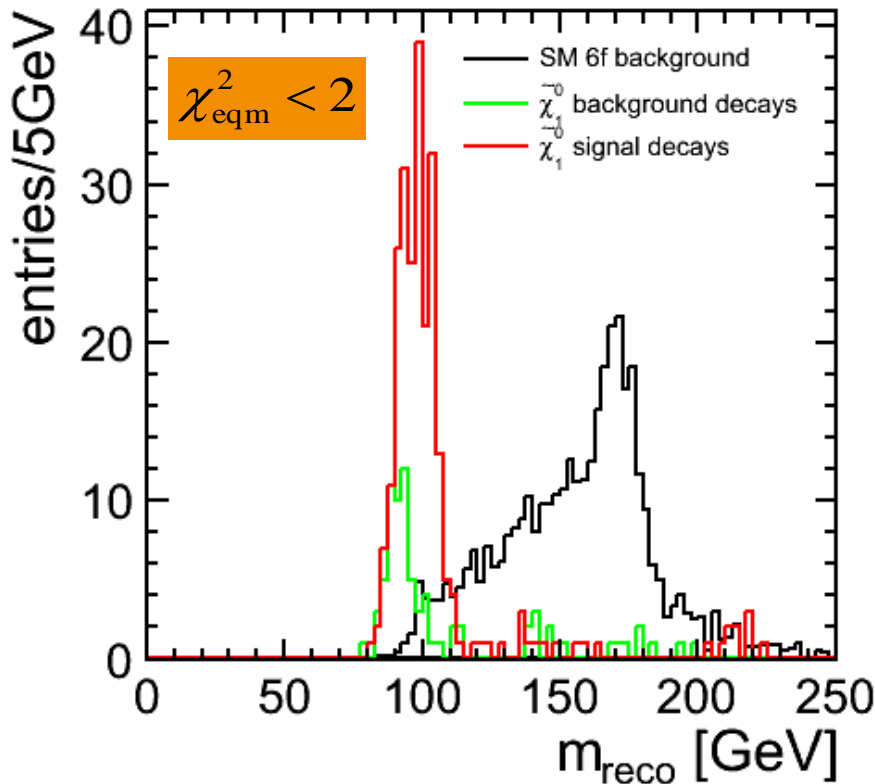
$$\chi_{\text{eqm}}^2 = \frac{(m_{p1} - m_{p2})^2}{(5\text{GeV})^2}$$

2 W

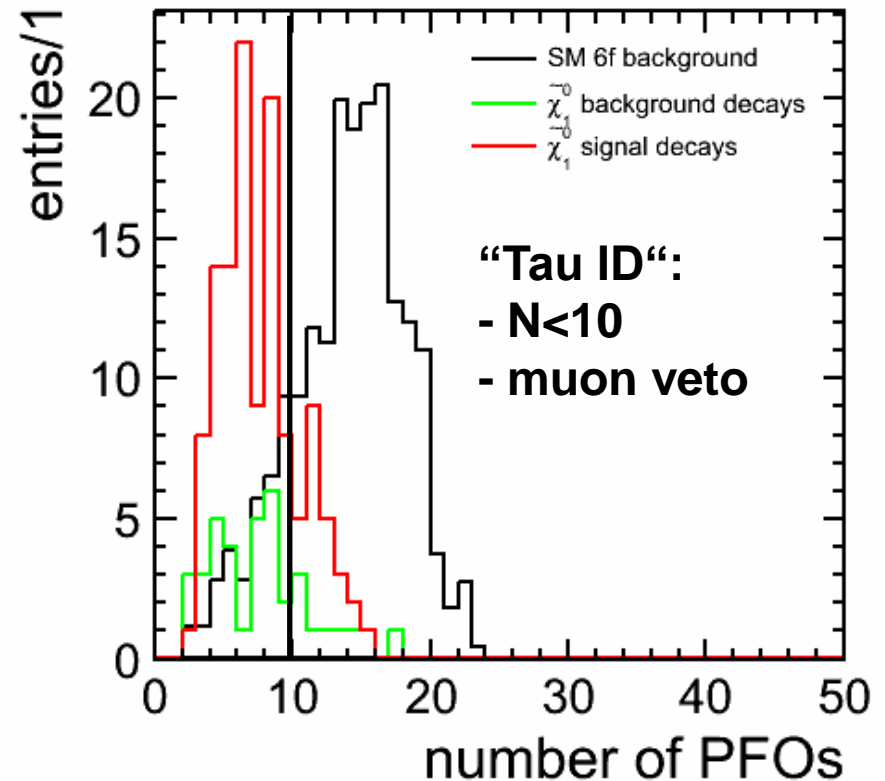


aka "2 jet with least components"

reconstructed mass in $W\tau W\tau$ channel



number of PFOs in biggest τ jet



Full event reconstruction ($\tau\tau$ channel)

combine into two equal mass objects

2 τ



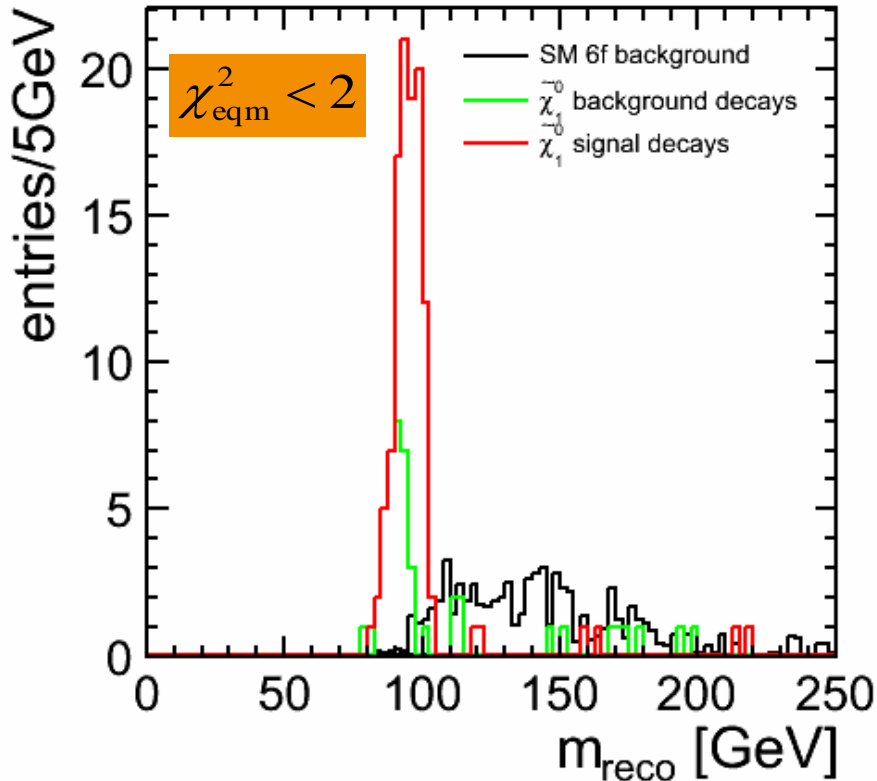
$$\chi_{\text{eqm}}^2 = \frac{(m_{p1} - m_{p2})^2}{(5\text{GeV})^2}$$

2 W

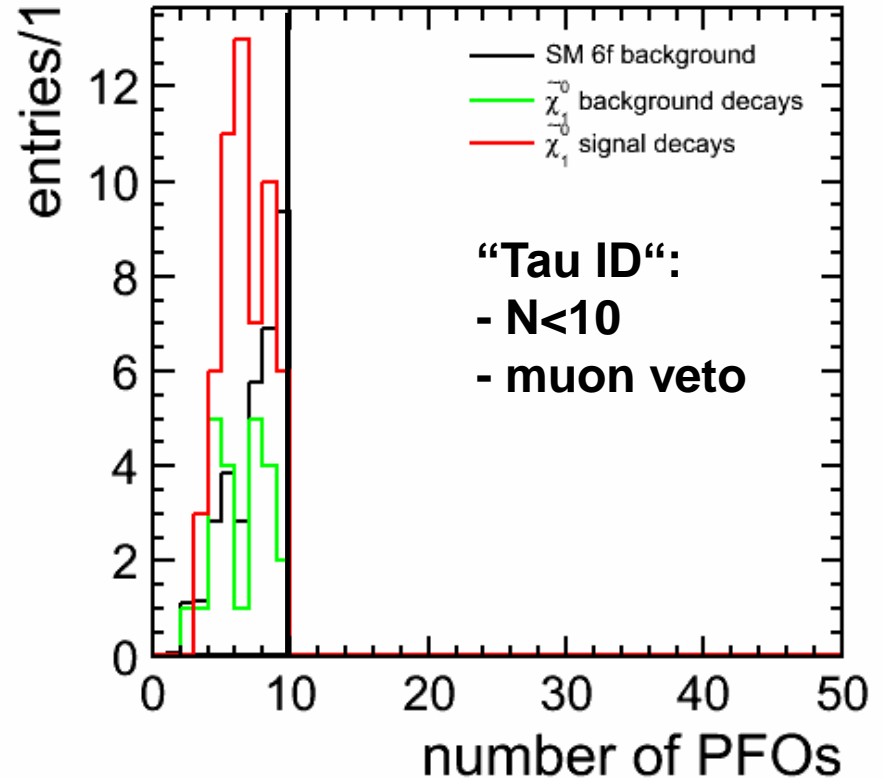


aka "2 jet with least components"

reconstructed mass in $W\tau W\tau$ channel



number of PFOs in biggest τ jet



Efficiency matrix

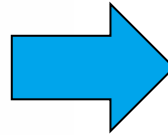
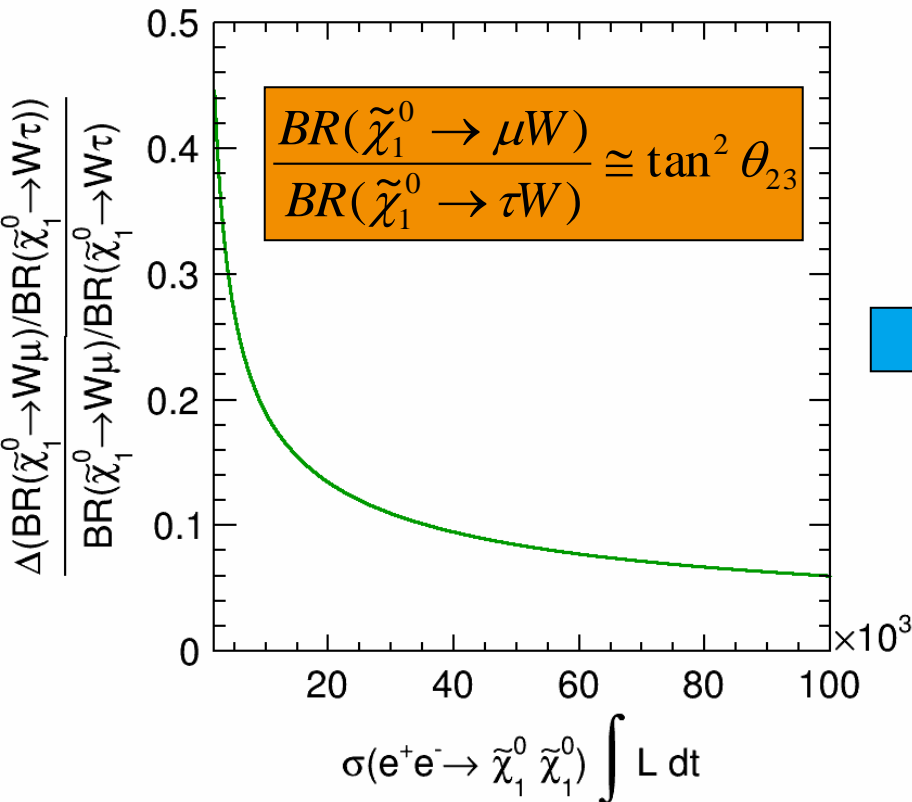
	$\text{true } \mu W_{\text{had}} \mu W_{\text{had}}$	$\text{true } \mu W_{\text{had}} T W_{\text{had}}$	$\text{true } T W_{\text{had}} T W_{\text{had}}$	SUSY non-signal	SM 6fBG
preselected	1561	2656	1173	8414	29825
N($\mu\mu$ channel)	513 0.329	91 0.034	13 0.011	51 0.006	13 0.0004
N($\mu\tau$ channel)	10 0.006	216 0.084	33 0.028	33 0.004	25 0.0008
N($\tau\tau$ channel)	0 0.000	2 0.009	54 0.046	23 0.003	34 0.0011

- SM 6f background controllable (especially in signal region)
- entries in efficiency matrix reasonable
- SUSY non-signal contribution dependent on SUSY parameters (mainly stau mass)

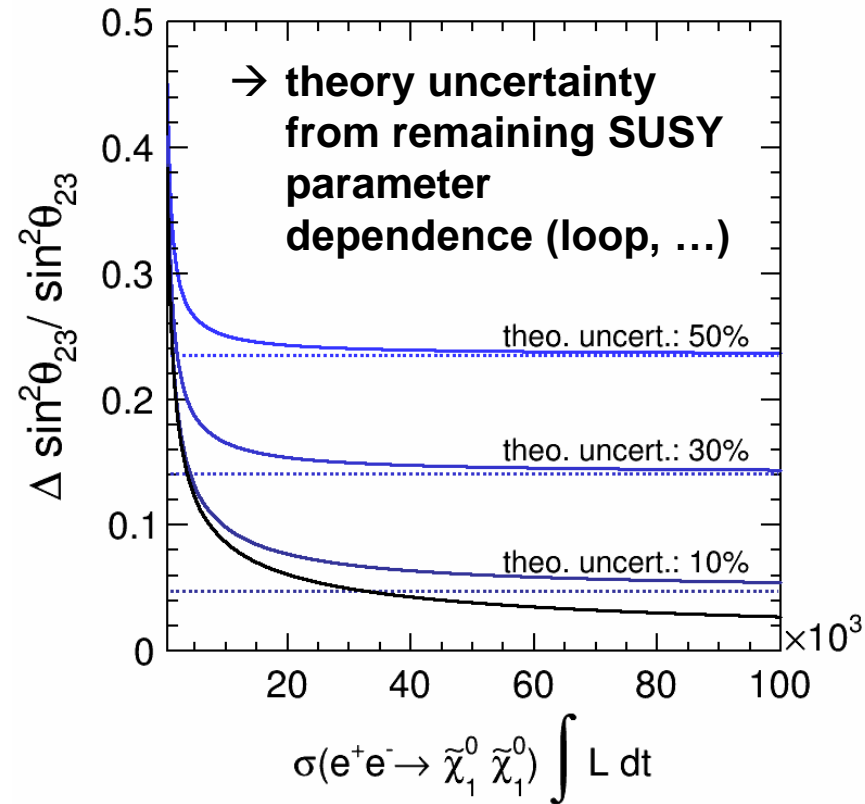


Precision estimation

relative error on ratio of BRs



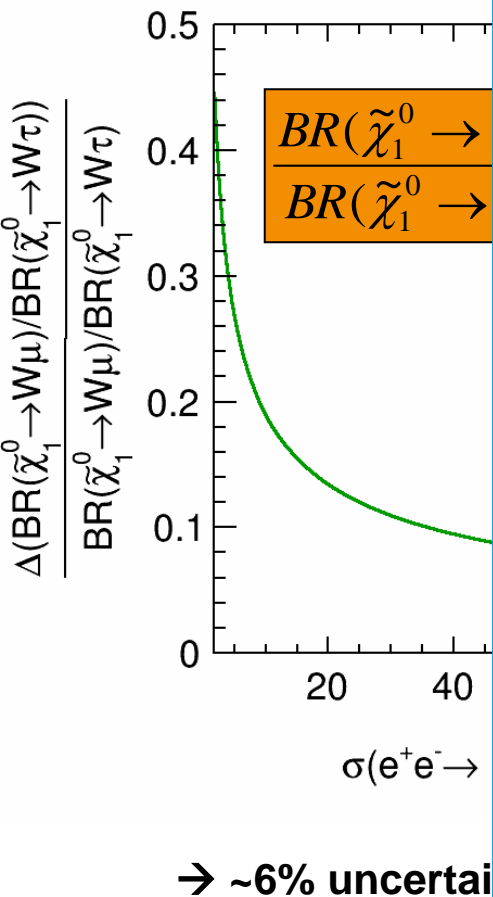
relative error on $\sin^2\theta_{23}$



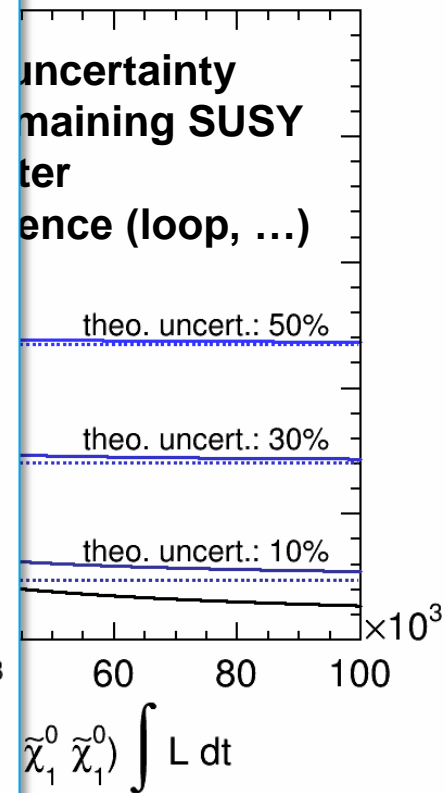
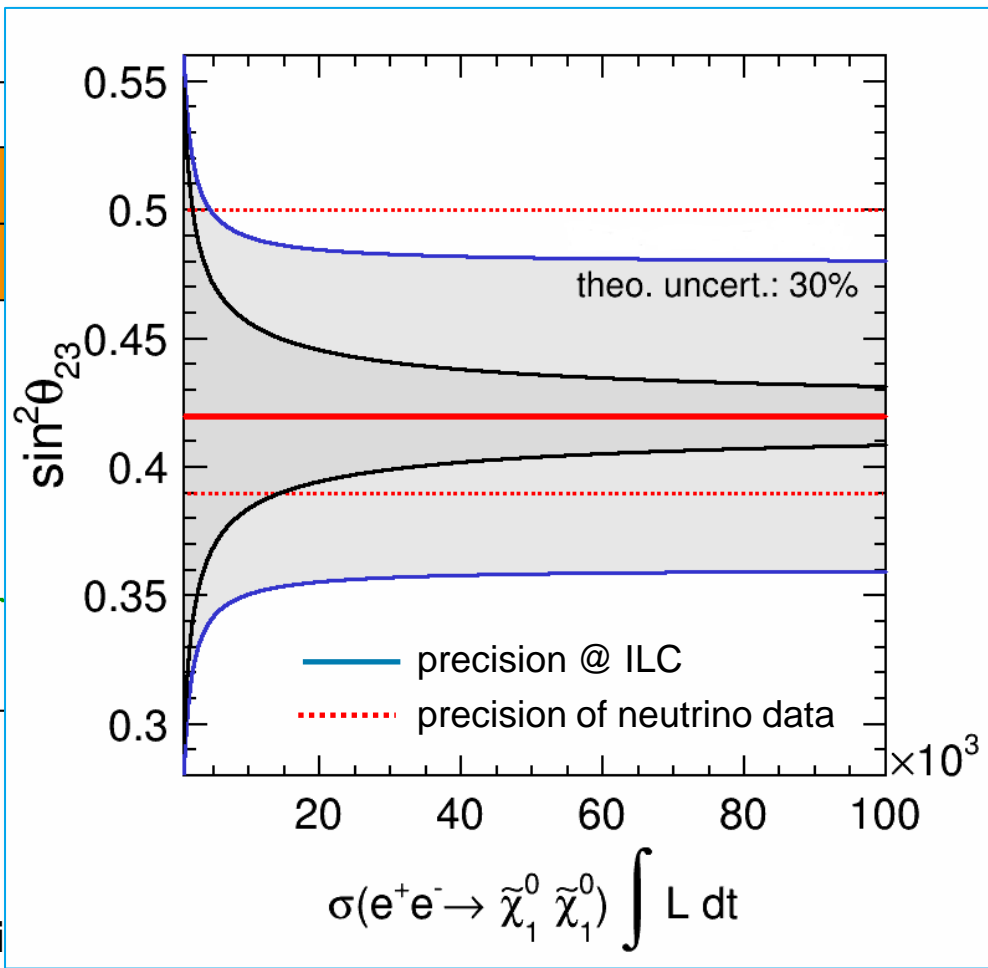
→ ~6% uncertainty after 100000 produced neutralino pairs

Precision estimation

relative error on ratio of BRs



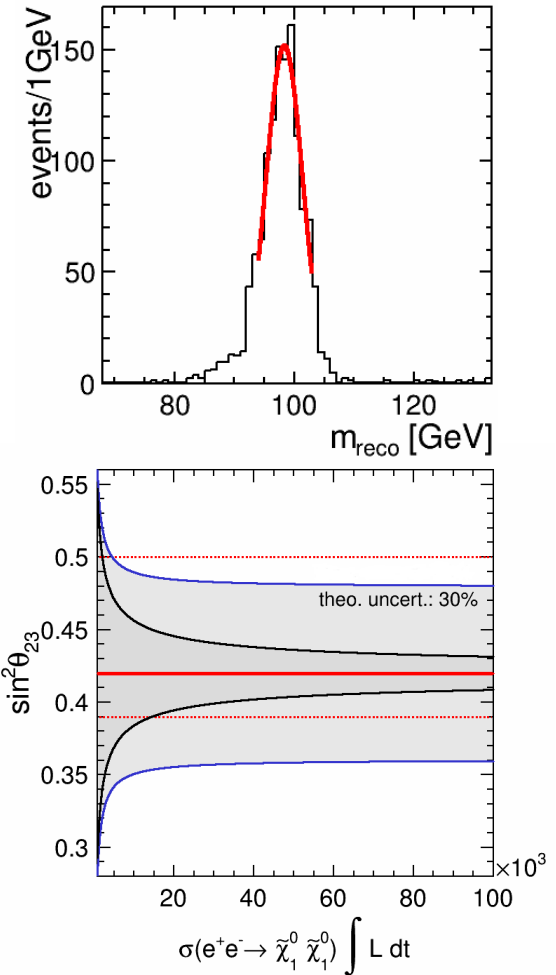
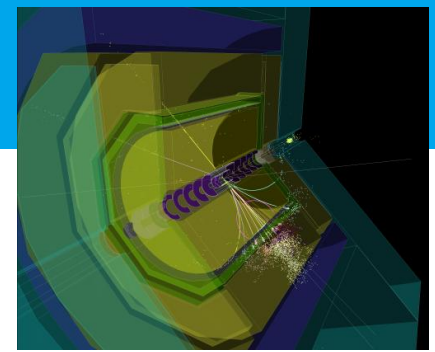
relative error on $\sin^2\theta_{23}$:



Conclusions

- R-parity violation is an interesting alternative to R-parity conserving SUSY
- allows an interesting **interpretation** in terms of **neutrino parameters**
- **full ILD simulation** of a bRPV SUSY model performed
- very clean **event class selection** possible, almost no background
- precise χ_{10} mass reconstruction:
 $m_{\chi} = 98.39 \pm 0.13 \text{ GeV}$
- **precision of atmospheric mixing angle measurement** in same ballpark as neutrino experiments

Thank you for your attention.



Backup slides



Superpotential

$$W = \underbrace{\varepsilon_{ab} \left(h_U^{ij} \hat{Q}_i^a \hat{U}_j \hat{H}_u^b + h_D^{ij} \hat{Q}_i^b \hat{D}_j \hat{H}_d^a + h_E^{ij} \hat{L}_i^b \hat{R}_j \hat{H}_u^a - \mu \hat{H}_d^a \hat{H}_u^b \right)}_{\text{MSSM superpotential}} + \underbrace{\varepsilon_i \hat{L}_i^a \hat{H}_u^b}_{\text{bRPV term}}$$

→ Higgs/Slepton-mixing

→ Sneutrinos acquire VEV $\langle \tilde{\nu}_i \rangle = v_i$

→ corresponding RPV soft SUSY breaking term $L_{soft}^{BRpV} = -B_i \varepsilon_{ab} \varepsilon_i \tilde{L}_i^a H_u^b$

$i=1\dots3$

masses and mixings of neutral fermions

Basis of neutral fermions: $\psi^{0T} = (-i\lambda', -i\lambda^3, \tilde{H}_d^1, \tilde{H}_u^2, \nu_e, \nu_\mu, \nu_\tau)$

Mass terms in the Lagrangian are given by: $L_m = -\frac{1}{2} (\psi^0)^T \mathbf{M}_N \psi^0 + h.c.$

$$\mathbf{M}_N = \begin{pmatrix} M_{\chi^0} & m^T \\ m & 0 \end{pmatrix}$$

4x4 MSSM neutralino mixing matrix → ← 4x3 RPV matrix



Approximate diagonalization of \mathbf{M}_N

$$\mathbf{M}_N = \begin{pmatrix} M_{\chi^0} & m^T \\ m & 0 \end{pmatrix}$$

\mathbf{M}_N can be block-diagonalized for small RPV parameters via the Seesaw-like diagonalization:

$$\mathbf{M}_N = \text{diag}(M_{\chi^0}, m_{\text{eff}})$$

$$m_{\text{eff}} = -m M_{\chi^0} m^T = \frac{M_1 g^2 + M_2 g'^2}{4 \det M_{\chi^0}} \begin{pmatrix} \Lambda_e^2 & \Lambda_e \Lambda_\mu & \Lambda_e \Lambda_\tau \\ \Lambda_\mu \Lambda_e & \Lambda_\mu^2 & \Lambda_\mu \Lambda_\tau \\ \Lambda_\tau \Lambda_e & \Lambda_\tau \Lambda_\mu & \Lambda_\tau^2 \end{pmatrix}$$

where $\Lambda_i = \varepsilon_i v_d + \mu v_i$ „alignment parameters“

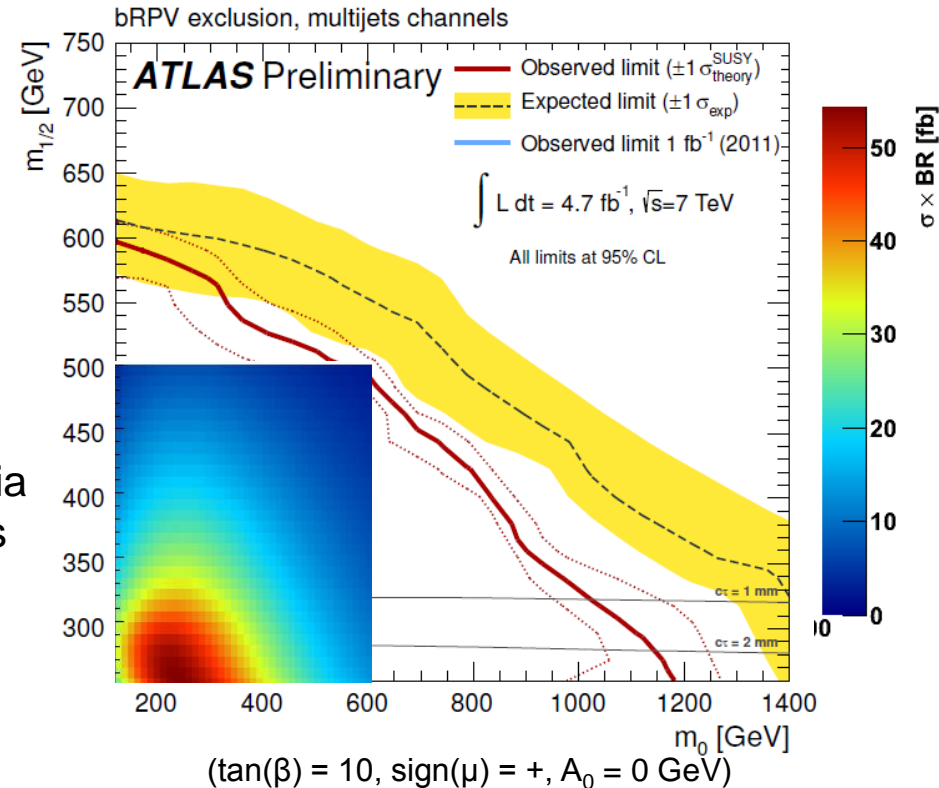
A final diagonalization of M_{χ^0} leads to the neutralino masses $m_{\chi_i^0}$ and a diagonalization of m_{eff} leads to one tree level neutrino mass.



Situation at LHC

One dedicated bRPV mSUGRA search from ATLAS (**ATLAS-CONF-2012-140**):

- large jet multiplicity
- 1 isolated lepton
- missing transverse momentum
- bRPV parameters fitted to neutrino data
- bRPV mSUGRA tested for $m_{1/2} > 240\text{GeV}$
- ($\rightarrow c\tau < 15\text{ mm}$)
- analysis probes colored sector of theory via squark production and subsequent decays
- coupling of EW sector and colored sector

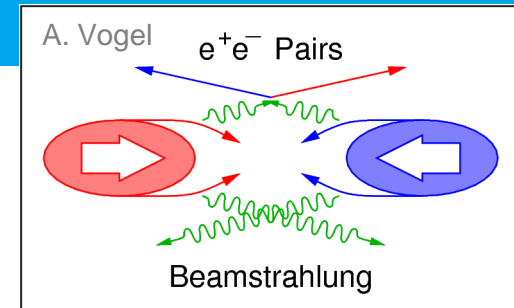


Situation at the ILC

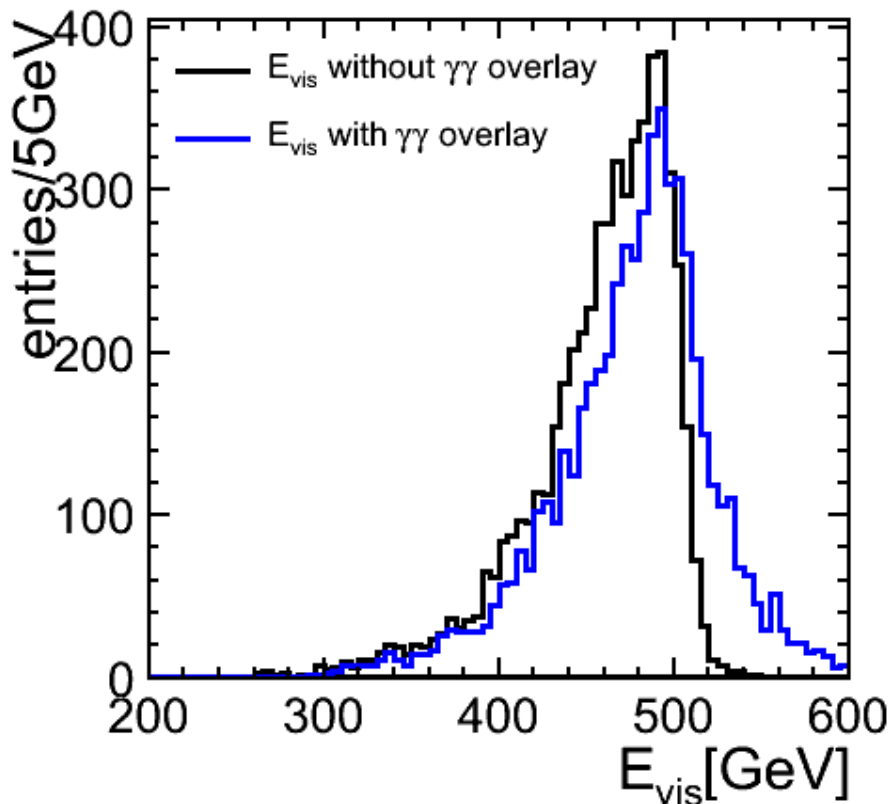
- direct neutralino production \rightarrow direct access to EW sector
- need better parametrization than mSUGRA to study phenomenology of this model, especially decouple EW sector from colored one \rightarrow generic model

Beam background

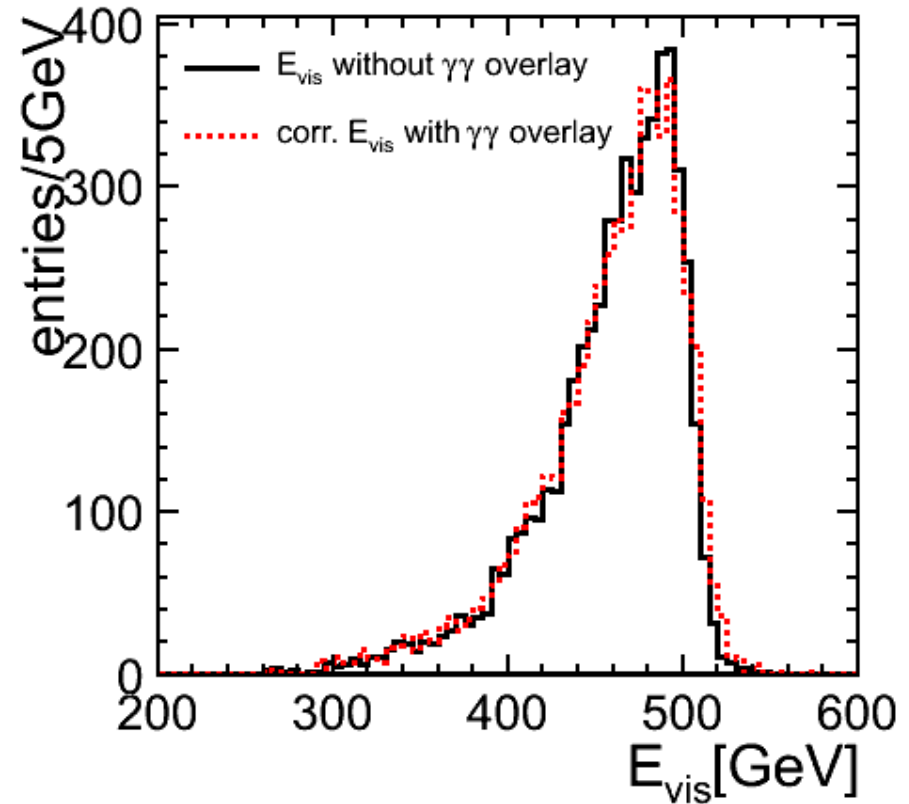
- overlaid $\gamma\gamma \rightarrow \text{hadron}$ events per interaction: $\langle N_{\gamma\gamma} \rangle = 1.7$
- exclusive jet clustering to remove beam background:
 k_T 1.3, ExclusiveNJets 6



effect of $\gamma\gamma$ overlay

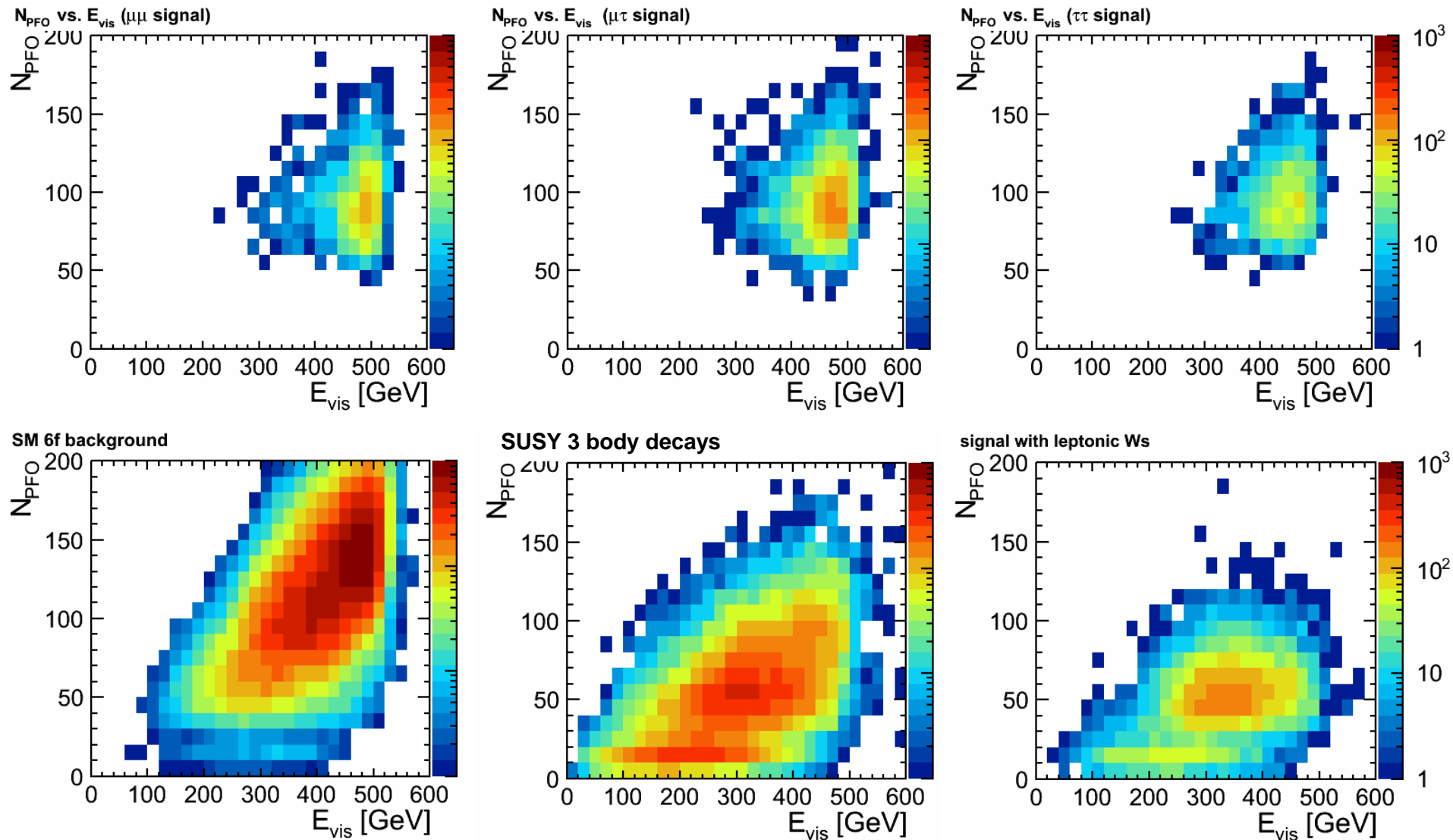


correction for $\gamma\gamma$ overlay



→ all following steps based on reconstructed particles in these 6 jets

Preselection (signal channels and background)



Preselection

select only events with high multiplicity and small missing energy:

- reduce leptonic W contribution
- reduce SM 6f background

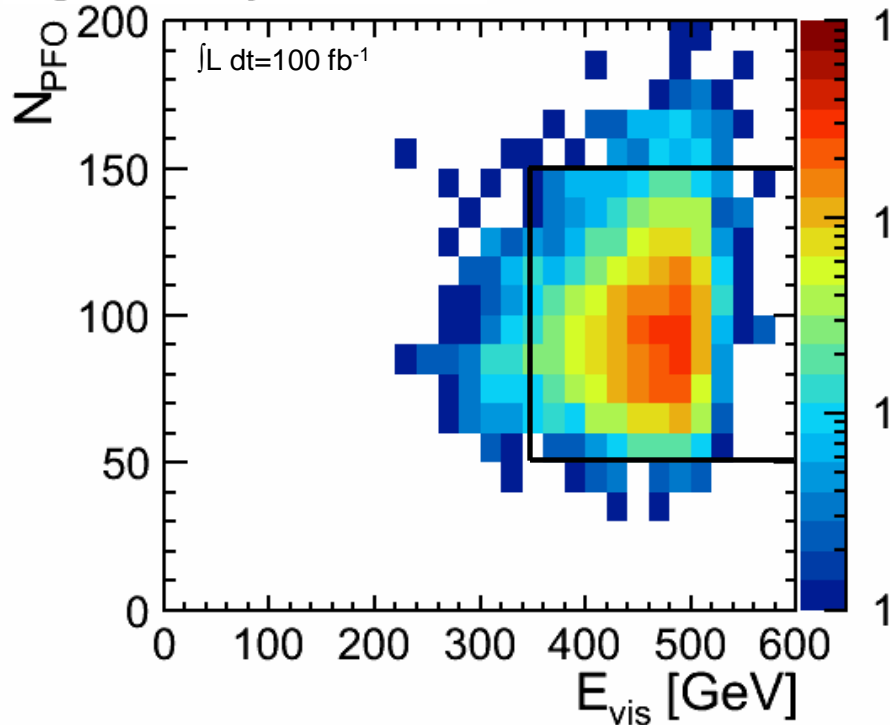
→ $E_{\text{vis}} > 350\text{GeV}$

→ $N_{\text{PFO}} > 50$

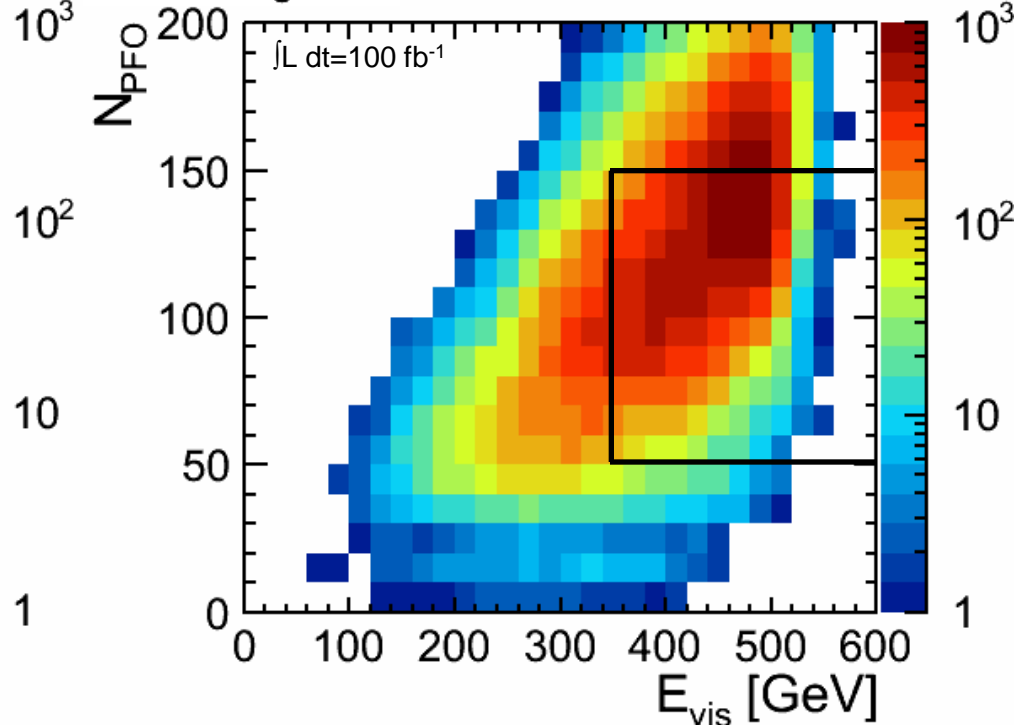
→ $N_{\text{PFO}} < 150$

$IW_{\text{had}}IW_{\text{had}}$

signal with fully hadronic Ws



SM 6f background

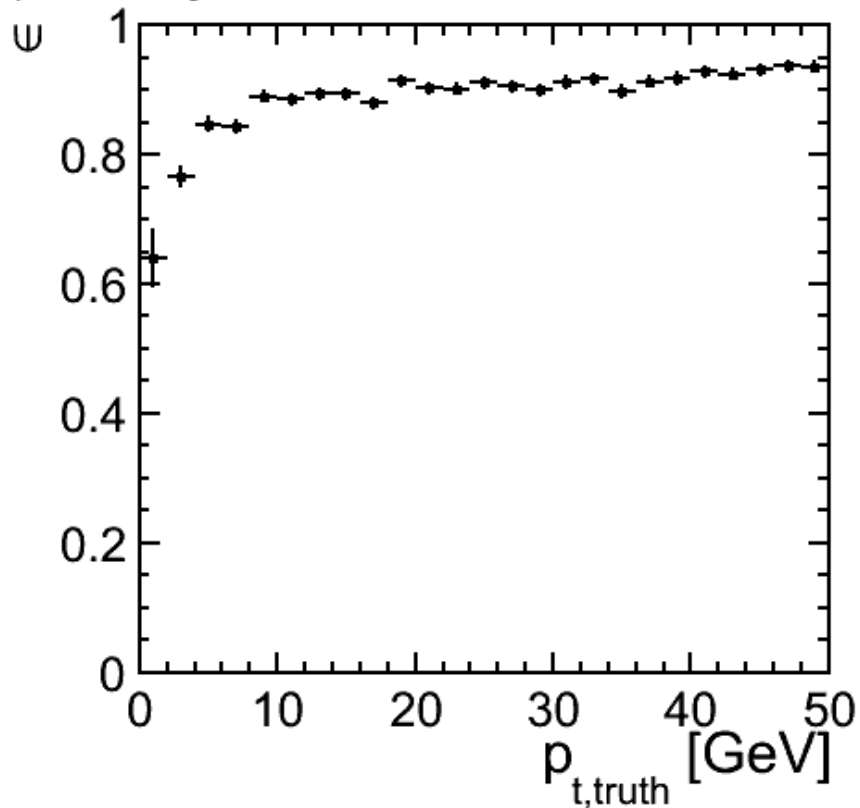


Muon reconstruction ($\mu\mu$ channel)

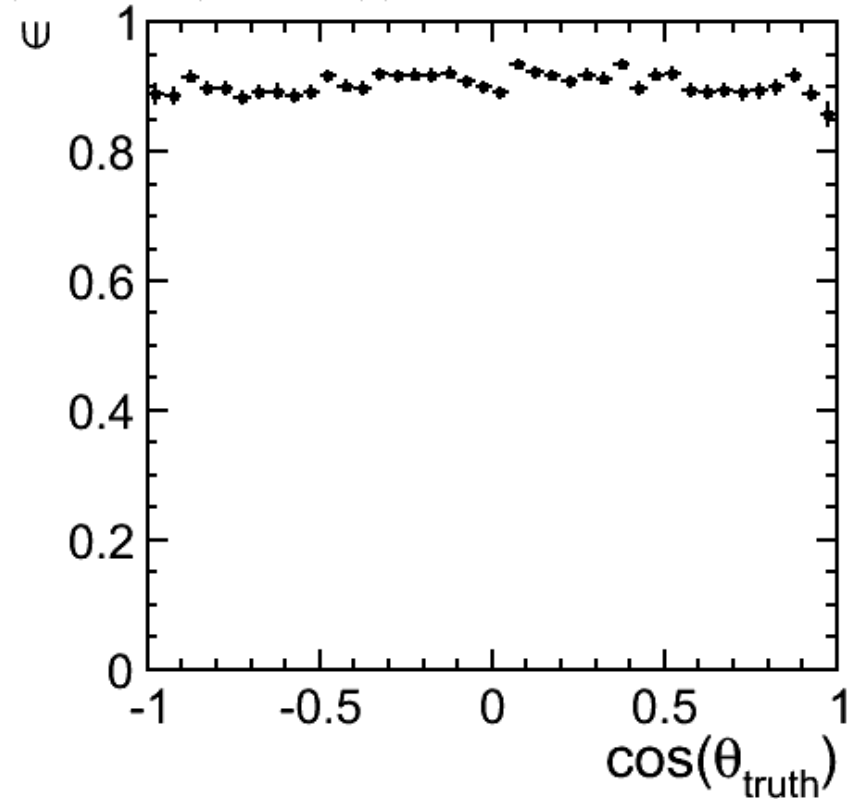
selection:

- Pandora PFO muons
- no isolation required \rightarrow depends on neutralino mass
- keep two most energetic muons as signal muons

μ efficiency vs. momentum



μ efficiency vs. $\cos(\theta)$



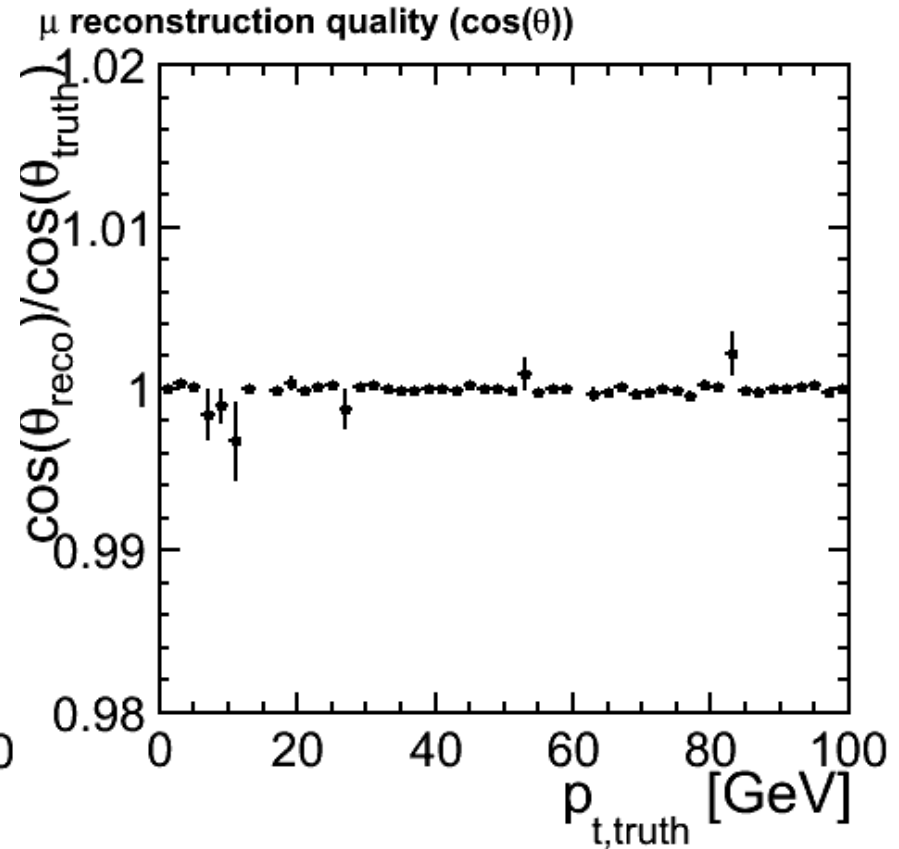
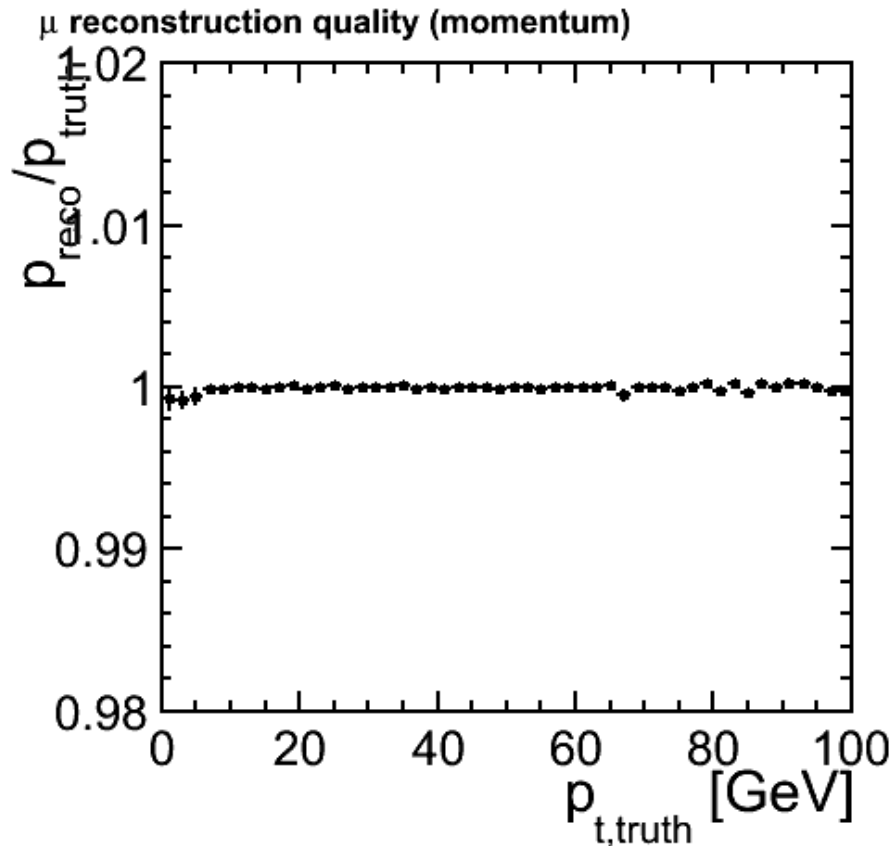
\rightarrow overall efficiency of signal muon: 91%



Muon reconstruction ($\mu\mu$ channel)

selection:

- Pandora PFO muons
- no isolation required \rightarrow depends on neutralino mass
- keep two most energetic muons as signal muons



\rightarrow almost perfect reconstruction of muons



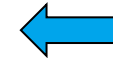
Full event reconstruction ($\mu\mu$ channel)

combine into two equal mass objects

2 μ

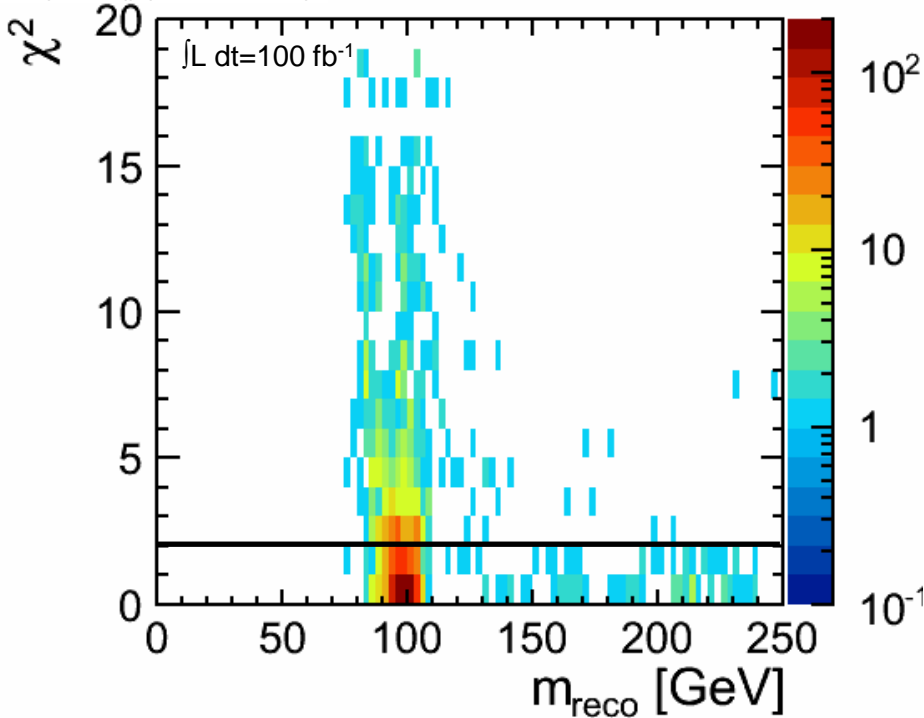


$$\chi_{\text{eqm}}^2 = \frac{(m_{p1} - m_{p2})^2}{(5\text{GeV})^2}$$

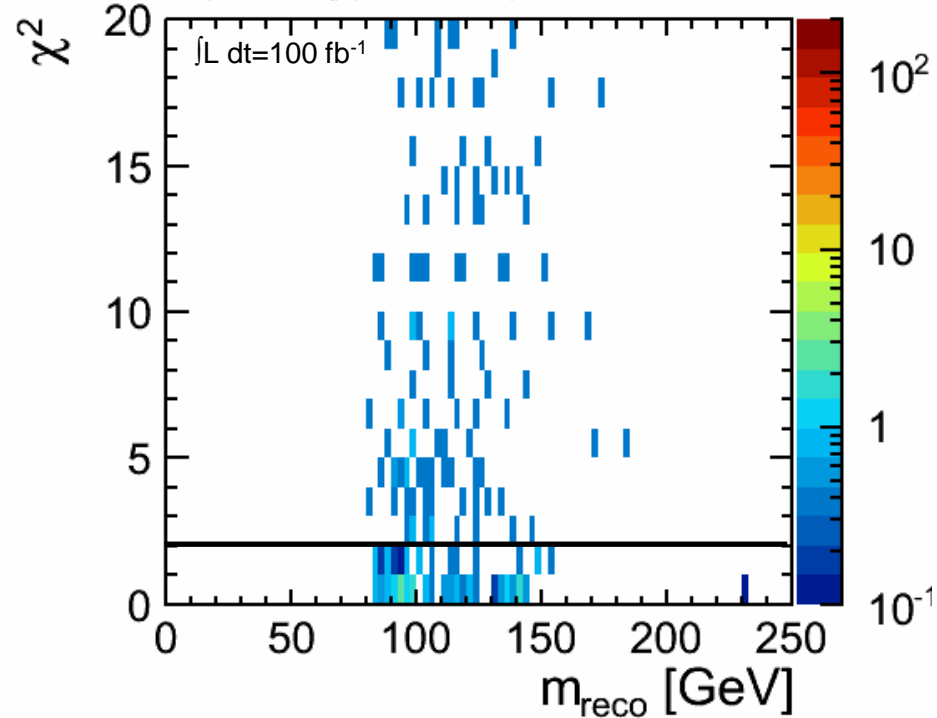


2 W

signal ($\mu\mu$ channel)



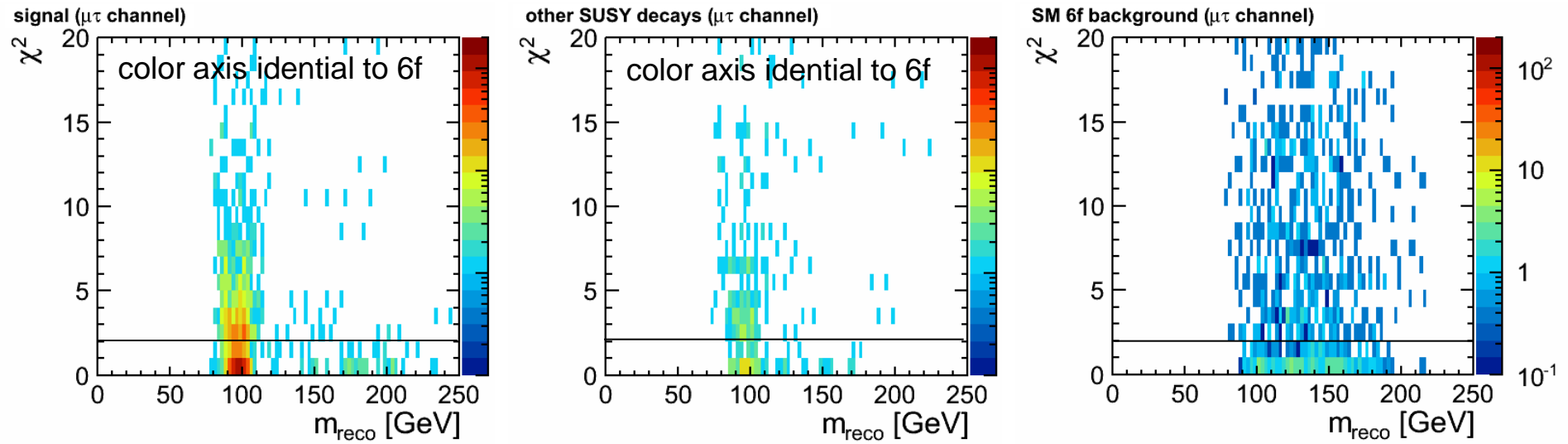
SM 6f background ($\mu\mu$ channel)



$\rightarrow \chi_{\text{eqm}}^2 < 2$



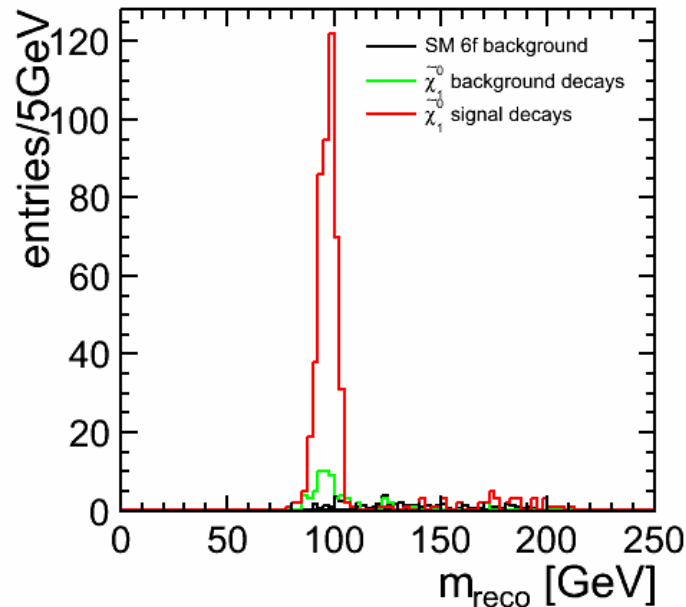
Full event reconstruction ($W\mu W\tau$ channel)



$$\chi_W^2 < 2$$

$$\chi_{eqm}^2 < 2$$

reconstructed mass in $W\mu W\tau$ channel

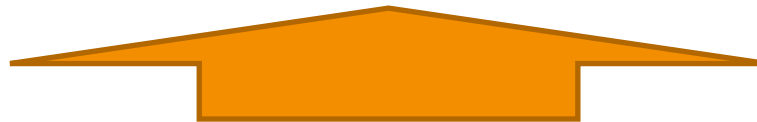


$$A = BR_{\chi \rightarrow W\mu}$$

$$B = BR_{\chi \rightarrow W\tau}$$

How many event would we expect to end up in each event class?

		true $\mu W\mu W$	true $\mu W\tau W$	true $\tau W\tau W$	
N($\mu\mu$ channel)	$W_{\text{had}}^2 \mathcal{E}_W^2$	$A^2 \mathcal{E}_\mu^2$	$2AB\tau_\mu \mathcal{E}_\mu^2$	$B^2 \tau_\mu^2 \mathcal{E}_\mu^2$	$\sigma \cdot \int L dt$
N($\mu\tau$ channel)		0	$2AB\tau_{\text{had}} \mathcal{E}_\mu \mathcal{E}_\tau$	$B^2 \tau_\mu \tau_{\text{had}} \mathcal{E}_\mu \mathcal{E}_\tau$	
N($\tau\tau$ channel)		0	0	$B^2 \tau_{\text{had}}^2 \mathcal{E}_\tau^2$	



assumptions for efficiencies and errors

use e.g. **N($\mu\mu$ channel)** and **N($\mu\tau$ channel)**
to estimate the statistical and systematical error on

$$\frac{A}{B} = \tan^2 \theta_{23}$$



Precision estimation

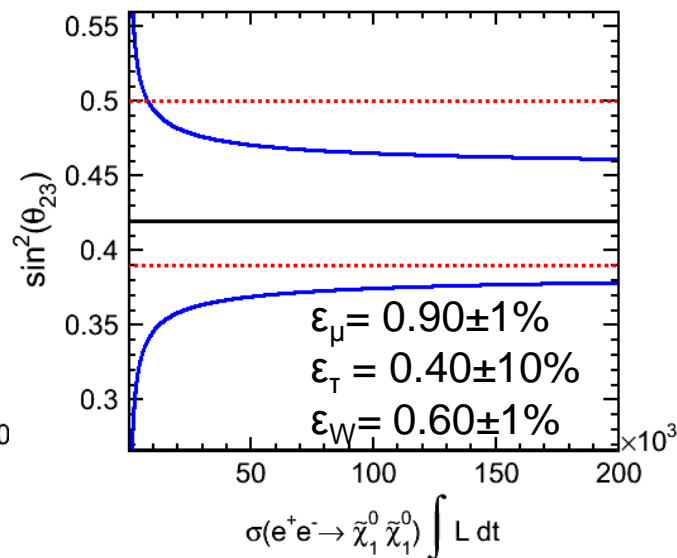
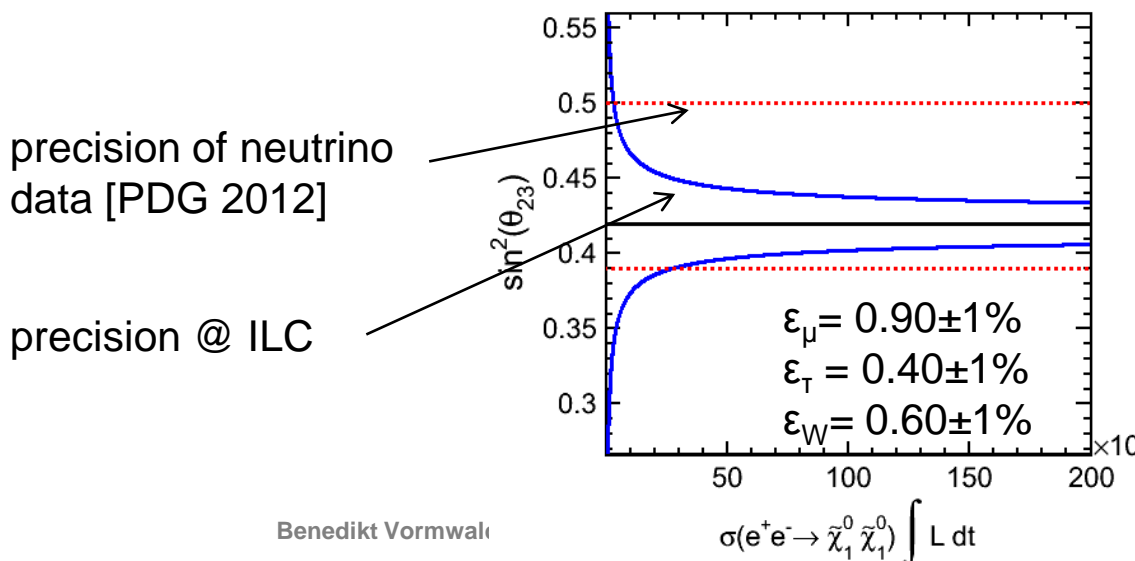
$$A = BR_{\chi \rightarrow W\mu}$$

$$B = BR_{\chi \rightarrow W\tau}$$

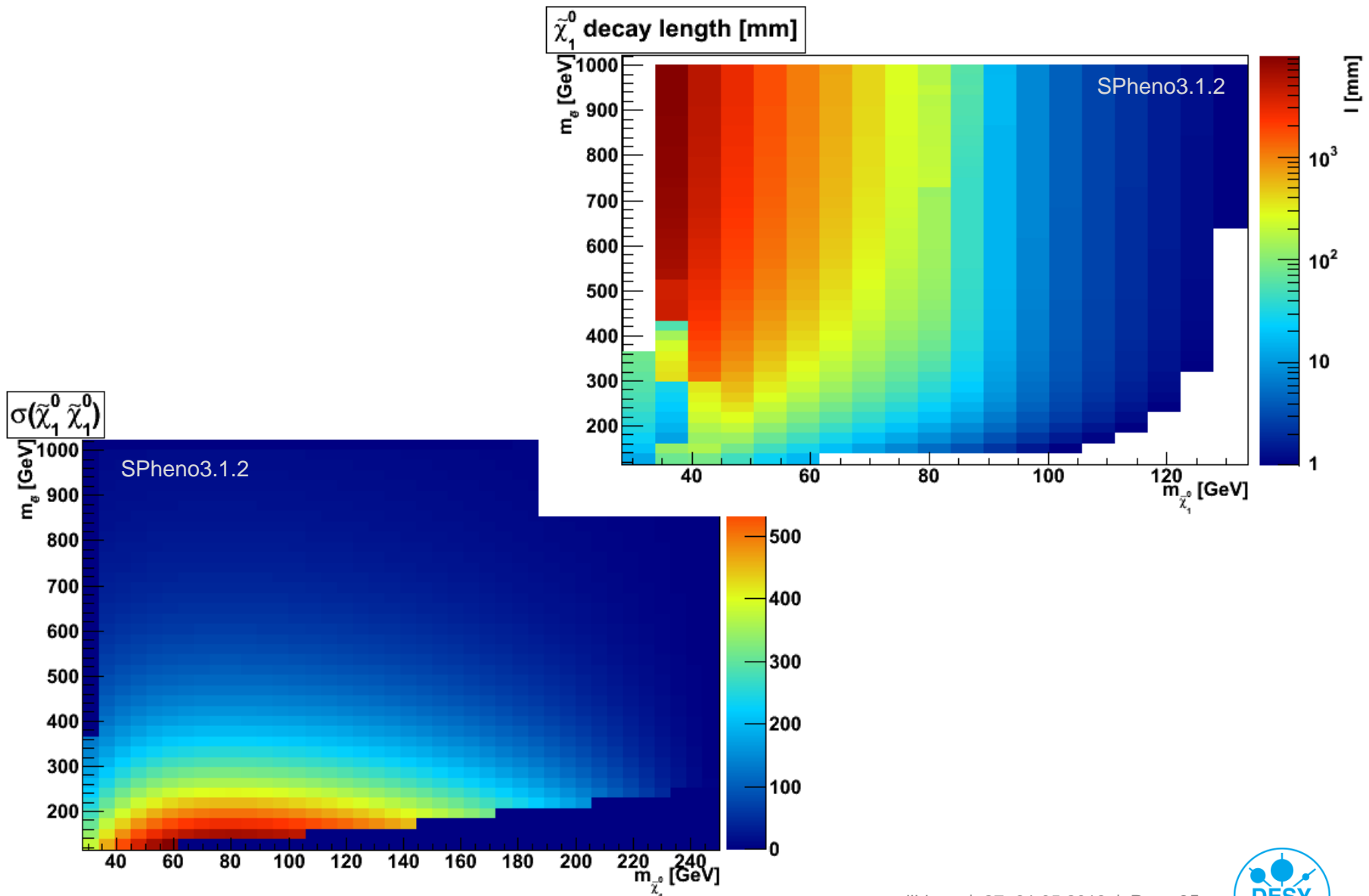
How many event would we expect to end up in each event class?

	true $\mu W\mu W$	true $\mu W\tau W$	true $\tau W\tau W$	
N($\mu\mu$ channel)	$A^2 \varepsilon_\mu^2$	$2AB\tau_\mu \varepsilon_\mu^2$	$B^2 \tau_\mu^2 \varepsilon_\mu^2$) $\sigma \cdot \int L dt$
N($\mu\tau$ channel) $W_{\text{had}}^2 \varepsilon_W^2$	0	$2AB\tau_{\text{had}} \varepsilon_\mu \varepsilon_\tau$	$B^2 \tau_\mu \tau_{\text{had}} \varepsilon_\mu \varepsilon_\tau$	
N($\tau\tau$ channel)	0	0	$B^2 \tau_{\text{had}}^2 \varepsilon_\tau^2$	

Translate into precision of neutrino mixing angle determination



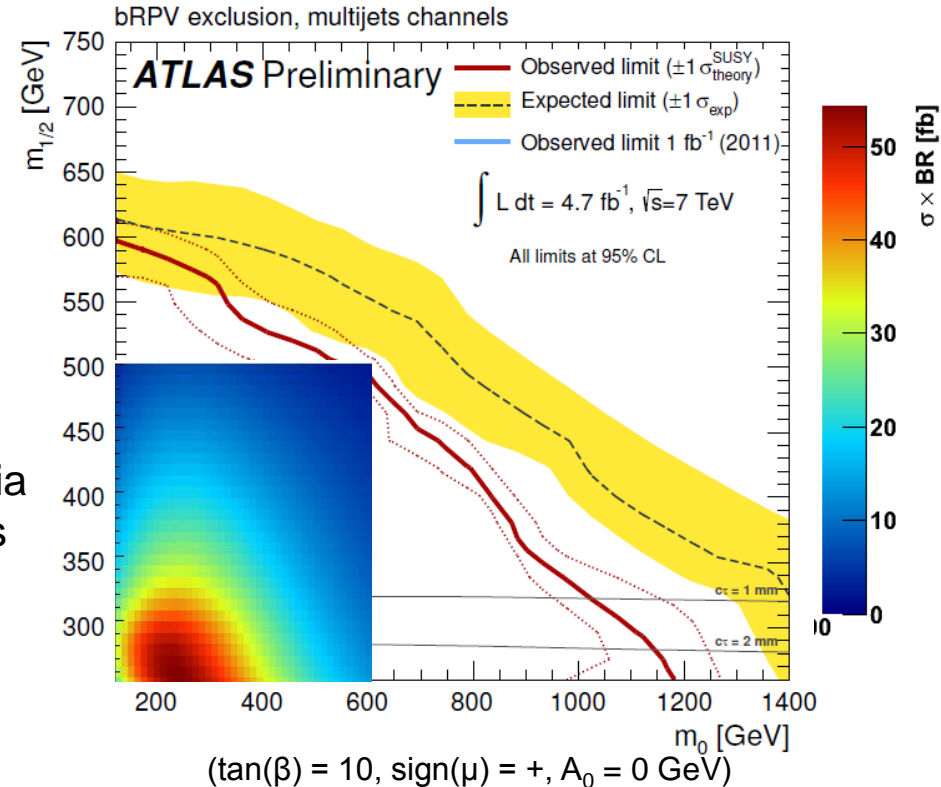
Bilinear R-parity violation



Situation at LHC

One dedicated bRPV mSUGRA search from ATLAS (**ATLAS-CONF-2012-140**):

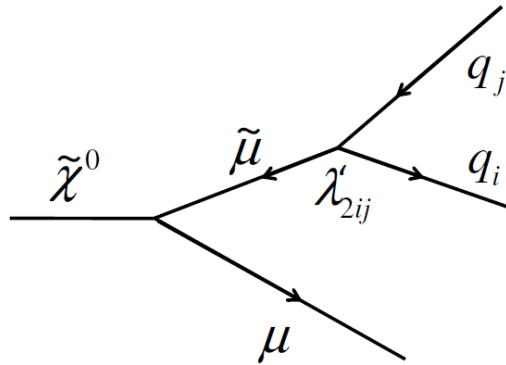
- large jet multiplicity
- 1 isolated lepton
- missing transverse momentum
- bRPV parameters fitted to neutrino data
- bRPV mSUGRA tested for $m_{1/2} > 240\text{GeV}$
- ($\rightarrow c\tau < 15\text{ mm}$)
- analysis probes colored sector of theory via squark production and subsequent decays
- coupling of EW sector and colored sector



Situation at the ILC

- direct neutralino production \rightarrow direct access to EW sector
- need better parametrization than mSUGRA to study phenomenology of this model, especially decouple EW sector from colored one \rightarrow generic model

Dedicated displaced vertex search ($\int Ldt = 33 \text{ pb}^{-1}$)



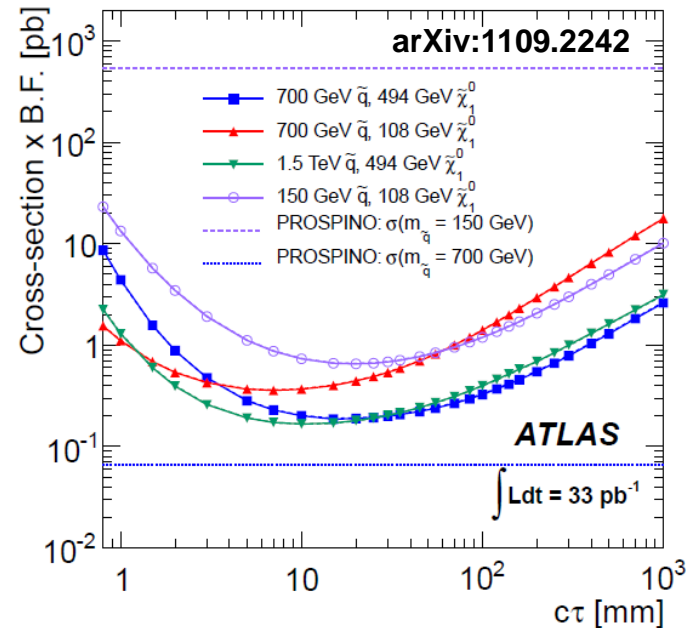
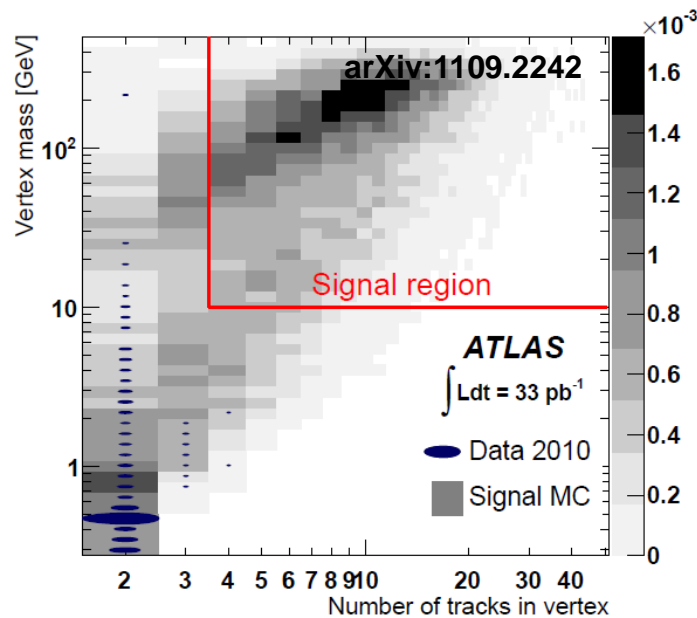
search for:

- $|z_{DV}| < 300\text{mm}$, $4\text{mm} < r_{DV} < 180\text{mm}$
- 1 high- p_t muon

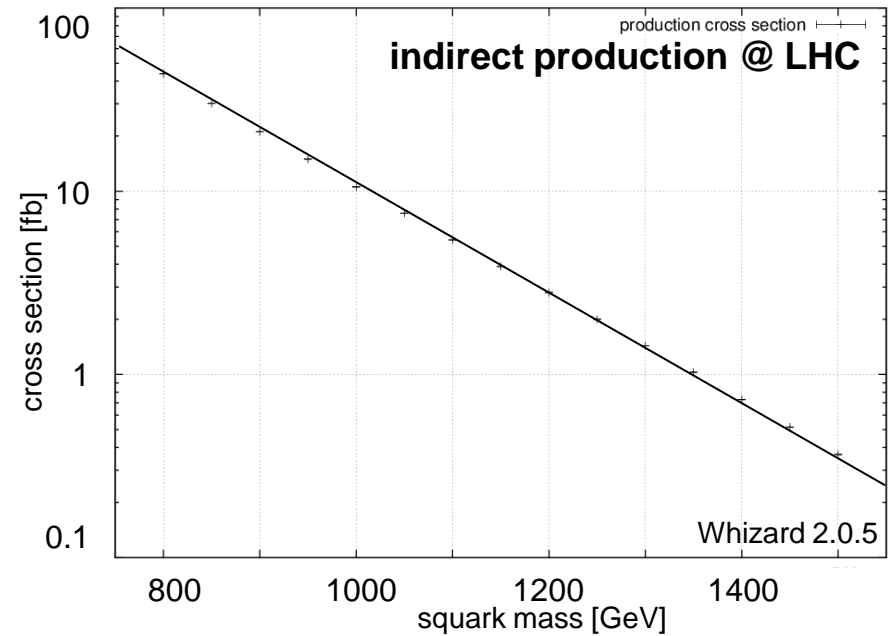
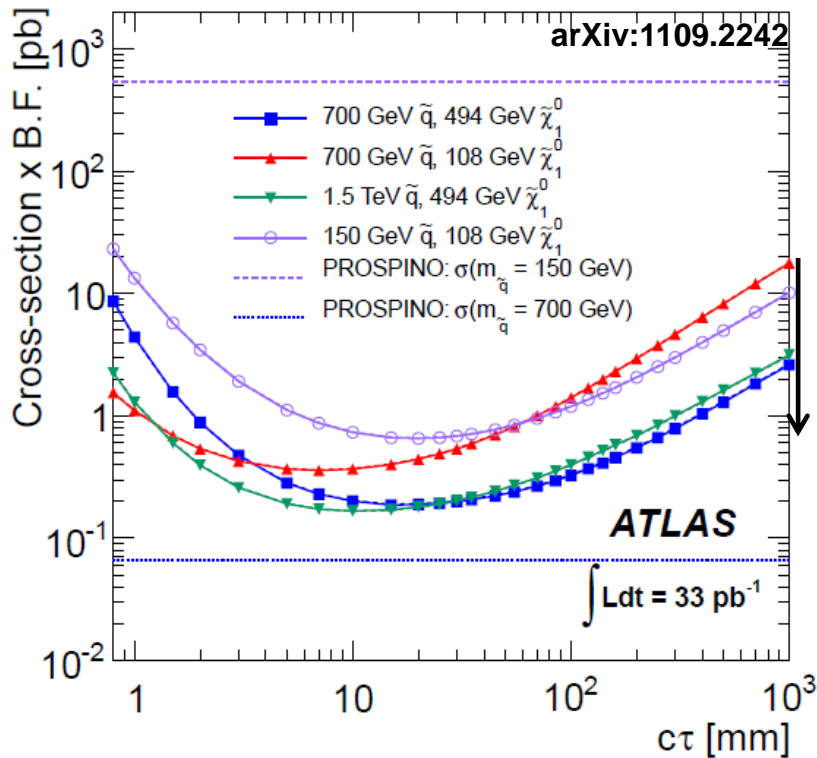
background free analysis ($N_{BG} < 0.03$)

assumption:

di-squark production \rightarrow direct decay to LSP



Dedicated displaced vertex search



extrapolation: $33 \text{ pb}^{-1} \rightarrow 5 \text{ fb}^{-1}$
 \rightarrow limits drop by a factor of $\sim \sqrt{200} (=14)$

- consider ILC-friendly case \rightarrow light neutralino (red curve)
- even with higher statistics LHC sensitive to $c\tau = [1 \text{ mm}; 12 \text{ mm}]$ for $m_{\text{squark}} = 700 \text{ GeV}$
- not sensitive in case of high squark masses and large $c\tau$

