

Hit finding and pad response function for the LCTPC using resistive Micromegas

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On behalf of the LCTPC collaboration





Outline

- **Intro: LCTPC Collaboration and MPGD**
- **Charge dispersion and Signal Pulse**
 - **Electronic response**
 - **Definition of amplitude and time (A_i, t_i) for a pad**
 - **Conceptual Pad Response Function (PRF)**
- **Determination of PRF parameters (calibration)**
 - **Parameterization of the PRF**
- **Results**
 - **Field distortions**
 - **Transverse resolution**
- **Summary**

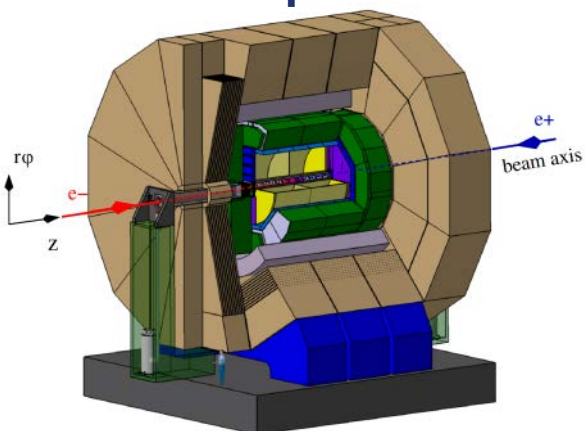


Time Projection Chamber (TPC) for ILD

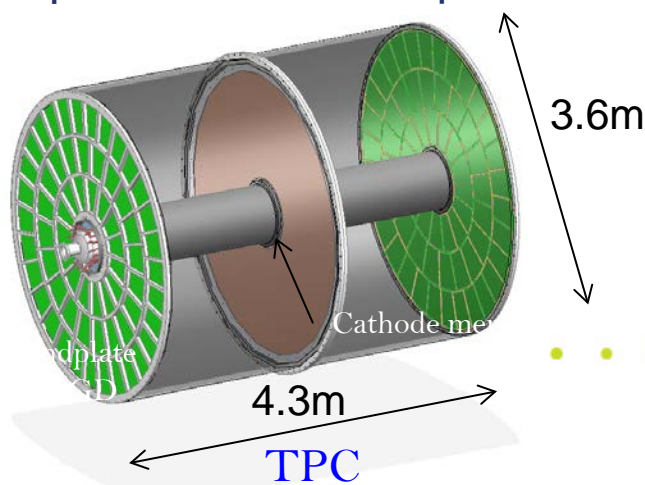
TPC is the central tracker for International Linear Detector

- Large number of 3D points → continuous tracking
- Good track separation and pattern recognition
- Low material budget inside the calorimeters (*c.f.* PFA)
 - Barrel: $\sim 5\% X_0$
 - Endplates: $\sim 25\% X_0$
- Two options for endplate readout:
 - **GEM**: $1.2 \times 5.8 \text{ mm}^2$ pads
 - **Resistive Micromegas**: $3 \times 7 \text{ mm}^2$ pads
- Alternative: **pixel** readout with pixel size $\sim 55 \times 55 \mu\text{m}^2$

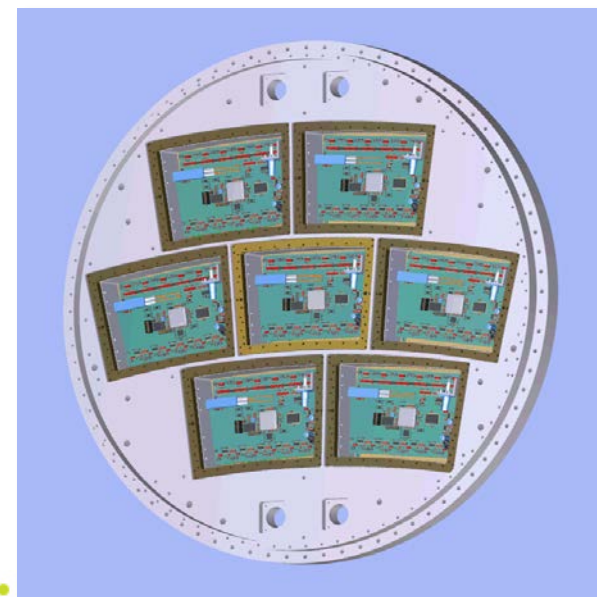
- TPC Requirements :**
- **Momentum resolution:**
 $\delta(1/p_T) < 9 \times 10^{-5} \text{ GeV}^{-1}$
 - **Single hit resolution 3.5T:**
 $\sigma(r\phi) < 100 \mu\text{m}$
 $\sigma(z) < 500 \mu\text{m}$
 - **Tracking eff.** for $p_T > 1 \text{ GeV}$:
97%
 - **dE/dx resolution** $\sim 5\%$



ILD



TPC



Large Prototype



Micro Pattern Gas Detector (MPGD)

Technology choice for TPC readout: Micro Pattern Gas Detector

- more robust than wires
- fast signal & high gain
- better ageing properties
- no $E \times B$ effect
- low ion backdrift
- easier to manufacture

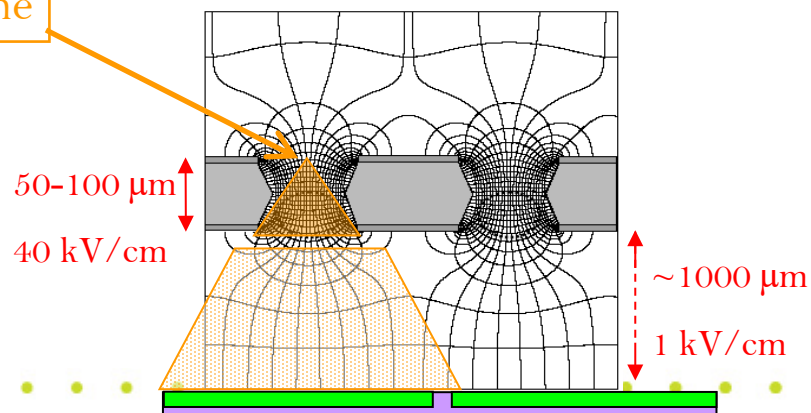
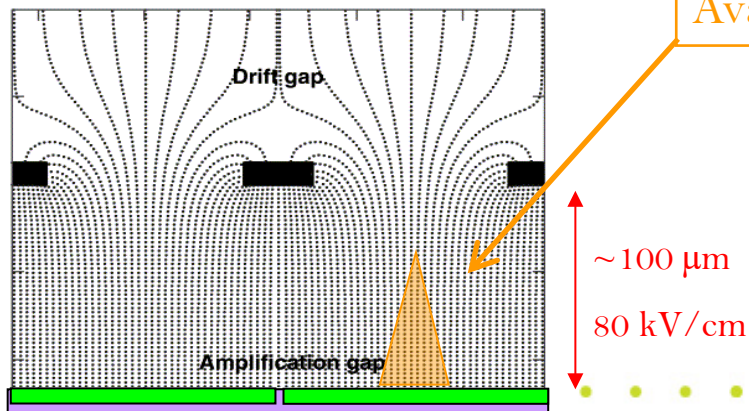
Micromegas (MM)

- MICROMesh Gaseous Structure
- metallic micromesh (typical pitch $50\mu\text{m}$)
- supported by $50\mu\text{m}$ pillars, multiplication between anode and mesh, high gain

GEM

- Gas Electron Multiplier
- 2 copper foils separated by kapton
- multiplication takes place in holes, with 2-3 layers needed

Avalanche

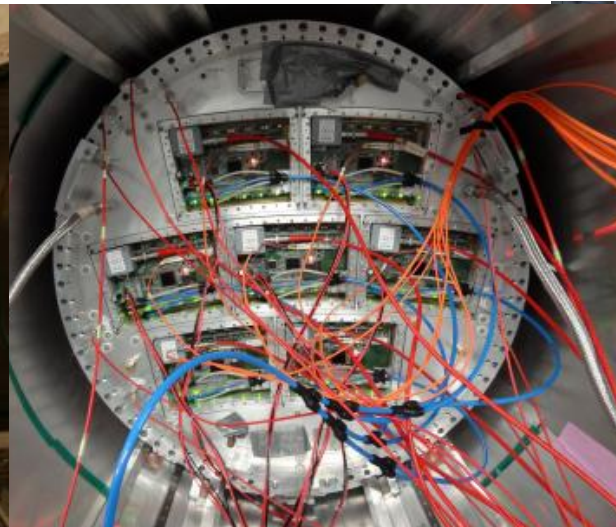


MPGD readout modules under studied

Readout		Pad Size	Electronics	Groups
MPGDs	Double GEMs (Laser-etched)	(~ 1 × 6 mm ² Pad)	ALTRO	Asia
	Triple GEMs (wet-etched)			DESY
	Micromegas (Resistive anode)	(~ 3 × 7 mm ² Pad)	AFTER	Saclay-Carleton



Large Prototype TPC



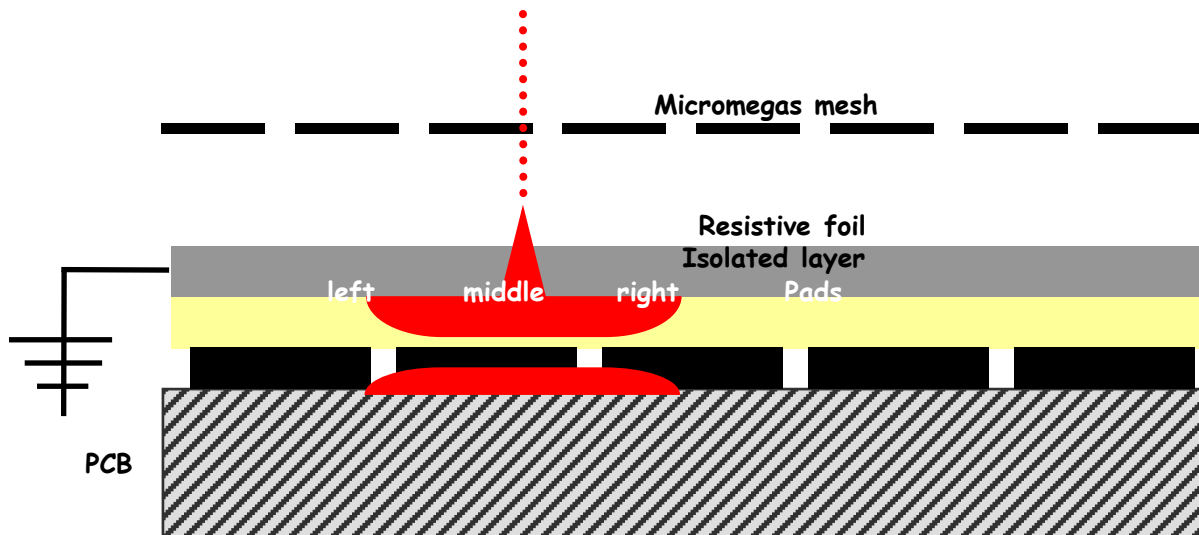
Endplate + 7 Micromegas modules



1T PC Magnet

Charge Dispersion

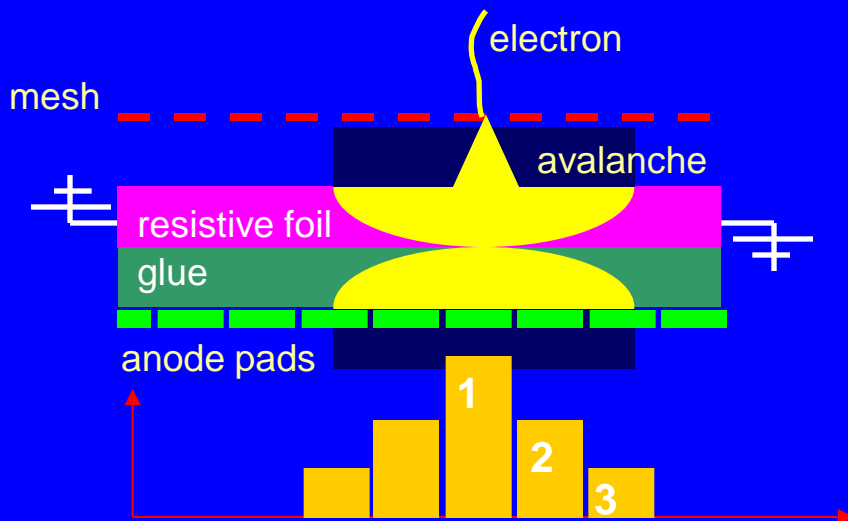
Resistive Anode



Charge dispersion

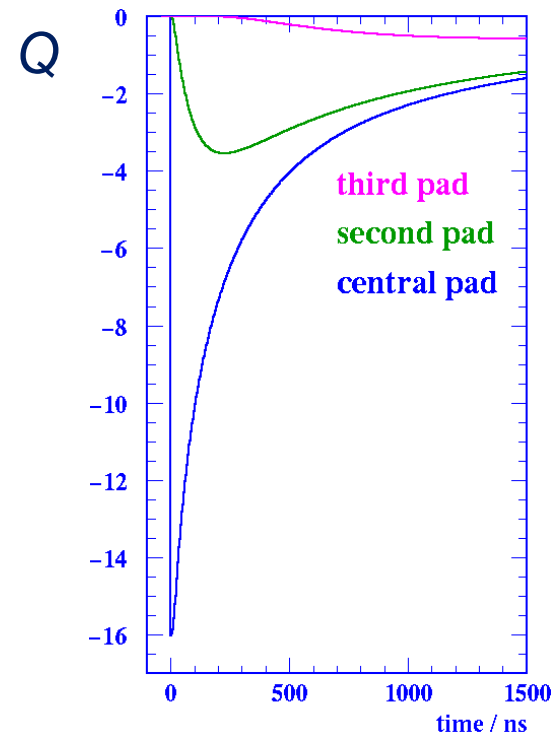
- A high resistivity film bonded to a readout plane with an insulating spacer
- 2D continuous RC network defined by material properties and geometry.
- point charge at $r = 0$ & $t = 0$ disperses with time.

Micromegas + resistive anode



$$\frac{\partial \rho}{\partial t} = \frac{1}{RC} \left[\frac{\partial^2 \rho}{\partial r^2} + \frac{1}{r} \frac{\partial \rho}{\partial r} \right]$$

$$\Rightarrow \rho(r, t) = \frac{RC}{2t} e^{-\frac{r^2 RC}{4t}}$$





Transverse diffusion

Pulse shape origin

$$T(x) = \frac{1}{\sigma_x \sqrt{2\pi}} \exp\left(\frac{-x^2}{2\sigma_x^2}\right)$$

Longitudinal diffusion

$$L(t) = \frac{1}{\sigma_t \sqrt{2\pi}} \exp\left(\frac{-t^2}{2\sigma_t^2}\right)$$

Induction gap

$$R(t) = \begin{cases} \frac{t}{T_{rise}} & 0 < t < T_{rise} \\ = 1 & t > T_{rise} \\ = 0 & t < 0 \end{cases}$$

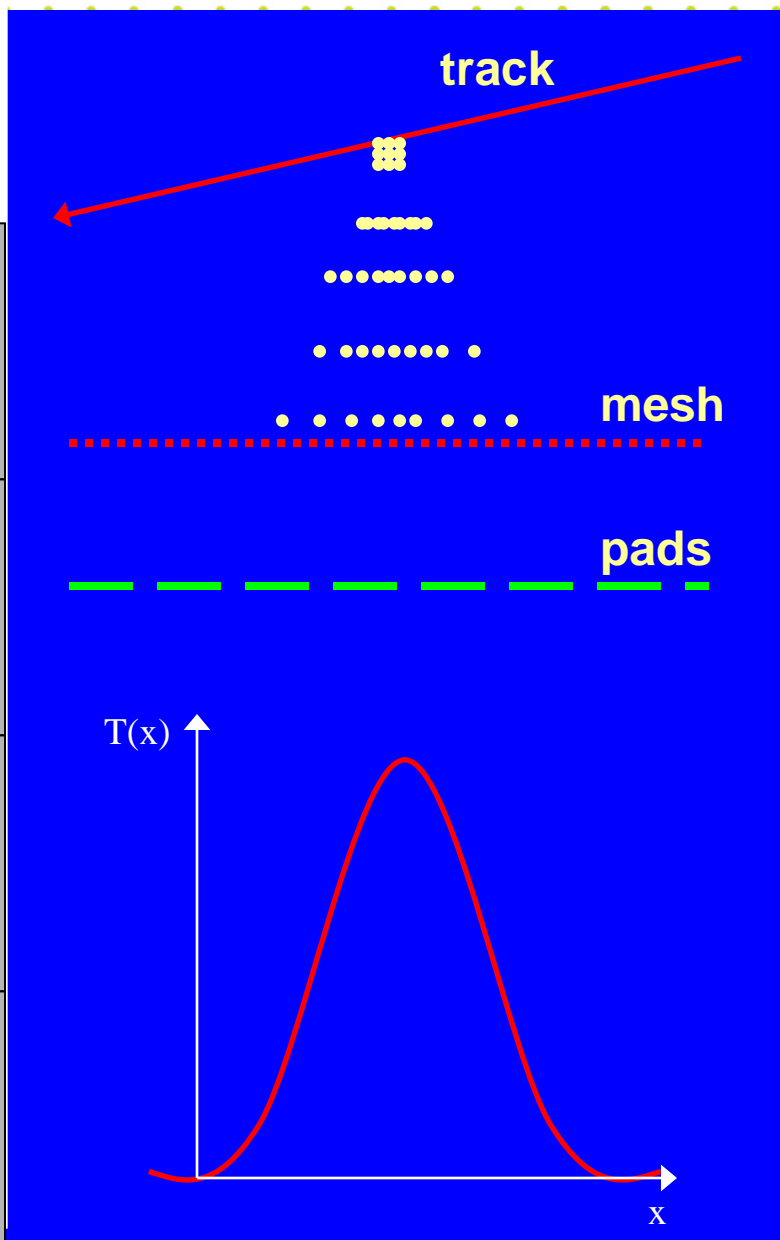
Preamplifier Response

$$H(t) = \begin{cases} \exp\left(-\frac{t}{t_f}\right) \left(1 - \exp\left(-\frac{t}{t_r}\right)\right) & t > 0 \\ = 0 & t < 0 \end{cases}$$

Resistive foil + glue

$$\rho(x, y, t) = \left(\frac{1}{\sigma_t \sqrt{\pi th}}\right)^2 \exp\left(\frac{-(x^2 + y^2)}{4th}\right)$$

$$h = 1/RC$$





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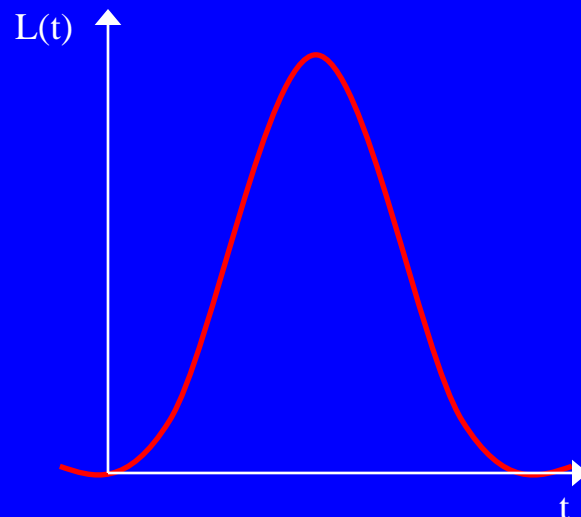
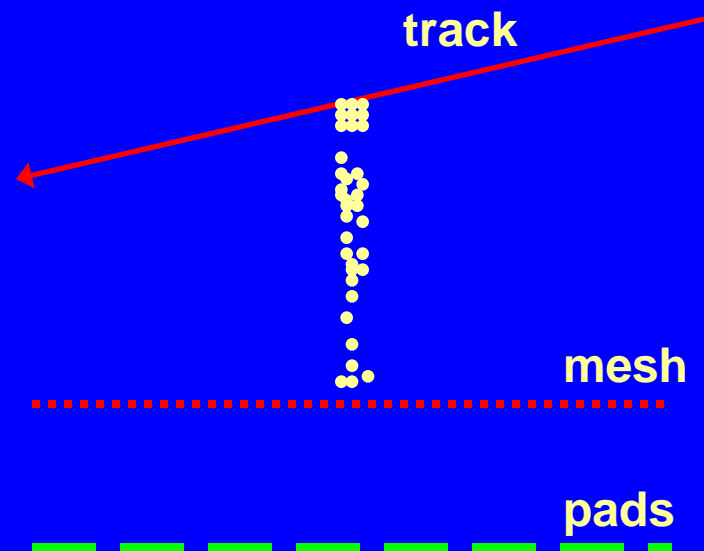
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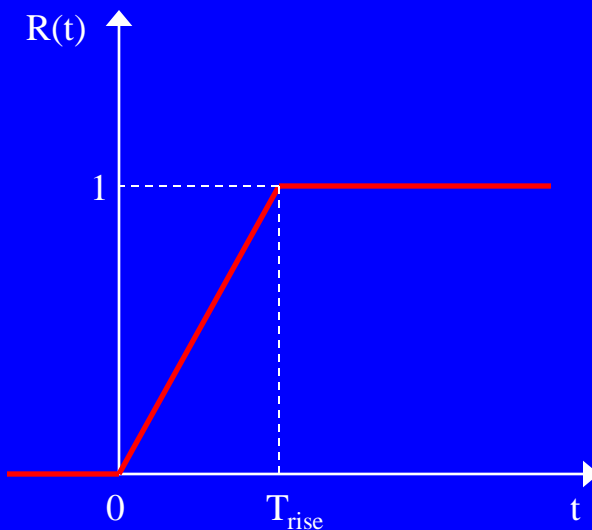
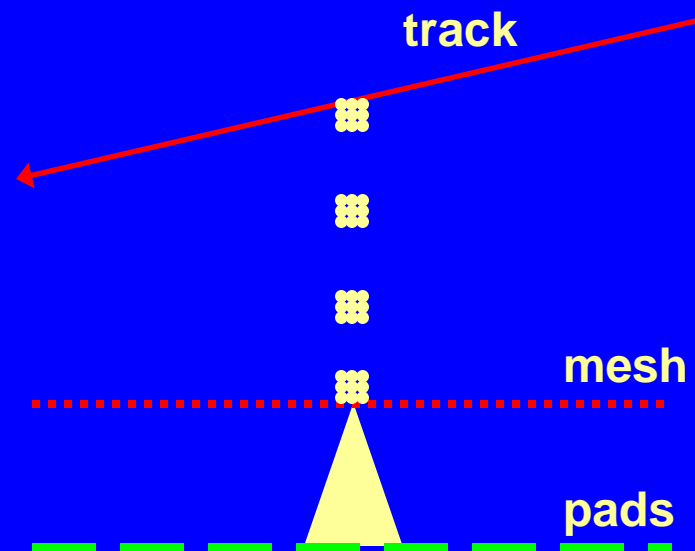
Preamplifier Response

$$A(t) = \begin{cases} \exp\left(-\frac{t}{t_f}\right) \left(1 - \exp\left(-\frac{t}{t_r}\right)\right) & t > 0 \\ 0 & t < 0 \end{cases}$$

Resistive foil + glue

$$\rho(x, y, t) = \left(\frac{1}{\sigma_t \sqrt{\pi t h}}\right)^2 \exp\left(\frac{-(x^2 + y^2)}{4th}\right)$$

$$h = 1/RC$$





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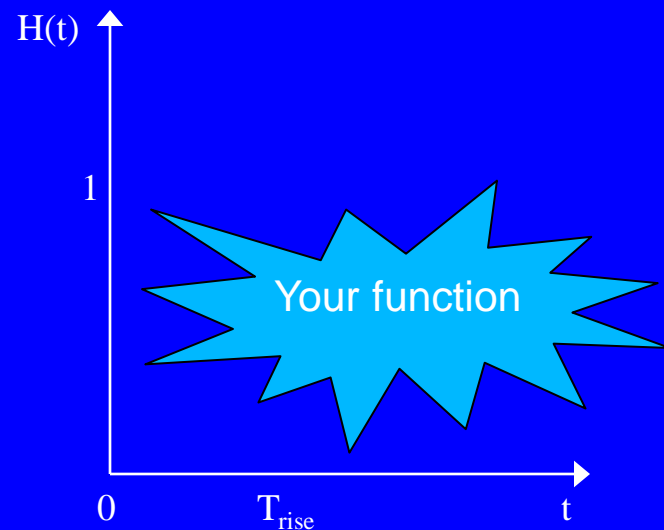
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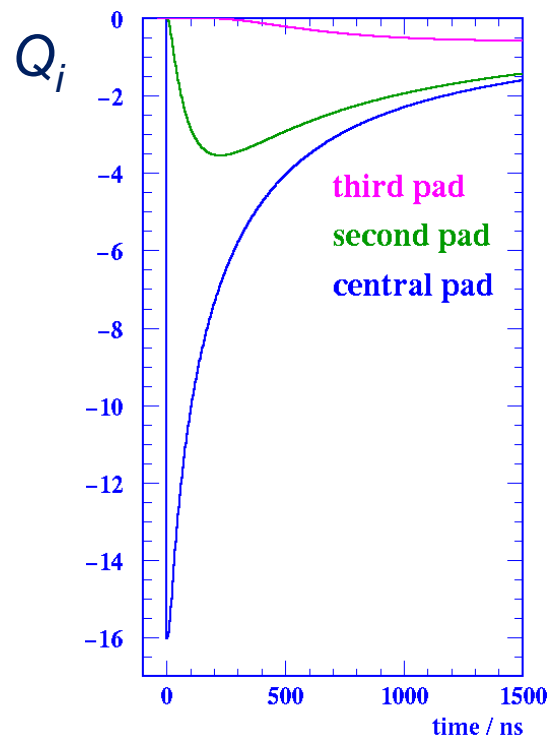
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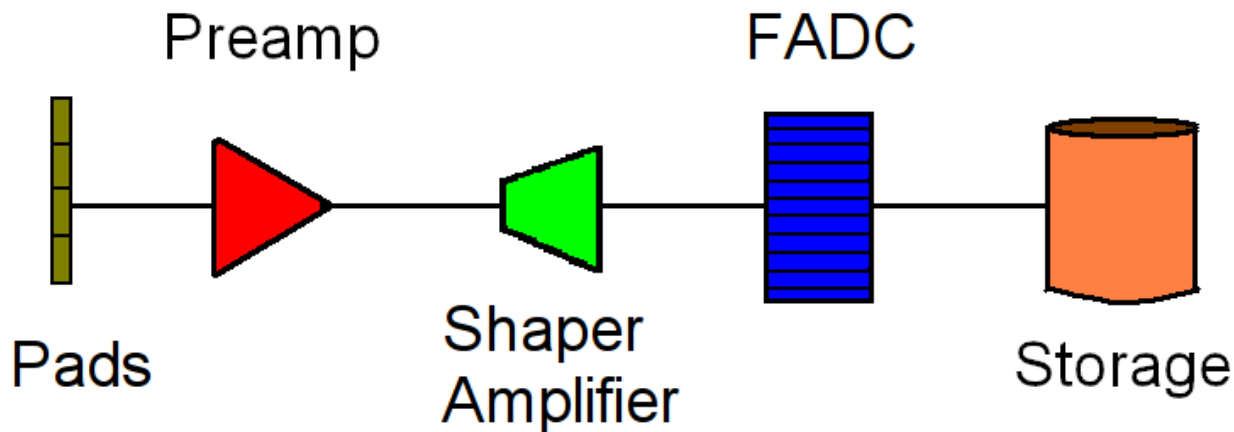
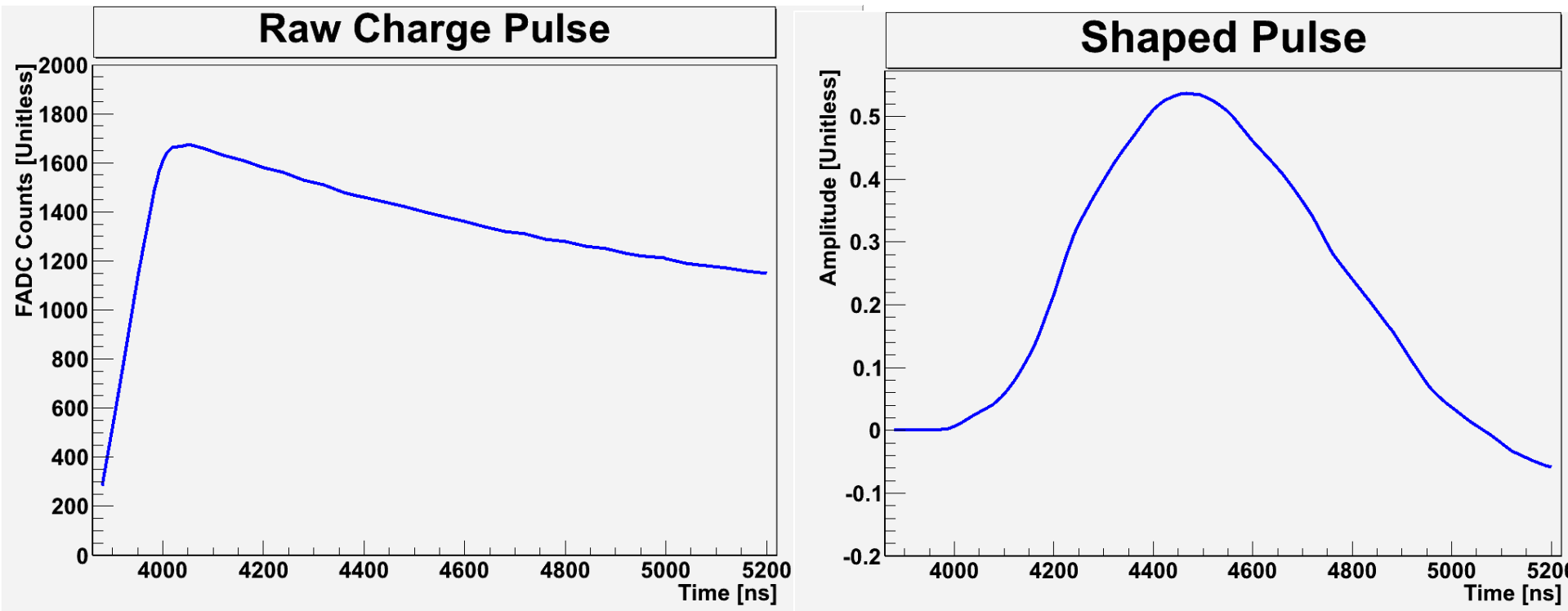
$$h = 1/RC$$

$$Q_i = \int \rho_i(r) dr$$

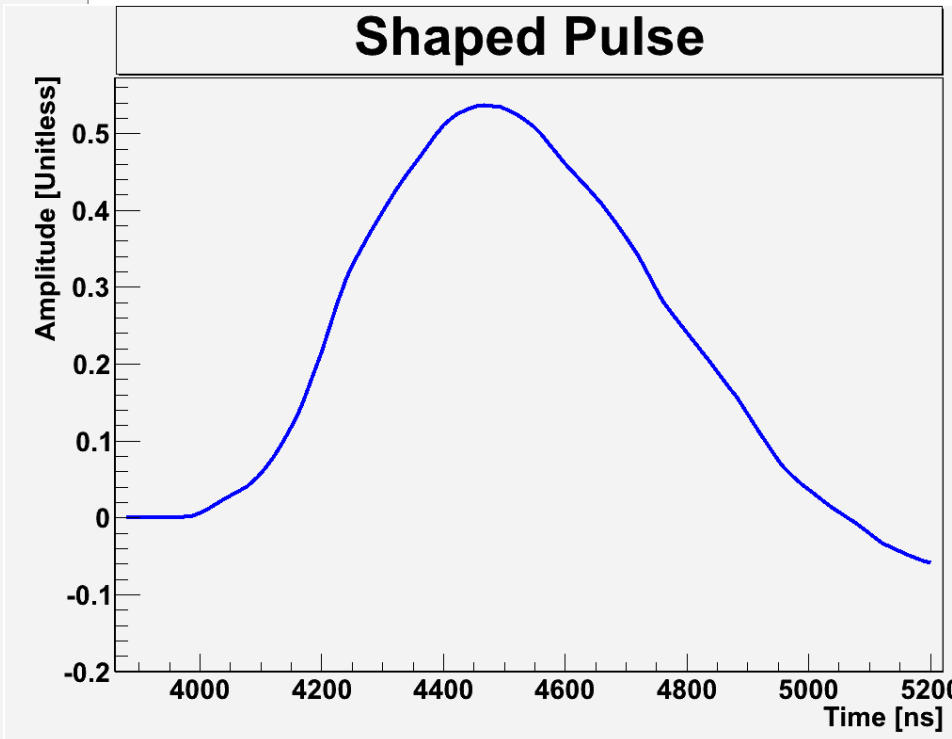
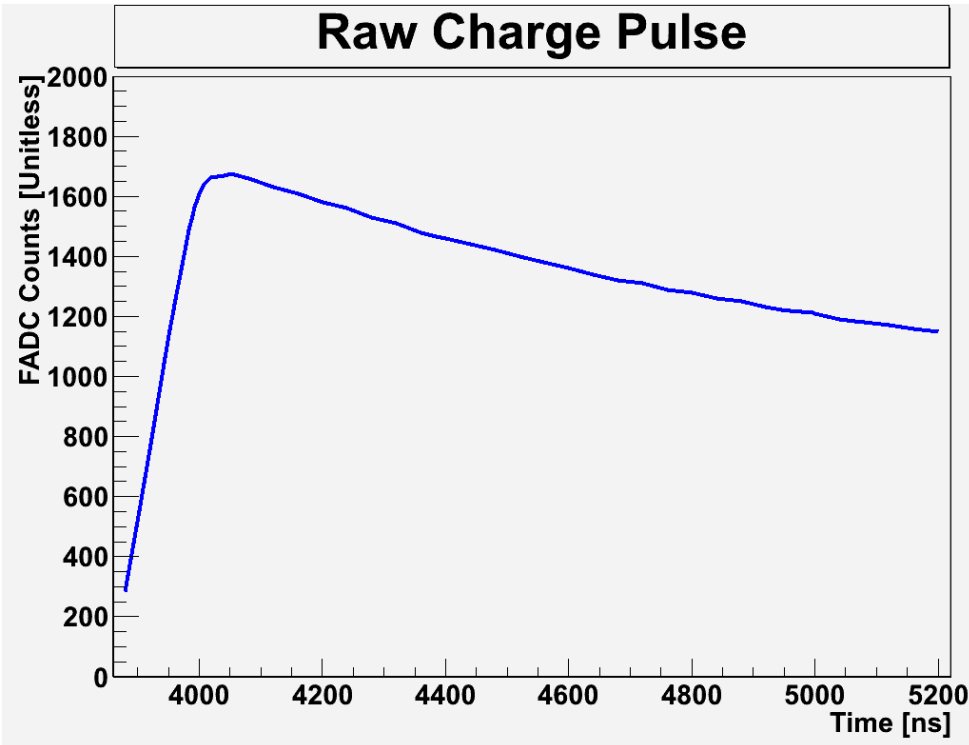
Stand alone simulation



Raw Charge Shape versus Shaped Pulse



Raw Charge Shape versus Shaped Pulse

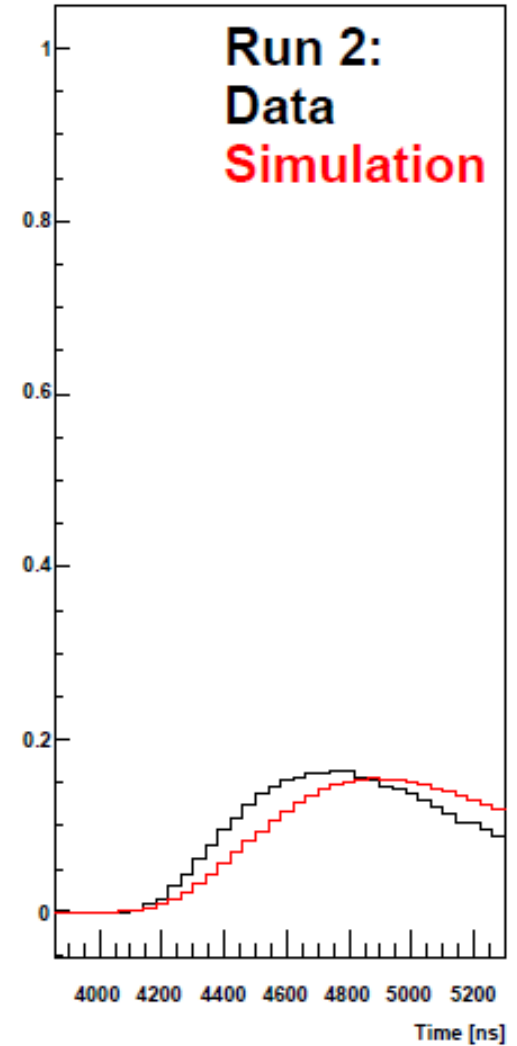
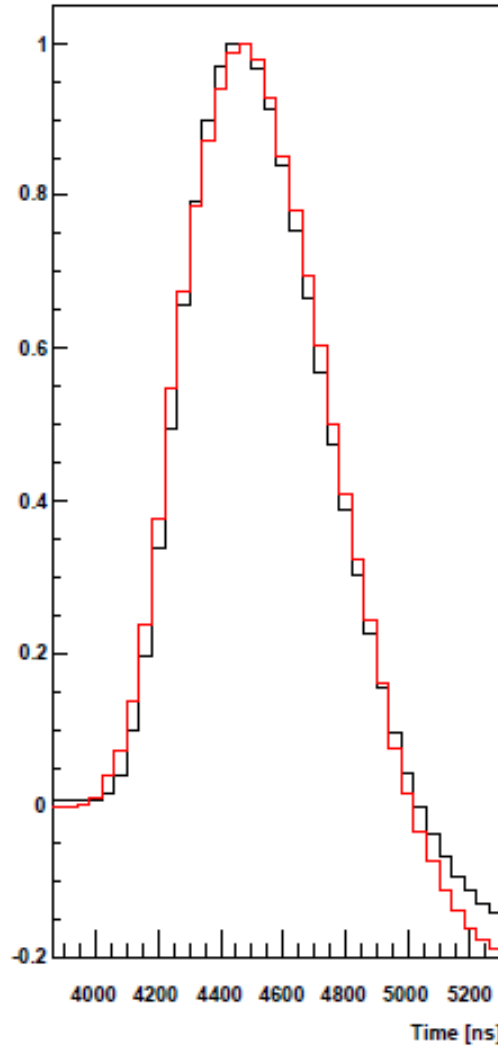
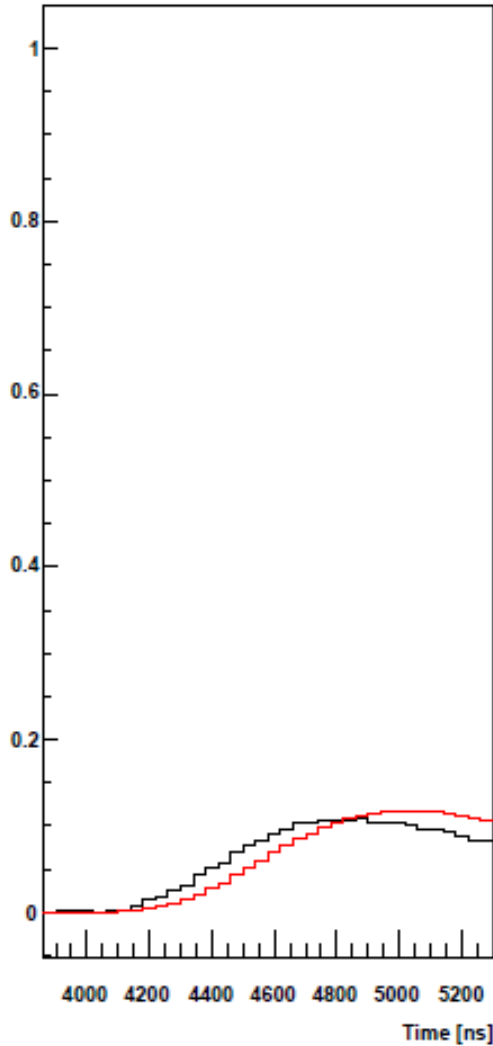


$$H(t) = A_0 \left(\frac{t}{\tau} \right)^3 \sin\left(\frac{t}{b\tau} \right) \exp\left(-\frac{t}{\tau} \right)$$

from Eric Delagnes et al at Saclay



Stand-Alone Calculation



CRUCIAL TO CHARACTERIZE DETECTOR PARAMETERS

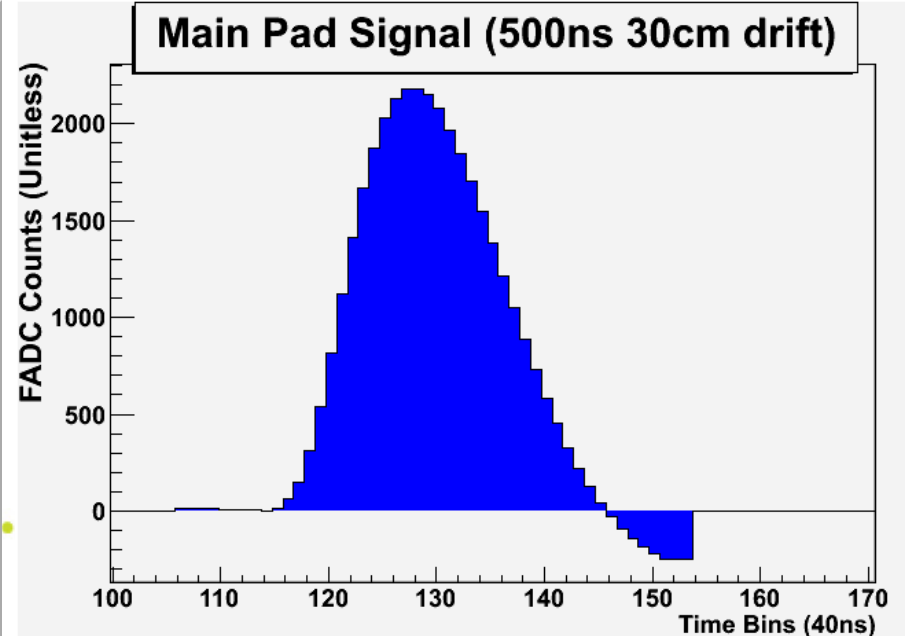
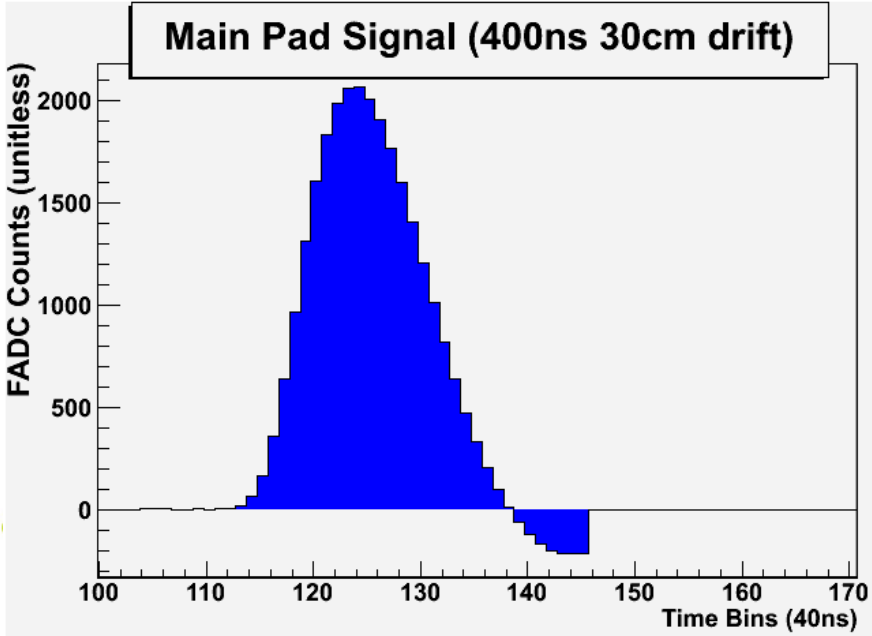
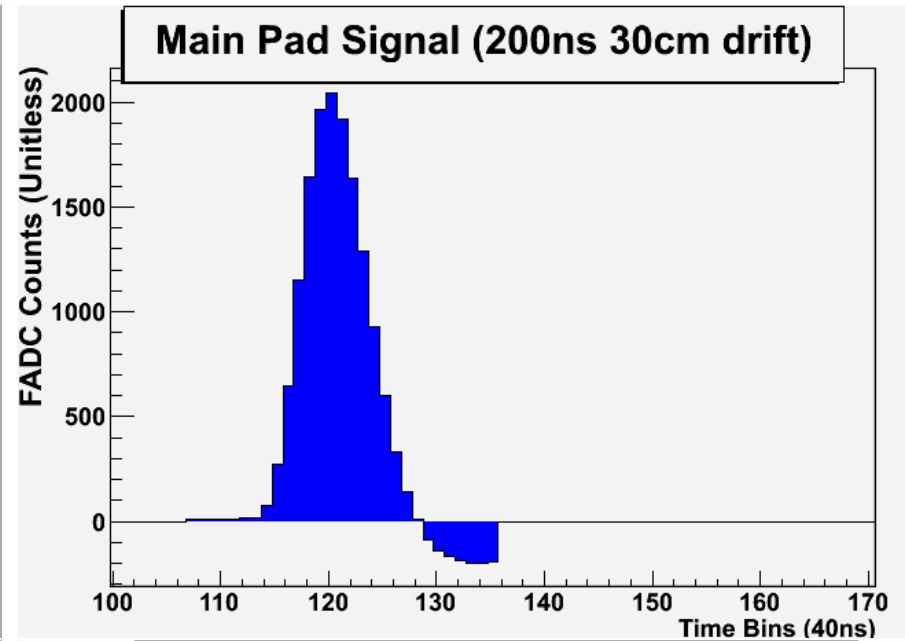
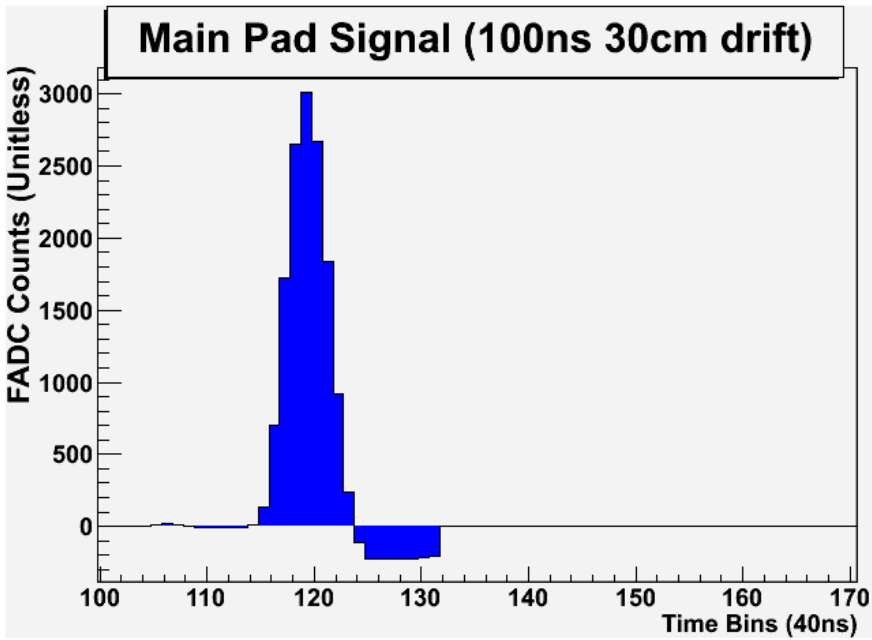


Stand-Alone Calculation

Parameter	Initial value	Final value
Drift speed	76.98 um/ns	fixed
Transverse diffusion	95.4 um/root(cm)	fixed
Longitudinal diffusion	231.289 um/root(cm)	fixed
Resistivity	2.9 MOhm/sq	fixed
Glue thickness	75 um	fixed
Dielectric constant	4.5	2.66
Induction time	120 ns	166 ns
b (shaper)	3.7	3.42
τ (shaper)	151 ns	151 ns
Pad angular width	0.001984 rad	fixed
Pad height	6.84 cm	fixed
Lower radius of bottom row	1.522457785 m	fixed
X_0 track	event dependent	
ϕ track	event dependent	
Drift distance	30 cm	30 cm

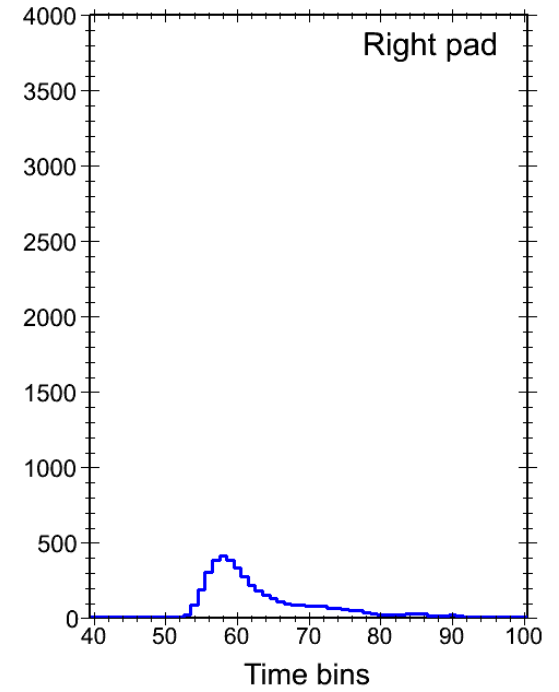
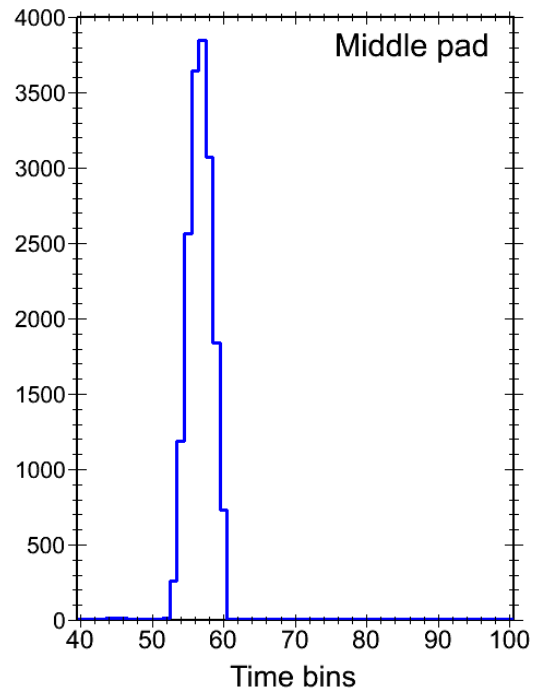
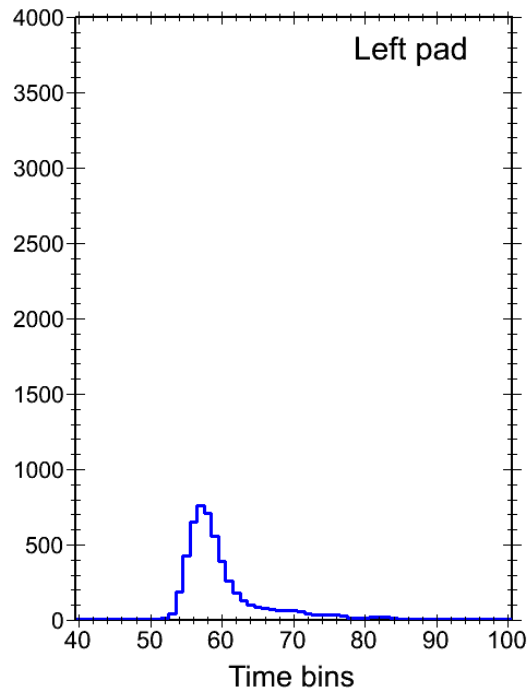
NEED INPUT OF DESIGN ENGINEER AND ELECTRONIC EXPERT

Shaped Pulse (for different shaping time)





Pad Amplitude

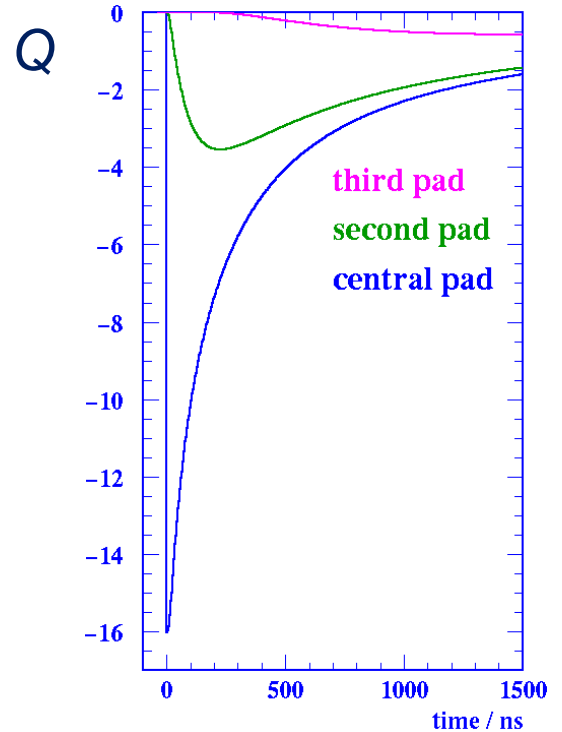
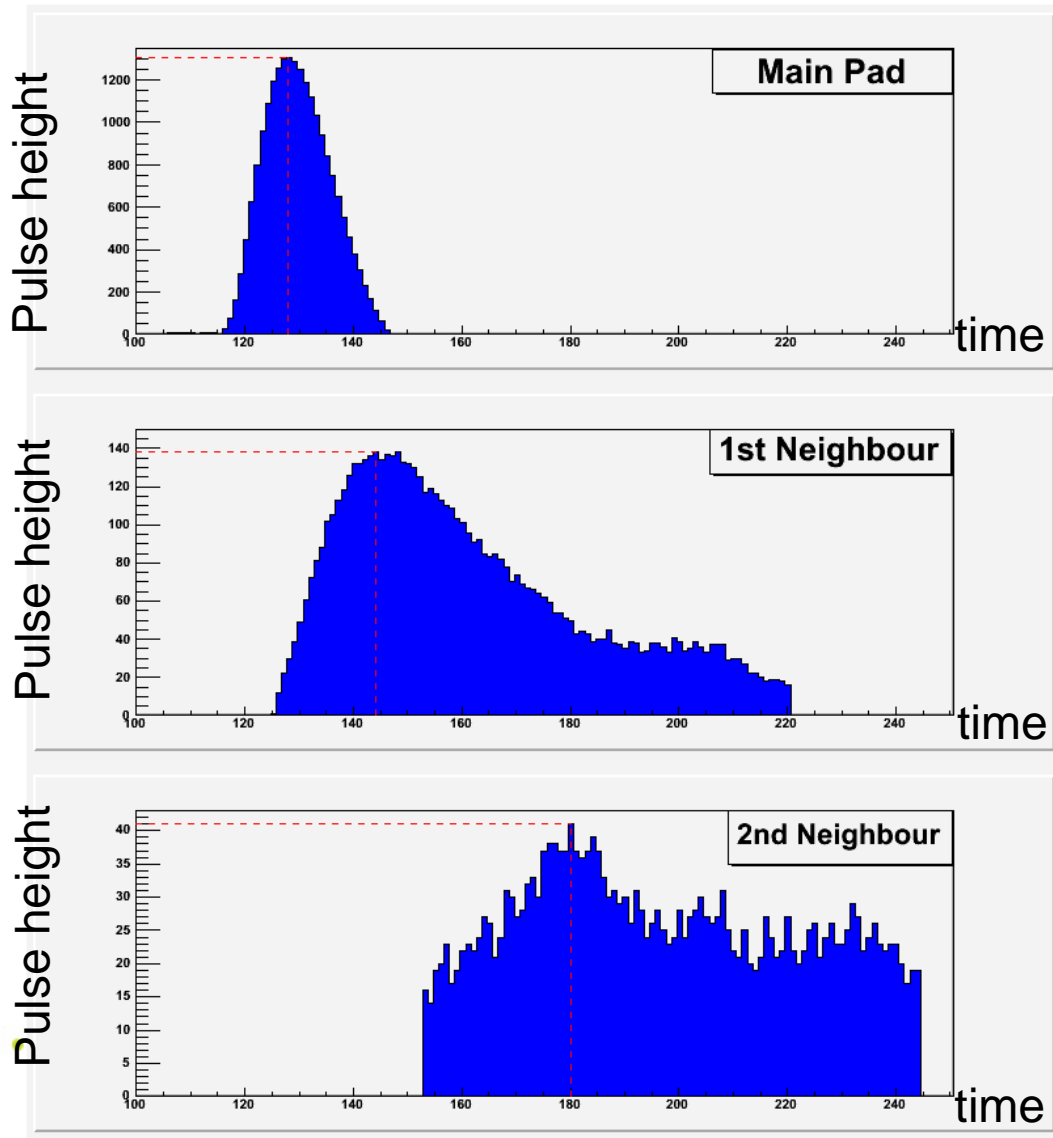


1) Use the maximum as the amplitude
Single Point Maximum(SPM)

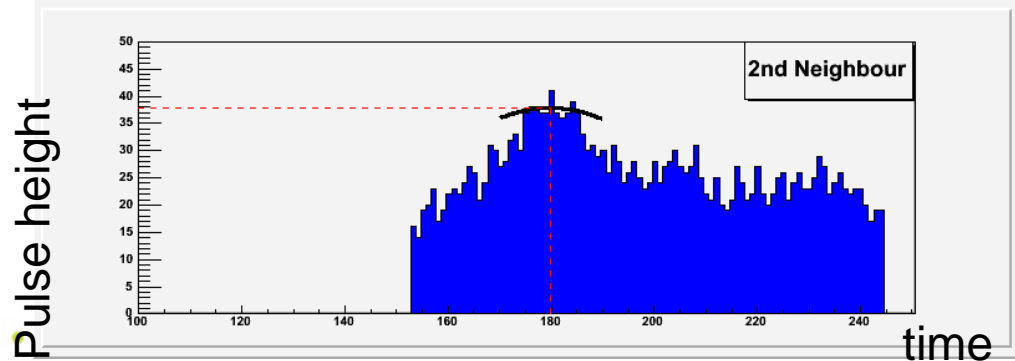
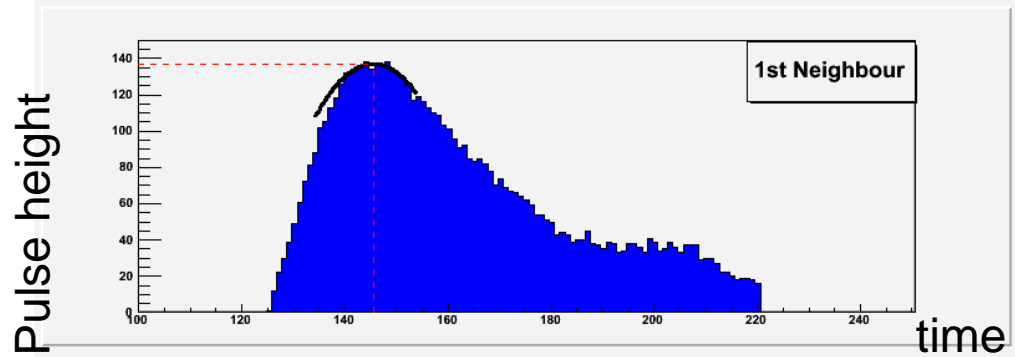
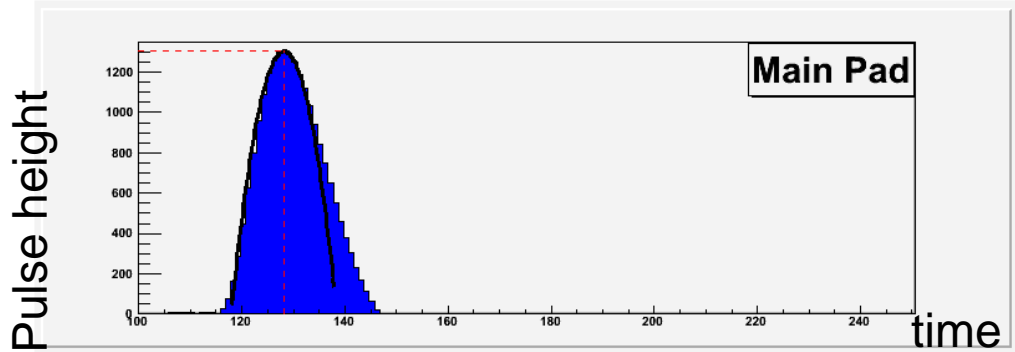
$$A_i = \max \text{ pulse height } P(i)$$

Pad Amplitude

method used here

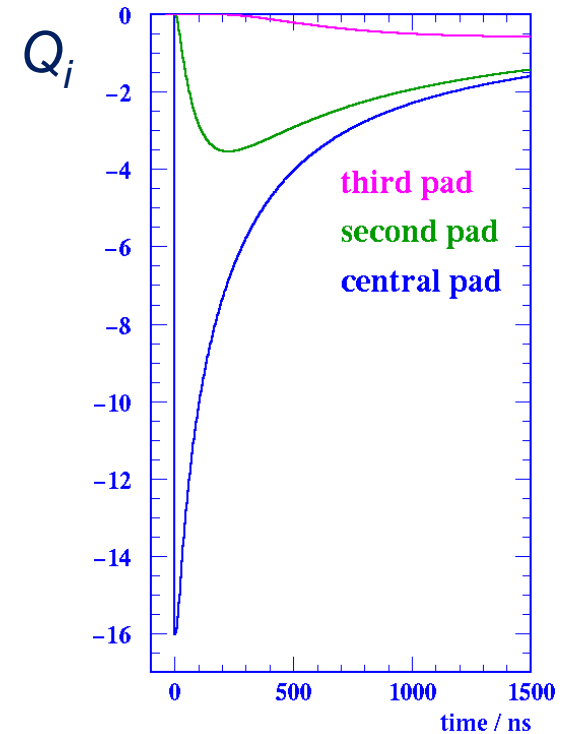


2) Maximum of Parabola Quadratic Fit Method (QFM) $A_i = \max$ of parabola $P(i)$



Pad Amplitude

Method use pre-2011

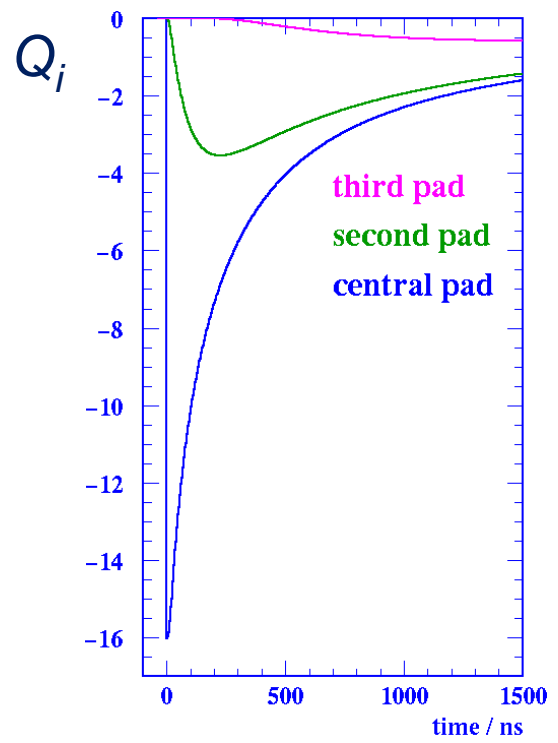
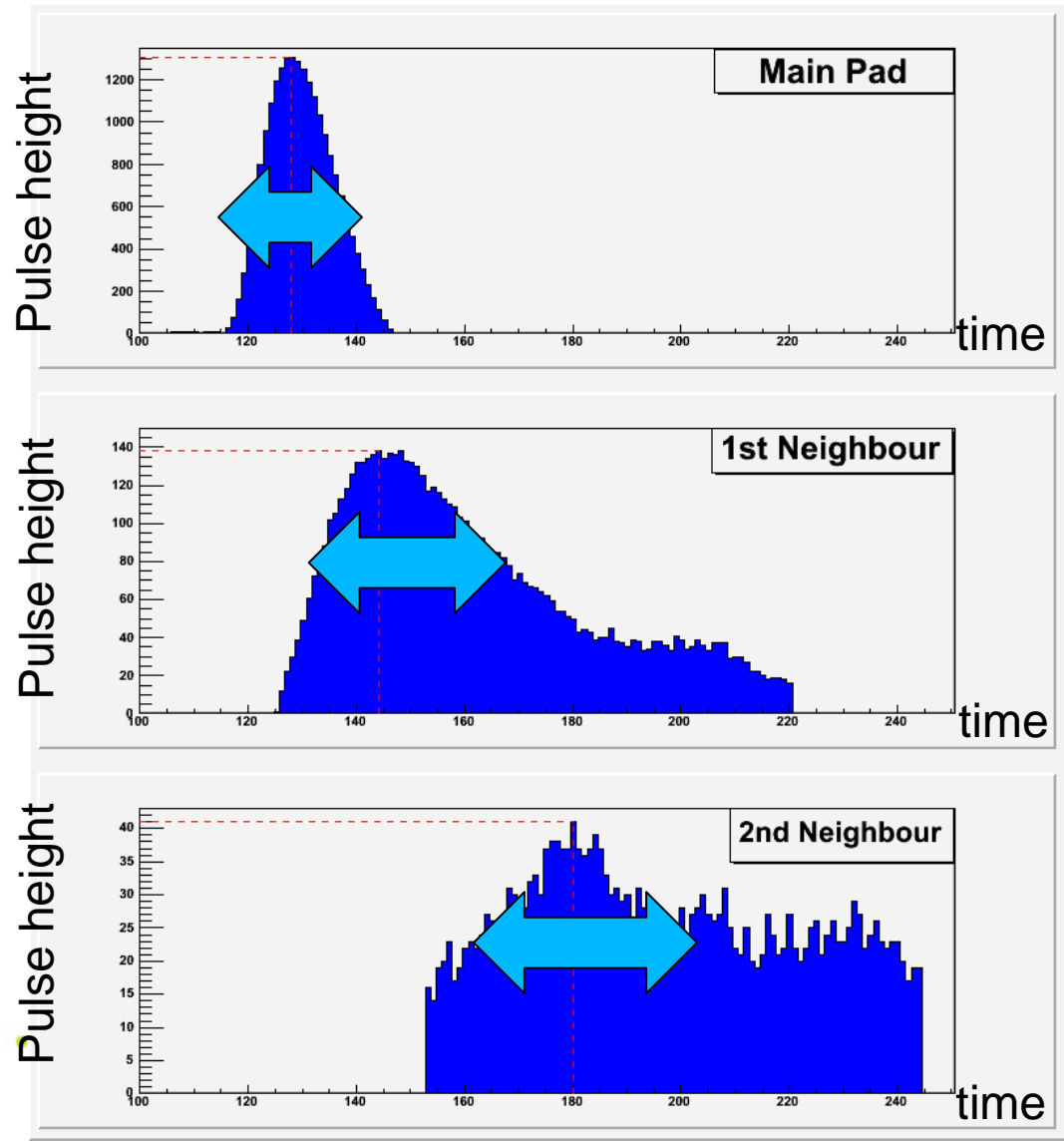


3) Integrate above threshold
Re-integration method (RM)

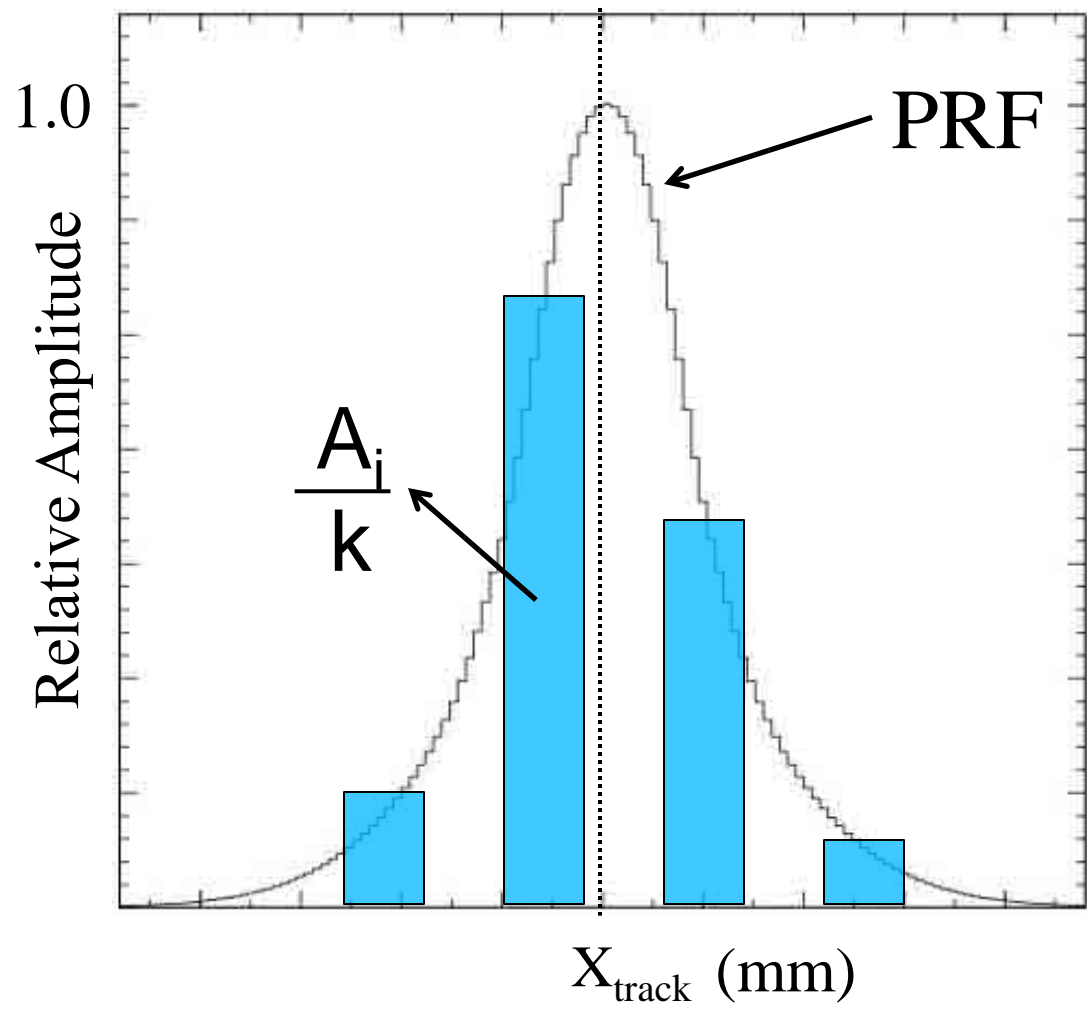
$$A_i = \text{Sum } P(i)$$

Pad Amplitude

Method use in 2011

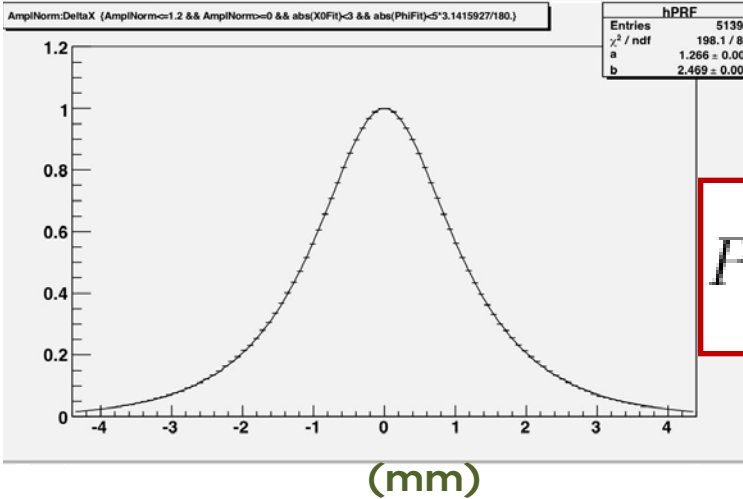
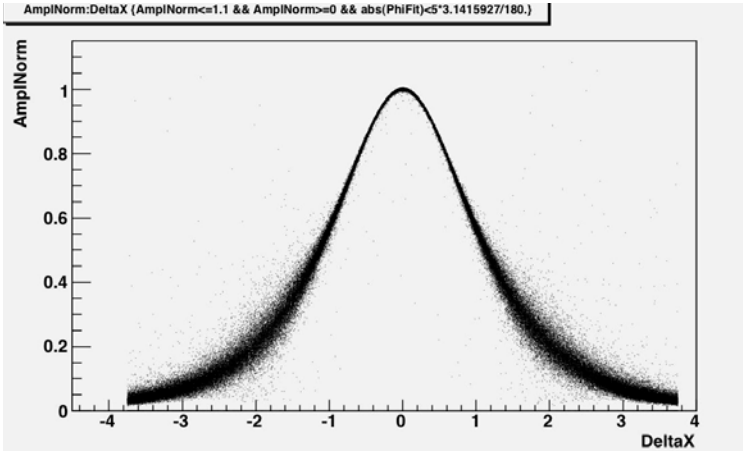


Pad Response Function (PRF)

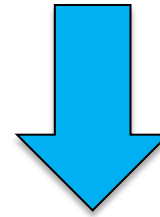


For a given X_{track} (known position) the PRF is defined to be unity

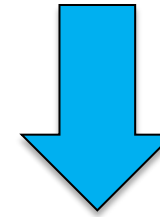
Pad Response Function (model)



$$PRF(x, \Gamma, \Delta, a, b) = \frac{1 + a_2x^2 + a_4x^4}{1 + b_2x^2 + b_4x^4}$$



$$PRF(x, a, b) = b^2 \frac{e^{-\frac{x^2}{2a^2}}}{x^2 + b^2}$$



new (used here)

$$PRF(x; r, w) = \frac{\exp(-4\ln(2)(1-r)x^2/w^2)}{1 + 4rx^2/w}$$

- Only two parameters (simpler model)
- Easier to work with
- Better fits to data



PRF versus Z

Micromegas

electron

mesh

anode

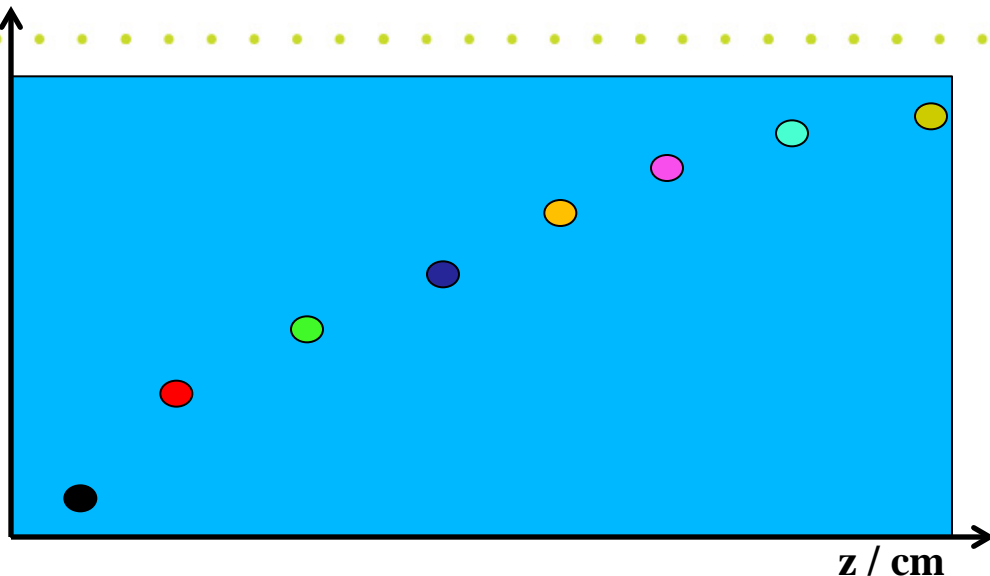
pads

avalanche

Direct signal

x

Width
PRF



z / cm

14 < z < 15cm

12 < z < 13cm

10 < z < 11cm

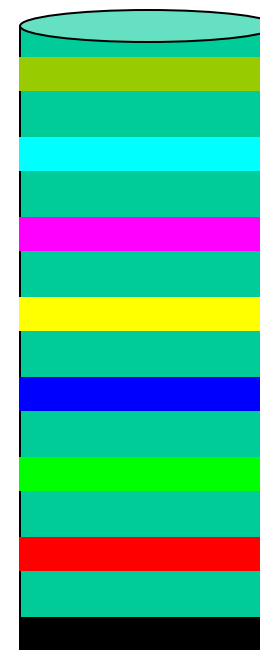
8 < z < 9cm

6 < z < 7cm

4 < z < 5cm

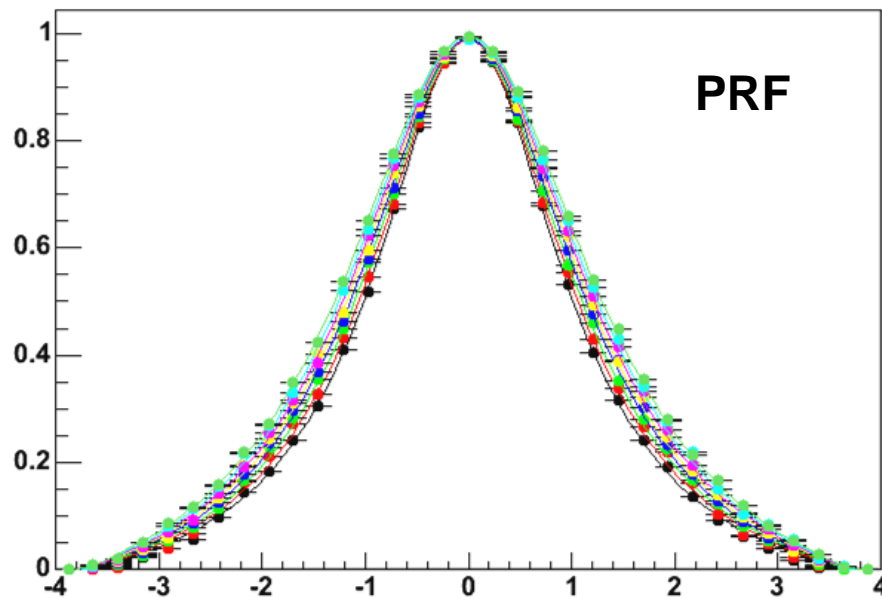
2 < z < 3cm

0 < z < 1cm



TPC

relative amplitude



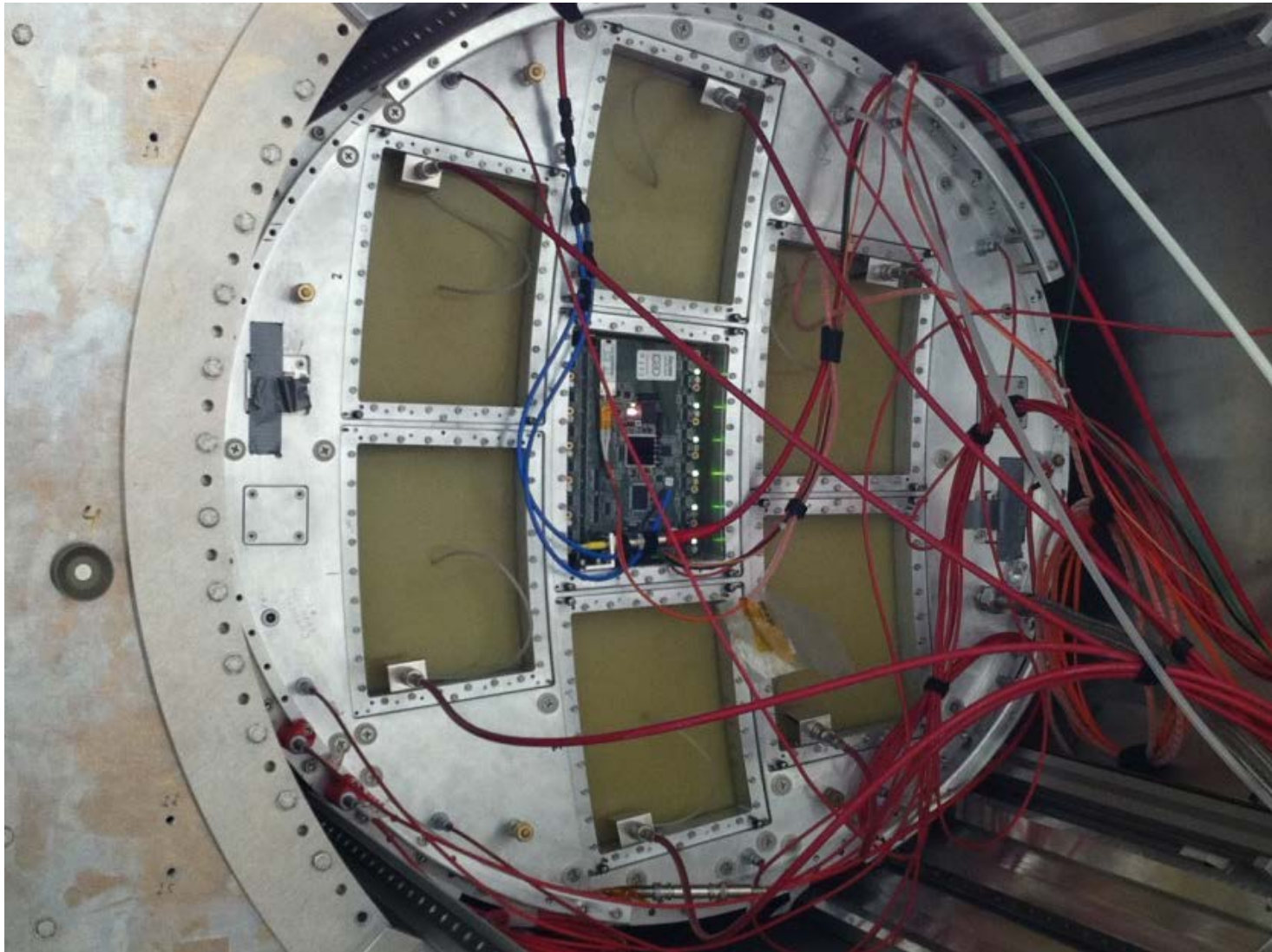
PRF

$x_{\text{pad}} - x_{\text{track}} / \text{mm}$

Single Module LCTPC (MM)

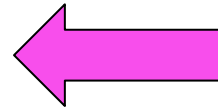
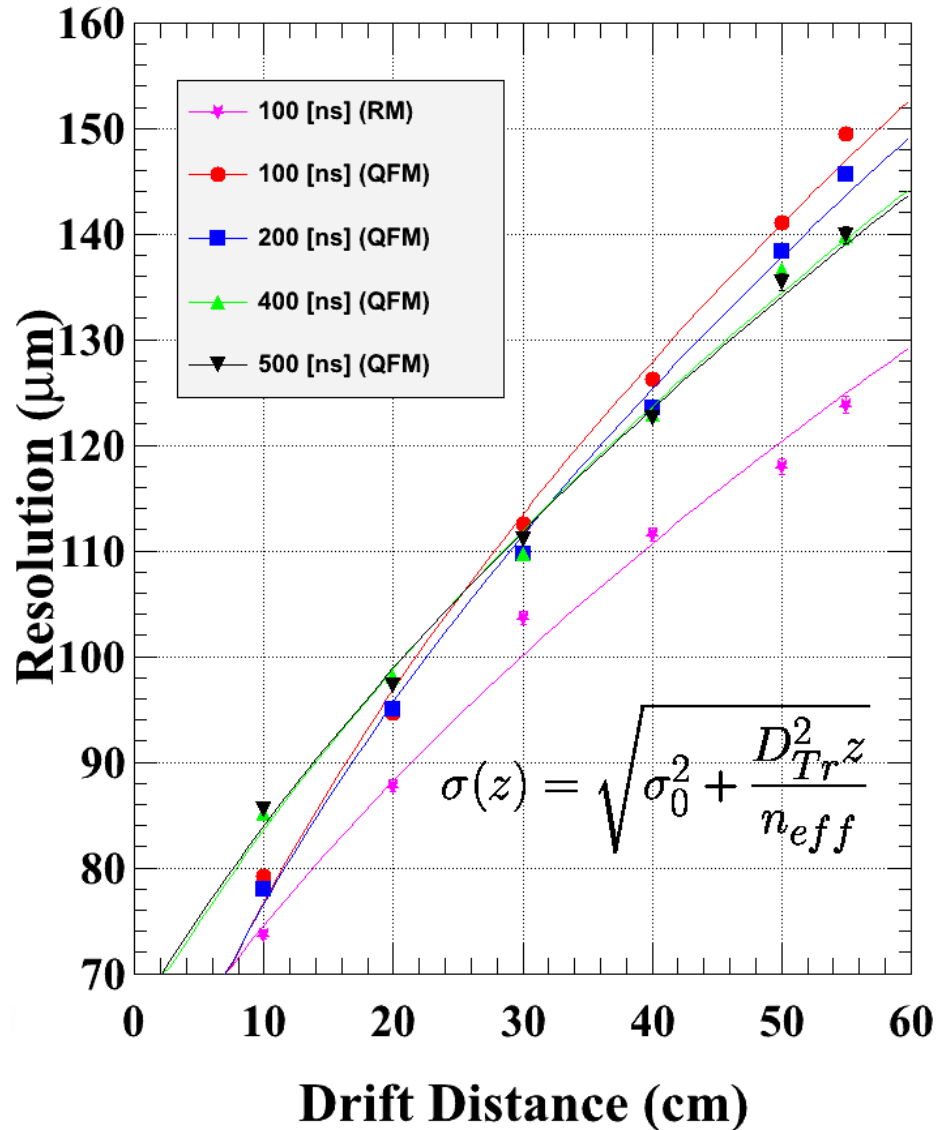
Period:
2008-2011

2011 data
Single module



Transverse Resolution MM

Resolution v. Drift Distance (All Scans)



2011 data
Single module

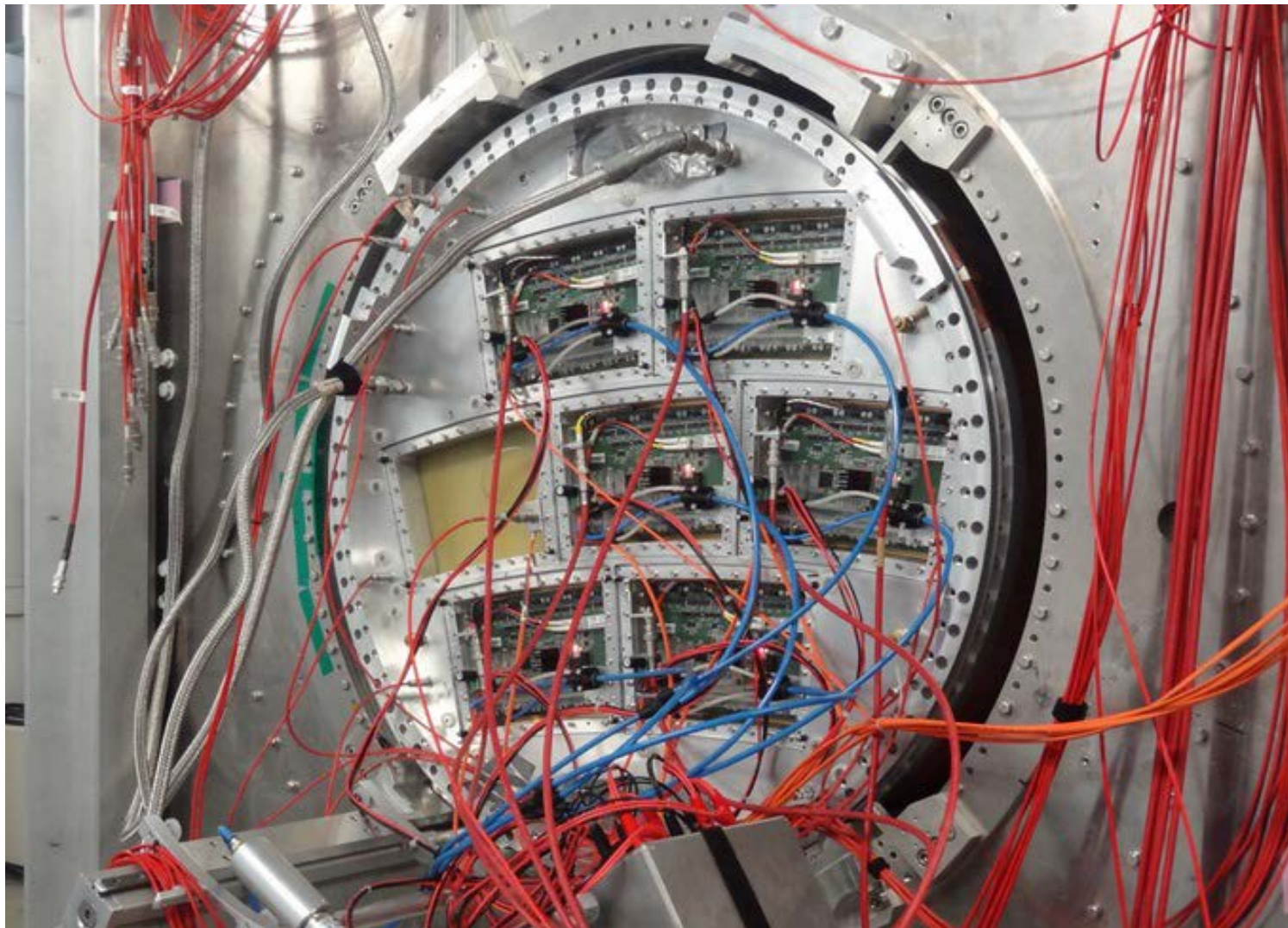
Source:
Nicholi Shiell
M.Sc. Thesis
Carleton University



7-module LCTPC (MM)

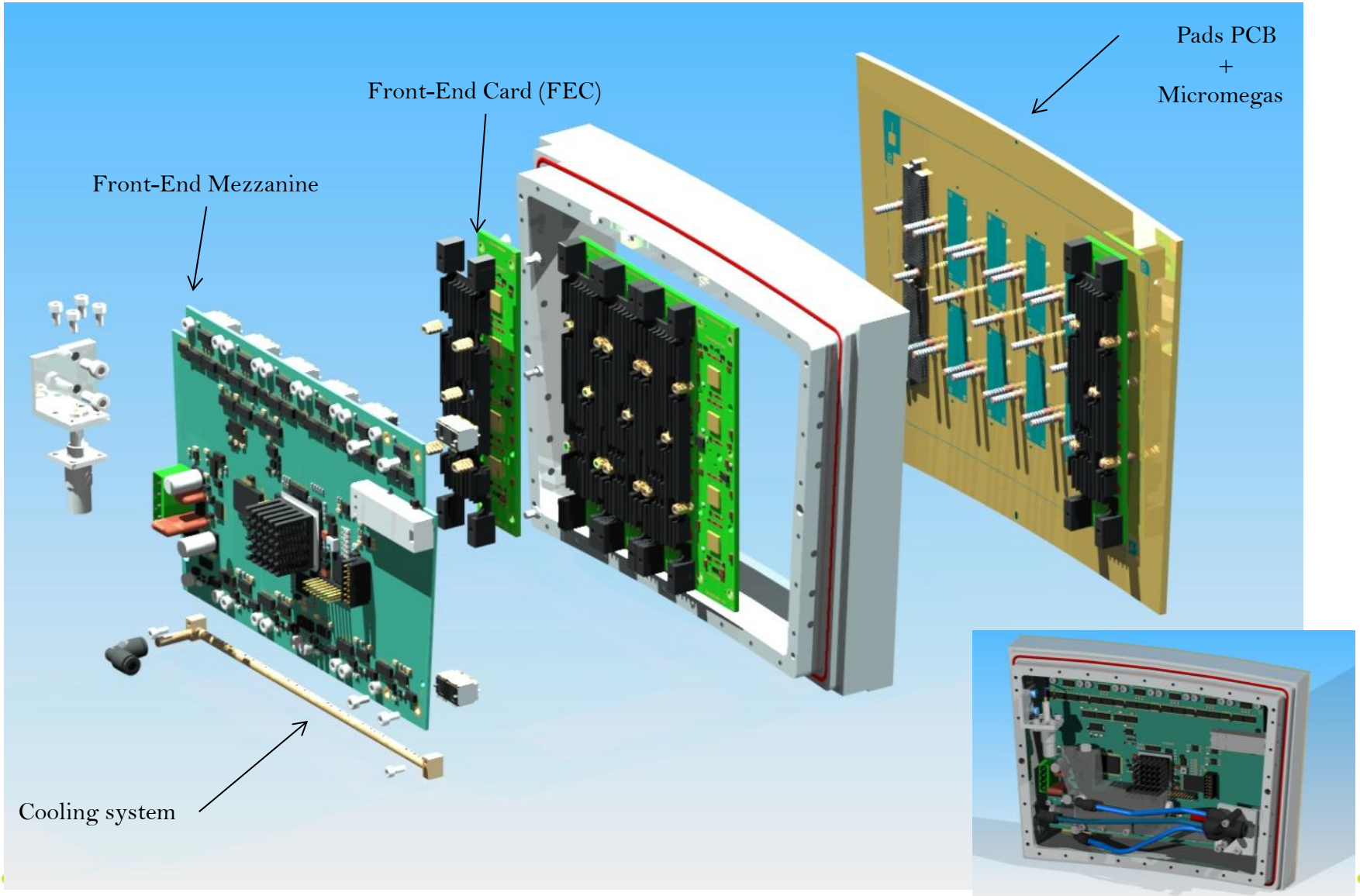
Period
2012-2013

2013 data
7-module

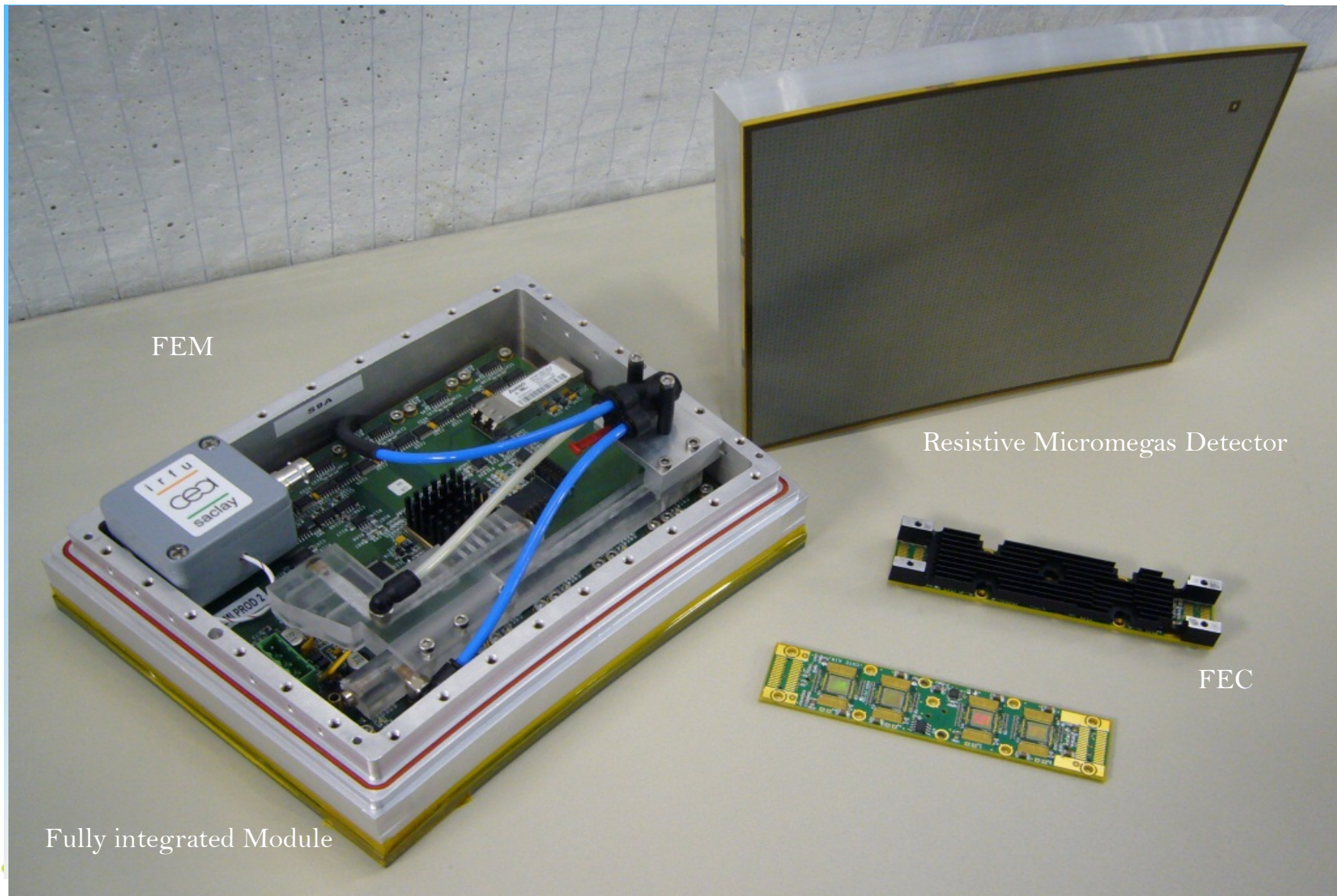




Resistive MM: Module Design



Resistive MM: Module Design



FEM

Resistive Micromegas Detector

FEC

Fully integrated Module



Analysis Framework: MarlinTPC

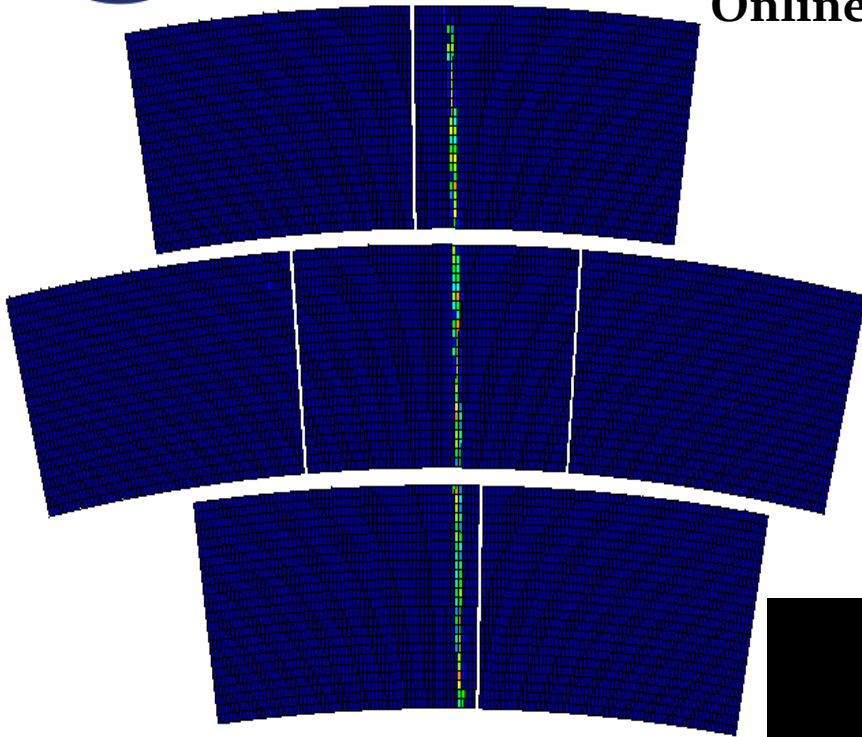
- MarlinTPC (LCIO) is the global effort to develop a single analysis code package for all the different prototype TPCs being developed.
- It is far from complete, but it has a solid foundation
- Furthermore, not sustainable to rely on stand alone code with hardcoded geometry, stand alone track-fit algorithm, calibration constants, etc...
- MarlinTPC processors: calibration for PRF determination, bias corrections and resolution determination (transverse and longitudinal)





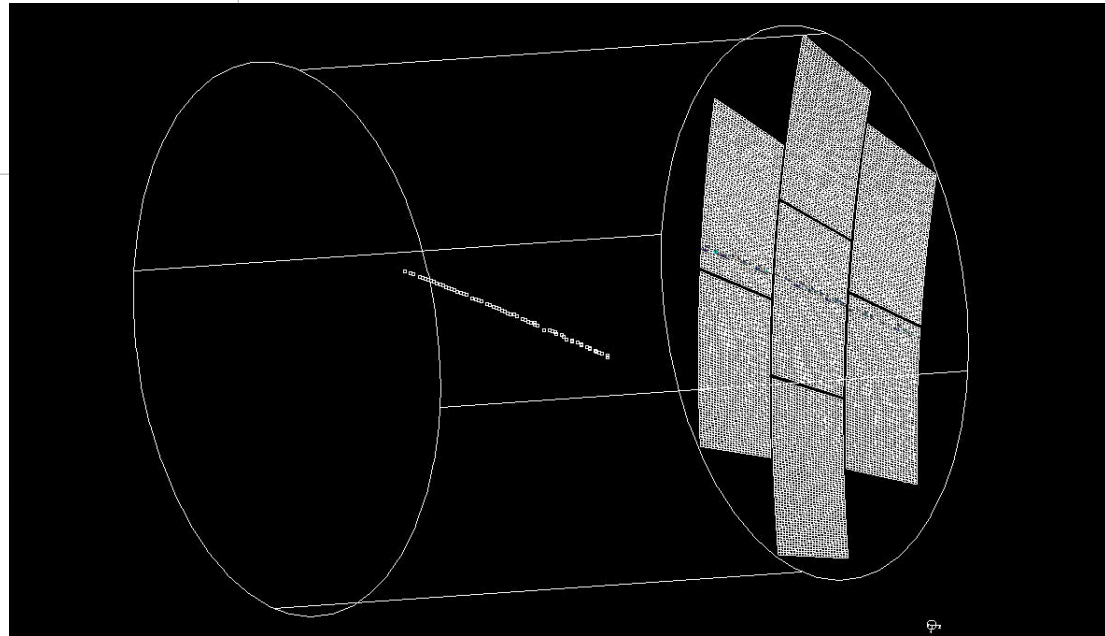
Event Display: MarlinTPC

Online monitor



2D or 3D display
software available

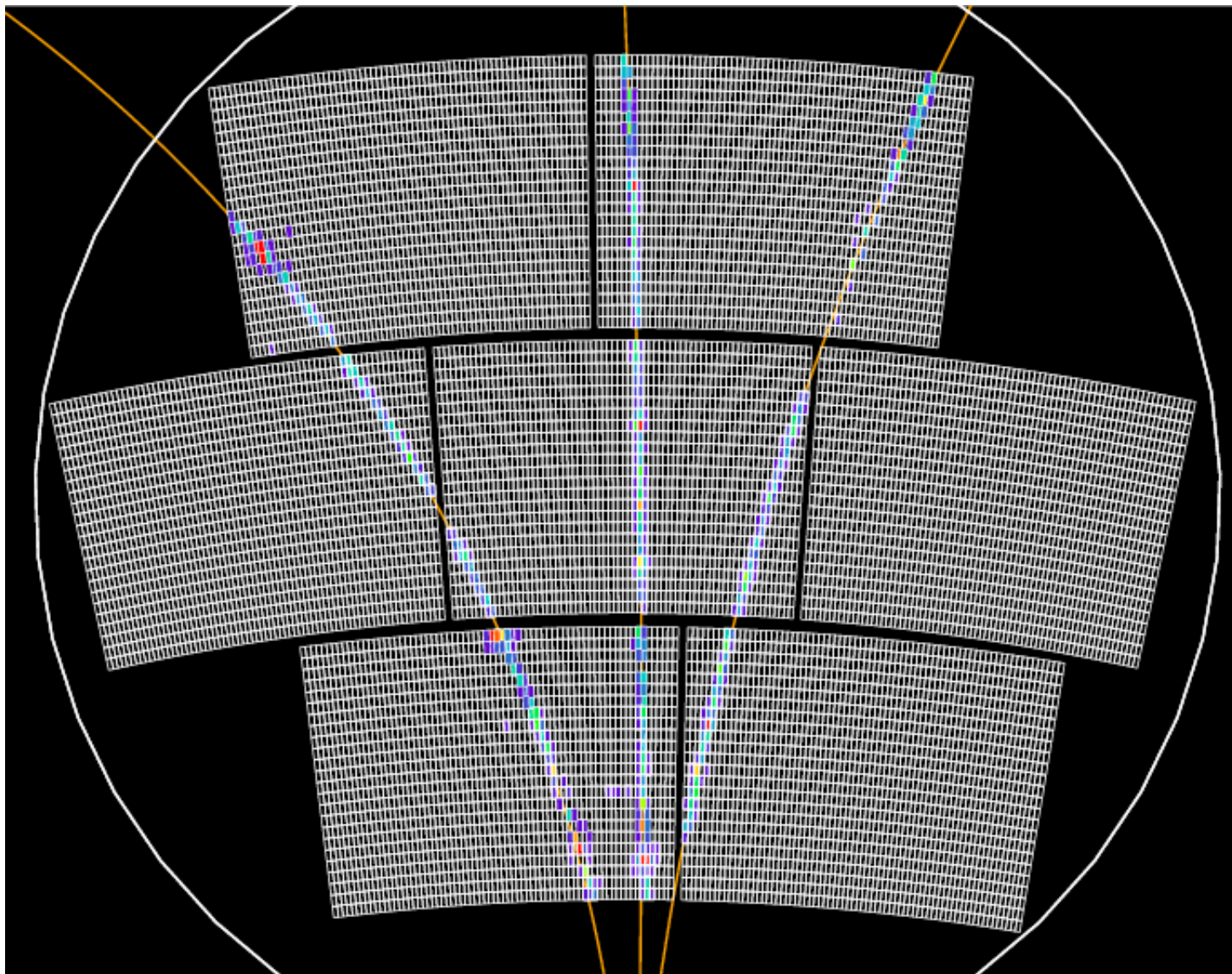
Offline monitor





Multi-track Pattern Recognition

Kalman Filter within MarlinTPC – LCIO geometry

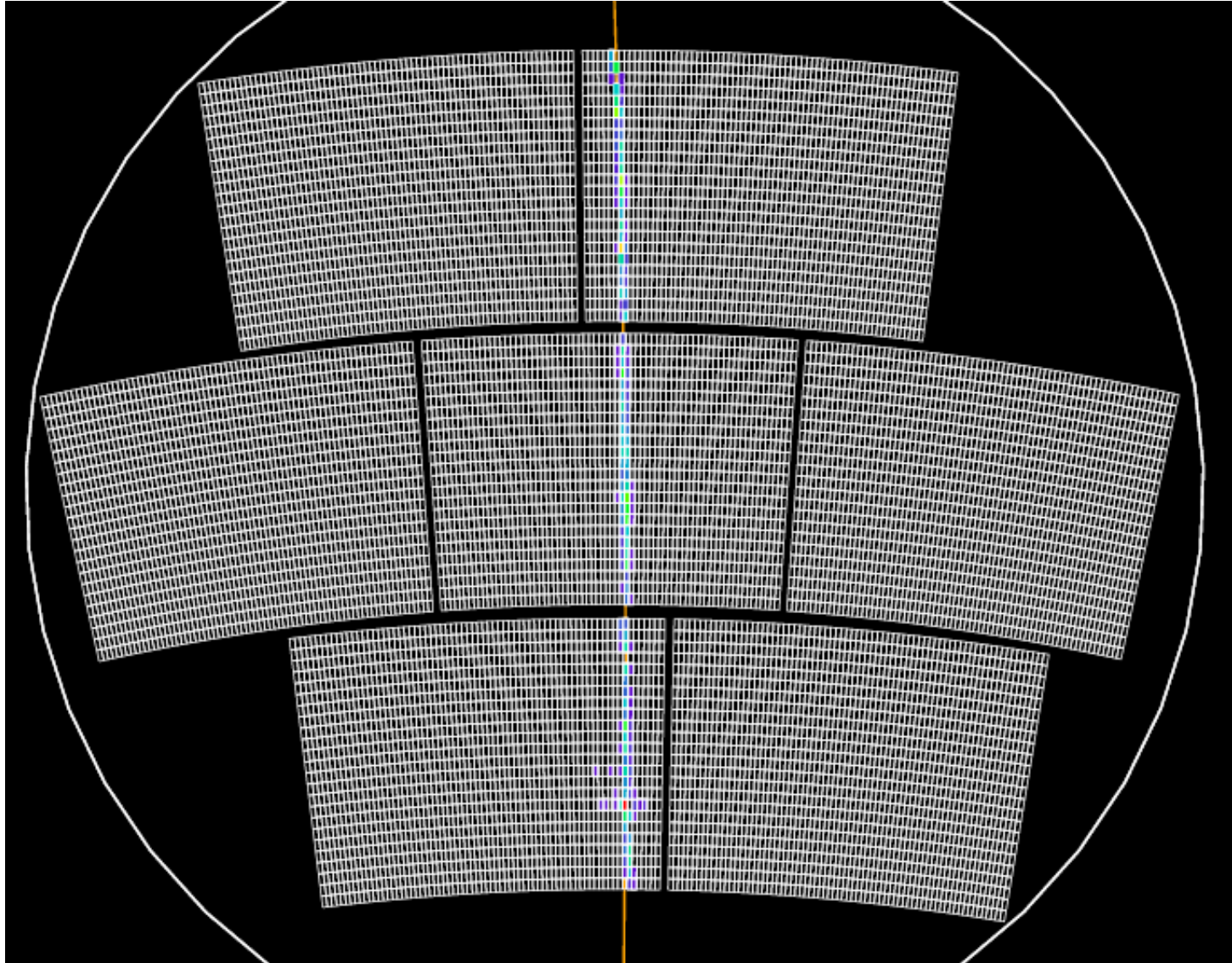


Acknowledgment:
Bo Li
Keisuke Fujii
Martin Killenberg

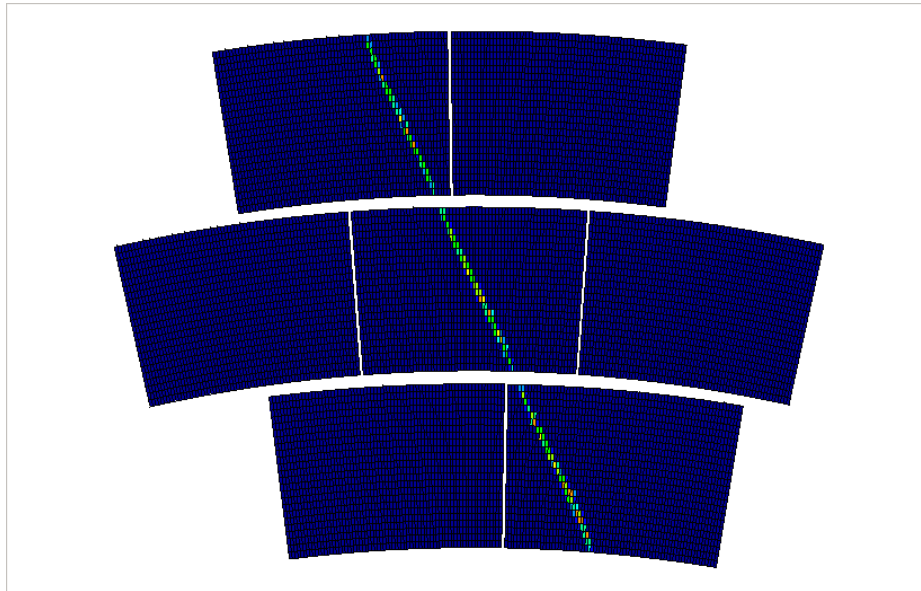


Single-track events for calibration

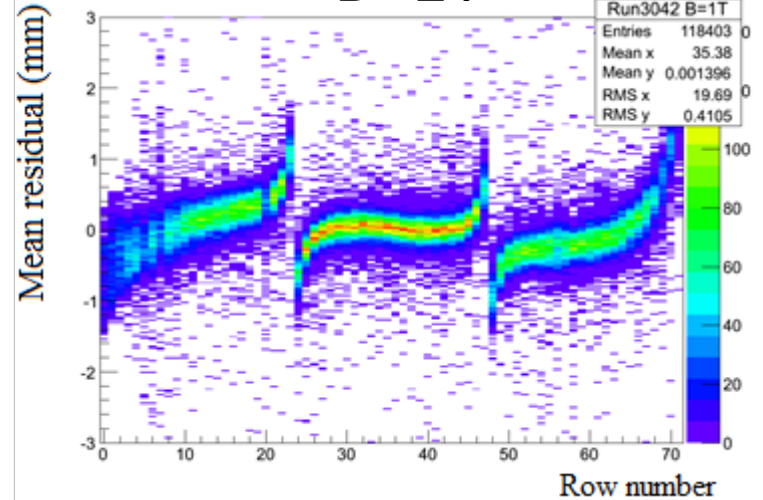
PRF calculation – bias – resolution study



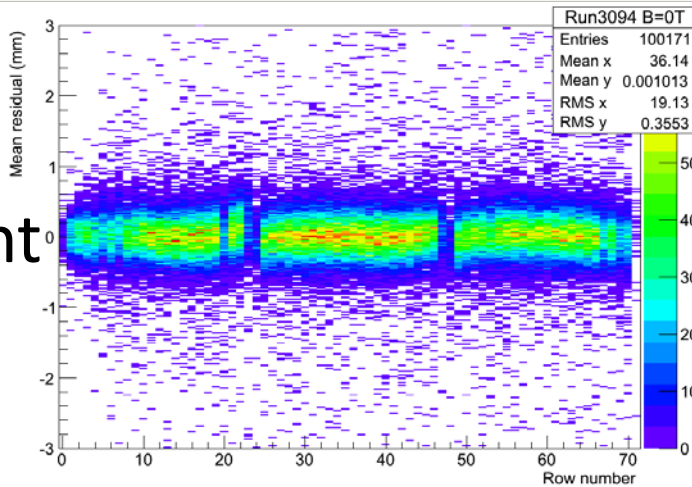
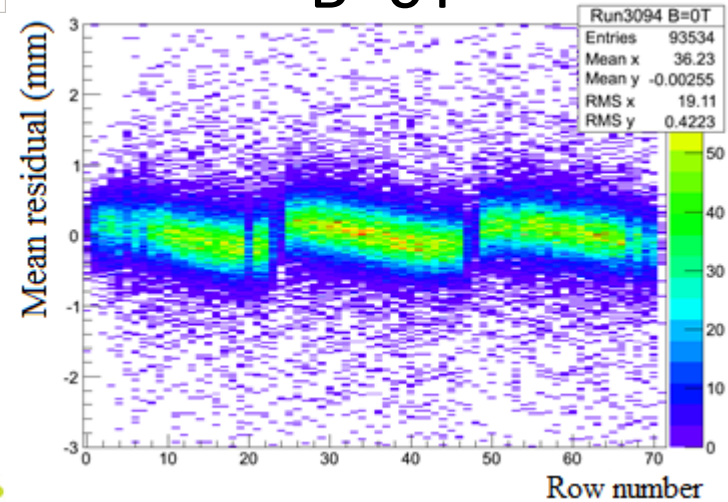
Field Distortions (E x B effect)



B=1T

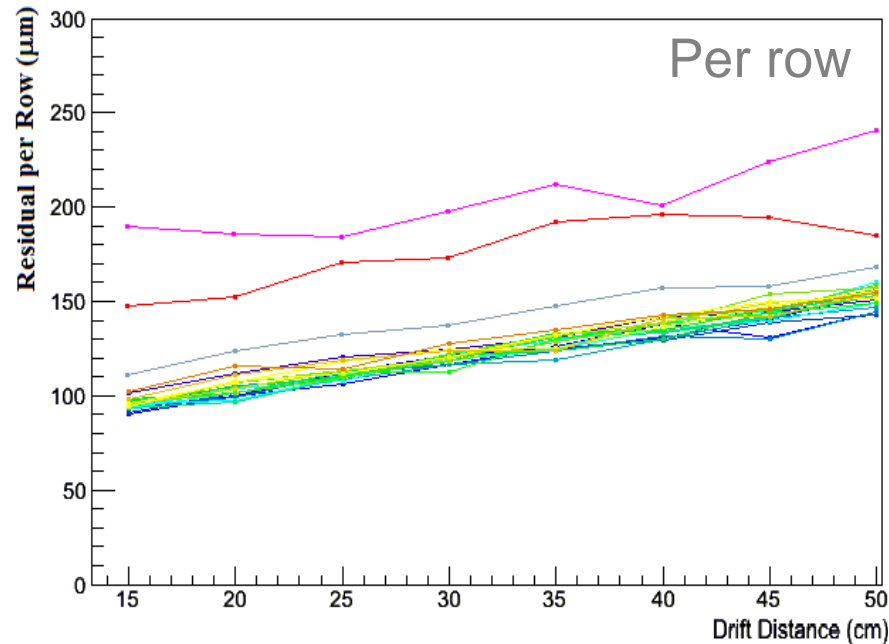


B=0T



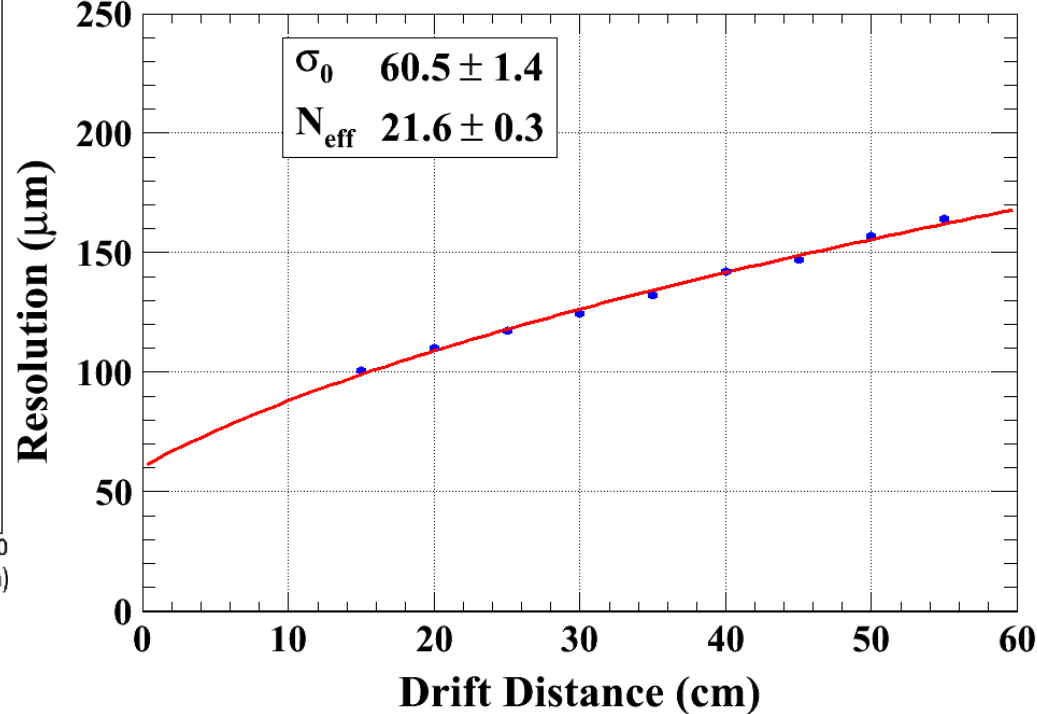
After alignment

2013 data
7 module



$$\sigma = \sqrt{\sigma_0^2 + \frac{C_d^2 \cdot z}{N_{eff}}}$$

$B=1\text{ T}$ $C_d = 94.2\ \mu\text{m}/\sqrt{\text{cm}}$ (Magboltz)

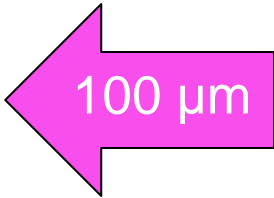
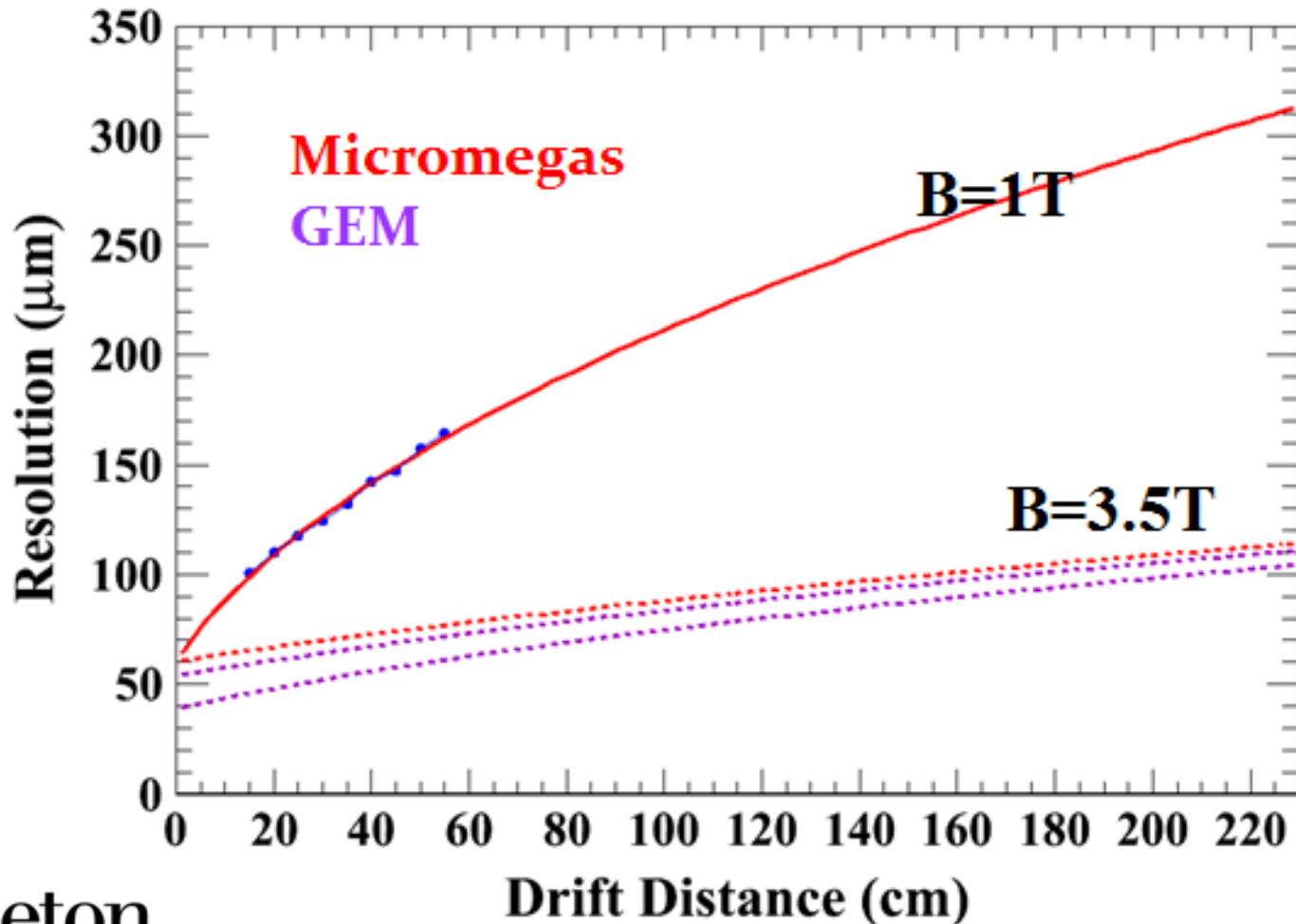


σ_0 : the resolution at $Z=0$
 N_{eff} : the effective number of electrons

Transverse Resolution

Micromegas (MM) versus GEM

Extrapolate to B=3.5T



- A lot of experience has been gained in building and operating Micromegas TPC panels.
- The characteristics of the Micromegas modules, such as the uniformity, spatial resolution, stability have been studied in detail.
- **7 modules** have been successfully tested with full integration of the electronics at the same time. The modules have been manufactured and characterized in a quasi-industrial process.
- Thanks to the **resistive technology**, the measured resolution is about **60 microns** at zero drift distance with **3 mm** wide pads. This meets ILC requirements of 100 μm single hit resolution in $r\phi$ (over 2 m drift).





Uniformity of Resistive Anode

Mean Residual vs Row Number

Z-independent distortions

Distortions up to 50 microns for resistive ink (blue points)

RMS of 7 microns for CLK film (red points)

