

# LC Precision in the MSSM: Getting It Under Control

*Sven Heinemeyer, IFCA (CSIC, Santander)*

Hamburg, 05/2013

based on collaboration with *A. Bharoucha, T. Fritzsche, F. v.d. Pahlen, H. Rzehak, C. Schappacher, G. Weiglein*

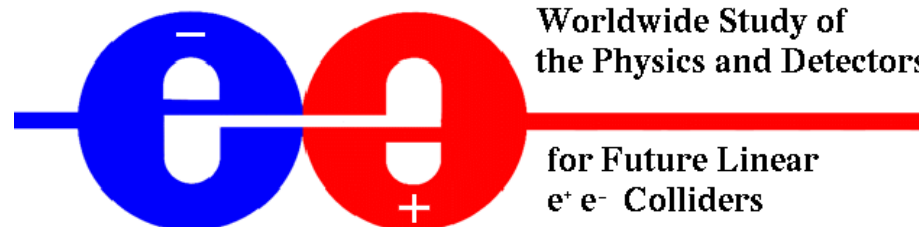
1. Introduction & The bigger picture
2. Renormalization schemes for stops and sbottoms
3. Renormalization schemes for charginos and neutralinos
4. Some numerical examples
5. Conclusions & Outlook

# 1. The Grand Scheme

The LHC will run at 13-14 TeV ...  
→ discovery of BSM physics in 2015?



The ILC is still coming ...  
... a bit later than anticipated  
→ to investigate BSM physics



⇒ New Physics is certainly around the corner

⇒ Time to get ready for BSM physics

The big question:

Which Lagrangian describes the world?

My guess:

It is a supersymmetric one

⇒ concentrate on the MSSM from now on

(other people ⇒ other guesses ⇒ other priorities . . . )

In any case:

⇒ we have to measure as many observables as possible

- masses
- branching ratios
- angular distributions
- cross sections
- . . .

The big question:

Which Lagrangian describes the world?

My guess:

It is a supersymmetric one

⇒ concentrate on the MSSM from now on

(other people ⇒ other guesses ⇒ other priorities . . .)

In any case:

⇒ we have to measure as many observables as possible

- masses
- branching ratios
- angular distributions
- cross sections
- . . .

⇒ compare with theory calculations at the same level of accuracy

# The Minimal Supersymmetric Standard Model (MSSM)

## Superpartners for Standard Model particles

$$\begin{array}{llll} [u, d, c, s, t, b]_{L,R} & [e, \mu, \tau]_{L,R} & [\nu_{e,\mu,\tau}]_L & \text{Spin } \frac{1}{2} \\ [\tilde{u}, \tilde{d}, \tilde{c}, \tilde{s}, \tilde{t}, \tilde{b}]_{L,R} & [\tilde{e}, \tilde{\mu}, \tilde{\tau}]_{L,R} & [\tilde{\nu}_{e,\mu,\tau}]_L & \text{Spin } 0 \\ g & \underbrace{W^\pm, H^\pm}_{\text{Spin } 1} & \underbrace{\gamma, Z, H_1^0, H_2^0}_{\text{Spin } 0} & \text{Spin } 1 / \text{Spin } 0 \\ \tilde{g} & \tilde{\chi}_{1,2}^\pm & \tilde{\chi}_{1,2,3,4}^0 & \text{Spin } \frac{1}{2} \end{array}$$

Enlarged Higgs sector: Two Higgs doublets

Problem in the MSSM: many scales

Problem in the MSSM: complex phases

## Generic problems for SUSY loop calculations:

- SUSY has to be preserved in the calculation
  - Many different mass scales
  - Many more mass scales than free parameters
  - Even more parameters: mixing angles, complex phases
  - Renormalization is much more involved than in the SM
    - much less explored than in the SM
    - has to preserve/respect mass relations
    - depend on mass scales realized in Nature
    - sometimes no really good solution exist (e.g.  $\tan\beta$ )
    - many sectors enter at the same time
- ⇒ this is the biggest issue!

## Enlarged Higgs sector: Two Higgs doublets

$$H_1 = \begin{pmatrix} H_1^1 \\ H_1^2 \end{pmatrix} = \begin{pmatrix} v_1 + (\phi_1 + i\chi_1)/\sqrt{2} \\ \phi_1^- \end{pmatrix}$$

$$H_2 = \begin{pmatrix} H_2^1 \\ H_2^2 \end{pmatrix} = \begin{pmatrix} \phi_2^+ \\ v_2 + (\phi_2 + i\chi_2)/\sqrt{2} \end{pmatrix}$$

$$V = m_1^2 H_1 \bar{H}_1 + m_2^2 H_2 \bar{H}_2 - m_{12}^2 (\epsilon_{ab} H_1^a H_2^b + \text{h.c.}) \\ + \underbrace{\frac{g'^2 + g^2}{8}}_{\text{gauge couplings, in contrast to SM}} (H_1 \bar{H}_1 - H_2 \bar{H}_2)^2 + \underbrace{\frac{g^2}{2}}_{\text{gauge couplings, in contrast to SM}} |H_1 \bar{H}_2|^2$$

physical states:  $h^0, H^0, A^0, H^\pm$

Goldstone bosons:  $G^0, G^\pm$

Input parameters: (to be determined experimentally)

$$\tan \beta = \frac{v_2}{v_1}, \quad M_A^2 = -m_{12}^2 (\tan \beta + \cot \beta)$$

## Enlarged Higgs sector: Two Higgs doublets with $\mathcal{CP}$ violation

$$H_1 = \begin{pmatrix} H_1^1 \\ H_1^2 \end{pmatrix} = \begin{pmatrix} v_1 + (\phi_1 + i\chi_1)/\sqrt{2} \\ \phi_1^- \end{pmatrix}$$
$$H_2 = \begin{pmatrix} H_2^1 \\ H_2^2 \end{pmatrix} = \begin{pmatrix} \phi_2^+ \\ v_2 + (\phi_2 + i\chi_2)/\sqrt{2} \end{pmatrix} e^{i\xi}$$

$$V = m_1^2 H_1 \bar{H}_1 + m_2^2 H_2 \bar{H}_2 - m_{12}^2 (\epsilon_{ab} H_1^a H_2^b + \text{h.c.})$$
$$+ \underbrace{\frac{g'^2 + g^2}{8}}_{\text{gauge couplings, in contrast to SM}} (H_1 \bar{H}_1 - H_2 \bar{H}_2)^2 + \underbrace{\frac{g^2}{2}}_{\text{gauge couplings, in contrast to SM}} |H_1 \bar{H}_2|^2$$

physical states:  $h^0, H^0, A^0, H^\pm$

2  $\mathcal{CP}$ -violating phases:  $\xi, \arg(m_{12}) \Rightarrow$  can be set/rotated to zero

Input parameters: (to be determined experimentally)

$$\tan \beta = \frac{v_2}{v_1}, \quad M_{H^\pm}^2$$



## The Higgs sector of the cMSSM at tree-level:

- phase of  $m_{12}$  :

$m_{12} = 0$  and  $\mu = 0 \Rightarrow$  additional  $U(1)$  (PQ) symmetry

reality:  $m_{12} \neq 0$ ,  $\mu \neq 0$

$\Rightarrow$  perform PQ transformation with  $\phi_{PQ}$

$$\begin{aligned} m_{12}'^2 &= |m_{12}^2| e^{i(\phi_{m_{12}} - \phi_{PQ})} \\ \mu' &= |\mu| e^{i(\phi_{\mu} - \phi_{PQ})} \end{aligned}$$

$\Rightarrow m_{12}$  can always be chosen real

- phase of  $H_2$ :  $\xi$  :

mixing between  $\mathcal{CP}$ -even and  $\mathcal{CP}$ -odd states:

$$\mathcal{M}_{\mathcal{CP}\text{-even}, \mathcal{CP}\text{-odd}} = \begin{pmatrix} 0 & m_{12}^2 \sin \xi \\ -m_{12}^2 \sin \xi & 0 \end{pmatrix}$$

Tadpoles have to vanish:  $T_A^{\text{tree}} \propto \sin \xi m_{12}^2 \stackrel{!}{=} 0$

$\Rightarrow \xi = 0 \Rightarrow$  no  $\mathcal{CPV}$  at tree-level

## The Higgs sector of the cMSSM at the loop-level:

Complex parameters enter via loop corrections:

- $\mu$  : Higgsino mass parameter
- $A_{t,b,\tau}$  : trilinear couplings  $\Rightarrow X_{t,b,\tau} = A_{t,b,\tau} - \mu^* \{\cot \beta, \tan \beta\}$  complex
- $M_{1,2}$  : gaugino mass parameter (one phase can be eliminated)
- $M_3$  : gluino mass parameter

$\Rightarrow$  can induce  $\mathcal{CP}$ -violating effects

Result:

$$(A, H, h) \rightarrow (h_3, h_2, h_1)$$

with

$$m_{h_3} > m_{h_2} > m_{h_1}$$

$\Rightarrow$  strong changes in Higgs couplings to SM gauge bosons and fermions

$\tilde{t}/\tilde{b}$  sector of the MSSM: (scalar partner of the top/bottom quark)

Stop, sbottom mass matrices ( $X_t = A_t - \mu^*/\tan\beta$ ,  $X_b = A_b - \mu^*\tan\beta$ ):

$$\mathcal{M}_{\tilde{t}}^2 = \begin{pmatrix} M_{\tilde{t}_L}^2 + m_t^2 + DT_{t_1} & m_t X_t^* \\ m_t X_t & M_{\tilde{t}_R}^2 + m_t^2 + DT_{t_2} \end{pmatrix} \xrightarrow{\theta_{\tilde{t}}} \begin{pmatrix} m_{\tilde{t}_1}^2 & 0 \\ 0 & m_{\tilde{t}_2}^2 \end{pmatrix}$$

$$\mathcal{M}_{\tilde{b}}^2 = \begin{pmatrix} M_{\tilde{b}_L}^2 + m_b^2 + DT_{b_1} & m_b X_b^* \\ m_b X_b & M_{\tilde{b}_R}^2 + m_b^2 + DT_{b_2} \end{pmatrix} \xrightarrow{\theta_{\tilde{b}}} \begin{pmatrix} m_{\tilde{b}_1}^2 & 0 \\ 0 & m_{\tilde{b}_2}^2 \end{pmatrix}$$

mixing important in stop sector (also in sbottom sector for large  $\tan\beta$ )

soft SUSY-breaking parameters  $A_t, A_b$  also appear in  $\phi$ - $\tilde{t}/\tilde{b}$  couplings

$$m_{\tilde{t}_{1,2}}^2 = m_t^2 + \frac{1}{2} \left( M_{\tilde{t}_L}^2 + M_{\tilde{t}_R}^2 \mp \sqrt{(M_{\tilde{t}_L}^2 - M_{\tilde{t}_R}^2)^2 + 4m_t^2 |X_t|^2} \right)$$

$\Rightarrow$  independent of  $\phi_{X_t}$   
but  $\theta_{\tilde{t}}$  is now complex

**$SU(2)$  relation**  $\Rightarrow M_{\tilde{t}_L} = M_{\tilde{b}_L} \Rightarrow$  relation between  $m_{\tilde{t}_1}, m_{\tilde{t}_2}, \theta_{\tilde{t}}, m_{\tilde{b}_1}, m_{\tilde{b}_2}, \theta_{\tilde{b}}$

More on complex phases: Neutralinos and charginos:

Higgsinos and electroweak gauginos mix

charged:

$$\tilde{W}^+, \tilde{h}_u^+ \rightarrow \tilde{\chi}_1^+, \tilde{\chi}_2^+, \quad \tilde{W}^-, \tilde{h}_d^- \rightarrow \tilde{\chi}_1^-, \tilde{\chi}_2^-$$

⇒ charginos: mass eigenstates

mass matrix given in terms of  $M_2$ ,  $\mu$ ,  $\tan \beta$

neutral:

$$\underbrace{\tilde{\gamma}, \tilde{Z}, \tilde{h}_u^0, \tilde{h}_d^0}_{\tilde{W}^0, \tilde{B}^0} \rightarrow \tilde{\chi}_1^0, \tilde{\chi}_2^0, \tilde{\chi}_3^0, \tilde{\chi}_4^0$$

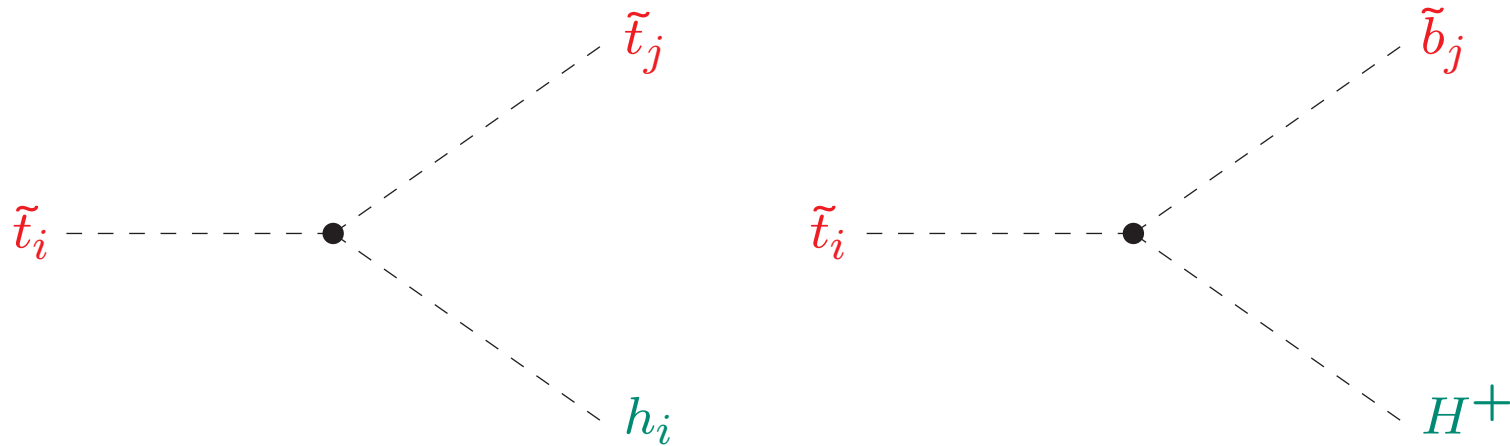
⇒ neutralinos: mass eigenstates

mass matrix given in terms of  $M_1$ ,  $M_2$ ,  $\mu$ ,  $\tan \beta$

⇒ only one new parameter

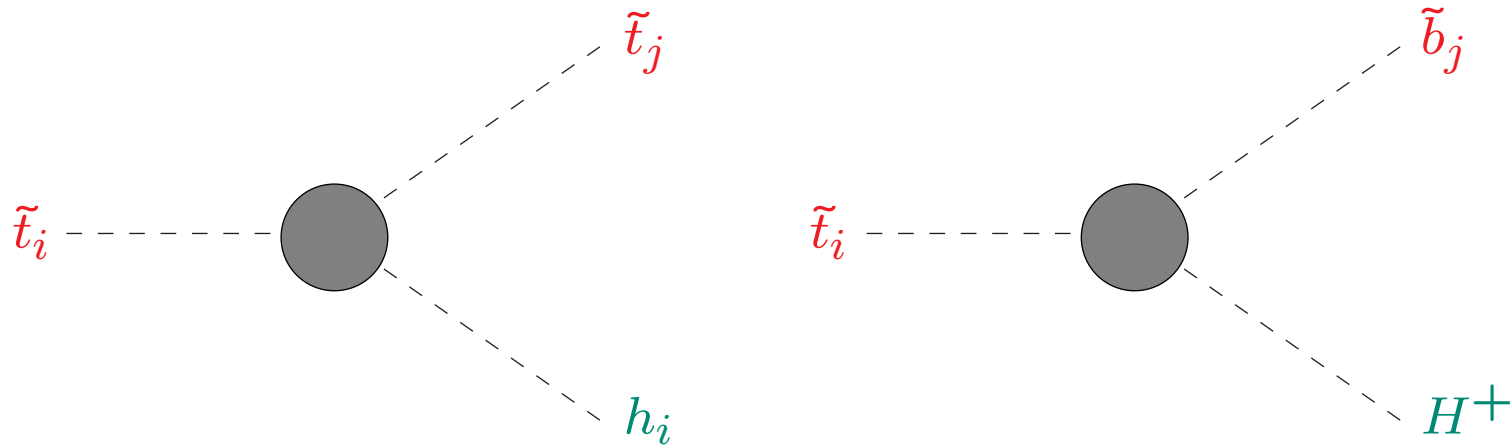
⇒ MSSM predicts mass relations between neutralinos and charginos

## Examples for processes with (external) stops and Higgs bosons:



- important decay modes of stops
- $A_t$  and  $A_b$  directly enter the vertex
- possible source of Higgs bosons at the LHC/ILC
- . . .

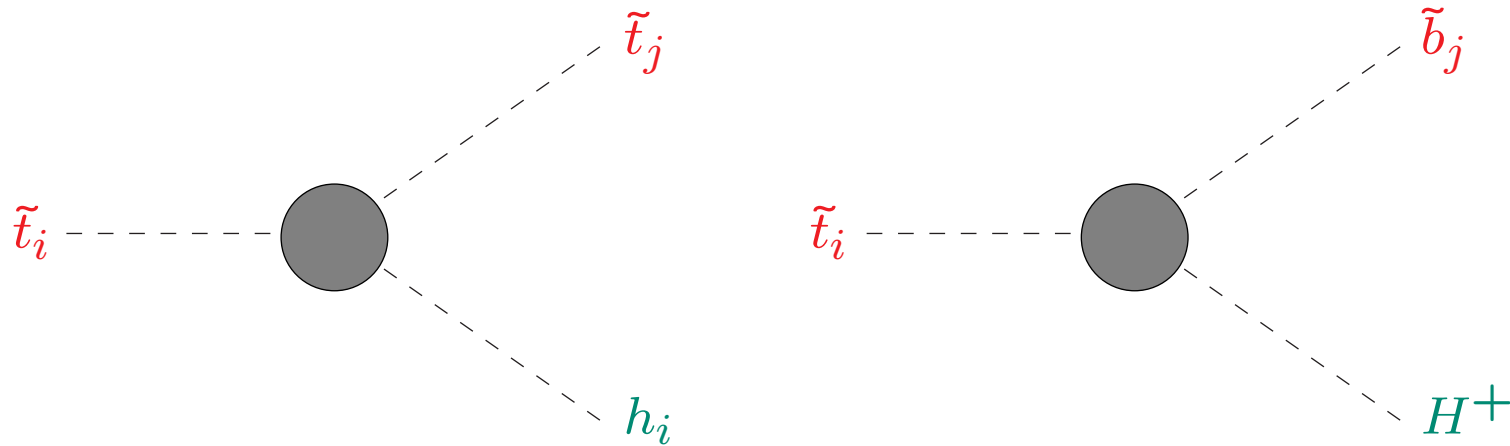
## Examples for processes with (external) stops and Higgs bosons:



- important decay modes of stops
- $A_t$  and  $A_b$  directly enter the vertex
- possible source of Higgs bosons at the LHC/ILC
- . . .

⇒ higher-order corrections important!

## Examples for processes with (external) stops and Higgs bosons:

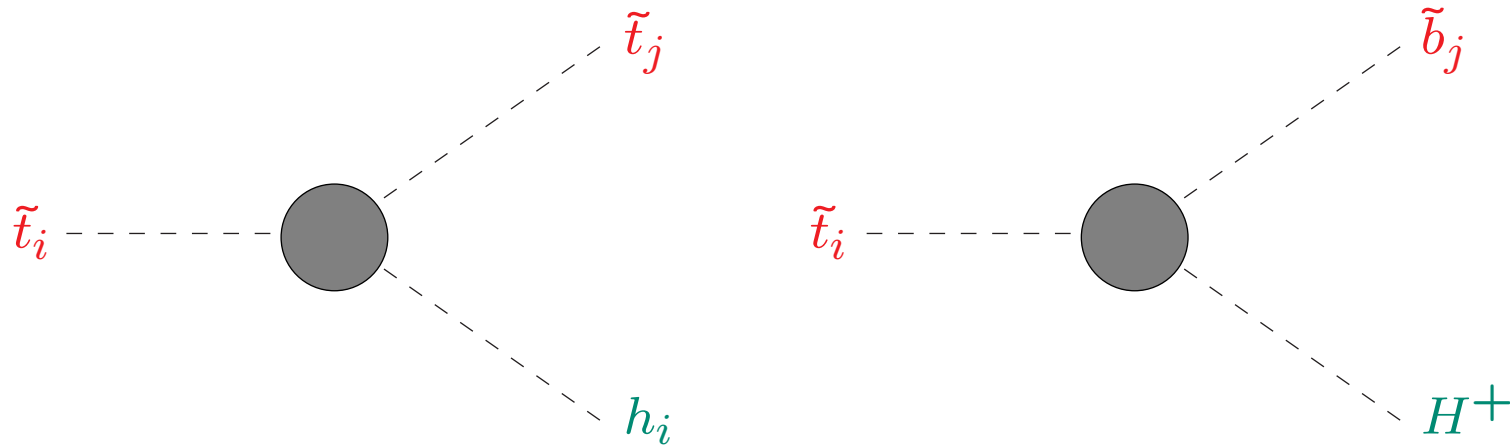


- important decay modes of stops
- $A_t$  and  $A_b$  directly enter the vertex
- possible source of Higgs bosons at the LHC/ILC
- . . .

⇒ higher-order corrections important!

⇒ simultaneous renormalization of stop and sbottom sector required!

## Examples for processes with (external) stops and Higgs bosons:



- important decay modes of stops
- $A_t$  and  $A_b$  directly enter the vertex
- possible source of Higgs bosons at the LHC/ILC
- . . .

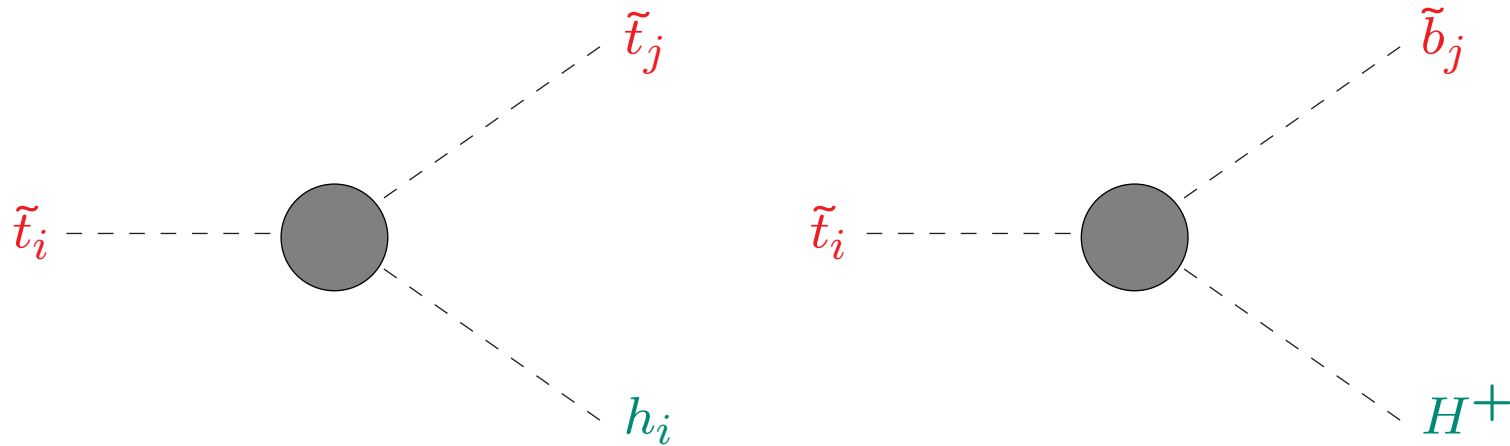
⇒ higher-order corrections important!

⇒ simultaneous renormalization of stop and sbottom sector required!

⇒ with on-shell properties for external particles!



## Examples for processes with (external) stops and Higgs bosons:



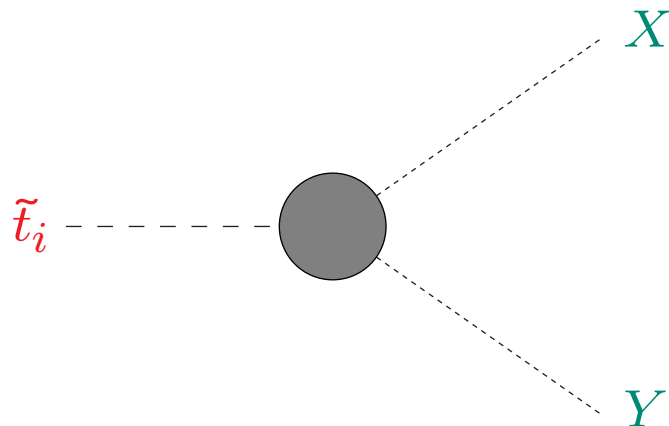
- important decay modes of stops
- $A_t$  and  $A_b$  directly enter the vertex **incl. complex phases!**
- possible source of Higgs bosons at the LHC/ILC
- . . .

⇒ higher-order corrections important!

⇒ simultaneous renormalization of stop and sbottom sector required!

⇒ including complex phases!

## The bigger picture: stop decays in the cMSSM

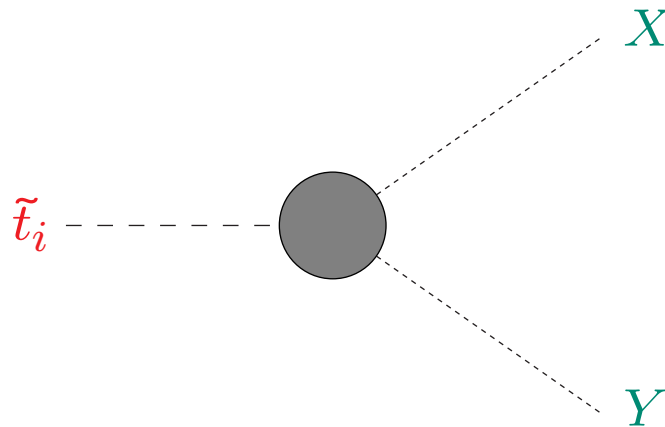


⇒ to get BRs right ⇒ all decays needed

⇒ (nearly) all sectors of the cMSSM enter as external particles

⇒ (nearly) all sectors of the cMSSM have to be renormalized simultaneously

## The bigger picture: stop decays in the cMSSM



⇒ to get BRs right ⇒ all decays needed

⇒ (nearly) all sectors of the cMSSM enter as external particles

⇒ (nearly) all sectors of the cMSSM have to be renormalized simultaneously

now ready:

- (heavy) stop, sbottom and stau decays ⇒ relevant for Higgs, LSP
- gluino decays
- (non-hadronic) chargino decays ⇒ relevant for Higgs, LSP
- (non-hadronic) neutralino decays ⇒ relevant for Higgs, LSP

⇒ combination of various tools and analyses:

- FeynArts/FormCalc for one-loop diagrams [T. Hahn et al.]
- MSSM counter term model file [T. Fritzsche et al. '07]
- LoopTools for numerical evaluation [T. Hahn]
- Renormalization: as usual the biggest issue
  - \* complex Higgs sector [M. Frank et al. '06]
  - \* (complex) stop/sbottom/stau sector [H. Rzehak et al. '04, '07][S.H. et al. '10, '12]
  - \* (complex) chargino/neutralino sector [T. Fritzsche et al. '11][A. Fowler et al. '10]  
[M. Drees et al. '11][A. Bharoucha et al. '12]
  - \* complex gluino sector

People used to choose the most convenient renormalization for their problem/sector

⇒ no longer possible

⇒ working FeynArts model file now ready!

[T. Fritzsche, T. Hahn, S.H., H. Rzehak, C. Schappacher '13]

– hard QED and QCD radiation

## 2. Renormalization schemes in the stop/sbottom sector

(“analogously” in the slepton sector!)

Generic parameter and field renormalization for scalar quarks:

$$\mathbf{D}_{\tilde{q}} = \mathbf{U}_{\tilde{q}} \mathbf{M}_{\tilde{q}} \mathbf{U}_{\tilde{q}}^\dagger \quad (\tilde{q} = \tilde{t}, \tilde{b})$$

$$\mathbf{U}_{\tilde{q}} \mathbf{M}_{\tilde{q}} \mathbf{U}_{\tilde{q}}^\dagger \rightarrow \mathbf{U}_{\tilde{q}} \mathbf{M}_{\tilde{q}} \mathbf{U}_{\tilde{q}}^\dagger + \mathbf{U}_{\tilde{q}} \delta \mathbf{M}_{\tilde{q}} \mathbf{U}_{\tilde{q}}^\dagger = \begin{pmatrix} m_{\tilde{q}1}^2 & Y_q \\ Y_q^* & m_{\tilde{q}2}^2 \end{pmatrix} + \begin{pmatrix} \delta m_{\tilde{q}1}^2 & \delta Y_q \\ \delta Y_q^* & \delta m_{\tilde{q}2}^2 \end{pmatrix}$$

$$\delta \mathbf{M}_{\tilde{q}12} = U_{\tilde{q}11}^* U_{\tilde{q}12} (\delta m_{\tilde{q}1}^2 - \delta m_{\tilde{q}2}^2) + U_{\tilde{q}11}^* U_{\tilde{q}22} \delta Y_q + U_{\tilde{q}12} U_{\tilde{q}21}^* \delta Y_q^*$$

$$\begin{pmatrix} \tilde{q}_1 \\ \tilde{q}_2 \end{pmatrix} \rightarrow \left( \mathbb{1} + \frac{1}{2} \delta \mathbf{Z}_{\tilde{q}} \right) \begin{pmatrix} \tilde{q}_1 \\ \tilde{q}_2 \end{pmatrix} \quad \text{with} \quad \delta \mathbf{Z}_{\tilde{q}} = \begin{pmatrix} \delta Z_{\tilde{q}11} & \delta Z_{\tilde{q}12} \\ \delta Z_{\tilde{q}21} & \delta Z_{\tilde{q}22} \end{pmatrix}$$

## Renormalization of the $t/\tilde{t}$ sector

→ employ the widely used **on-shell renormalization**

$$\delta m_t = \frac{1}{2} \widetilde{\text{Re}} \left\{ m_t \left[ \Sigma_t^L(m_t^2) + \Sigma_t^R(m_t^2) \right] + \left[ \Sigma_t^{SL}(m_t^2) + \Sigma_t^{SR}(m_t^2) \right] \right\}$$

$$\delta m_{\tilde{t}_i}^2 = \widetilde{\text{Re}} \Sigma_{\tilde{t}_{ii}}(m_{\tilde{t}_i}^2) \quad (i = 1, 2)$$

$$\delta Y_t = \frac{1}{2} \widetilde{\text{Re}} \left\{ \Sigma_{\tilde{t}_{12}}(m_{\tilde{t}_1}^2) + \Sigma_{\tilde{t}_{12}}(m_{\tilde{t}_2}^2) \right\} \quad [\text{W. Hollik, H. Rzehak '03}]$$

This defines the counter term for  $A_t$ :

$$\begin{aligned} \delta A_t = & \frac{1}{m_t} \left[ U_{\tilde{t}_{11}} U_{\tilde{t}_{12}}^* (\delta m_{\tilde{t}_1}^2 - \delta m_{\tilde{t}_2}^2) + U_{\tilde{t}_{11}} U_{\tilde{t}_{22}}^* \delta Y_t^* + U_{\tilde{t}_{12}}^* U_{\tilde{t}_{21}} \delta Y_t \right. \\ & \left. - (A_t - \mu^* \cot \beta) \delta m_t \right] + (\delta \mu^* \cot \beta - \mu^* \cot^2 \beta \delta \tan \beta) \end{aligned}$$

(with  $\delta \mu$  from chargino/neutralino sector,  $\delta \tan \beta$  from Higgs sector)

## Field renormalization for on-shell squarks ( $\tilde{t}$ , $\tilde{b}$ , ...):

### Diagonal $Z$ factors:

the real part of the residua of propagators is set to unity:

$$\widetilde{\text{Re}} \frac{\partial \widehat{\Sigma}_{\tilde{q}ii}(k^2)}{\partial k^2} \Big|_{k^2=m_{\tilde{q}_i}^2} = 0 \quad (i = 1, 2)$$

yielding

$$\text{Re} \delta Z_{\tilde{q}ii} = -\widetilde{\text{Re}} \frac{\partial \widehat{\Sigma}_{\tilde{q}ii}(k^2)}{\partial k^2} \Big|_{k^2=m_{\tilde{q}_i}^2} \quad \text{Im} \delta Z_{\tilde{q}ii} = 0 \quad (i = 1, 2)$$

### Off-diagonal $Z$ factors:

no transition from one squark to the other occurs:

$$\widetilde{\text{Re}} \widehat{\Sigma}_{\tilde{q}_{12}}(m_{\tilde{q}_1}^2) = 0 \quad \widetilde{\text{Re}} \widehat{\Sigma}_{\tilde{q}_{12}}(m_{\tilde{q}_2}^2) = 0$$

yielding

$$\delta Z_{\tilde{q}_{12}} = +2 \frac{\widetilde{\text{Re}} \widehat{\Sigma}_{\tilde{q}_{12}}(m_{\tilde{q}_2}^2) - \delta Y_q}{(m_{\tilde{q}_1}^2 - m_{\tilde{q}_2}^2)} \quad \delta Z_{\tilde{q}_{21}} = -2 \frac{\widetilde{\text{Re}} \widehat{\Sigma}_{\tilde{q}_{21}}(m_{\tilde{q}_1}^2) - \delta Y_q^*}{(m_{\tilde{q}_1}^2 - m_{\tilde{q}_2}^2)}$$

$$SU(2) \text{ relation} \Rightarrow M_{\tilde{t}_L} = M_{\tilde{b}_L}$$

“LL” soft SUSY-breaking term for  $\tilde{q} = \{\tilde{t}, \tilde{b}\}$ :

$$M_{\tilde{Q}_L}^2(\tilde{q}) = |U_{\tilde{q}_{11}}|^2 m_{\tilde{q}_1}^2 + |U_{\tilde{q}_{12}}|^2 m_{\tilde{q}_2}^2 - M_Z^2 c_{2\beta} (T_q^3 - Q_q s_W^2) - m_q^2$$

Keeping  $SU(2)$  relation at the **one-loop level** leads to a shift in the soft SUSY-breaking parameters

[A. Bartl, H. Eberl, K. Hidaka, S. Kraml, W. Majerotto, W. Porod, Y. Yamada '97, '98]

[A. Djouadi, P. Gambino, S.H., W. Hollik, C. Jünger, G. Weiglein '98]

$$M_{\tilde{Q}_L}^2(\tilde{b}) = M_{\tilde{Q}_L}^2(\tilde{t}) + \delta M_{\tilde{Q}_L}^2(\tilde{t}) - \delta M_{\tilde{Q}_L}^2(\tilde{b})$$

with

$$\begin{aligned} \delta M_{\tilde{Q}_L}^2(\tilde{q}) = & |U_{\tilde{q}_{11}}|^2 \delta m_{\tilde{q}_1}^2 + |U_{\tilde{q}_{12}}|^2 \delta m_{\tilde{q}_2}^2 - U_{\tilde{q}_{22}} U_{\tilde{q}_{12}}^* \delta Y_q - U_{\tilde{q}_{12}} U_{\tilde{q}_{22}}^* \delta Y_q^* - 2m_q \delta m_q \\ & + M_Z^2 c_{2\beta} Q_q \delta s_W^2 - (T_q^3 - Q_q s_W^2) (c_{2\beta} \delta M_Z^2 + M_Z^2 \delta c_{2\beta}) \end{aligned}$$

→ under control



## Renormalizations of the $b/\tilde{b}$ sector in the complex MSSM:

scheme	$m_{\tilde{b}_{1,2}}$	$m_b$	$A_b$	$Y_b$	name
analogous to the $t/\tilde{t}$ sector: "OS"	OS	OS	—	OS	RS1
" $m_b, A_b \overline{\text{DR}}$ "	OS	$\overline{\text{DR}}$	$\overline{\text{DR}}$	—	RS2
" $m_b, Y_b \overline{\text{DR}}$ "	OS	$\overline{\text{DR}}$	—	$\overline{\text{DR}}$	RS3
" $m_b \overline{\text{DR}}, Y_b \text{OS}$ "	OS	$\overline{\text{DR}}$	—	OS	RS4
" $A_b \overline{\text{DR}}, \text{Re}Y_b \text{OS}$ "	OS	—	$\overline{\text{DR}}$	$\text{Re}Y_b: \text{OS}$	RS5
" $A_b \text{vertex}, \text{Re}Y_b \text{OS}$ "	OS	—	vertex	$\text{Re}Y_b: \text{OS}$	RS6

"—" = dependent parameter

⇒ often very involved analytical dependences

→ more combinations possible

... also tested

... upcoming results remain unchanged

## Renormalization of the sbottom masses:

OS renormalization:

$$\delta m_{\tilde{b}_i}^2 = \widetilde{\text{Re}} \Sigma_{\tilde{b}_{ii}}(m_{\tilde{b}_i}^2) \quad (i = 1, 2)$$

## Renormalization of the bottom mass:

OS renormalization:

$$\delta m_b = \frac{1}{2} \widetilde{\text{Re}} \left\{ m_b \left[ \Sigma_b^L(m_b^2) + \Sigma_b^R(m_b^2) \right] + \left[ \Sigma_b^{SL}(m_b^2) + \Sigma_b^{SL}(m_b^2) \right] \right\}$$

$\overline{\text{DR}}$  renormalization:

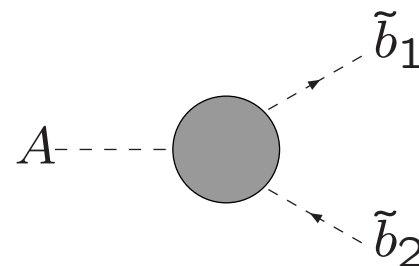
$$\delta m_b = \frac{1}{2} \widetilde{\text{Re}} \left\{ m_b \left[ \Sigma_b^L(m_b^2) + \Sigma_b^R(m_b^2) \right]_{\text{div}} + \left[ \Sigma_b^{SL}(m_b^2) + \Sigma_b^{SL}(m_b^2) \right]_{\text{div}} \right\}$$

## Renormalization of $A_b$ :

$\overline{\text{DR}}$  renormalization: analogous to  $A_t$ :

$$\begin{aligned}
 \delta A_b = & \frac{1}{m_b} \left[ U_{\tilde{b}_{11}} U_{\tilde{b}_{12}}^* \left( \widetilde{\text{Re}}\Sigma_{\tilde{b}_{11}}(m_{\tilde{b}_1}^2) |_{\text{div}} - \widetilde{\text{Re}}\Sigma_{\tilde{b}_{22}}(m_{\tilde{b}_2}^2) |_{\text{div}} \right) \right. \\
 & + \frac{1}{2} U_{\tilde{b}_{12}}^* U_{\tilde{b}_{21}} \left( \widetilde{\text{Re}}\Sigma_{\tilde{b}_{12}}(m_{\tilde{b}_1}^2) |_{\text{div}} + \widetilde{\text{Re}}\Sigma_{\tilde{b}_{12}}(m_{\tilde{b}_2}^2) |_{\text{div}} \right) \\
 & + \frac{1}{2} U_{\tilde{b}_{11}} U_{\tilde{b}_{22}}^* \left( \widetilde{\text{Re}}\Sigma_{\tilde{b}_{12}}(m_{\tilde{b}_1}^2) |_{\text{div}} + \widetilde{\text{Re}}\Sigma_{\tilde{b}_{12}}(m_{\tilde{b}_2}^2) |_{\text{div}} \right)^* \\
 & - \frac{1}{2} (A_b - \mu^* \tan \beta) \widetilde{\text{Re}} \left\{ m_b \left[ \Sigma_b^L(m_b^2) + \Sigma_b^R(m_b^2) \right] |_{\text{div}} \right. \\
 & \left. + \left[ \Sigma_b^{SL}(m_b^2) + \Sigma_b^{SR}(m_b^2) \right] |_{\text{div}} \right\} \left. \right] + \delta \mu^* |_{\text{div}} \tan \beta + \mu^* \delta \tan \beta
 \end{aligned}$$

Vertex renormalization:



$$\text{Diagram} \cong i \hat{\Lambda}(p_A^2, p_{\tilde{b}_1}^2, p_{\tilde{b}_2}^2)$$

$$\text{via } \widetilde{\text{Re}}\hat{\Lambda}(0, m_{\tilde{b}_1}^2, m_{\tilde{b}_1}^2) + \widetilde{\text{Re}}\hat{\Lambda}(0, m_{\tilde{b}_2}^2, m_{\tilde{b}_2}^2) \stackrel{!}{=} 0$$

## Renormalization of $Y_b$ :

OS renormalization:

$$\delta Y_b = \frac{1}{2} \widetilde{\text{Re}} \left\{ \Sigma_{\tilde{b}_{12}}(m_{\tilde{b}_1}^2) + \Sigma_{\tilde{b}_{12}}(m_{\tilde{b}_2}^2) \right\}$$

$\overline{\text{DR}}$  renormalization:

$$\delta Y_b = \frac{1}{2} \widetilde{\text{Re}} \left\{ \Sigma_{\tilde{b}_{12}}(m_{\tilde{b}_1}^2)|_{\text{div}} + \Sigma_{\tilde{b}_{12}}(m_{\tilde{b}_2}^2)|_{\text{div}} \right\}$$

$\text{Re}Y_b$  OS renormalization

$$\text{Re}\delta Y_b = \frac{1}{2} \text{Re} \left\{ \widetilde{\text{Re}}\Sigma_{\tilde{b}_{12}}(m_{\tilde{b}_1}^2) + \widetilde{\text{Re}}\Sigma_{\tilde{b}_{12}}(m_{\tilde{b}_2}^2) \right\}$$

## Existing analyses all in the **real MSSM**:

- [A. Bartl et al. '98] [L. Jin, C. Li '01]  
“OS” used for stop and sbottom decays  
(→ implemented into SDecay)
- [C. Weber, K. Kovarik, H. Eberl, W. Majerotto '07]  
similar to “ $m_b, A_b \overline{DR}$ ” used for Higgs decays to sfermions
- [A. Arhrib, R. Benbrik '04]  
an “OS” scheme used for  $\tilde{f} \rightarrow \tilde{f}'V$
- [Q. Li, L. Jin, C. Li '02]  
an “OS” scheme with running  $m_t, m_b, A_t, A_b$  used for  $\tilde{t}_2 \rightarrow \tilde{t}_1\phi$
- [H. Eberl et al. '10]  
pure  $\overline{DR}$  scheme used for stop decays
- [A. Brignole, G. Degrassi, P. Slavich and F. Zwirner '02]  
[S.H., W. Hollik, H. Rzehak, G. Weiglein '04]  
real “ $A_b$  vertex,  $\text{Re}Y_b$  OS” used for two-loop Higgs self-energies

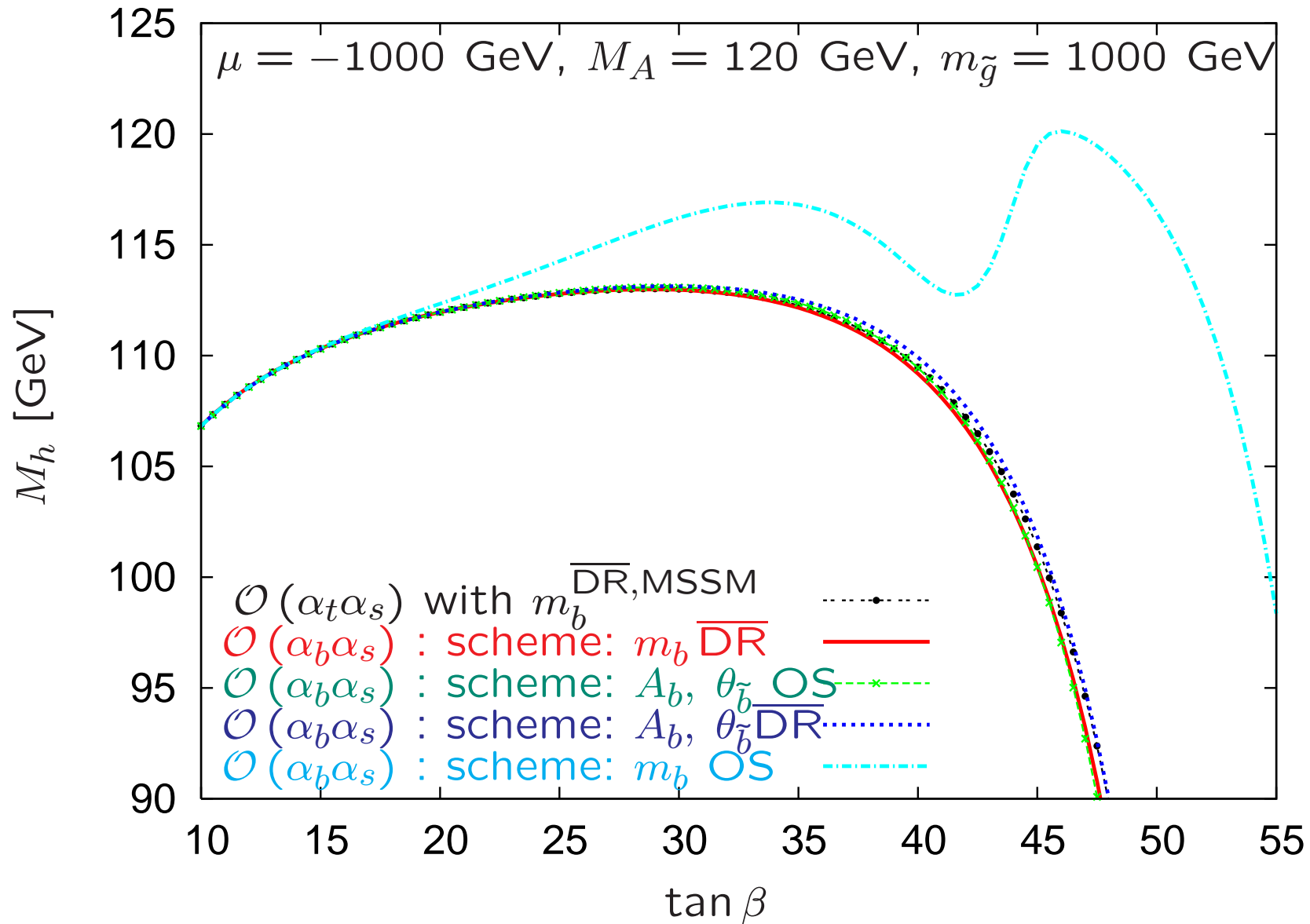
## Analysis of the renormalization schemes

Numerical scenarios:

Scen.	$M_{H^\pm}$	$m_{\tilde{t}_2}$	$\mu$	$A_t$	$A_b$	$M_1$	$M_2$	$M_3$
S1	150	600	200	900	400	200	300	800
S2	180	900	300	1800	1600	150	200	400

Scen.	$\tan \beta$	$m_{\tilde{t}_1}$	$m_{\tilde{t}_2}$	$m_{\tilde{b}_1}$	$m_{\tilde{b}_2}$
S1	2	293.391	600.000	441.987	447.168
	20	235.073	600.000	418.824	439.226
	50	230.662	600.000	400.815	449.638
S2	2	495.014	900.000	702.522	707.598
	20	445.885	900.000	678.531	695.180
	50	442.416	900.000	628.615	697.202

“OS” scheme:  $\delta A_b = \frac{1}{m_b} [-(A_b - \mu^* \tan \beta) \delta m_b + \dots]$

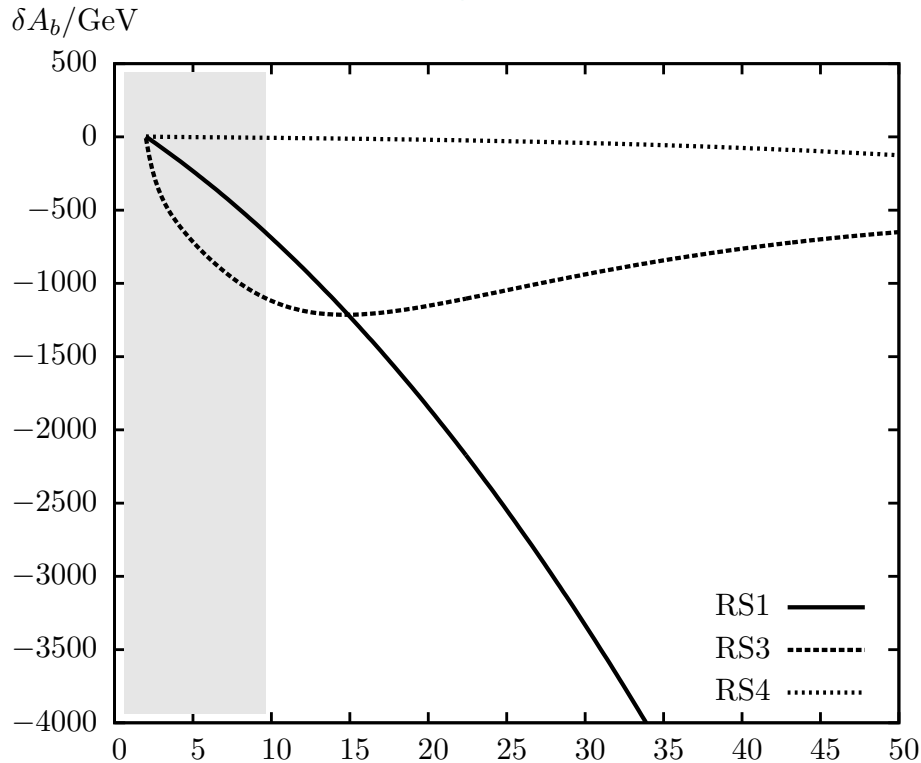


$\Rightarrow$  fails already for Higgs boson self-energies

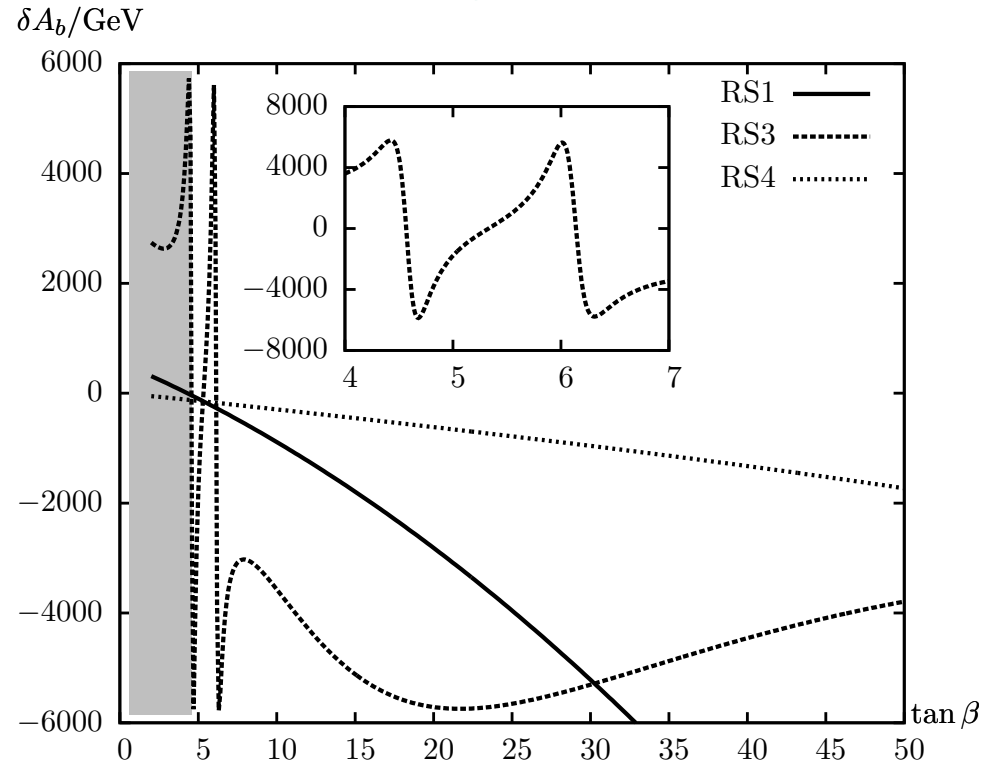
# Problems of non- $A_b$ renormalizations:

$$\delta A_b|_{\text{fin}} = \frac{1}{m_b} \left[ U_{\tilde{b}_{11}} U_{\tilde{b}_{12}}^* \left( \delta m_{\tilde{b}_1}^2 - \delta m_{\tilde{b}_2}^2 \right) \right]_{\text{fin}} + \dots$$

S1



S2



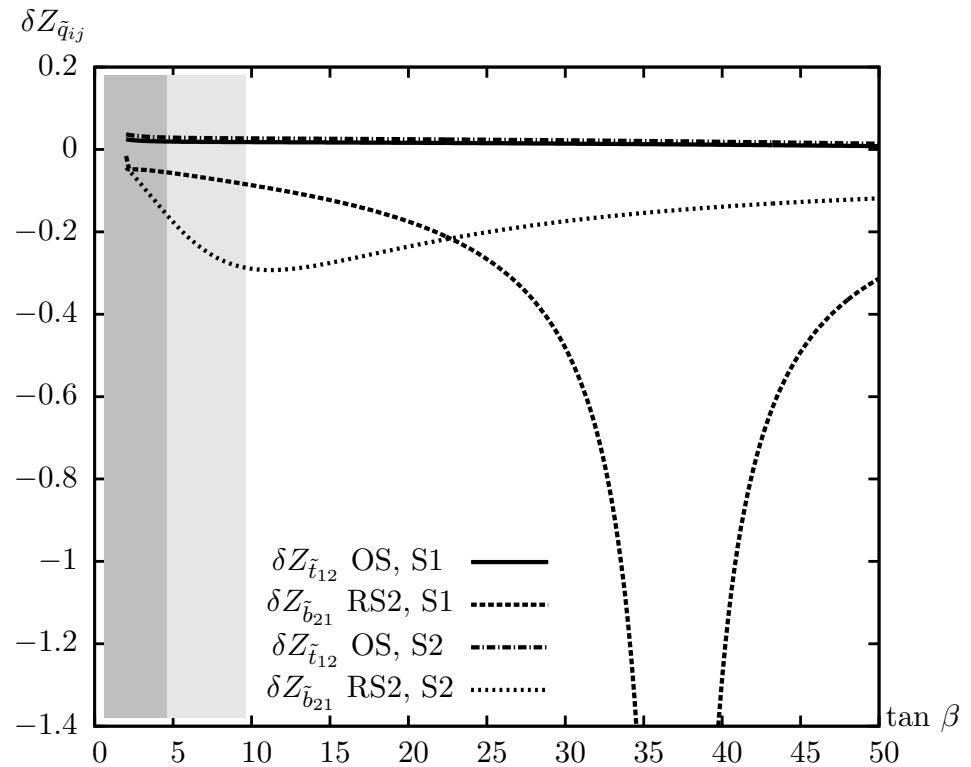
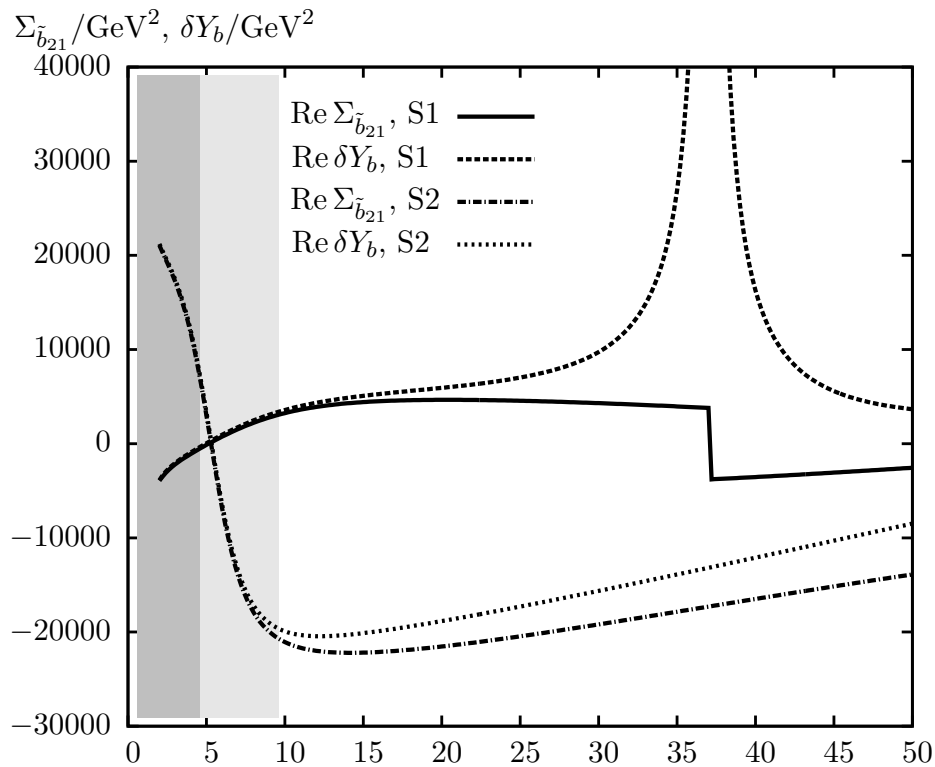
⇒ too large contributions to  $A_b$  are induced



# Problems of $m_b$ - $A_b$ renormalizations:

$$\delta Y_b = \frac{U_{\tilde{b}_{11}} U_{\tilde{b}_{21}}}{|U_{\tilde{b}_{11}}|^2 - |U_{\tilde{b}_{12}}|^2} \left( \delta m_{\tilde{b}_1}^2 - \delta m_{\tilde{b}_2}^2 \right) + \dots, \quad \delta Z_{\tilde{b}_{21}} = -2 \frac{\text{Re} \Sigma_{\tilde{b}_{21}}(m_{\tilde{b}_2}^2) - \delta Y_b}{m_{\tilde{b}_1}^2 - m_{\tilde{b}_2}^2}$$

$\Rightarrow$  divergence for  $|U_{\tilde{b}_{11}}| = |U_{\tilde{b}_{12}}|$  reached for  $\tan \beta \approx 37$  in S1:



## Problems of non- $m_b$ renormalizations:

“ $A_b$   $\overline{\text{DR}}$ ,  $\text{Re}Y_b$  OS” (RS5): (rMSSM)

$$\delta m_b = -\frac{m_b \delta A_b + \delta S}{(A_b - \mu \tan \beta)}$$

$\Rightarrow$  divergent for  $A_b = \mu \tan \beta$

“ $A_b$  vertex,  $\text{Re}Y_b$  OS” (RS6): (rMSSM)

$$\delta m_b = \frac{\delta S + F}{\mu (\tan \beta + 1/\tan \beta)}$$

$\Rightarrow$  no problem in the rMSSM!

“ $A_b$  vertex,  $\text{Re}Y_b$  OS” (RS6): (cMSSM:  $U_- = U_{\tilde{b}_{11}} U_{\tilde{b}_{22}}^* - U_{\tilde{b}_{12}} U_{\tilde{b}_{21}}^*$ )

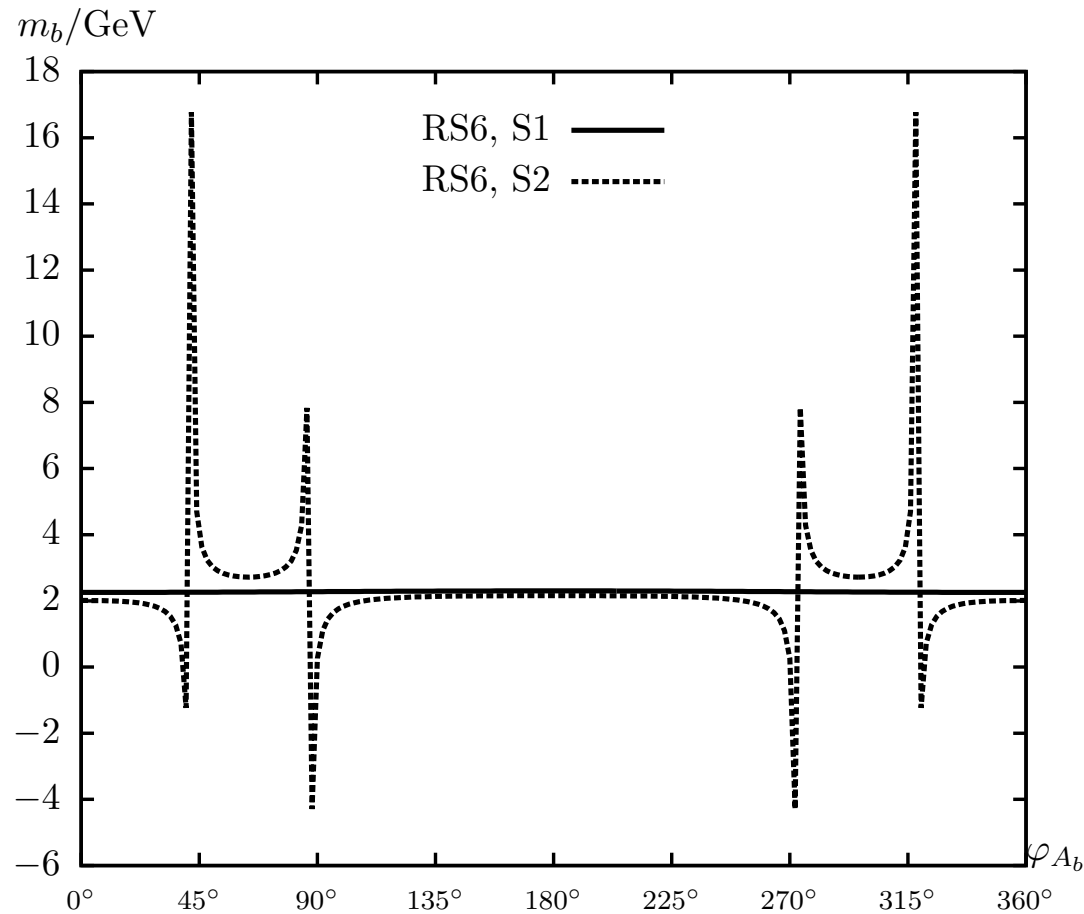
$$\frac{1}{\delta m_b} \sim 4 \mu \tan^3 \beta \left[ \text{Re} U_- \left( |U_{\tilde{b}_{11}}|^2 - |U_{\tilde{b}_{12}}|^2 \right) + \text{Im} U_- \frac{4 m_b}{m_{\tilde{b}_1}^2 - m_{\tilde{b}_2}^2} \text{Im} \left( U_{\tilde{b}_{11}}^* U_{\tilde{b}_{12}} A_b \right) \right]$$

$\Rightarrow$  divergences appear depending on  $\phi_{A_b}$ !

“ $A_b$  vertex,  $\text{Re}Y_b$  OS” (RS6): (cMSSM:  $U_- = U_{\tilde{b}_{11}} U_{\tilde{b}_{22}}^* - U_{\tilde{b}_{12}} U_{\tilde{b}_{21}}^*$ )

$$\frac{1}{\delta m_b} \sim 4 \mu \tan^3 \beta \left[ \text{Re} U_- \left( |U_{\tilde{b}_{11}}|^2 - |U_{\tilde{b}_{12}}|^2 \right) + \text{Im} U_- \frac{4 m_b}{m_{\tilde{b}_1}^2 - m_{\tilde{b}_2}^2} \text{Im} \left( U_{\tilde{b}_{11}}^* U_{\tilde{b}_{12}} A_b \right) \right]$$

$\Rightarrow$  divergences appear depending on  $\phi_{A_b}$ !



## What is the “preferred” renormalization scheme?

one counterterm is a “dependent” quantity

⇒ no scheme can be identified that shows “good” behavior over the full cMSSM parameter space

## What is the “preferred” renormalization scheme?

one counterterm is a “dependent” quantity

⇒ no scheme can be identified that shows “good” behavior over the full cMSSM parameter space

Most “robust” behavior:

- RS2: “ $m_b, A_b \overline{DR}$ ”  
⇒ problems only for maximal sbottom mixing
- RS6: “ $A_b$  vertex,  $\text{Re}Y_b$  OS”  
⇒ problems depending on  $\phi_{A_b}$

## What is the “preferred” renormalization scheme?

one counterterm is a “dependent” quantity

⇒ no scheme can be identified that shows “good” behavior over the full cMSSM parameter space

Most “robust” behavior:

- RS2: “ $m_b, A_b \overline{DR}$ ”  
⇒ problems only for maximal sbottom mixing
- RS6: “ $A_b$  vertex,  $\text{Re}Y_b$  OS”  
⇒ problems depending on  $\phi_{A_b}$

All problems could be avoided in a pure  $\overline{DR}$  scheme

⇒ not suited for external stops and sbottoms

## What is the “preferred” renormalization scheme?

one counterterm is a “dependent” quantity

⇒ no scheme can be identified that shows “good” behavior over the full cMSSM parameter space

Most “robust” behavior:

- RS2: “ $m_b, A_b \overline{\text{DR}}$ ”  
⇒ problems only for maximal sbottom mixing
- RS6: “ $A_b$  vertex,  $\text{Re}Y_b$  OS”  
⇒ problems depending on  $\phi_{A_b}$

All problems could be avoided in a pure  $\overline{\text{DR}}$  scheme

⇒ not suited for external stops and sbottoms

⇒ we choose RS2: “ $m_b, A_b \overline{\text{DR}}$ ” as our “preferred” scheme

### 3. Renormalization in the chargino/neutralino sector

⇒ Two “OS” schemes:

#### 1. Scheme I:

[T. Fritzsche, S.H., H. Rzehak, C. Schappacher '11][S.H., F. v.d. Pahlen, C. Schappacher '12]

$$\left( \left[ \widetilde{\mathbf{Re}}\widehat{\Sigma}_{\tilde{\chi}^-}(p) \right]_{ii} \tilde{\chi}_i^-(p) \right) \Big|_{p^2=m_{\tilde{\chi}_i^\pm}^2} = 0 \quad (i = 1, 2) ,$$
$$\left( \left[ \widetilde{\mathbf{Re}}\widehat{\Sigma}_{\tilde{\chi}^0}(p) \right]_{11} \tilde{\chi}_1^0(p) \right) \Big|_{p^2=m_{\tilde{\chi}_1^0}^2} = 0$$

#### 2. Scheme II:

[A. Fowler, G. Weiglein '09]

$$\left( \left[ \mathbf{Re}\widehat{\Sigma}_{\tilde{\chi}^-}(p) \right]_{ii} \tilde{\chi}_i^-(p) \right) \Big|_{p^2=m_{\tilde{\chi}_i^\pm}^2} = 0 \quad (i = 1, 2) ,$$
$$\left( \left[ \mathbf{Re}\widehat{\Sigma}_{\tilde{\chi}^0}(p) \right]_{11} \tilde{\chi}_1^0(p) \right) \Big|_{p^2=m_{\tilde{\chi}_1^0}^2} = 0$$

⇒ more details in Federico’s talk, Thursday 12.40pm



## Some comments:

– **Scheme I** and **Scheme II** agree for real parameters

– Both schemes can easily be extended to other variants, e.g.

$$\text{CCN}_i \ (i = 1, 2, 3, 4) \quad \text{or} \quad \text{CNN}_{ijk} \ (i = 1, 2; j, k = 1, 2, 3, 4)$$

→ relevant for  $|\mu| \approx M_2$  [*F. v.d. Pahlen et al., in progress*]

(see also: [*Drees et al. '11*] )

– Both schemes require a shift of three (neutralino) masses to their on-shell value:

$$\Delta m_{\tilde{\chi}_i^0} = -\frac{1}{2} \text{Re} \left\{ m_{\tilde{\chi}_i^0} \left( \hat{\Sigma}_{\tilde{\chi}_i^0}^L(m_{\tilde{\chi}_i^0}^2) + \hat{\Sigma}_{\tilde{\chi}_i^0}^R(m_{\tilde{\chi}_i^0}^2) \right) \right. \\ \left. + \hat{\Sigma}_{\tilde{\chi}_i^0}^{SL}(m_{\tilde{\chi}_i^0}^2) + \hat{\Sigma}_{\tilde{\chi}_i^0}^{SR}(m_{\tilde{\chi}_i^0}^2) \right\}$$

$$m_{\tilde{\chi}_i^0}^{\text{OS}} = m_{\tilde{\chi}_i^0} + \Delta m_{\tilde{\chi}_i^0}$$

## Comparison of the renormalization schemes

Parameters:

$\tan \beta$	$M_{H^\pm}$	$m_{\tilde{\chi}_2^\pm}$	$m_{\tilde{\chi}_1^\pm}$	$M_{\tilde{l}_L}$	$M_{\tilde{l}_R}$	$A_l$	$M_{\tilde{q}_L}$	$M_{\tilde{q}_R}$	$A_q$
20	160	600	350	300	310	400	1300	1100	2000

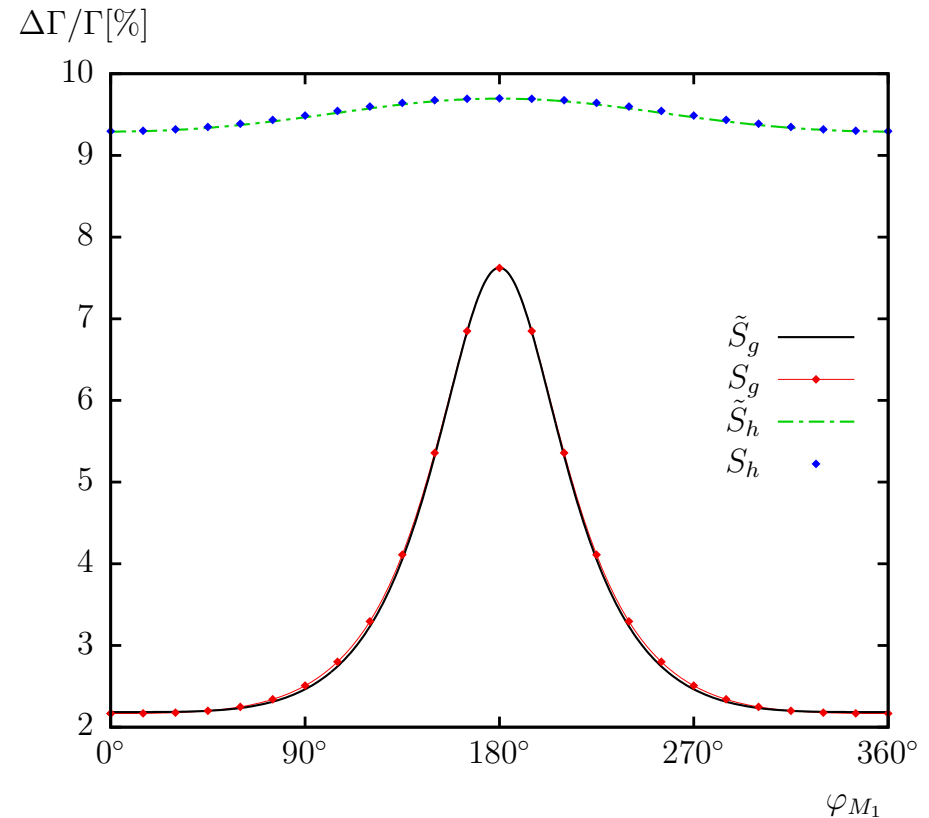
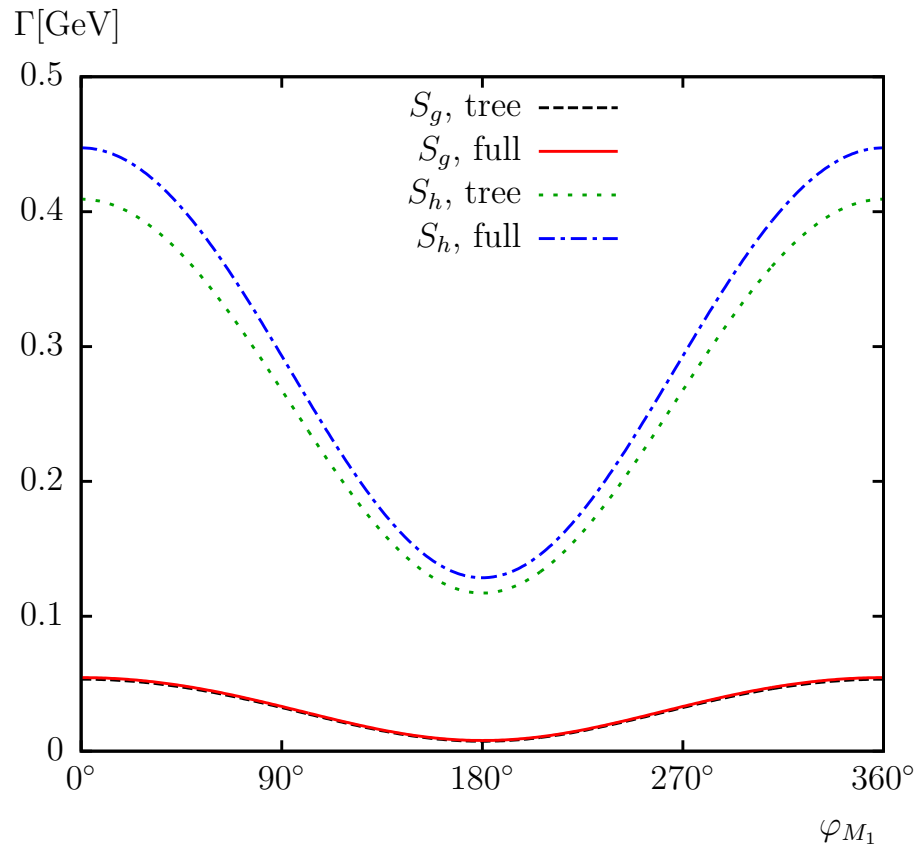
$$|M_1| = \frac{5}{3} \tan^2 \theta_w M_2 \approx \frac{1}{2} M_2$$

$\mathcal{S}_g : \mu > M_2$  ( $\tilde{\chi}_4^0$  more higgsino-like)  
 $\mathcal{S}_h : \mu < M_2$  ( $\tilde{\chi}_4^0$  more gaugino-like)

Scen.	$m_{\tilde{\chi}_2^\pm}$	$m_{\tilde{\chi}_1^\pm}$	$m_{\tilde{\chi}_4^0}$	$m_{\tilde{\chi}_3^0}$	$m_{\tilde{\chi}_2^0}$	$m_{\tilde{\chi}_1^0}$	$\mu$	$M_2$	$M_1$
$\mathcal{S}_g$	600.0	350.0	600.0	364.2	359.6	267.2	362.1	581.8	277.7
$\mathcal{S}_h$	600.0	350.0	600.1	586.2	349.9	171.4	581.8	362.1	172.8

# $\Gamma(\tilde{\chi}_4^0 \rightarrow \tilde{\chi}_1^0 h_1)$ : dependence on $\varphi_{M_1}$

[A. Bharoucha, S.H., F. v.d. Pahlen, C. Schappacher '12]

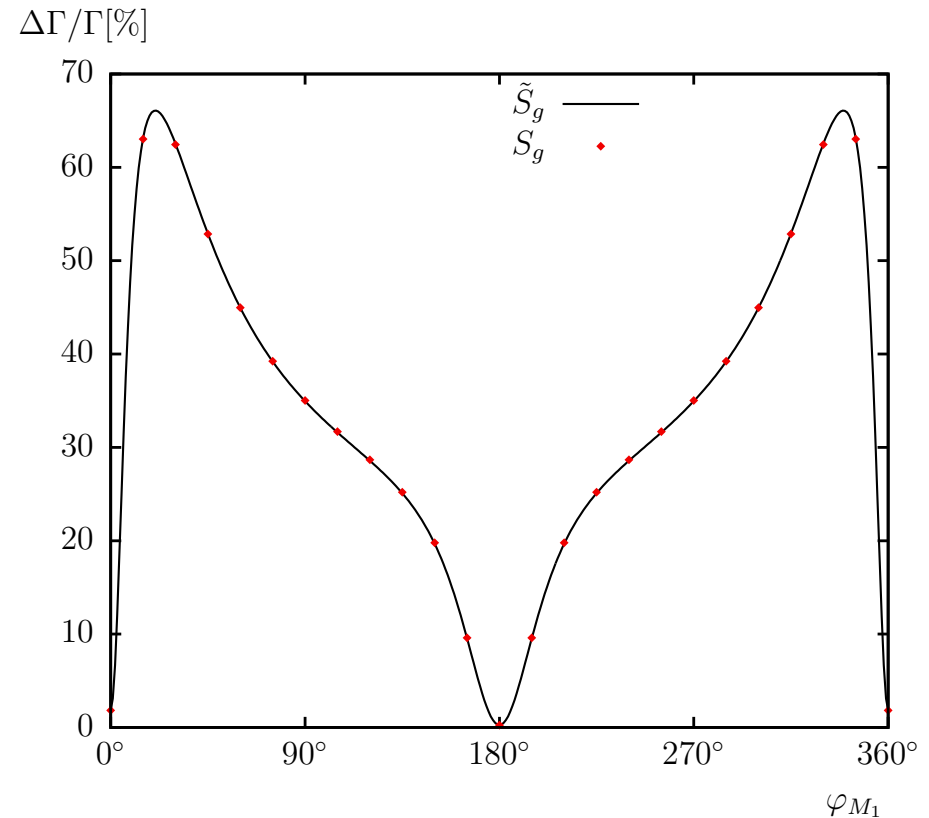
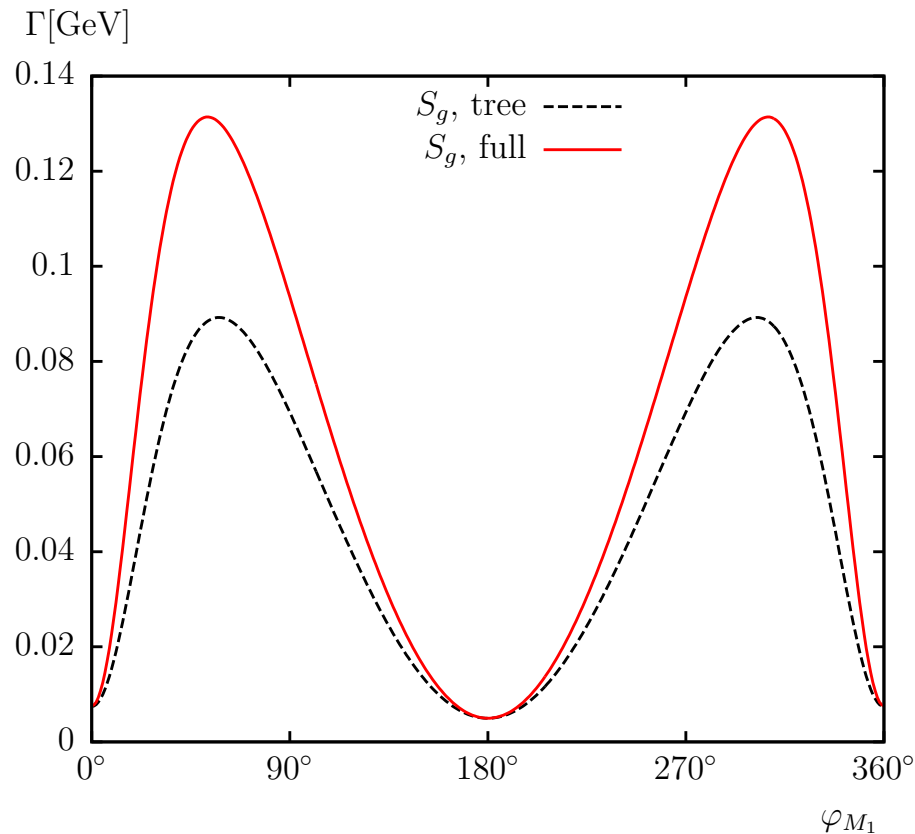


⇒ one-loop corrections under control and non-negligible

⇒ renormalization schemes agree (as expected)

# $\Gamma(\tilde{\chi}_4^0 \rightarrow \tilde{\chi}_3^0 h_1)$ : dependence on $\varphi_{M_1}$

[A. Bharoucha, S.H., F. v.d. Pahlen, C. Schappacher '12]

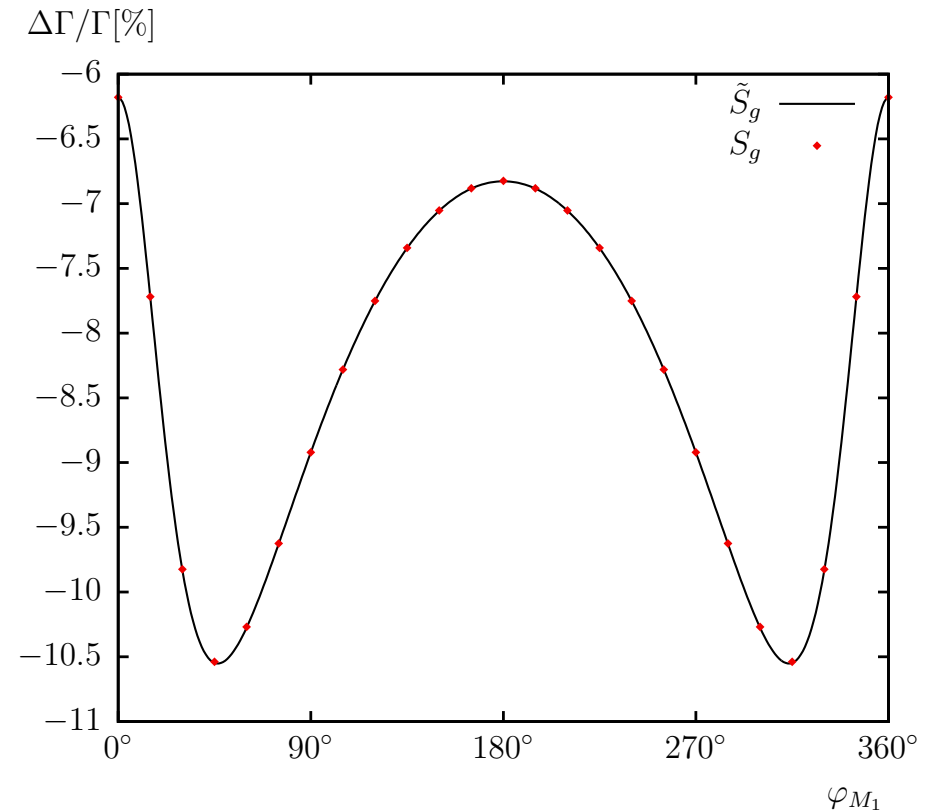
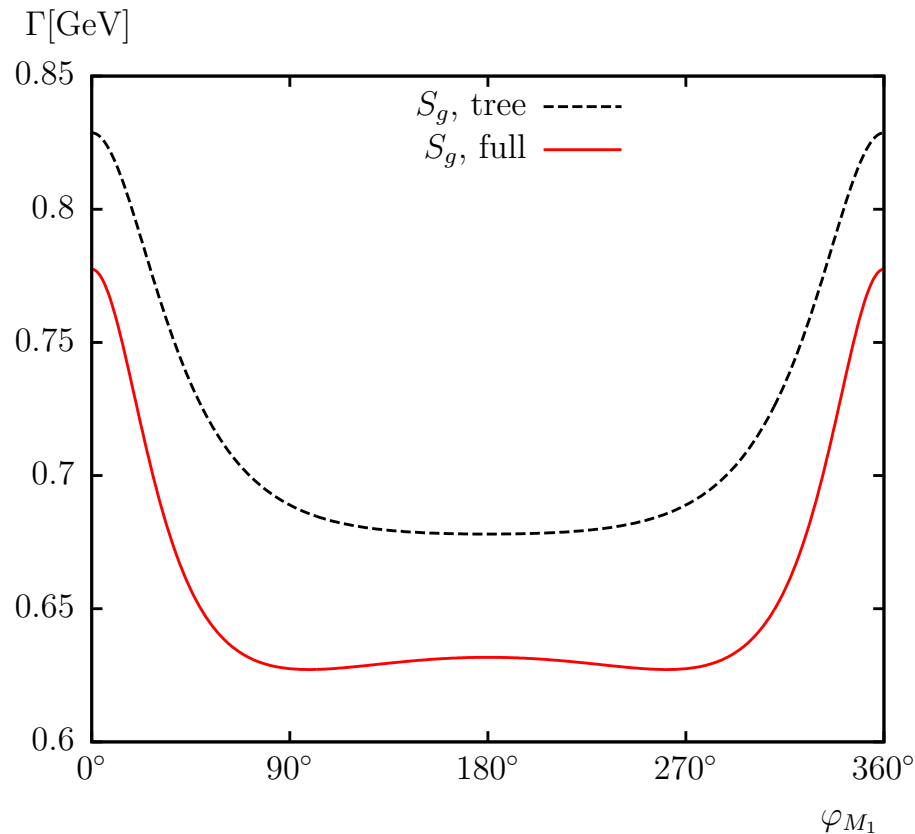


⇒ one-loop corrections under control and non-negligible

⇒ renormalization schemes agree (as expected)

# $\Gamma(\tilde{\chi}_4^0 \rightarrow \tilde{\chi}_3^0 Z)$ : dependence on $\varphi_{M_1}$

[A. Bharoucha, S.H., F. v.d. Pahlen, C. Schappacher '12]



⇒ one-loop corrections under control and non-negligible

⇒ renormalization schemes agree (as expected)

## 4. Some numerical examples

### 4A) Heavy Stop Decays

$$\Gamma(\tilde{t}_2 \rightarrow \tilde{t}_1 h_i) \quad (i = 1, 2, 3) ,$$

$$\Gamma(\tilde{t}_2 \rightarrow \tilde{t}_1 Z) ,$$

$$\Gamma(\tilde{t}_2 \rightarrow t \tilde{\chi}_k^0) \quad (k = 1 \dots 4) ,$$

$$\Gamma(\tilde{t}_2 \rightarrow t \tilde{g}) ,$$

$$\Gamma(\tilde{t}_2 \rightarrow \tilde{b}_i H^+) \quad (i = 1, 2) ,$$

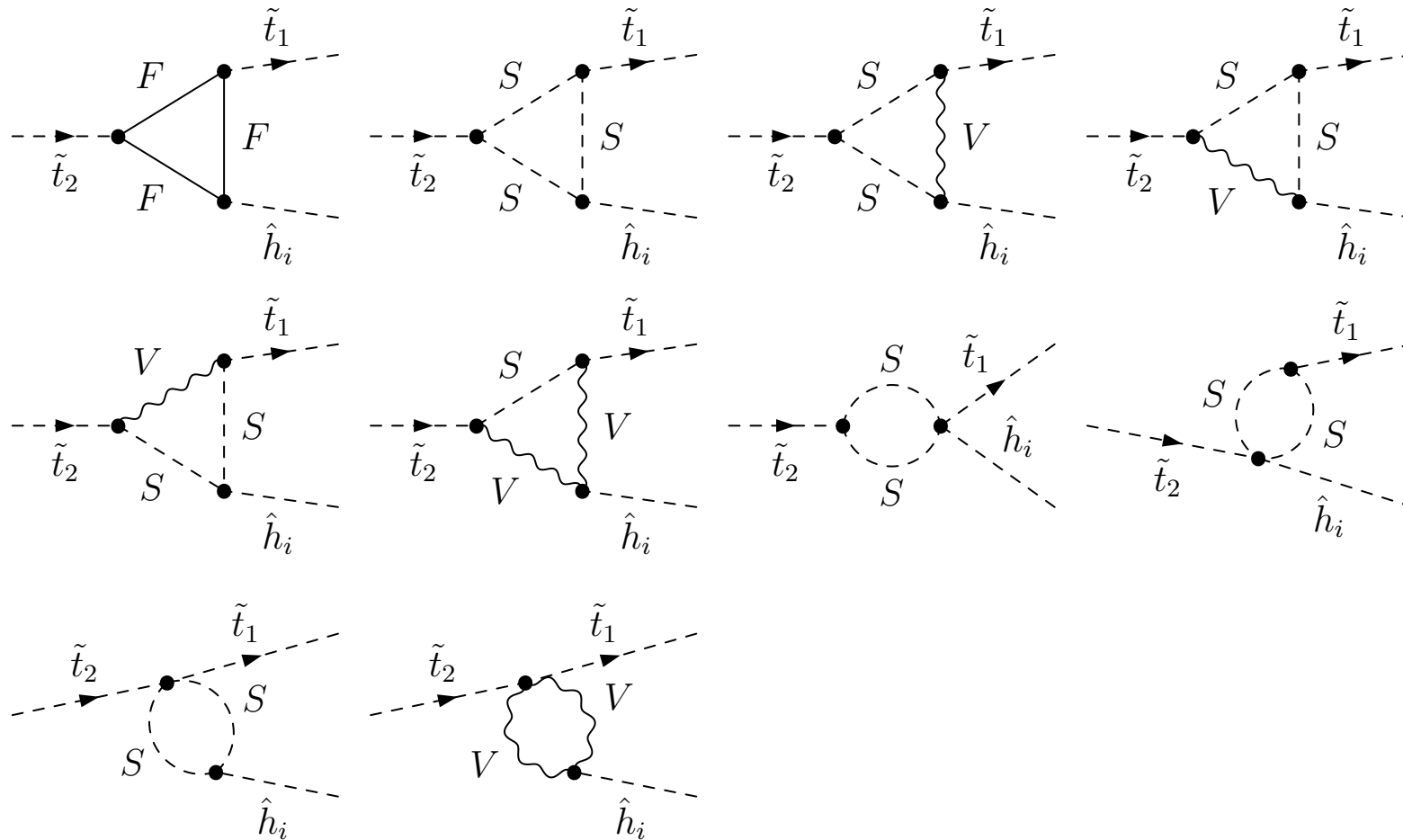
$$\Gamma(\tilde{t}_2 \rightarrow \tilde{b}_i W^+) \quad (i = 1, 2) ,$$

$$\Gamma(\tilde{t}_2 \rightarrow b \tilde{\chi}_k^+) \quad (k = 1, 2) .$$

## Calculation of partial widths and branching ratios:

- all diagrams created with **FeynArts** → TT
- model file with all counterterms in the cMSSM
- including all soft/hard QED/QCD diagrams
- further evaluation with **FormCalc**
- Dimensional **REDuction**
- all **UV** and **IR** divergences cancel
- results will be included into **FeynHiggs** ([www.feynhiggs.de](http://www.feynhiggs.de))
- example plots will focus on  $BR(\tilde{t}_2 \rightarrow \tilde{t}_1 h_1)$ ,  $BR(\tilde{t}_2 \rightarrow t \tilde{\chi}_1^0)$

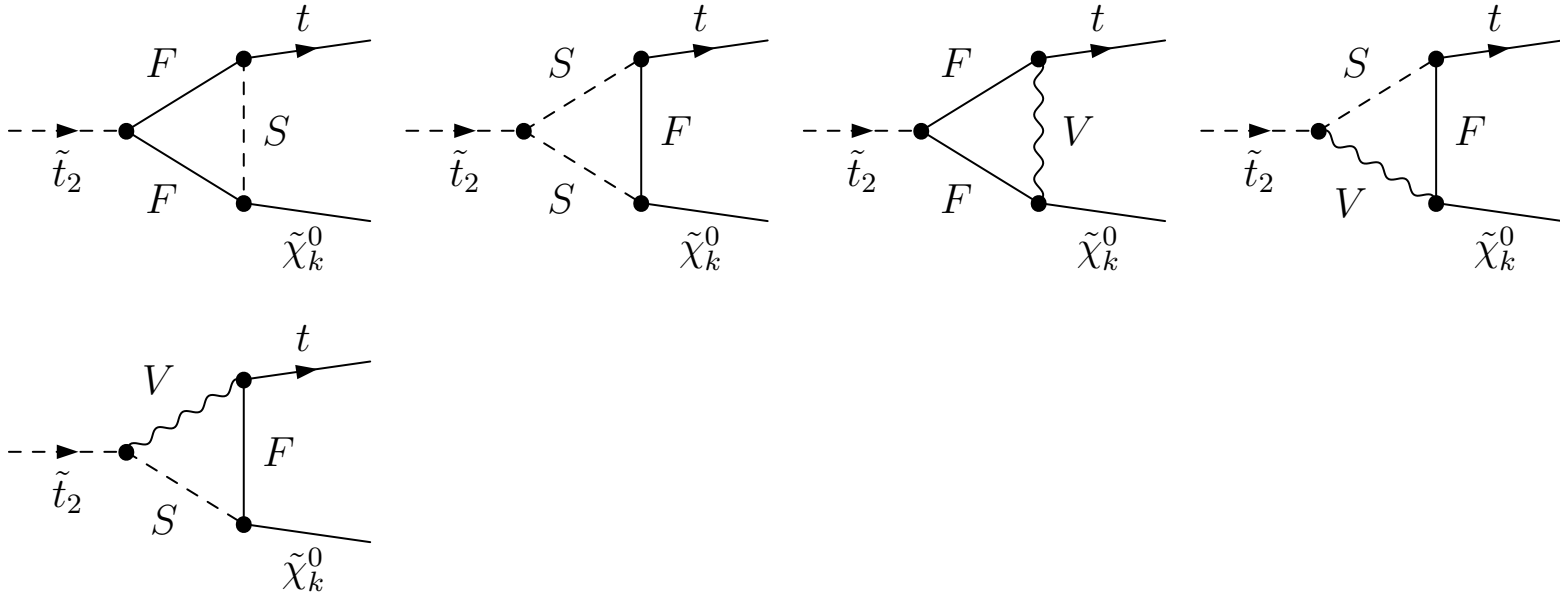
# Feynman diagrams for $\tilde{t}_2 \rightarrow \tilde{t}_1 h_i$



- including  $Z$ – $A$  or  $G$ – $A$  transition contribution on the external Higgs boson leg
- including all soft/hard QED/QCD diagrams



# Feynman diagrams for $\tilde{t}_2 \rightarrow t\tilde{\chi}_1^0$



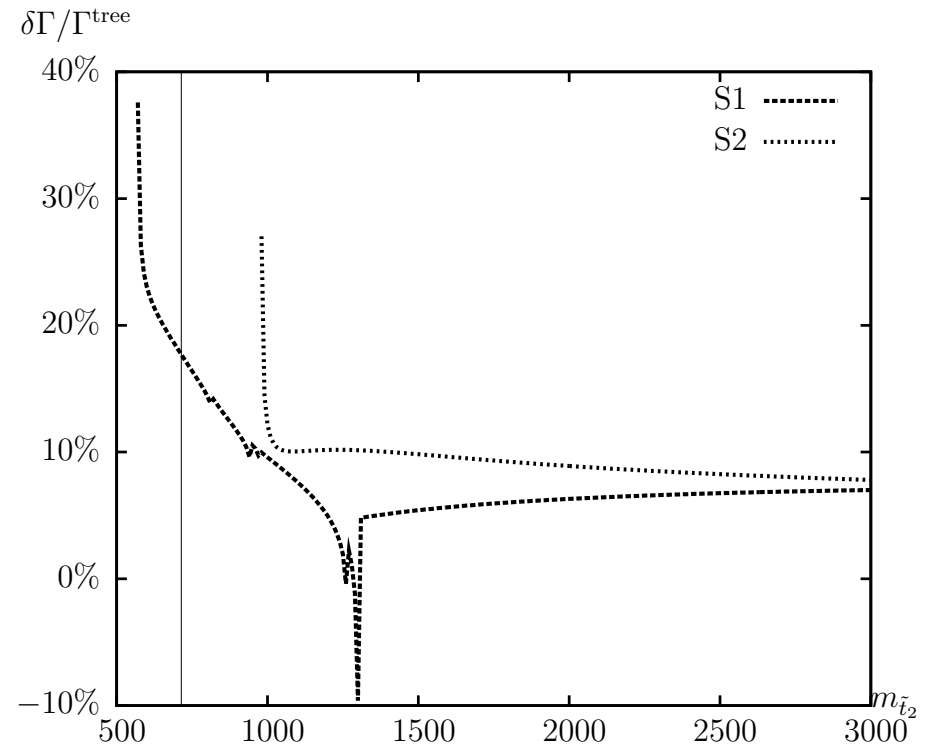
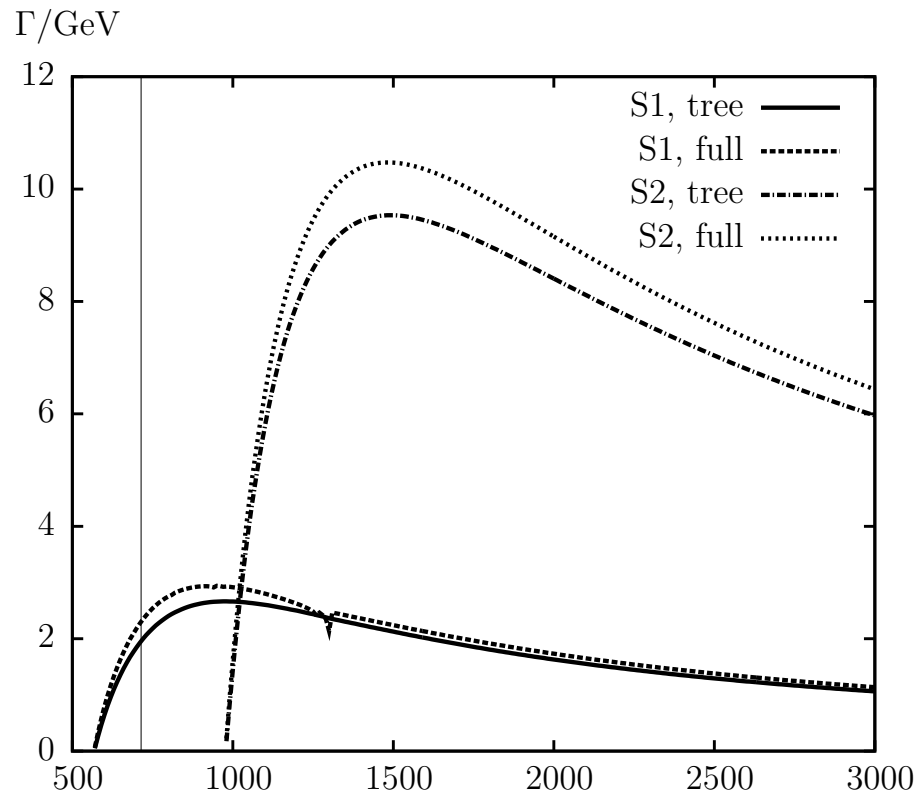
– including all soft/hard QED/QCD diagrams

## Numerical scenarios:

Scen.	$M_{H^\pm}$	$m_{\tilde{t}_2}$	$m_{\tilde{t}_1}$	$m_{\tilde{b}_2}$	$\mu$	$A_t$	$A_b$	$M_1$	$M_2$	$M_3$
S1	150	650	$0.4 m_{\tilde{t}_2}$	$0.7 m_{\tilde{t}_2}$	200	900	400	200	300	800
S2	180	1200	$0.6 m_{\tilde{t}_2}$	$0.8 m_{\tilde{t}_2}$	300	1800	1600	150	200	400

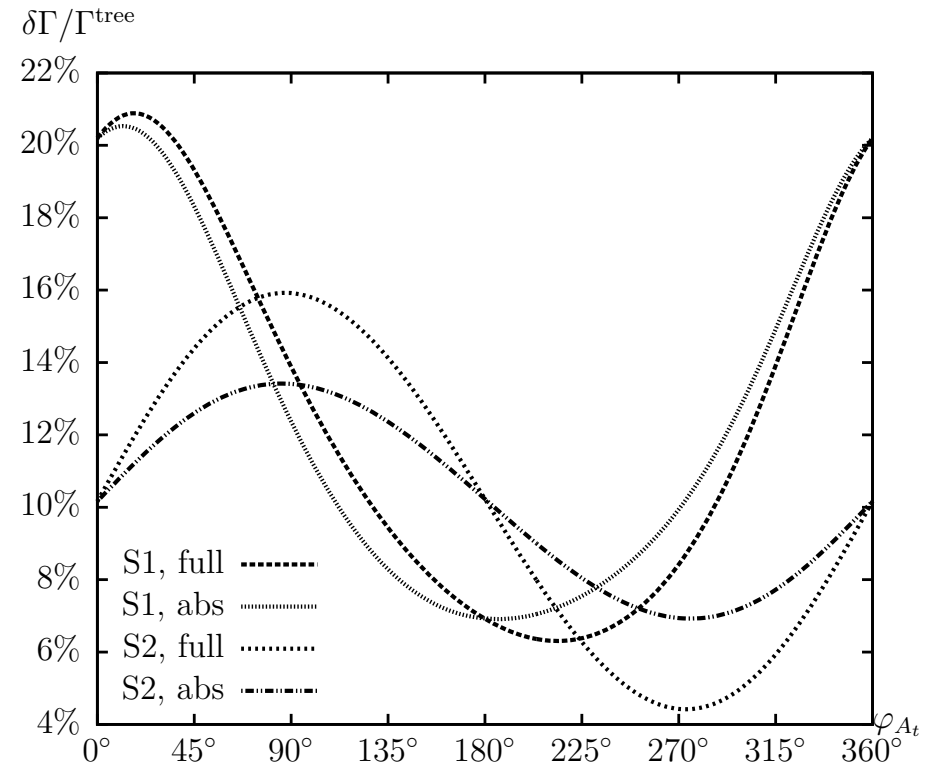
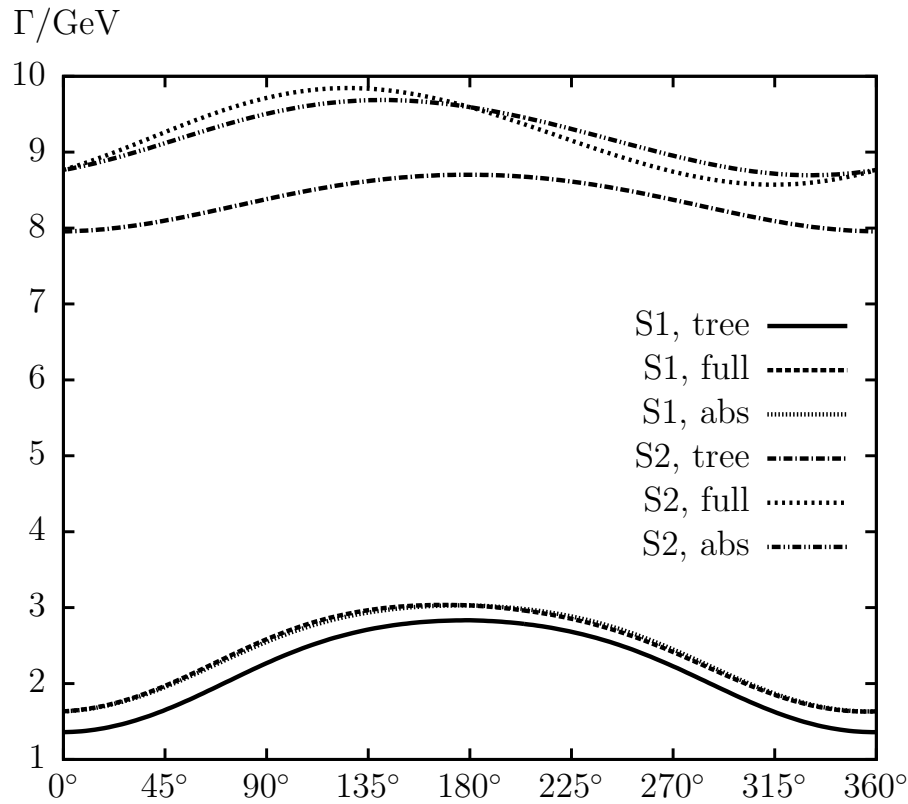
Scen.	$\tan \beta$	$m_{\tilde{t}_1}$	$m_{\tilde{t}_2}$	$m_{\tilde{b}_1}$	$m_{\tilde{b}_2}$
S1	2	260.000	650.000	305.436	455.000
	20	260.000	650.000	333.572	455.000
	50	260.000	650.000	329.755	455.000
S2	2	720.000	1200.000	769.801	960.000
	20	720.000	1200.000	783.300	960.000
	50	720.000	1200.000	783.094	960.000

Scenarios chosen such that *all* decay channels are open



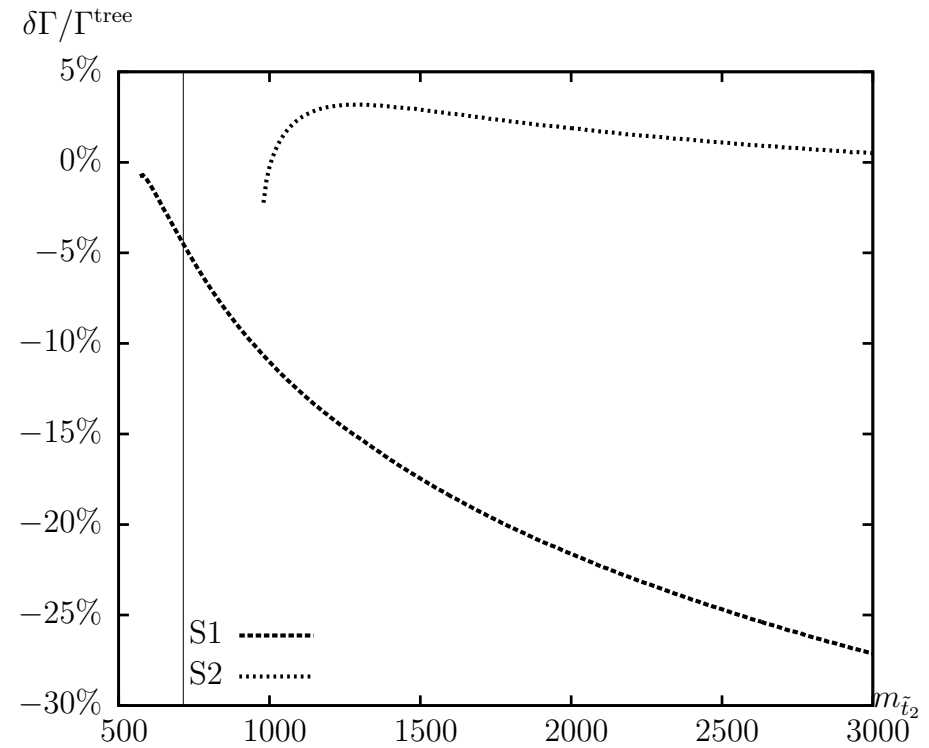
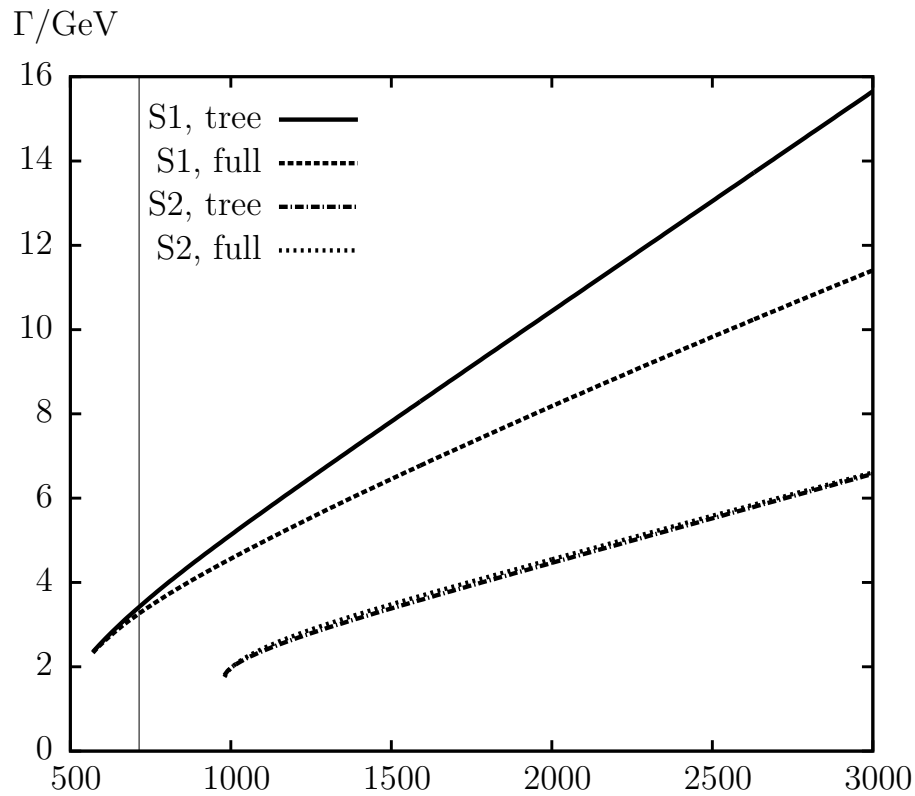
⇒ one-loop corrections under control and non-negligible

⇒ size of BR highly scenario dependent



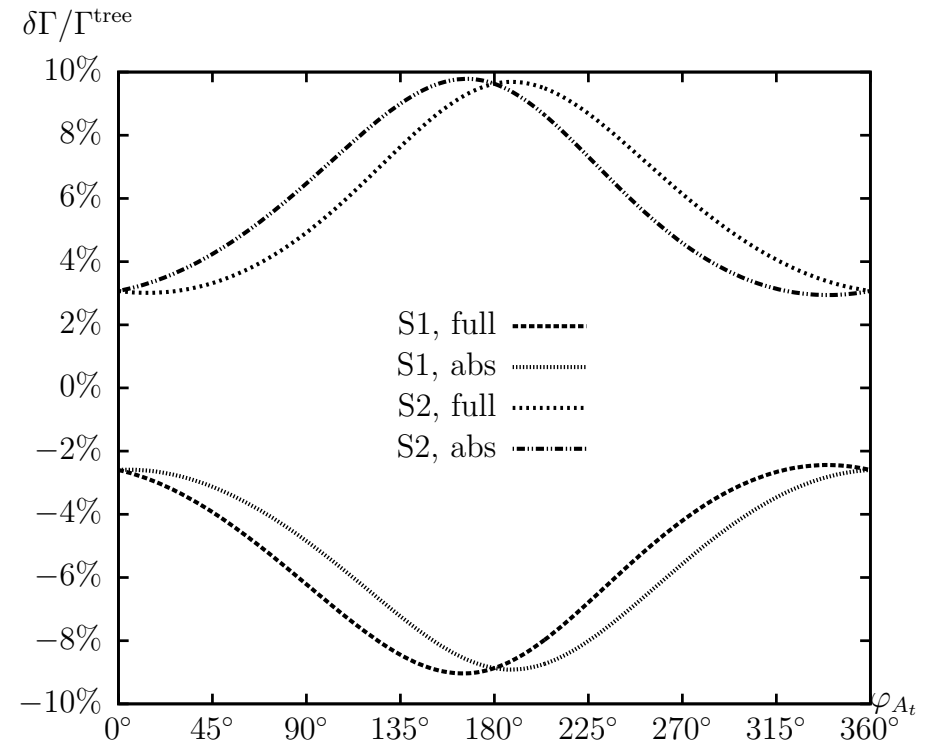
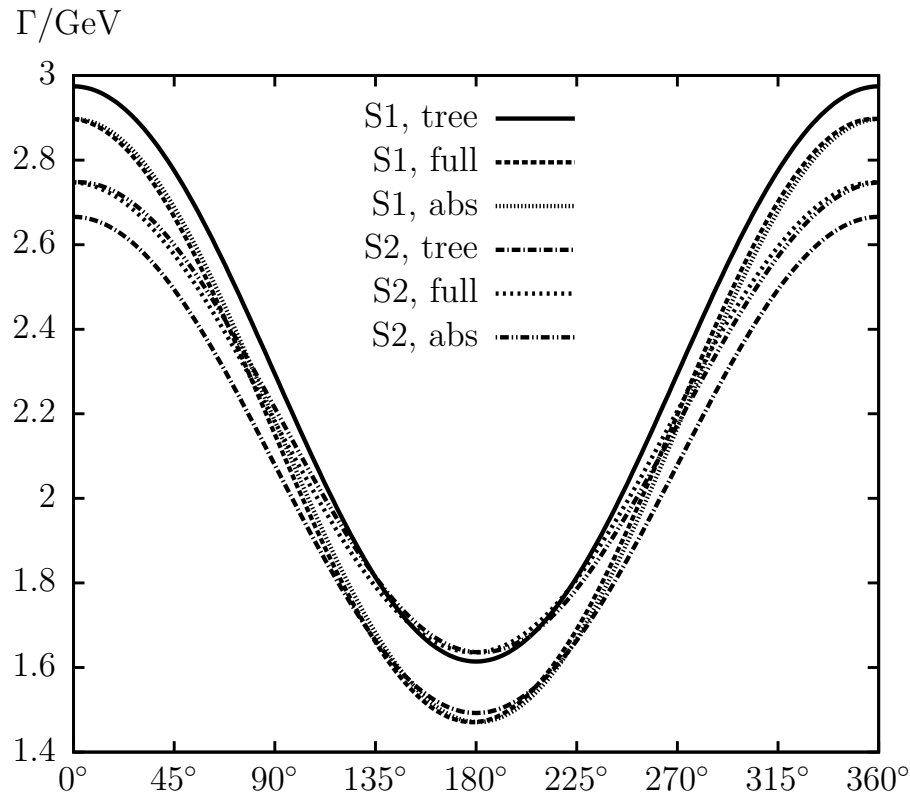
⇒ one-loop corrections under control and non-negligible

⇒ size of BR highly scenario dependent



⇒ one-loop corrections under control and non-negligible

⇒ size of BR highly scenario dependent



⇒ one-loop corrections under control and non-negligible

⇒ size of BR highly scenario dependent

## 4B) Chargino decays

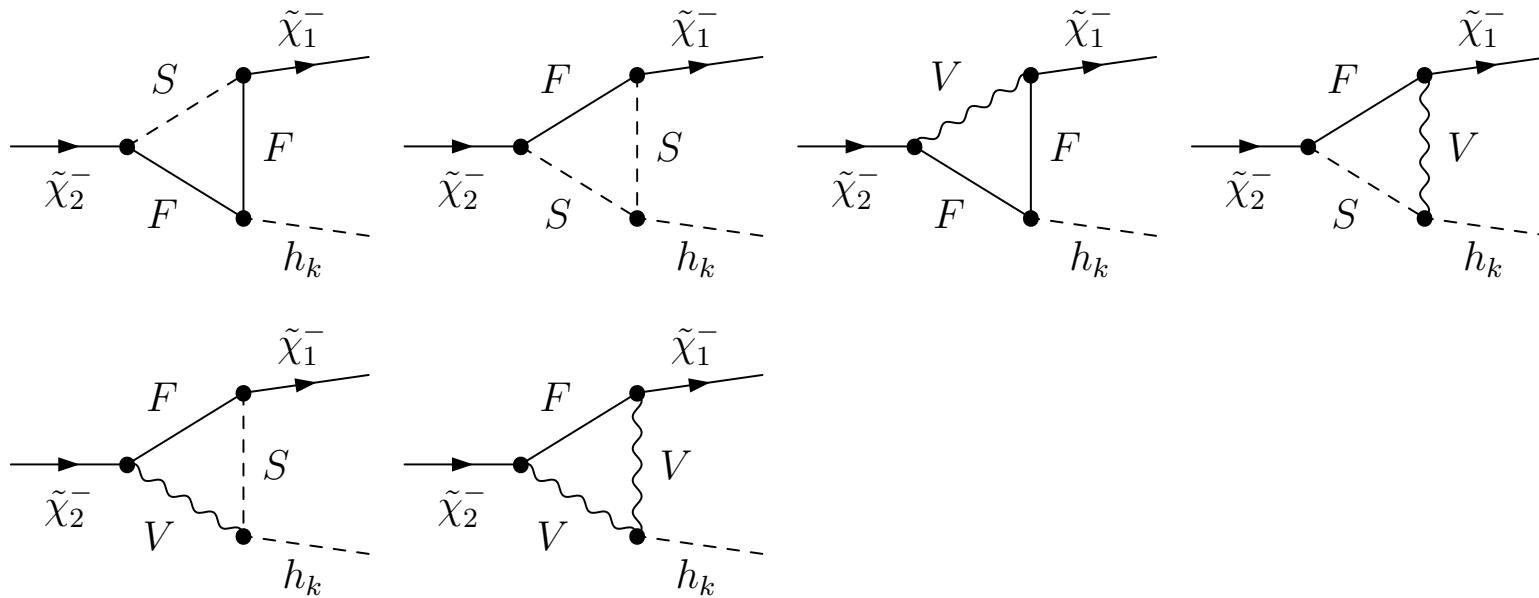
$$\begin{aligned}
 & \Gamma(\tilde{\chi}_2^\pm \rightarrow \tilde{\chi}_1^\pm h_k) && (k = 1, 2, 3) , \\
 & \Gamma(\tilde{\chi}_2^\pm \rightarrow \tilde{\chi}_1^\pm Z) , \\
 & \Gamma(\tilde{\chi}_i^\pm \rightarrow \tilde{\chi}_j^0 H^\pm) && (i = 1, 2, j = 1, 2, 3, 4) , \\
 & \Gamma(\tilde{\chi}_i^\pm \rightarrow \tilde{\chi}_j^0 W^\pm) && (i = 1, 2, j = 1, 2, 3, 4) , \\
 & \Gamma(\tilde{\chi}_i^\pm \rightarrow \tilde{l}_k^\pm \nu_l) && (i = 1, 2, l = e, \mu, \tau, k = 1, 2) , \\
 & \Gamma(\tilde{\chi}_i^\pm \rightarrow \tilde{\nu}_l l^\pm) && (i = 1, 2, l = e, \mu, \tau) .
 \end{aligned}$$

No hadronic decays yet . . .

Scen.	$\tan \beta$	$M_{H^\pm}$	$m_{\tilde{\chi}_2^\pm}$	$m_{\tilde{\chi}_1^\pm}$	$M_{\tilde{l}_L}$	$M_{\tilde{l}_R}$	$A_l$
$S$	20	160	650	350	300	310	400

$$\begin{aligned}
 S_{>} & : \mu > M_2 && (\tilde{\chi}_2^\pm \text{ more higgsino-like}) \\
 S_{<} & : \mu < M_2 && (\tilde{\chi}_2^\pm \text{ more gaugino-like})
 \end{aligned}$$

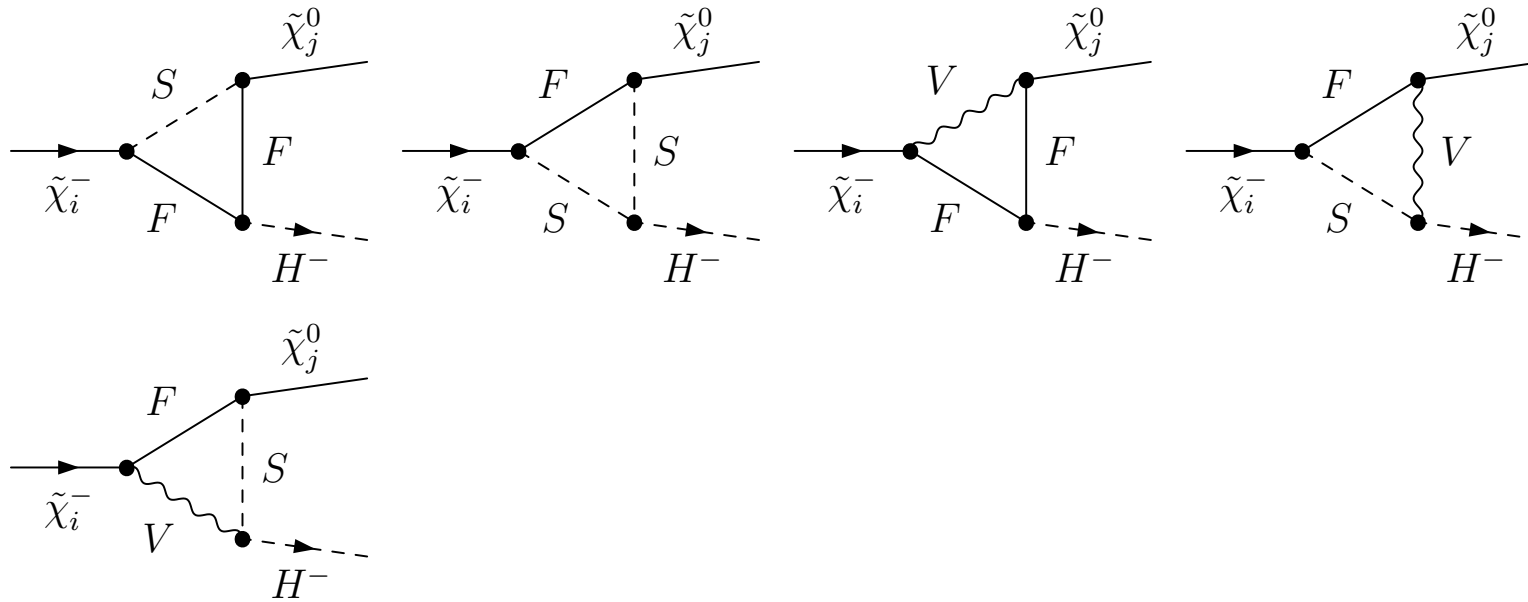
# Feynman diagrams for $\tilde{\chi}_2^- \rightarrow \tilde{\chi}_1^- h_k$



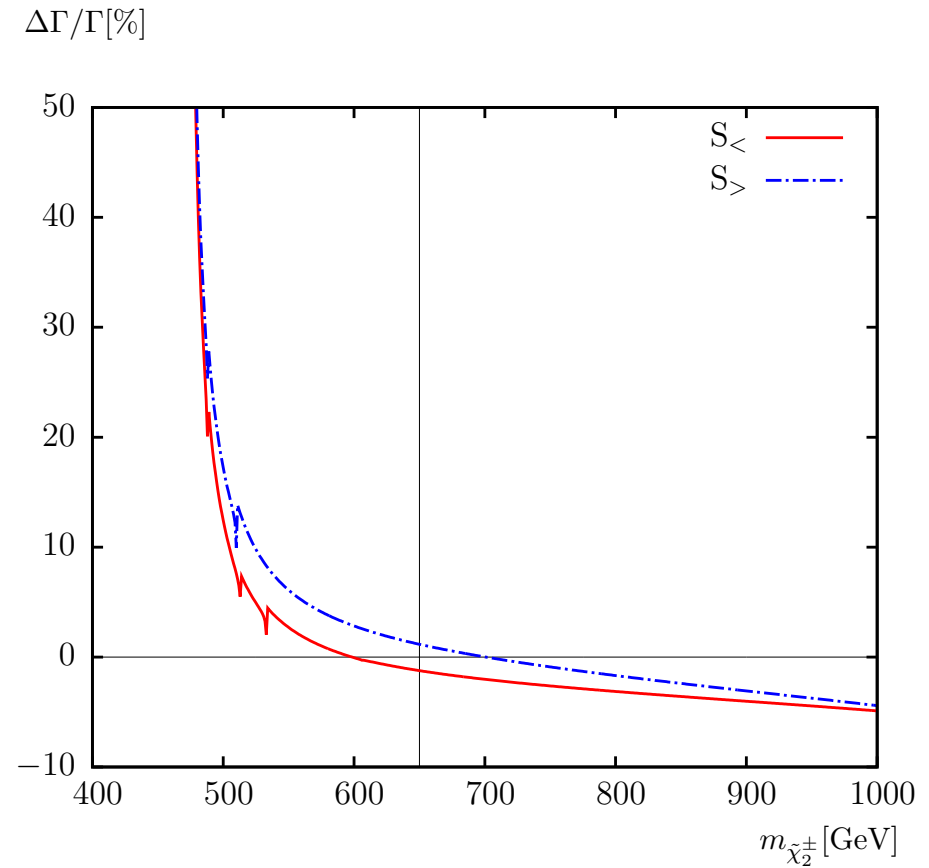
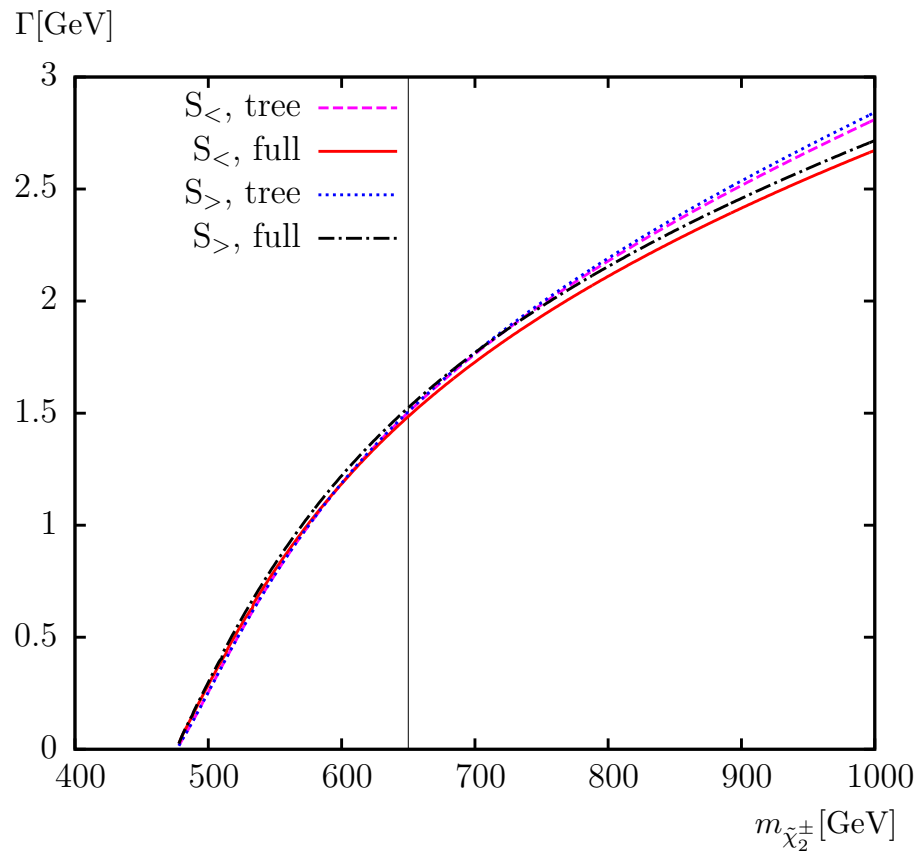
- including  $Z-A$  or  $G-A$  transition contribution on the external Higgs boson leg
- including all soft/hard QED/QCD diagrams



# Feynman diagrams for $\tilde{\chi}_i^- \rightarrow \tilde{\chi}_j^0 H^-$

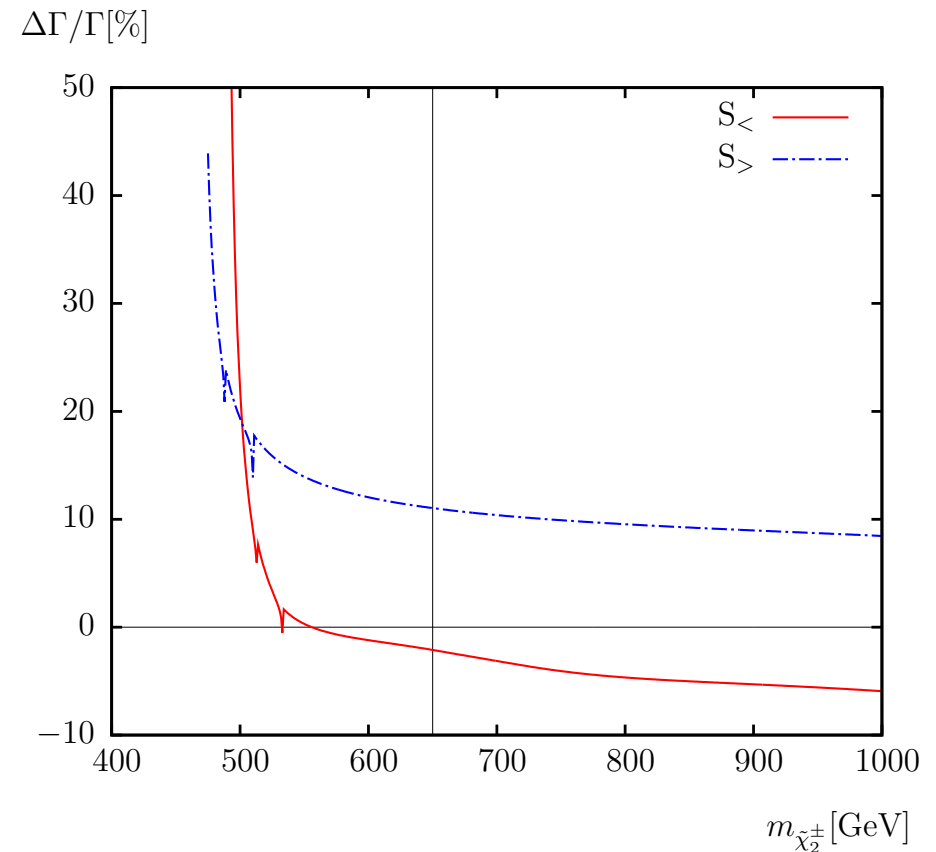
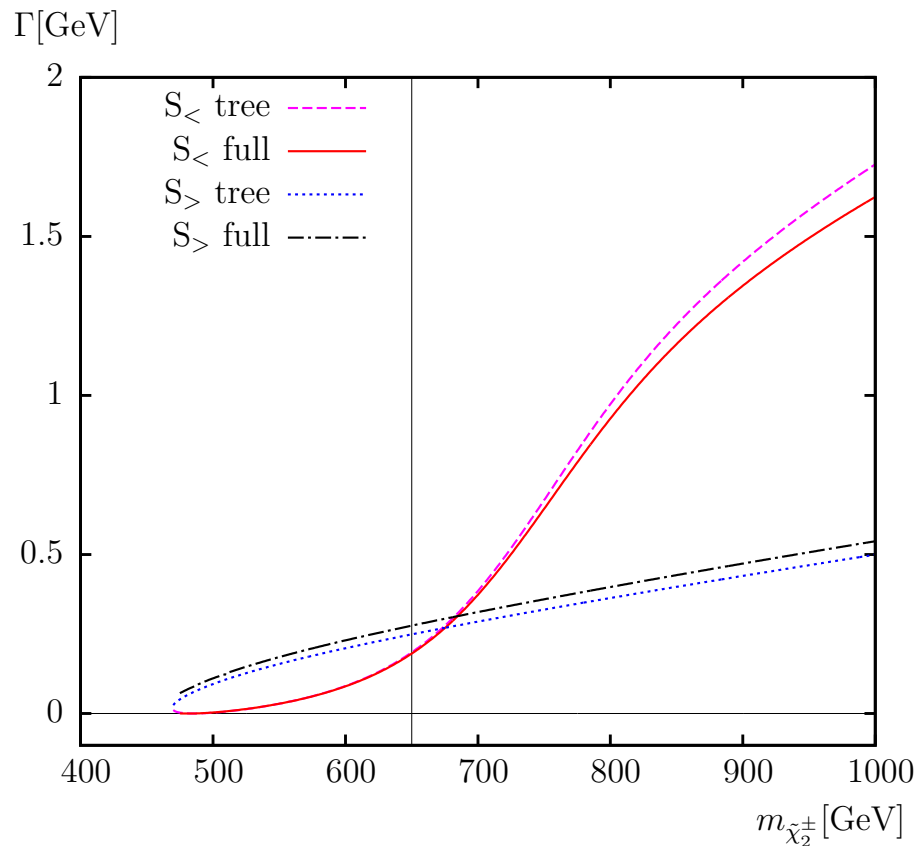


- including  $W^+-H^+$  or  $G^+-H^+$  transition contribution on the external Higgs boson leg
- including all soft/hard QED/QCD diagrams



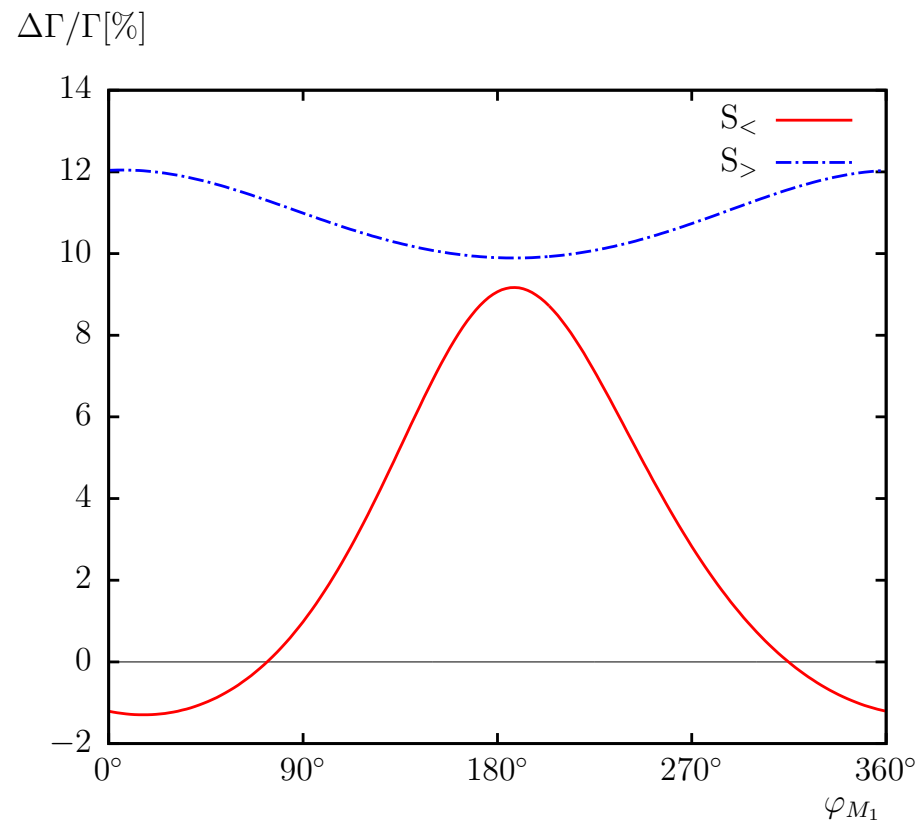
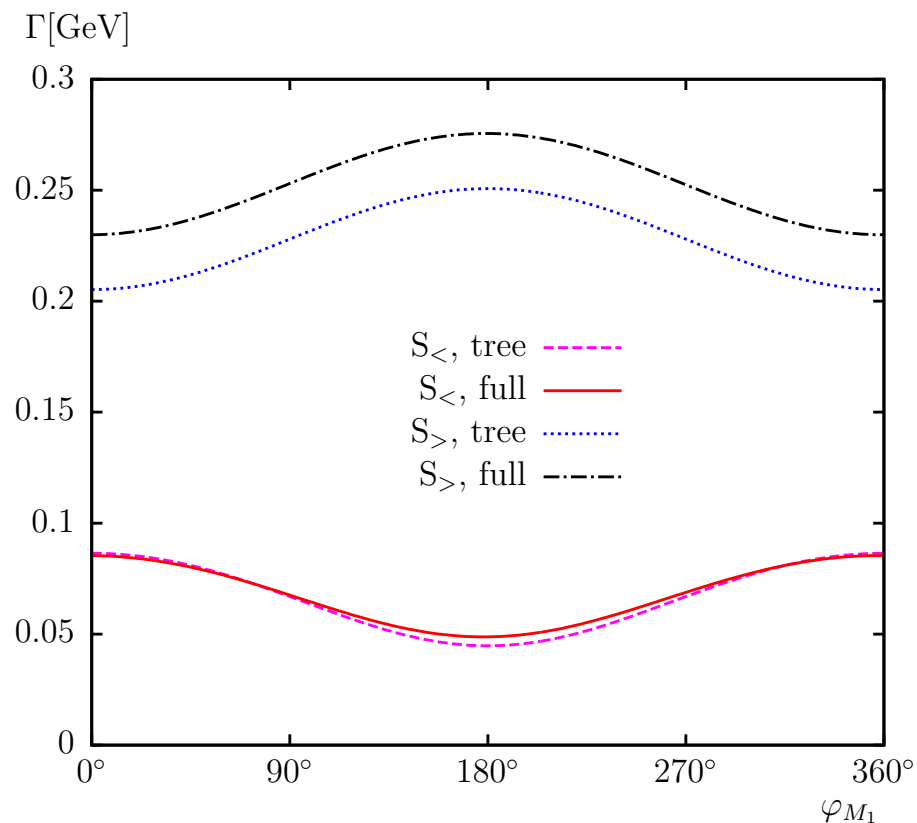
⇒ one-loop corrections under control and non-negligible

⇒ size of BR highly scenario dependent



⇒ one-loop corrections under control and non-negligible

⇒ size of BR highly scenario dependent



⇒ one-loop corrections under control and non-negligible

⇒ size of BR highly scenario dependent

## 5. Conclusinos

- Needed: reliable prediction for SUSY cascades at the LHC  
Of special intrest: decays involving Higgs or LSP
- Our work: renormalization of the full cMSSM!  
⇒ Calculation of decay widths and branching ratios
  - all two-body decays
  - full one-loop (incl. hard QED/QCD radiation)
  - in the complex MSSM for arbitrary parameters
- Stop/Sbottom sector:
  - 6+ schemes compared
  - “ $m_b, A_b \overline{DR}$ ” identified as preferred scheme
- Chargino/Neutralino sector:
  - 2 on-shell schemes compared
  - very good agreement found as expected
- FeynArts model file ready for cMSSM calculations
- Heavy Stop decays:  $\tilde{t}_2 \rightarrow \tilde{t}_1 h_1: \sim 20\%$ ,  $\tilde{t}_2 \rightarrow t \tilde{\chi}_1^0: \sim \pm 10\%$
- Chargino decays:  $\tilde{\chi}_2^- \rightarrow \tilde{\chi}_1^- h_1: \sim 10\%$ ,  $\tilde{\chi}_2^- \rightarrow \tilde{\chi}_1^0 H^-: \sim 10\%$