

Summary on the dead channel effect analysis

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Calice Asia Meeting 7. Jun. 2013

Reminder

Jet Energy Resolution (JER) is not affected significantly with

~15% dead pixels

~5% dead chips

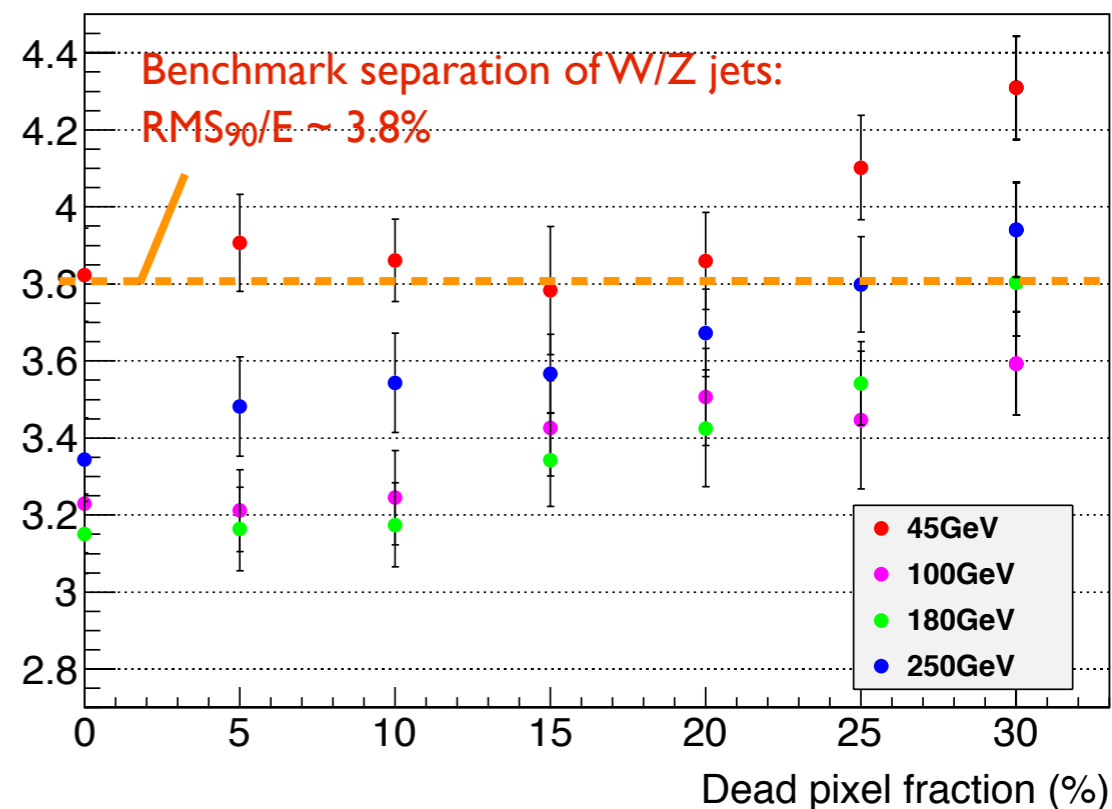
(Everybody has been funny to see this result. Actually I was not confident too.)

■ Miscellaneous checks

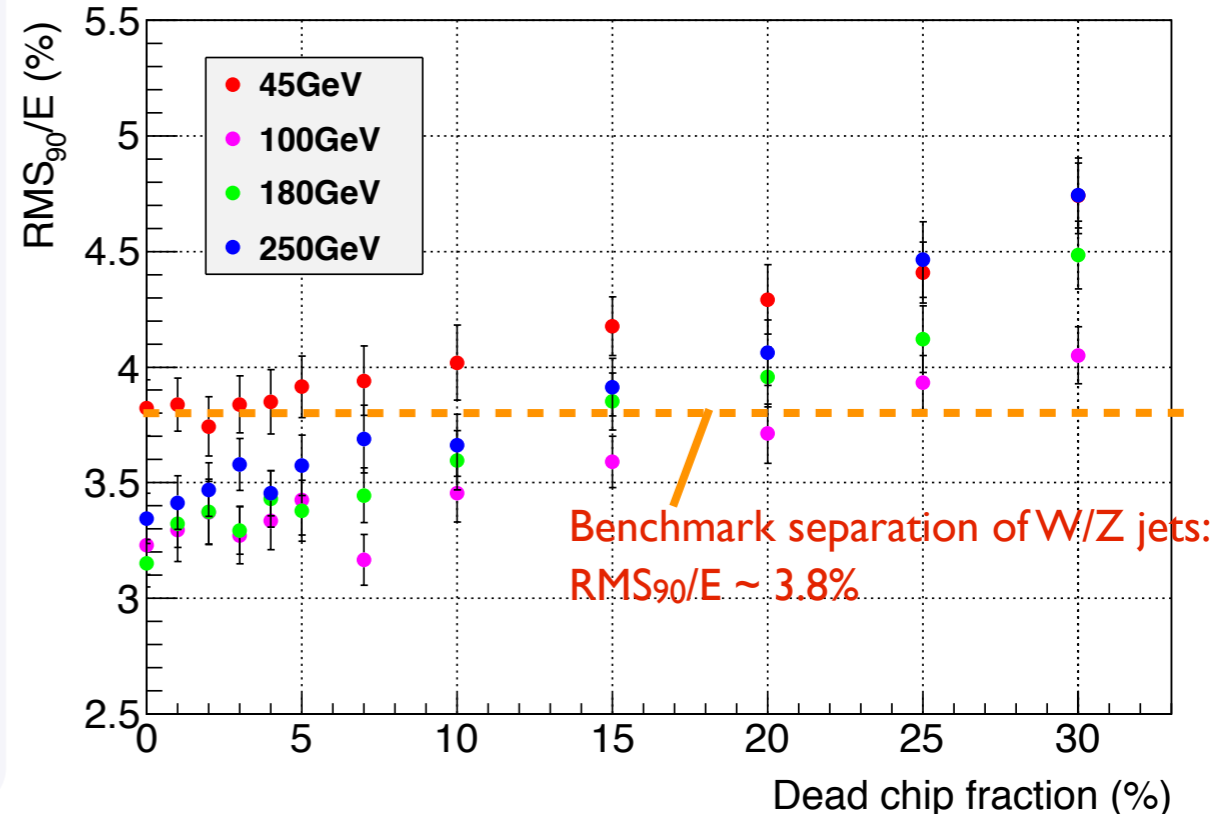
Mean of energy distribution

Mean of hit number

Dead pixel



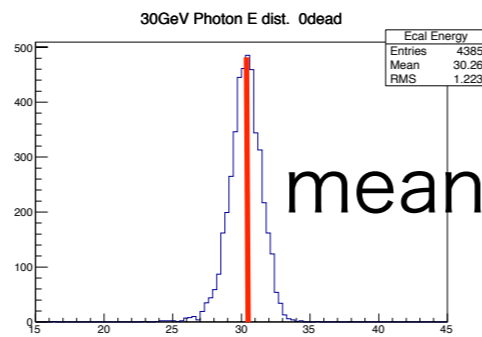
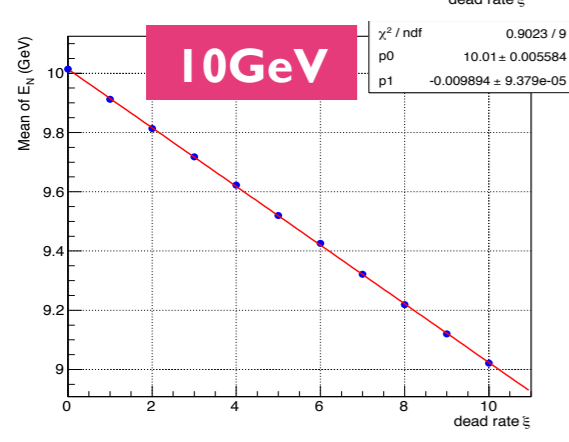
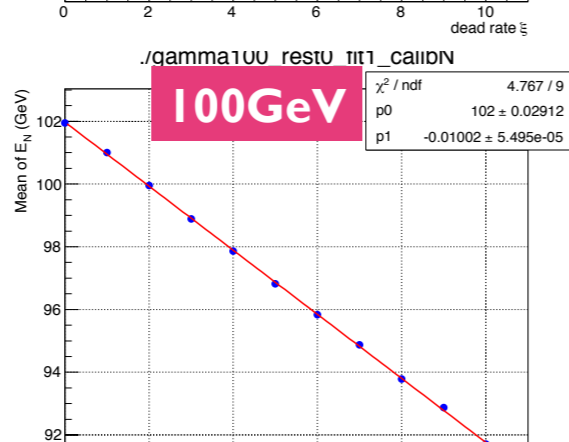
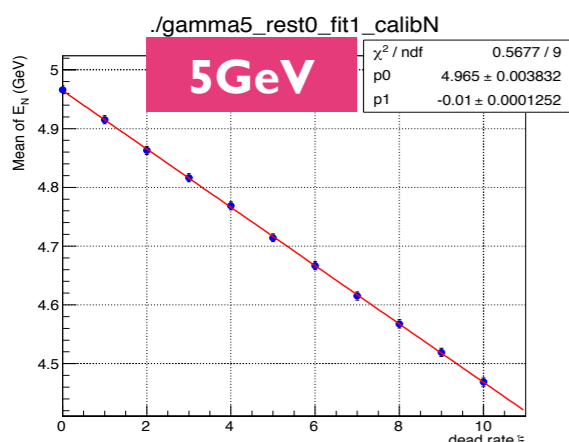
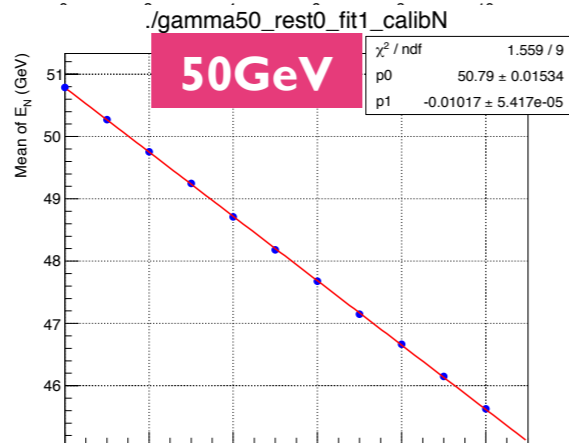
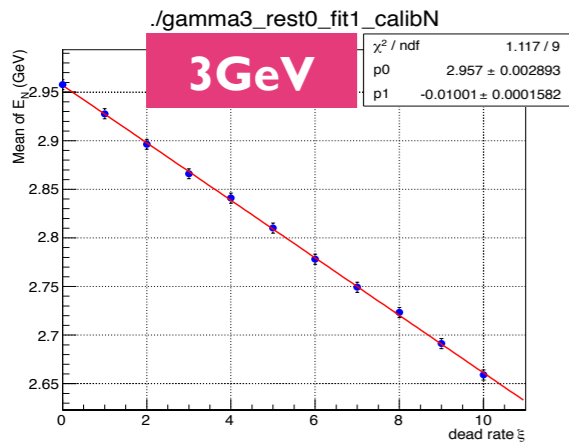
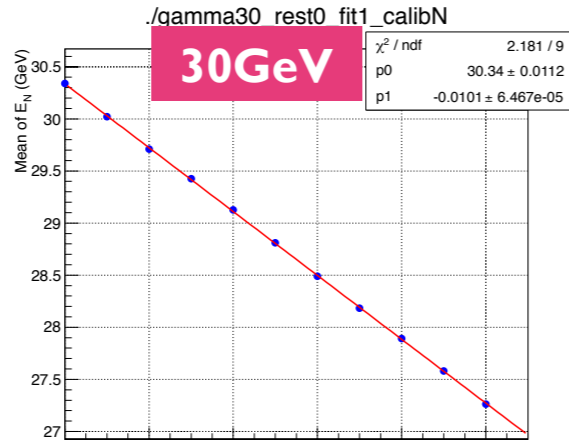
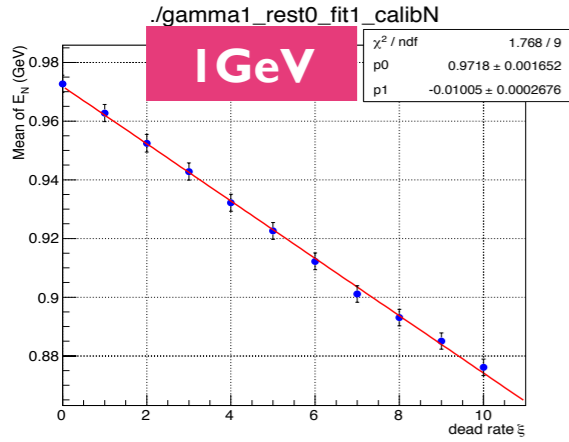
Dead ASIC chip (8x8 pixels)



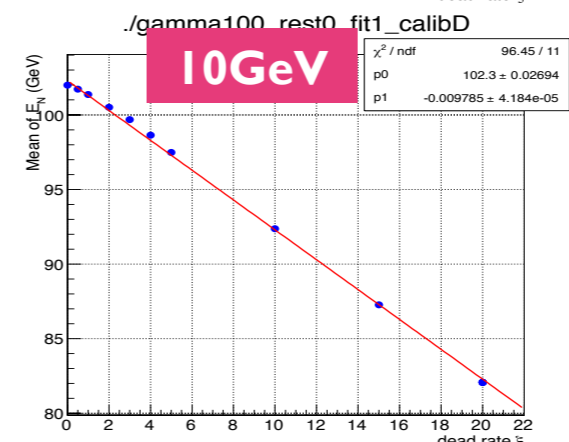
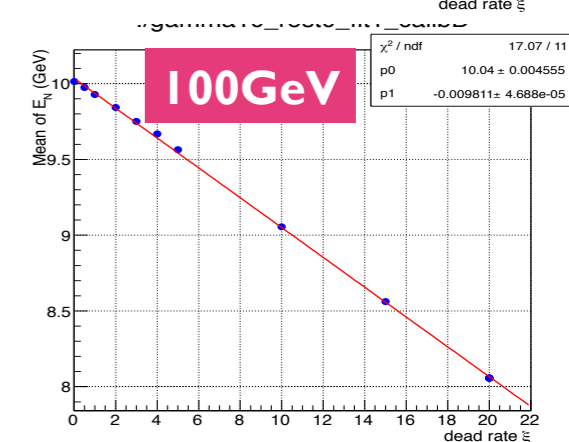
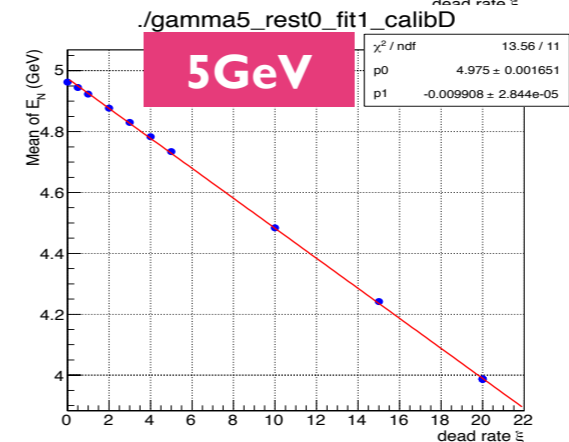
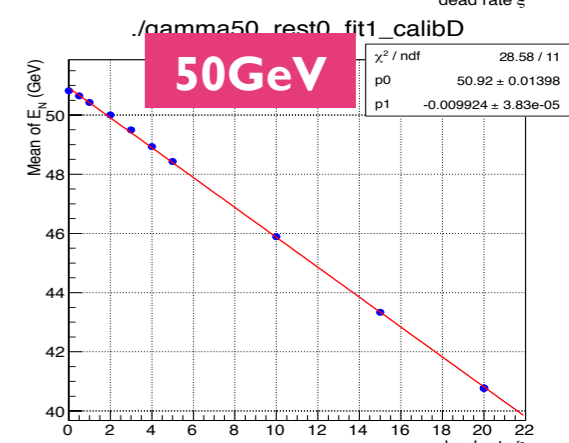
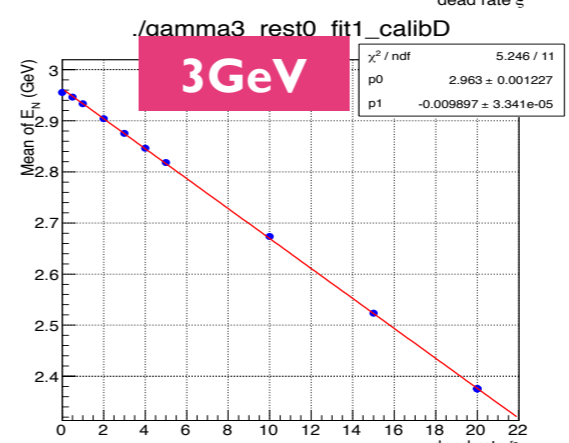
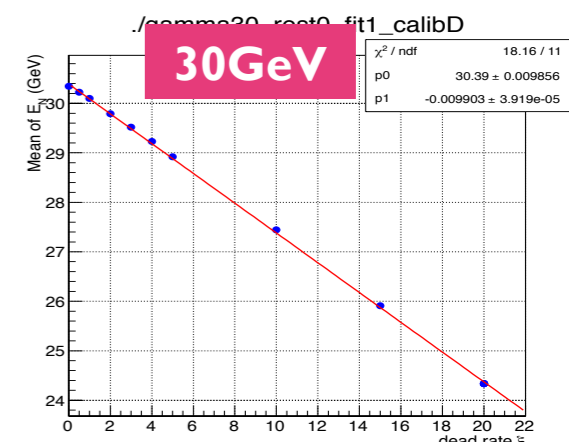
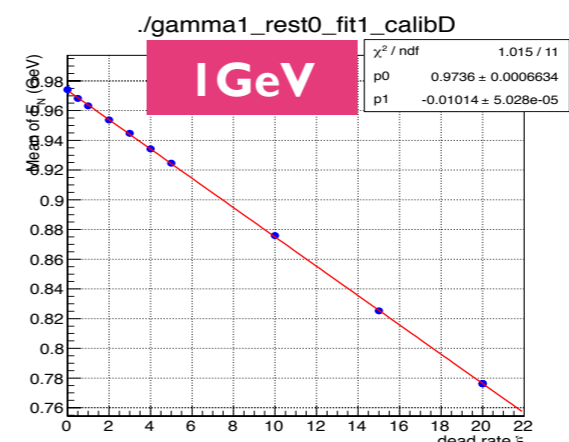
Mean of energy (Single photon event)

The drop rate = dead fraction

(Dead pixels)



(Dead chips)



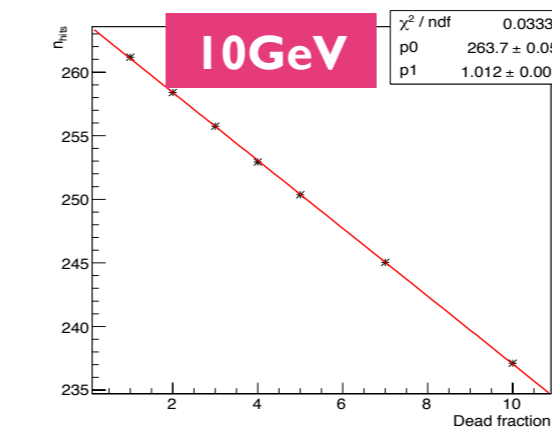
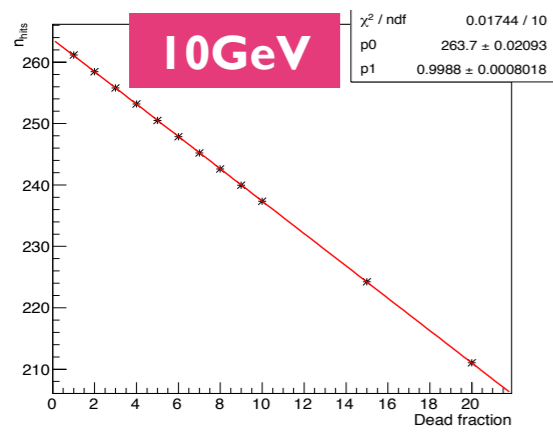
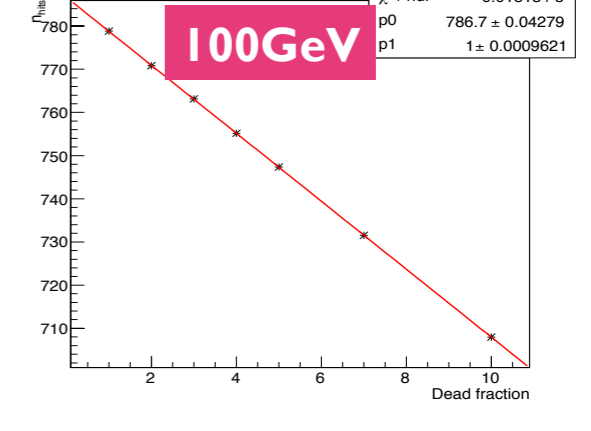
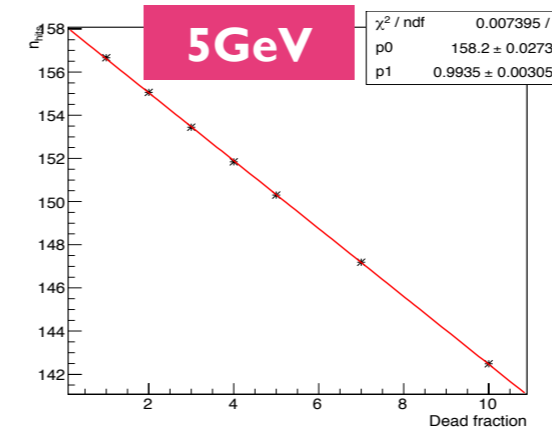
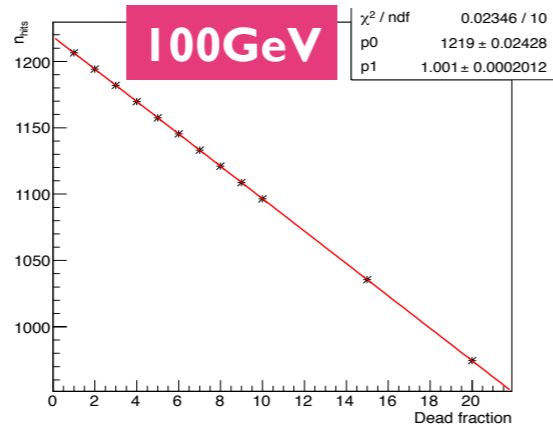
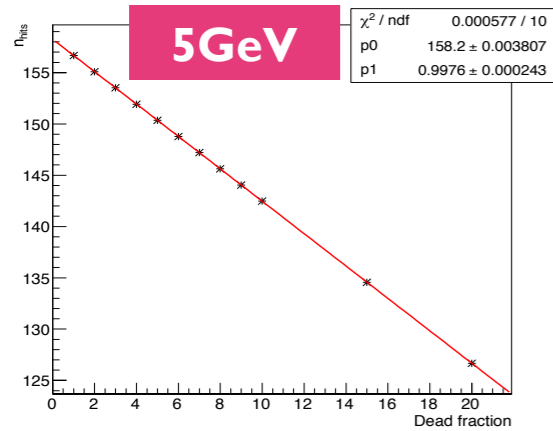
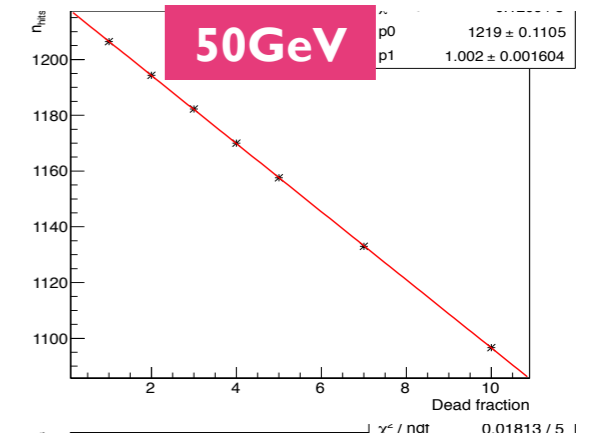
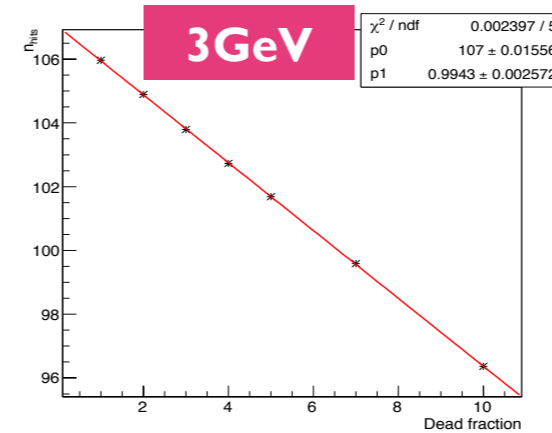
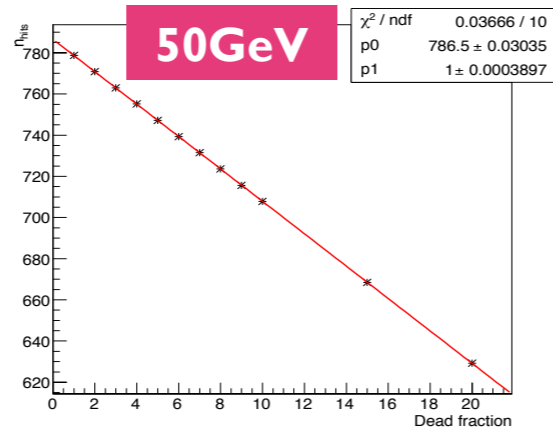
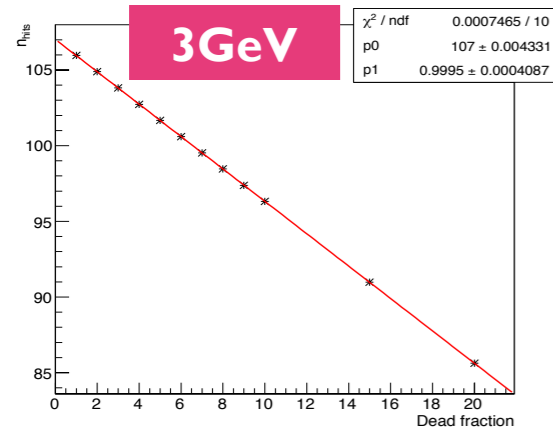
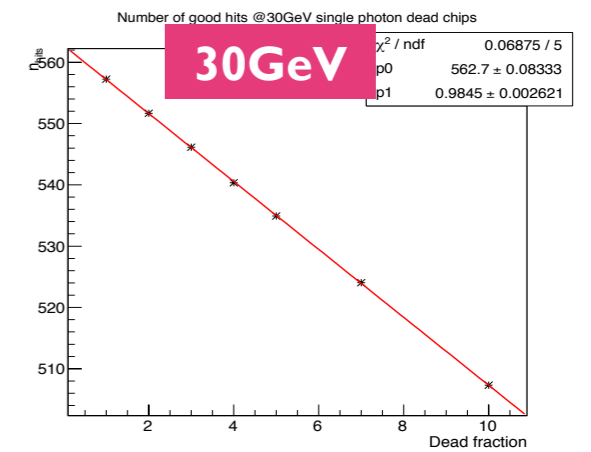
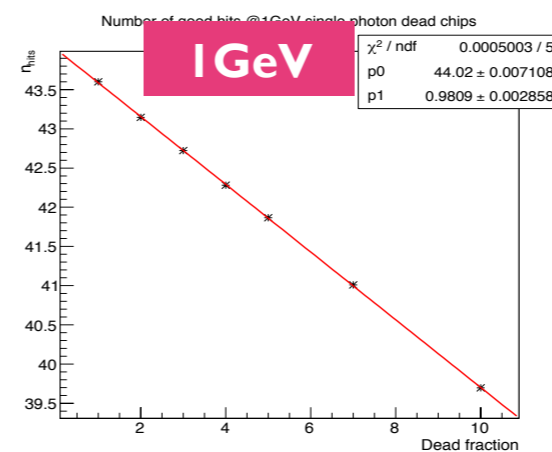
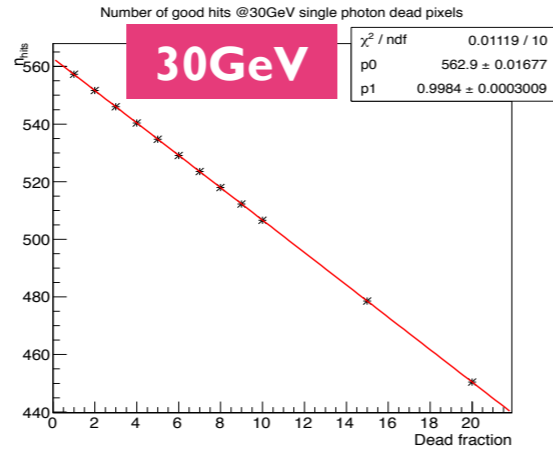
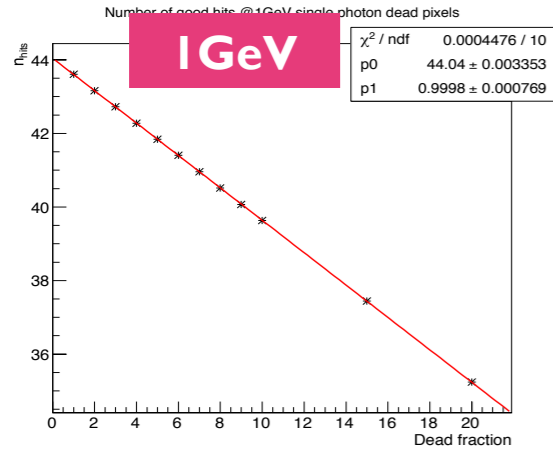
$$(fit) E = p_0(1 + p_1 \xi)$$

Mean of number of hits in a qqbar 2 jet event

The drop rate = dead fraction

(Dead pixels)

(Dead chips)



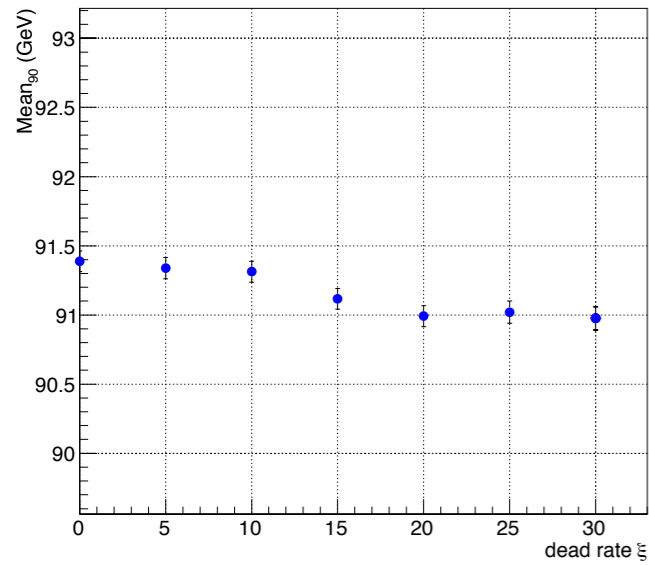
(fit) $E = p_0(1 + p_1 \xi)$

Mean of energy (qqbar 2jets event)

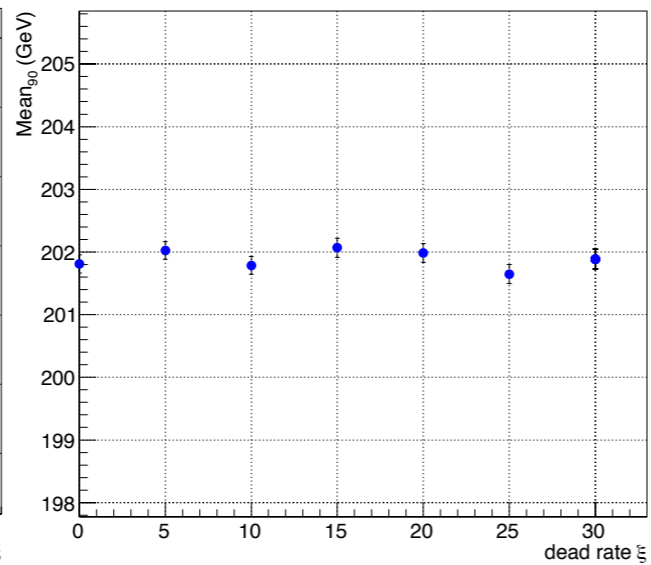
After re-calibration $C \rightarrow C/(1-\xi)$
(in order to match the calibration
to TPC and HCAL)

(Dead pixels)

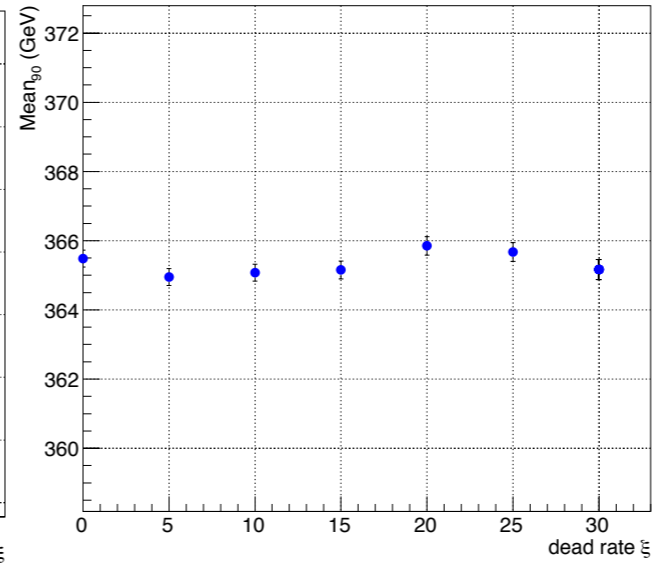
91GeV



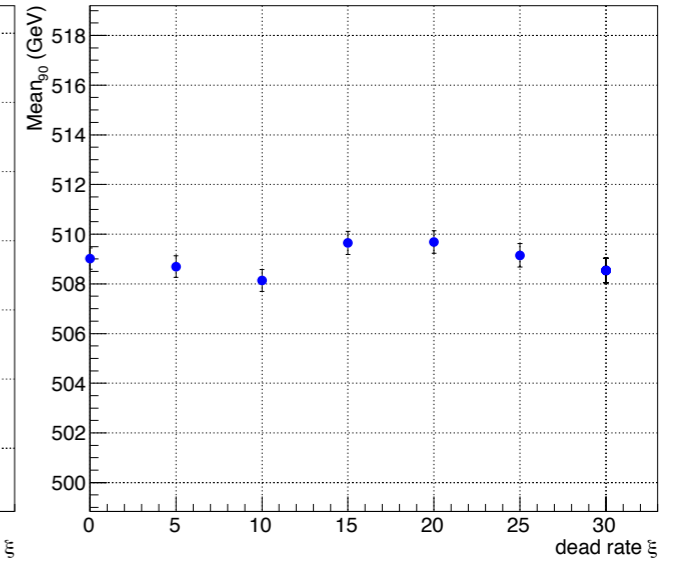
200GeV



360GeV

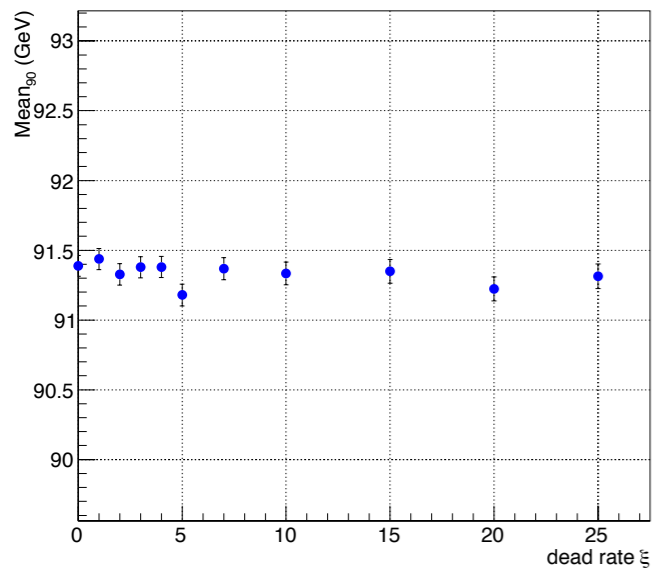


500GeV

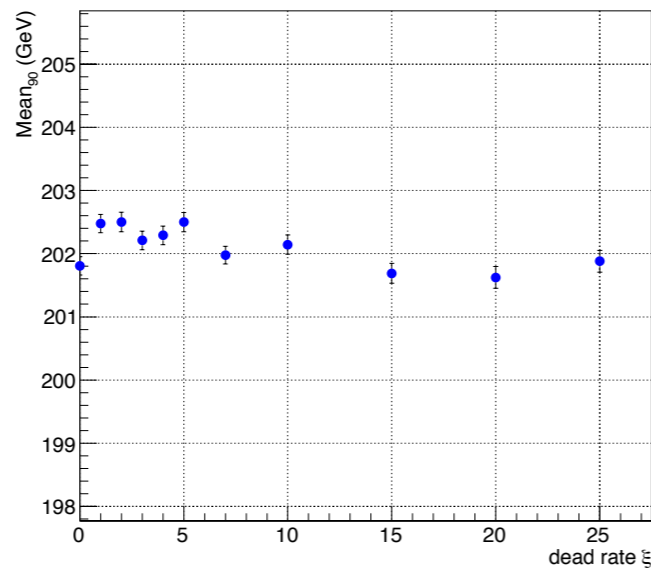


(Dead chips)

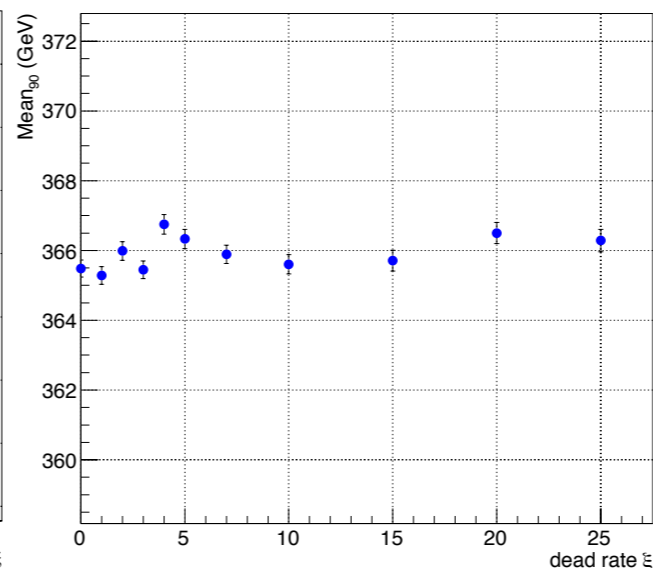
91GeV



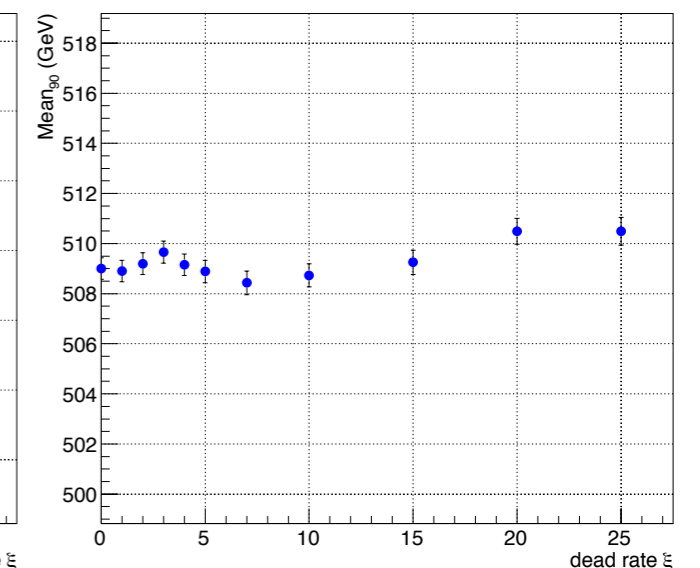
200GeV



360GeV



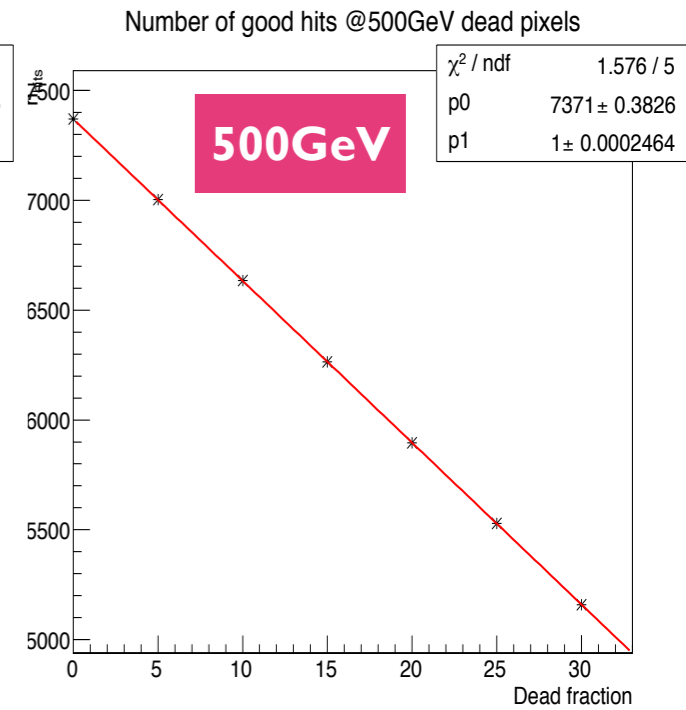
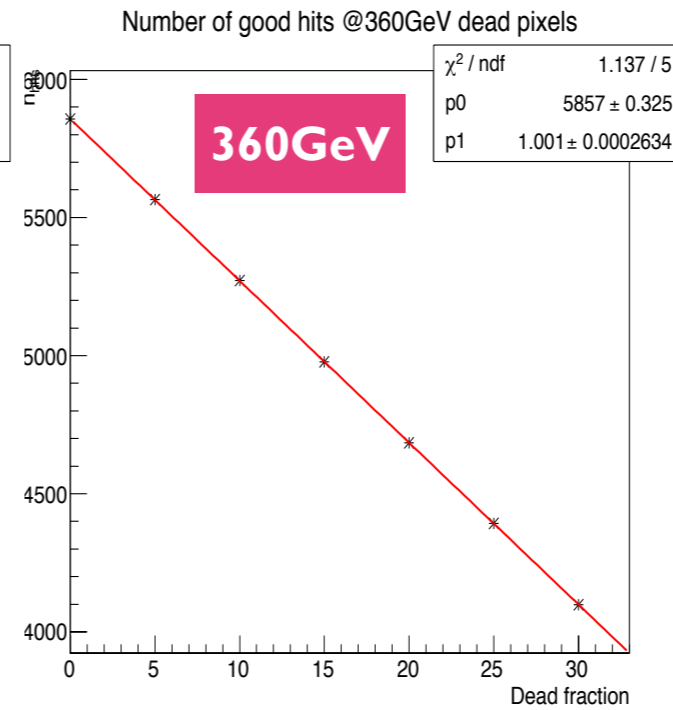
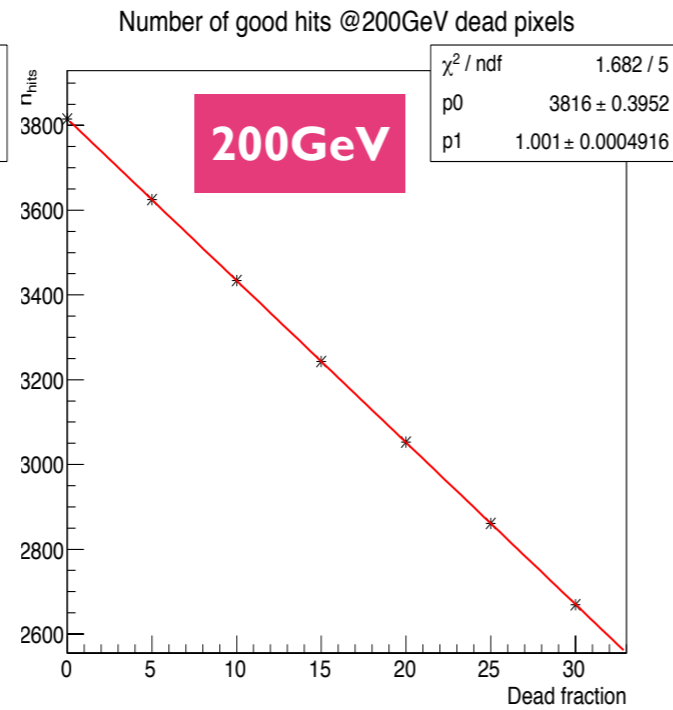
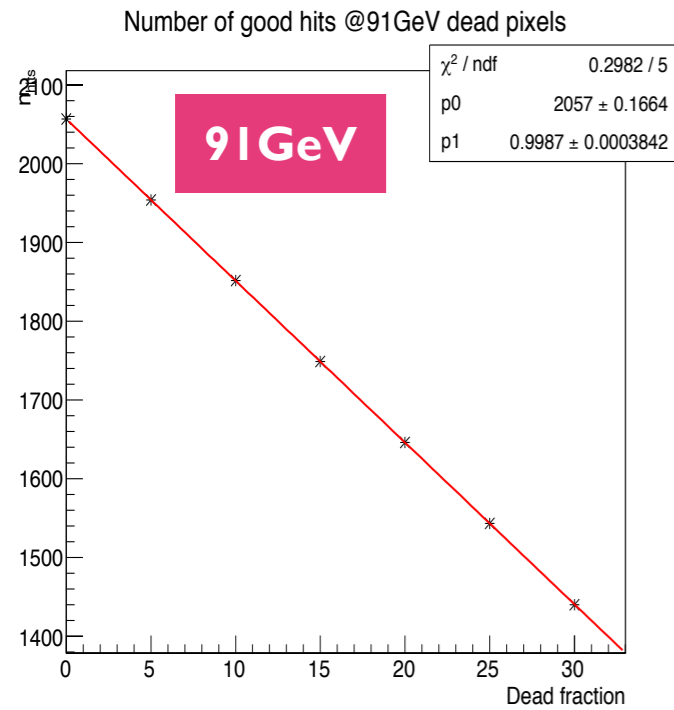
500GeV



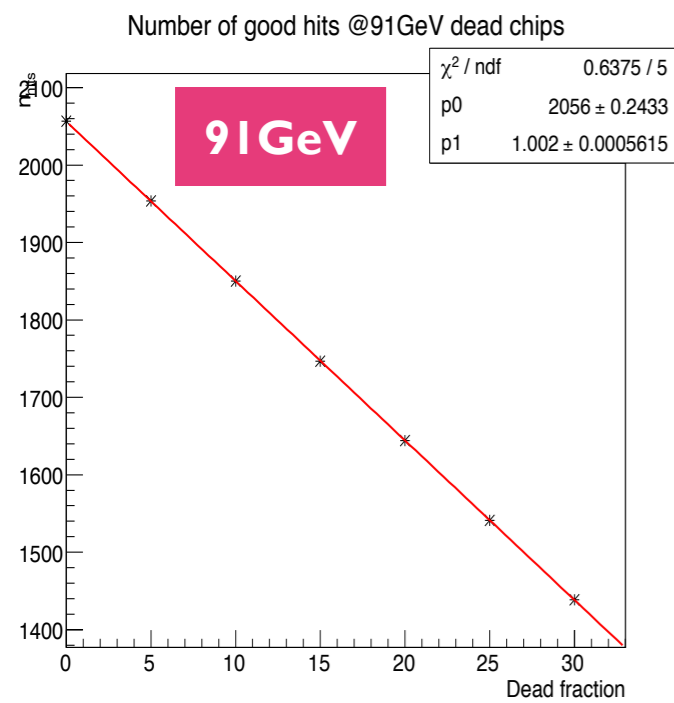
Mean of number of hits in a qqbar 2 jet event

The drop rate = dead fraction

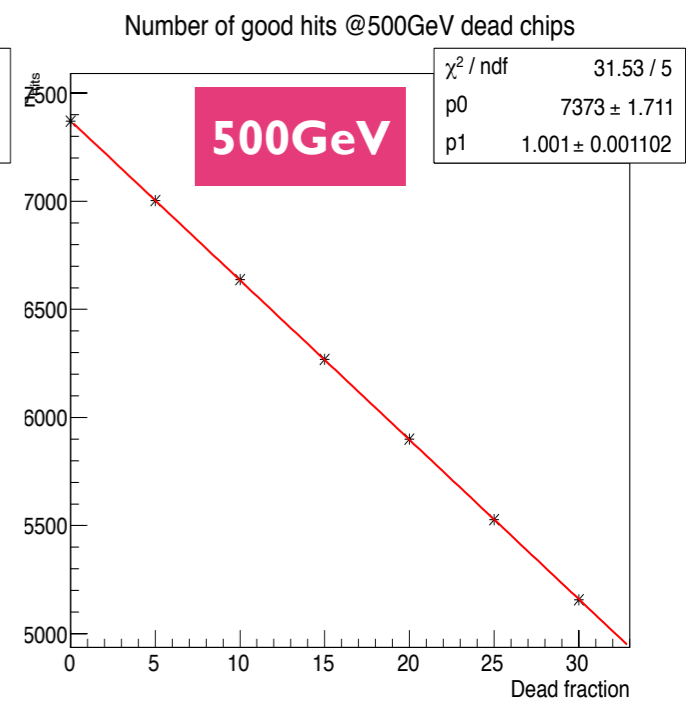
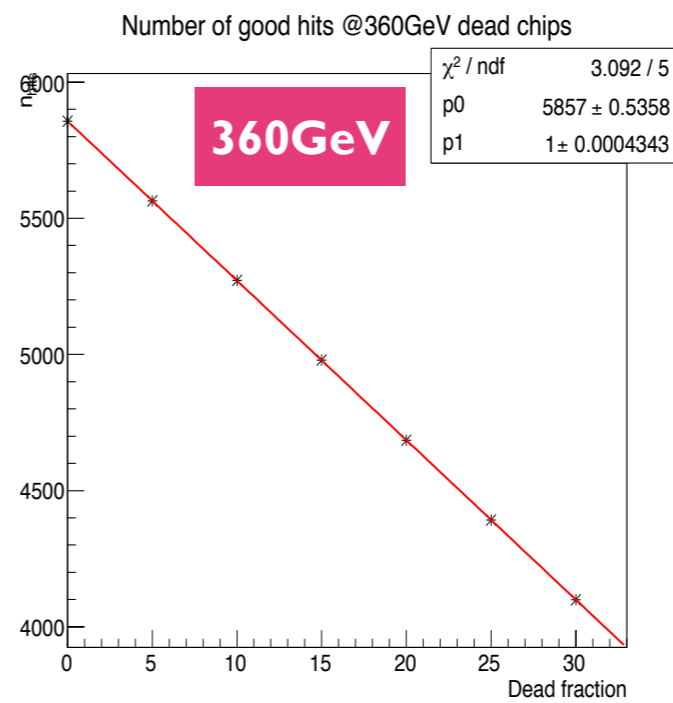
(Dead pixels)



(Dead chips)



The file of 200GeV/chip was lost...



(fit) $E = p_0(1 + p_1 \xi)$

Reminder

Jet Energy Resolution (JER) is not affected significantly with

- ~15% dead pixels
- ~5% dead chips

(Everybody has been funny to see this result. Actually I was not confident too.)

■ Miscellaneous checks

Mean of energy distribution

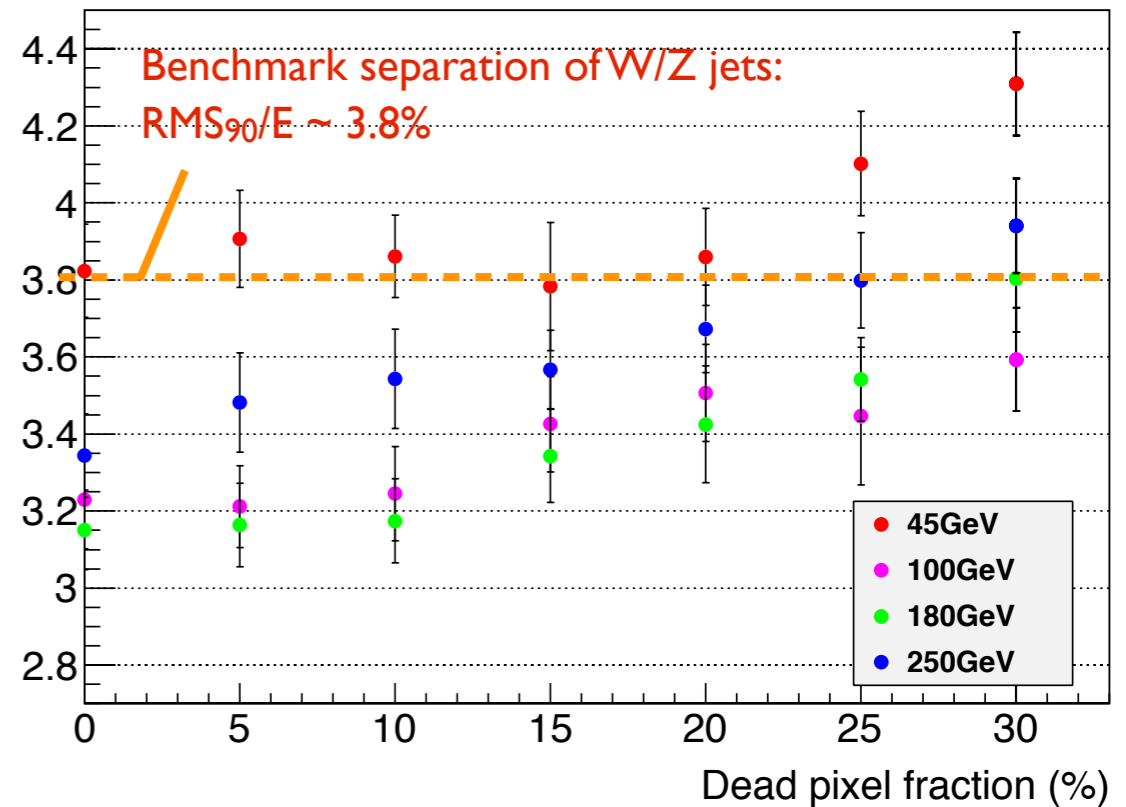
Mean of hit number

--- drop linearly as expected

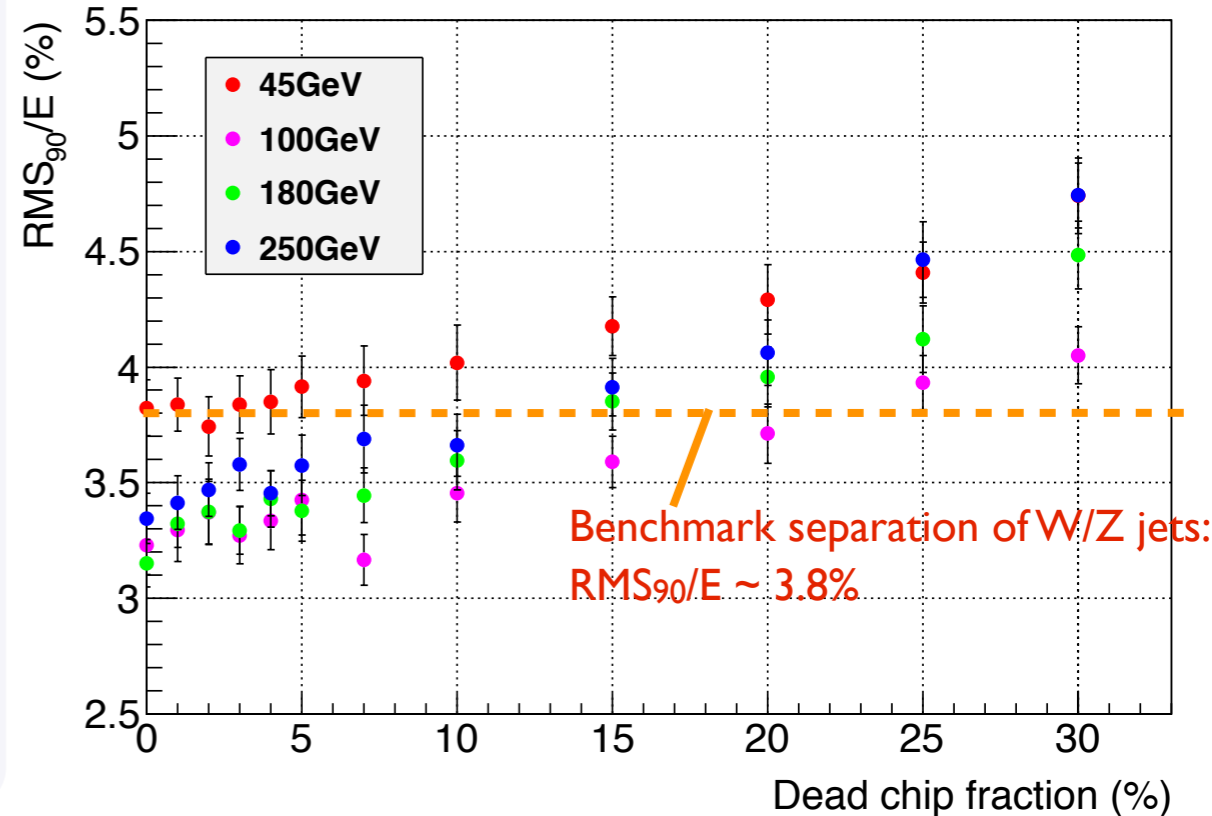
Comparison between event-by-event selecting configuration and fixed one

--- no difference

Dead pixel

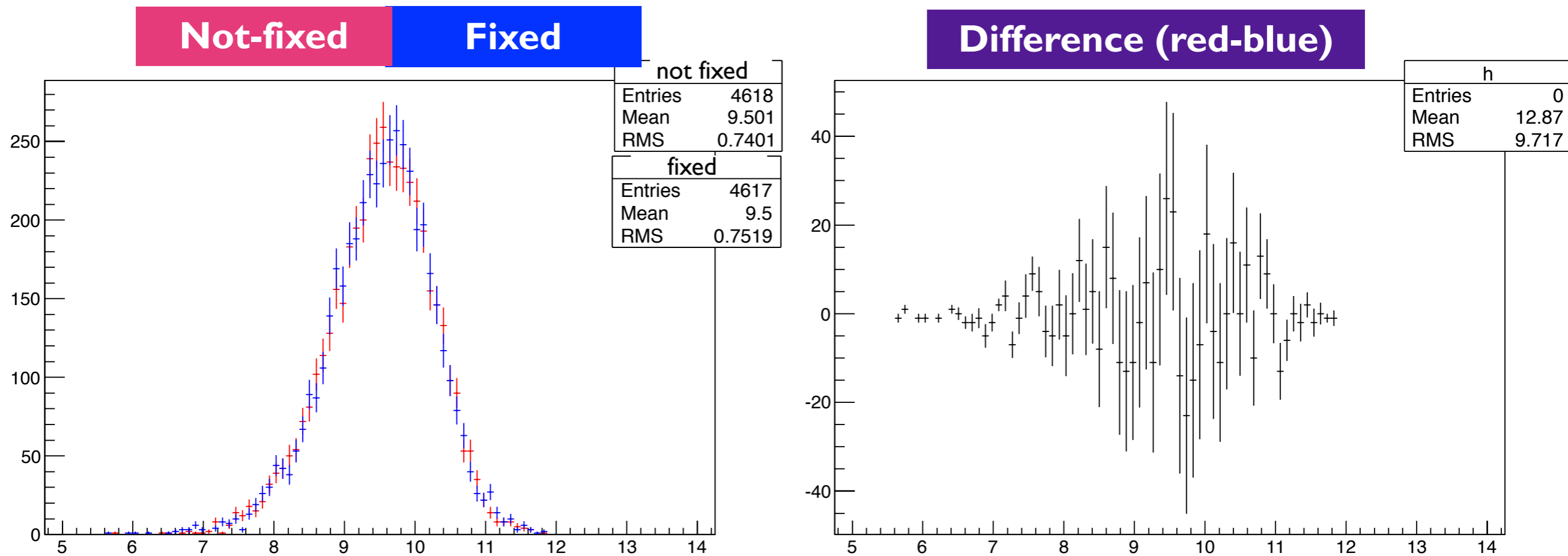


Dead ASIC chip (8x8 pixels)



Event-by-event choice vs Fixed configuration

e.g. Energy distribution of 10GeV Single photon evt w/ 5% of dead chips



Consistent with statistic fluctuation

Other E, Dead fraction: Same

Reminder

Jet Energy Resolution (JER) is not affected significantly with

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- ~5% dead chips

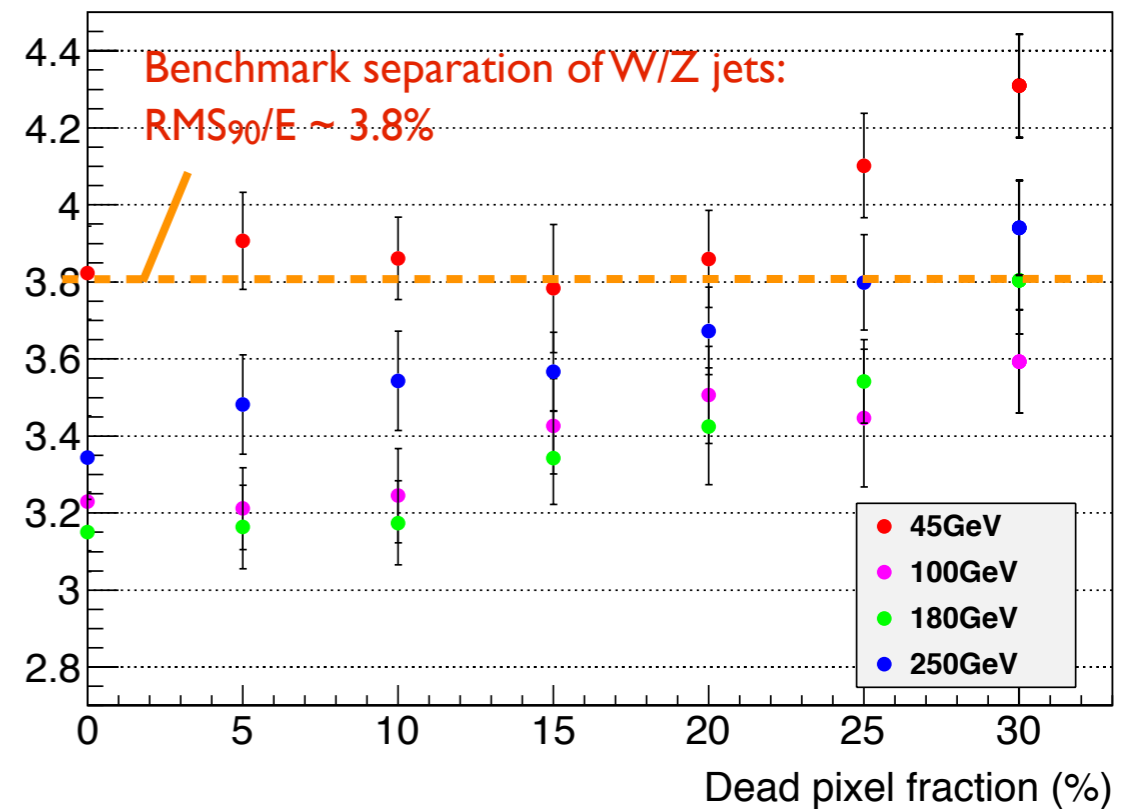
■ Simulation seems to work appropriately

Why 15% of dead pixels are ok?

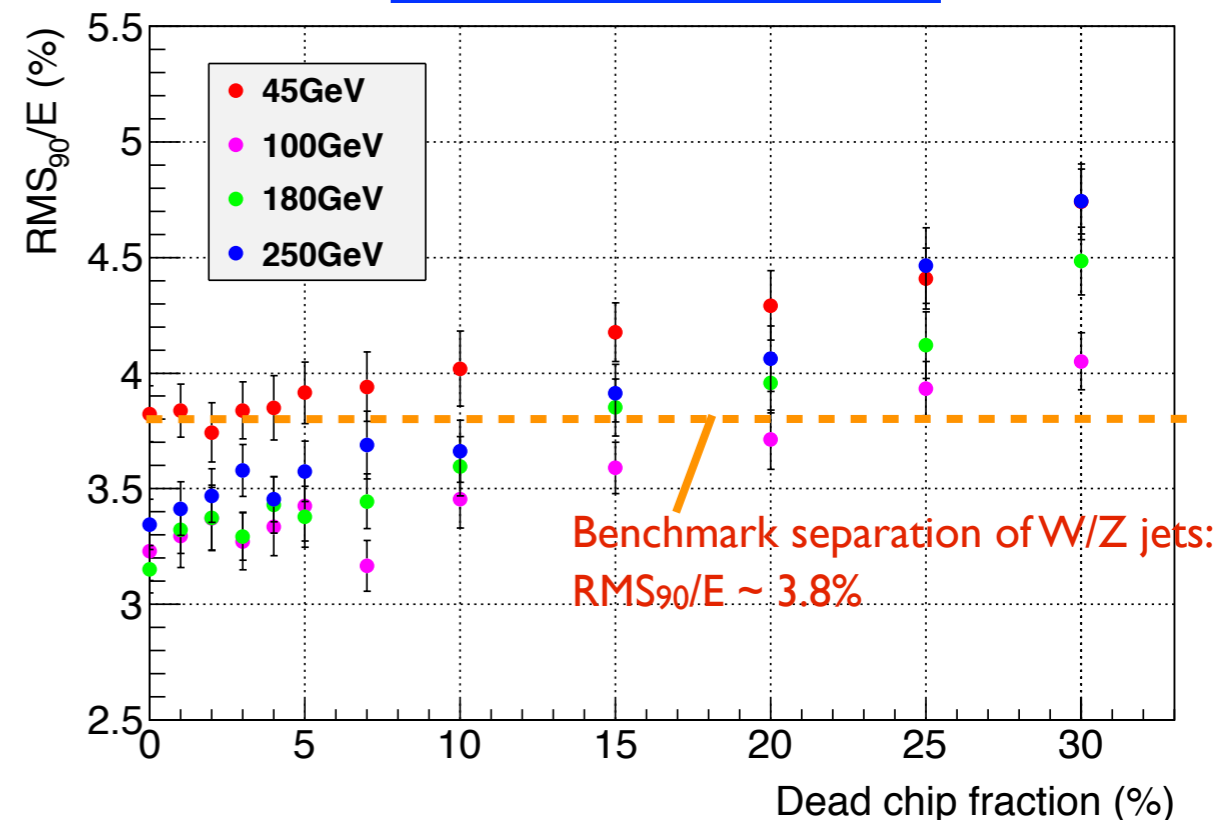
Study

- Quantitate analysis of **dead channel** effect to **ECAL** resolution
- Discuss **dead channel** impact on **JER** with the result of above

Dead pixel



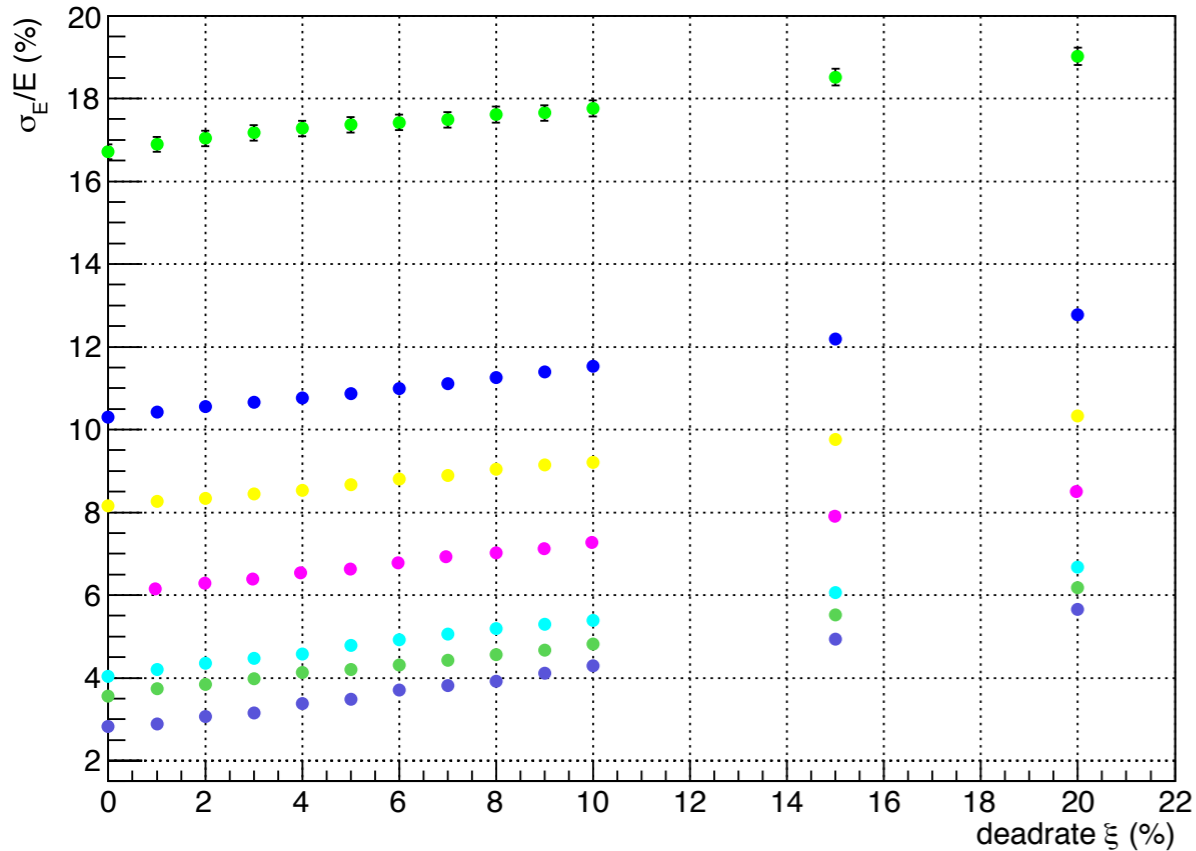
Dead chip



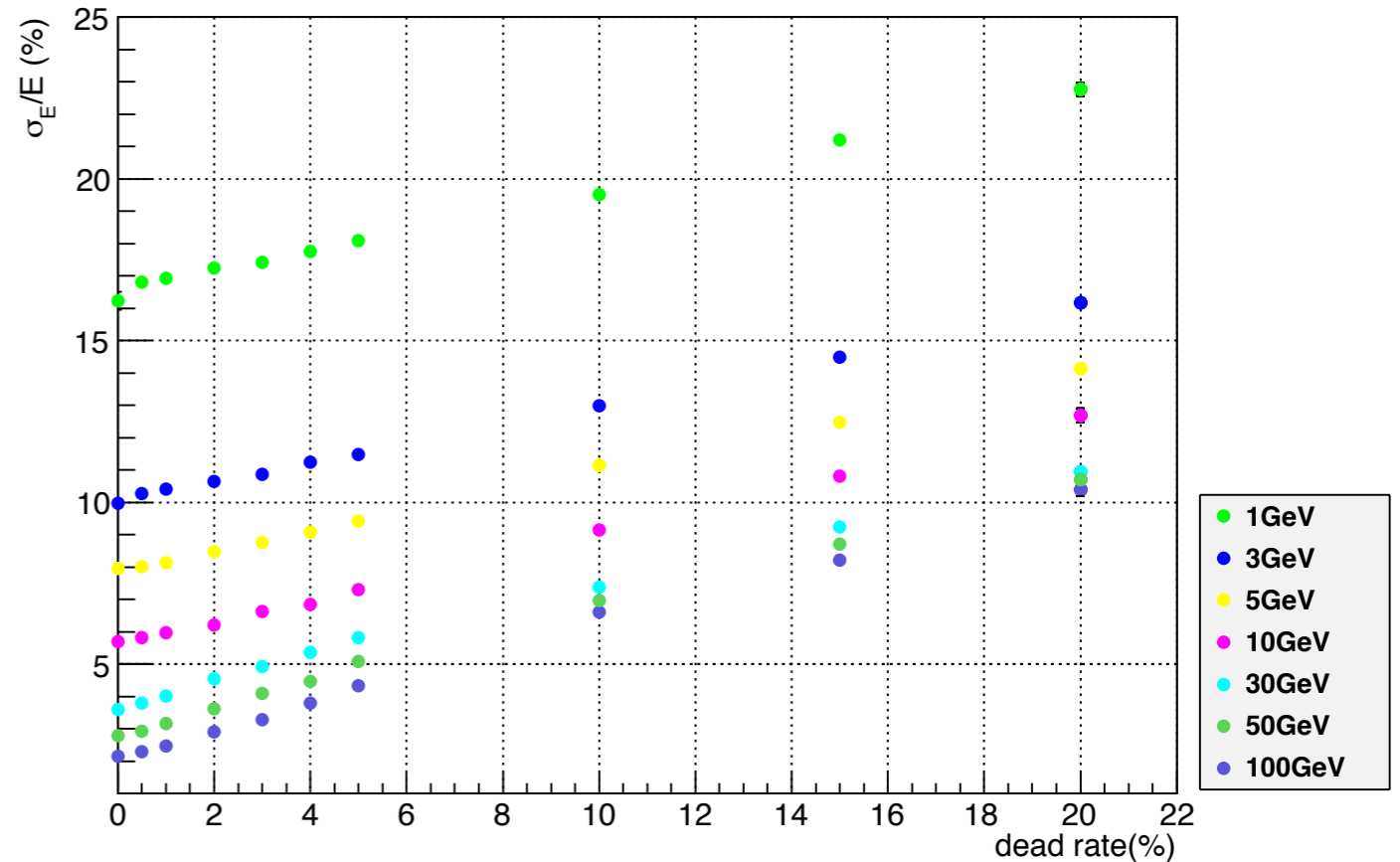
Dead channels effect to ECAL resolution

Evaluate ECAL performance by energy resolution of single photon events

Dead pixel



Dead chip



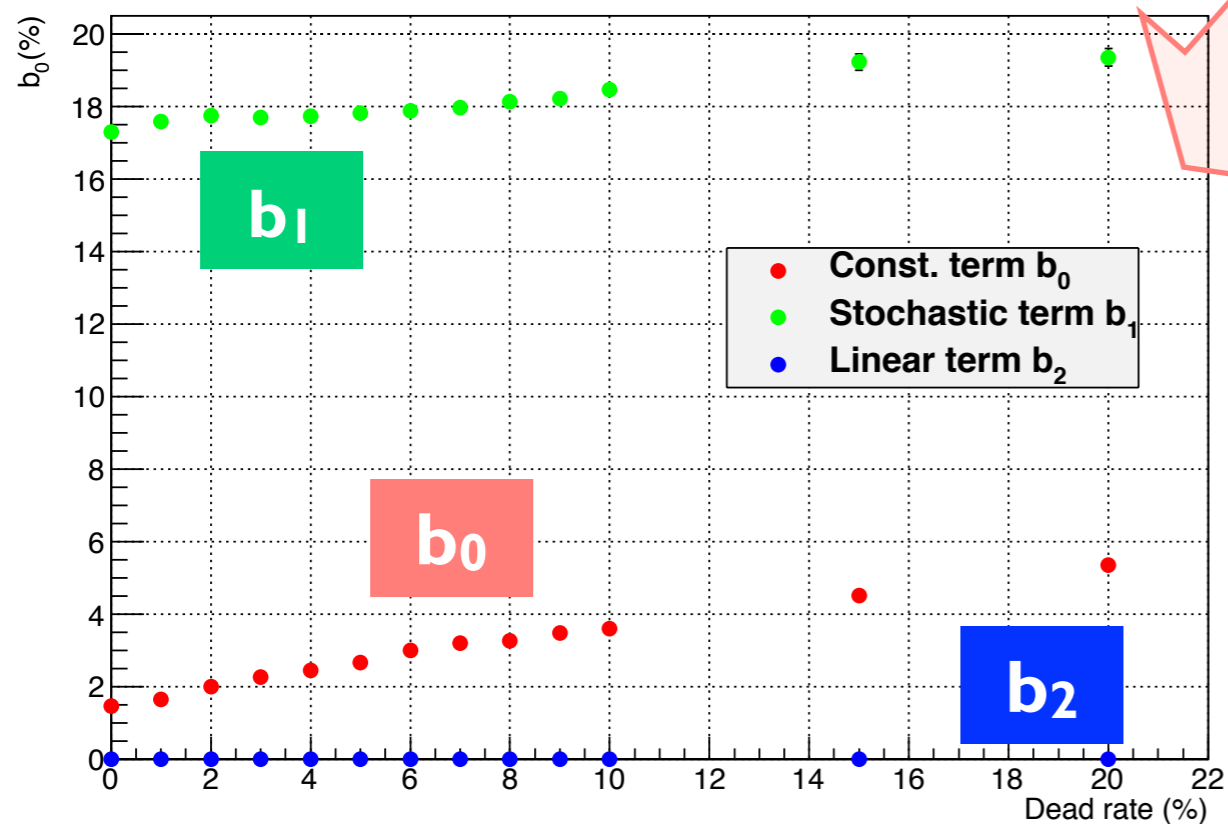
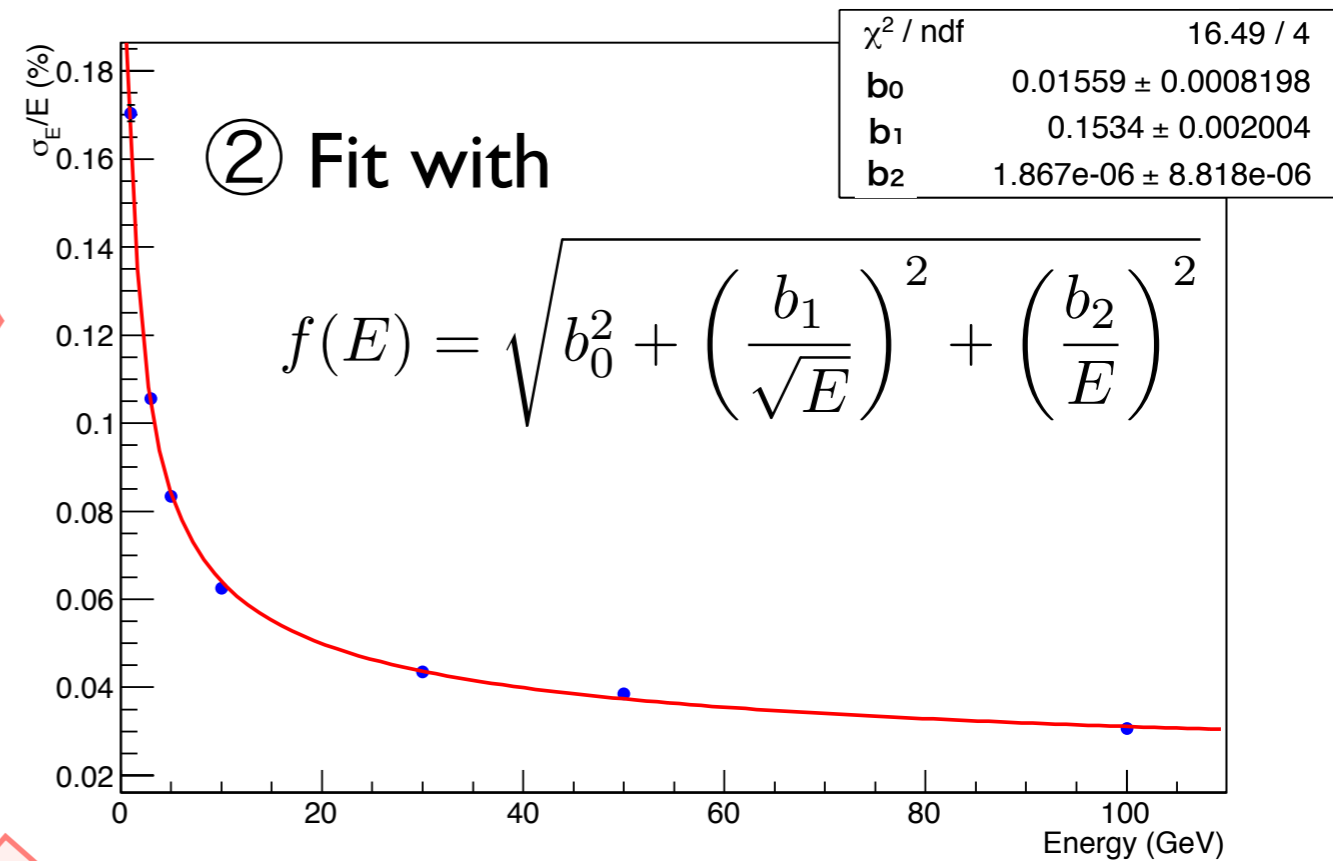
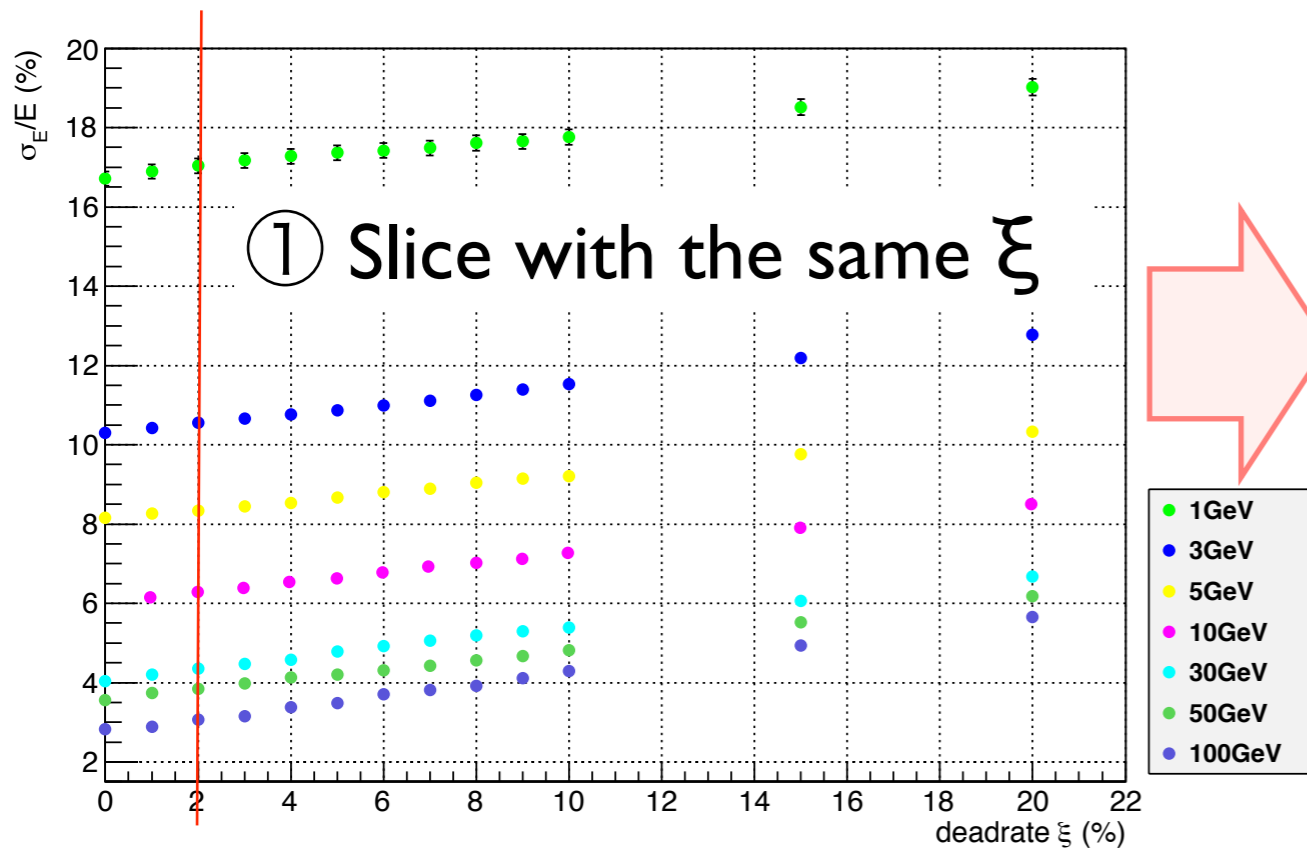
Single particle energy resolution:

$$\frac{\sigma_E}{E} = \overset{\text{Const.}}{\boxed{b_0(\xi)}} \oplus \overset{\text{Stochastic}}{\boxed{\frac{b_1(\xi)}{\sqrt{E}}}} \oplus \overset{\text{Noise}}{\boxed{\frac{b_2(\xi)}{E}}}$$

Photons with higher energy experience more degrade

Dead channel effect can be reduced to b_0, b_1, b_2 dependences on ξ

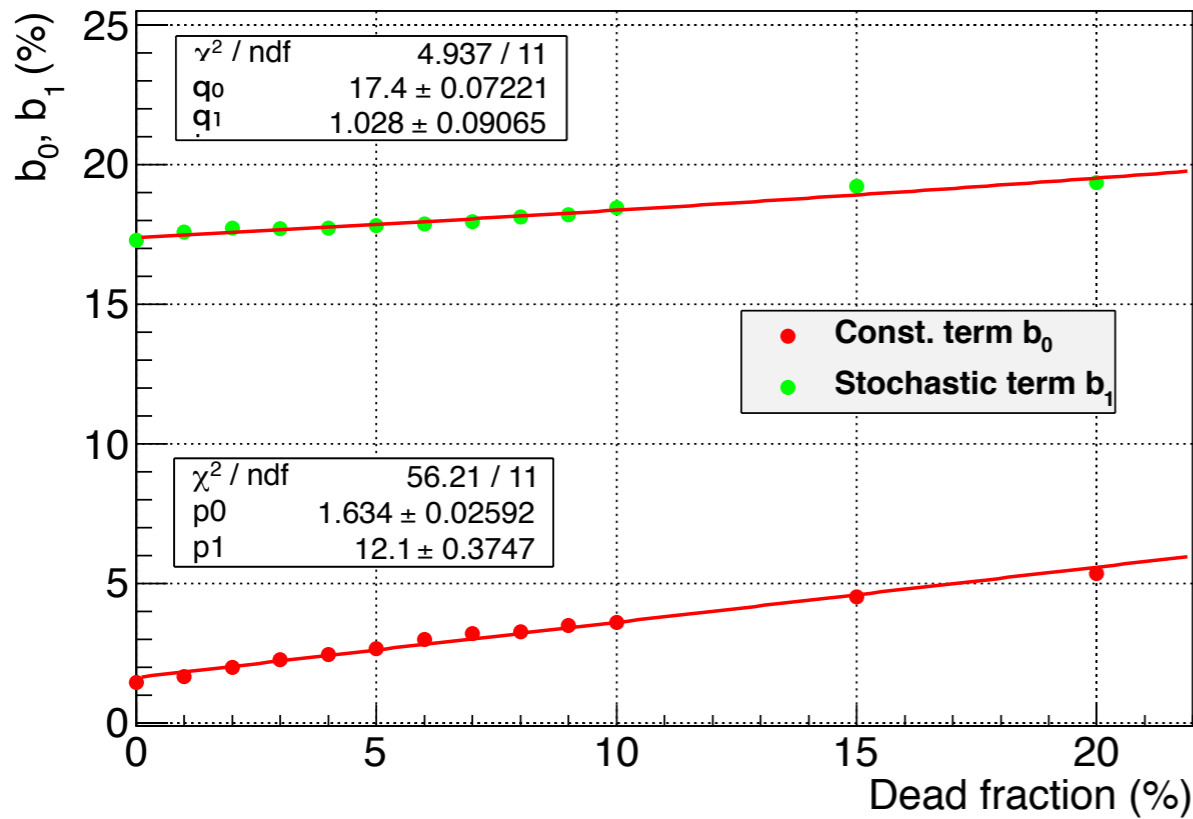
ξ dependence of b_0, b_1, b_2



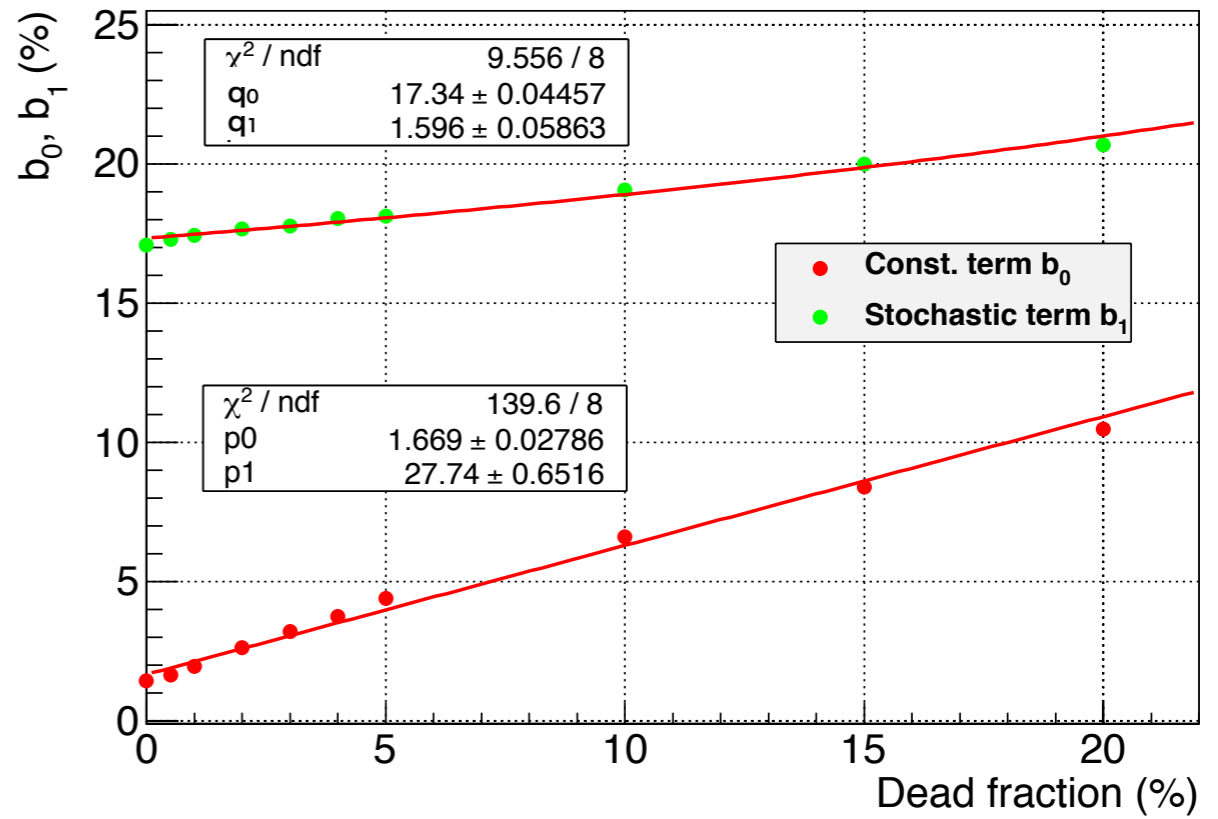
ξ dependence of b_0, b_1

$$\frac{\sigma_E}{E} = b_0(\xi) \oplus \frac{b_1(\xi)}{\sqrt{E}}$$

Dead Pixel



Dead Chip



- Dead channels **mainly affect constant term**
- Low energy → stoch. (b_1) is dominant
→ small effect by dead channels

High energy → const. (b_0) isn't negligible → large effect

- Parametrize as $b_0(\xi) = p_0 (1 + p_1 \xi)$ & $b_1(\xi) = \frac{q_0}{\sqrt{1 - q_1 \xi}}$

(Fit parameters)

	Pixel	Chip
p_0	1.6	
p_1	12	28
q_0	17.4	
q_1	1.0	1.6

How does dead channels make **stoch. term** worse ?

--- The effective sampling fraction change

- **Shower energy:** (“~”: the average of LHS/RHS match)

$$E \sim E_{MIP} \times n_{MIP}, \quad \sigma_E/E \propto 1/\sqrt{n_{MIP}} \propto 1/\sqrt{E} \quad \text{(Poisson statistics)}$$

“stochastic”

- **Measured energy in a sampling calorimeter**

$$E \sim E_{MIP} \times n_{MIP} \sim E_{MIP} \times \underbrace{n_{MIP,S}}_{\text{Number of MIP signals in sensor area}} \times \underbrace{I/C_s}_{\text{sampling ratio}}$$

$$\sigma_E/E \propto 1/\sqrt{n_{MIP,S}} \propto 1/\sqrt{E C_s}$$

- **When with a fraction of ξ dead channels in sensor area**

$$n_{MIP,S} \rightarrow (1-\xi) n_{MIP,S}$$

Sampling ratio changes accordingly: $C_s \rightarrow (1-\xi) C_s$

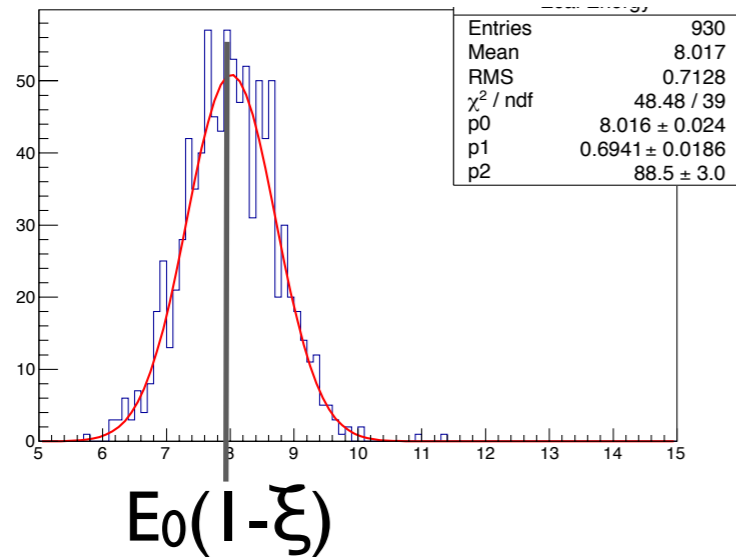
$$\sigma_{Em}/E \propto 1/\sqrt{E(1-\xi)C_s} \rightarrow b_1 \propto 1/\sqrt{1-\xi}$$

$$b_1(\xi) = \frac{q_0}{\sqrt{1 - q_1 \xi}}$$

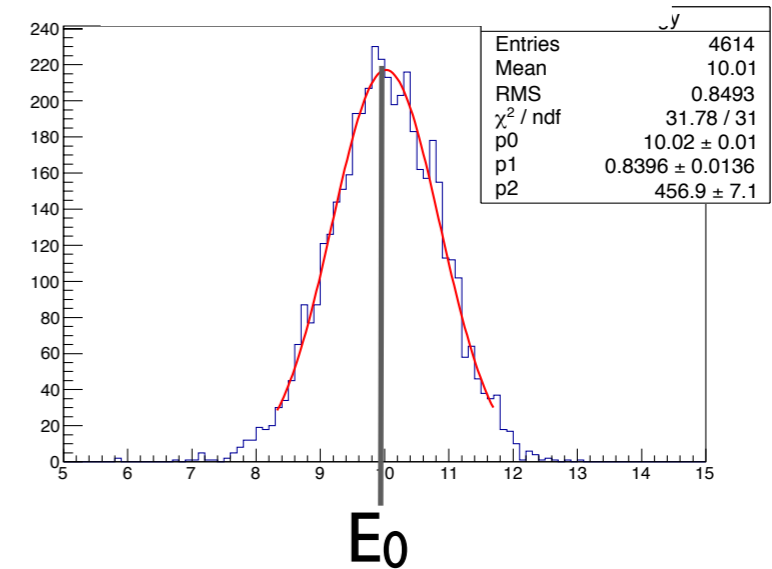
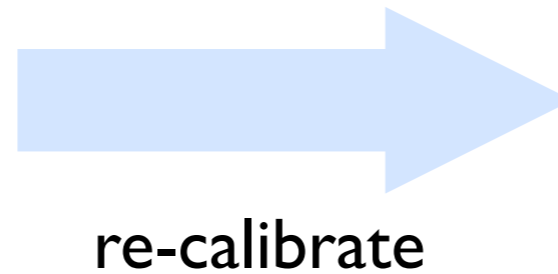
$q_1 = 1$ if no other contribution to $1/\sqrt{E}$ term

How does dead channels make **const. term** worse ?

The calibration coefficient C is scaled to $C/(1-\xi)$, according to the sampling ration change $C_s \rightarrow C_s(1-\xi)$ (So that mean energy remains in the correct position)



$$C \rightarrow C/(1-\xi)$$



Uniformly distributed dead channels are assumed. (ξ : **average** dead channel fraction)

But! the fraction in a single shower fluctuates statistically

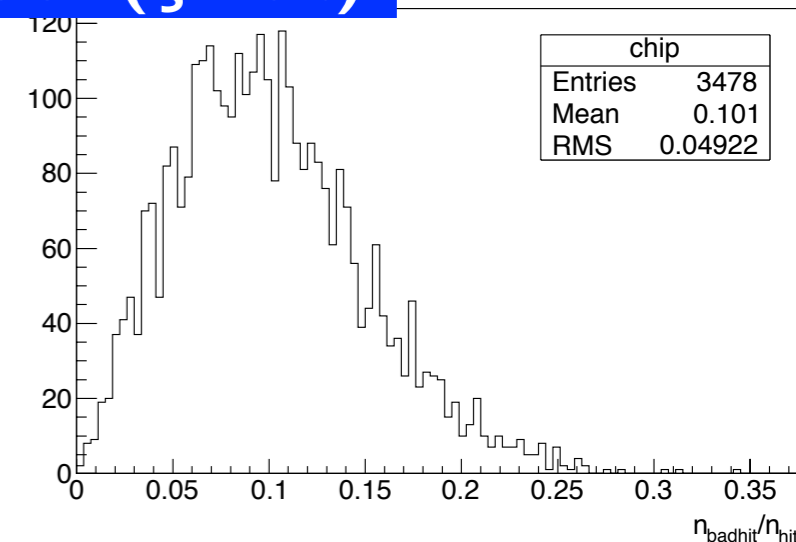
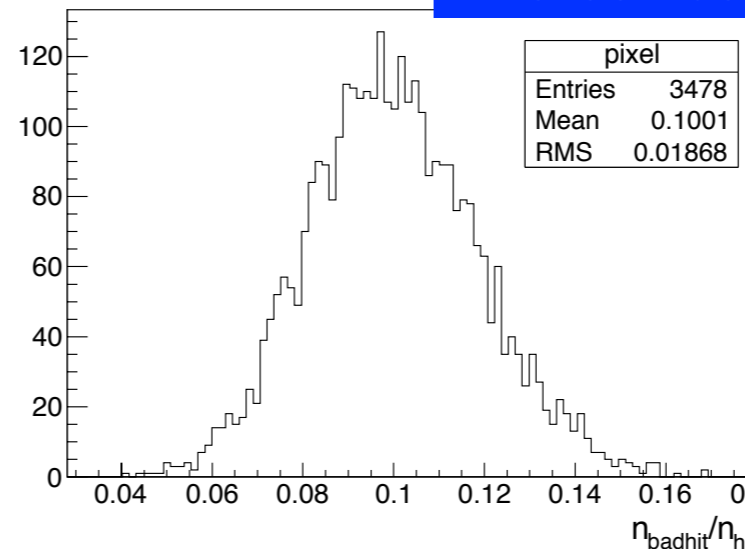
Binomial distribution: $P(n) = {}_N C_n \xi^n (1-\xi)^{N-n}$ (N: #hits, n: #bad hits)

$x := n/N$

The mean position is not recovered correctly if $x \neq \xi$

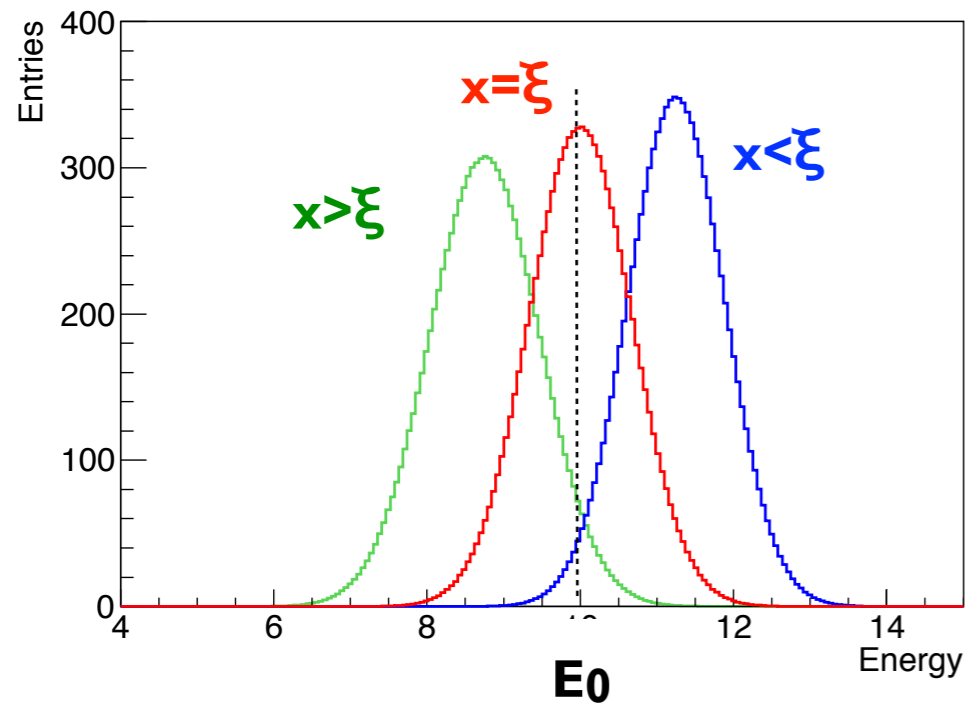
(Dead chips give the larger dispersion)

x distribution ($\xi=10\%$)



How does dead channels make **const. term** worse ?

- Energy distribution ends up in the superposition of many gaussians with different mean positions. → **Broaden the peak more (const. term effect)**



- ※ For each Gaussian:
width \sim stochastic behavior: $\sigma \propto 1/\sqrt{1-x}$
- ※ Weight of superposition $\sim x$ dist.
- ※ Const. term usually referred as “detector non-uniformity” or “mis-calibration”.

Essence: shower-to-shower difference of sampling fraction

- Since x dist. also has E dependence (higher $E \rightarrow$ more hits \rightarrow less fluctuation), this effect may contribute $1/\sqrt{E}$ term as well.

$$b_1(\xi) = \frac{q_0}{\sqrt{1 - q_1 \xi}}$$

	Pixel	Chip
q_1	1.0	1.6

($q_1 = 1$ if with stochastic effect only)

Jet Energy Resolution

4 terms mainly contribute to JER:

$$\frac{\text{rms}_{90}}{E} = \frac{21}{\sqrt{E}} \oplus 0.7 \oplus 0.004E \oplus 2.1 \left(\frac{R}{1825}\right)^{-1.0} \left(\frac{B}{3.5}\right)^{-0.3} \left(\frac{E}{100}\right)^{0.3} \% \quad (\text{M.Thomson 2008})$$

Calorimetry Leakage Tracker Confusion(Nature of PFA)

※ Leakage, tracker terms are probably independent of ξ

The rest of slides show that

- The dead channel effect to “calorimetry term” is not serious
- At least in low E_j or low ξ region, where the confusion term does not seem to rise significantly, the simulation result looks reasonable.

Calorimetry term

Calorimetry term contribution can be (simply) estimated for **each single jet** by the **error propagation of each jet particle energy measurement**

For a jet consisting of N_c charged particles, N_γ photons and N_h neutral hadrons

$$\sigma_{\text{calo}} \sim \sqrt{\sum_i^{N_c} (\sigma_c^i)^2 + \sum_i^{N_\gamma} (\sigma_\gamma^i)^2 + \sum_i^{N_h} (\sigma_h^i)^2}$$

energy: E_c^i, E_γ^i, E_h^i
 error: $\sigma_c^i, \sigma_\gamma^i, \sigma_h^i$ ($i=1,2,\dots,N_c (N_\gamma,N_h)$)

$$\sim \sqrt{\sum_i^{N_\gamma} (\sigma_\gamma^i)^2 + \sum_i^{N_h} (\sigma_h^i)^2}$$

Small contribution by charged particles can be neglected

$$\sigma_\gamma = E_\gamma \sqrt{b_0^2(\xi) + \left(\frac{b_1(\xi)}{\sqrt{E_\gamma}}\right)^2}$$

(ξ : dead rate)

$$\sigma_h = \underline{0.71} \sqrt{E(\text{GeV})}$$

Chosen so that σ_{calo} is consistent to M.Thomson's value.

(usually referred to 0.55-0.60)

$$\frac{\text{rms}_{90}}{E} = \frac{21}{\sqrt{E}}$$

Calorimetry term

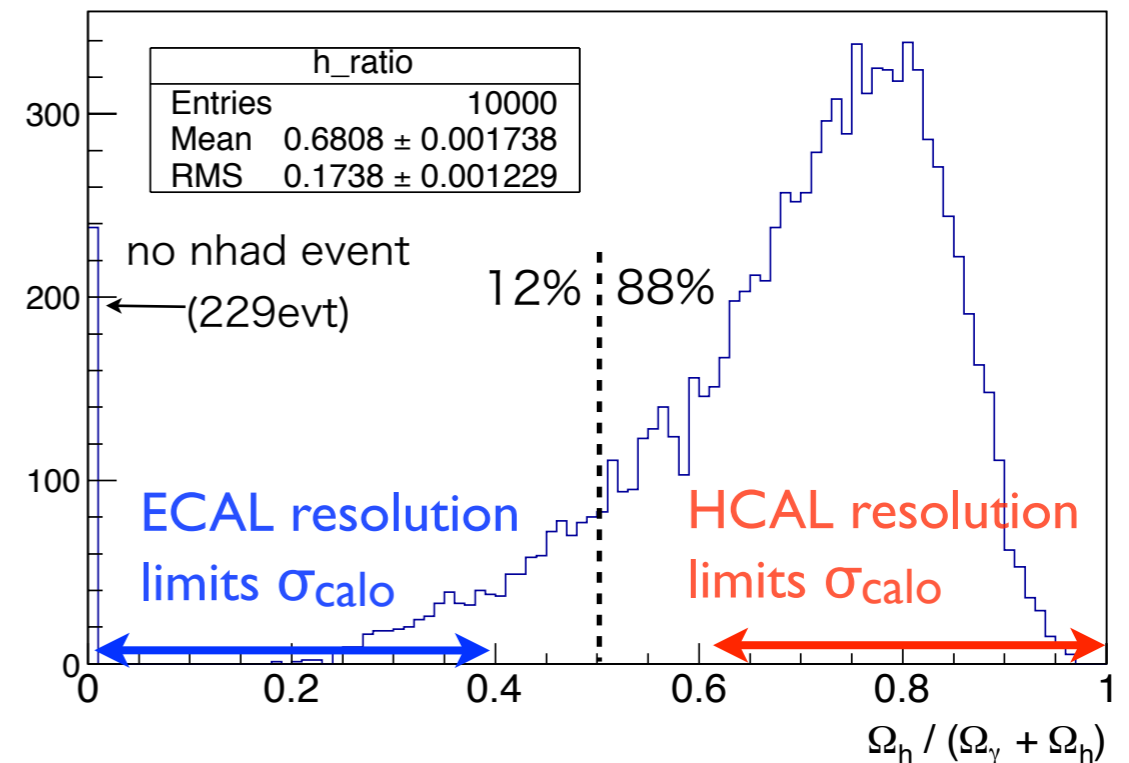
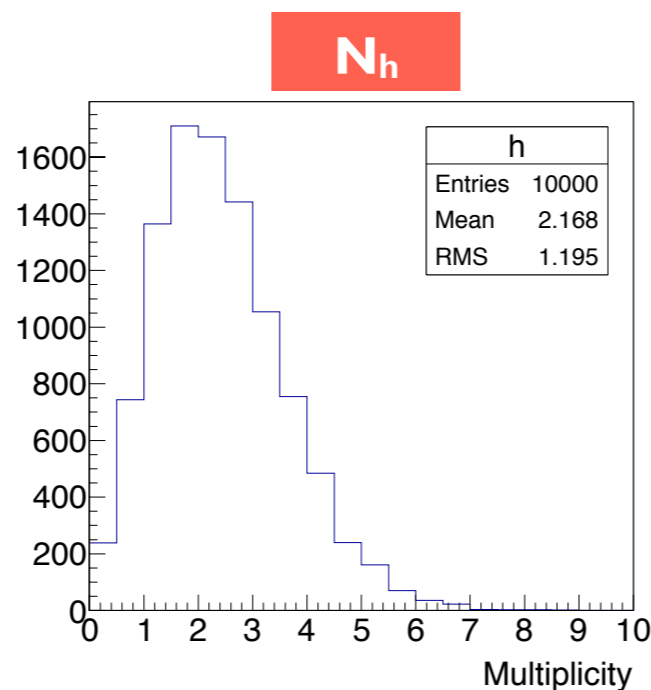
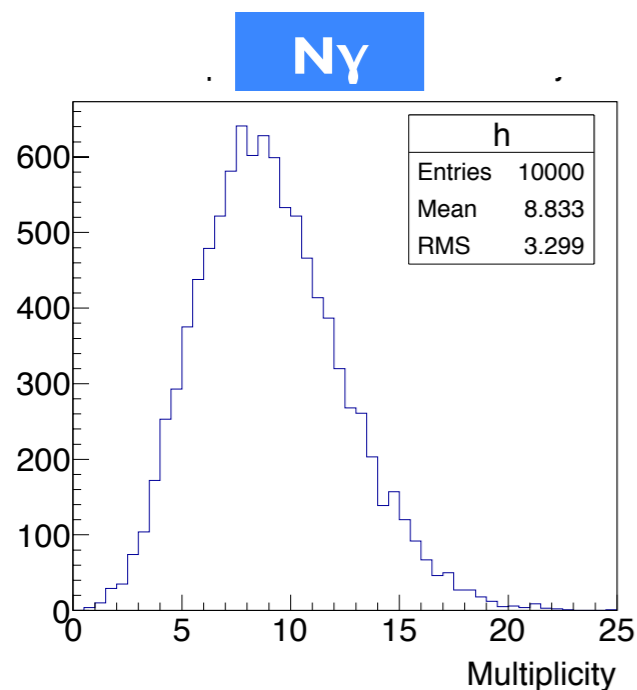
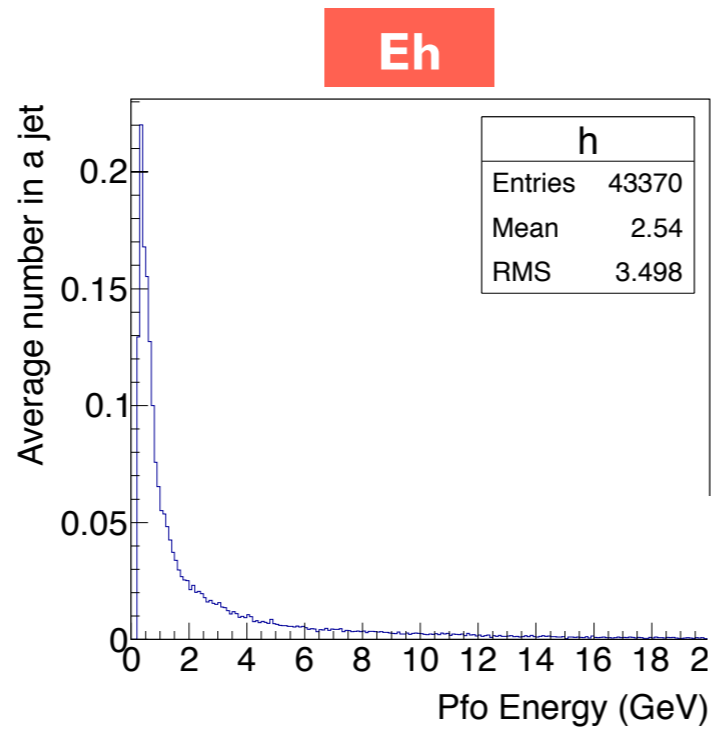
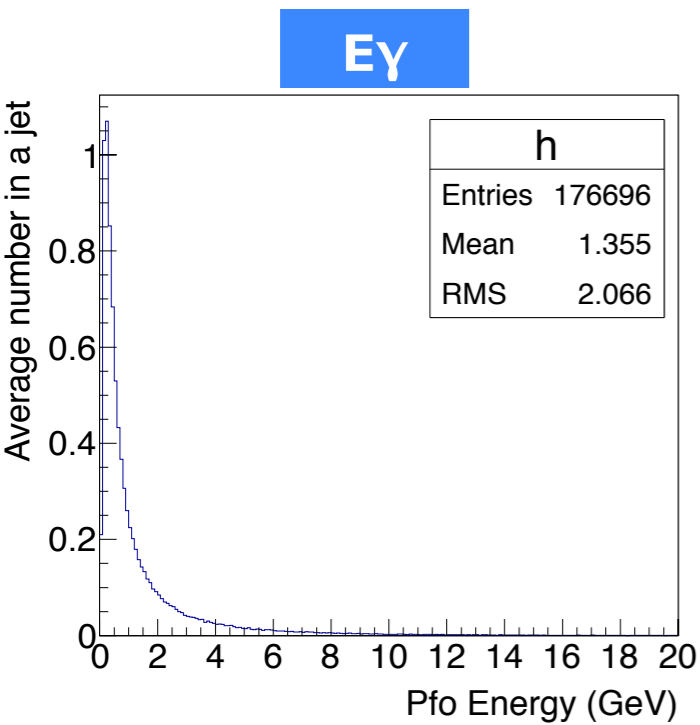
(45GeV jets sample / 10000events)

However, contribution from σ_h is **dominant** in σ_{calo} for most of jets

$$\sigma_{\text{calo}} \sim \sqrt{\sum_i^{N_\gamma} (\sigma_\gamma^i)^2 + \sum_i^{N_h} (\sigma_h^i)^2}$$

$$\equiv: \sqrt{\Omega_\gamma^2 + \Omega_h^2}$$

$\Omega_h / (\Omega_\gamma + \Omega_h)$

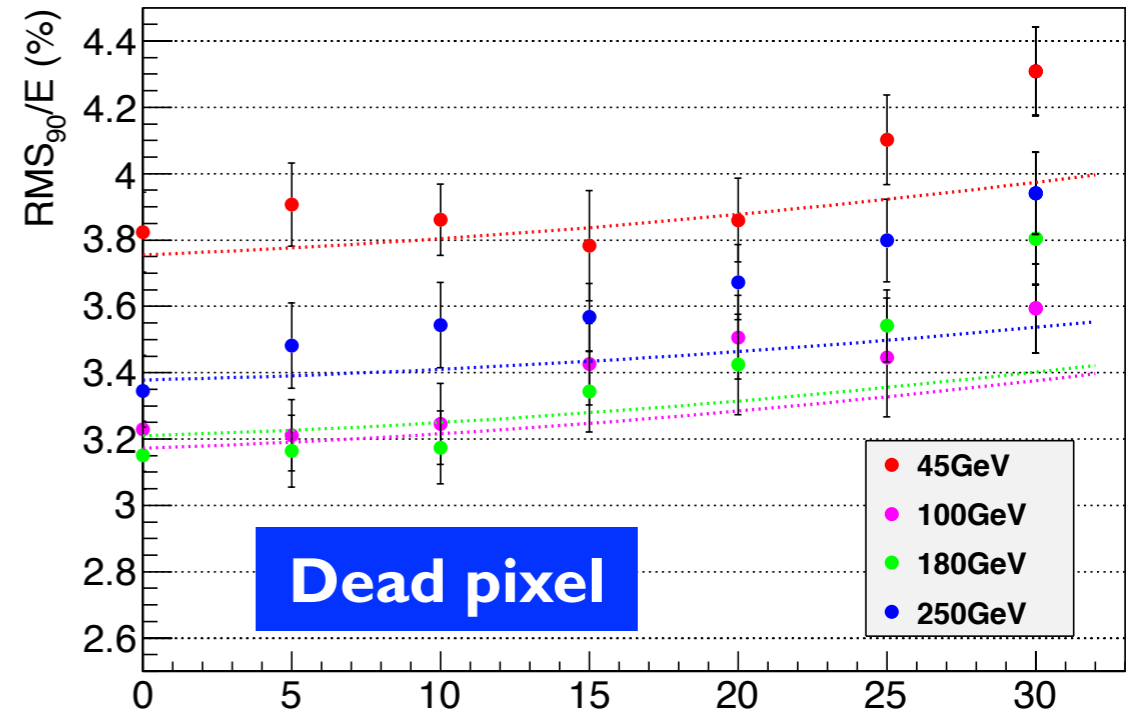
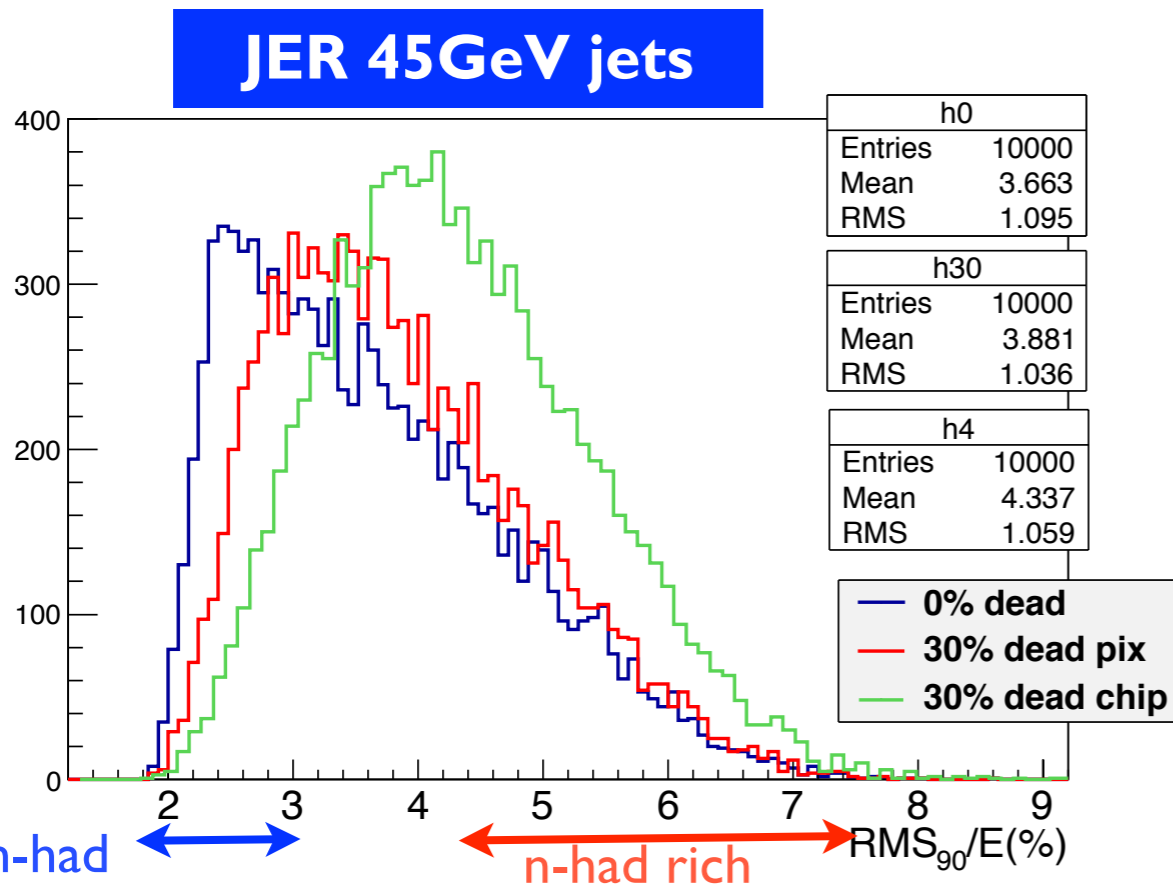


ECAL resolution mainly affects jets with less neutral hadron energy contribution

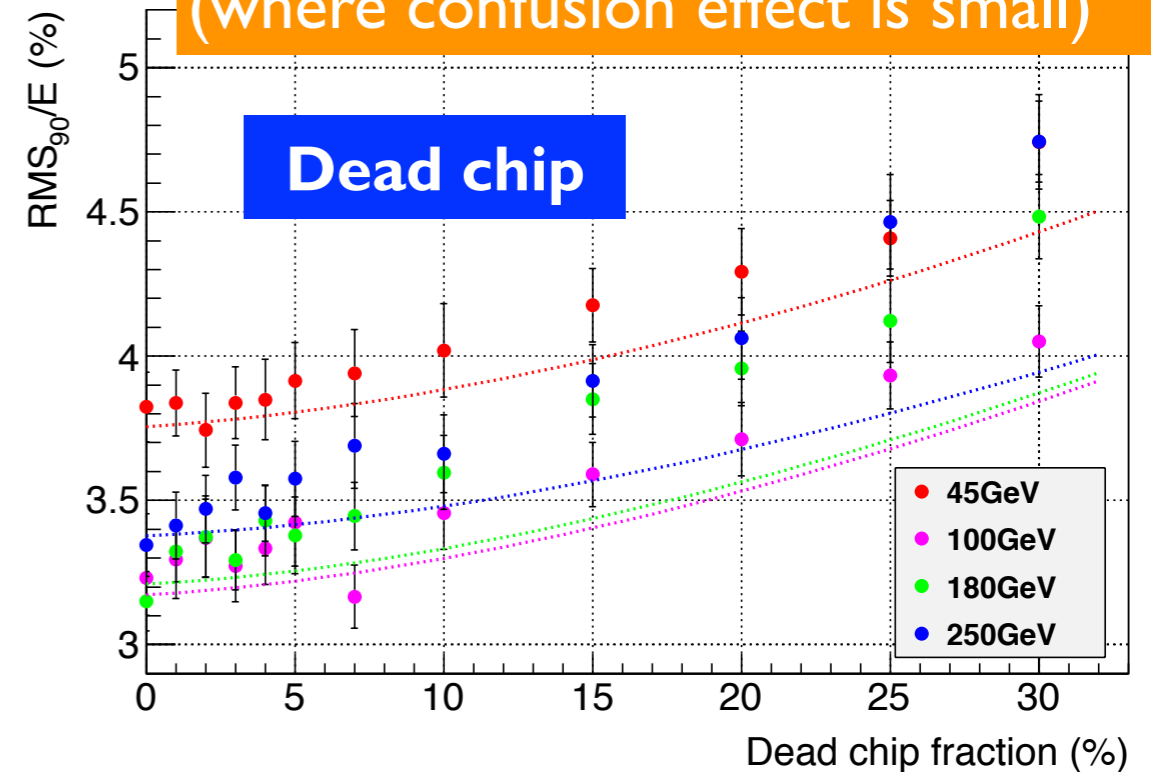
Calorimetry term

JER can be calculated from σ_{calo} , for each jet with different combination of the components

JER growth when only ξ dependence in the calorimetry term is taken in
(\bullet : simulation, $---$: calculation)



Well agree in low ξ / low E_j region
(where confusion effect is small)



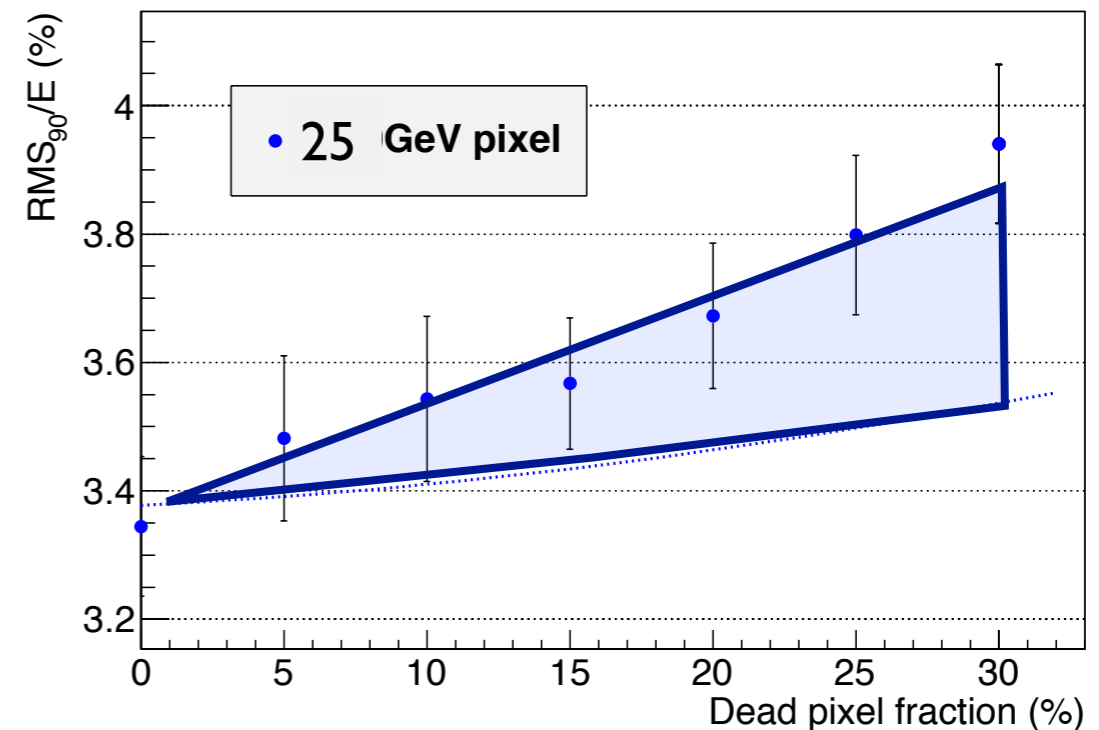
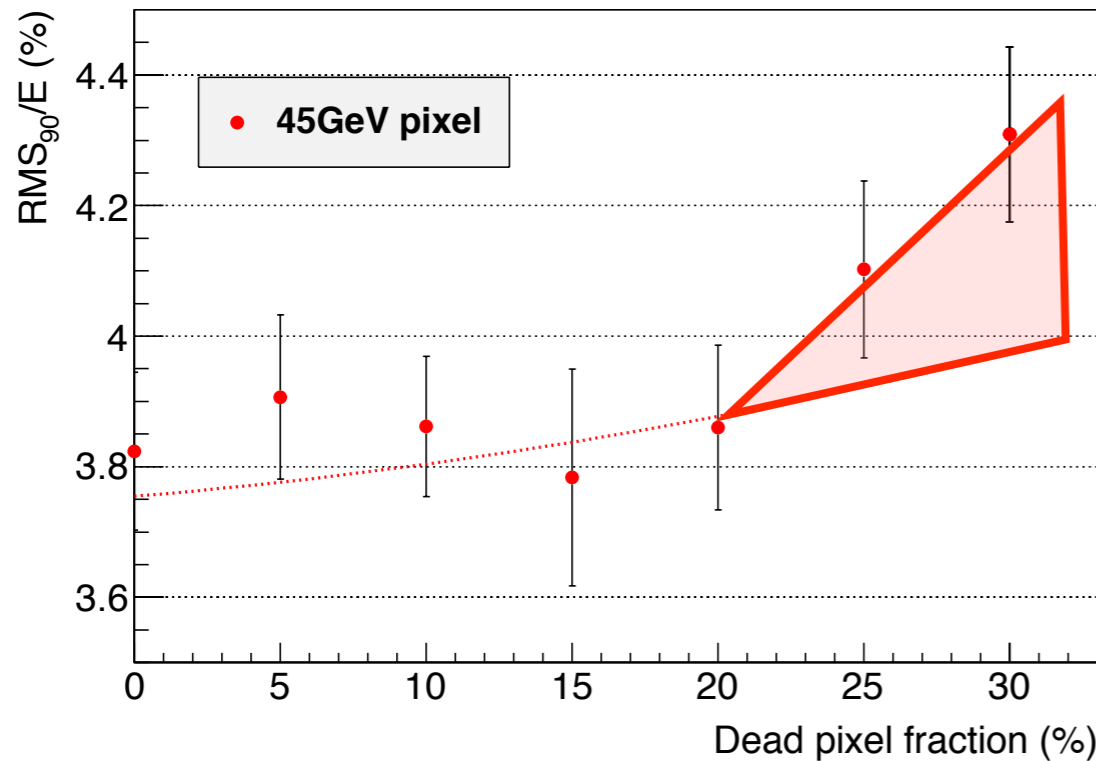
$$\text{JER} = \frac{0.79 \times \sigma_{\text{calo}}}{E_j} \oplus 0.7 \oplus 0.004 E_j \oplus 2.1 \left(\frac{E_j}{100} \right)^{0.3}$$

(if Gaussian) $\text{RMS}_{90} = 0.79 \times \text{RMS}$

ξ dep. of JER is calculated using the ξ dep. of ECAL obtained in page 7

Confusion term

$$\text{JER} = \frac{0.79 \times \sigma_{\text{calo}}}{E_j} \oplus 0.7 \oplus 0.004 E_j \oplus 2.1 \left(\frac{E_j}{100} \right)^{0.3}$$



Confusion becomes serious in high E jets, due to the closely overlapping showers.
(Already difficult to separate even with $\xi=0$. No allowance for dead channels)

While **low energy jet showers** seem to have some “allowance”?

(No problem with some effective granularity drop for good separation of showers)

Quantitate validation of this hypothesis is difficult... (statistics is too poor → grid?)

But this is highly consistent with our intuition!

Summary

- ECAL resolution does go worse

The degrade is quantitatively evaluated

$$\sigma_{\gamma} = E_{\gamma} \sqrt{b_0^2(\xi) + \left(\frac{b_1(\xi)}{\sqrt{E_{\gamma}}}\right)^2}$$

(ξ : dead rate)

(pixel)	(chip)
$b_0(\xi) = 1.6 (1 + 12\xi) (\%)$	$b_0(\xi) = 1.6 (1 + 28\xi) (\%)$
$b_1(\xi) = \frac{17.4}{\sqrt{1 - \xi}} (\%)$	$b_1(\xi) = \frac{17.4}{\sqrt{1 - 1.5\xi}} (\%)$

Small fraction of dead channels does not matter JER since

- ECAL resolution gives little influence on the calorimetry term in JER
HCAL resolution set the limit for most of the jets

- (For low E jet) Confusion does not rise with some dead channels
The allowance depends on E_j

Further implications

- Other dead channel models?

Non-uniform distribution (radiation damage etc.)

Dead sub-chip (4×4pix) etc.

⇒ The extent of degrade should be between uniform dead pix & uniform dead chip case

(The uniformity of sampling fraction is essential in thinking of dead effect!!)

- Schemes for recover resolution? (Restoration etc.)

As long as JER is concerned, not very necessary.

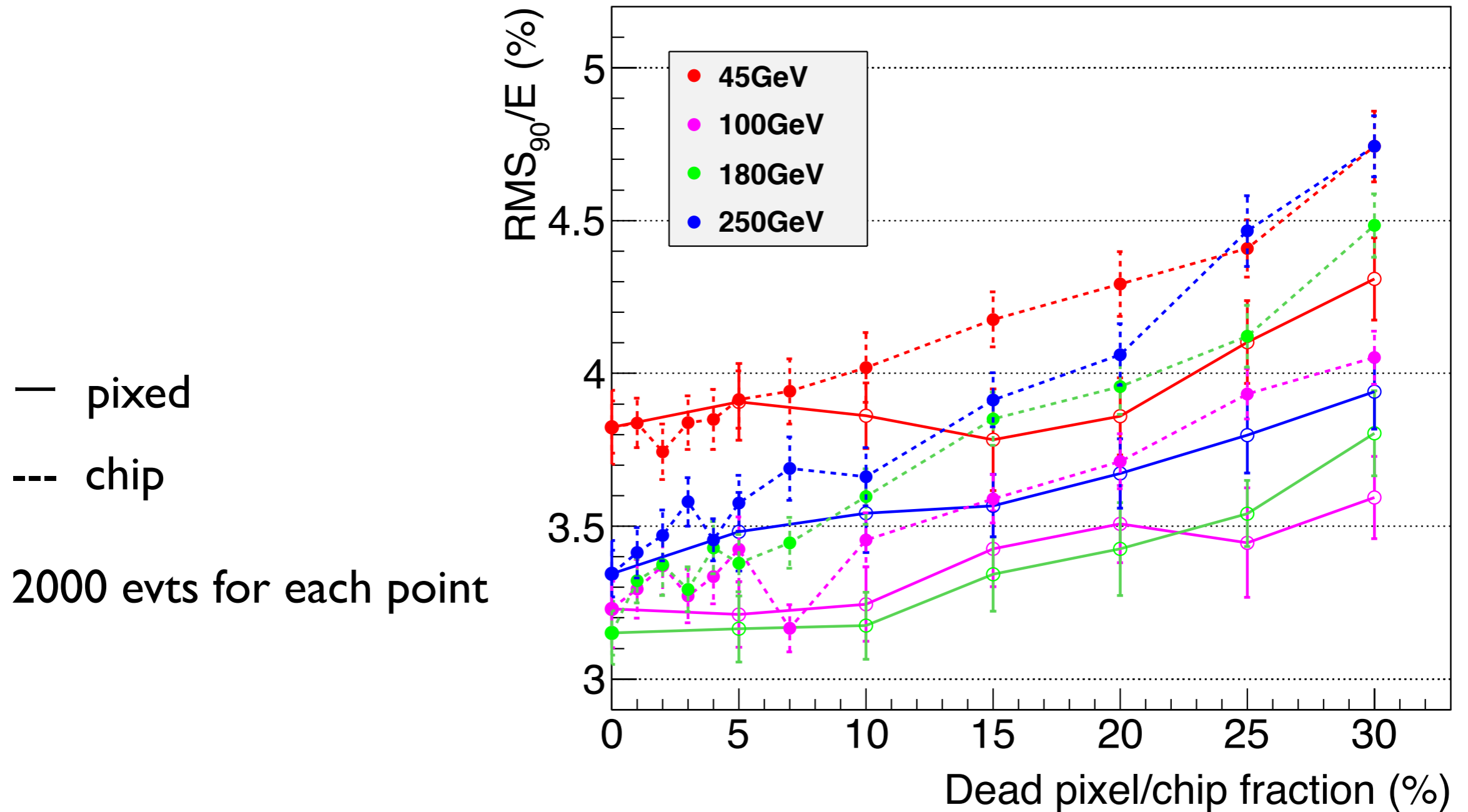
(>10% dead channels are not likely to be, damage to JER is limited)

But important for precise measurement of single photons
(especially with high energy)

Also in case with local defect, restoration is more effective than just shifting calibration coefficient

Backup

Combined plot

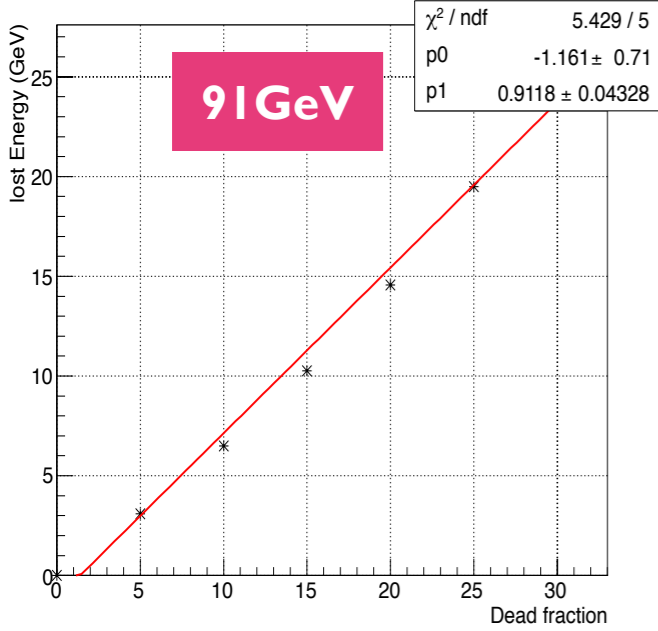


Unrecorded energy in ECAL (due to dead channels)

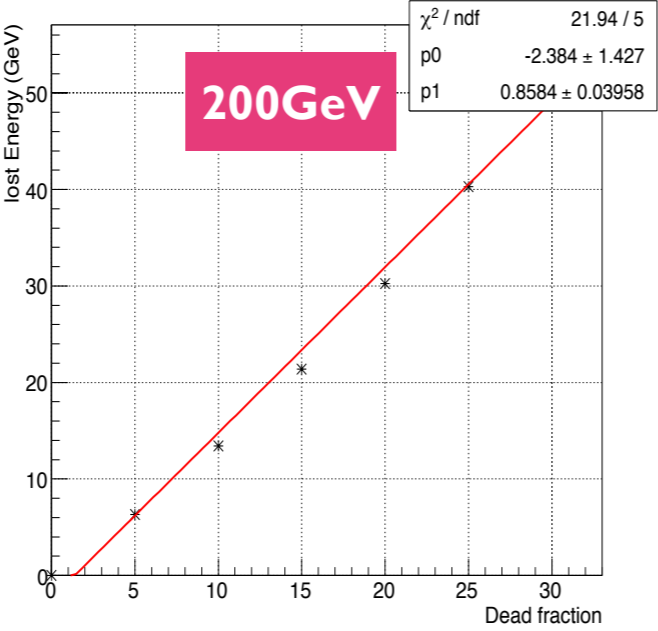
steepness < 1 (jet particles does not deposit whole energy in ECAL), which varies along E

(Dead pixels, jet events)

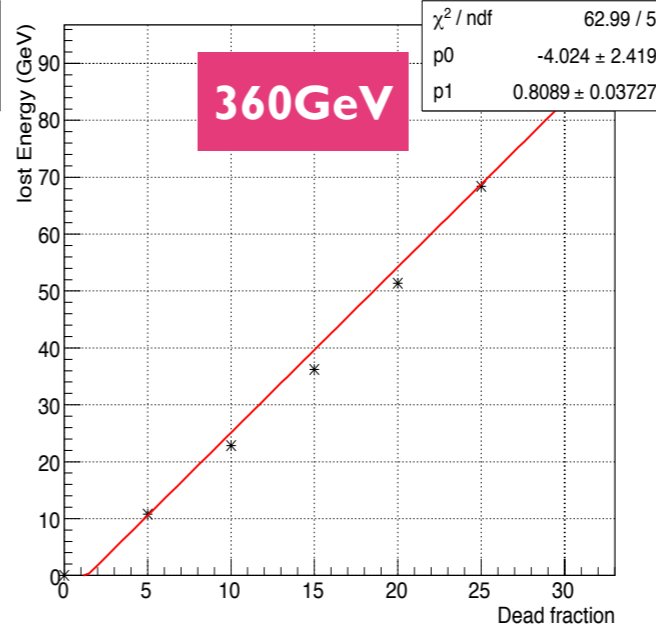
Lost energy @91GeV dead pixels



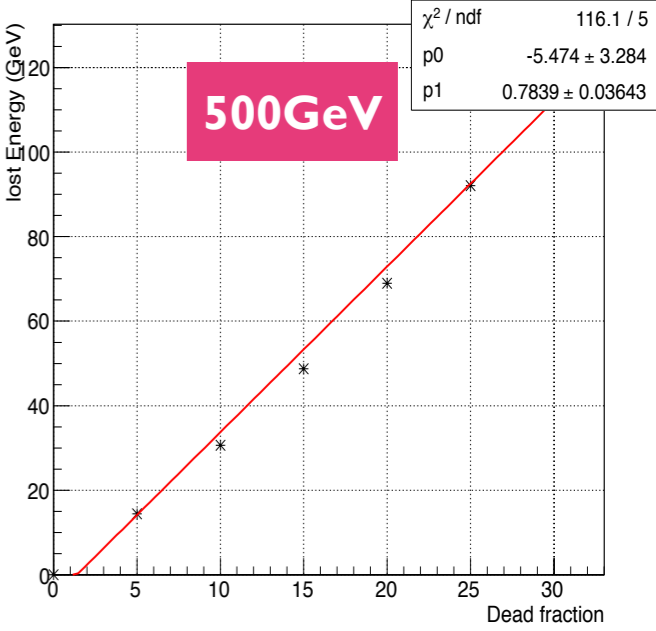
Lost energy @200GeV dead pixels



Lost energy @360GeV dead pixels

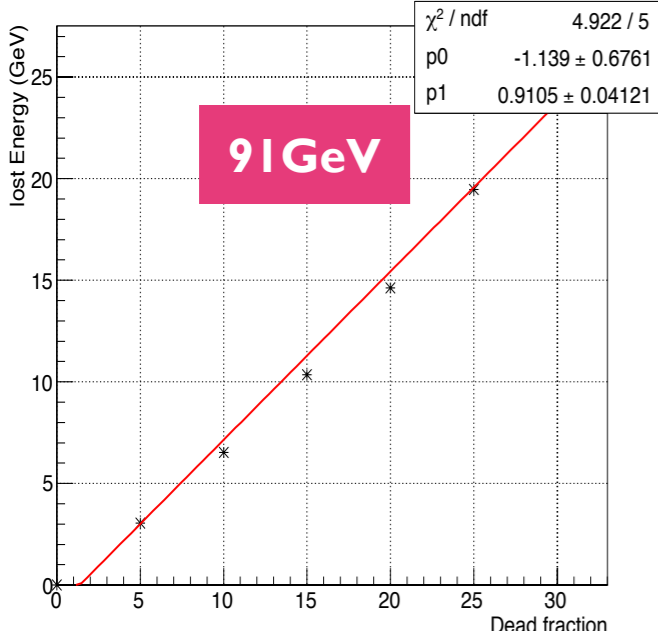


Lost energy @500GeV dead pixels



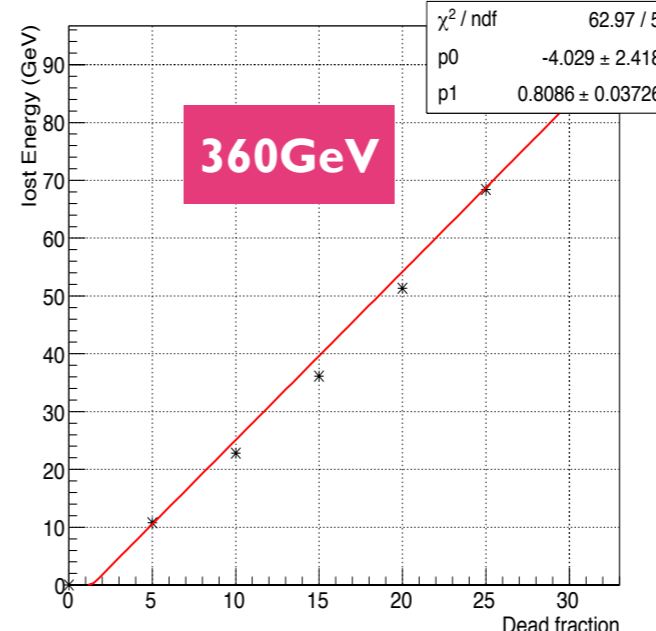
(Dead chips, jet events)

Lost energy @91GeV dead chips

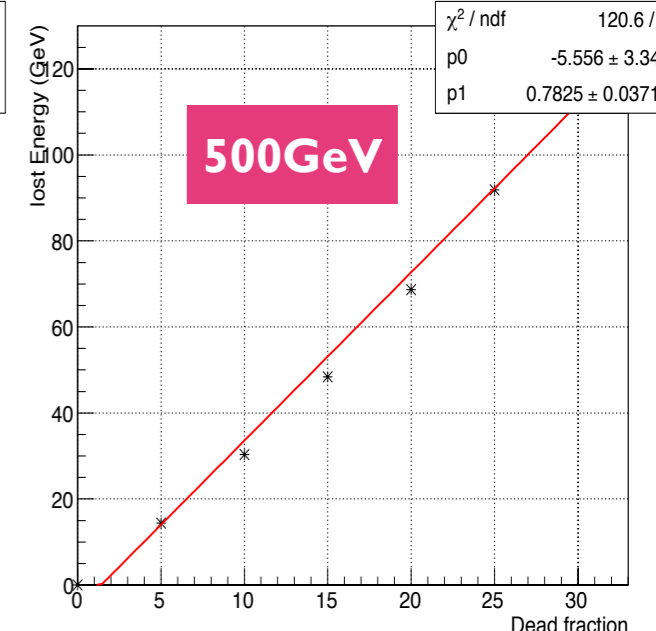


The file of 200GeV/dead chip was lost...

Lost energy @360GeV dead chips

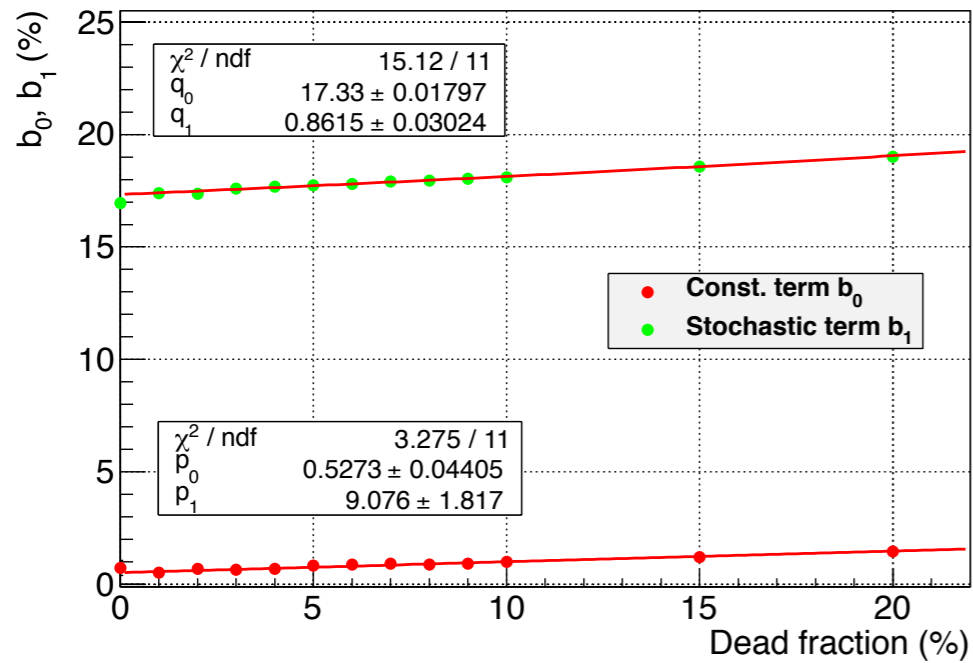


Lost energy @500GeV dead chips

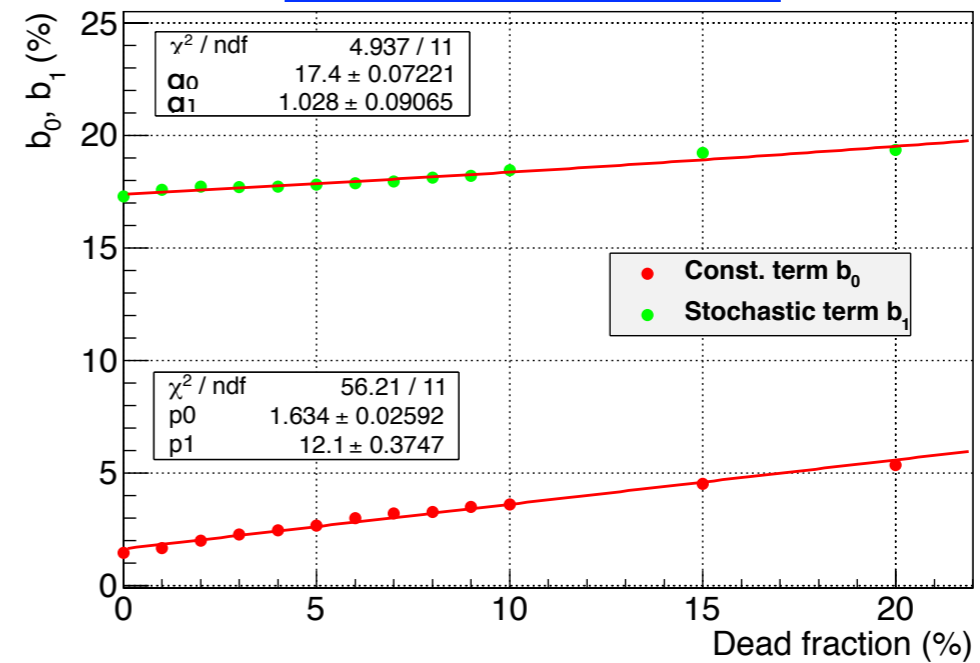


Hypothesis on stoch./const. term - backup by Toy MC

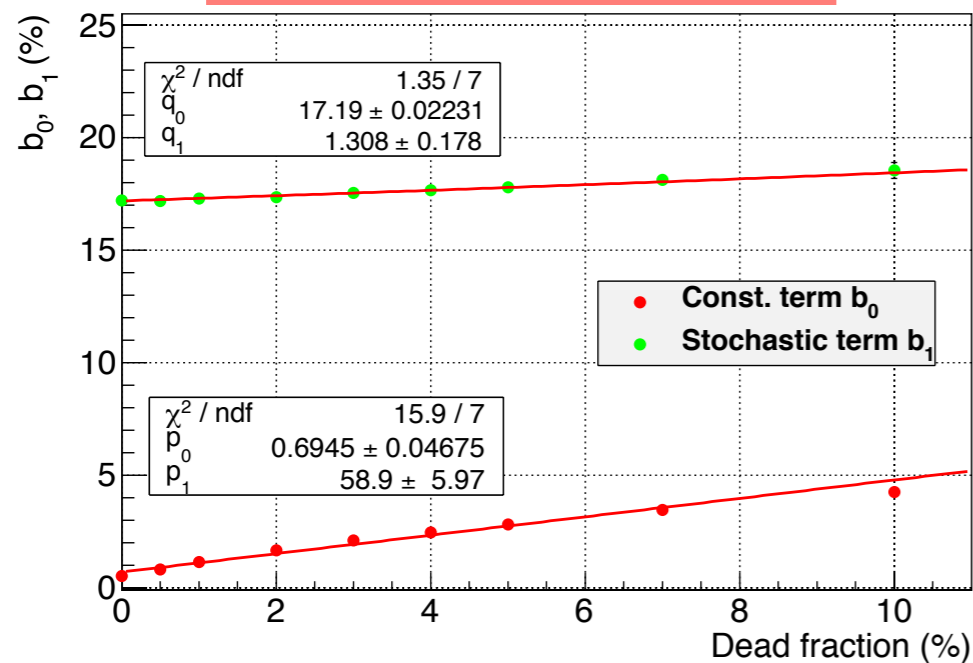
ToyMC / Pix



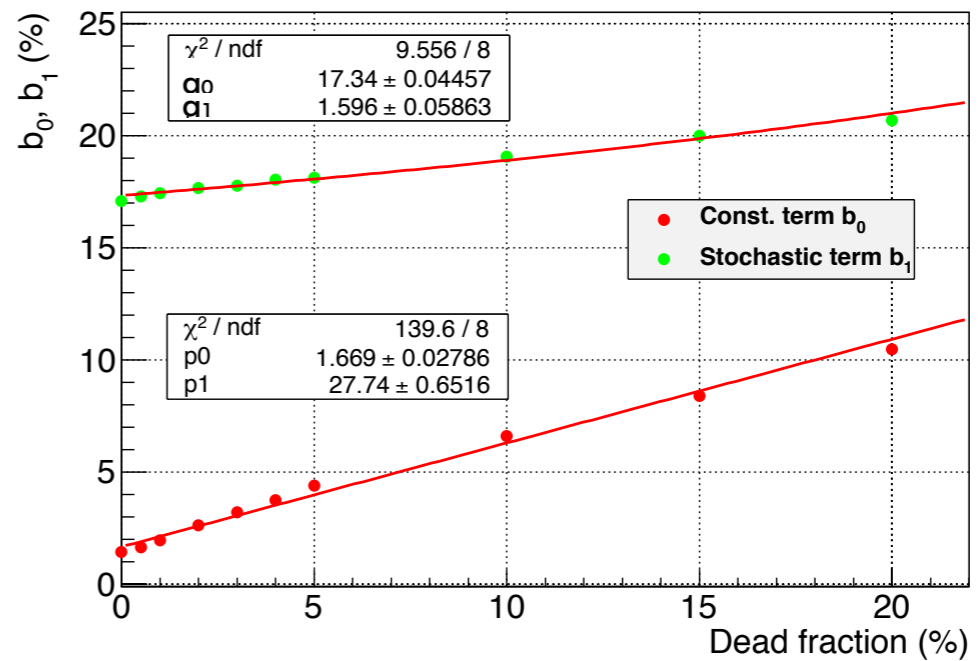
Dead Pixel



ToyMC / Chip



Dead Chip



Tendency is reproduced?

The slope / offset are systematically small than simu. \rightarrow still some minor effect?

Neutral hadron resolution modeling

$$\sigma_h = 0.71 \sqrt{E(\text{GeV})}$$

0.71 is too large?

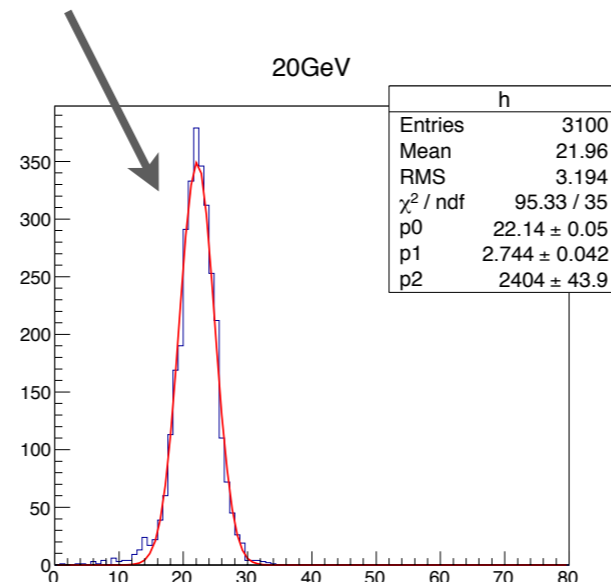
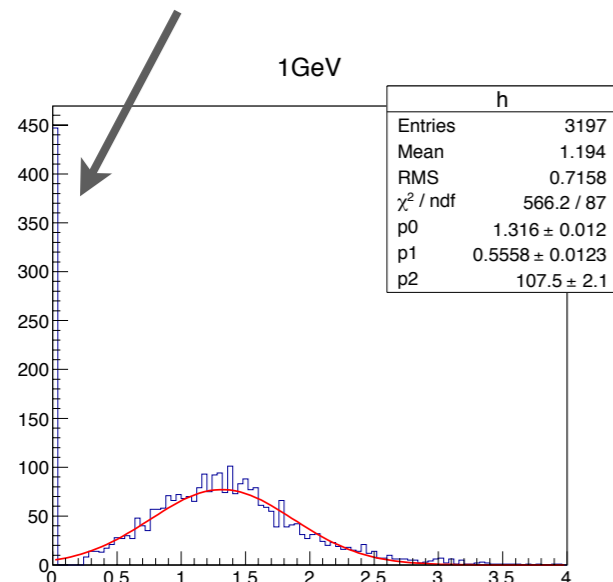
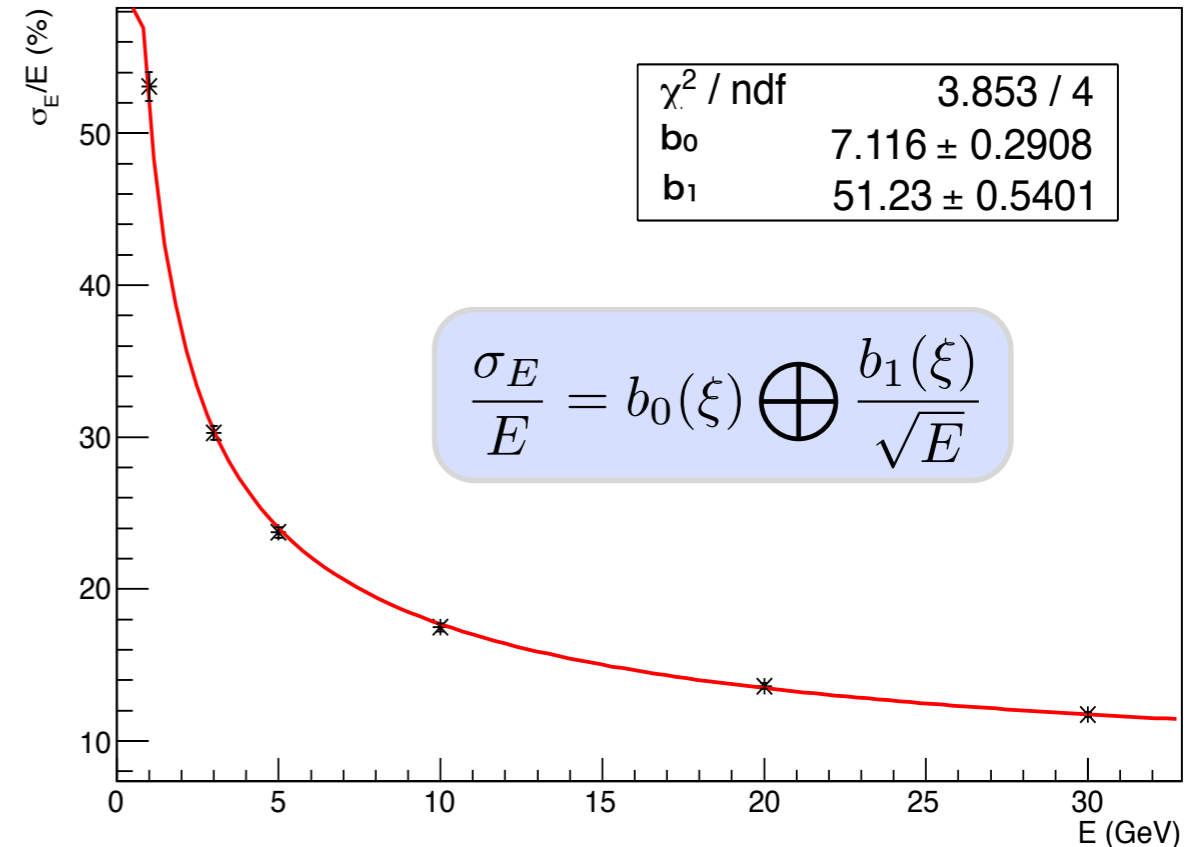
Tried to estimated by own using single K_L sample

($\cos\theta < 0.7$, use events including only neutral hadron PFOs)

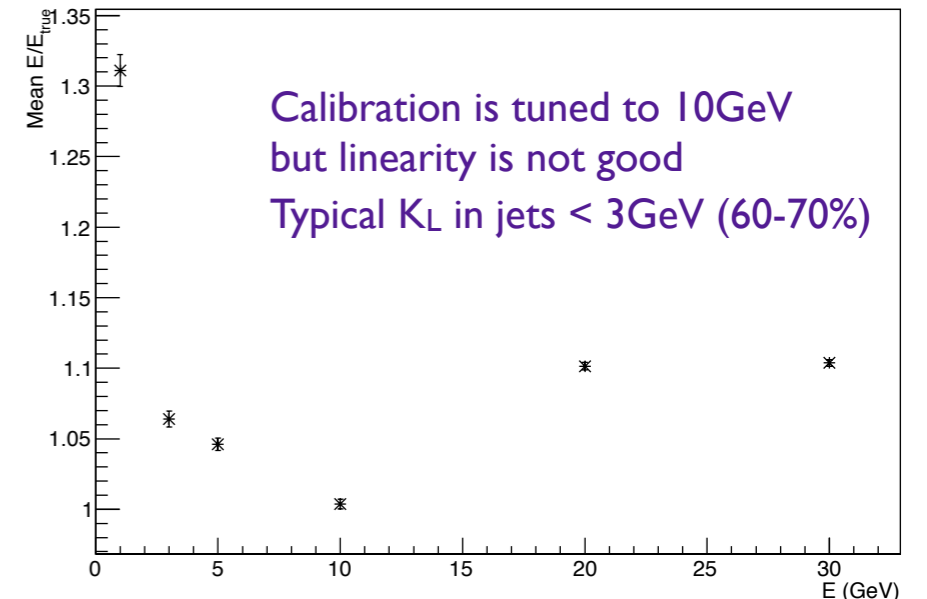
Well fit with const. term
Stochastic factor ~ 0.5 ?

But many abnormal behaviors in energy distribution (0.71 as effective coeff. is possible?)
(0 energy events / wrong mean position)

Neutral hadron pfo resolution $\sigma_E/E = b_0 + b_1/\sqrt{E}$ (G-fit)

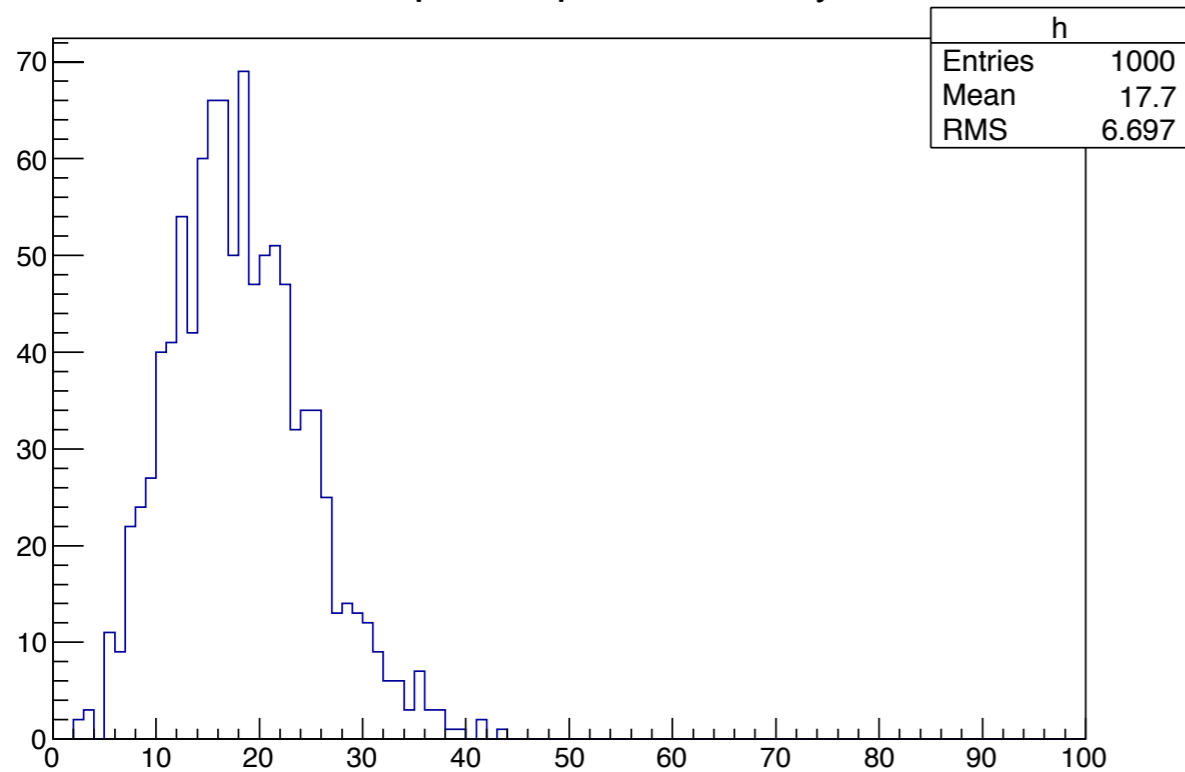


Mean energy of K_L events (G-fit)

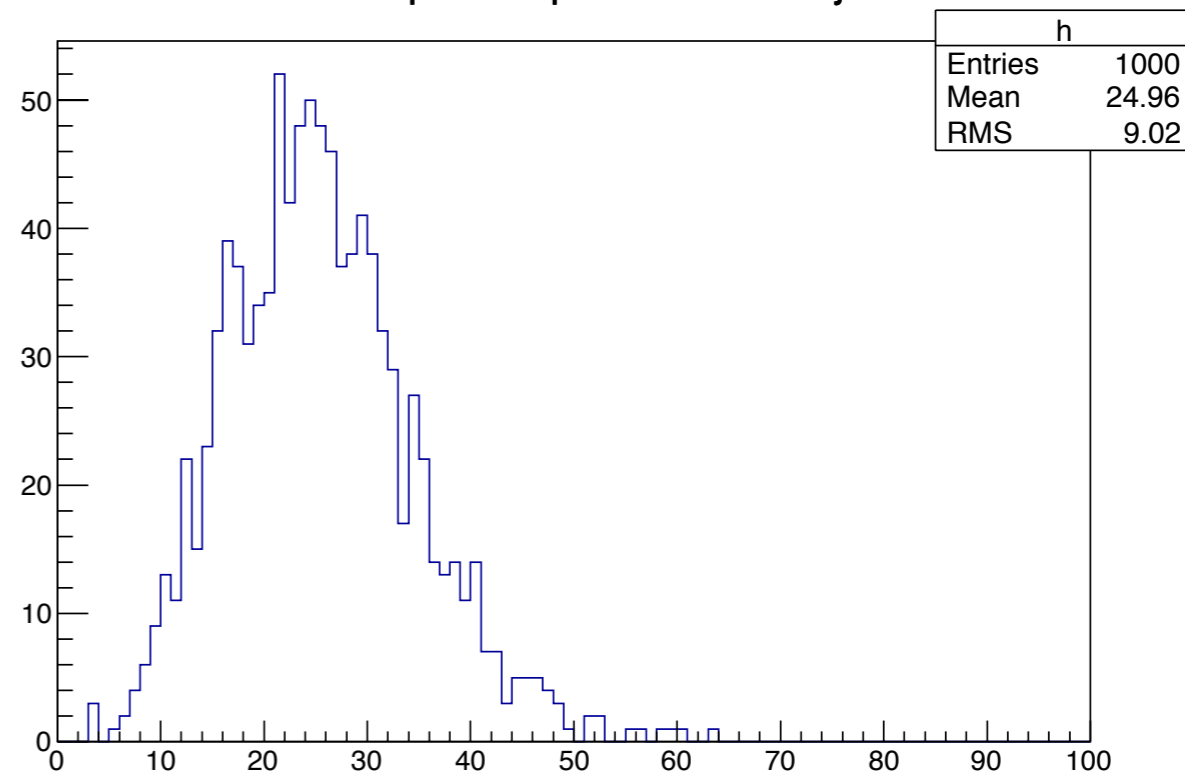


Number of photon pfo in a jet

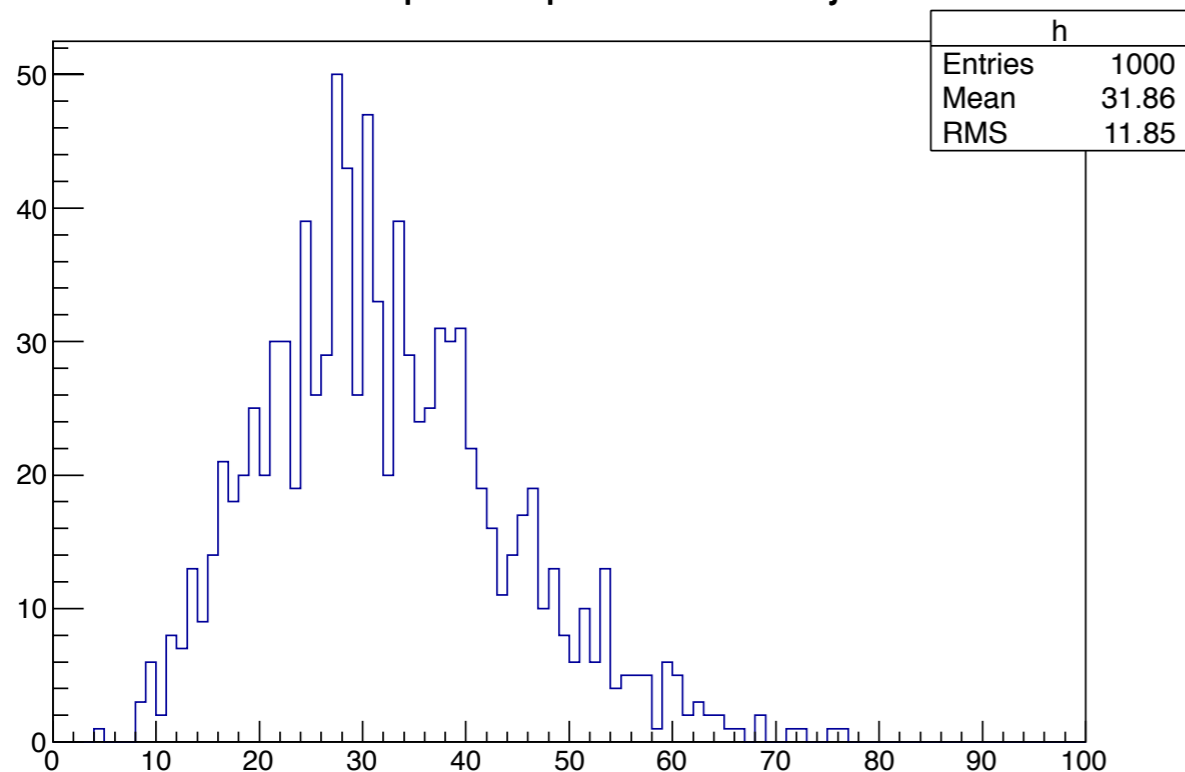
Number of photon pfo in 91GeV jet evt



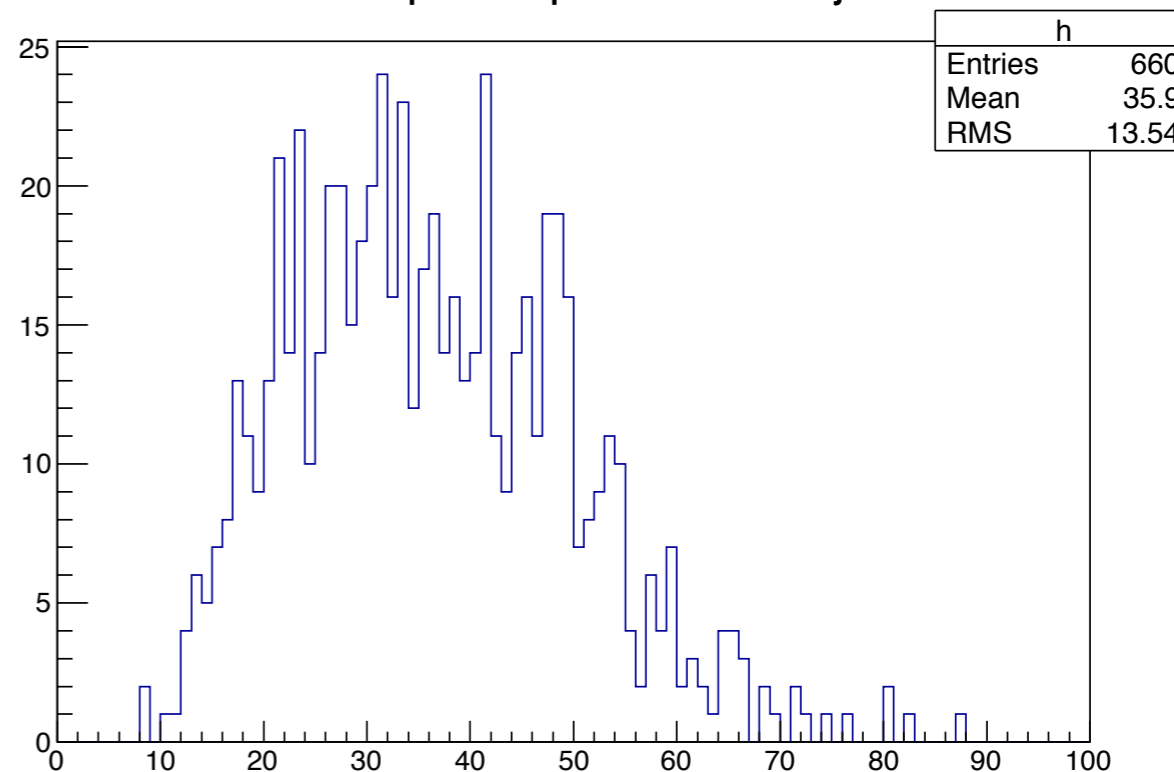
Number of photon pfo in 200GeV jet evt



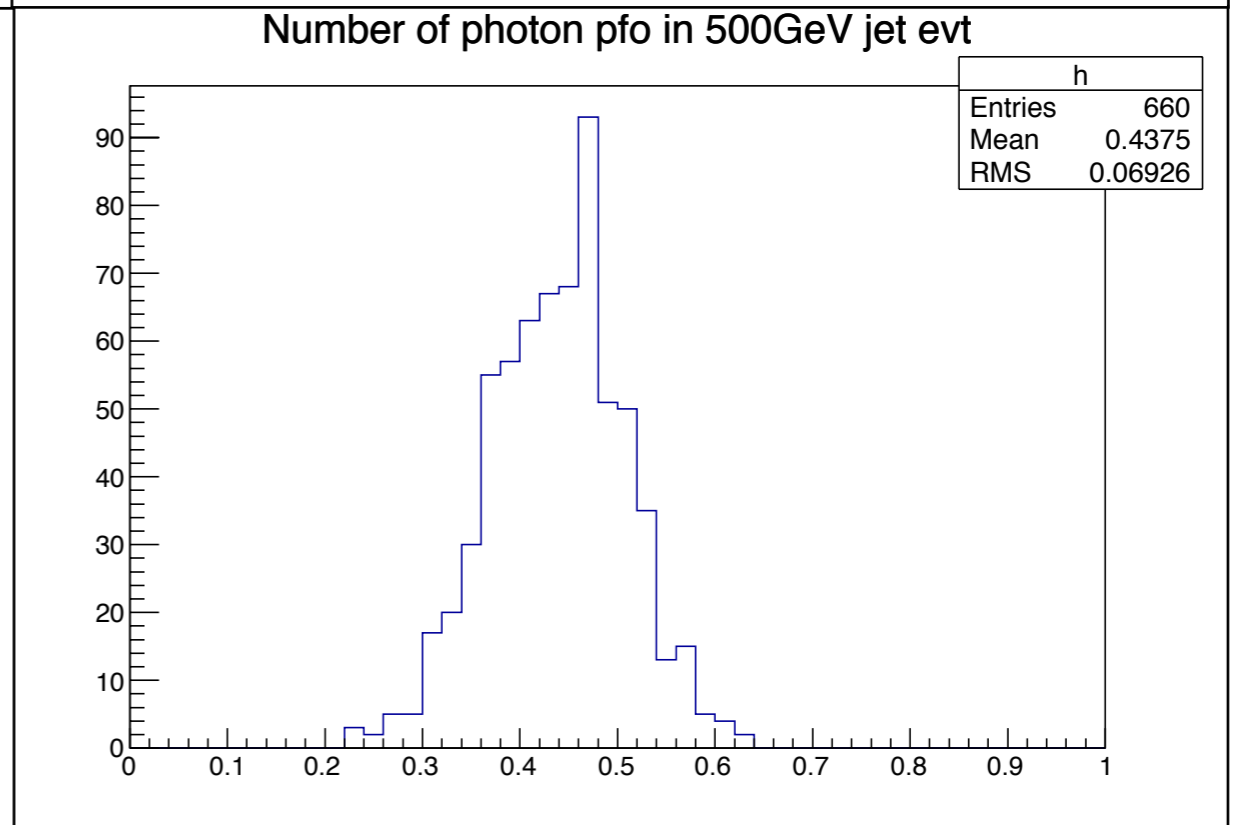
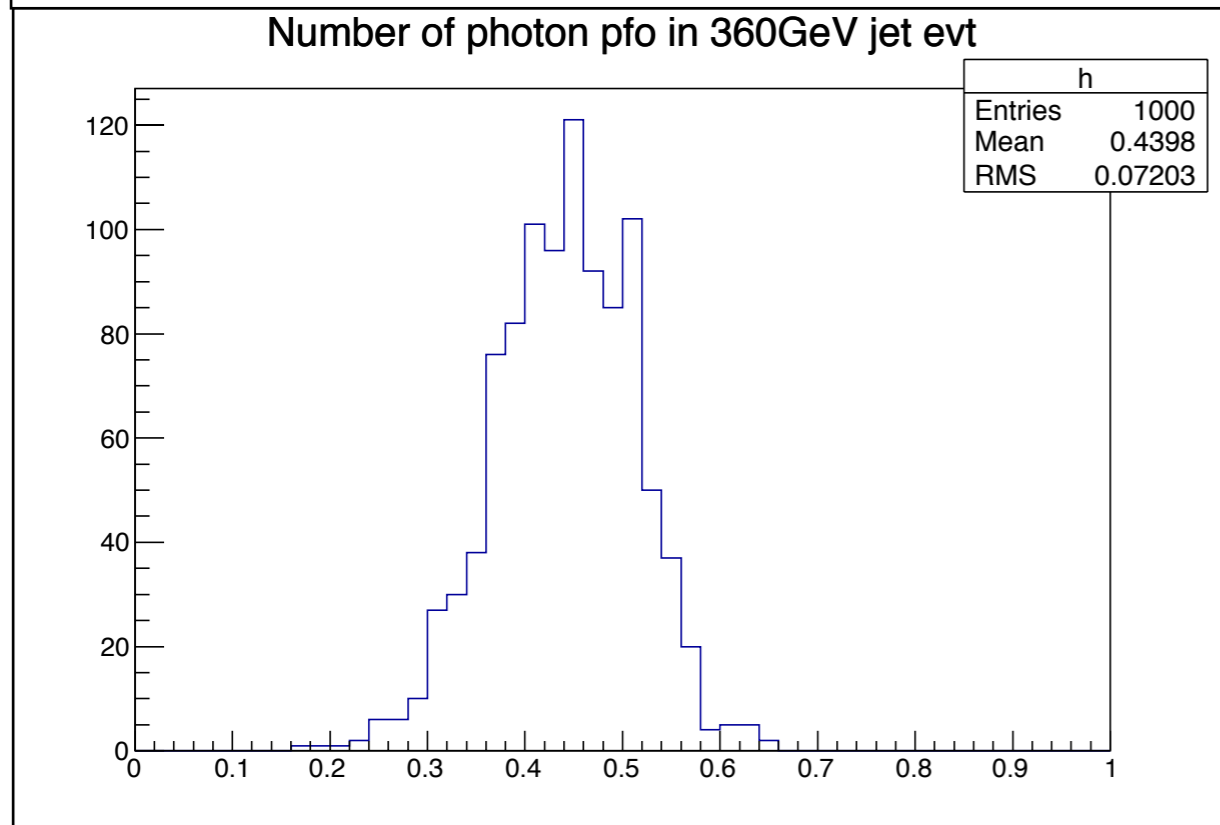
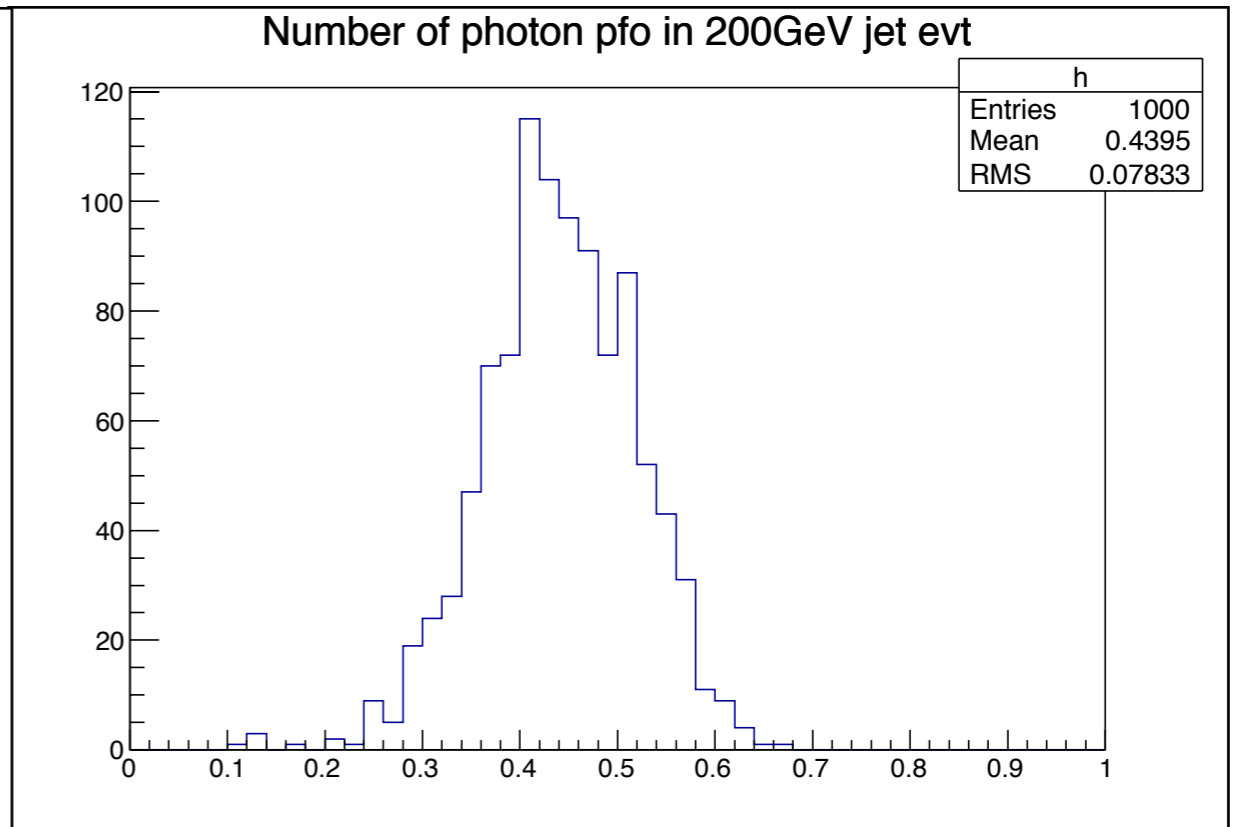
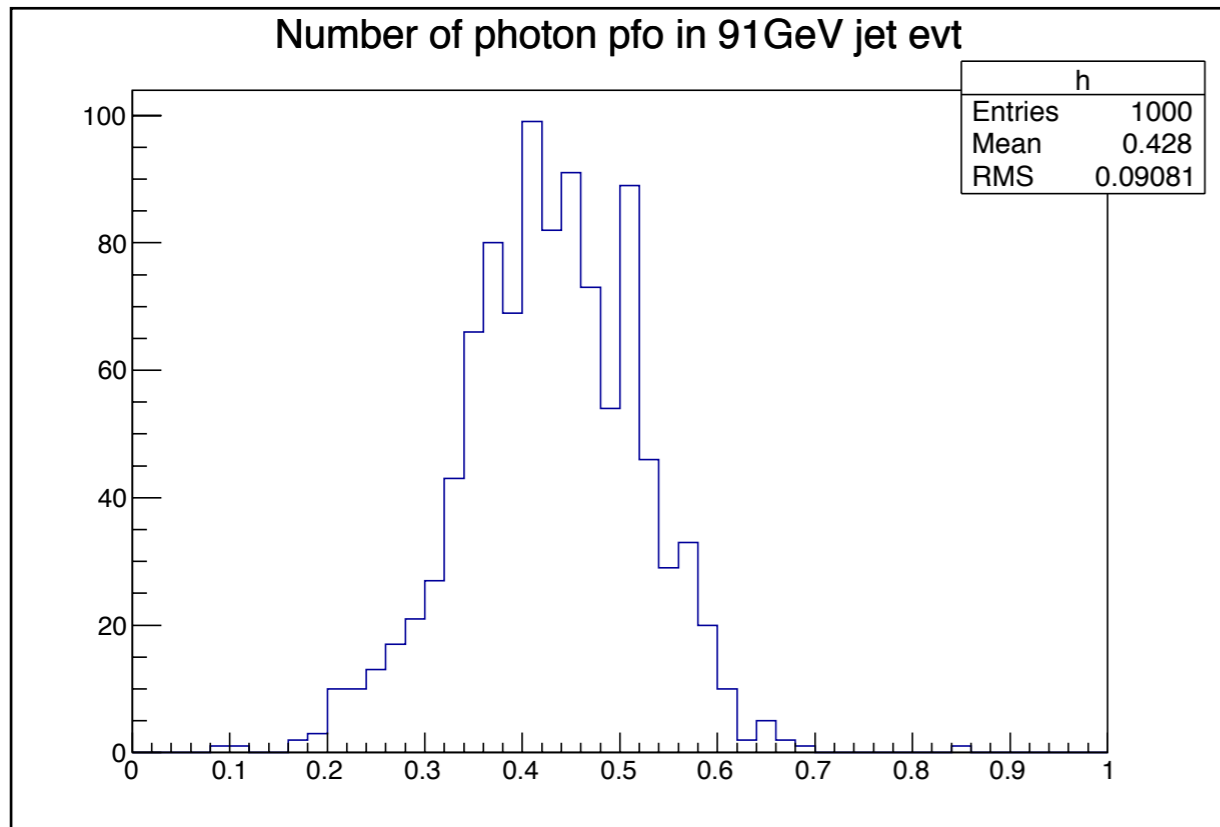
Number of photon pfo in 360GeV jet evt



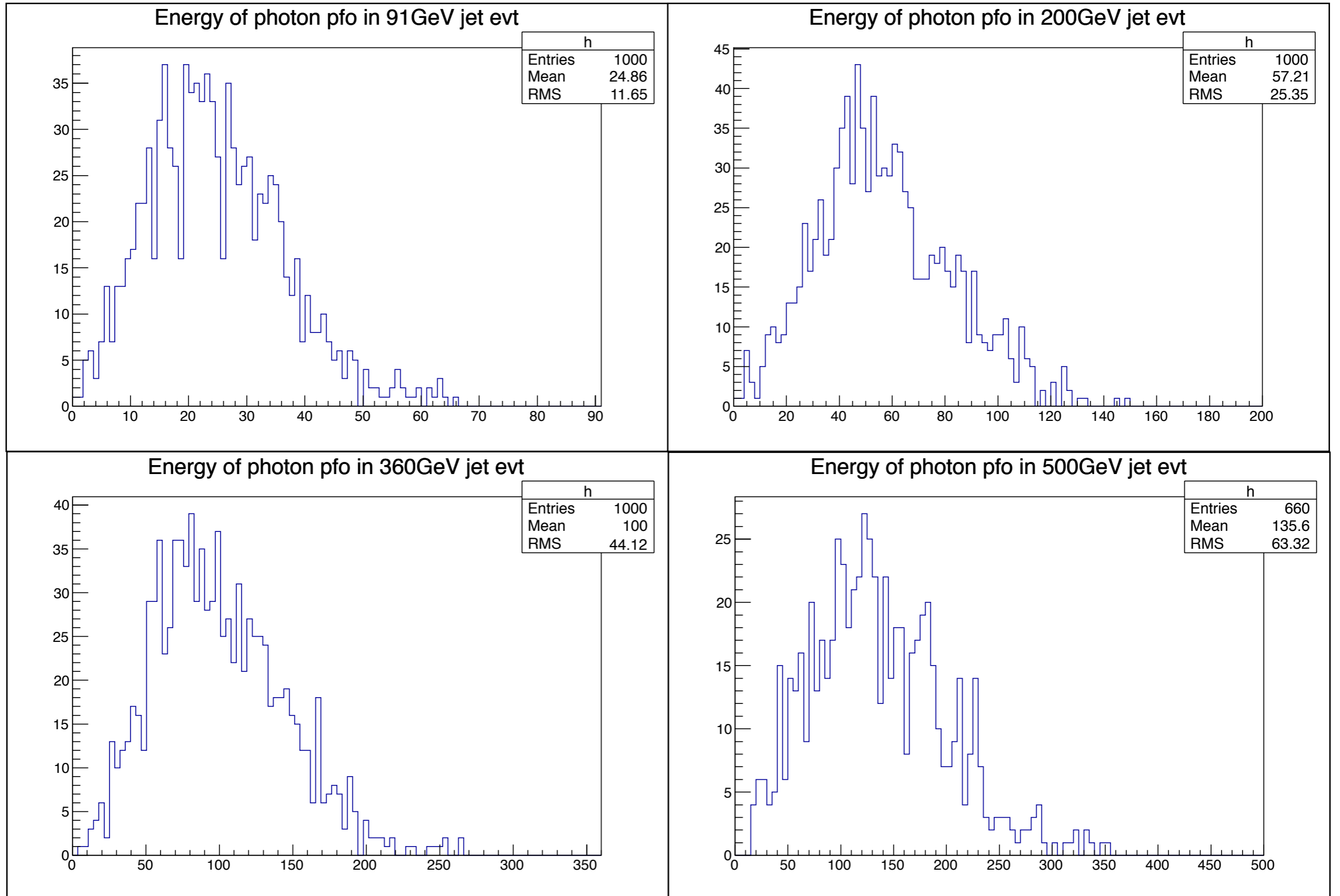
Number of photon pfo in 500GeV jet evt



Number fraction of photon pfo in a jet

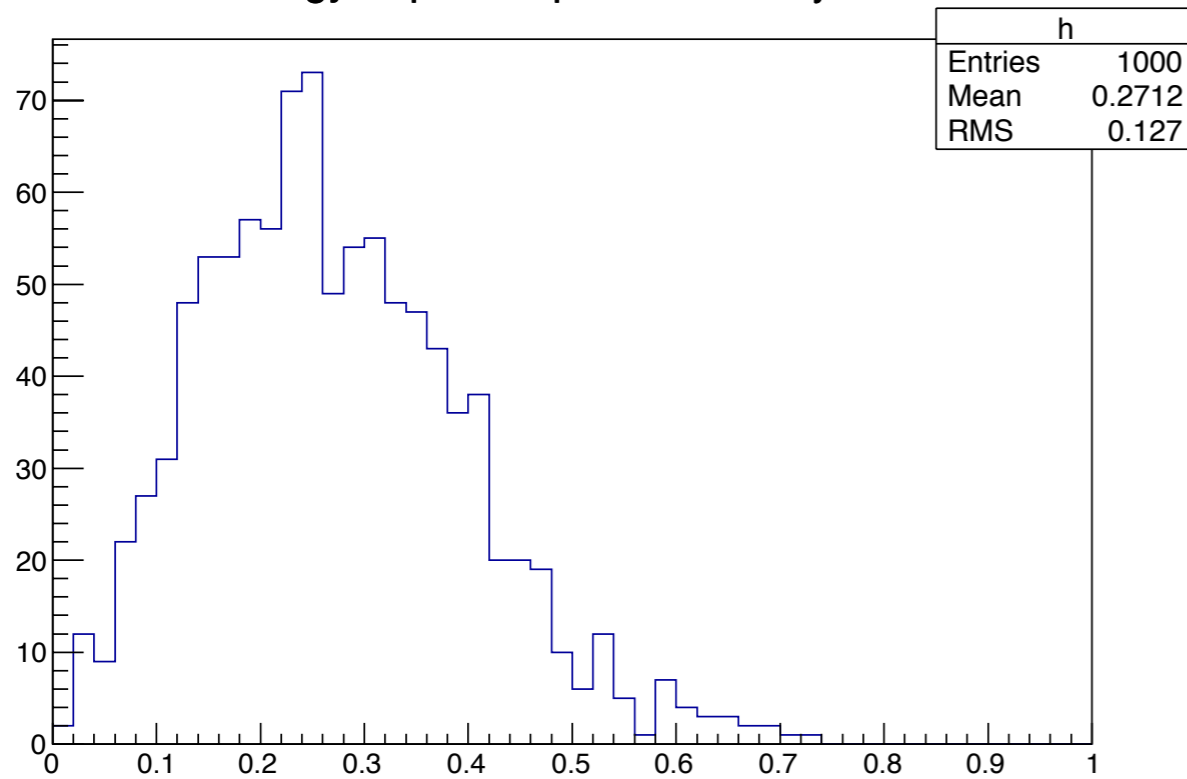


Photon Energy in a jet (GeV)

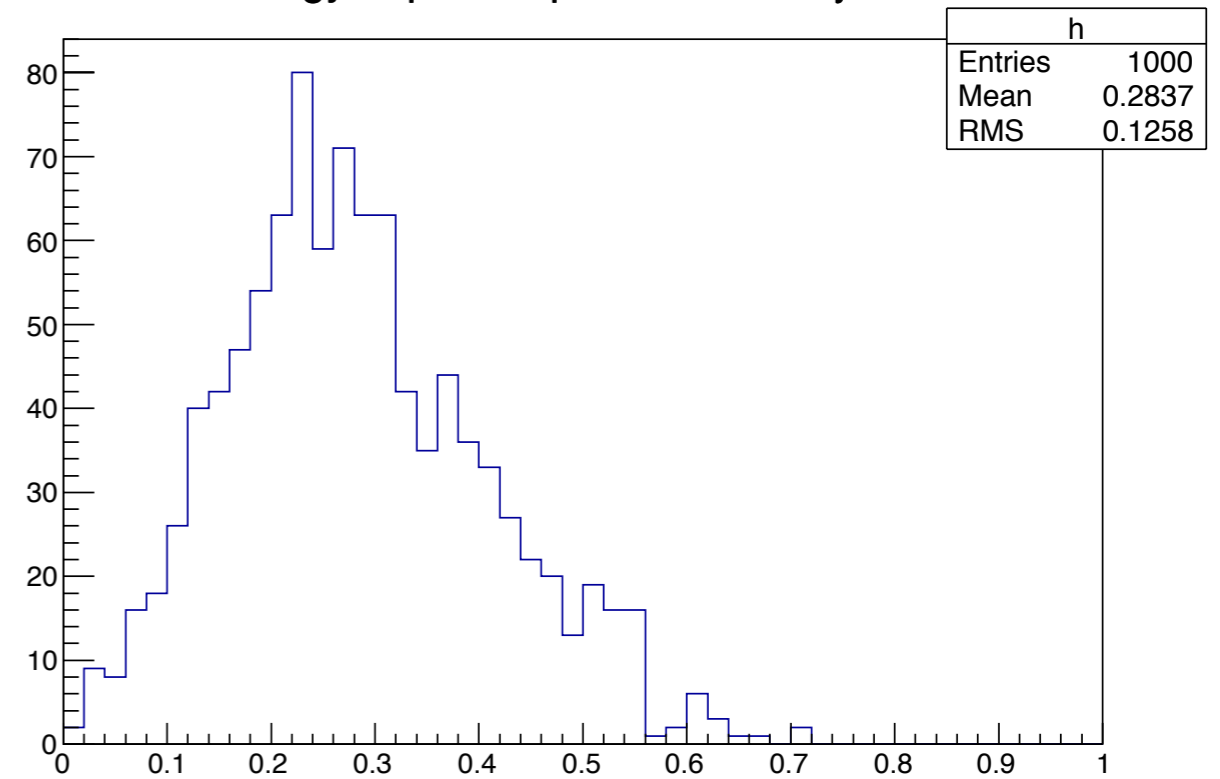


Photon Energy fraction in a jet

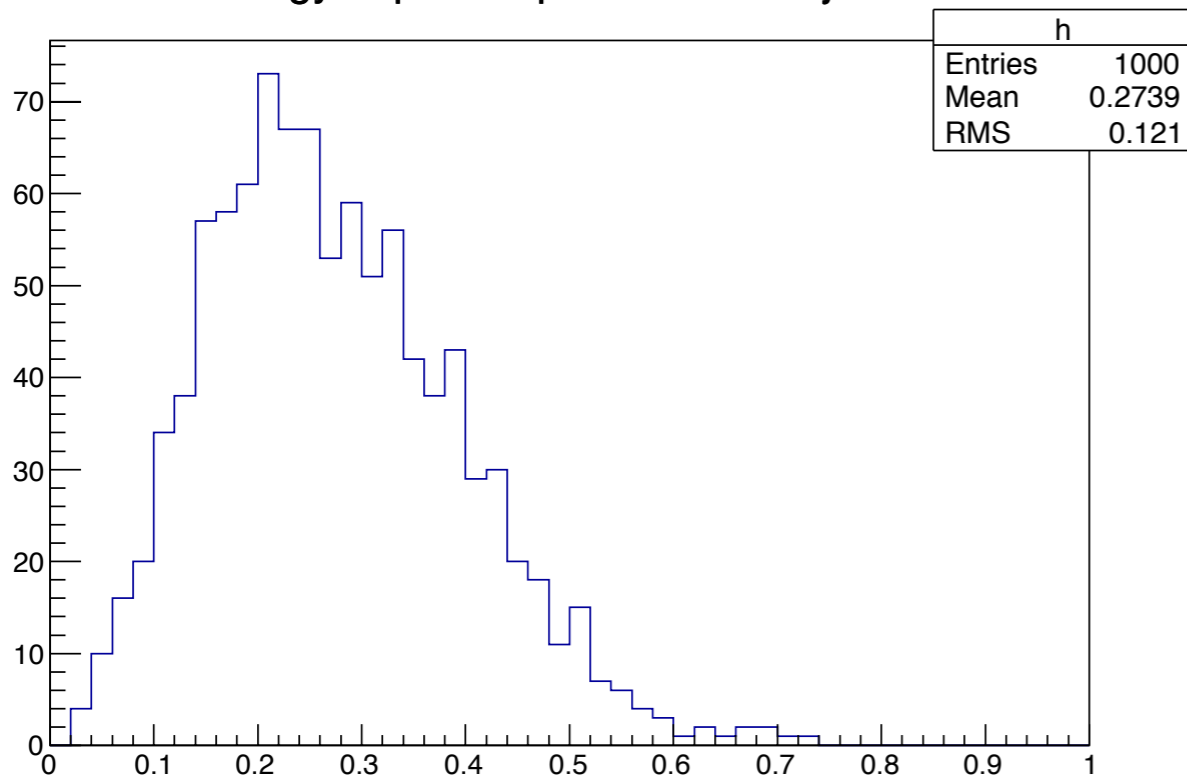
Energy of photon pfo in 91GeV jet evt



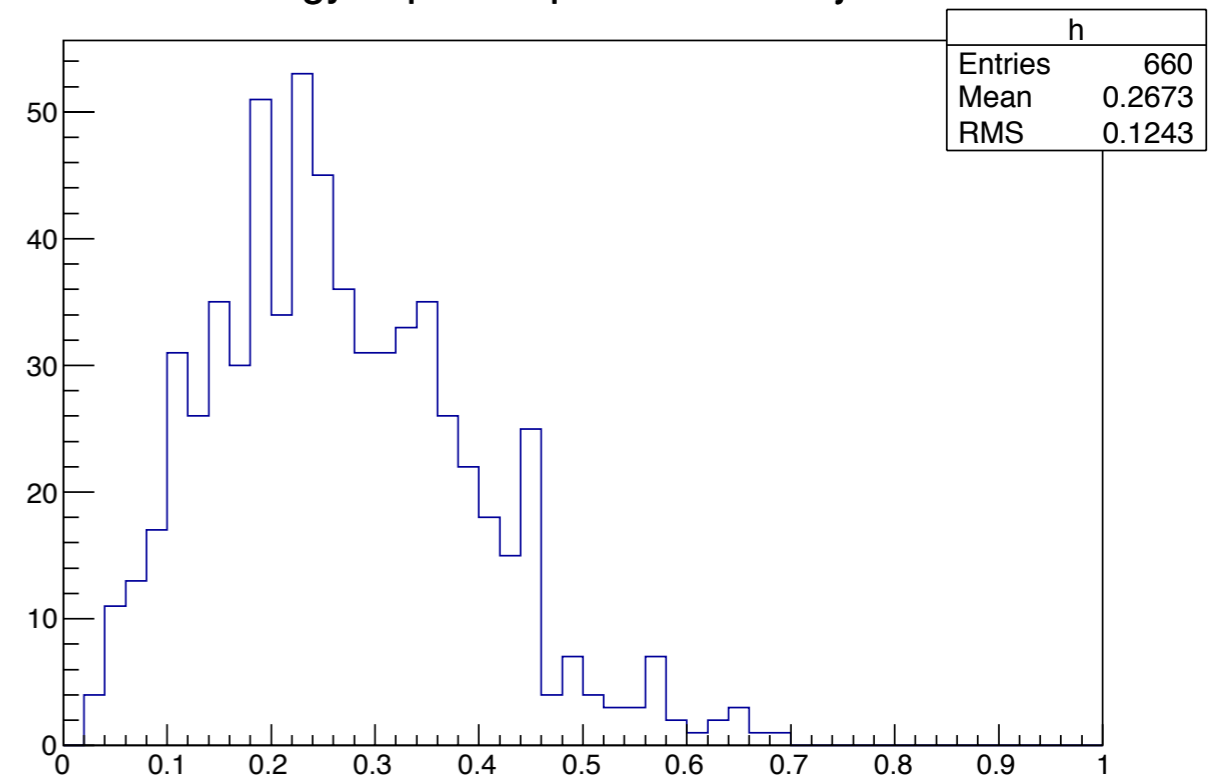
Energy of photon pfo in 200GeV jet evt



Energy of photon pfo in 360GeV jet evt

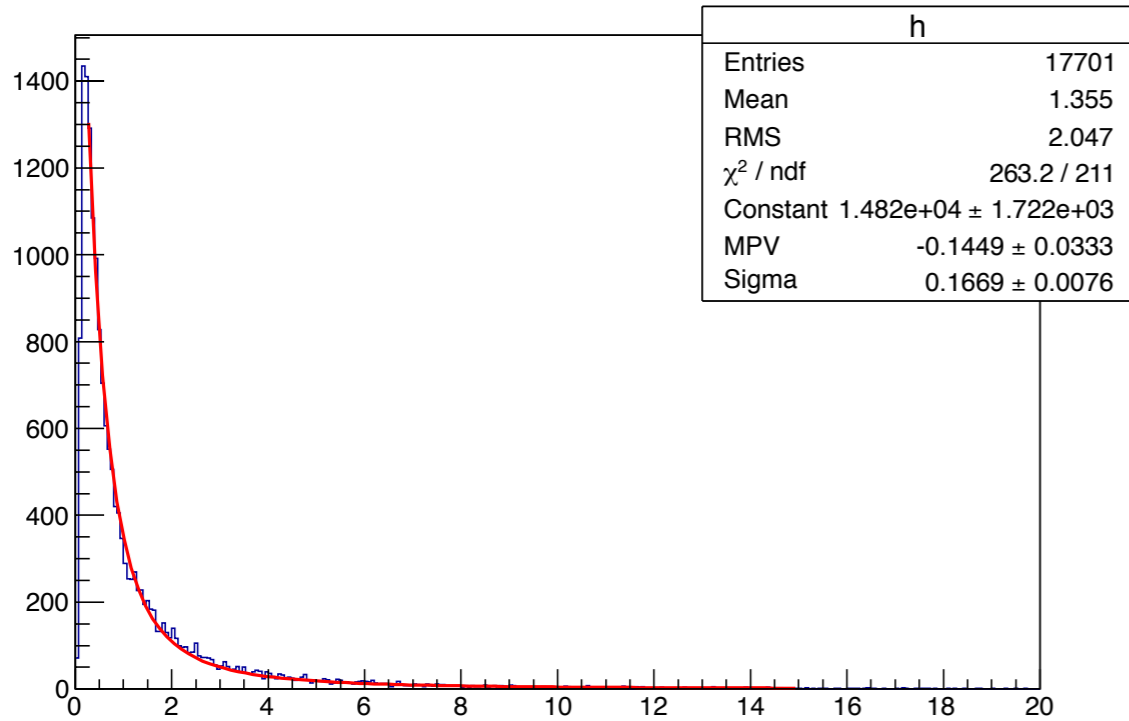


Energy of photon pfo in 500GeV jet evt

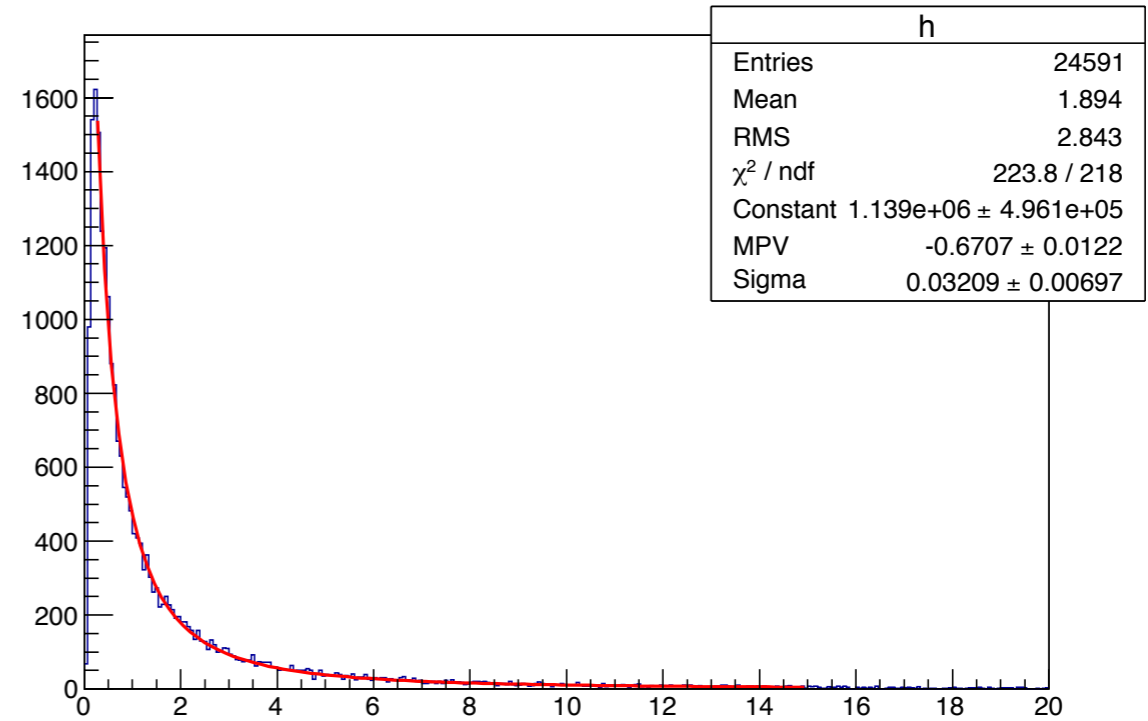


Energy of photon pfo in a jet (GeV)

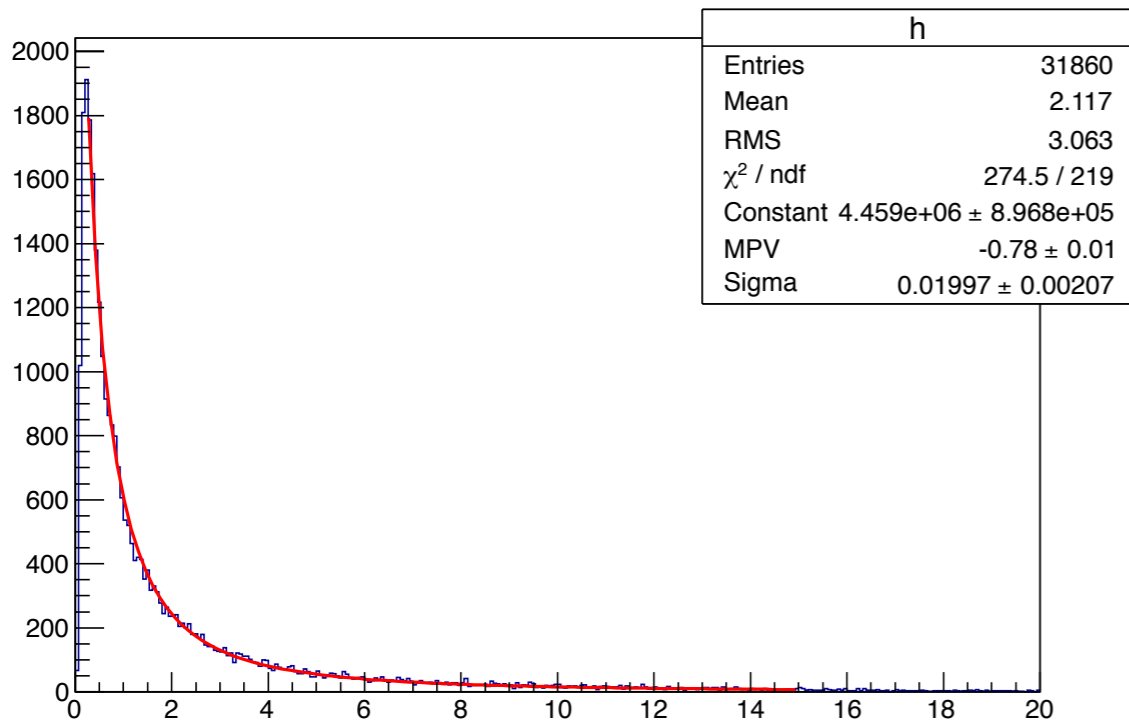
Energy of a photon pfo in 91GeV jets (1000evt averaged)



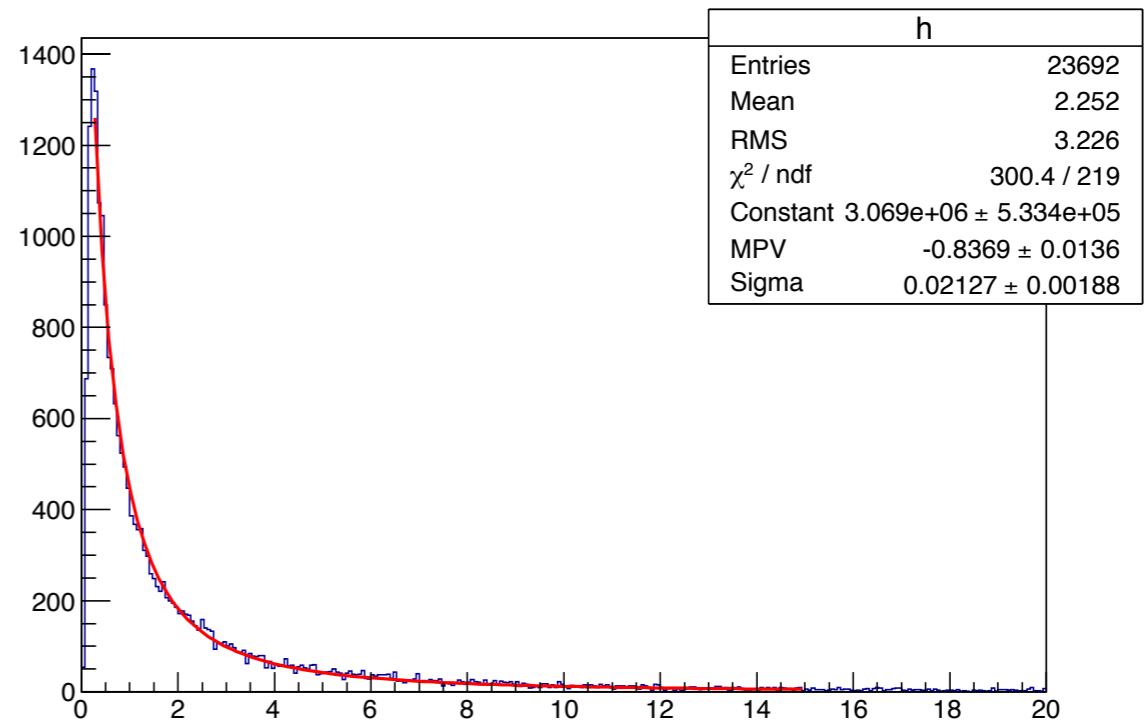
Energy of a photon pfo in 200GeV jets (1000evt averaged)



Energy of a photon pfo in 360GeV jets (1000evt averaged)



Energy of a photon pfo in 500GeV jets (1000evt averaged)



@0.2~15GeV: Good fit by Landau tail

Energy of photon pfo in a jet (GeV)

Percentage of photon pfo which has energy lower than 2,3,4,10GeV

Single Jet Energy

	45.5GeV	100GeV	180GeV	250GeV
<2GeV	81.4	73.3	69.2	66.7
<3GeV	88.7	81.6	77.7	75.6
<4GeV	92.3	86.1	82.8	80.7
<10GeV	98.5	95.6	93.5	92.2