## Wakefield effect

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## Transverse, dipole Wakefield

Wakepotential is integral of

wakefunction for point charge x charge distribution

$$W(z) = \int_{-\infty}^{z} W_{\delta}(z-z')\rho(z')dz' \Big/ \int_{-\infty}^{\infty} \rho(z')dz'$$

 $W_{\delta}(z)$ : wakefunction, or wake for point charge ( $W_{\delta}(z) = 0$  if z < 0)  $\rho(z)$ : charge density of bunch (bunch head : negative z)

Wake for point charge



~ size of structure

For very long bunch, compared with size of wake source, Wakepotential is almost resistive.

For very short bunch, Wakepotential is capacitive

## Transverse, dipole Wakefield

Particle at position *z* change transverse momentum as

$$\Delta p_{y}(z) = e \int_{-\infty}^{z} y(z') W_{\delta}(z-z') \rho(z') dz'/c$$

y(z): transverse offset at position z, w.r.t. wake source

Ignoring y difference along bunch (bunch shape distortion)

$$\Delta p_{y}(z) = ey \int_{-\infty}^{z} W_{\delta}(z-z') \rho(z') dz' / c = eqy W(z) / c$$

Kick angle

$$\theta(z) = eqyW(z)/E$$

$$q = \int_{-\infty}^{\infty} \rho(z') dz'$$

## For 7 mm Gaussian bunch



Calc. by A. Lyapin

# Effect of wake

- Average kick
  - Orbit change

kick angle of center of mass

$$a = \int_{-\infty}^{\infty} \rho(z)\theta(z)dz \Big/ \int_{-\infty}^{\infty} \rho(z)dz = \frac{ey}{E} \int_{-\infty}^{\infty} \rho(z)W(z)dz$$

- Particles at different z are kicked differently. Induce zcorrelated transverse motion.
  - Beam size increase

Spread of kick angle

$$\sigma_{\theta} = \left[ \int_{-\infty}^{\infty} \rho(z) (\theta(z))^2 dz / q - a^2 \right]^{1/2}$$
$$= \frac{ey}{E} \left[ q \int_{-\infty}^{\infty} \rho(z) W^2(z) dz - \left( \int_{-\infty}^{\infty} \rho(z) W(z) dz \right)^2 \right]^{1/2}$$

## Resulted particle position distribution at IP (~Projection of wakepotential)



## Effect of single wake source

Center of mass position change

$$\Delta y = R_{34}a = R_{34}\frac{ey}{E}\int_{-\infty}^{\infty}\rho(z)W(z)dz = \sqrt{\beta\beta^*}\sin\varphi\frac{eqy}{E}a_W$$

• Beam size increase

$$\sqrt{\sigma^2 - \sigma_0^2} = R_{34}\sigma_\theta$$
$$= \sqrt{\beta\beta^*} \sin \varphi \frac{ey}{E} \left[ q \int_{-\infty}^{\infty} \rho(z) W^2(z) dz - \left( \int_{-\infty}^{\infty} \rho(z) W(z) dz \right)^2 \right]^{1/2}$$
$$= \sqrt{\beta\beta^*} \sin \varphi \frac{eqy}{E} \sigma_W$$

$$a_W \equiv \int_{-\infty}^{\infty} \rho(z) W(z) dz / q$$
$$\sigma_W \equiv \left[ \int_{-\infty}^{\infty} \rho(z) W^2(z) dz / q - a_W^2 \right]^{1/2}$$

Average of wake potential

Spread of wake potential

#### Wake potential

	C-band ref.	C-band BPM	Bellows
Peak (V/pC/mm)	-0.153	-0.1124	-0.105
$a_W$ (V/pC/mm)	-0.0921	-0.0645	-0.0640
$\sigma_{\!_W}$ (V/pC/mm)	0.0492	0.0356	0.0353

#### Effect of single wake source at the mover, beta=6260 m, offset 1 mm, bunch charge 1 nC.

		C-band ref.	C-band BPM	Bellows
IP position (nm)	Calc. from $a_W$	-61	-42.7	-42.4
	Tracking	-61	-43.0	-42.7
IP beam size (nm)	Calc. from $\sigma_{\!\scriptscriptstyle W}$	32.6	23.6	23.3
	Tracking	32.2	23.6	22.6

## IP beam size vs. mover position experiment

Effect of offset 1 mm, bunch charge 1 nC. IP beam size increase (nm/nC/mm)

Experimental data analyzed by Okugi



# IP beam size vs mover position experiment and calc.

Effect of wake source at the mover, offset 1 mm, bunch charge 1 nC. IP beam size increase (nm/mm/nC)

	C-band ref.	No mask Bellows	Masked Bellows
Experiment	55	47~50	7
Calc	32.2	22.6	?

More discussion later by Jochem

# Effect of many wake sources

- Can be estimated by adding effect of each source.
- Depend on  $\sin\phi$  but almost +1 or -1 for all structures in large beta region
- Random misalignment
  - Effects are random
  - Proportional to sqrt(beta)
- Orbit deviation:
  - Effect of every source is added with the same phase.
  - Proportional to beta.
  - Depend on phase of orbit

### beam size increase by random misalignment





#### Experiment: ~120 nm/ nC (?)

No clear improvement after mask bellows . (?)

#### $\rightarrow$ random misalignment 1.3 mm and 0.6 mm.

For bellows, 1 mm does not seem too large.

But they were shielded in May-June.

mover position was optimized in most cases (fixed offset was compensated?).

Wake of fixed offset can be corrected by on-mover wake source at other place (If shape of wake potential is same).



## Simulation of beam size increase by orbit distortion

Orbit of angle-at-IP phase



**Experiment: ~120 nm/ nC** (from IPBSM 30 deg mode measurements

For explaining by orbit,

need orbit distortion >2-sigma of nominal (no bellows), ~1 sigma (with bellows) (if assuming calculated wakepotentials)

Simulation of beam size increase by orbit distortion Orbit of position-at-IP.



Orbit of position-at-IP does not induce significant wakefield effect.

# Summary of this talk

- Experiments of on-mover wake source
  - Suggested larger wake than calculation
    - Factor 1.7 for C-band reference cavity
    - Factor 2 for no mask bellows
  - Wake of masked bellows was about 1/7 times of no mask bellows
- Beam size dependence on intensity ~120 nm/nC
  - Wake of cavity BPM, bellows or wake of similar shape cannot explain observations
  - Orbit distortion 1-sigma of y at IP phase may explain, assuming wake of cavity BPM + 2 bellows at every cavity BPMs (Much larger than expected from calculation with most of bellows are masked.)
- Other wake sources with much different wakepotential shape????
- More discussions by Jochem.