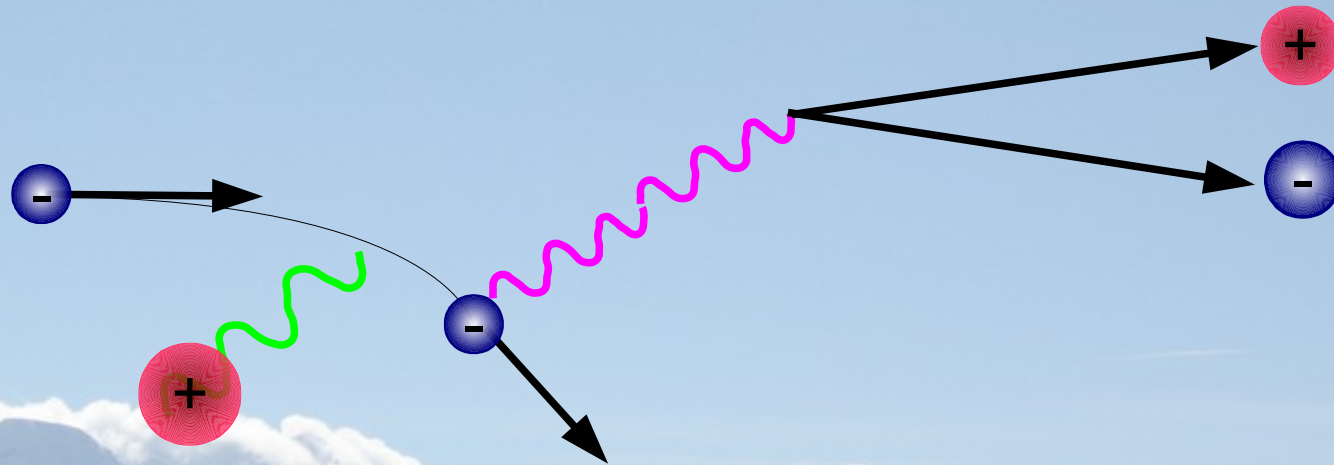


# Positron Source for Linear Colliders

KURIKI Masao (Hiroshima/KEK)



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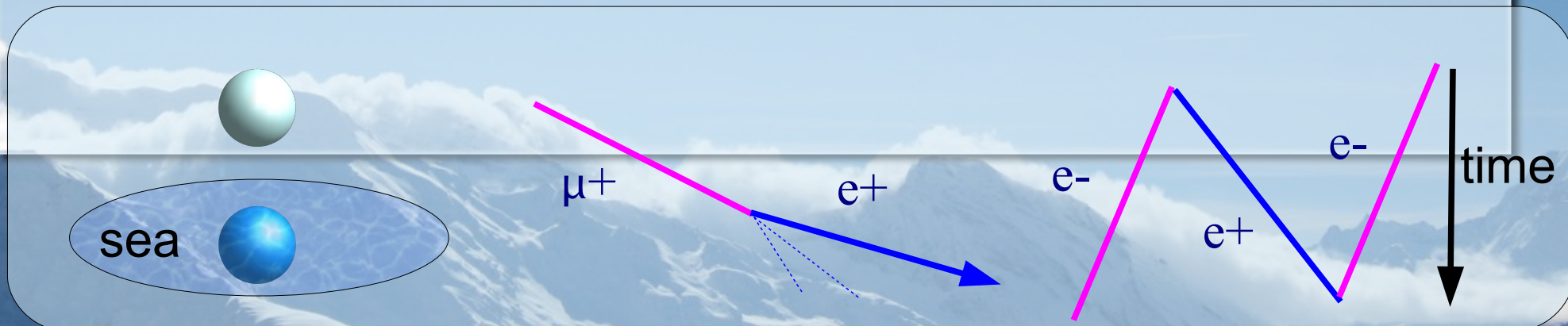
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- Positron Source for Linear Colliders
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# Introduction

**4 Nov. - 14 Dec., Antalya, Turkey**  
**8<sup>th</sup> Accelerator School for Linear Colliders**

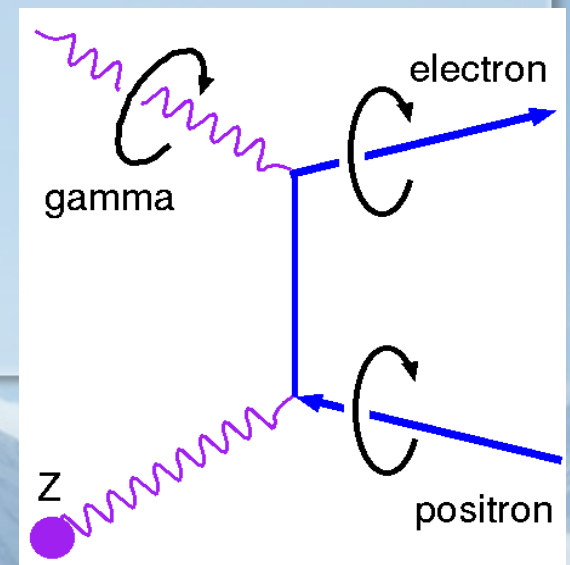
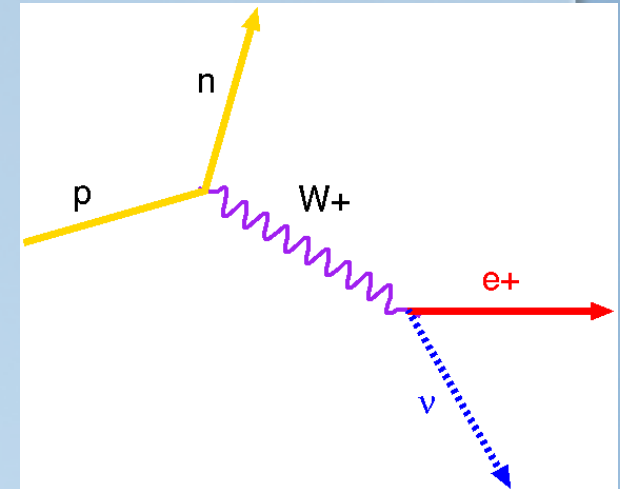
# What is Positron?

- 1928: Dirac equation suggested electrons with negative energy. Hole hypothesis: "vacuum" is filled with this negative energy electrons to prohibit Klein's paradox. "hole" in the sea of this electrons, acts as positrons.
- 1932: Anderson discovered positrons in cosmic rays with cloud chamber.
- In the modern field theory, positrons is considered to be electrons, which propagate inversely.



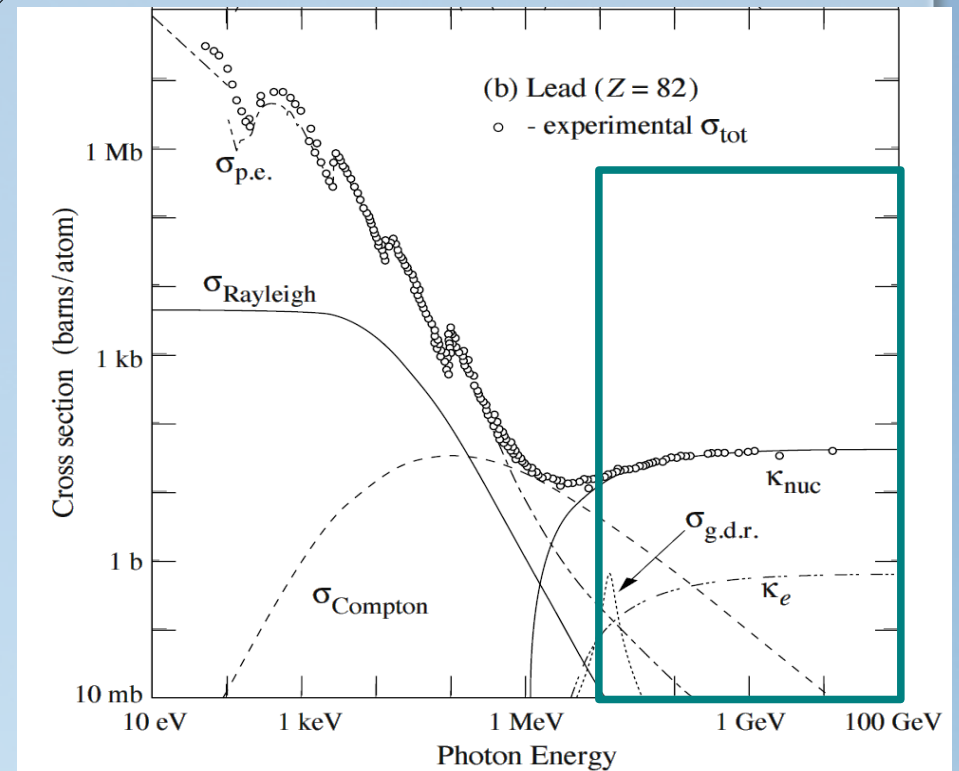
# Positron Production (1)

- There is only few positrons in nature.
- Two ways to produce positrons :
  - Create radio-active elements, which beta + decays;  $p \rightarrow n e^+ \text{ neutrino}$ .
  - **Pair-creation ;  $\text{gamma} \rightarrow e^+ e^-$**
- All of the positron beam sources with a time structure, employ the pair-creation process.



# Positron Production (2)

- Photon interaction in material:
  - Photo-electron effect (<1MeV)
  - Compton scattering (1-10MeV)
  - Pair-creation (>10MeV)
- Gamma ray, energy >10MeV is required for effective pair creation.



$\sigma_{p.e.}$  : photo-electron

$\sigma_{Compton}$ : Compton scattering

$\kappa_{nuc}$ ,  $\kappa_e$ : pair creation

(from Particle Data Group, <http://pdg.lbl.gov>)

# Need Photon?

- We need many photons to create enough amount of positrons through the pair creation.
- How to create the photons?
  - Brems-strahlung, channeling radiation : electron interaction in material. Very effective.
  - Undulator radiation: Synchrotron Radiation. Need very long undulator with very high energy electron.
  - Inverse Compton scattering : Laser and electron interaction. Need very high density laser field.

# Positron Generation

4 Nov. - 14 Dec., Antalya, Turkey  
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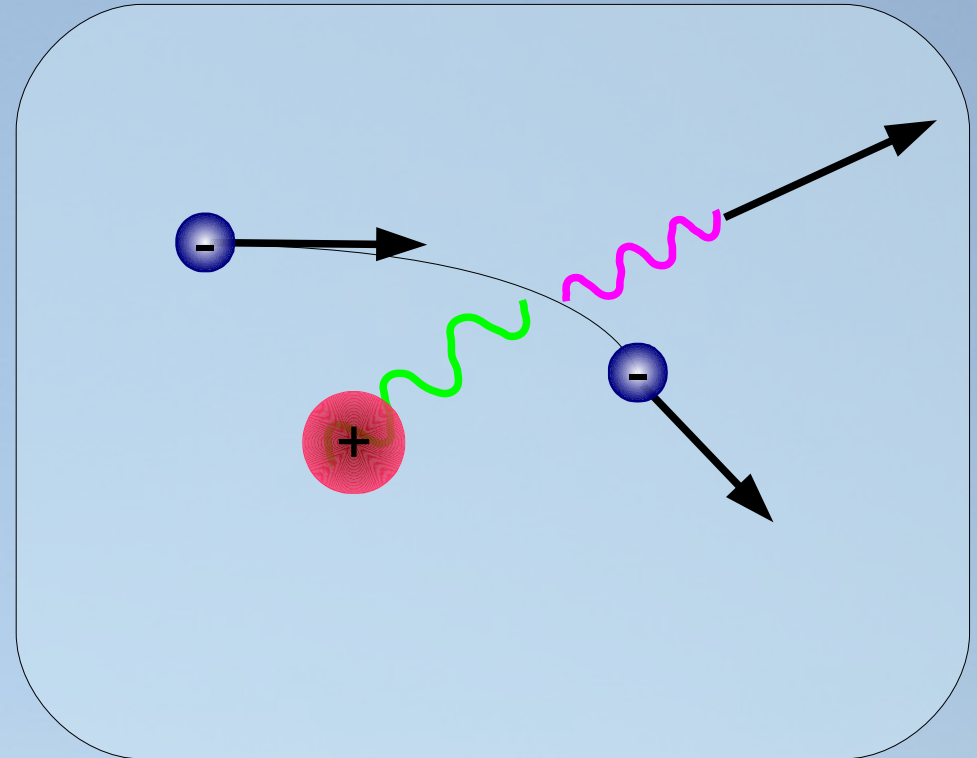


# Positron Generation

- Positron beam is generated by the pair-creation process.
- There are several schemes for positron generation, depending on way to generate high energy gamma rays.
- Electron driven
  - Authentic
  - Channeling radiation
- Direct Pair-creation
  - Undulator
  - Laser-Compton

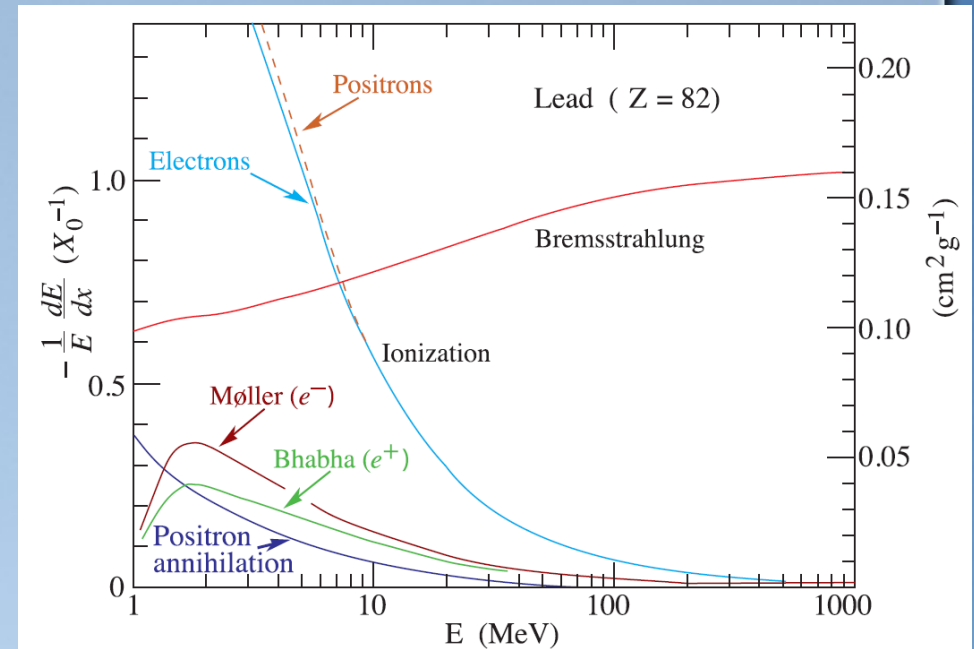
# Bremsstrahlung (1)

- Electron is decelerated by nucleus field.
- Photon is emitted by the energy conservation.
- Gamma rays are obtained with MeV or GeV electrons.



# Bremsstrahlung (2)

- Bremsstrahlung is dominant in high energy region.
- Below some energy ( $E_c$  critical energy) ionization is dominant.
- When high energy electrons are injected into material, electrons lose their energy by Bremsstrahlung.
- When the energy becomes less than  $E_c$ , Bremsstrahlung is not dominant.



## Critical Energy $E_c$

$$\left( \frac{dE}{dx} \right)_{ion} = \left( \frac{dE}{dx} \right)_{Brems}$$

$$E_c [MeV] \sim \frac{800}{Z + 1.2}$$

# Cascade Shower

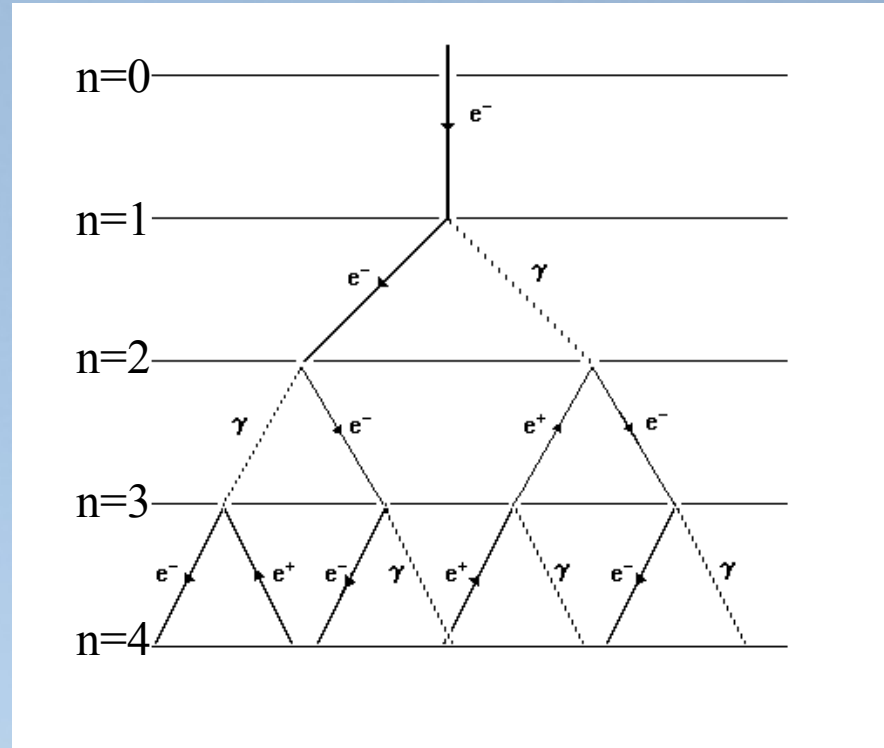
Radiation length  $X_0$ :  $\frac{dE}{dx} = -\frac{E}{X_0}$

Energy at each steps:  $E_n = \frac{E_0}{2^n}$

This process is continued up to;

$$n_{max} = \frac{\ln\left(\frac{E_0}{E_c}\right)}{\ln 2} - 1$$

$$x_{max} = X_0 \left[ \ln\left(\frac{E_0}{E_c}\right) - \ln 2 \right]$$

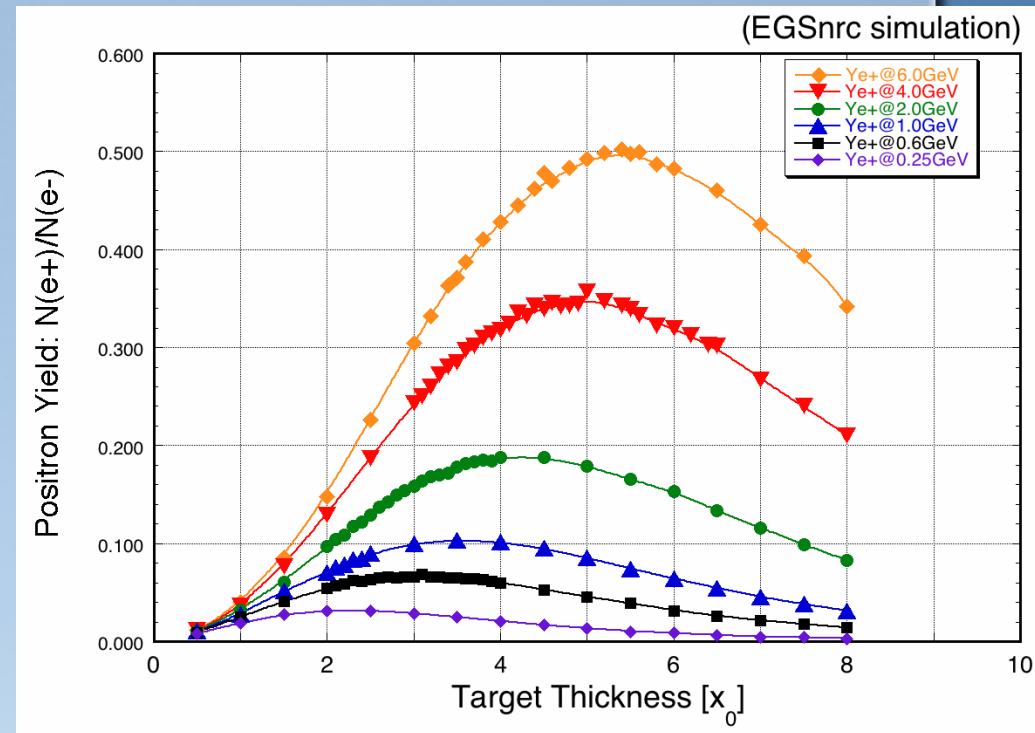


# Cascade Shower (2)

- As consequence of the cascade shower by the high energy electron in material, many positrons are generated.
- Number of positron is maximized at shower max determined by  $X_0$ ,  $E_0$ , and  $E_c$ .

$$x_{max} = X_0 \left[ \ln \left( \frac{E_0}{E_c} \right) - \ln 2 \right]$$

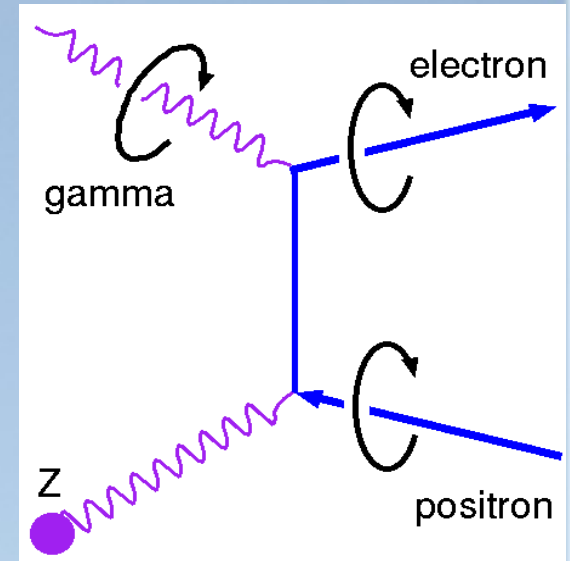
$$X_0 = \frac{716.4 [g.cm^{-2}] A}{Z(Z+1) \ln(287/\sqrt{Z})}$$



Courtesy of T.Kamitani

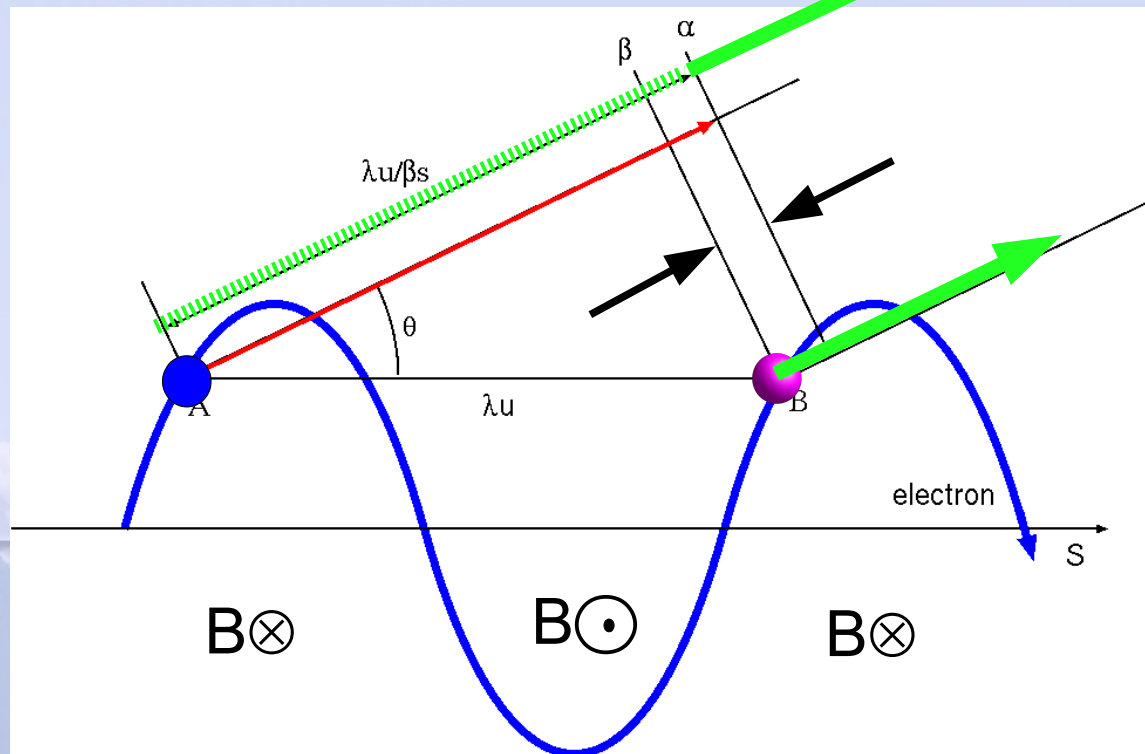
# Direct Pair Creation

- With 10s MeV photons, photons directly generate positrons through pair creation process.
- Due to this simplicity, if the photons are polarized, the positrons are also polarized. (Polarized Positron).
- # of particles is not multiplied. Each photon can generate only up to one positron. We need many photons.



# Undulator Radiation (1)

- In alternate dipole B field(undulator), electron wiggles periodically.
- Electron speed in undulator along the longitudinal axis is less than speed of light due to the zig-zag motion.
- Photons are emitted to the direction where wave-plane distance corresponds to integer of the photon wave length.



# Undulator radiation (2)

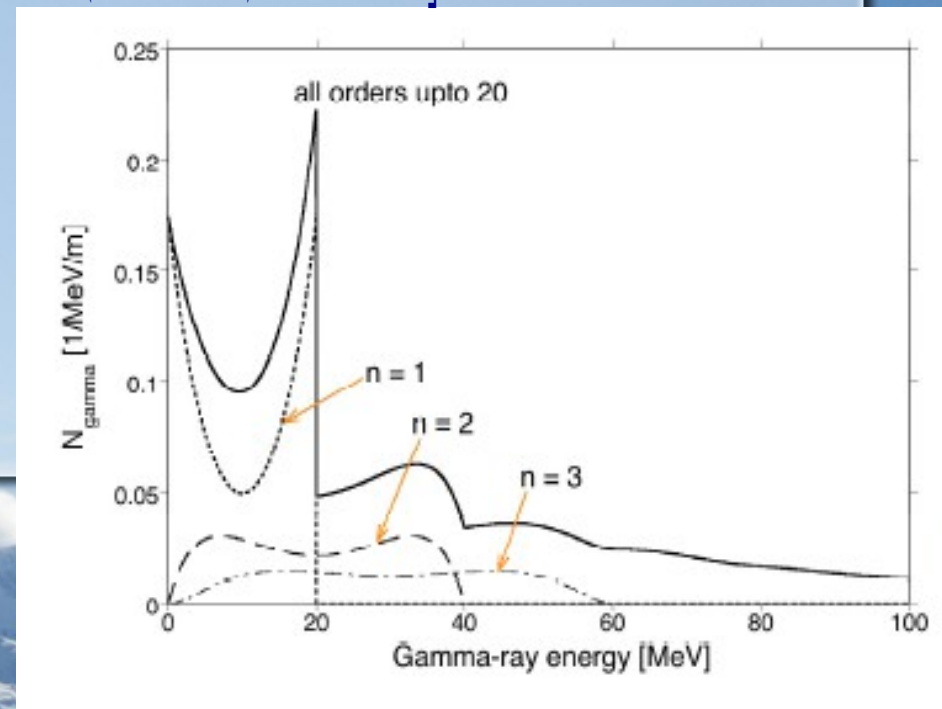
Lienard-Wiechert form ( $\omega$  photon angular,  $\Omega$  is solid angle,  $\mathbf{n}$  is unit vector to observation)

$$\frac{d^2 I}{d\omega d\Omega} = \frac{e^2 \omega^2}{16\pi^3 \epsilon_0 c} \left| \int_{-\infty}^{+\infty} \mathbf{n} \times (\mathbf{n} \times \boldsymbol{\beta}) \exp \left[ i\omega \left( t - \frac{\mathbf{n} \cdot \mathbf{r}}{c} \right) \right] \right|^2 \quad (3-8)$$

$$\frac{d^2 N_{ph}}{dEdL} \left[ \frac{1}{m.MeV} \right] = \frac{10^6 e^3}{4\pi \epsilon c^2 h^2} \frac{K^2}{\gamma^2} \left[ J'_n(x)^2 + \left( \frac{\alpha_n}{K} - \frac{n}{x} \right)^2 J_n(x)^2 \right] \quad (3-8')$$

$$E_1[eV] = 9.50 \frac{nE^2[GeV^2]}{\lambda_u[m](1+K^2+\theta^2\gamma^2)}$$

$$\sim 9.50 \frac{nE^2[GeV]}{\lambda_u[m](1+K^2)}$$





# Undulator Radiation (3)

- The cut off photon energy from undulator is rewritten as

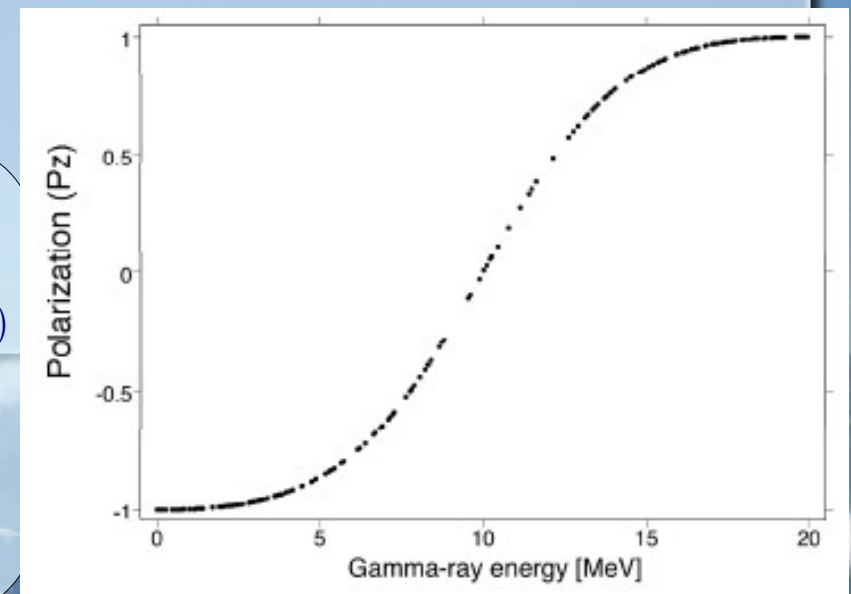
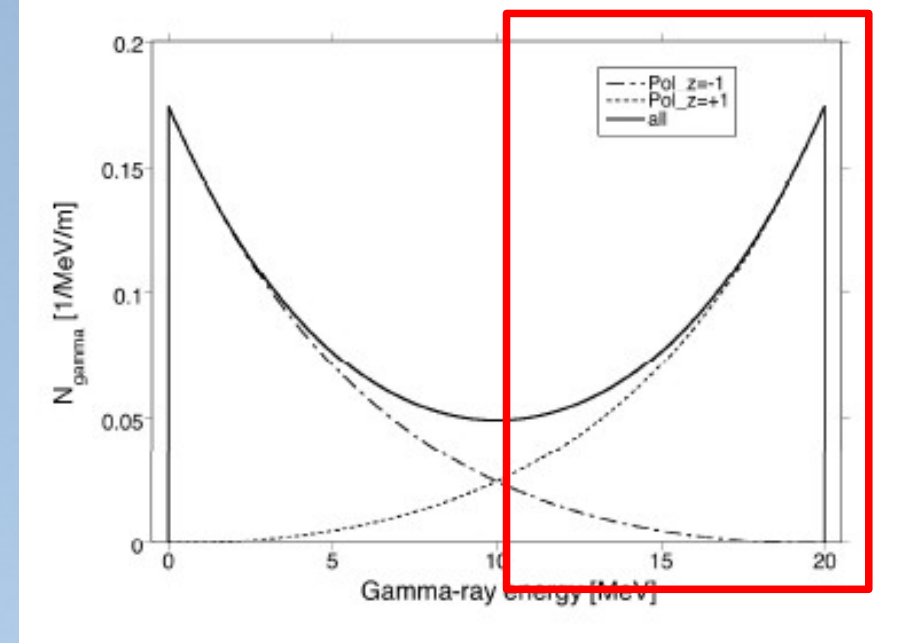
$$E = \frac{2n\gamma^2\hbar\omega_0}{1+K^2} \quad (3-12)$$

$$\omega_0 = \frac{2\pi\beta c}{\lambda_u} \quad (3-13)$$

- The undulator radiation = electron and “photon ( $\hbar\omega_0$ )“ scattering.
  - Photon wave length = undulator period.
  - The photon energy is boosted by  $\gamma^2$ .
- ▶ Due to the long undulator period, high energy electron beam is necessary.

# Polarized Positron

- Energy, angle, and helicity from undulator radiation are correlated.
- By taking gammas in super-forward direction, gamma rays and positrons are polarized.
- Number of particle is decreased by the collimation; need longer undulator.



$$\frac{dN_n}{dE} \left[ \frac{1}{\text{MeV}} \right] = \frac{10^6 e^3 L}{4\pi \epsilon c^2 h^2} \frac{K^2}{y^2} \left[ J_n'(x)^2 + \left( \frac{\alpha_n}{K} - \frac{n}{x} \right)^2 J_n(x)^2 \right] \quad (4-1)$$

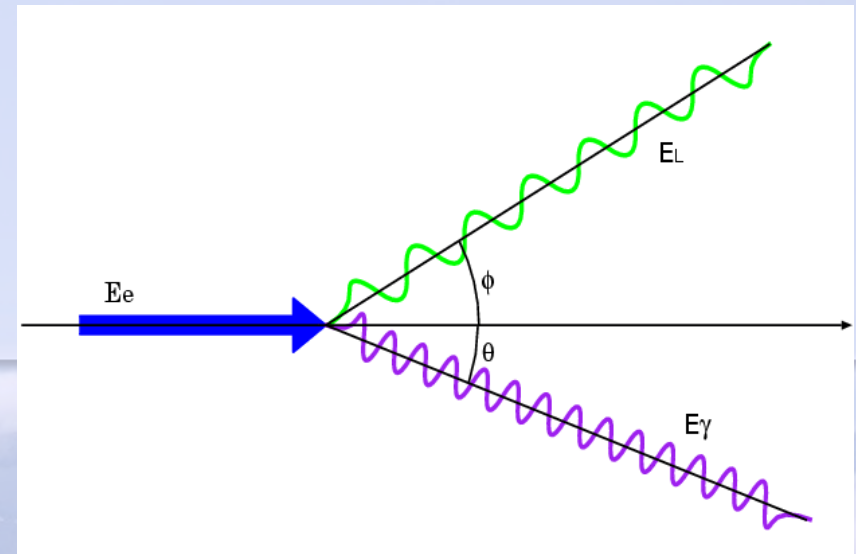
$$\theta = \frac{1}{y} \sqrt{n \frac{\omega_n (1 + K^2)}{\omega} - 1 - K^2} \quad (4-2)$$

# Laser Compton(1)

- Inverse Compton scattering between laser photon and electron beam.
- Laser photon (wavelength is in  $\mu\text{m}$  order) is scattered by high energy electron and its energy is boosted.
- As a result, high energy gamma-ray is obtained.

$$E_{\gamma} \sim \frac{4\gamma^2 mc^2 E_L}{mc^2 + 4\gamma E_L} \quad (3-16)$$

- $E_L$  : Laser energy 1.2eV @ 1 $\mu\text{m}$ .
- Electron beam 1GeV,  $\gamma=2000$ .
- $E_{\gamma} \sim 16\text{MeV}$



## Laser Compton (2)

- Laser acts as a quite short period undulator. The energy from Compton scattering is rewritten as

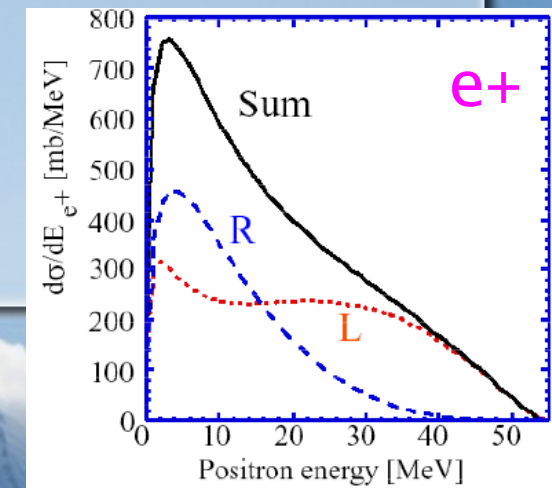
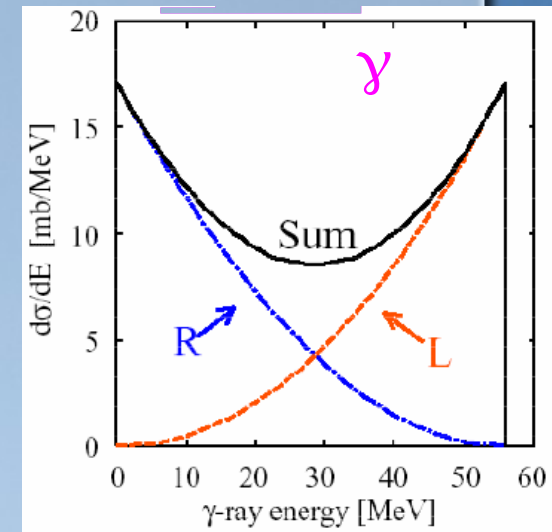
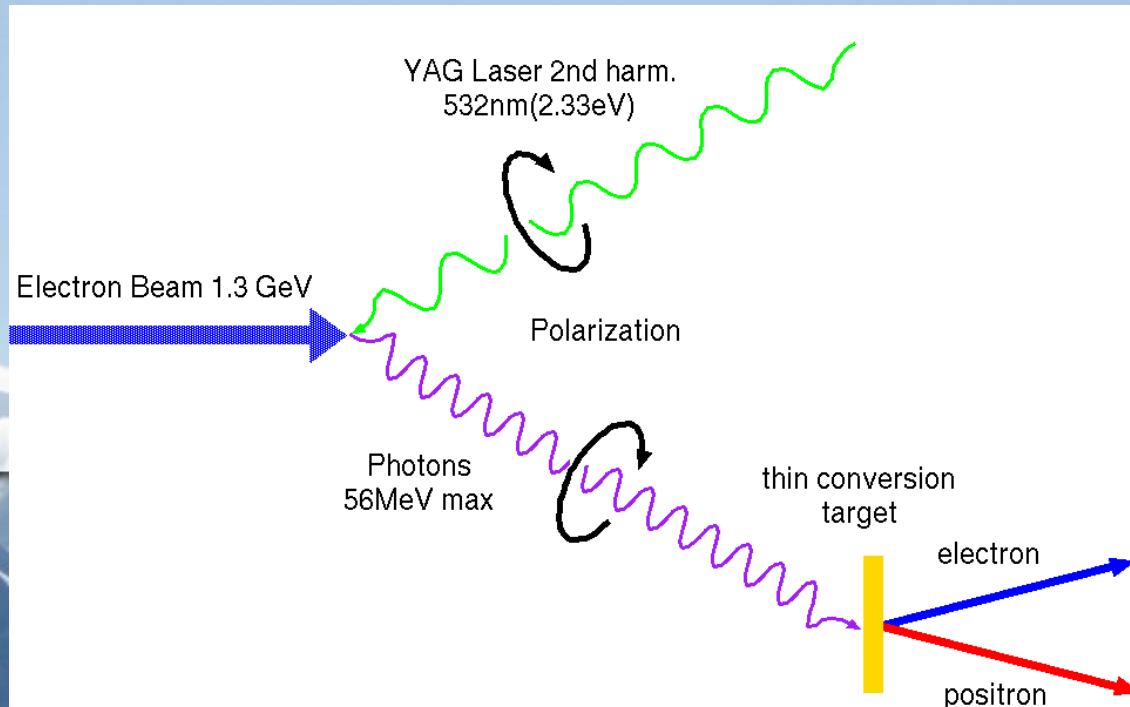
$$E_\gamma \sim 4\gamma^2 \hbar \frac{2\pi c}{\lambda_L} \quad (3-17)$$

where  $\lambda_L$  is laser wave length.

- High energy gamma (several 10s MeV) is obtained with few GeV electron beam.
- Laser focal length is limited to Rayleigh length. It is difficult to make a long “laser undulator”.

# Laser Compton (3)

- By employing circularly polarized laser, the final photon spectrum different for polarization.
- By taking high energy region, the polarized photon is obtained.
- The positron generated from the polarized photon, is also polarized.





# *Positron Source*

**4 Nov. - 14 Dec., Antalya, Turkey**  
**8<sup>th</sup> Accelerator School for Linear Colliders**

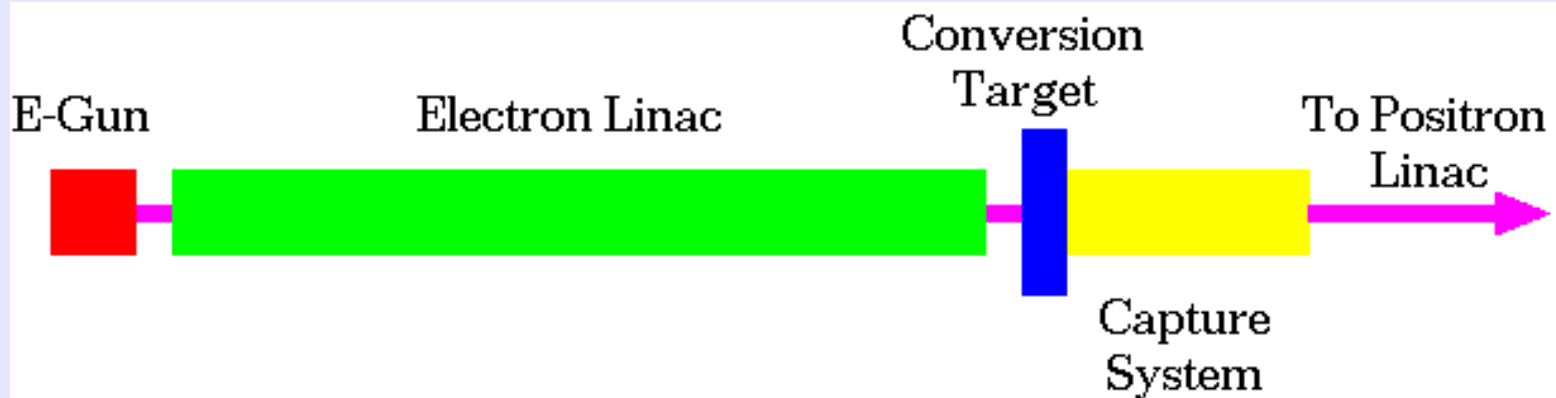
# Positron Source

- Positron source is a system, composed from:
  - Drive Beam (Electron or Photon)
  - Conversion target
  - Matching Device
  - Capture Accelerator
- Three concepts of positron source have been proposed.
  - Electron driven (conventional), undualtor, and laser compton.



# Electron Driven (1)

- Sub or Several GeVs driver electron beam.
- High Density Material for shower development.
- Positron capture by Solenoid, QWT, or AMD.
- NC accelerator tube with solenoid focusing.
- All positron sources based on accelerator, is this concept. That is why it is called “conventional”.





# Electron Driven (2)

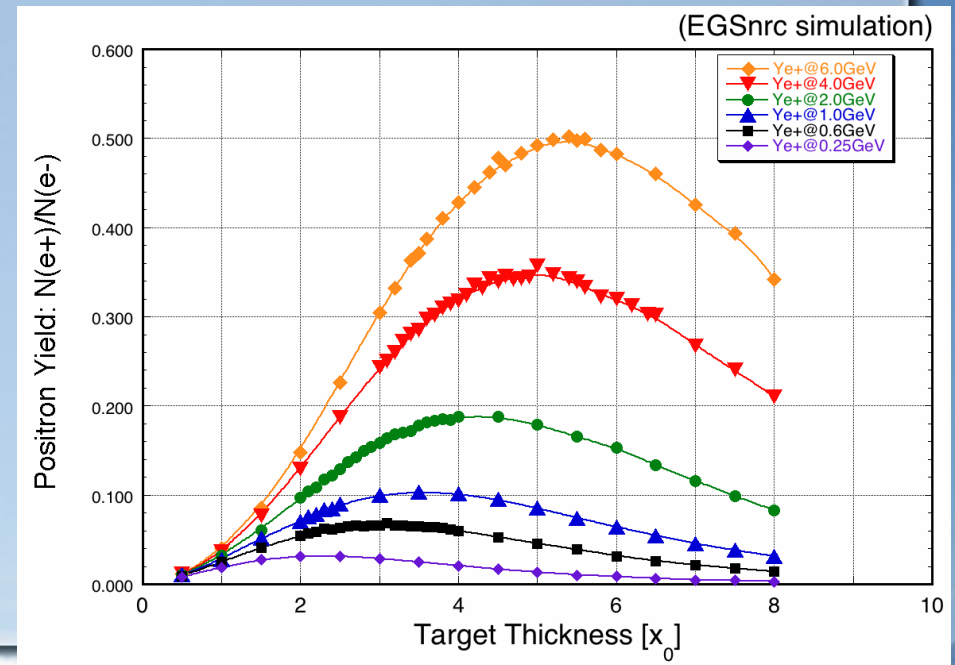
Thickness and material of the target for positron generation is determined by the shower max;

$$T_{max} = 1.01 \left[ \ln \left( \frac{E_0}{E_c} \right) - 1 \right] \quad (3-1)$$

Positron yield  $\eta$  and normalized yield  $\eta_n$  are defined as;

$$\eta = \frac{N_{pos}}{N_{ele}} \quad (3-2)$$

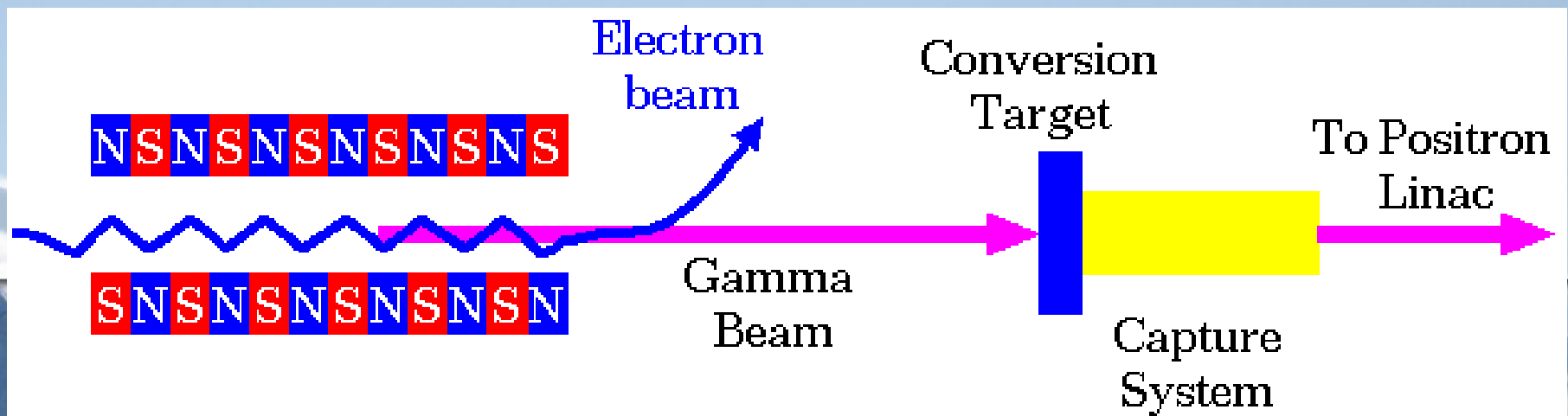
$$\eta_n = \frac{N_{pos}}{N_{ele} E_{ele}} \quad (3-3)$$



Courtesy of T.Kamitani

# Undulator Scheme (1)

- By passing more than 130 GeV energy electrons through a short period undulator, more than  $\sim 10$  MeV energy gamma rays are generated as synchrotron radiation.
- This gamma ray is converted to positrons in a heavy material.
- With helical undulator, the photon is circularly polarized and polarized positron is generated.

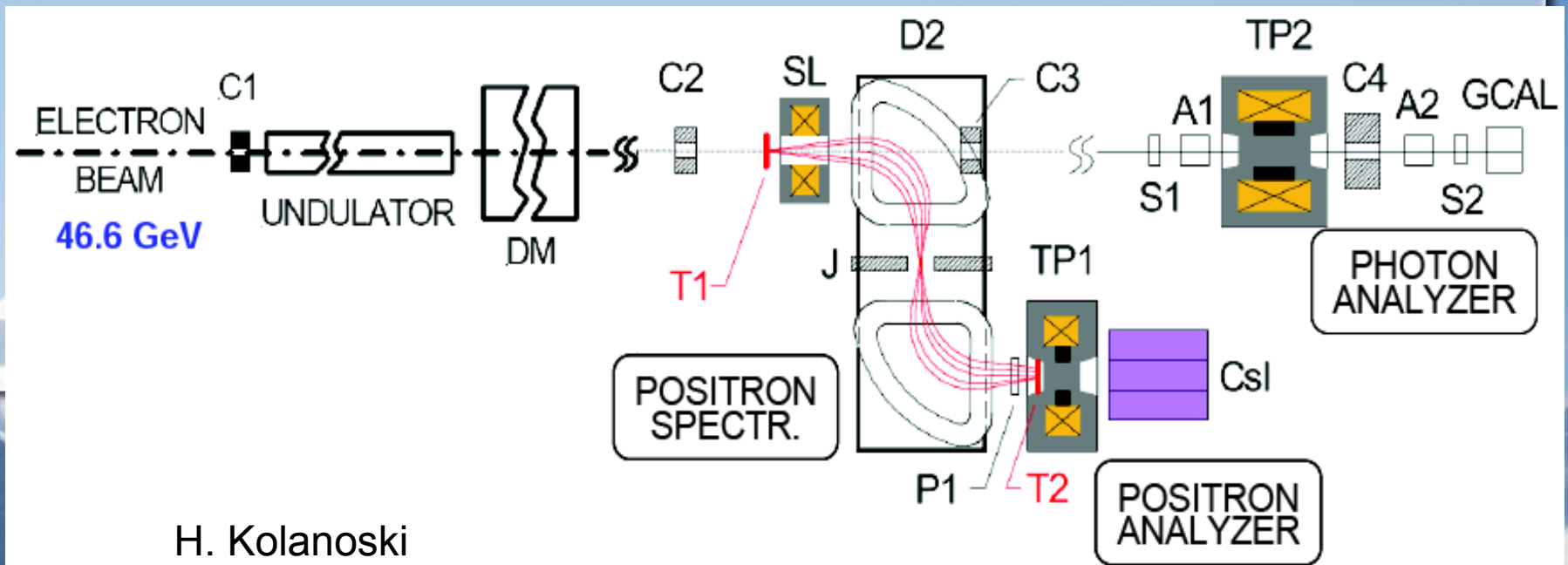


# Undulator Scheme (2)

- Constructing a 130 GeV electron linac dedicated to positron generation is not realistic.
- The main electron linac is shared by collision beam and positron generation.
- In low energy operation, the positron yield becomes very low. It could be solved by alternate-pulse operation.
- By employing helical undulator, polarized positron is obtained.

# E166 (1)

- E166 is an experiment, which was carried out at SLAC to demonstrate the polarized positron production with helical undulator.
- 46.6 GeV electron beam passes through 1m undulator,  $K=0.17$  ( $0.71\text{T}$ ,  $\lambda_u=2.54\text{mm}$ ).
- $\gamma$  and positron polarization is analyzed by transmission method.



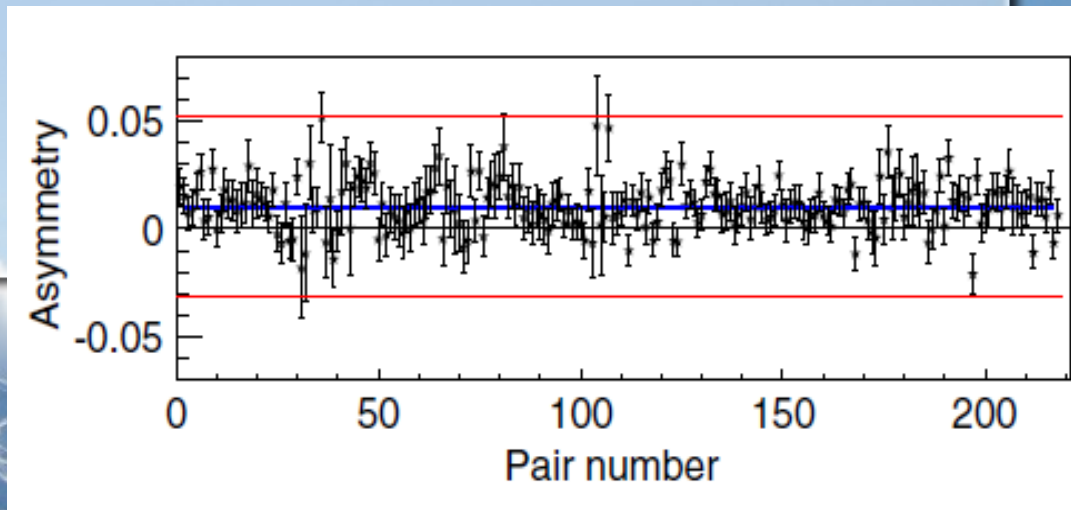
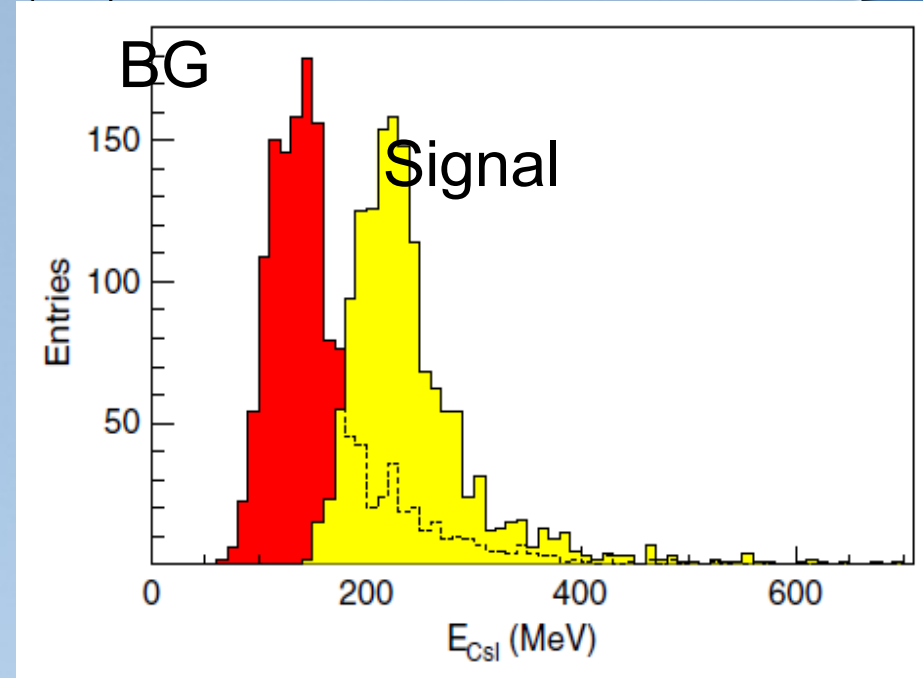
H. Kolanoski

# E166 (2)

- The signal is observed from the undulator radiation.
- The asymmetry is calculated with each pair of data with opposite magnetization of the polarimeter for polarization measurement.

$$\delta_y = \frac{S_{CsI}^- - S_{CsI}^+}{S_{CsI}^- + S_{CsI}^+} \quad (3-14)$$

G. Alexander

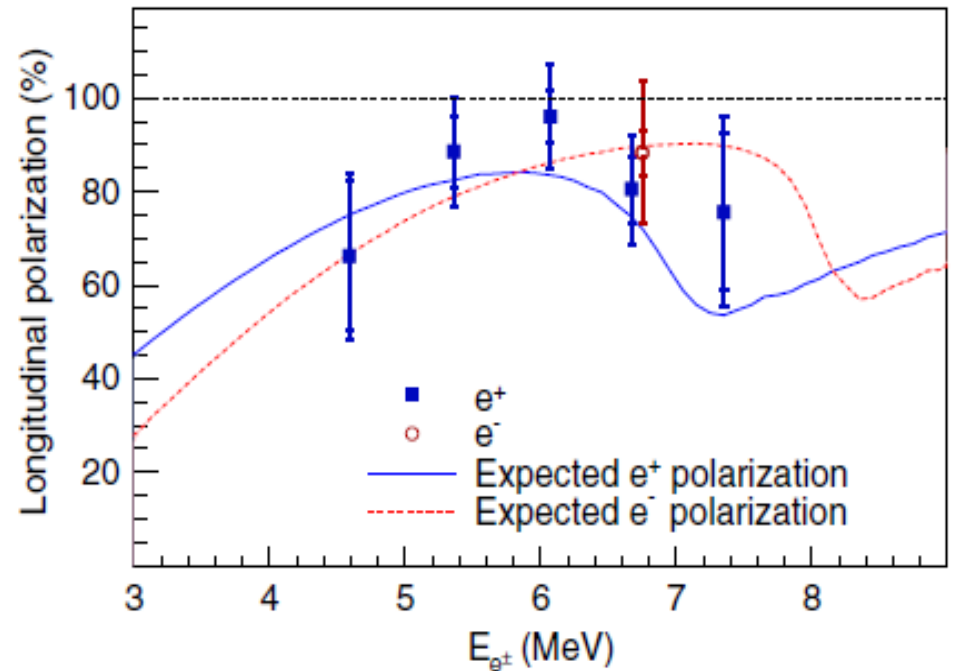


# E166 (3)

From the asymmetry of the polarimeter, the positron asymmetry is extracted as

$$P_{e^+} = \frac{\delta_y}{A_{e^+} P_{e^-}^{Fe}} \quad (3-15)$$

~80% positron polarization is obtained, which is consistent with expected value.

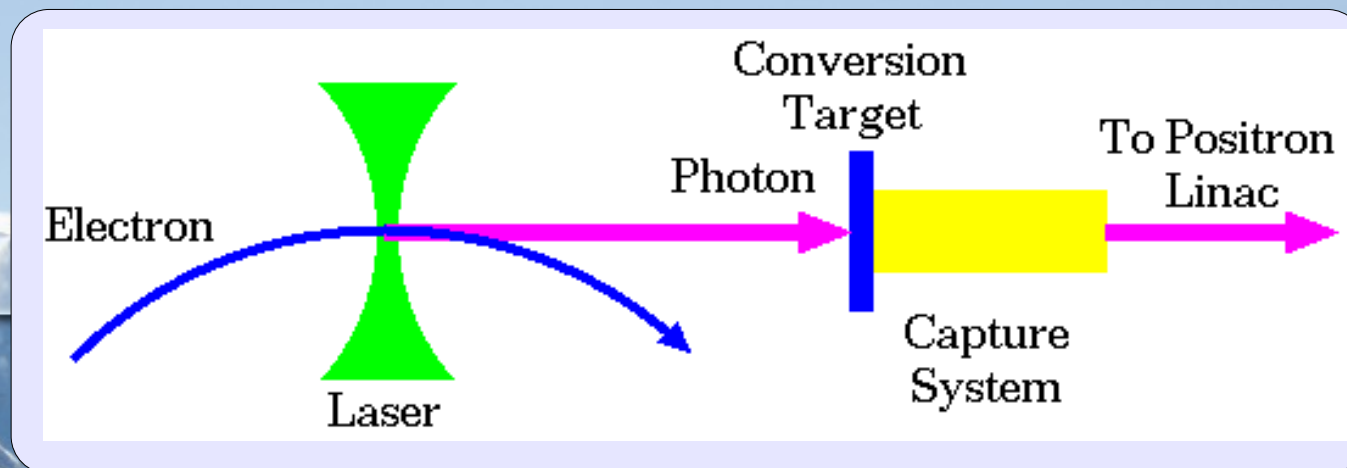


$E_{e^\pm}$	$\delta \pm \sigma_\delta(\text{stat})$	$A$	$P \pm \sigma_P(\text{stat}) \pm \sigma_P(\text{syst})$
4.6 ( $e^+$ )	$0.69 \pm 0.17$	0.150	$66 \pm 16 \pm 8$
5.4 ( $e^+$ )	$0.96 \pm 0.08$	0.156	$89 \pm 8 \pm 9$
6.1 ( $e^+$ )	$1.08 \pm 0.06$	0.162	$96 \pm 6 \pm 10$
6.7 ( $e^+$ )	$0.92 \pm 0.08$	0.165	$80 \pm 7 \pm 9$
6.7 ( $e^-$ )	$0.94 \pm 0.05$	0.153	$88 \pm 5 \pm 15$
7.4 ( $e^+$ )	$0.89 \pm 0.20$	0.169	$76 \pm 17 \pm 12$

G. Alexander

# Compton Scheme (1)

- Compton back scattering between several GeVs electron and laser photons generates  $\sim 30$  MeV gamma rays.
- These gamma rays are converted to positrons.
- When the laser photon is circularly polarized, the generated positron is also polarized.
- It is hard to make a long “laser undulator” , because of limitation on the laser focus.



# Compton Scheme (2)

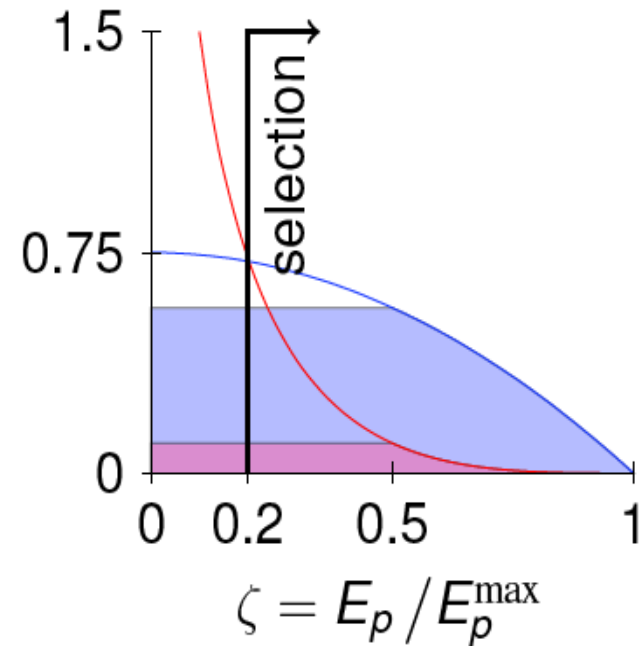
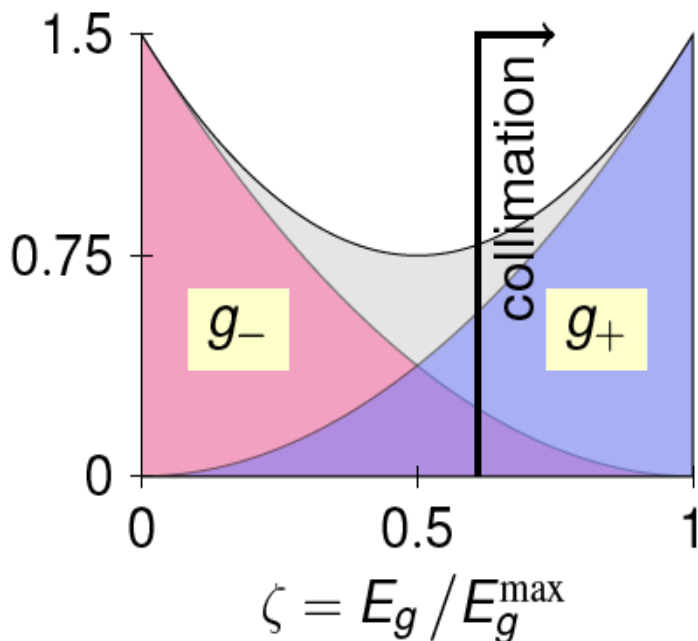
- ▶ Positron Polarization.
  - **Higher degree up to 90 %.**
  - **Train by train flipping (5Hz) by laser polarity control.**
- ▶ Dedicated e- beam.
  - No concern for e- beam quality degradation.
  - No inter-system dependence.
    - **Simple, easier construction, operation, commissioning, maintenance, high availability.**
- ▶ No problem on low energy operation.
- ▶ To obtain enough amount of positron is a technical challenge.

$$Y = \sigma_C N_e N_L f_{rep} G$$



# Compton Scheme (3)

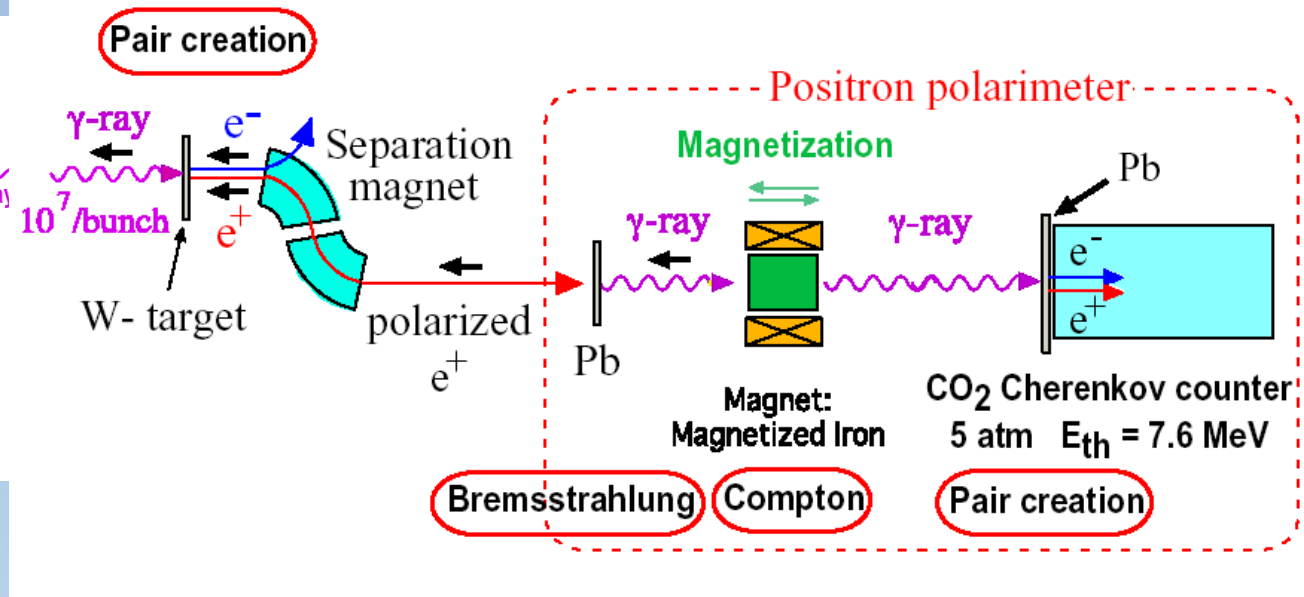
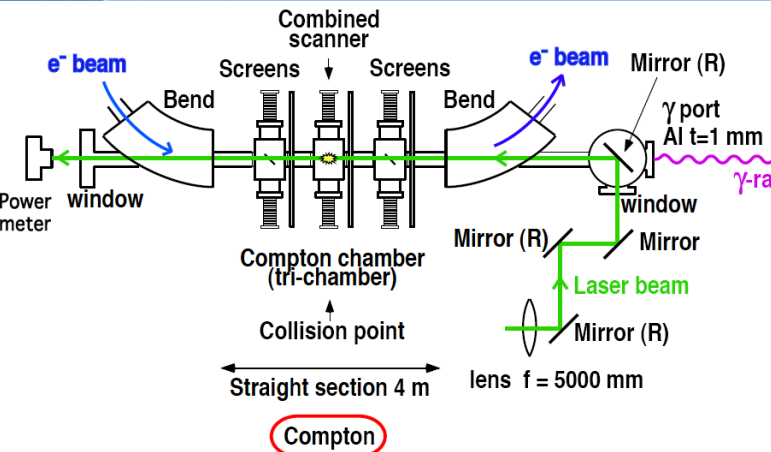
- Polarized gamma is obtained by collimation (pre-selection).
- The positron polarization is enhanced by the energy selection (post selection).



Selection of gammas before target

Selection of positrons after target

# KEK-ATF experiment



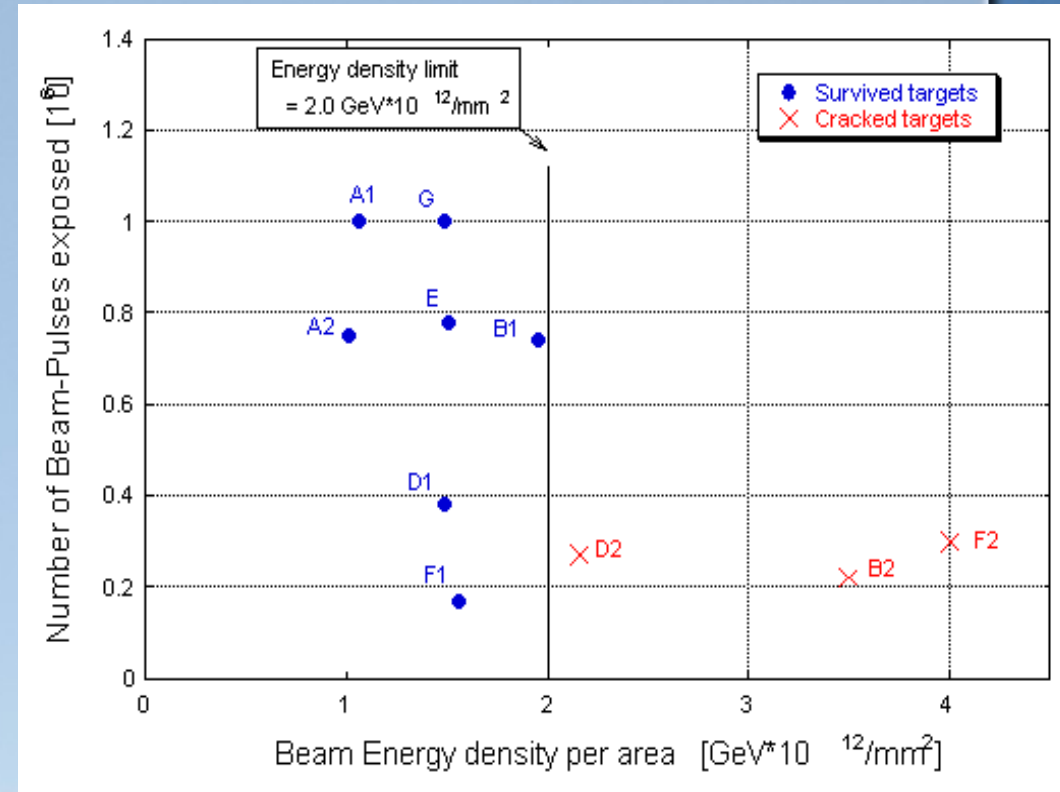
- ▶  $N_{e^+}(\text{design}) = 3 \times 10^4/\text{bunch}$
- ▶  $\text{Pol}(\text{estimation}) = 80\%$
- ▶  $\text{Pol}(\text{experiment}) \sim 73 \pm 15(\text{stat}) \pm 19(\text{sys})\%$

# Target Heat Load

- A fraction of electron (gamma) energy is deposited in the target as thermal energy.
- An actual limit on the positron generation is given by the target destruction.
- The destruction can be occurred several processes,
  - Melting,
  - Fatigue,
  - Destruction by thermal shock wave,
  - Radiation damage, etc.
- The heat load is heavier for electron driven than gamma driven, because of the higher beam energy.

# Damage Threshold (1)

- Damage threshold of electron driven (W-Re target) is examined at SLAC.
- Single bunch beam is injected to target repeatedly in 120Hz.
- The damage depends only on beam energy density, not for number of shots.
- Threshold is  $2.0 \text{ GeV} \cdot 10^{12}/\text{mm}^2$  or  $320\text{J}/\text{mm}^2$ .



S. Ecklund, SLAC-CN-128

# Damage Threshold (2)

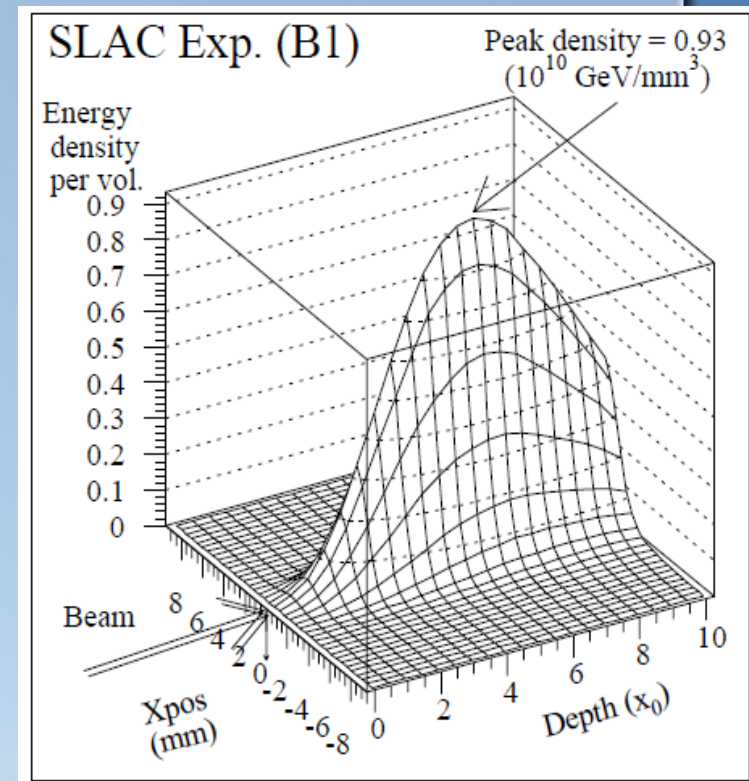
To evaluate the universal damage threshold, the energy deposited density in the SLAC experiment is evaluated as

$$\rho = 0.93 \times 10^{10} \text{ [GeV/mm}^3\text{]}$$

$$\rho = 76 \text{ [J/g]}$$

Although SLC had been operated below this limit, a significant damage is observed at the production target. The actual limit is now considered to be the condition of SLC,

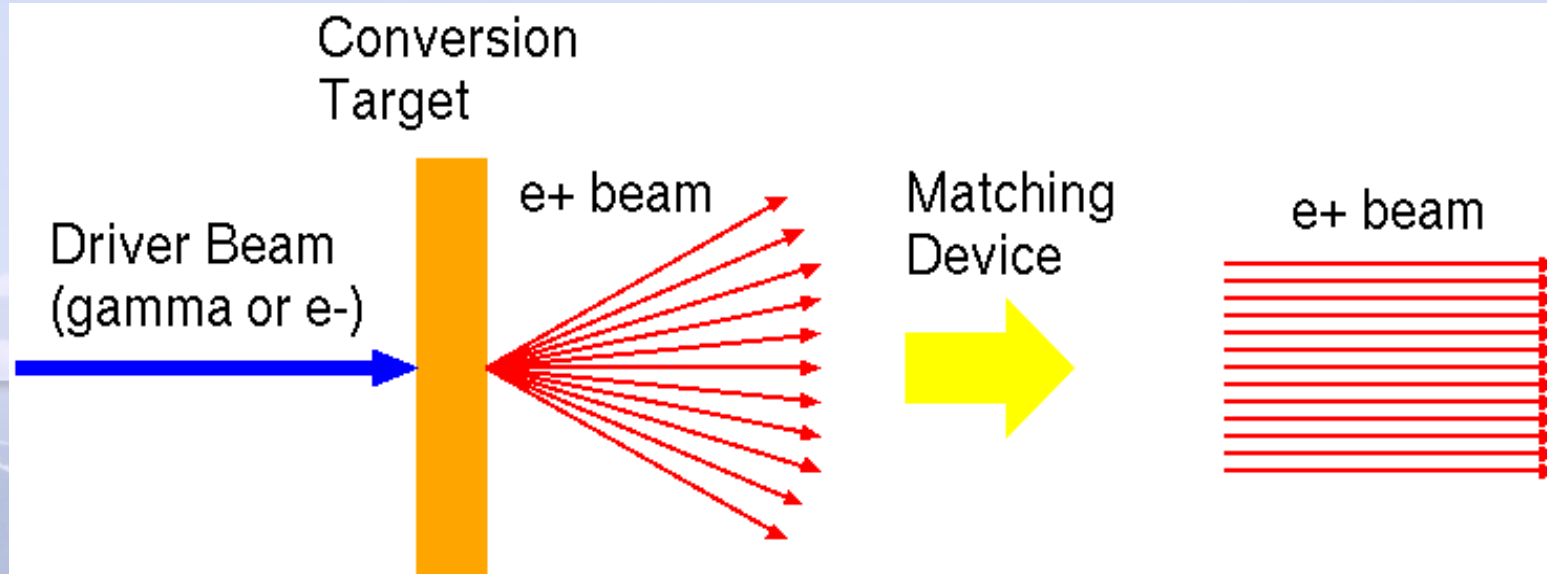
$$\rho = 35 \text{ [J/g]}$$



T. Kamitani

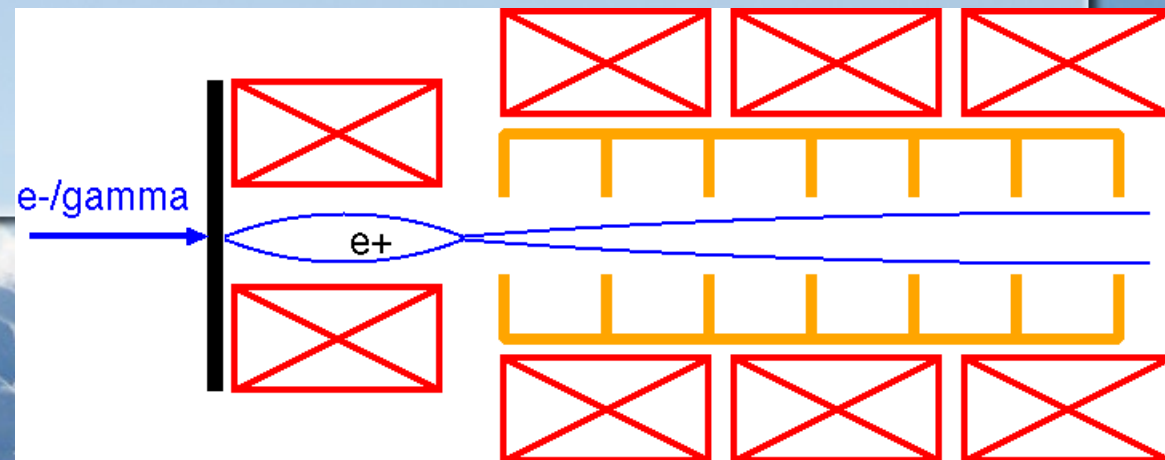
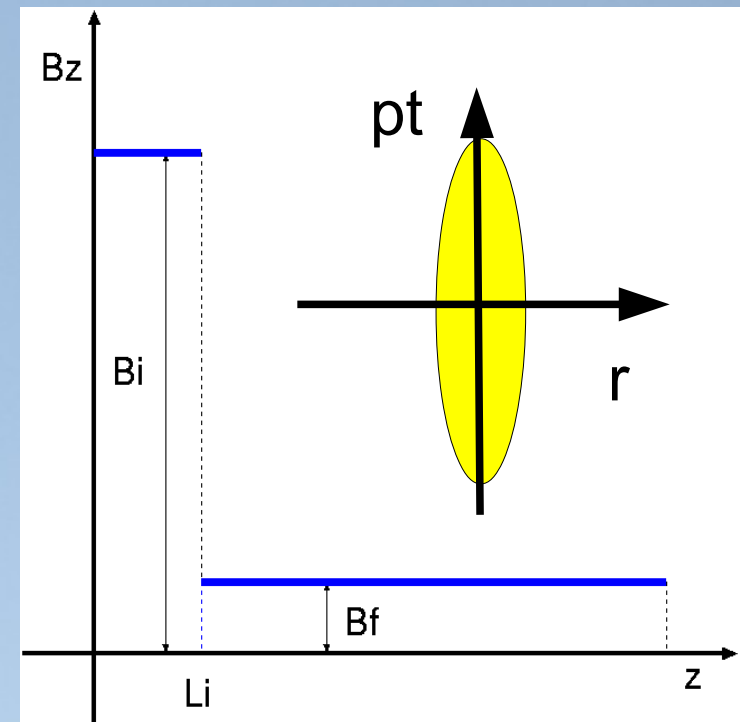
# Positron Capture

- The generated positrons are distributed in a small spot size and in a large momentum space. To convert it to the parallel beam, a couple of solenoid-like magnetic field with different profile are employed.
  - QWT (Quarter Wave Transformer)
  - AMD (Adiabatic Matching Device)



# QWT(1)

- QWT consists from initial strong solenoid field,  $B_i$ , and weak solenoid field,  $B_f$ , along  $z$  direction.
- Accelerator is placed in  $B_f$  region compensating transverse motion.
- It transforms  $90^\circ$  in the phase space, that is why it is called as Quarter Wave Transformer.



# QWT(2)

Positrons are circulated with radius  $\rho$ .

$$\rho = \frac{p_{t0}}{eB_i} \quad (2-1)$$

Time to travel  $\pi\rho$  in  $xy$  plane,

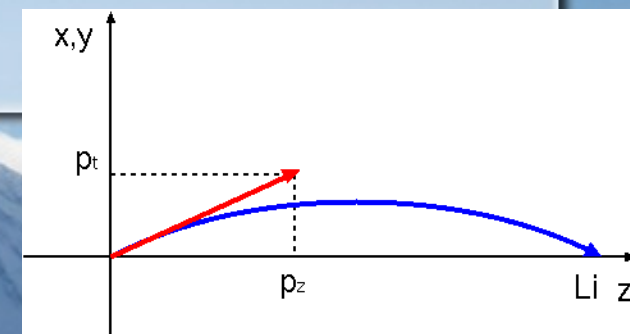
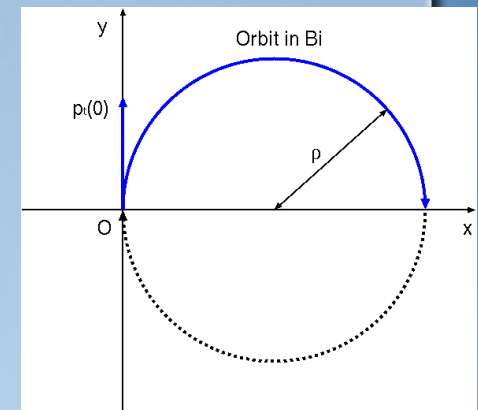
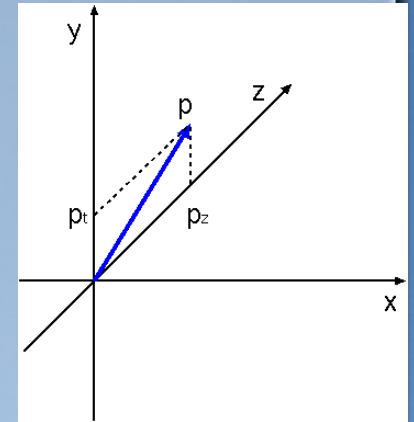
$$t_{xy} = \frac{\gamma m \pi \rho}{p_{t0}} = \frac{\gamma m \pi}{eB_i} \quad (2-2)$$

Time to travels  $L_i$

$$t_z = \frac{L_i m \gamma}{p_z} \quad (2-3)$$

Only positrons satisfying these conditions are captured by QWT.

$$\frac{L_i m \gamma}{p_z} = \frac{\gamma m \pi}{eB_i} \quad (2-4)$$





# QWT(3)

At the boundary of  $B_i$  and  $B_f$ , transverse magnetic field  $B_t(z)$  is appeared. In radius  $2\rho$ , magnetic flux in  $B_i$  region is

$$\Phi_i = \pi (2\rho)^2 B_i \quad (2-5)$$

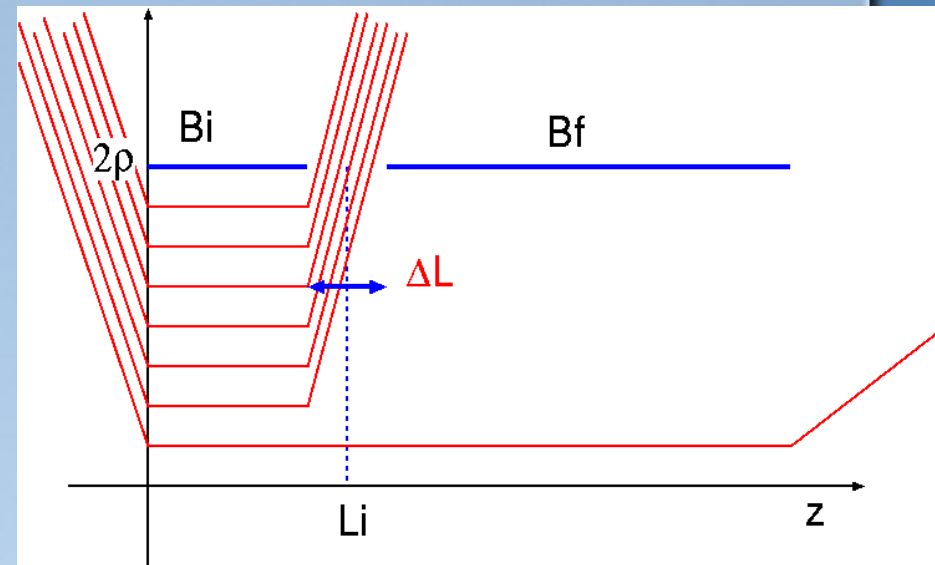
Magnetic flux in  $B_f$  region is

$$\Phi_f = \pi (2\rho)^2 B_f \quad (2-6)$$

Taking the integral of  $B_t(z)$  along  $z$ ,

$$\begin{aligned} \int 4\pi\rho B_t(z) dz &= \Phi_i - \Phi_f \\ &= 4\pi\rho^2 (B_i - B_f) \quad (2-7) \end{aligned}$$

$$\int B_t(z) dz = \rho (B_i - B_f) \quad (2-8)$$



# QWT(4)

Momentum change at the boundary is

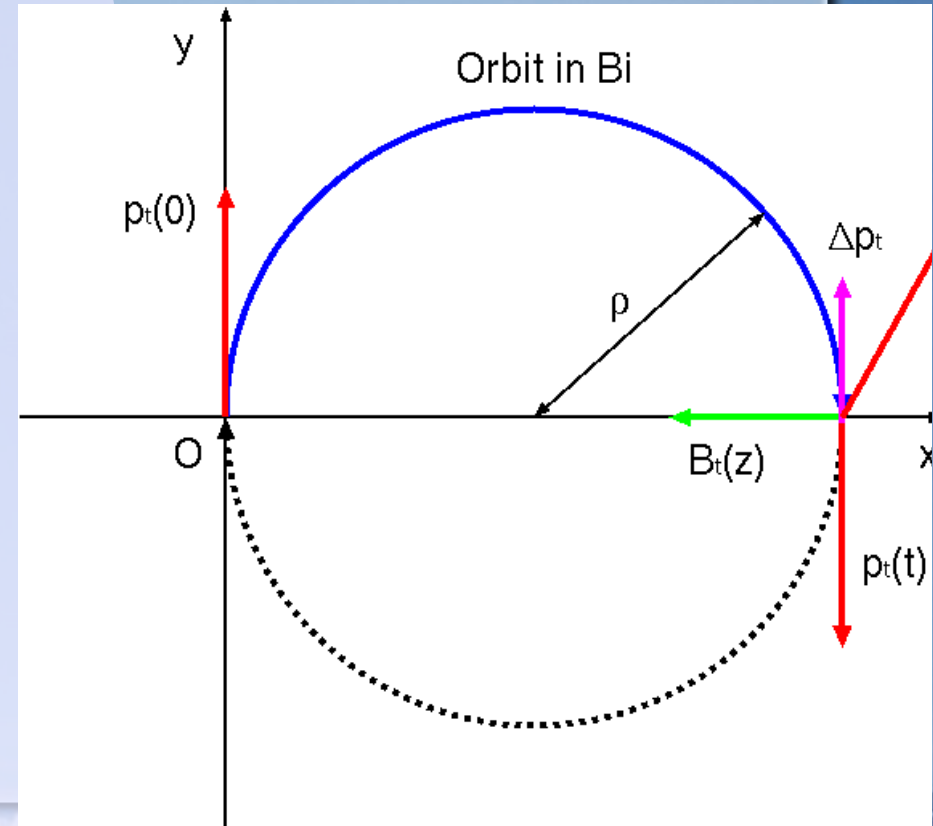
$$\frac{dp_t(t)}{dt} = e v_z B_t(z) \quad (2-9)$$

Integrating this equation, total momentum change is

$$\begin{aligned} \Delta p_t &= e v_z \int B_t(z) dt \\ &= e v_z \int B_t(z) \frac{dz}{v_z} \\ &= e \rho (B_i - B_f) \quad (2-10) \end{aligned}$$

The kick is opposite to  $p_t(t)$ , then  $p_t(t)$  after the kick is

$$\begin{aligned} p_t(t) &= p_{t0} - \Delta p_t = p_{t0} - \frac{p_{t0}}{B_i} (B_i - B_f) \\ &= p_{t0} \frac{B_f}{B_i} \quad (2-11) \end{aligned}$$



# QWT(5)

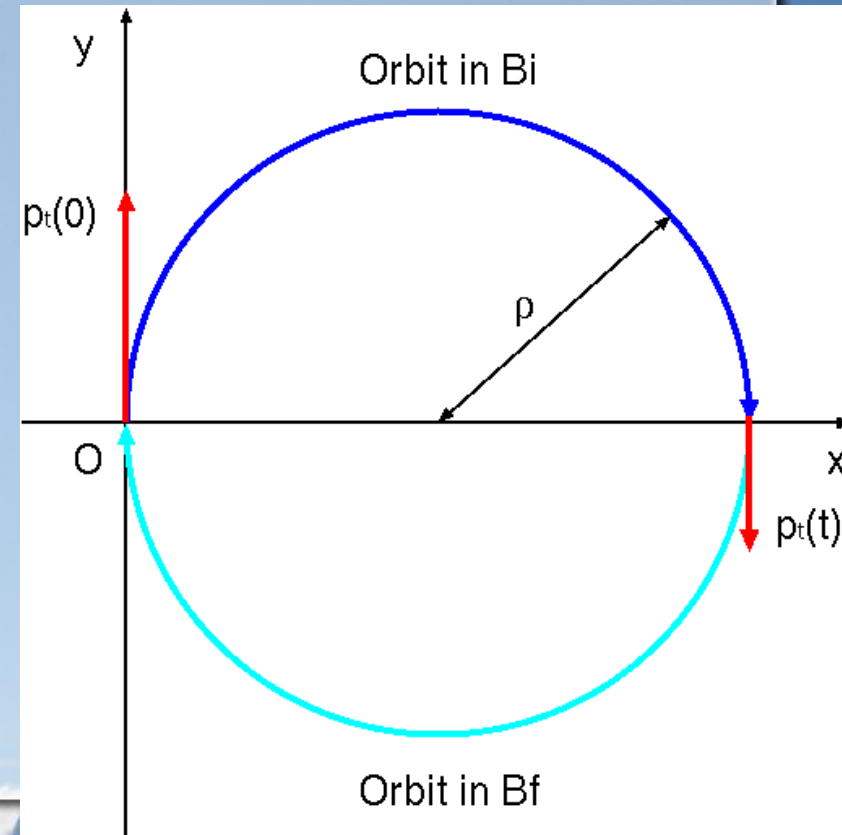
$P_t(t)$  after the kick is

$$p_t(t) = p_{t0} \frac{B_f}{B_i} \quad (2-12)$$

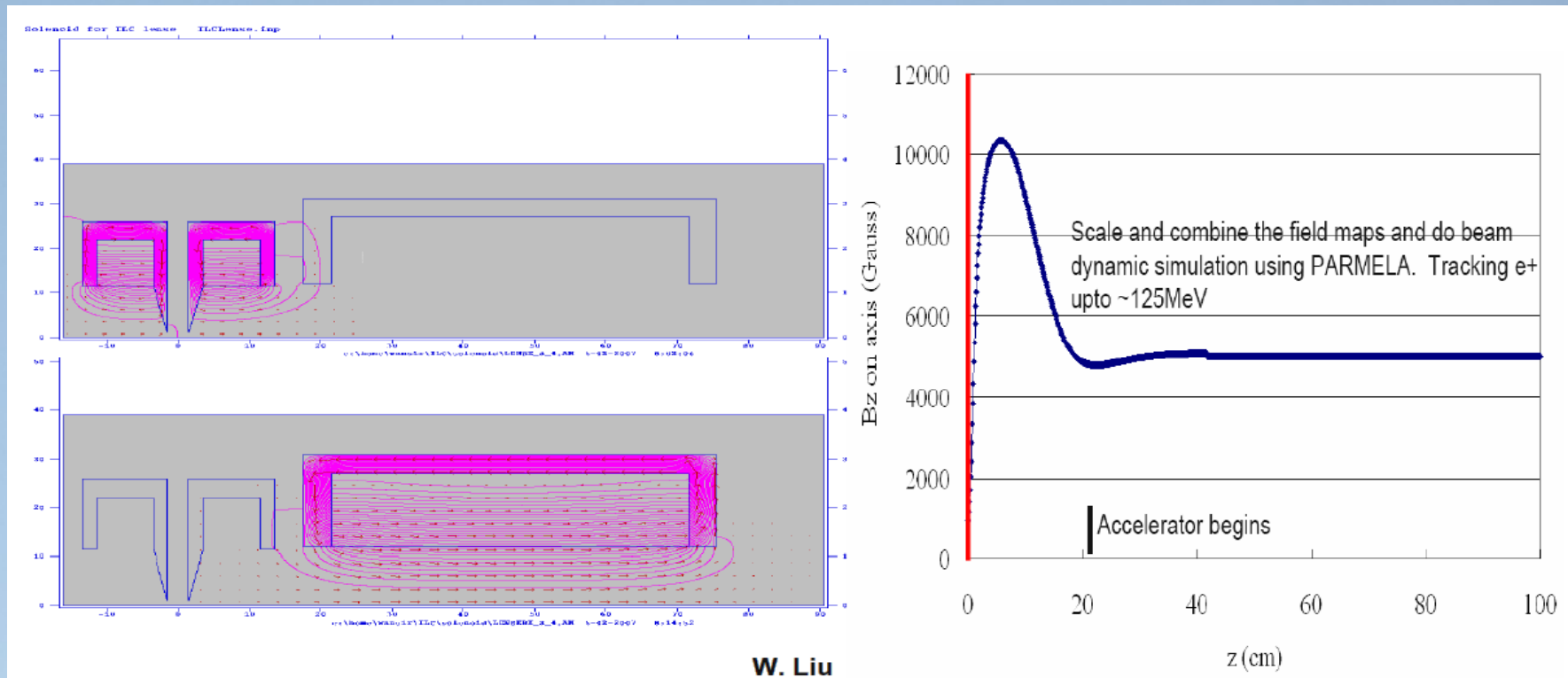
Radius of circulating motion of this particle in  $B_f$  is

$$\rho_f = \frac{1}{eB_f} \frac{P_{t0} B_f}{B_i} = \frac{P_{t0}}{eB_i} \quad (2-13)$$

The particle continues the circulation with the same radius, but less  $P_t$ .



# QWT(6)

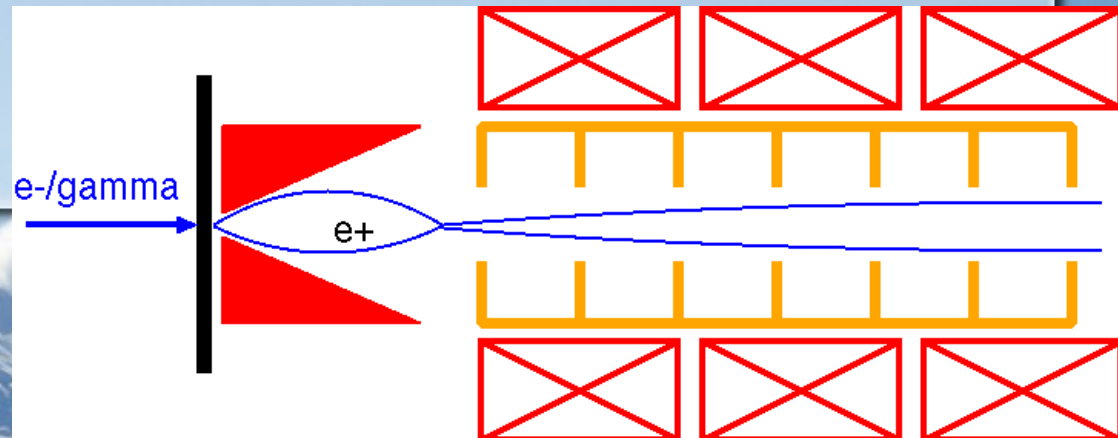
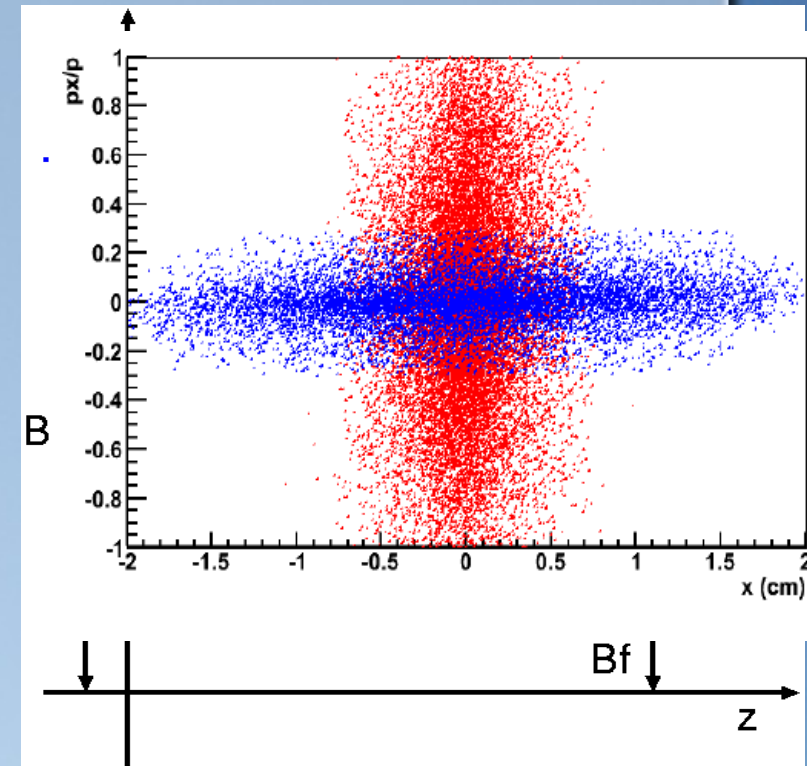


- Initial strong solenoid magnet with bucking to cancel B field on target.
- $B_f$  is 0.5 T.
- NC L-band accelerator is placed in  $B_f$  region.

# AMD(1)

AMD consists from the initial strong solenoid field along z direction,  $B_i$ , which is decreased down to  $B_f$  continuously.

$$B(z) = \frac{B_i}{1 + \mu z} \quad (2-18)$$



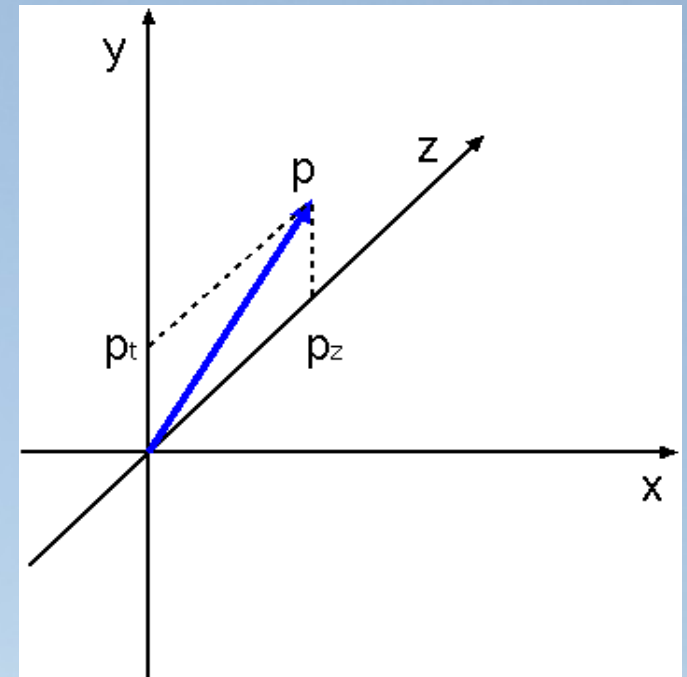
# AMD (2)

In xy plane, positrons are circulated with radius  $\rho(z)$ ,

$$\rho(z) = \frac{p_t(z)}{eB(z)} \quad (2-19)$$

If a parameter of the motion is changed slowly compare to the circulating frequency, adiabatic invariant is constant during the motion.

$$\frac{1}{2\pi} \int p dq = 2 \rho p_t(z) = 2 \frac{p_t(z)^2}{eB(z)} \quad (2-20)$$



# AMD(3)

Due to the adiabatic condition,

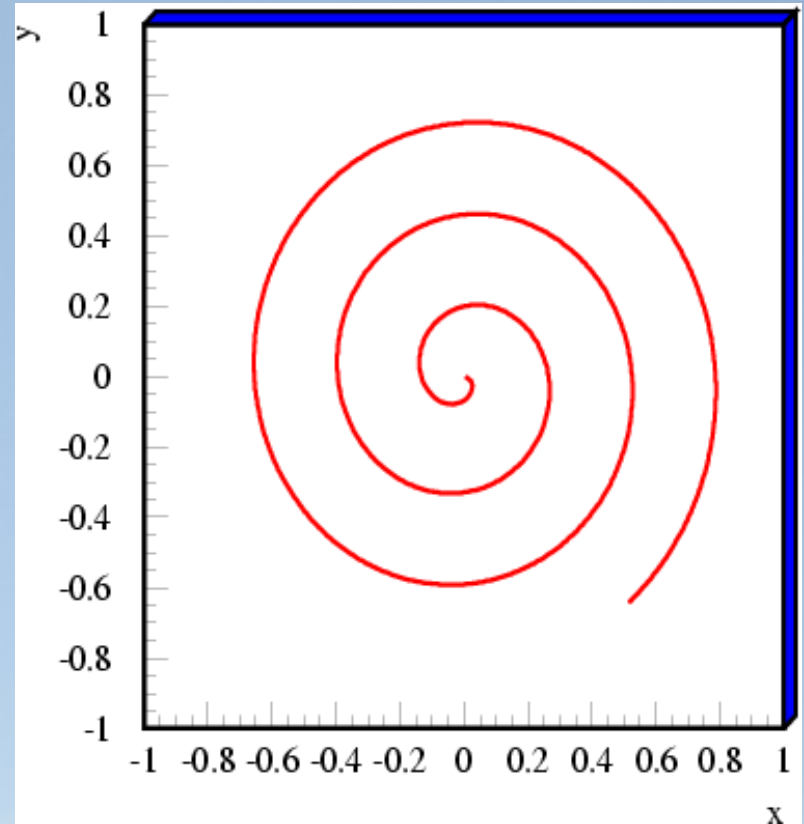
$$\frac{p_t(z)^2}{eB(z)} = \frac{p_{t0}^2}{eB_i} \quad (2-21)$$

$$p_t(z) = \sqrt{\frac{B(z)}{B_i}} p_{t0} \quad (2-22)$$

The radius is

$$\rho(z) = \frac{p_t(z)}{eB(z)} = \frac{1}{e\sqrt{B(z)B_i}} p_{t0} \quad (2-23)$$

$$\rho_f = \frac{1}{e\sqrt{B_f B_i}} p_{t0} \quad (2-24)$$



# AMD(5)

Pt at the exit of AMD is

$$p_t = \sqrt{\frac{B_f}{B_i}} p_{t0} \quad (2-25)$$

Acceptance on transverse momentum (aperture of accelerator)

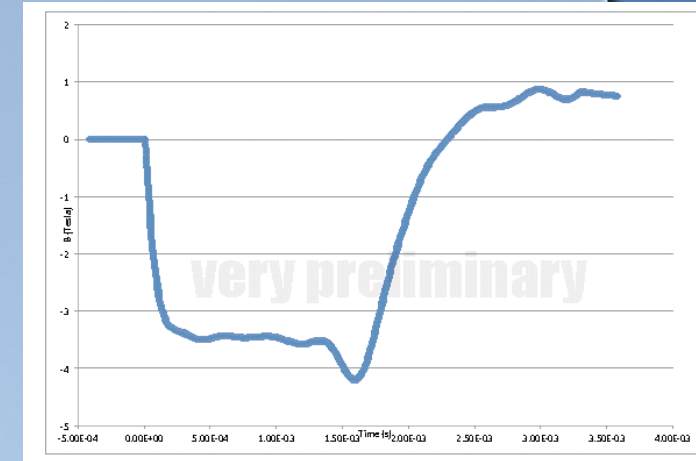
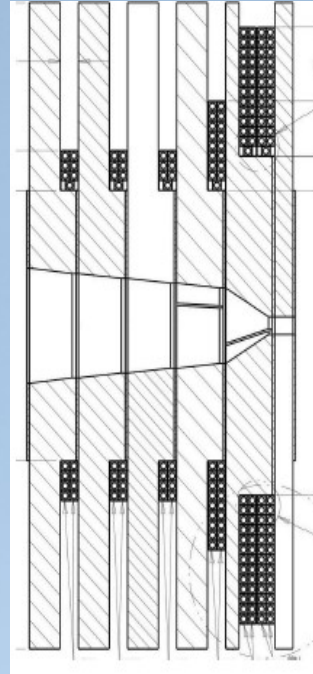
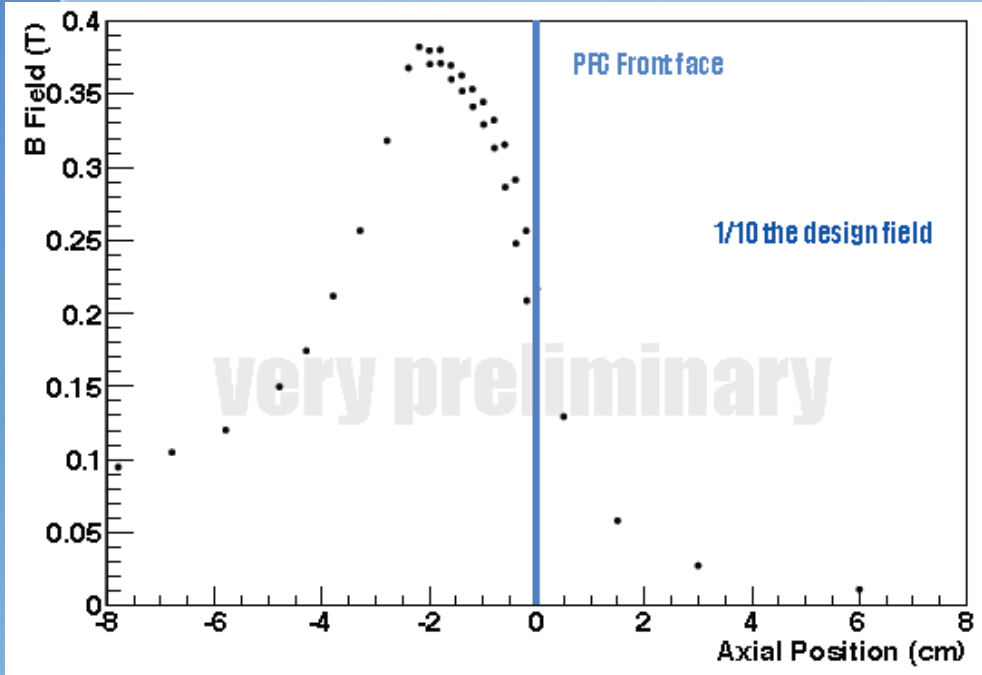
$$p_t < \frac{a}{2} e \sqrt{B_f B_i} \quad (2-27)$$

Acceptance on longitudinal momentum (adiabatic condition)

$$p_z < 0.5 \frac{eB_i}{\mu} \quad (2-28)$$



# AMD(6)



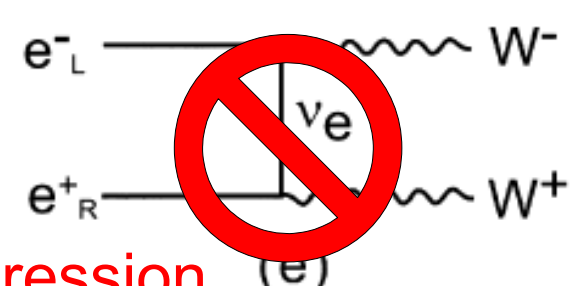
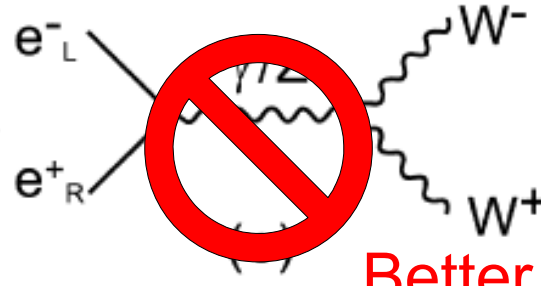
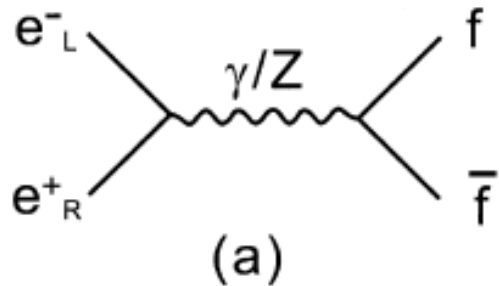
- AMD field is produced by flux-concentrator.
- Primary coil induces eddy current in the inner conductor.
- Because of the tapered shape of the inner conductor, the magnetic field is concentrated.

# Positron Source For LC

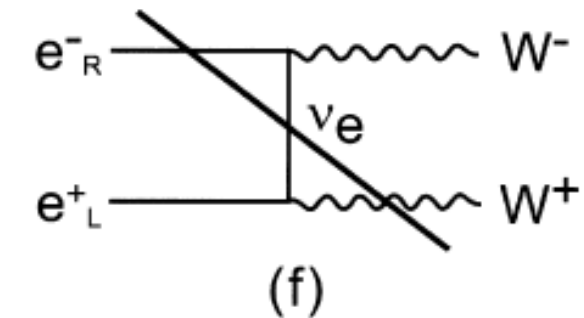
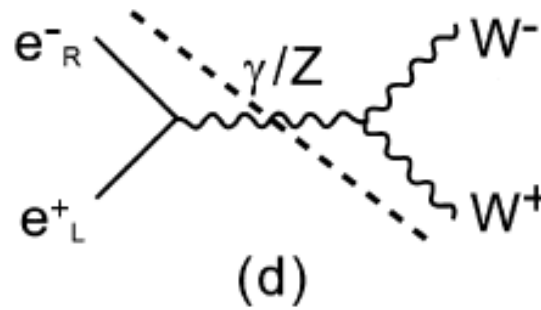
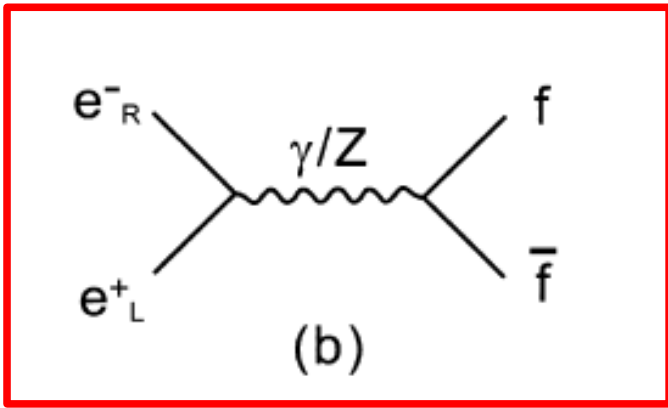
4 Nov. - 14 Dec., Antalya, Turkey  
8<sup>th</sup> Accelerator School for Linear Colliders

# Positron Polarization

- Since the high electron polarization is expected as high as 90%, the positron polarization is helpful, but not mandate

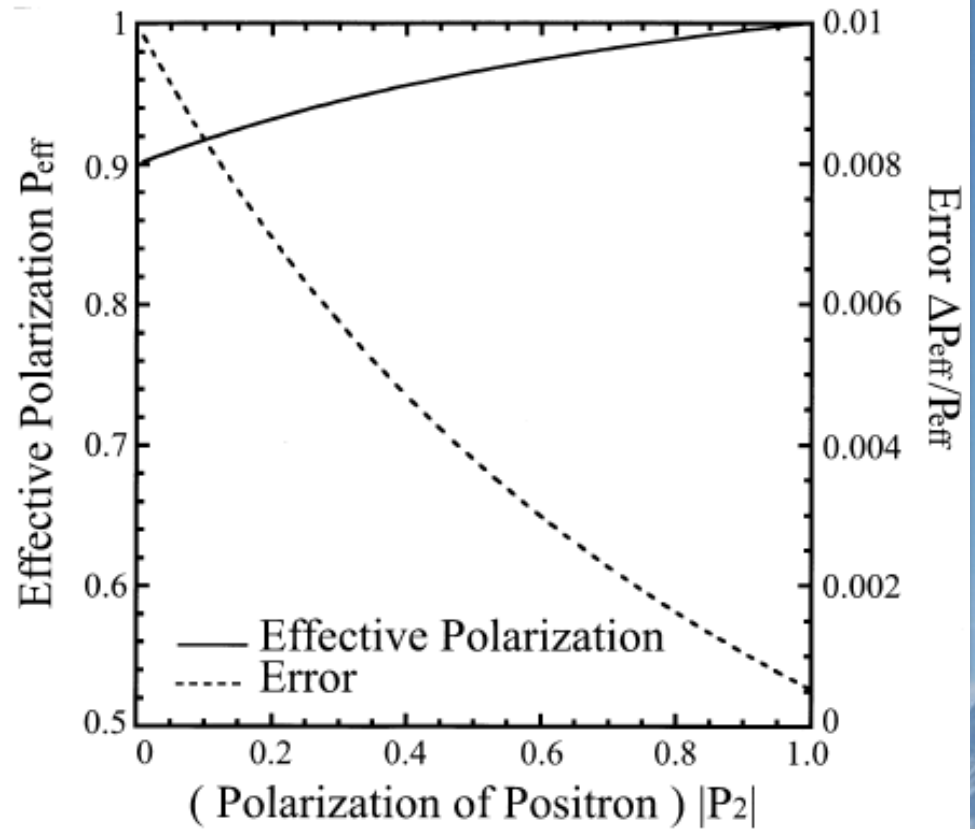
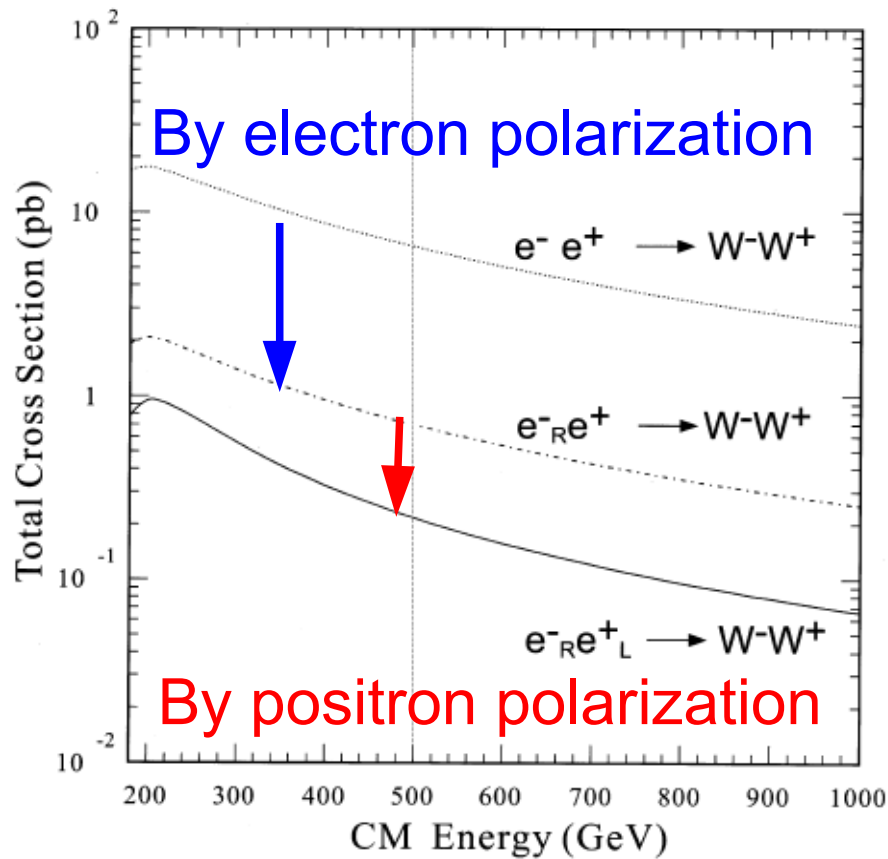


Better suppression



# Effective Polarization

$$P_{\text{eff}} = (P_- - P_+) / (1 - P_- P_+)$$



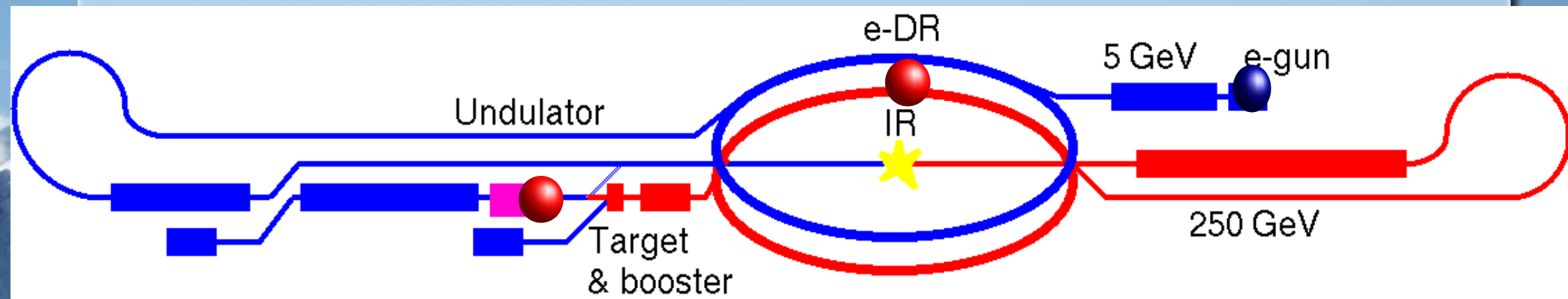
# Parameters

Parameter	ILC	CLIC	Unit
Bunch charge	3.20	0.60	nC
Norm. emittance ( $\epsilon_x + \epsilon_y$ )	0.09	?	m.rad
Bunch separation	369 (670)	0.5	ns
Bunch number in macro pulse	2625(1312)	312	number
Macro pulse length	970(880)	0.16	$\mu$ s

- ▶ ILC: Large bunch charge, low repetition, low current, long pulse are optimized for SC.
  - Baseline : undulator
  - Alternative : electron driven, laser Compton
- ▶ CLIC: Low bunch charge, high repetition, high current, short pulse are optimized for NC.
  - Baseline: electron driven (channeling),
  - Backup: Laser Compton, undulator.

# ILC Positron Source

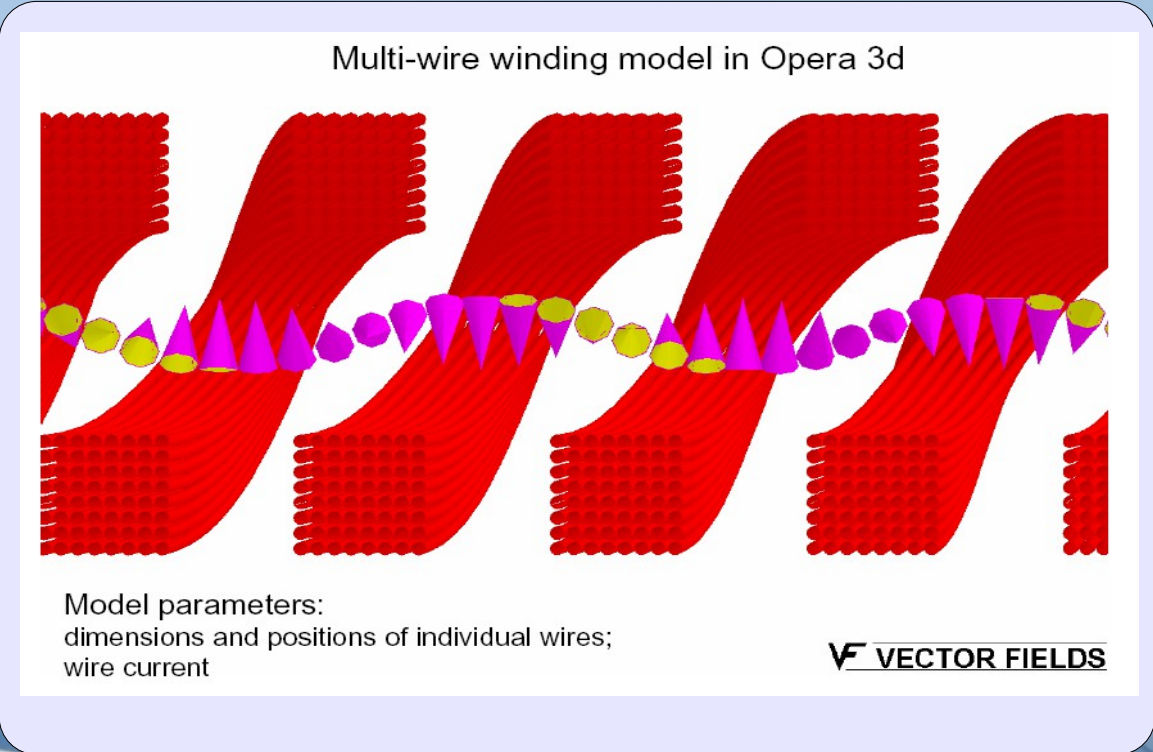
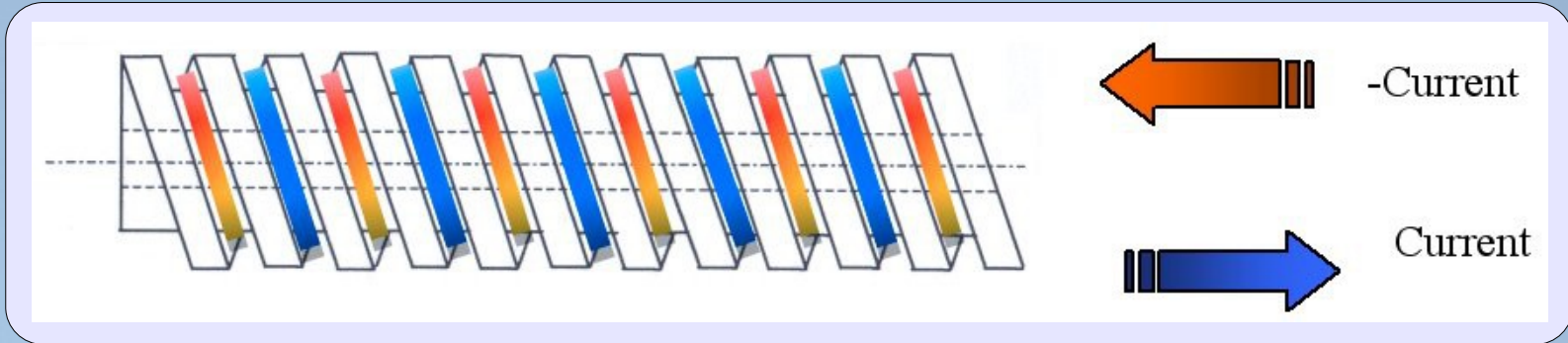
- ▶ It is the first undulator based positron source in the world.
- ▶ 250 GeV electrons generate gammas.
- ▶ Gamma rays are converted to positron.
- ▶ 5 GeV positron booster.



# System Specifications

Parameter	Value	Unit
Gamma/bunch	1.20E+13	Number
Positrons/bunch	2.00E+10	Number
Positron yield	1.5	e+/e-
Electron drive energy	150-250	GeV
Drive beam energy loss	4.8	GeV
Undulator length	147-231	m
Polarization	30-60	%

# Helical Undulator



By Yury Ivanyushenkov



# Undulator Specifications

Parameter	Value	Unit
Undulator Type	SC Helical	-
Undulator period	11.5	mm
Undulator Strength (K)	0.92	-
Magnet Current	205 (86% of critical)	A
Magnetic field (on axis)	0.86	T
Undulator Length (unpolarize)	147 (231)	m
Beam Aperture	5.85	mm
Photon Energy (1st h <sub>rm</sub> )	10.07	MeV
Max. photon power	131	kW

# Undulator Cryo-module

Stainless steel vacuum vessel  
with Central turret

50K Al Alloy Thermal shield.  
Supported from He bath

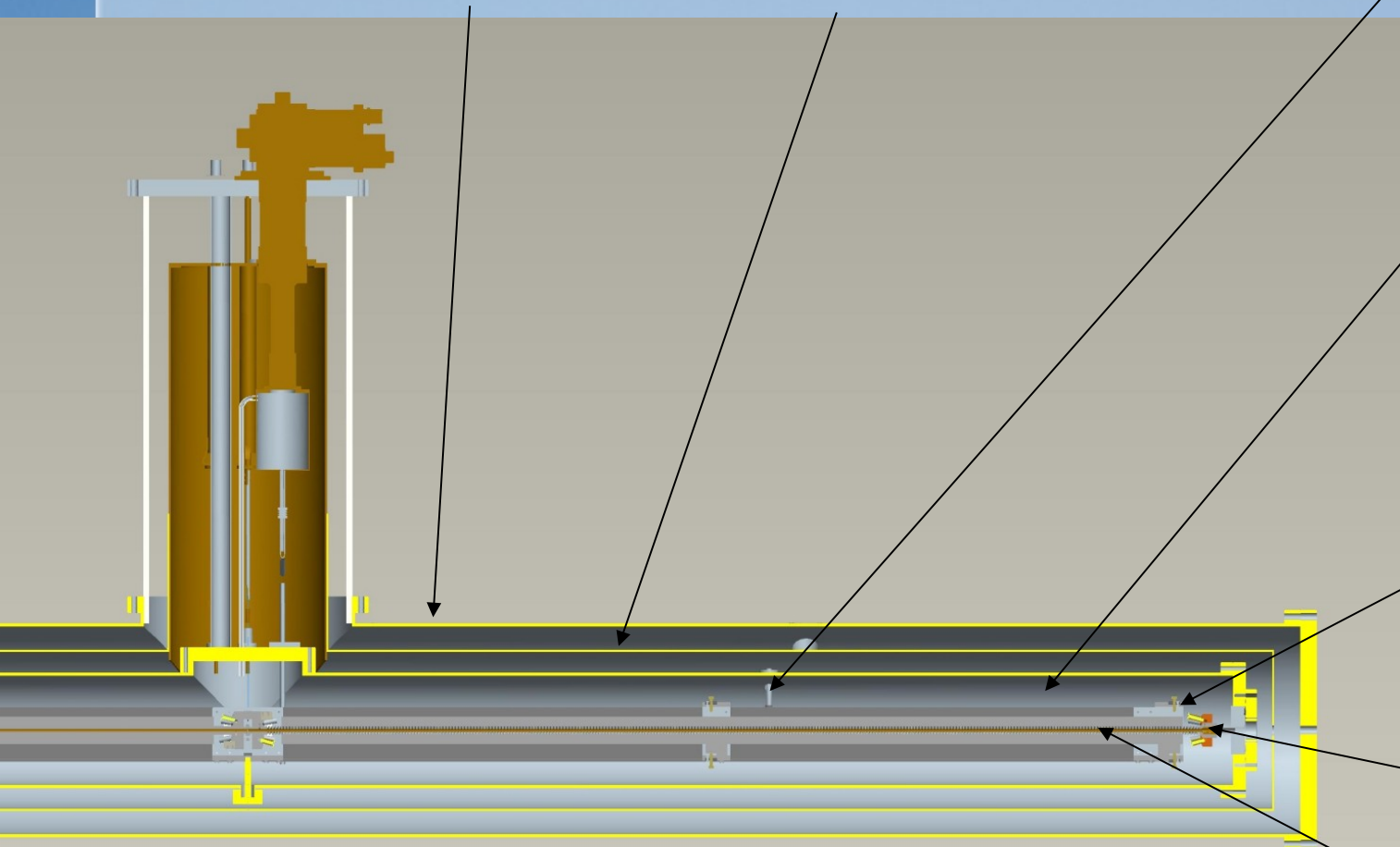
U beam  
Support rod

Stainless Steel He  
bath contains 100L liq  
He. Supported by 4  
rods attached to the  
vacuum vessel

U Beam used to  
support/align the  
magnet.

Beam Tube

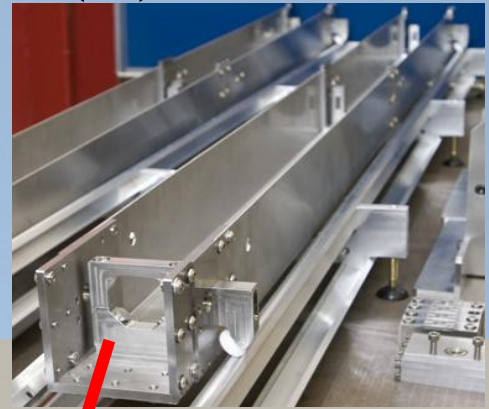
Magnet cooled  
to 4.2K by liq He  
in bath.



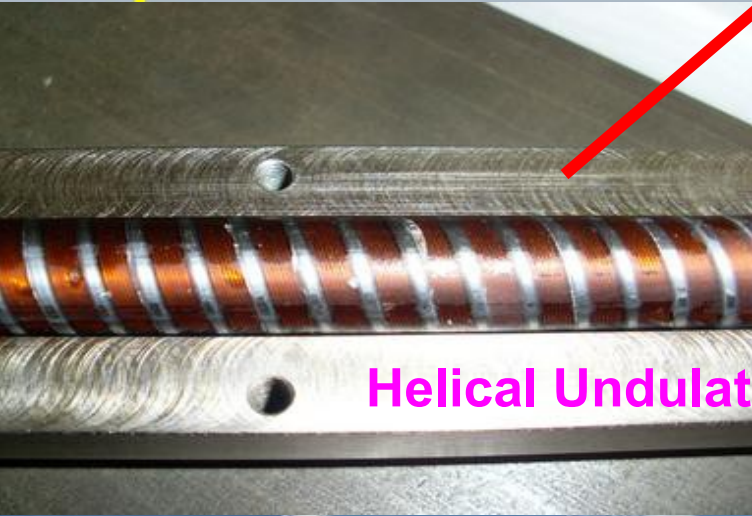
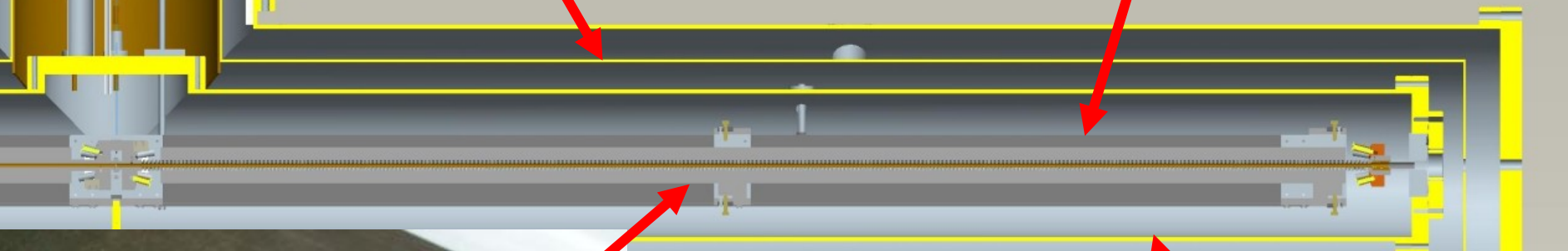
# Undulator Cryomodule (2)



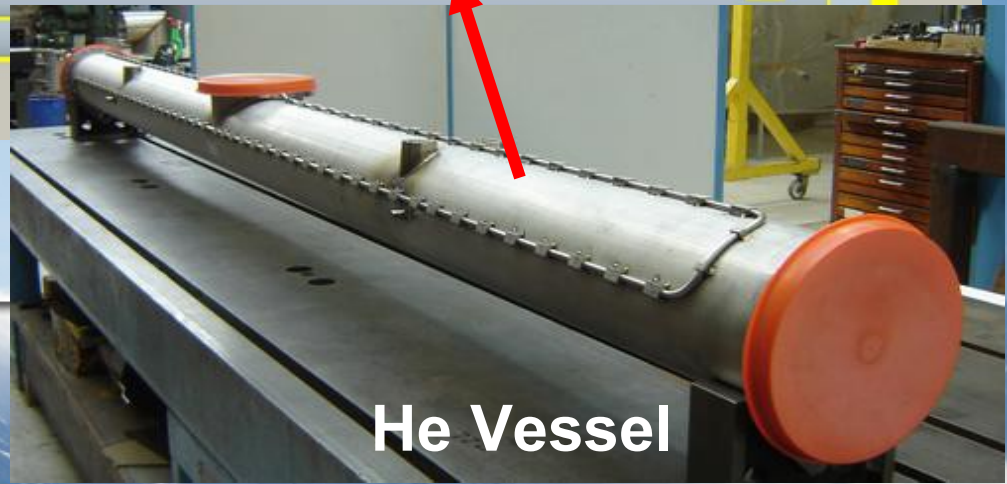
Heat Shield



U Beam

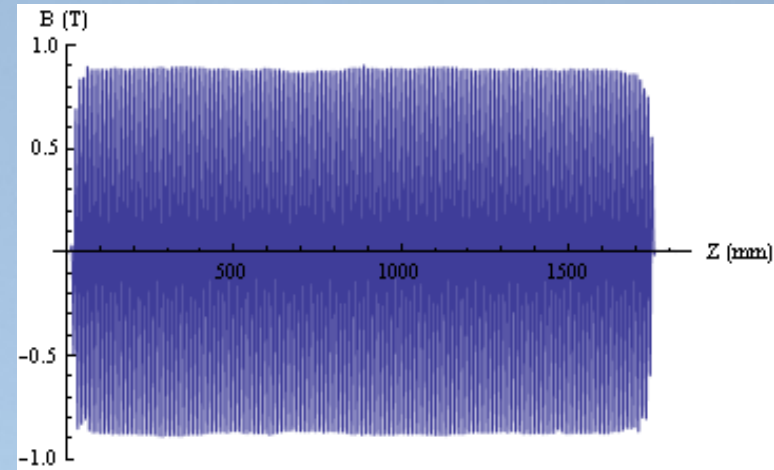
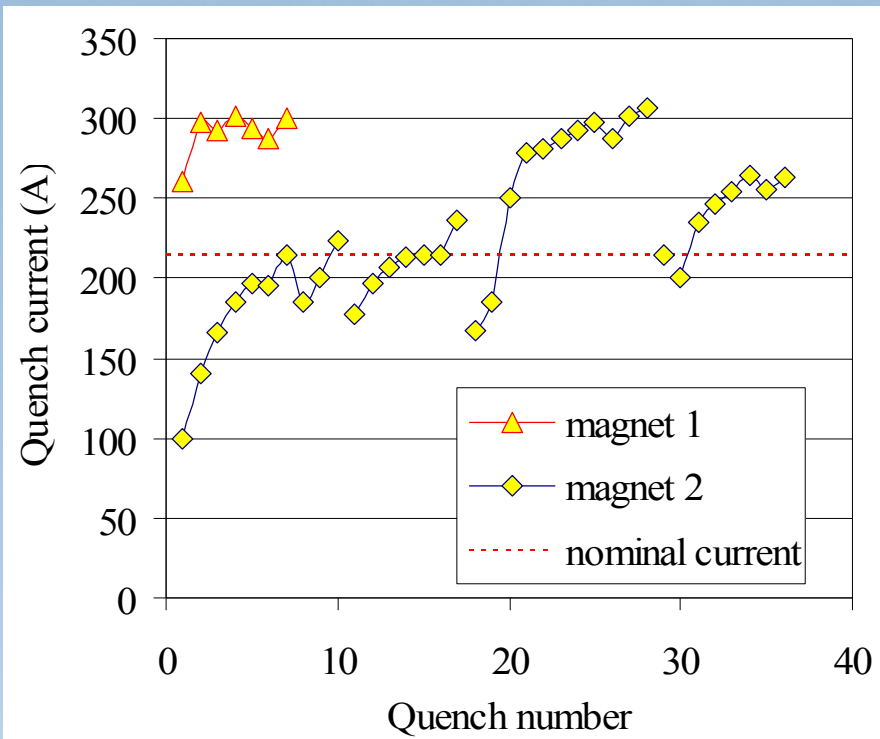


Helical Undulator



He Vessel

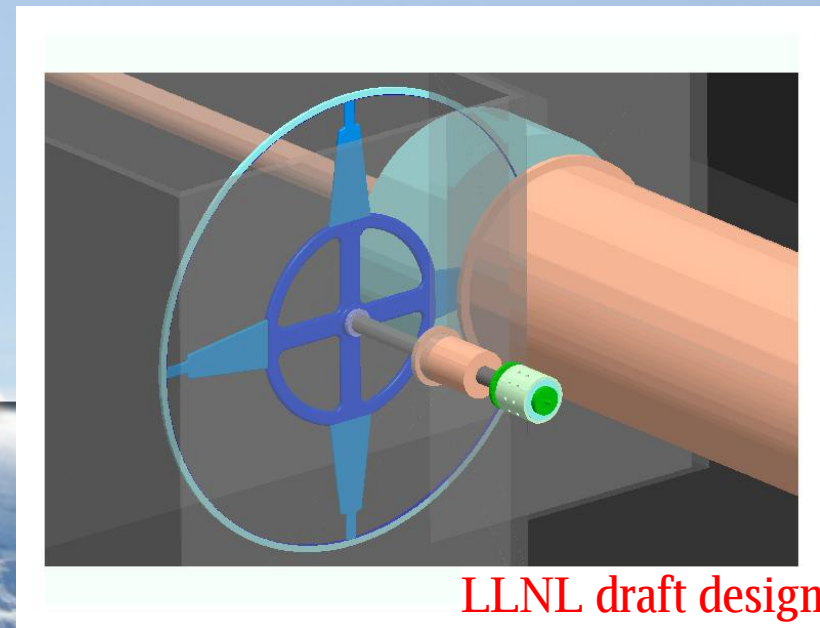
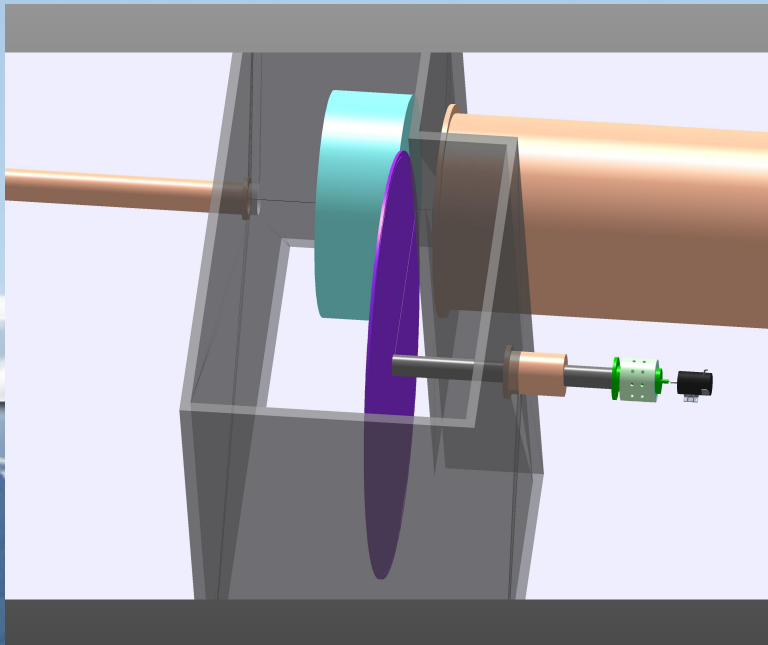
# Undulator: Field test



- All two magnets finally satisfied the specification.
- Field profile is measured by hall probe, showing a good quality.

# Target

- Target : Ti-6% Al-4% V with  $0.4 X_0$ , rotating with tangential speed 100 m/s .
- Beam spot : 15 mm
- Heat load by gamma : 18 kW
- Heat load by Eddy current :20kW (rim) when the target is immersed in B field.
- Vacuum seal is a technical issue.

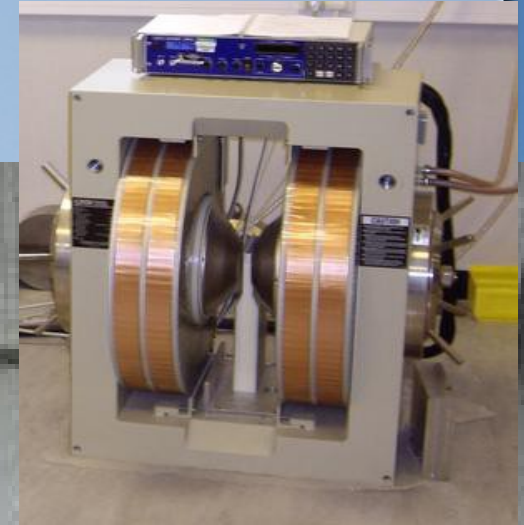


LLNL draft design

# Target Prototype

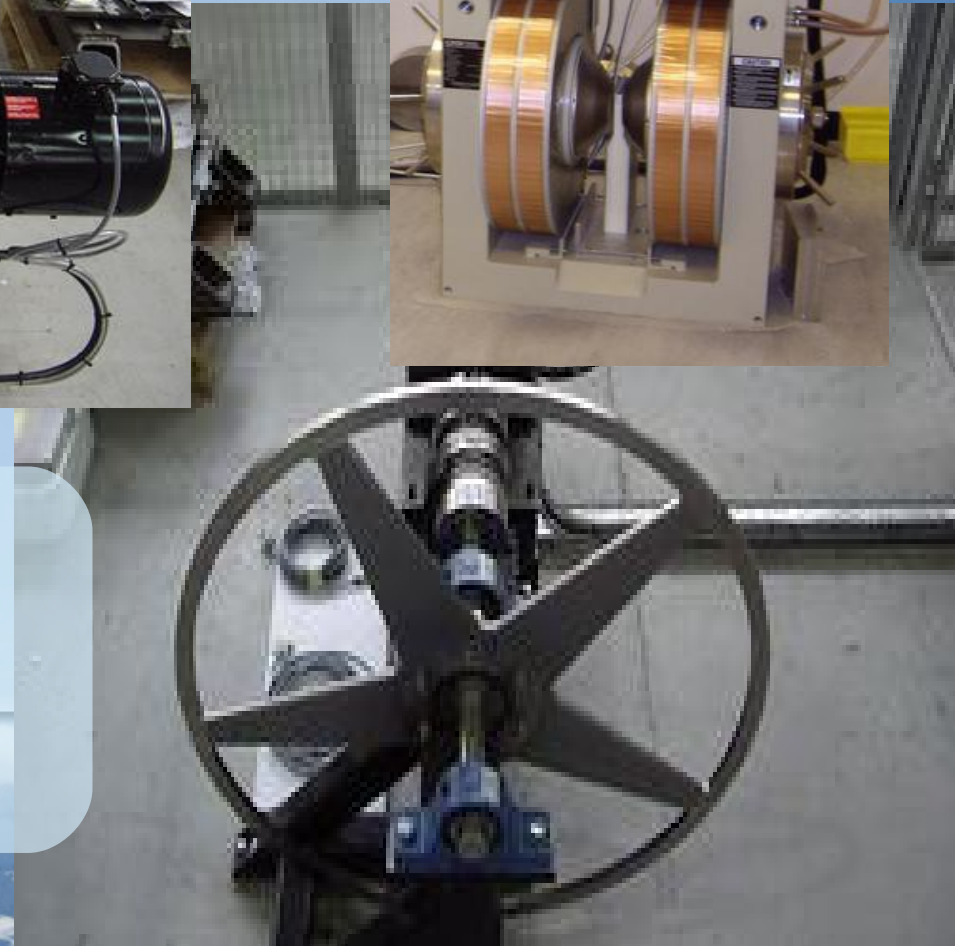


Experiment in Cock-croft Inst. UK



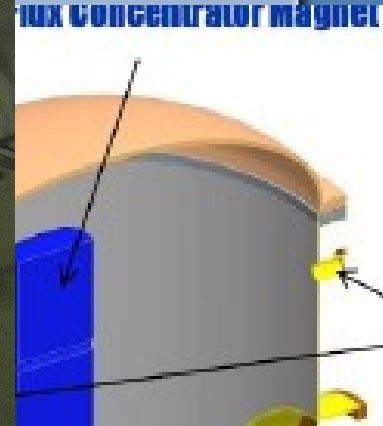
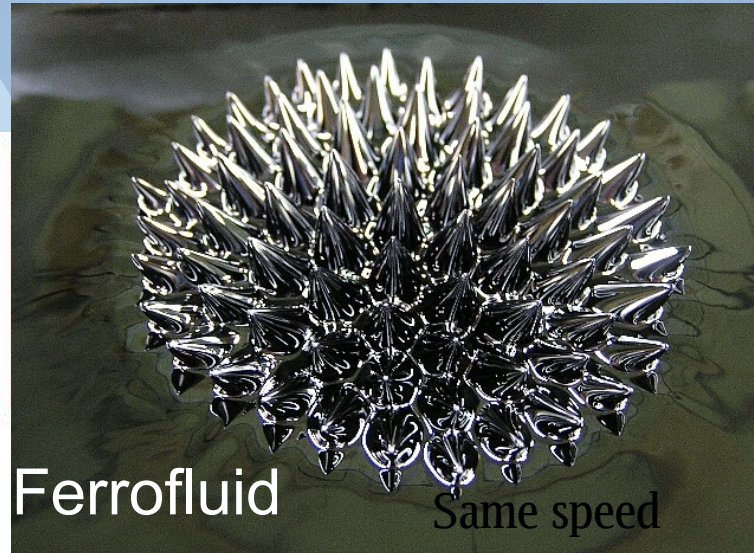
- Test with  $<1800$ rpm was done.
- Extrapolating to  $2000$ rpm shows that wheel will be able to operate in immersed fields  $\sim 1$ T.

I. Bailey

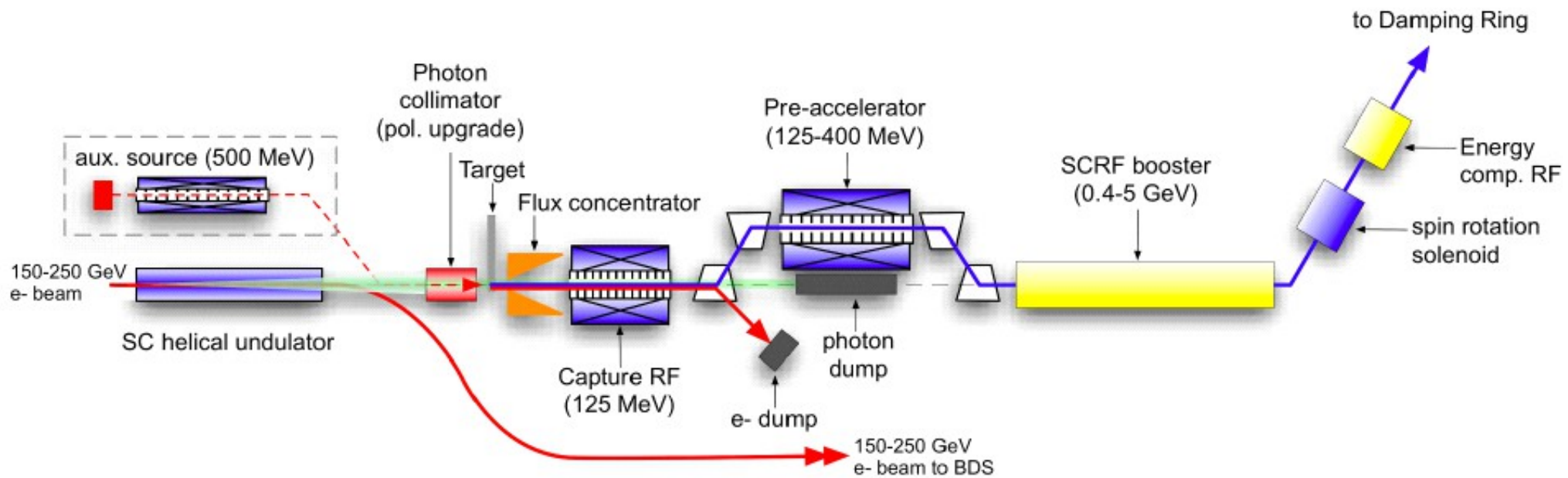


# Target Design

- The target should be fastly rotated (100m/s, 2000rpm) in high vacuum,  $1e-7$ Pa.
- We need a good vacuum seal with the rotation rod.
- Magnetic fluid seal is a candidate.
- Need a system integration to demonstrate the technical feasibility.

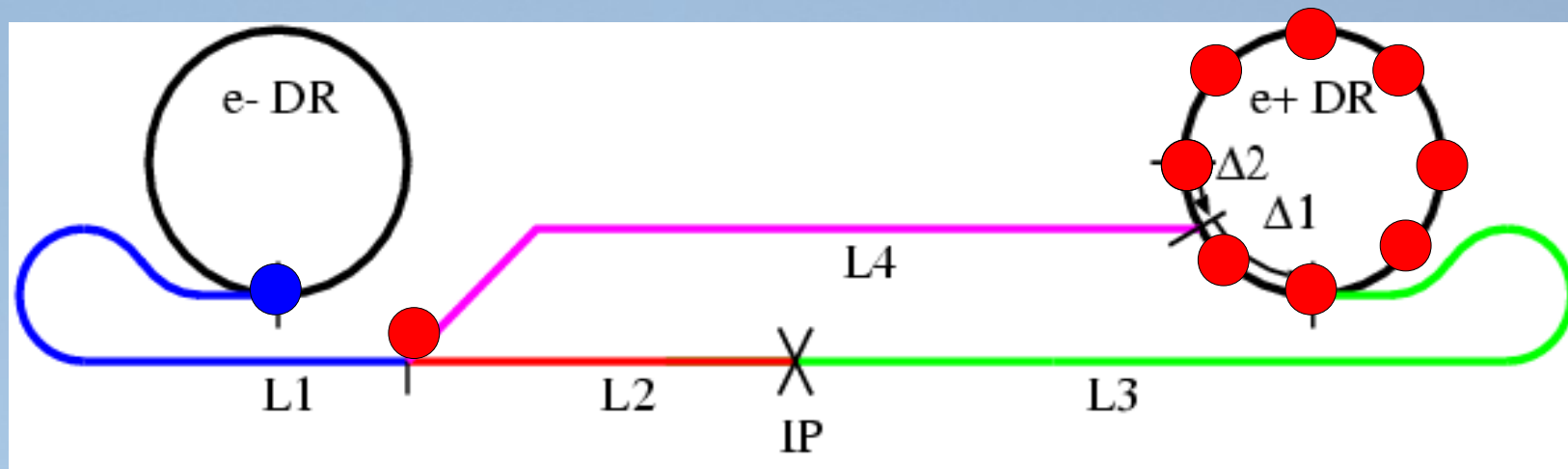


# ILC Undulator Positron Source Layout



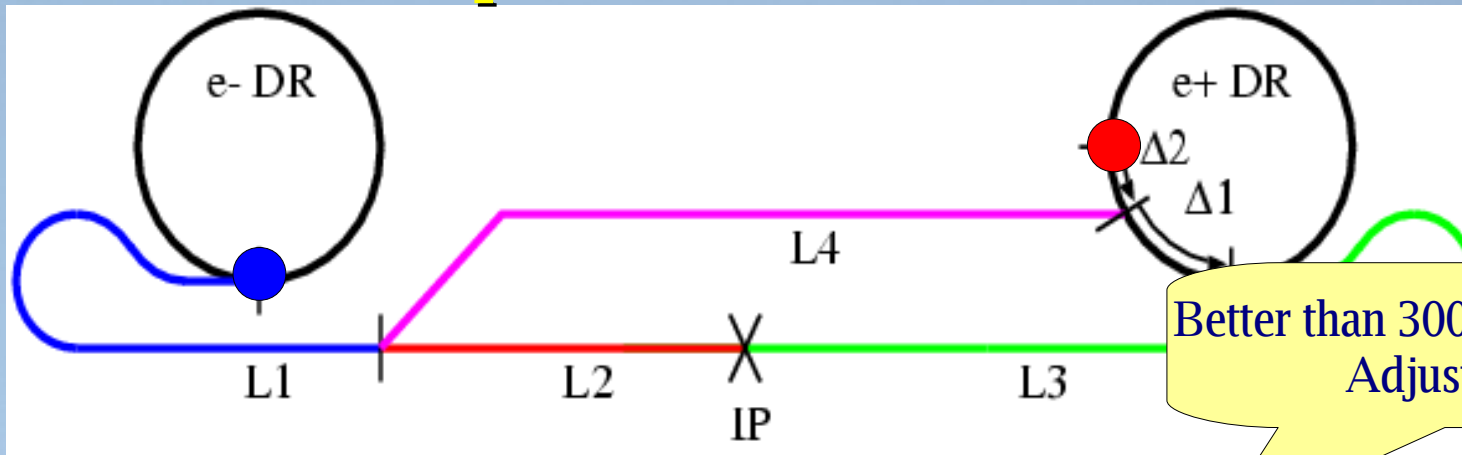


# Path Length Condition



- Positron beam is generated by electron bunch.
- The generated positron must wait 200ms in DR until the next collision.
- Generation and collision are performed simultaneously. The DR bucket must be vacant for the generated positron.
- To fulfill the condition with a flexibility, the path-length must satisfy the self-reproduction condition.
- The positron is stored in the DR bucket where the collision partner of the electron which generates the new positron.

# Pathlength condition: Self-reproduction + collision



• Collision condition:

$$L_1 + L_2 = \Delta_1 + \Delta_2 + L_3,$$

• Self-reproduction condition:  $L_1 + L_4 = \Delta_2 + nC_{DR},$

$$L_3 + L_4 + \Delta_1 = L_2 + nC_{DR},$$

Better than RF bucket height (5mm)  
Adjusted by physical length.

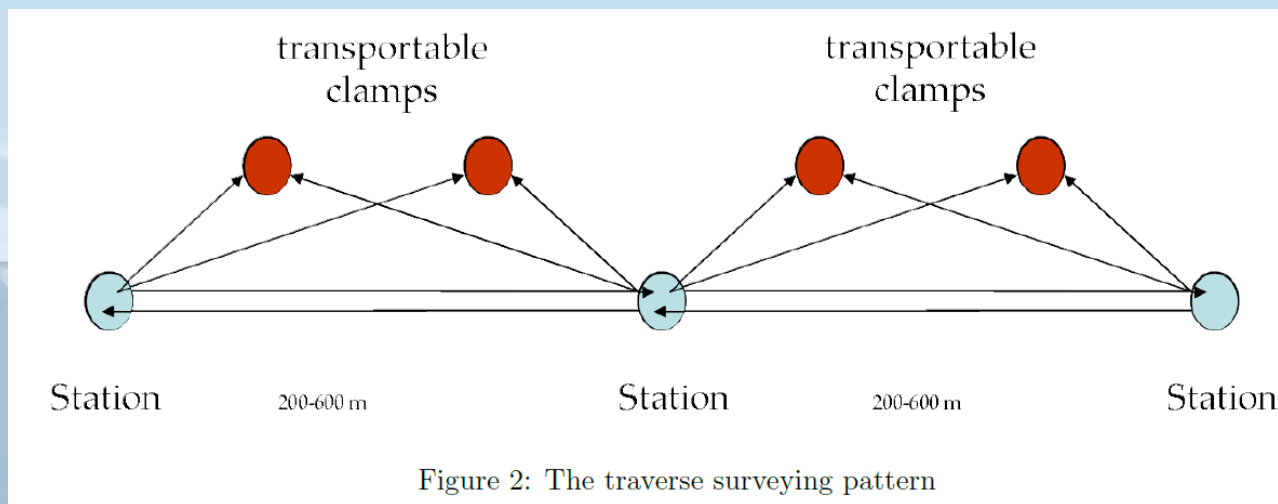
**Physical path length has to be adjusted.**

# Adjustment



# Installation accuracy OPERA's study

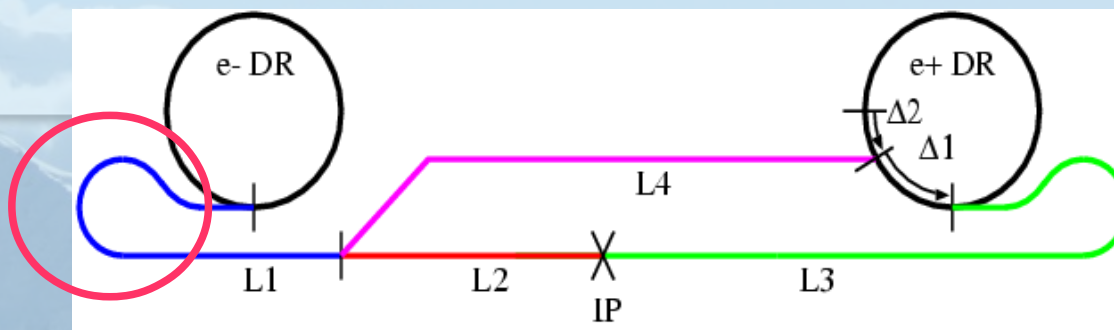
- GPS determines position in a common system with high accuracy, e.g. path from CERN to Gran Sasso is determined as  $700\text{km} \pm 3\text{cm}$ .
- GPS can not be used in tunnel or underground.
- To examine the super-light speed neutrino, distance from the tunnel entrance to OPERA detector was measured with surveying meter,  $10.5\text{km} \pm 20\text{cm}$ .
- The accuracy in 15km ILC tunnel could be 30cm, worse than 5mm.



OPERA Public Note 132 v3

# Pathlength Adjustment

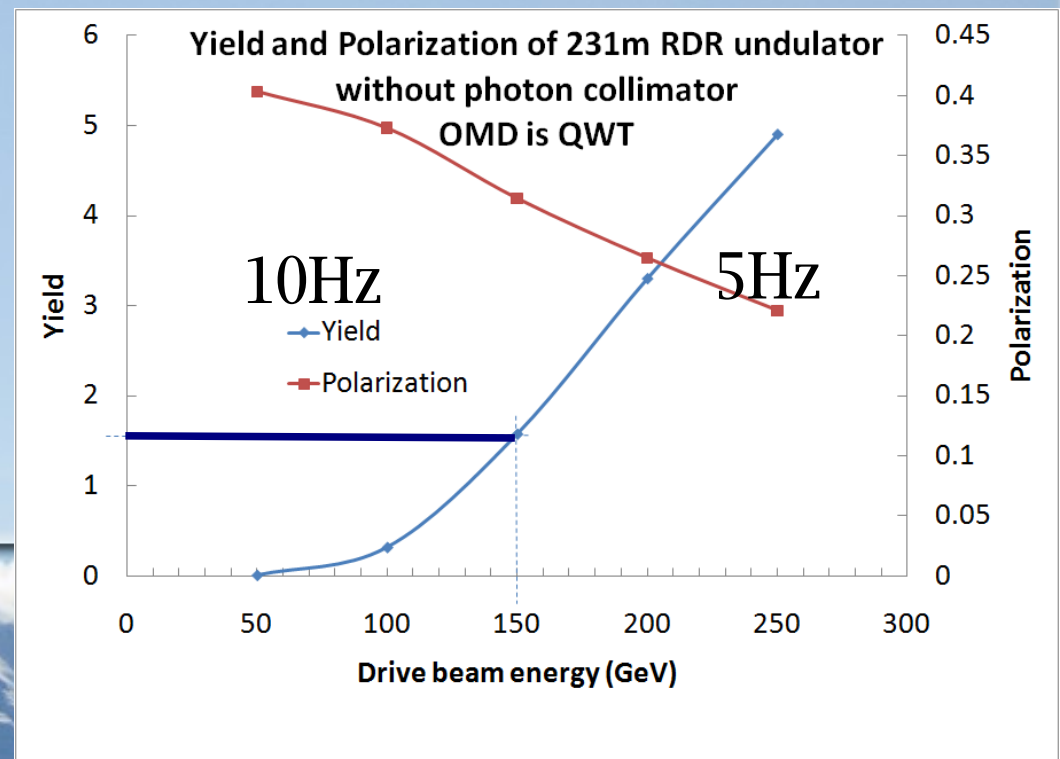
- To adjust 30cm by 50 chicane sections with 1m shift, the total length could be 1500m. It is unrealistic.
- DR circumference  $C_{DR}$  can be adjusted by RF frequency with extremely good accuracy. In early commissioning, the adjustment length can be estimated by varying  $C_{DR}$ .
- The physical pathlength is adjusted according to the estimation.
- Small adjustment mechanism, e.g. orbit in turn around, is necessary.



$$L_1 + L_4 = \Delta_2 + nC_{DR},$$

# Positron Yield

- Drive energy for undulator is same as the collision energy.
- Positron yield at the low energy becomes less because of the low gamma energy and almost zero at less than 100 GeV.
- The electron beam dedicated for the positron generation is accelerated alternately with the beam for collision.
- Electron and positron linacs are operated in 10 and 5 Hz, respectively.



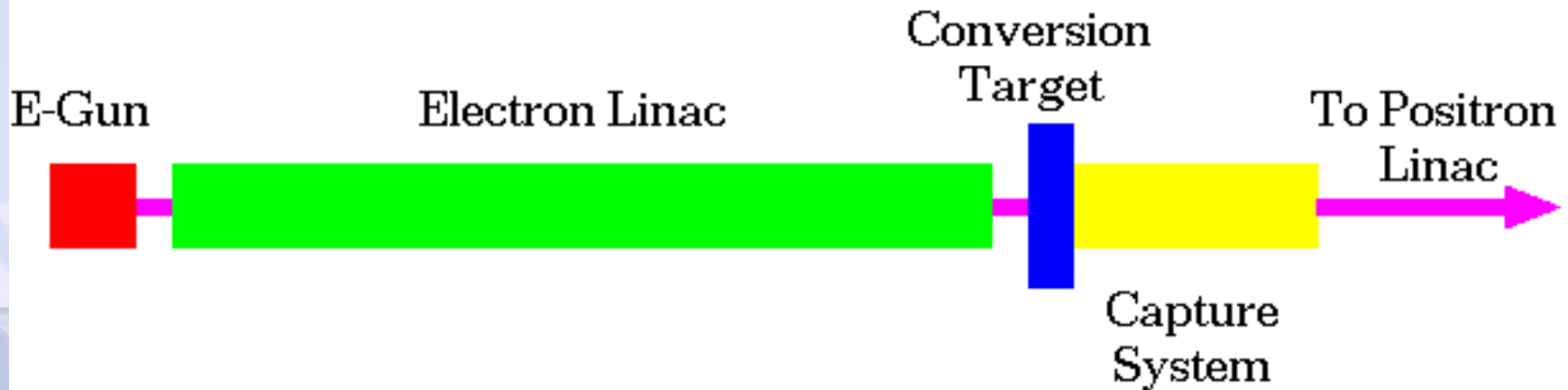
# Alternate Linac Operation

Need more electricity

Energy	Reaction	Physics Goal	Linac
91 GeV	$e^+e^- \rightarrow Z$	ultra-precision EW	10Hz
160 GeV	$e^+e^- \rightarrow WW$	ultra-precision Wmass	10Hz
250 GeV	$e^+e^- \rightarrow Zh$	precision Higgs coupling	10Hz
350-450 GeV	$e^+e^- \rightarrow tt$ $e^+e^- \rightarrow WW$ $e^+e^- \rightarrow \nu\nu h$	top quark mass and coupling precision W coupling precision Higgs coupling	5Hz
500 GeV	$e^+e^- \rightarrow f\bar{f}$ $e^+e^- \rightarrow t\bar{t}h$ $e^+e^- \rightarrow Zh h$ $e^+e^- \rightarrow \tilde{\chi}\tilde{\chi}$ $e^+e^- \rightarrow AH, H^+H^-$	precision search for Z' Higgs coupling to top Higgs self coupling search for super-symmetry search for extended Higgs sector	5Hz
1000GeV	<i>and more..</i>		5Hz

# Electron Driven Scheme

- Electron driven is the only scheme, which is ever been operated, but possible target damage has to be managed.
- Positron polarization is not possible.





# Why is it so difficult?

	$N^{e^+}/\text{bunch}$	Repetition(Hz)	$N^{e^+}/\text{sec}$
ILC	$2.0 \times 10^{10}$	$5 \times 2625$	$2.6 \times 10^{14}$
SLC	$4.0 \times 10^{10}$	120	$4.8 \times 10^{12}$

- ILC has to produce 50 times more positron than that of SLC.
- But, number does not matter, PEDD (Peak Energy Deposition Density) does.

$$PEDD \sim \kappa \frac{E(\text{GeV}) Q(\text{nC})}{V \rho} \frac{2r N_b}{vt_p}$$

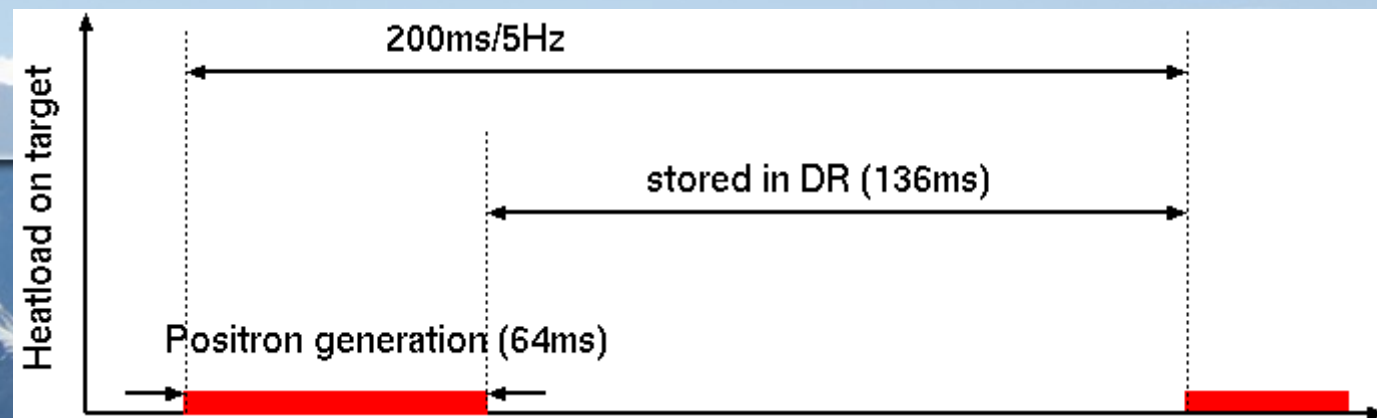
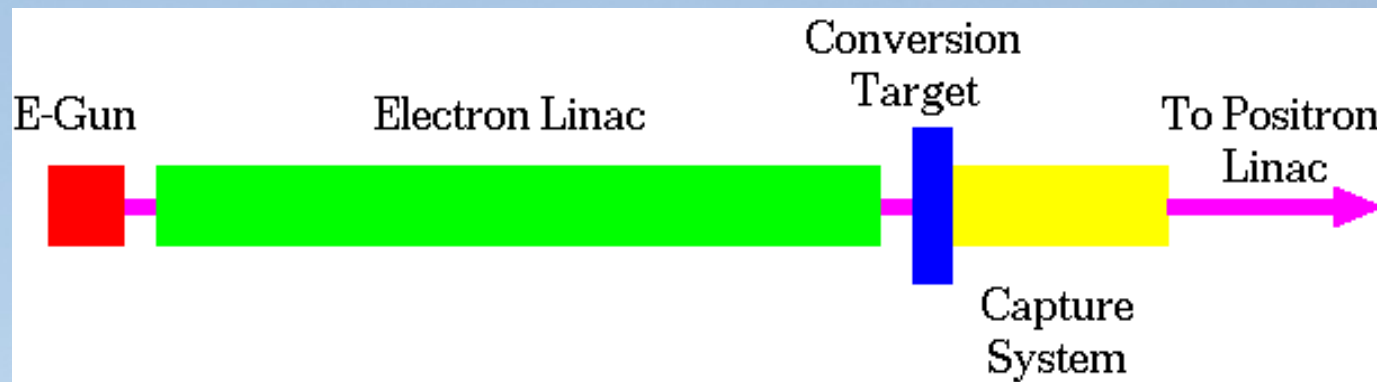
#of bunch

target speed

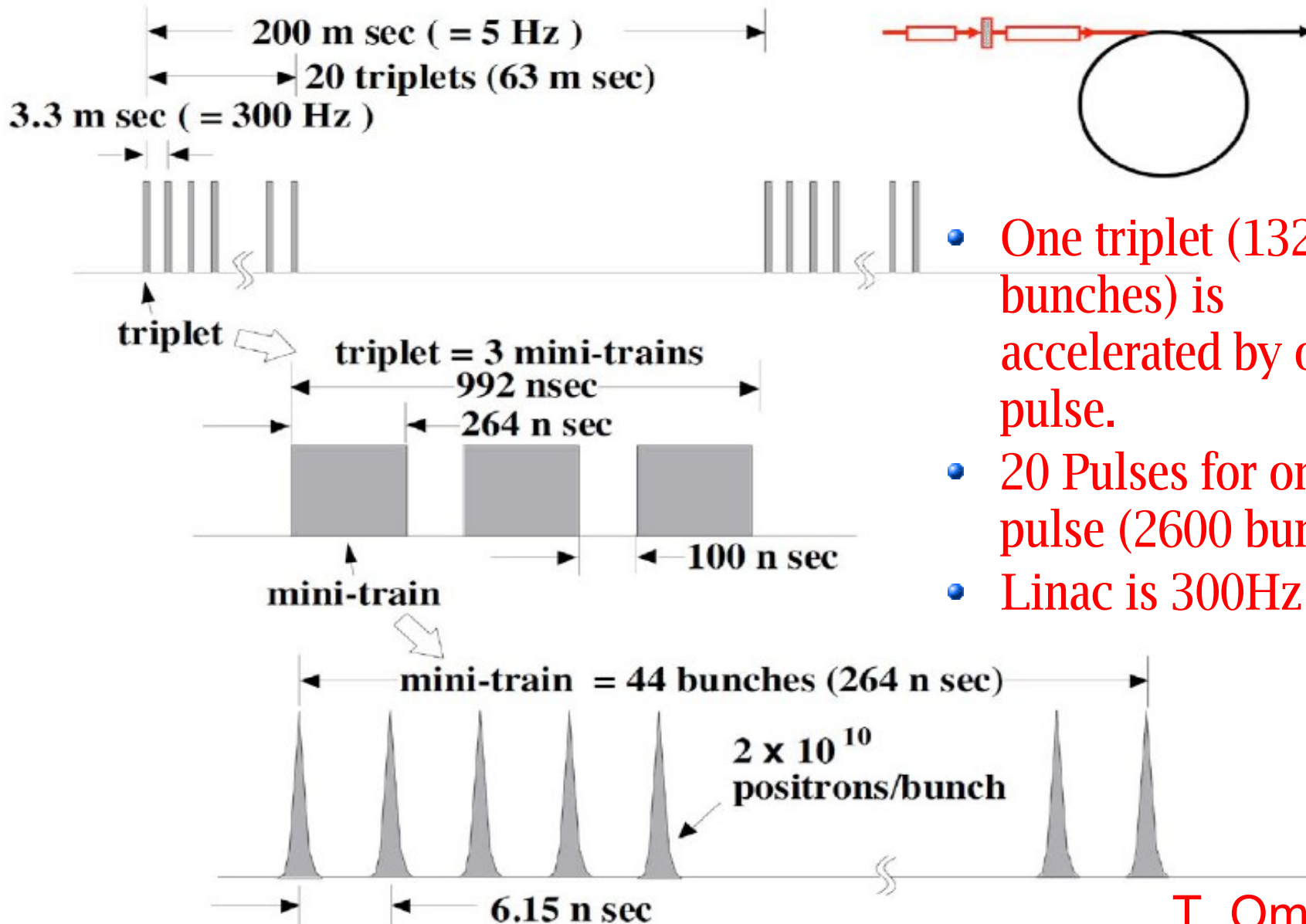
Pulse duration

# Pulse Structure Manipulation

- Several GeV e- beam on W-Re target.
- By manipulating the beam structure (64ms pulses), heat load on the production target is manageable.
- 5 m/s target speed is even enough.



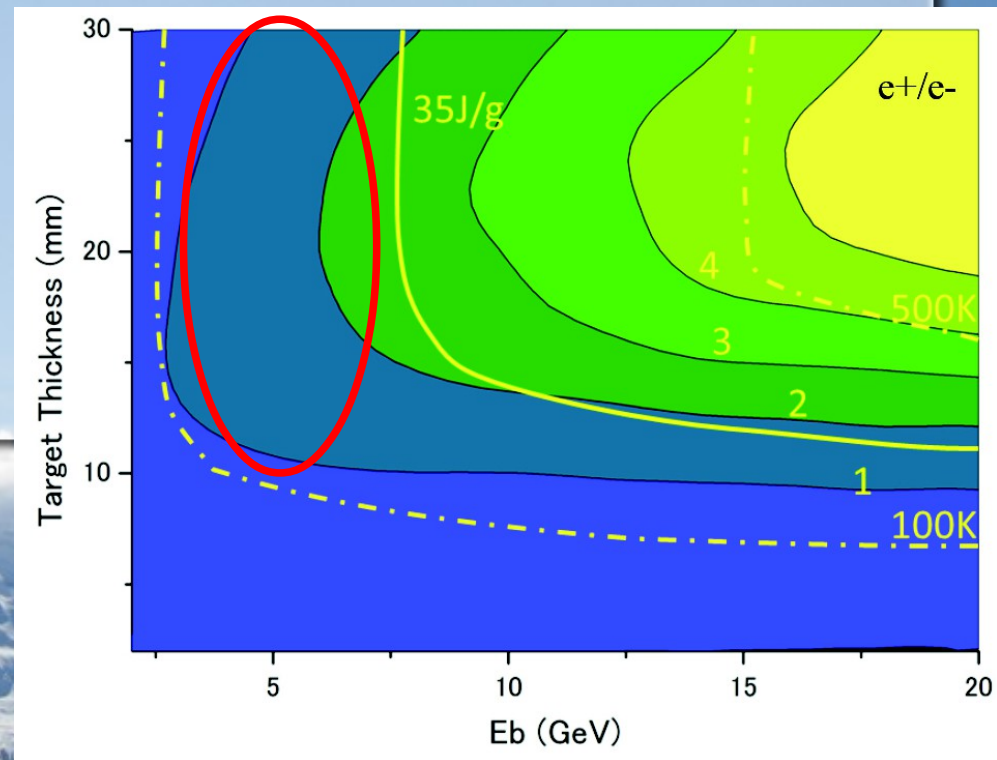
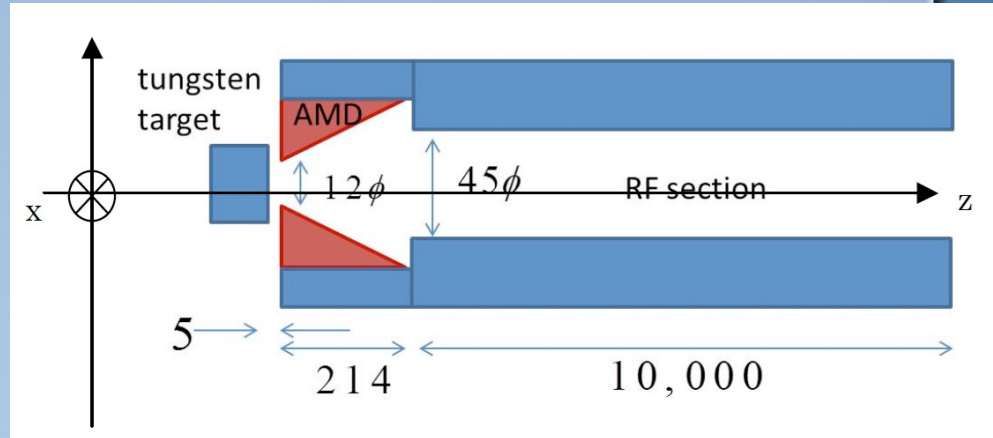
# 300Hz Generation



- One triplet (132 bunches) is accelerated by one RF pulse.
- 20 Pulses for one ILC pulse (2600 bunches).
- Linac is 300Hz NC.

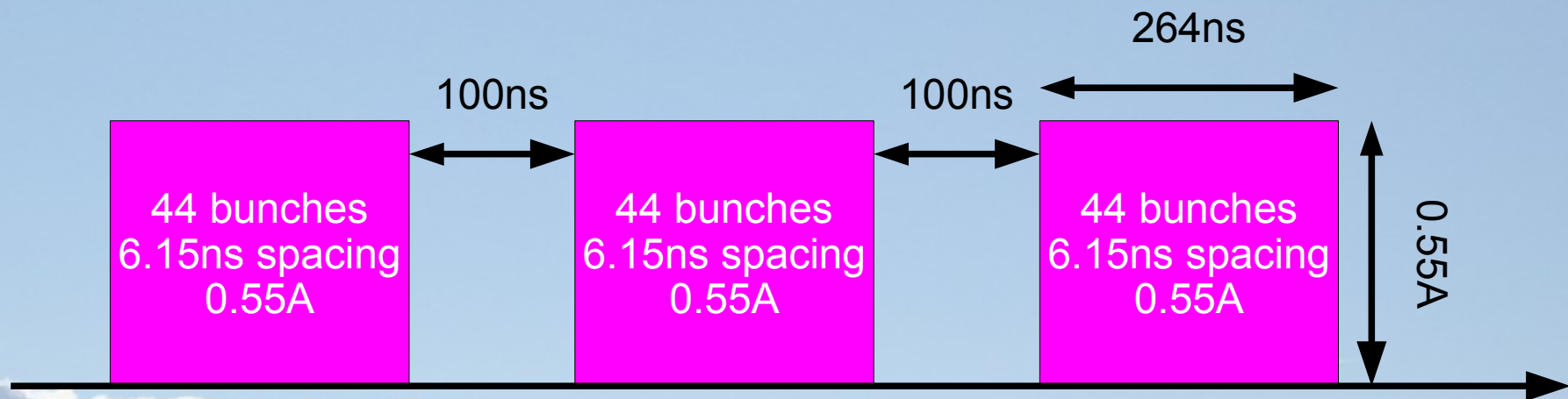
# Target PEDD

- Because there is no overlap between triplets, we consider only PEDD by one triplet.
- Energy by one triplet (132 bunches) deposited on a same spot.
- PEDD and  $e^+$  yield is evaluated.
- There is workable area;
  - PEDD  $< 35\text{J/g}$
  - Yield  $e^+/e^- > 1.5$



# Pulse Structure and Beamloading

- Positrons are accelerated by triplet multi-bunch pulse.
- The triplet pulse is repeated in 300Hz.
- Transient beamloading should be compensated, otherwise, the beam is not accepted by DR.



# Beamloading Compensation by AM

- Beamloading compensation by AM (Amplitude Modulation) is considered.
- By solving RF envelope giving a flat acceleration for the triplet, the acceleration field with the beamloading becomes flat.

Acceleration voltage by a flat RF ( $E_0$ ),

Beamloading term

$$V(t) = E_0L + \frac{r_0LI_0}{2(1 - e^{-2\tau})} \left[ \frac{\omega}{Q} e^{-2\tau}(t - t_f) - 1 + e^{2\tau - \frac{\omega}{Q}t} \right].$$

To compensate the transient beamloading, AM is introduced as follows,

$$E(t) = E_0U(t) + E_1U(t - t_f) - E_2(t - t_f)U(t - t_f) + E_2(t - 2t_f)U(t - 2t_f),$$

For steady beam loading suppression

For transient beam loading suppression

# Beamloading Compensation by AM

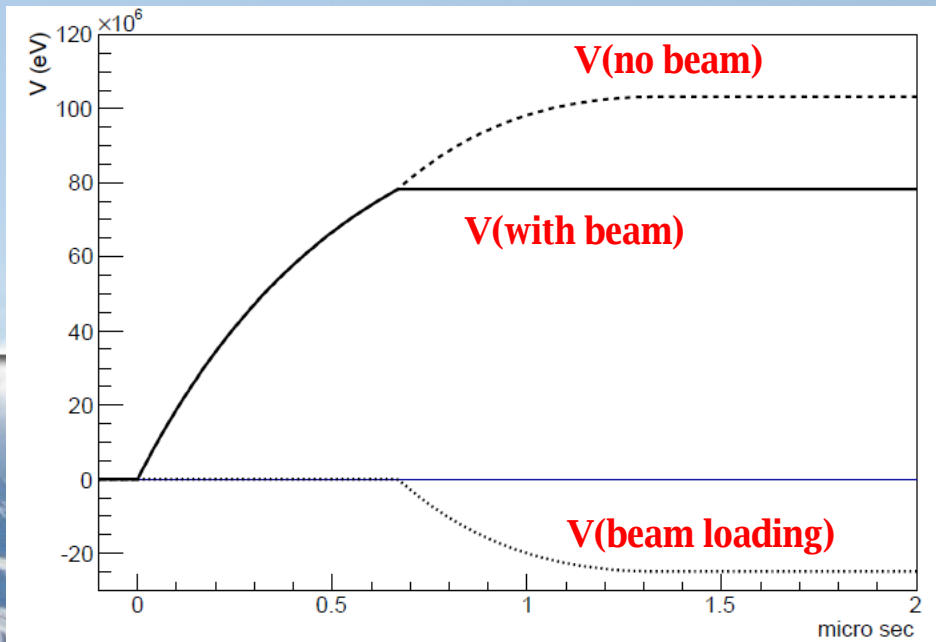
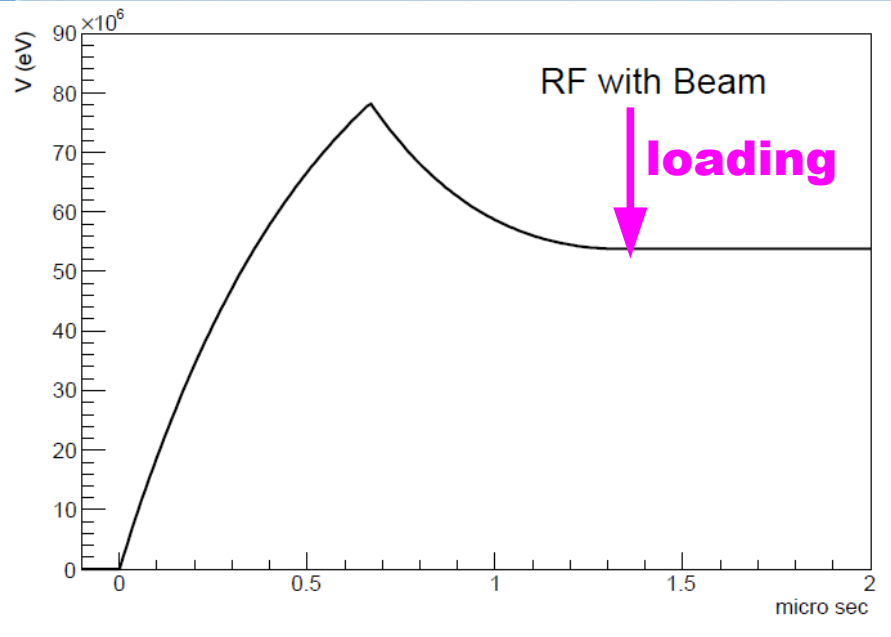
Acceleration voltage by AM RF ( $E_0 + E_1 + E_2$ ),

$$V(t) = E_0 L + \frac{L}{1 - e^{-2\tau}} \left( E_1 + \frac{Q}{\omega} E_2 \right) \left( 1 - e^{-\frac{\omega}{Q}(t-t_f)} \right) - \frac{L}{1 - e^{-2\tau}} E_2 (t - t_f) + \frac{r_0 L I_0}{2(1 - e^{-2\tau})} \left[ \frac{\omega}{Q} (t - t_i) - 1 + e^{-\frac{\omega}{Q}(t-t_f)} \right],$$

Solution for the flat acceleration

$$E_1 = \frac{r_0 I_0}{2} (1 - e^{-2\tau}),$$

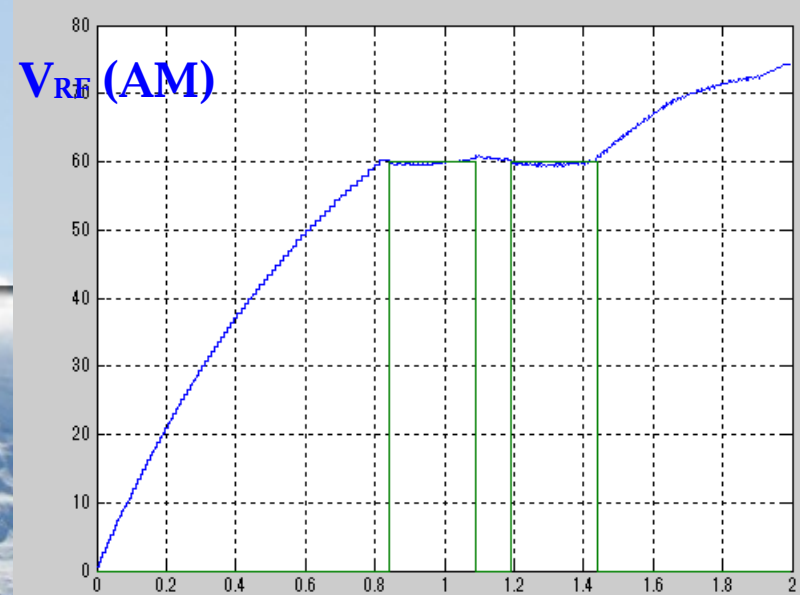
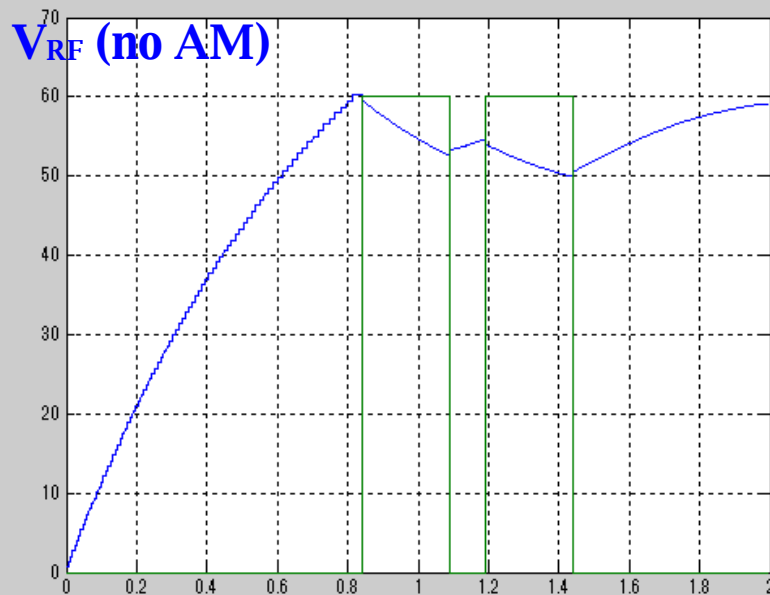
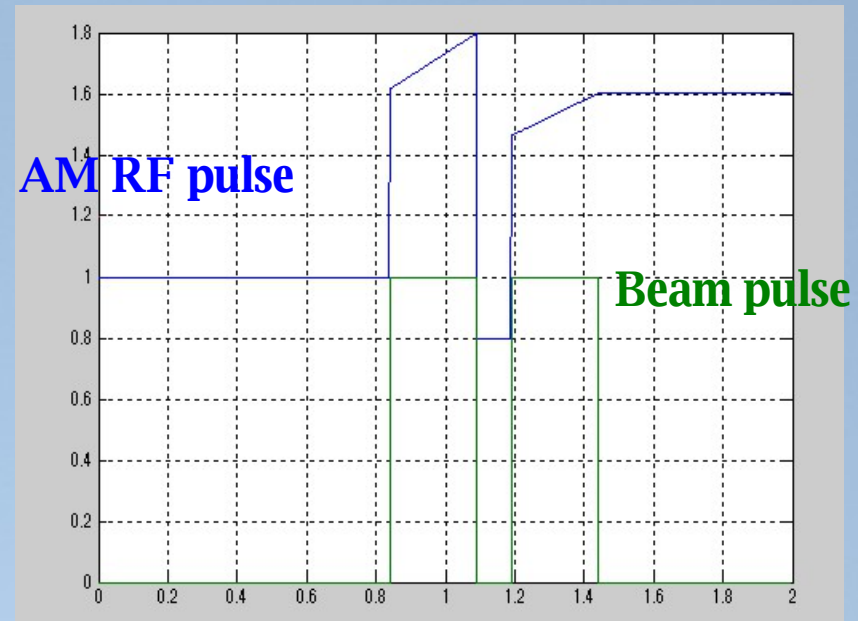
$$E_2 = \frac{r_0 I_0}{2} \frac{\omega}{Q} e^{-2\tau},$$



# Multi-Pulse Acceleration

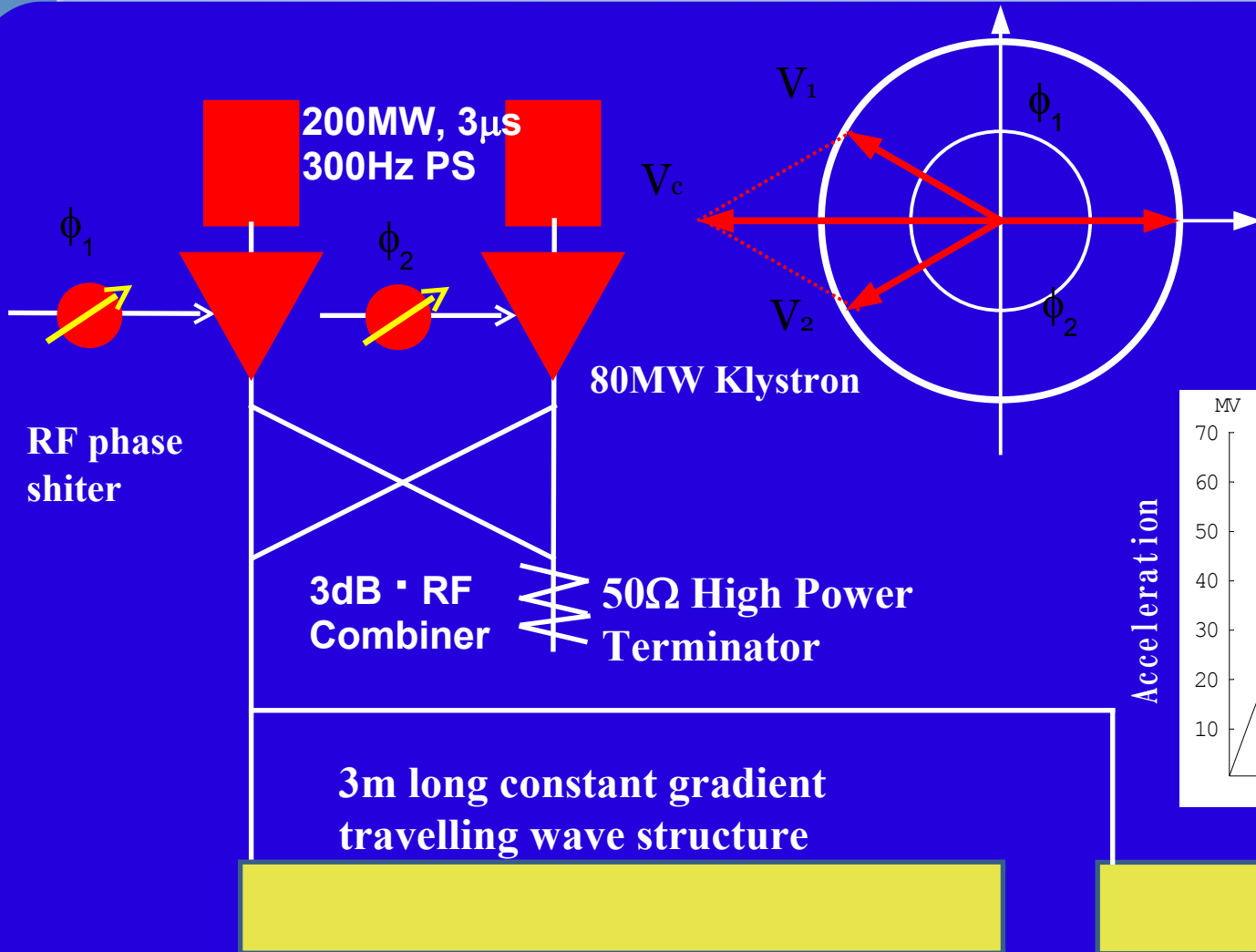
M. Satoh

- Same method can be extended to the multi-pulse case.
- AM should be applied to not only on the pulse head, but also pulse interval;

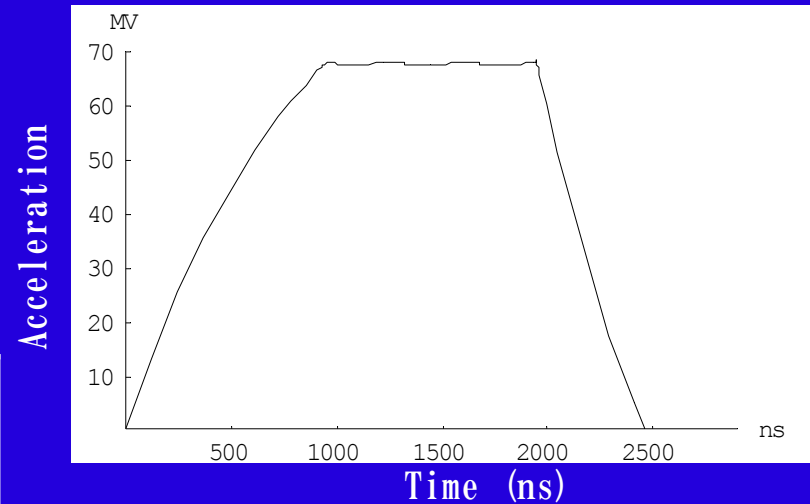




# AM by phase shift



- Amplitude is fastly controlled by phase shifter.
- FF control make the flat acceleration.

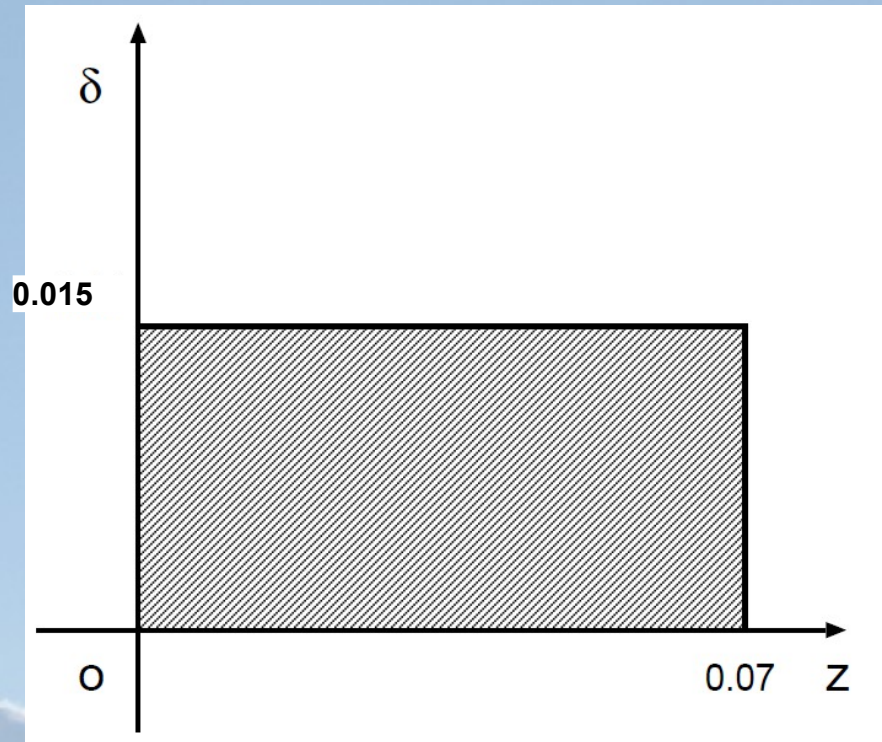


# Positron Capture Simulation

- By assuming the beamloading compensation, any loading effect is not involved.
- $e^+$  distribution was made by GEANT4.
- Tracking simulation in the injector section ( $<250\text{MeV}$ ) by GPT; AMD positron capture ( $B_0 \sim 7.0\text{T}$ ) followed by solenoid focusing section ( $0.5\text{T}$ ) with S-band Acceleration tube ( $25\text{MeV/m}$ ).
- Booster linac and EC (Energy Compressor) is treated as linear transformation.



# DR acceptance



- DR acceptance is
  - $\gamma A_x + \gamma A_y < 0.07\text{m}$
  - $dE < 1.5\%$ ,  $dz < 0.07\text{m}$  (FW)
- By considering RF acceleration in S or L-band, wider  $dE$  is desirable even with less  $dz$ .

# Phase-space Matching with EC

- EC (Energy Compressor) is a reverse process of bunch compressor.
- Bunch compressor : energy spread  $\rightarrow$  large, bunch length  $\rightarrow$  short.
- Energy compressor: energy spread  $\rightarrow$  short, bunch length  $\rightarrow$  large

## Bunch compressor

$$\begin{aligned} \begin{bmatrix} z(s) \\ \delta(s) \end{bmatrix} &= \begin{bmatrix} 1 & R_{56} \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 1 & 0 \\ R_{65} & 1 \end{bmatrix} \begin{bmatrix} z(0) \\ \delta(0) \end{bmatrix} \\ &= \begin{bmatrix} 0 & R_{56} \\ R_{65} & 1 \end{bmatrix} \begin{bmatrix} z(0) \\ \delta(0) \end{bmatrix} \end{aligned}$$

## Energy compressor

$$\begin{aligned} \begin{bmatrix} z(s) \\ \delta(s) \end{bmatrix} &= \begin{bmatrix} 1 & 0 \\ R_{65} & 1 \end{bmatrix} \begin{bmatrix} 1 & R_{56} \\ 0 & 1 \end{bmatrix} \begin{bmatrix} z(0) \\ \delta(0) \end{bmatrix} \\ &= \begin{bmatrix} 1 & R_{56} \\ R_{65} & 0 \end{bmatrix} \begin{bmatrix} z(0) \\ \delta(0) \end{bmatrix} \end{aligned}$$

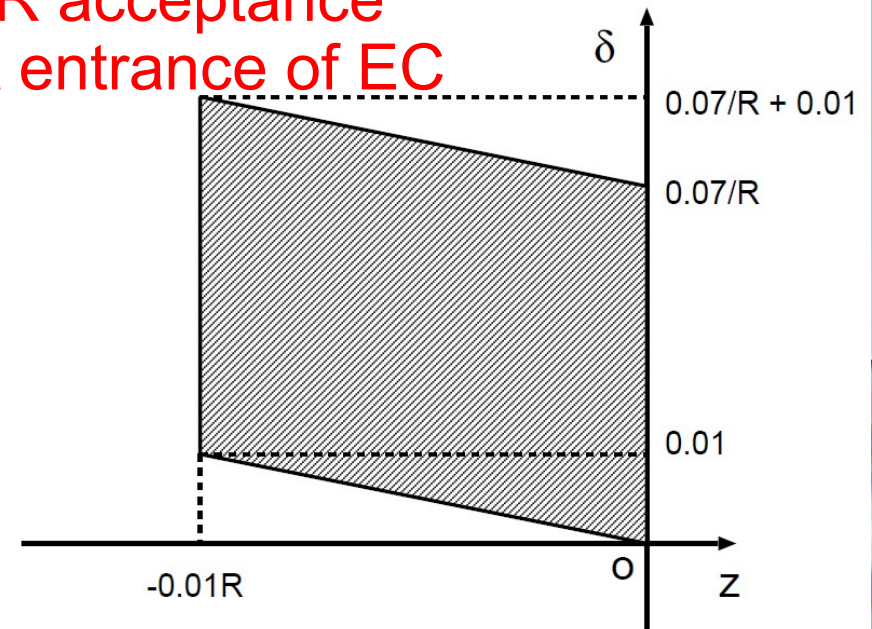
# Phase-space Matching with EC

- Transfer matrix of EC ( $R \equiv R_{56}$ ).
- $r_1$  (EC entrance) is written by  $r_2$  (EC exit).
- Effective DR acceptance is operable by EC( $R$ ).

$$M_{EC}(R) = \begin{bmatrix} 1 & R \\ -1/R & 1 \end{bmatrix}$$

$$r_1 = \begin{bmatrix} 1 & R \\ -1/R & 1 \end{bmatrix}^{-1} r_2 = \begin{bmatrix} -R\delta \\ \frac{z}{R} + \delta \end{bmatrix}$$

DR acceptance  
at entrance of EC



# Optimization

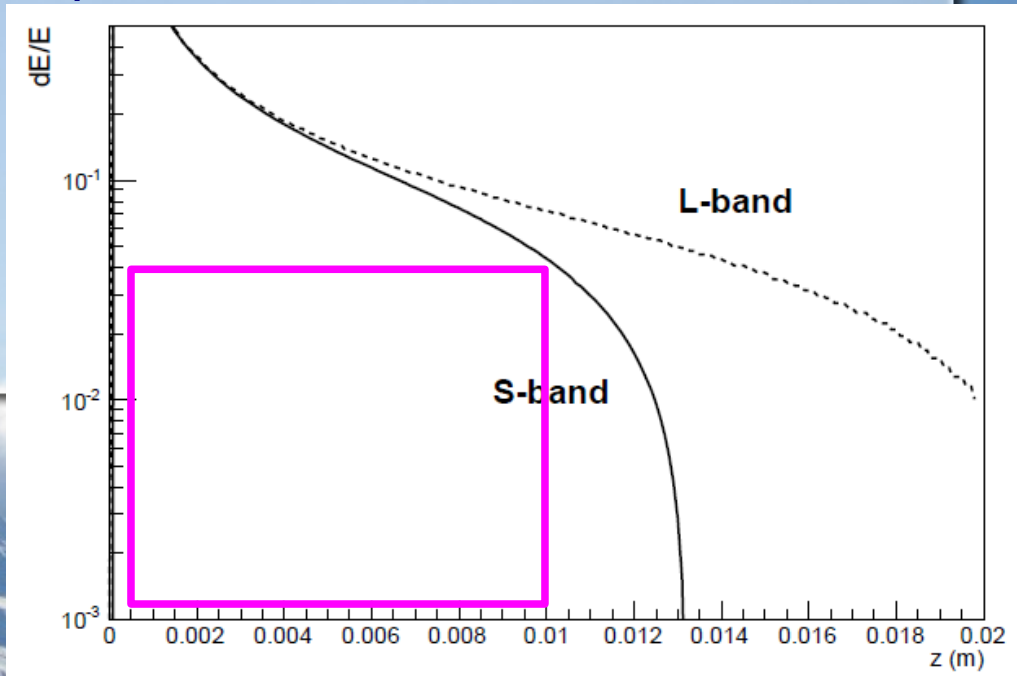
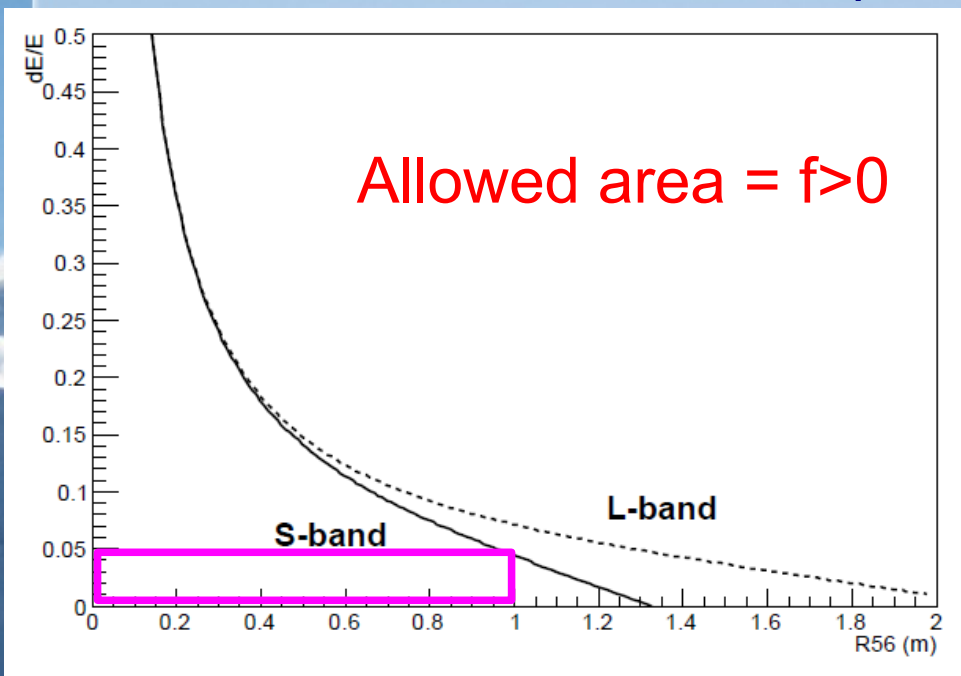
dE by RF

DR acceptance

$$1 - \cos\left(\omega \frac{0.015R}{2c}\right) + \delta < \frac{0.07}{R} + 0.015$$

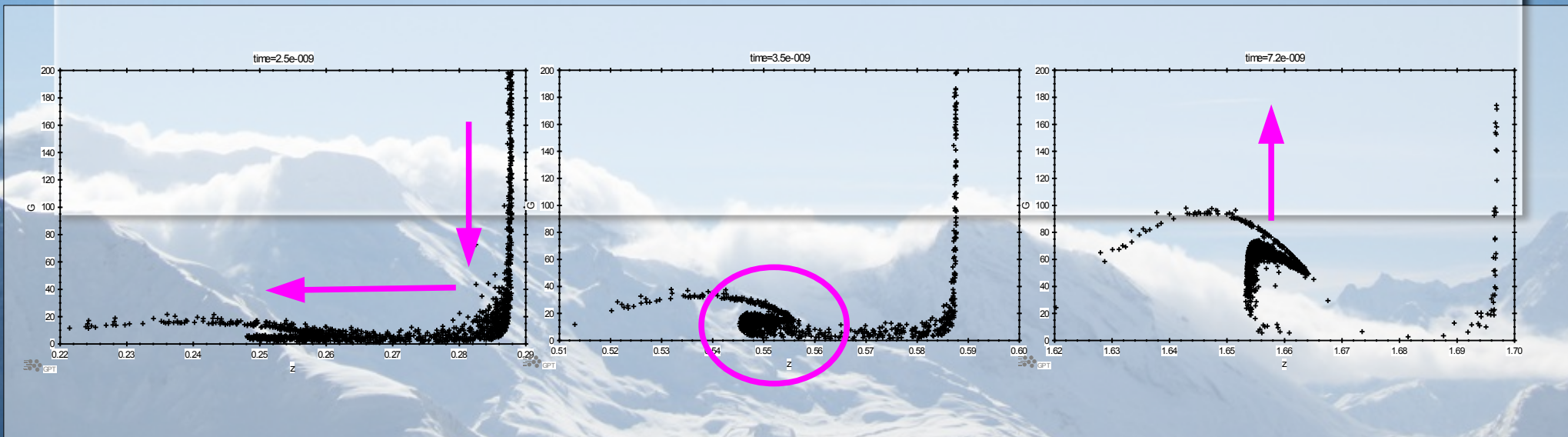
Initial dE

$$f(R) = \frac{0.07}{R} + 0.015 - 1 + \cos\left(\omega \frac{0.015R}{2c}\right)$$



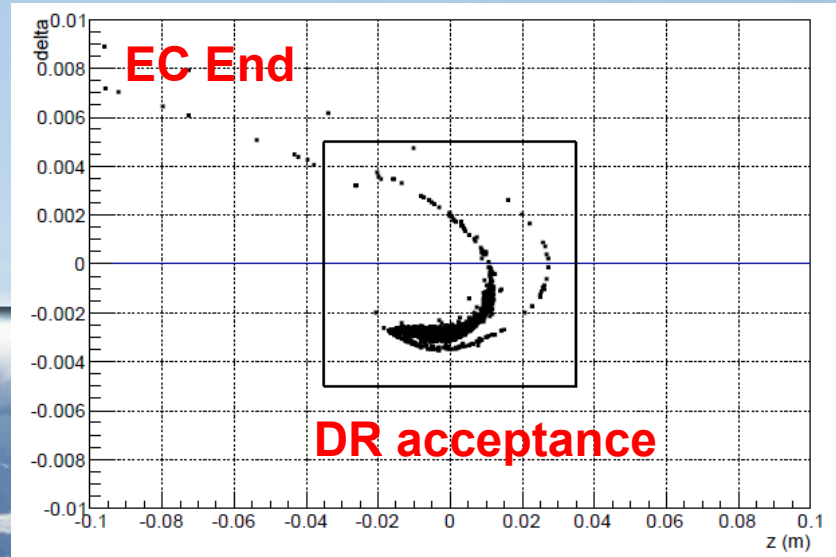
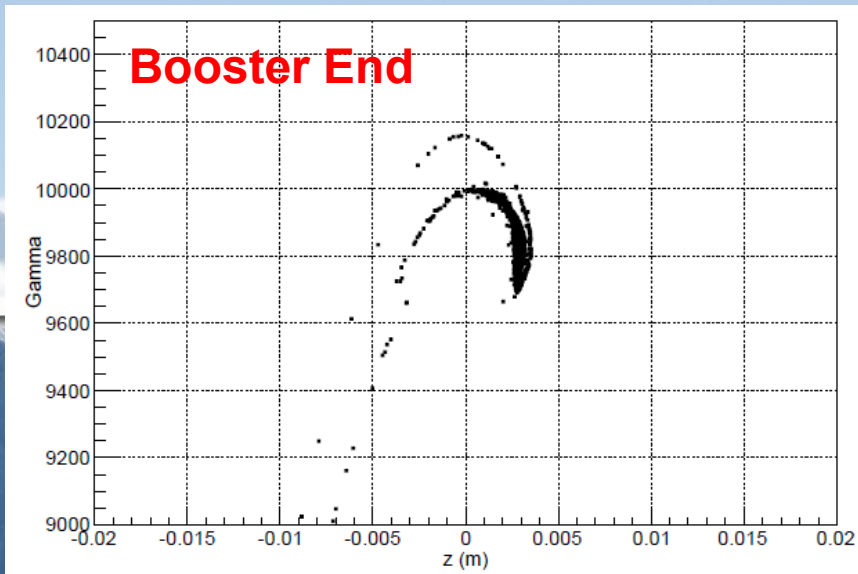
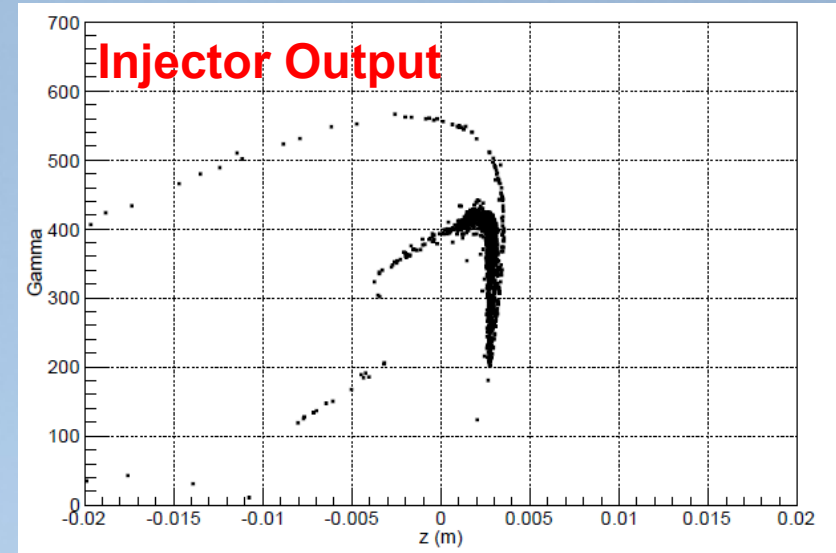
# Deceleration Capture

- The positron peak is on deceleration phase.
- These positrons are slipped down to the acceleration phase where these positrons are captured.
- Slight enhancement on the capture efficiency, and less longitudinal emittance (z-d).



# $\delta$ -z phase-space

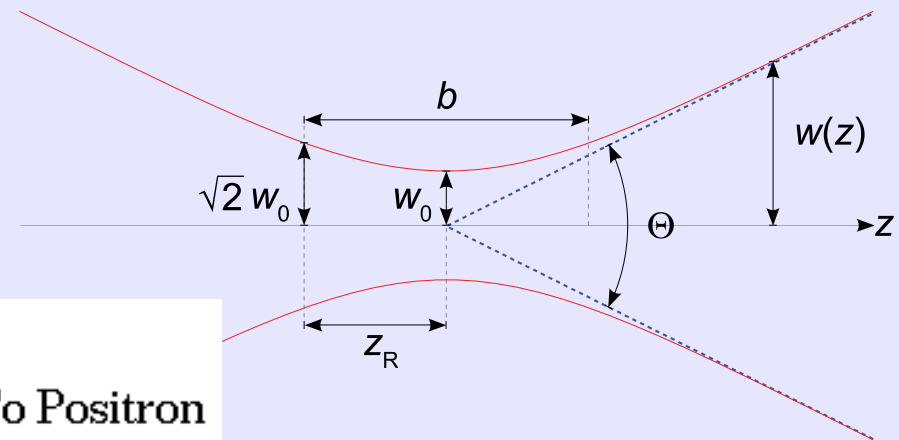
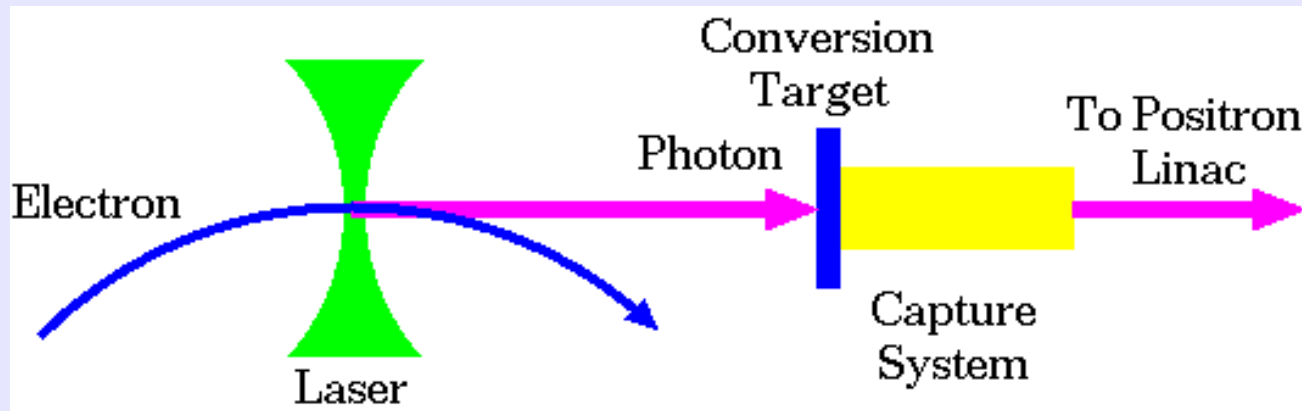
- 1000 electrons on target.
- $>8000$  positrons are generated.
- 1100 positrons accepted by DR.
- The yield is 1.1 ( $e^+/e^-$ ).
- 1.5 is likely to be realized by optimization.





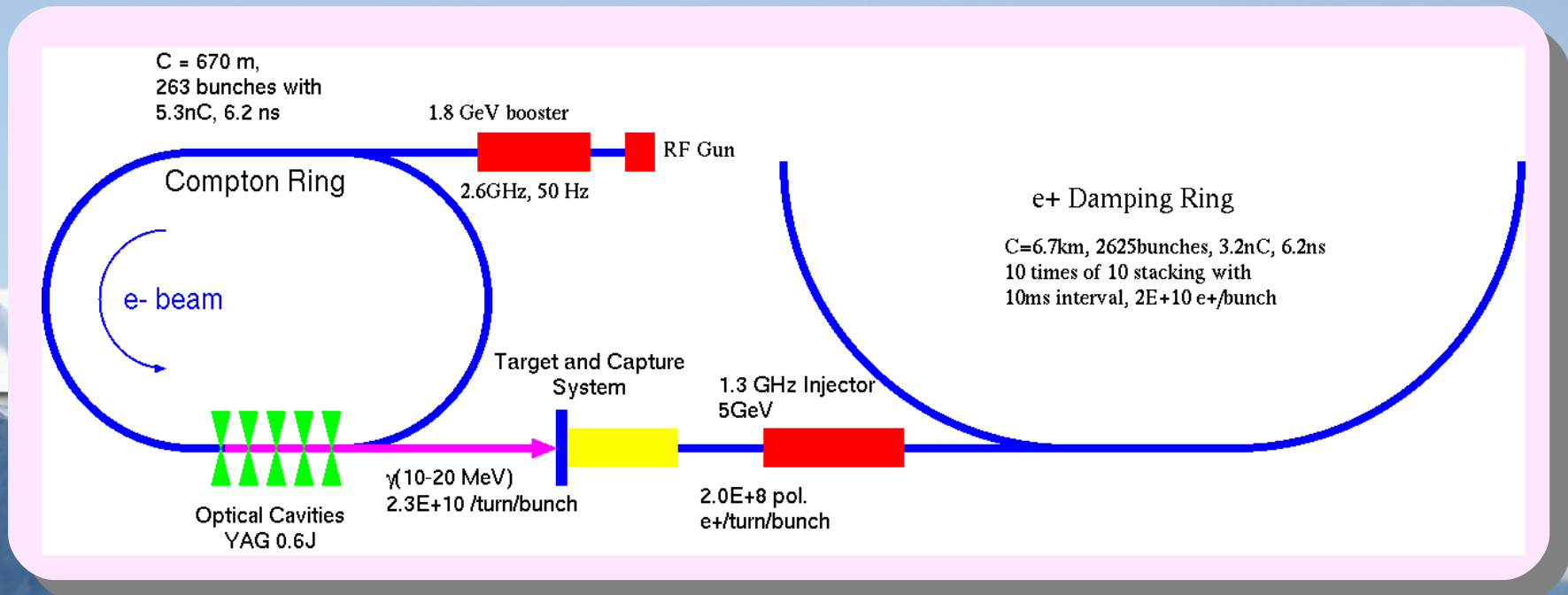
# Laser Compton Scheme

- The required electron energy is a few GeV and a dedicated electron driver is reasonable.
- But it is a technical challenge to obtain an enough amount of  $e^+$  for LC, because length of “Laser undulator” is limited to be Rayleigh length.

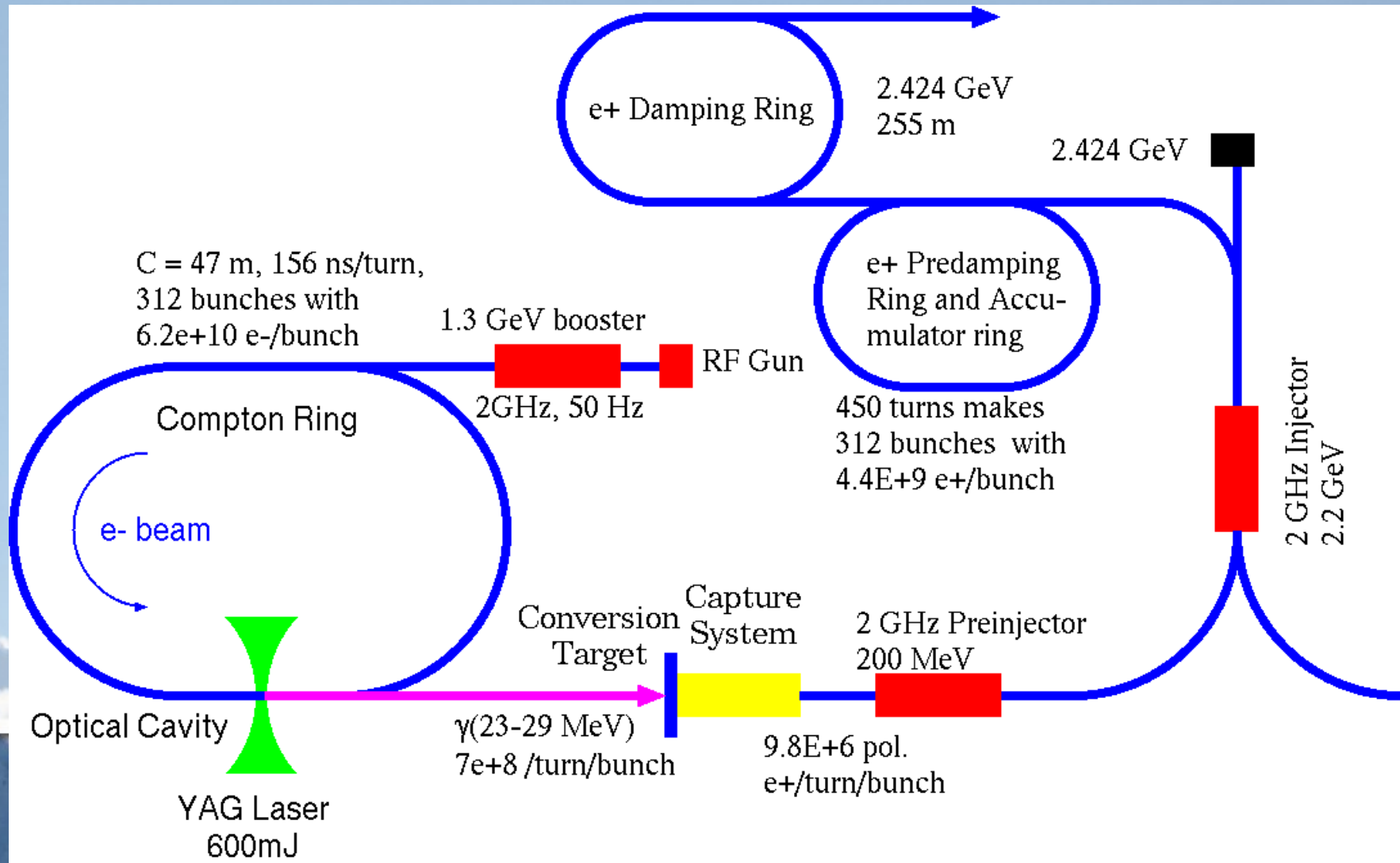


# Compton Ring

- A storage ring for electron driver: 5.3nC, 6.2ns, 1ps, 1.8GeV.
- Laser pulse is stored in optical cavity, 0.6Jx5.
- Positron bunch ( $\text{Ne}^+$ :  $2.0\text{E}+8$ ) is generated.
- 10 bunches are stacked on a same bucket. This process is repeated 10 times with 10ms interval for beam cooling.
- Finally,  $\text{Ne}^+$ :  $2\text{E}+10$  is obtained.



# CLIC Compton Scheme

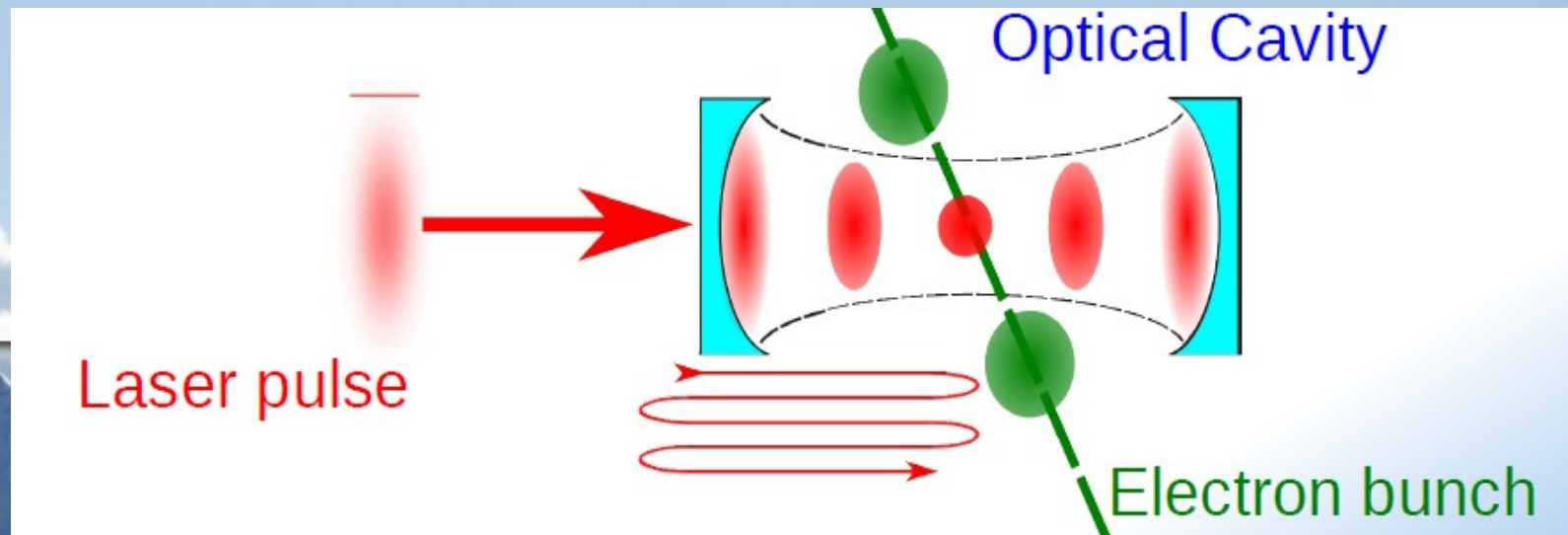


# Pulse Stacking Cavity

- Many laser pulses are stored and the power is enhanced by the pulse stacking.
- Pulsed laser is stacked when appropriate conditions of the external cavity are satisfied simultaneously for
  - Laser wave length
  - Mode-locking frequency

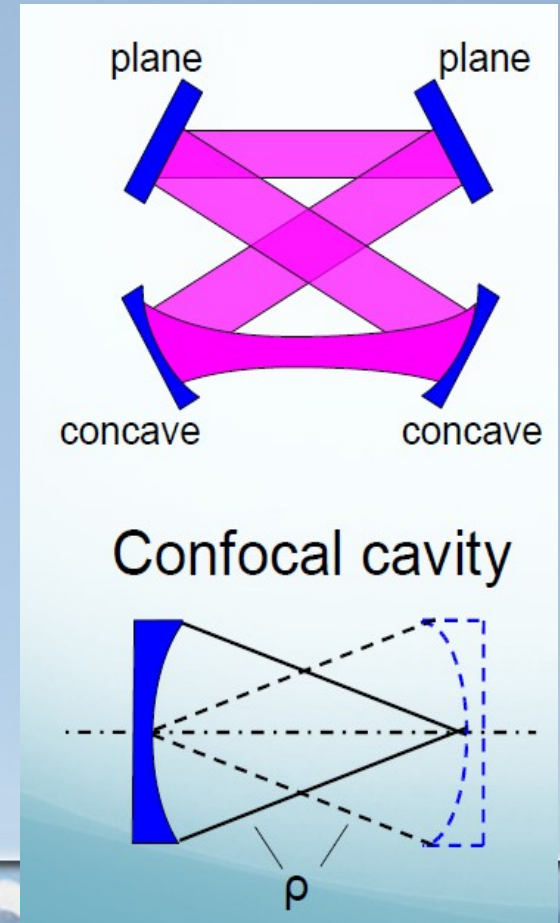
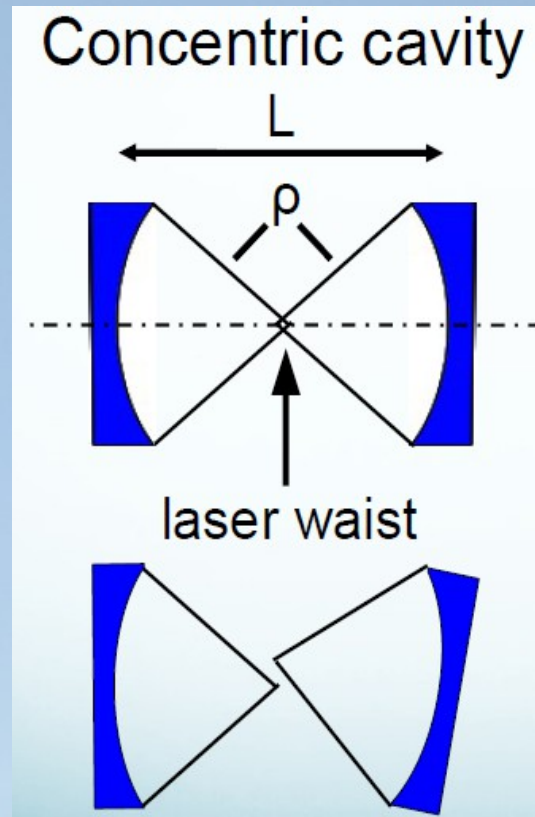
$$L_{cav} = m \frac{\lambda}{2}$$

$$L_{cav} = n L_{rep}$$



# How many mirrors?

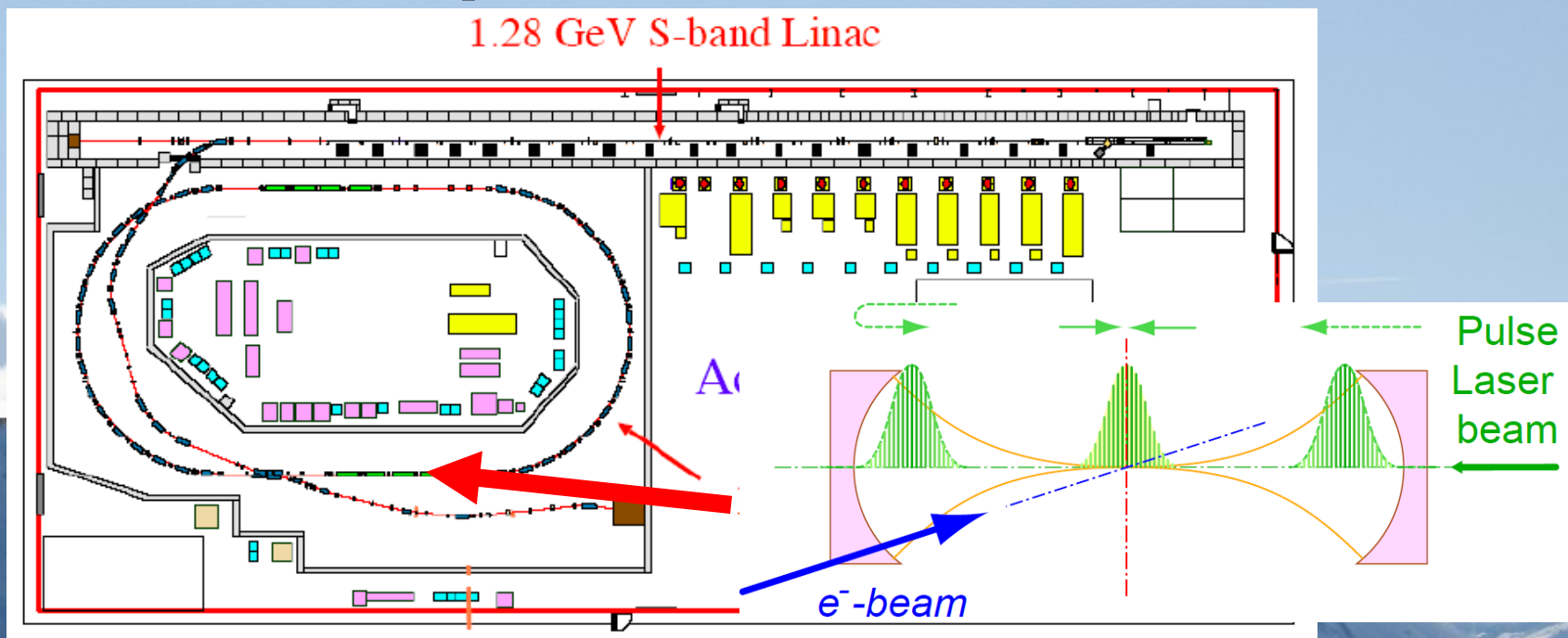
- 2 mirrors:
  - Simple,
  - unstable due to concentric geometry,
- 4 mirrors:
  - Complicated,
  - stable due to confocal geometry,



# KEK-ATF experiment (1)

Hiroshima-Waseda-KEK

- ▶ Pulse train from 10 W YAG:VAN 357 Mhz mode-lock laser is stored in an optical cavity.
- ▶  $L_{\text{cav}}=420$  mm, crossing angle 12 deg.
- ▶  $R=99.7\%$ , 1000 finesse.
- ▶  $2\sigma=60\mu\text{m}$ .
- ▶ Laser-Compton collision with stored electron beam.



# Fibre Laser (1)

- ▶ Double clad-core optical fiber.
- ▶ InGaAs LD (940nm) is for pumping.
- ▶ Typical core size is 6 – 40  $\mu\text{m}$ .
- ▶ It is an ideal laser for high power operation.

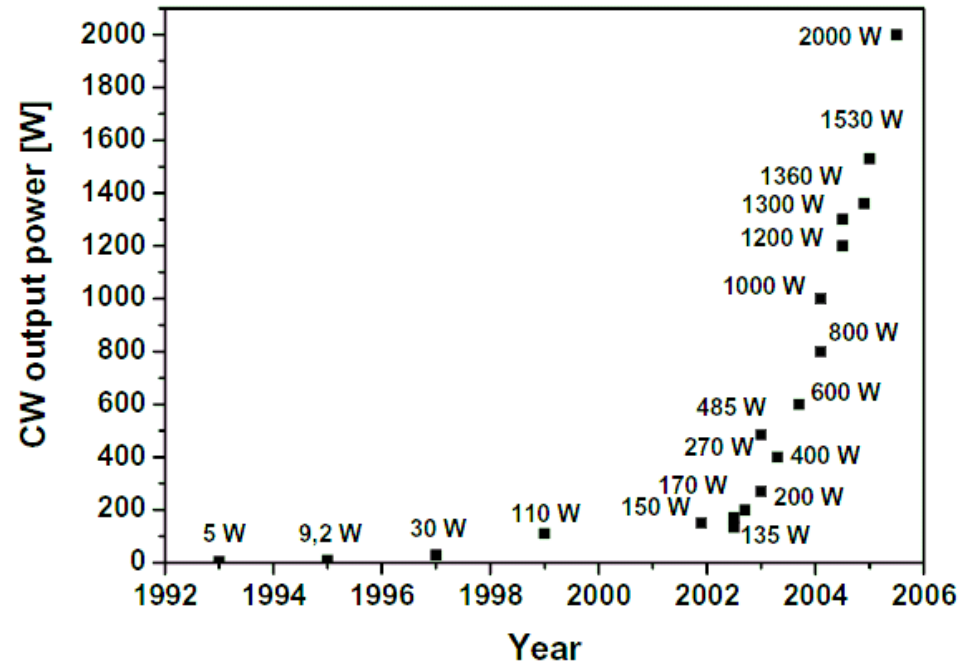
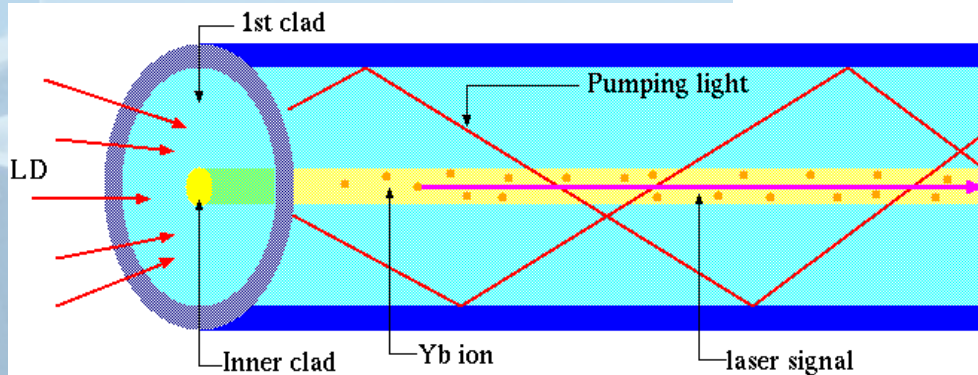


Fig. 4: Power evolution of cw double-clad fiber lasers with diffraction-limited beam quality over the last decade

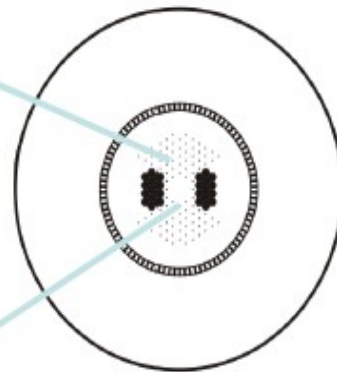
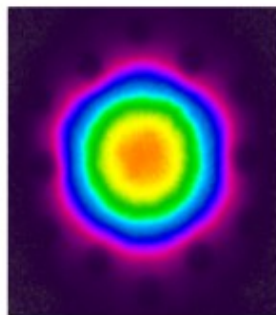
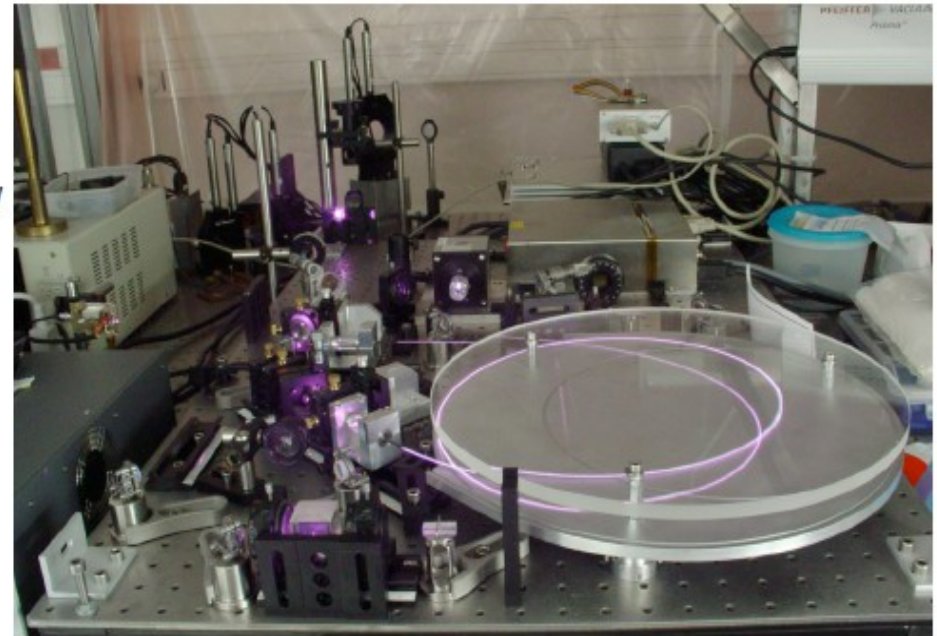
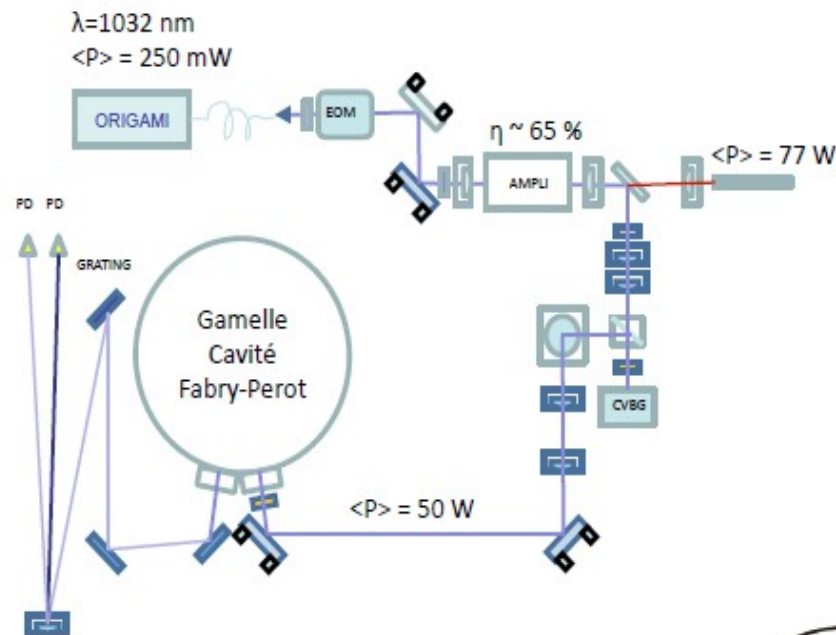


J. Limpert



By M. Hanna

# Fibre Laser (2)

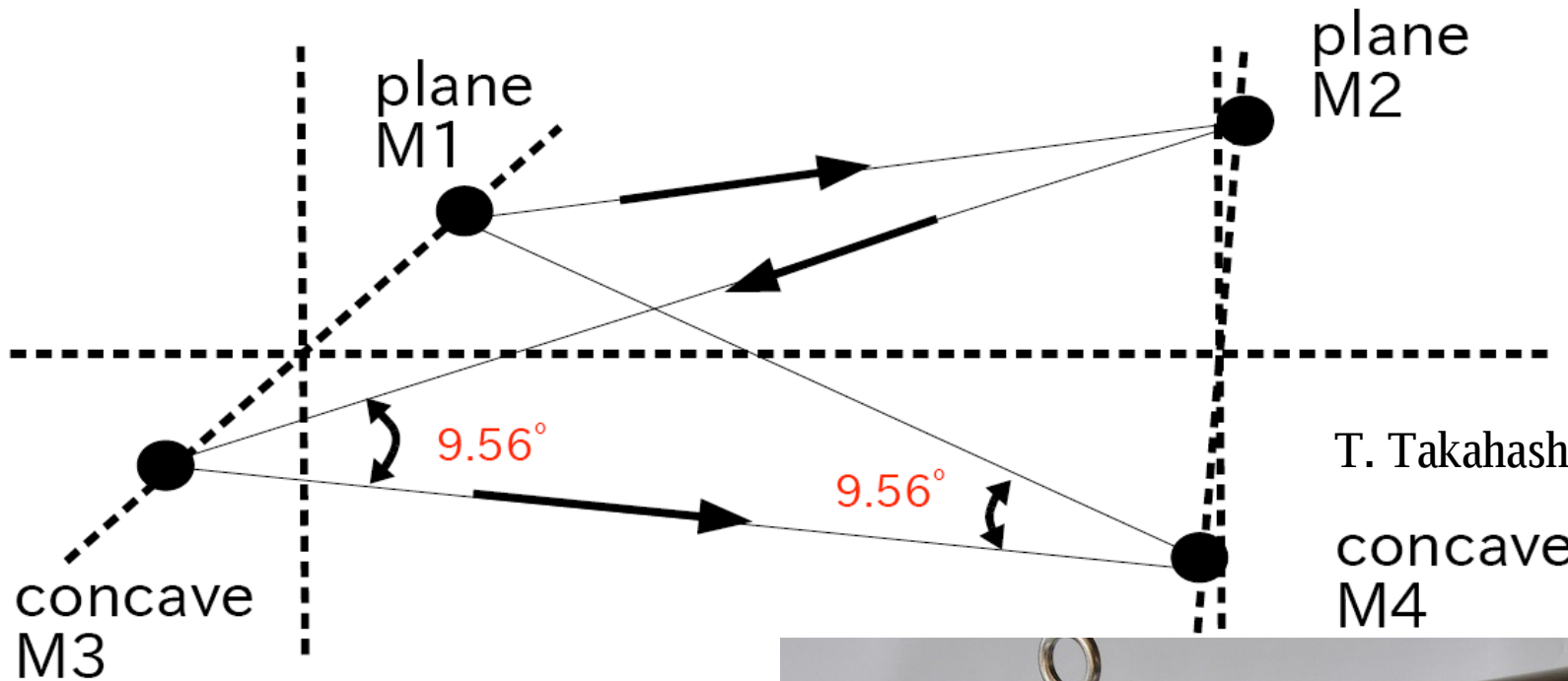


$\varnothing \text{ core} = 40 \mu\text{m}$   
 $\varnothing \text{ cladding} = 200 \mu\text{m}$

We obtained 200W but spot was not stable  
 We fix the power to 50-60W to get stable laser beam

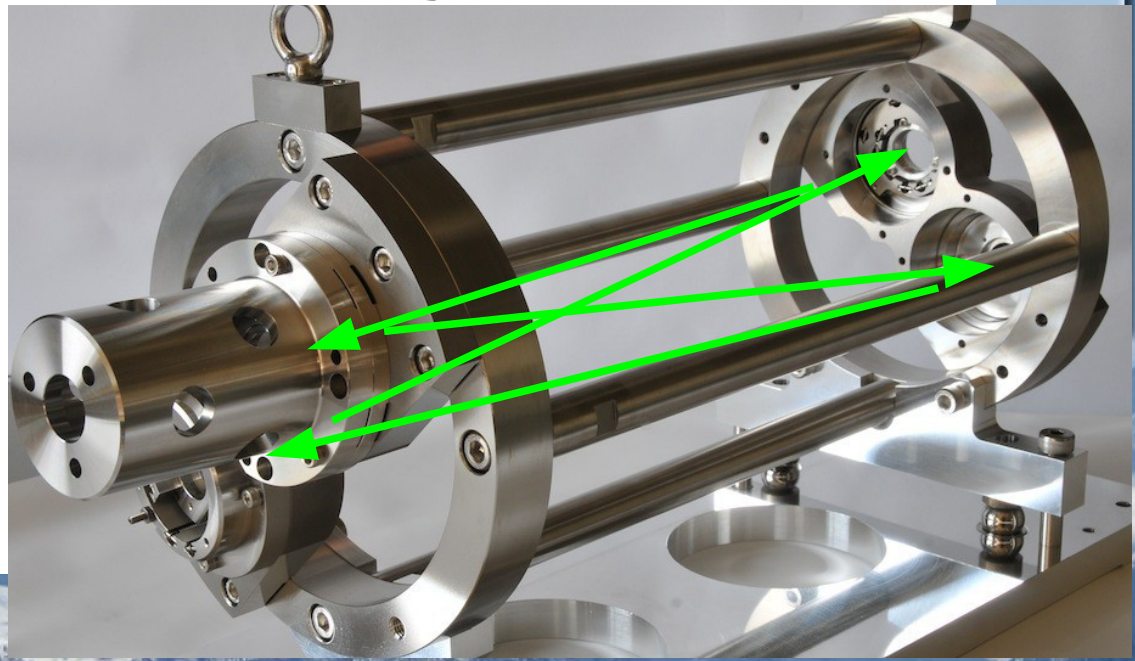


# New 4 mirror cavity



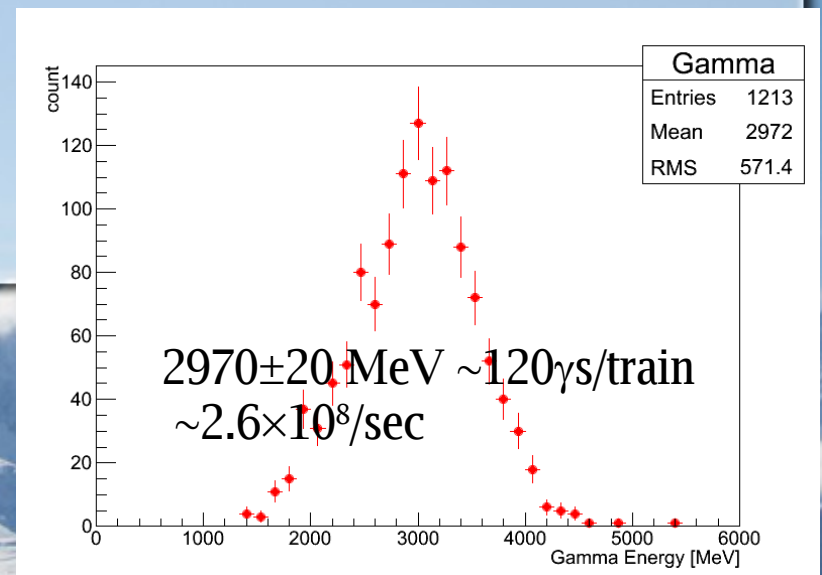
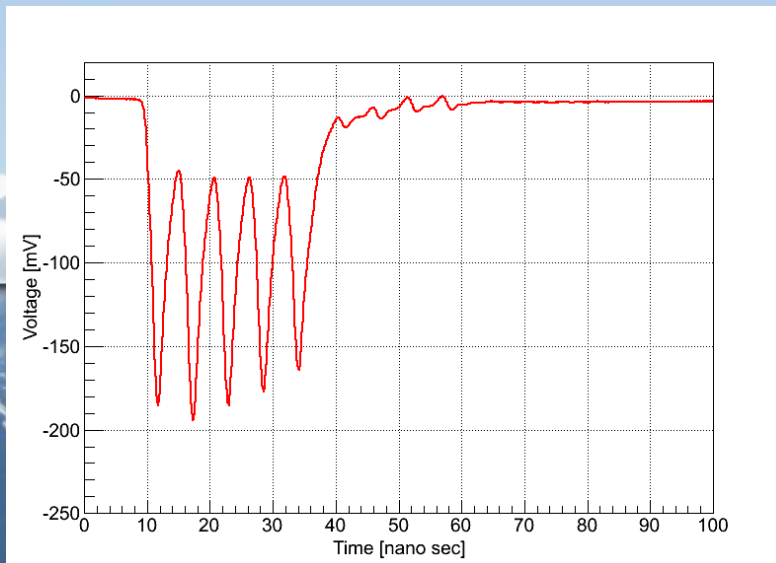
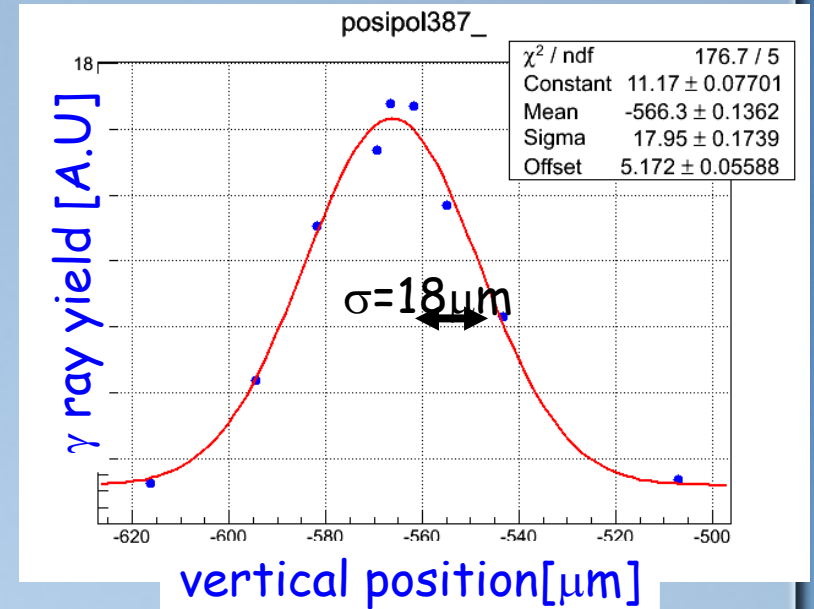
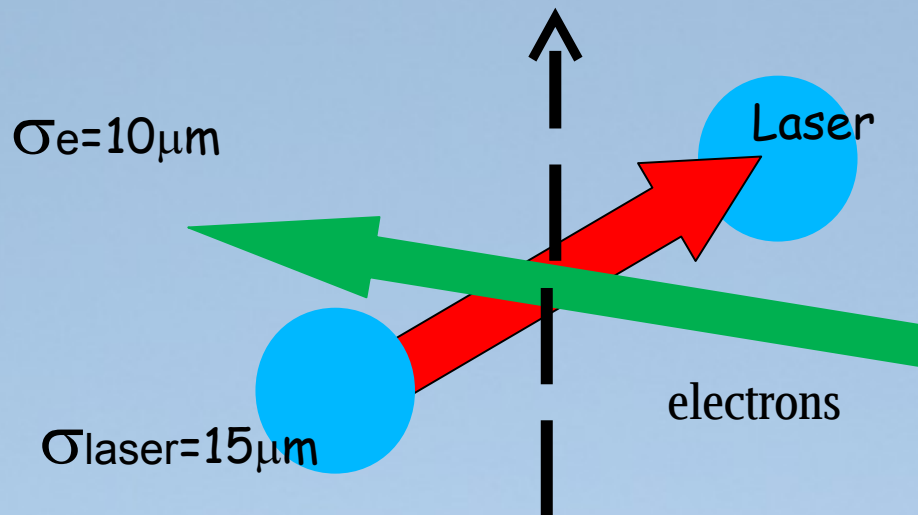
T. Takahashi(Posipol2012)

- $L1 = M1 - M2 = 420\text{mm}$
- $L2 = M2 - M3 = 420\text{mm}$
- $L3 = M3 - M4 = 420\text{mm}$
- $L4 = M4 - M1 = 420\text{mm}$



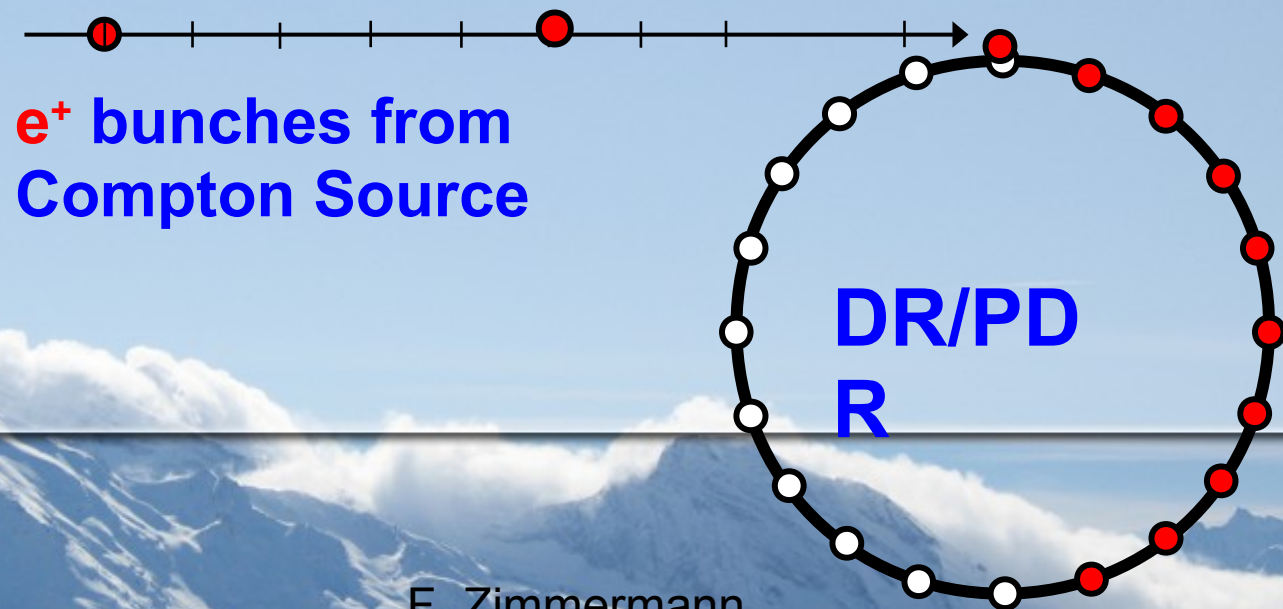
# $\gamma$ ray Generation at ATF

T. Takahashi(Posipol2012)



# Positron Stacking (1)

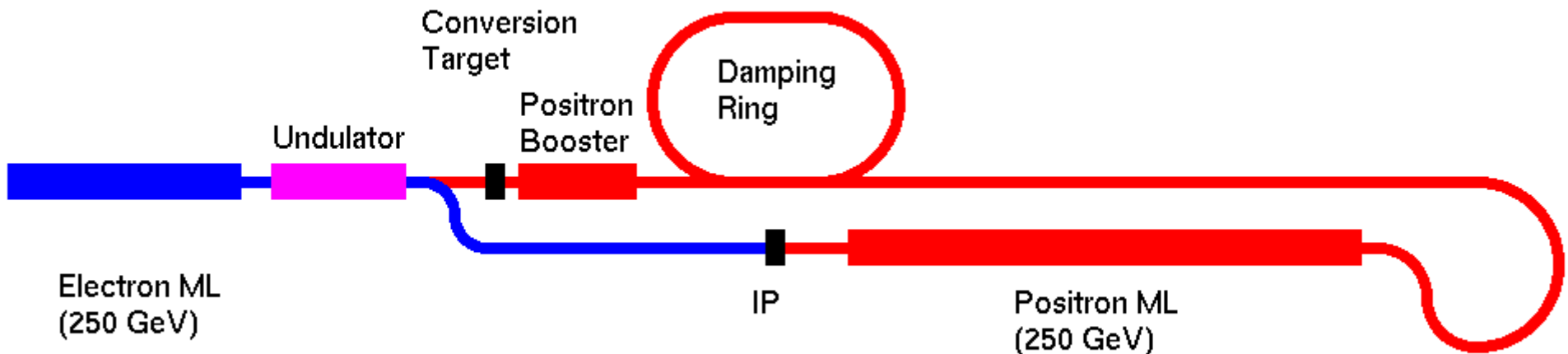
- Except linac scheme, # of positron by a single collision is not sufficient.
- We need accumulate positrons from many collisions to achieve the required bunch intensity for ILC and CLIC.
- Positron stacking: many positron bunches are injected to a same bucket in DR/PDR.



F. Zimmermann

# Positron Source another staging approach

- Staging approach to minimize technical risks and maximize physics potential.
  - 1<sup>st</sup> stage : Unpolarized e-driven e+ source .  
(no polarizatio, but “conventional”)
  - 2<sup>nd</sup> stage: Undulator e+ source. (polarized, but totally new)



# Comparison

	Electron driven	Undulator	Laser Compton
<b>Electron Driver</b>	3.0-6.0 GeV NC Dedicated	150-250GeV SC Common, alternate	1.8 GeV Ring/ERL Dedicated
<b>Radiator</b>	W-Re target	Undulator $\lambda=0.8\text{cm}$	Laser $\lambda=1.0\mu\text{m}$
<b>Converter</b>	W-Re target 1 m/s	Ti-alloy 100 m/s	W target 1 m/s
<b>Matching Device</b>	SC DC solenoid/Pulsed FC	QWT/Pulsed FC	SC DC solenoid
<b>E+ booster</b>	NC	SC	SC
<b>Path length adjustment</b>	NO	YES	NO
<b>Polarization</b>	NO	30-60%	0-90%

# Summary

- Fundamentals of positron generation are explained .
- ILC Positron Source
  - Undulator Scheme is the baseline.
  - Electron driven is a promising technical backup.
  - Laser Compton is still challenging.
- A technical demonstration of the undulator system is not practically difficult.
- To maximize the technical feasibility and minimize the possible risks, a staging approach is desirable.