



# Sub-Micrometre Resolution Transverse Electron Beam Size Diagnostics Using Spatial Properties of OTR Point Spread Function

**R. Ainsworth, T. Aumeyr, S. T. Boogert, P. Karataev, K. Kruchinin, L. Nevay**

John Adams Institute at Royal Holloway

**A. Aryshev, M. Shevelev, N. Terunuma, J. Urakawa**

KEK

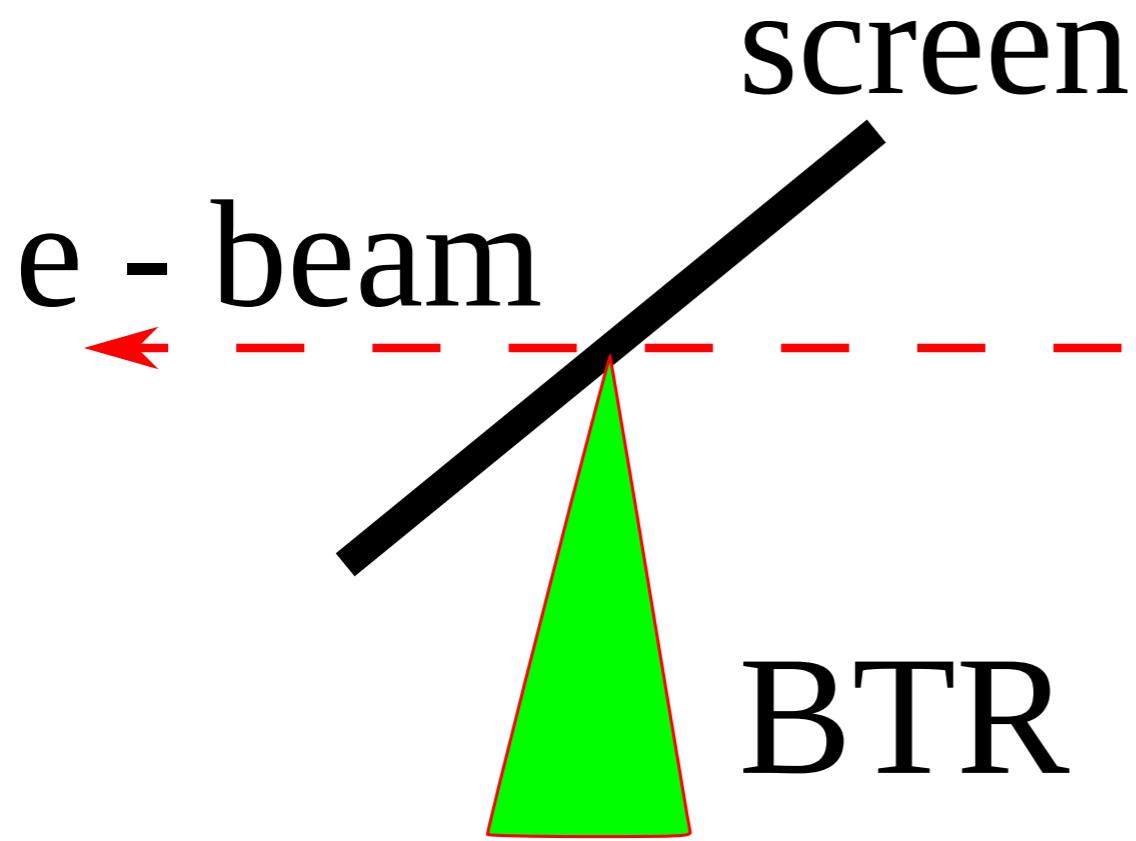
**B. Bolzon, T. Lefevre, S. Mazzoni**

CERN

# OUTLINE

- Introduction
- Experimental setup
- Calibration
- Quad Scan
- Window size
- Summary

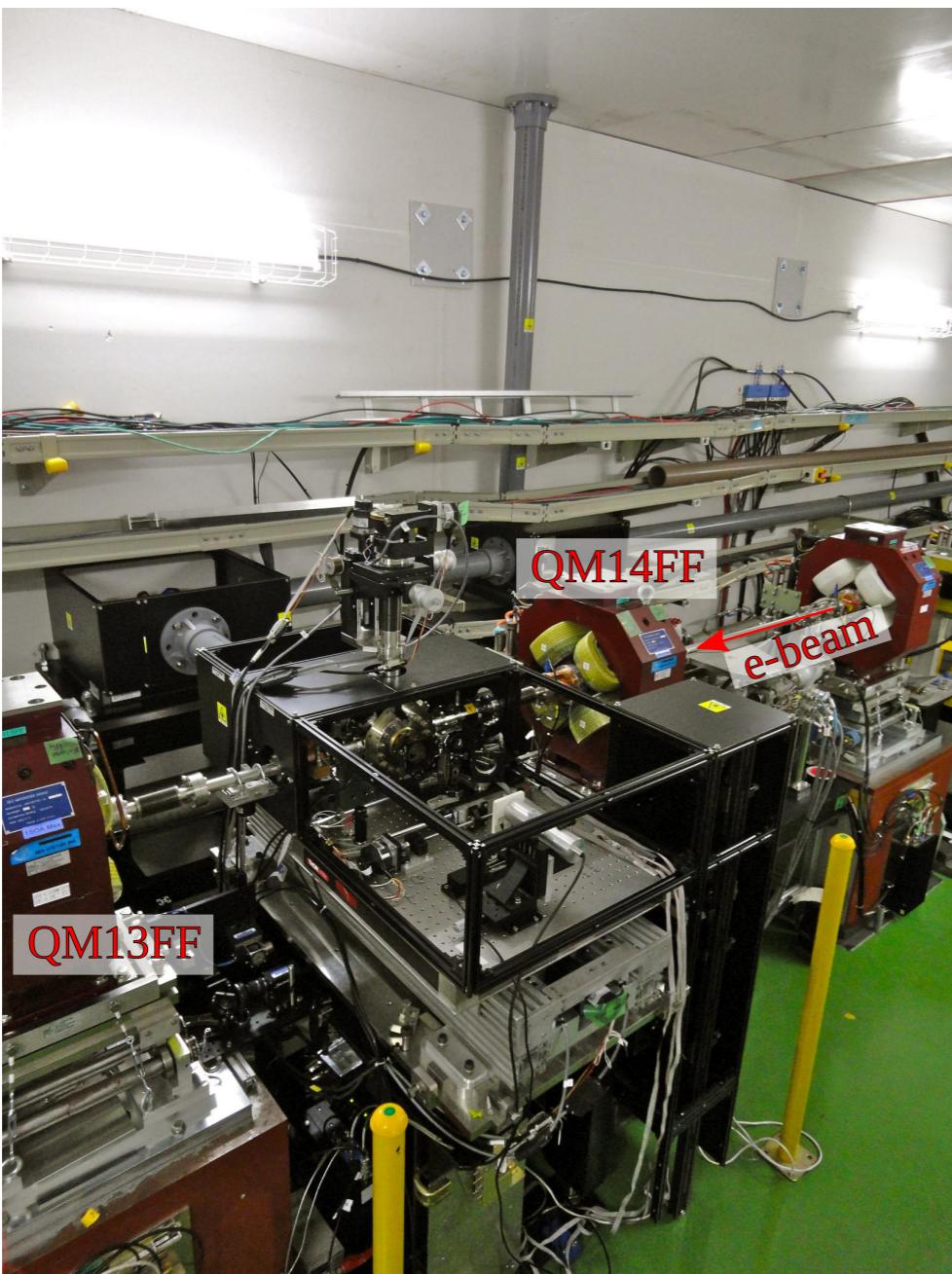
# OTR



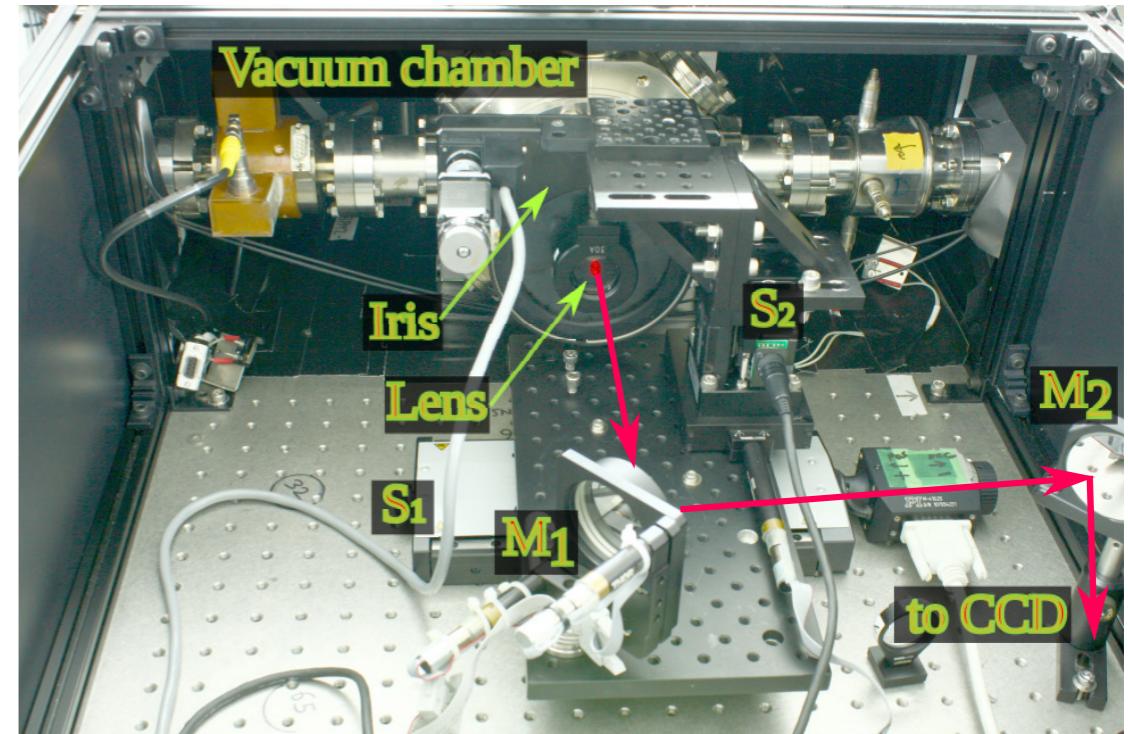
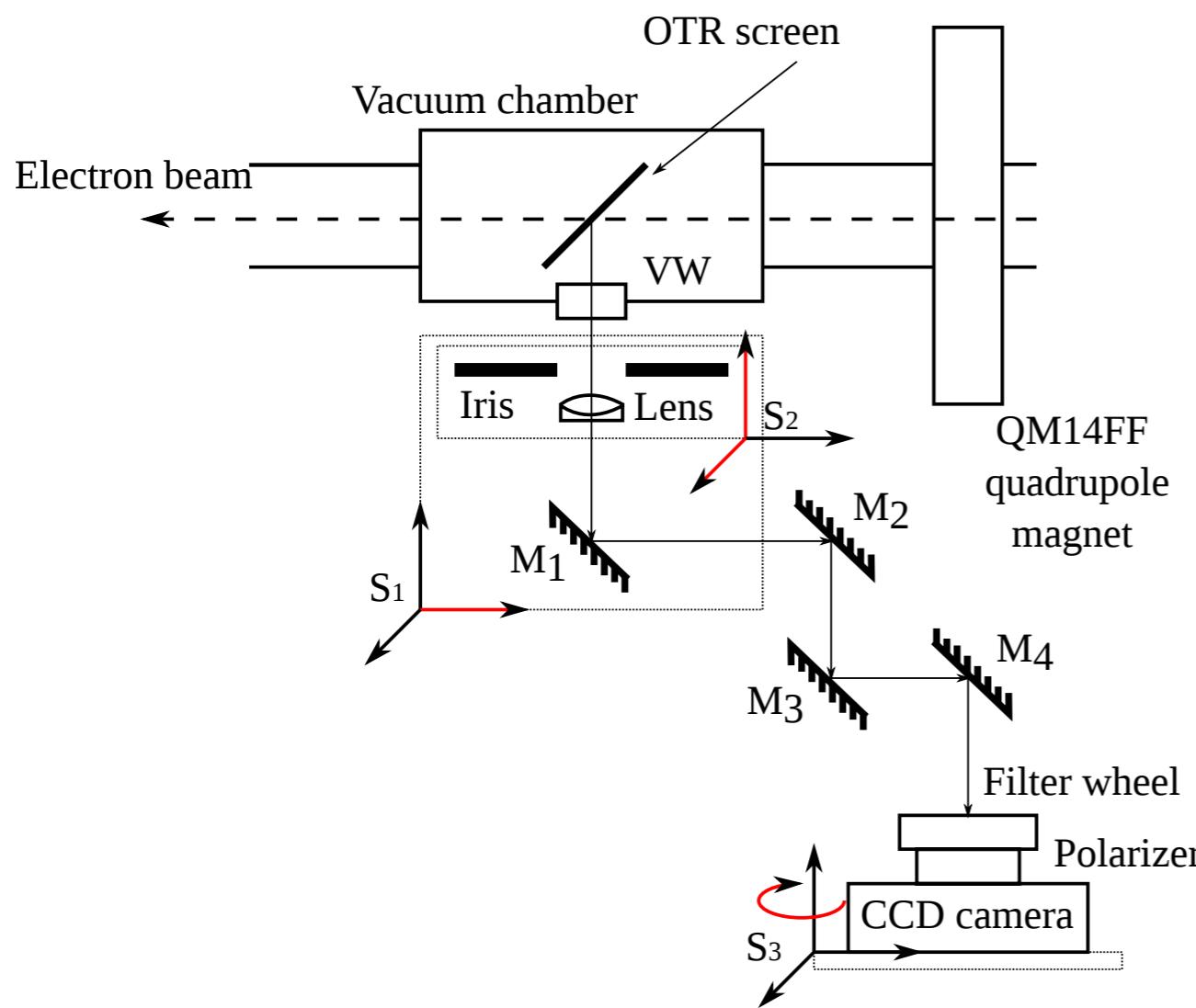
Transition radiation (TR) appears when a charged particle crosses a boundary between two media with different dielectric constants.

The resolution is determined by the source dimensions induced by a single particle plus distortion caused by the optical system (diffraction of OTR tails)

# ATF2 EXTRACTION LINE

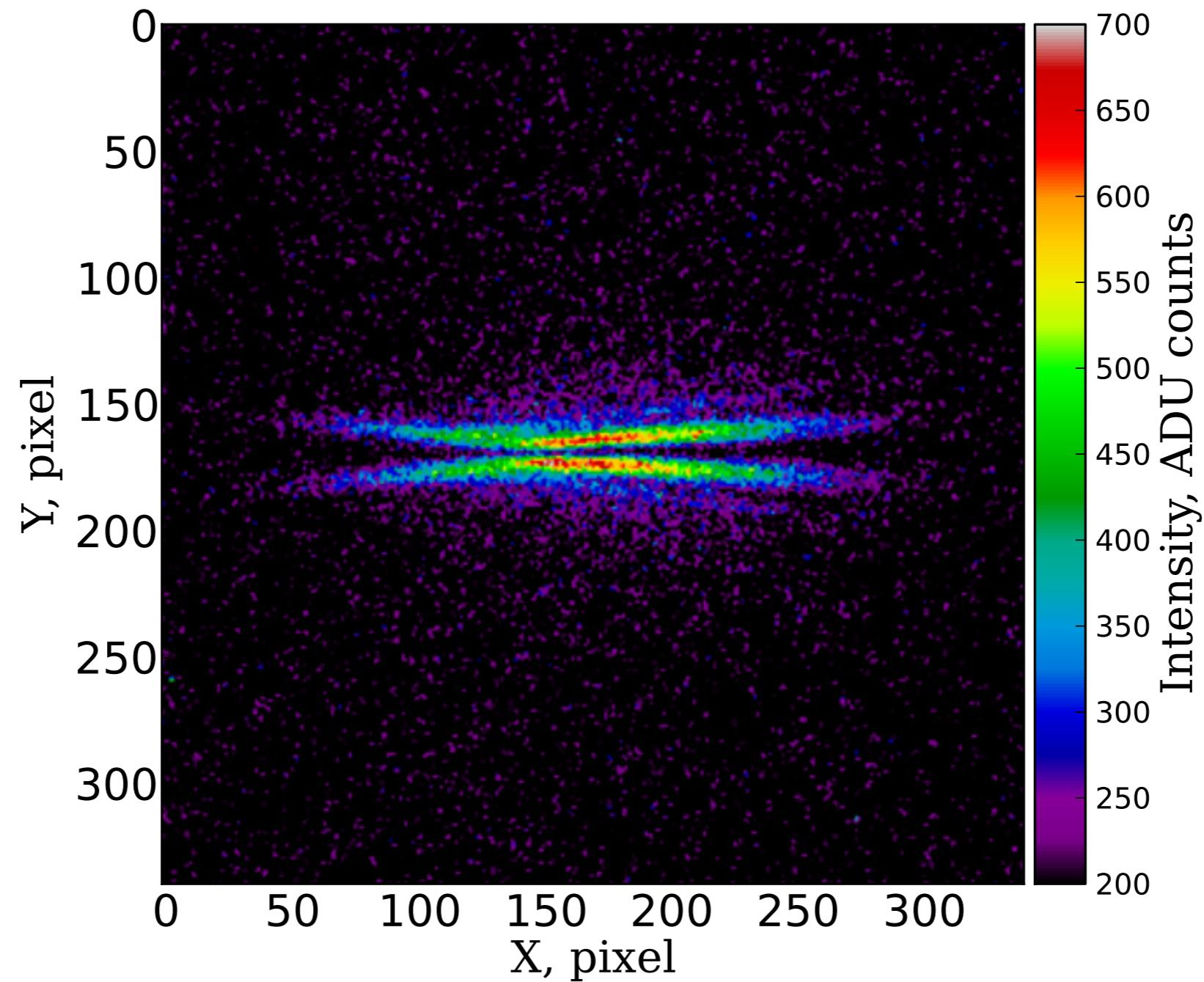


# EXPERIMENTAL SETUP

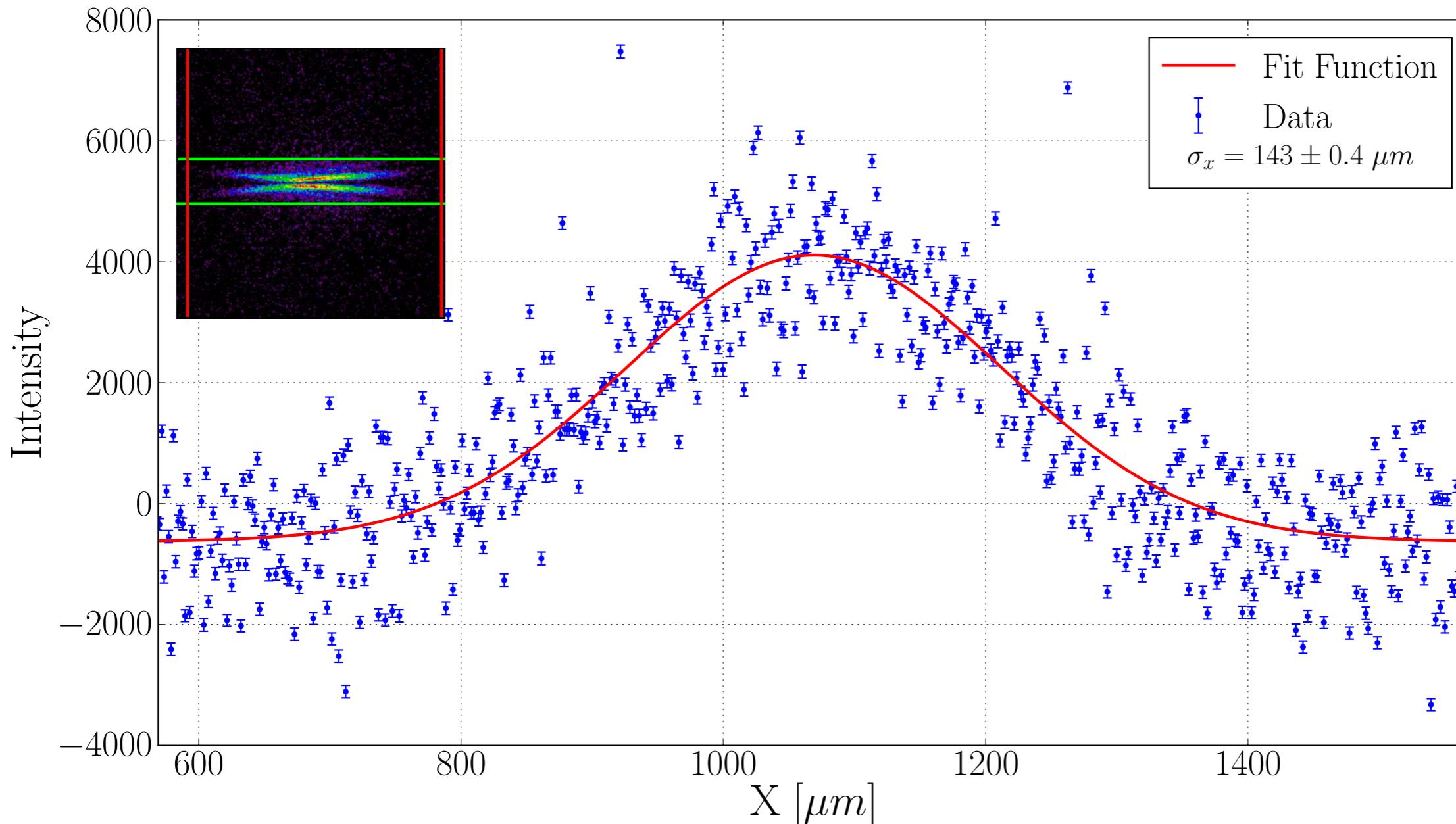


CCD Camera - SBIG-ST8300M with  $5.4 \mu\text{m}$  pixel size,  $3352 \times 2532$  pixel array and  $\sim 50\%$  quantum efficiency

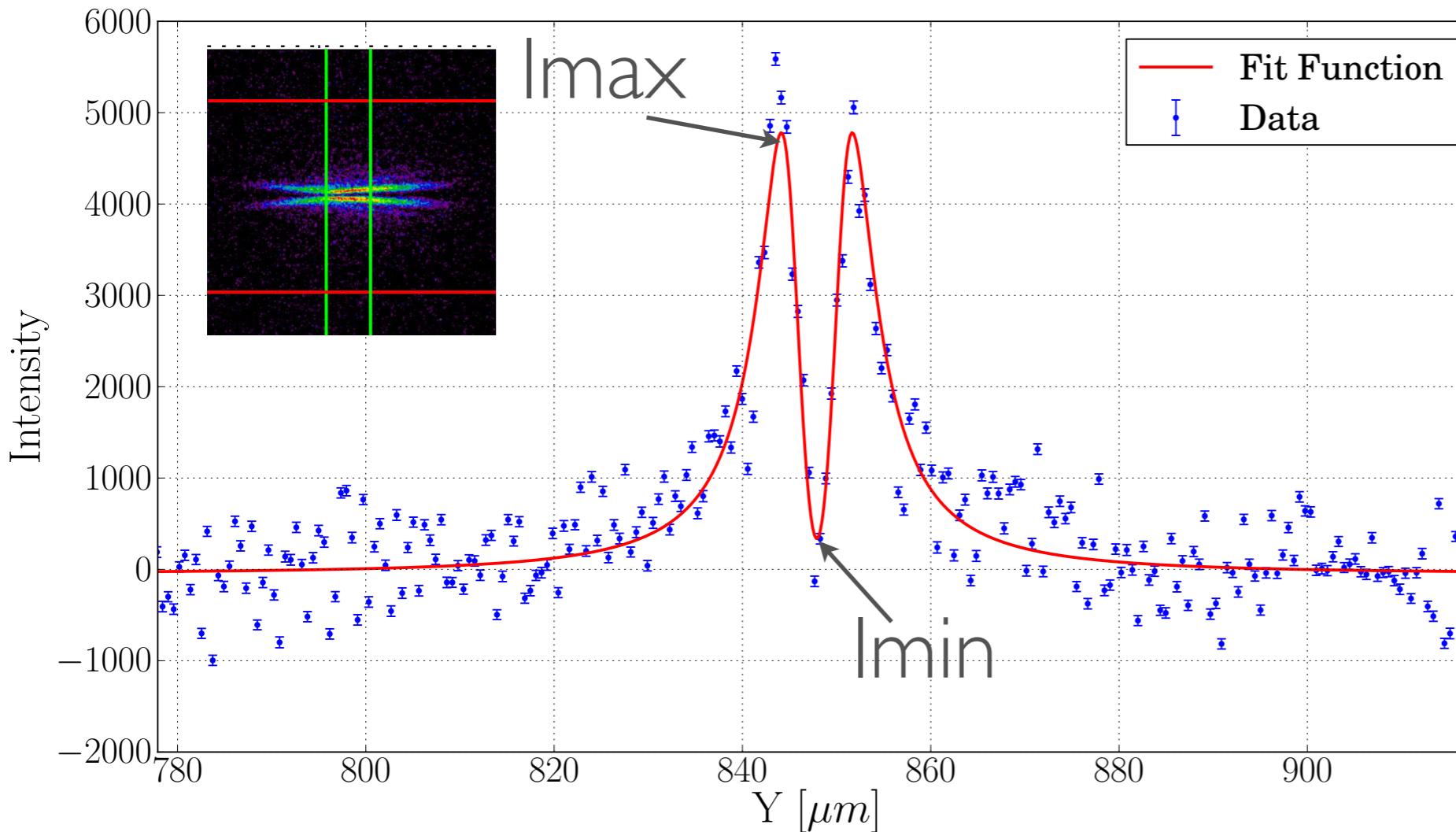
# OTR IMAGE



# HORIZONTAL PROJECTION



# VERTICAL PROJECTION



- $a_0$  is the vertical offset of the distribution with respect to zero
- $a_1$  is the amplitude of the distribution
- $a_2$  is the smoothing parameter
- $a_3$  is the horizontal offset of the distribution with respect to zero
- $a_4$  is the distribution width

$$f(x) = a_0 + \frac{a_1 (a_4 + (x - a_3)^2)}{1 + (a_2(x - a_3))^4}$$

# PSF-LIKE FIT FUNCTION

Contrast ratio

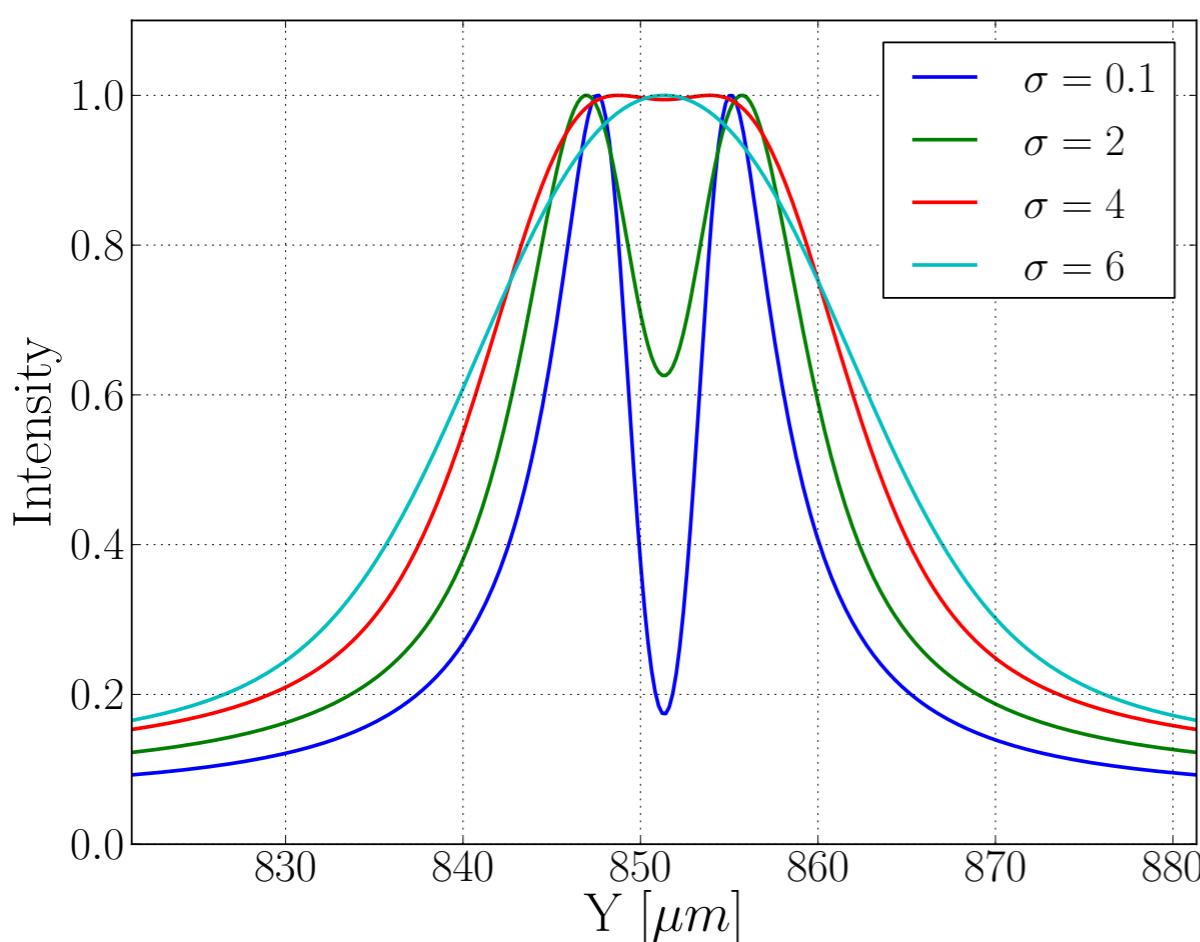
$$\frac{I_{\min}}{I_{\max}} = \frac{2a_2^2 a_4}{a_2^2 a_4 + \sqrt{1 + a_2^4 a_4^2}}$$

Distance between peaks

$$\frac{2\sqrt{-a_2^2 a_4 + \sqrt{1 + a_2^4 a_4^2}}}{a_2}$$

# SELF-CALIBRATION

In the whole data set find a file with smallest Imin/Imax



Regenerate fit curve  $f(x)$  with errors  
for the calibration file  
substituting zeros  $a_0$  and  $a_4$

Convolute fit with Gaussian distribution as  
follows

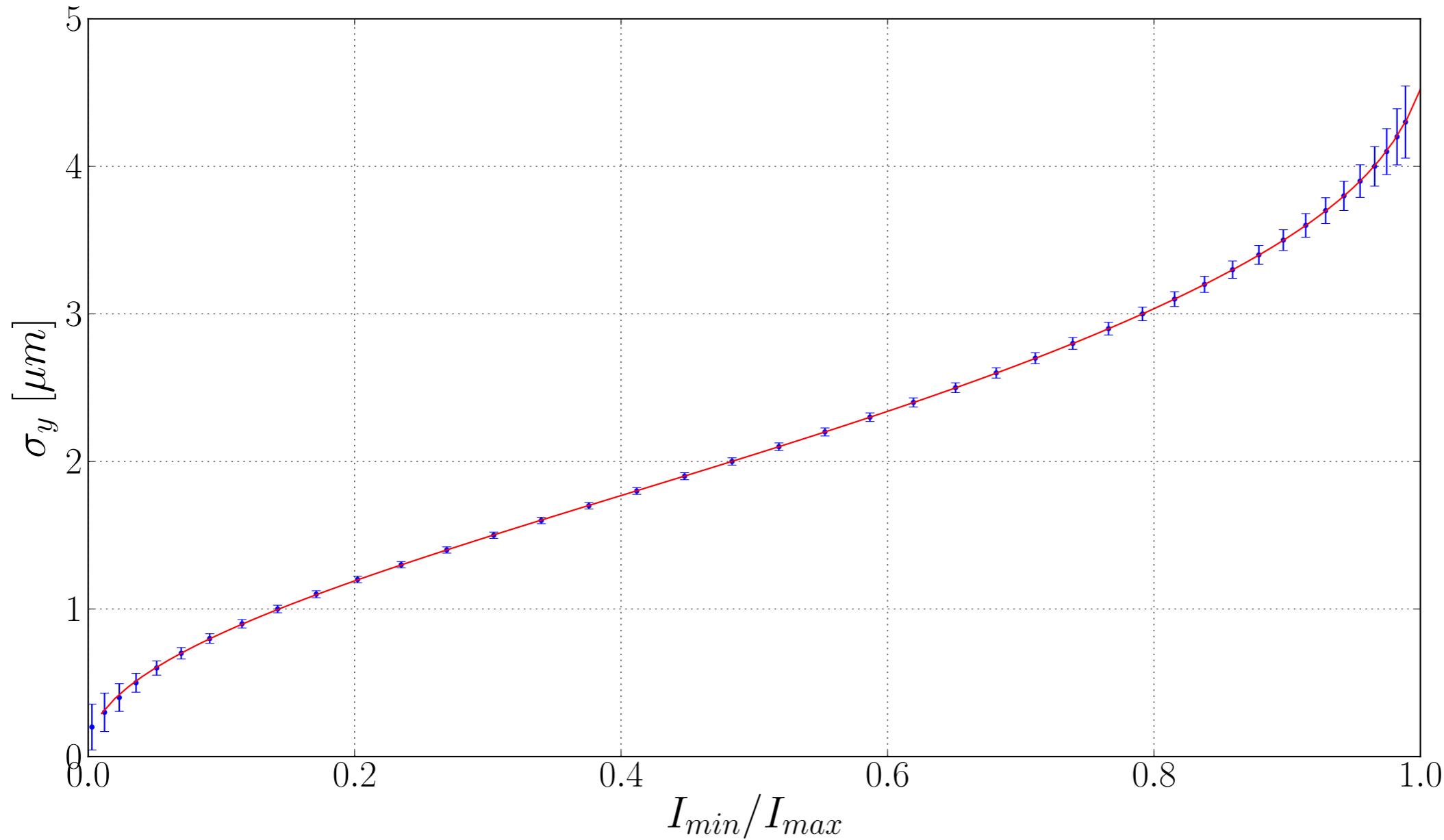
$$F(x_j) = \frac{\sum_{i=1}^N f(x_i) \exp\left(\frac{-(x_j - x_i)^2}{2\sigma^2}\right)}{\sum_{i=1}^N \exp\left(\frac{-(x_j - x_i)^2}{2\sigma^2}\right)}$$

Propagate errors through convolution.

Repeat convolution N times varying  $\sigma$  from 0 to  $\sigma_m$  with a fine step.

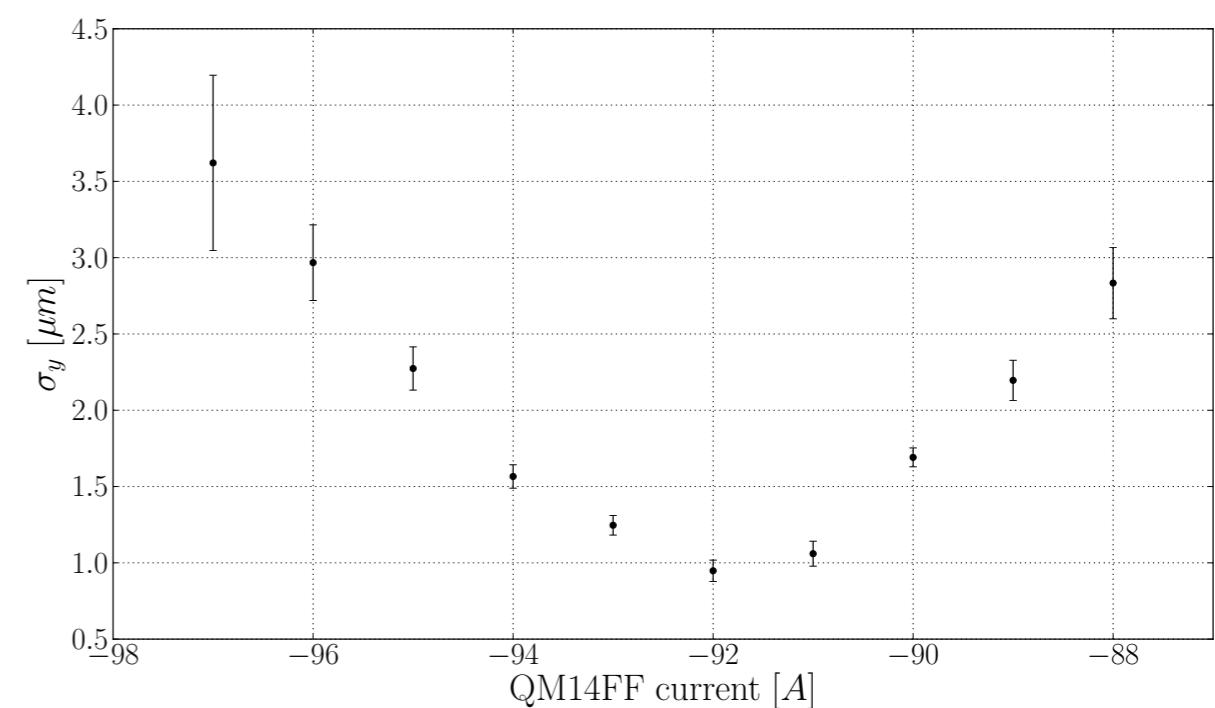
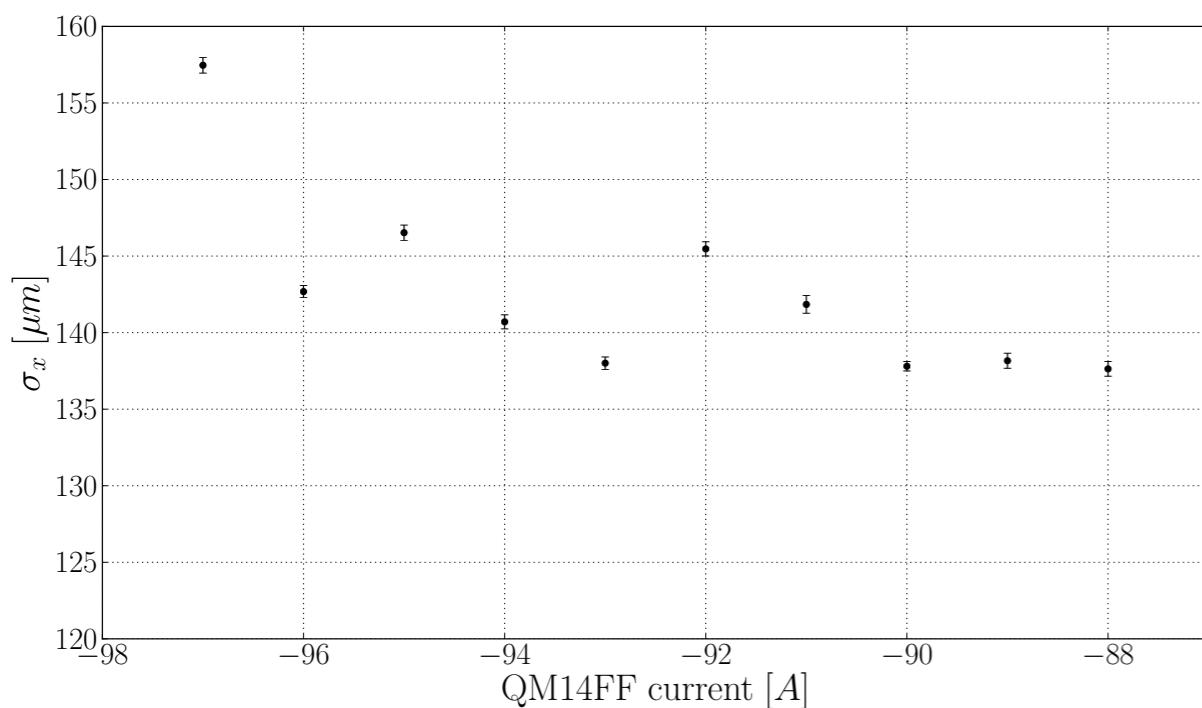
For each iteration, find Imin/Imax and calculate its  
errors resulting in calibration curve

# SELF-CALIBRATION

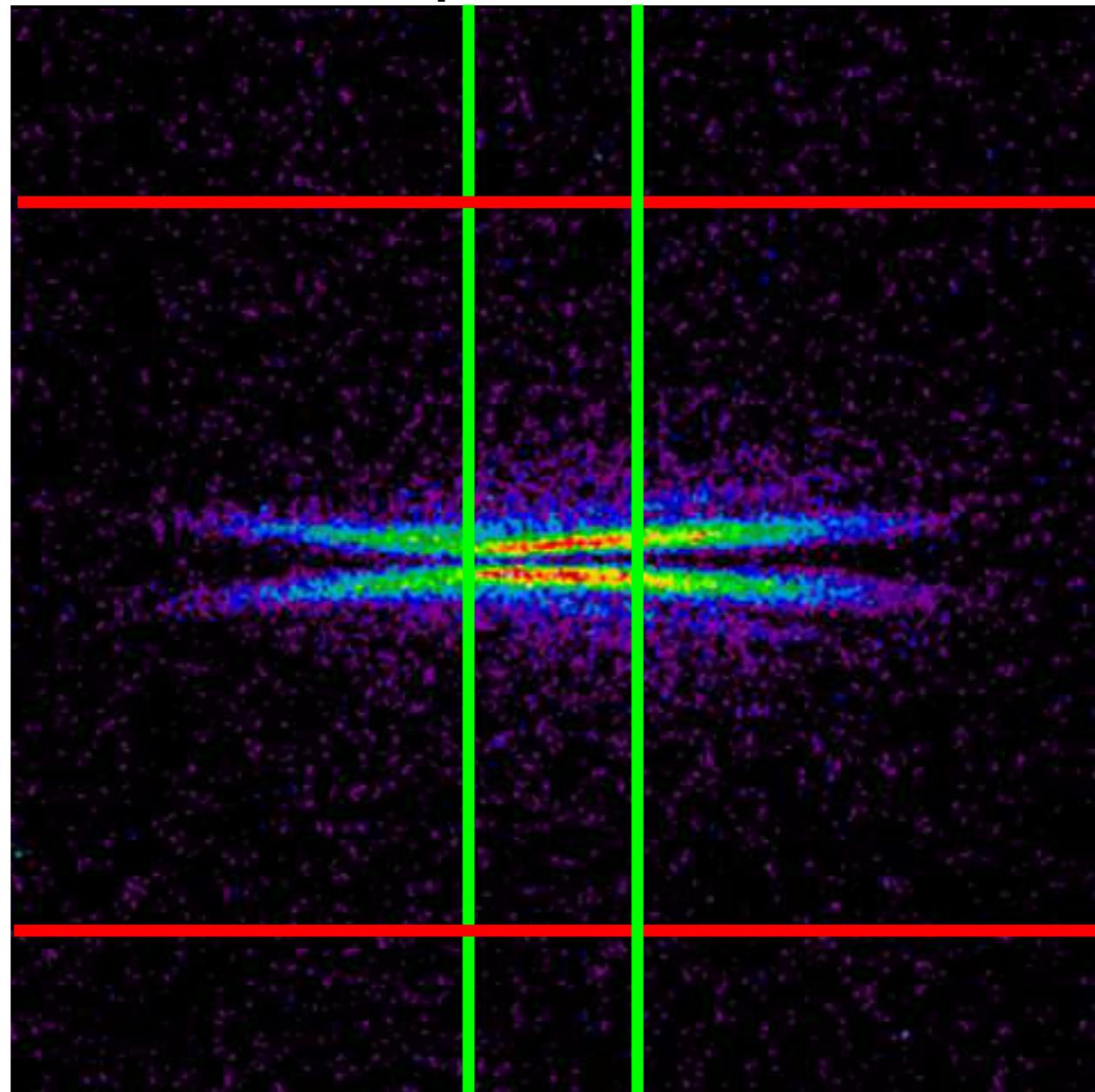


$$f(x) = a_0 + \frac{1}{a_1} \left( -\ln \left( 1 - \frac{x}{a_2} \right) \right)^{a_3} + a_4 x^{12}$$

# QUAD SCAN



# GAP SIZE



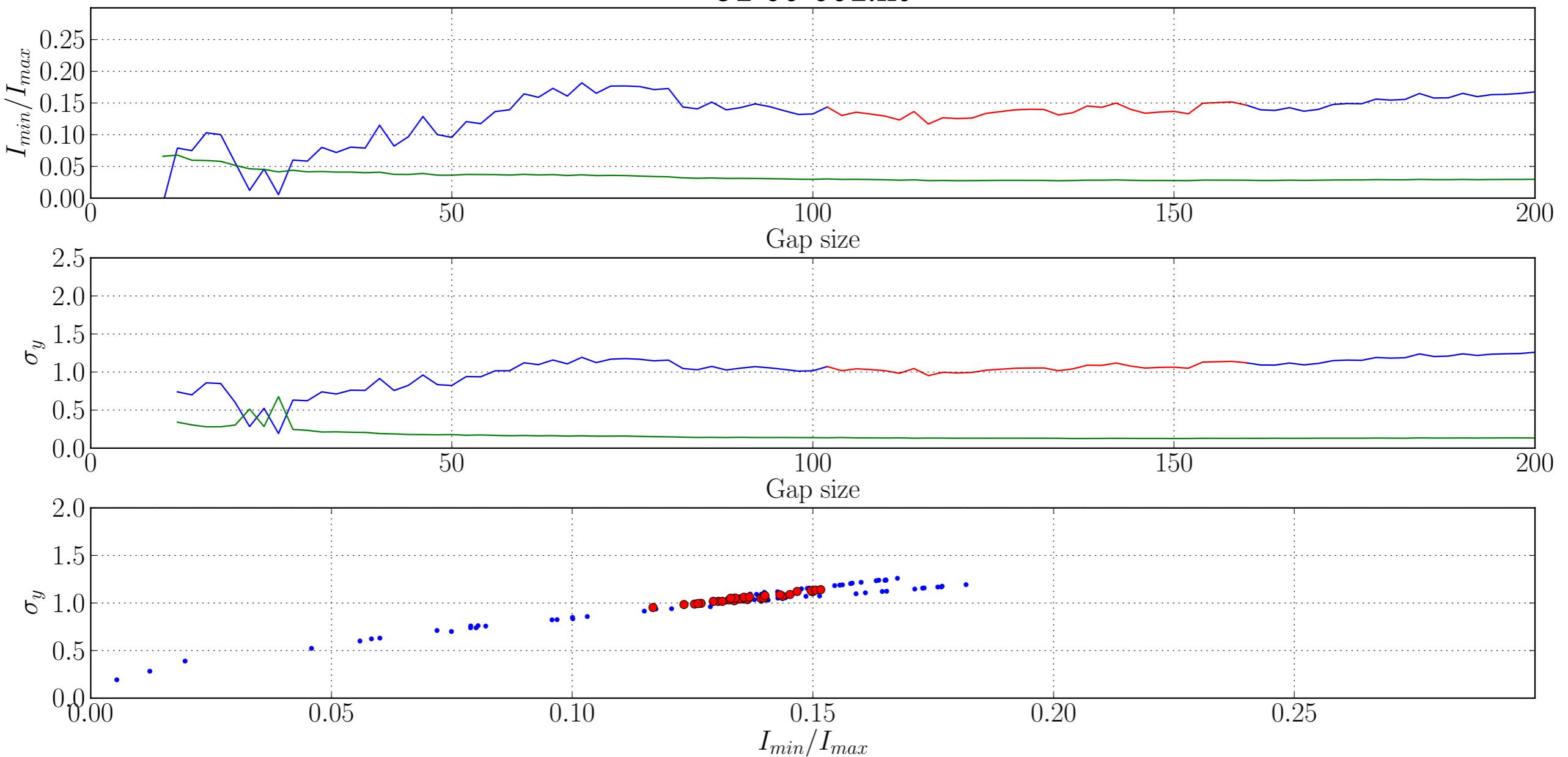
↔  
Gap

The choice of gap size affects the contrast ratio and beam size

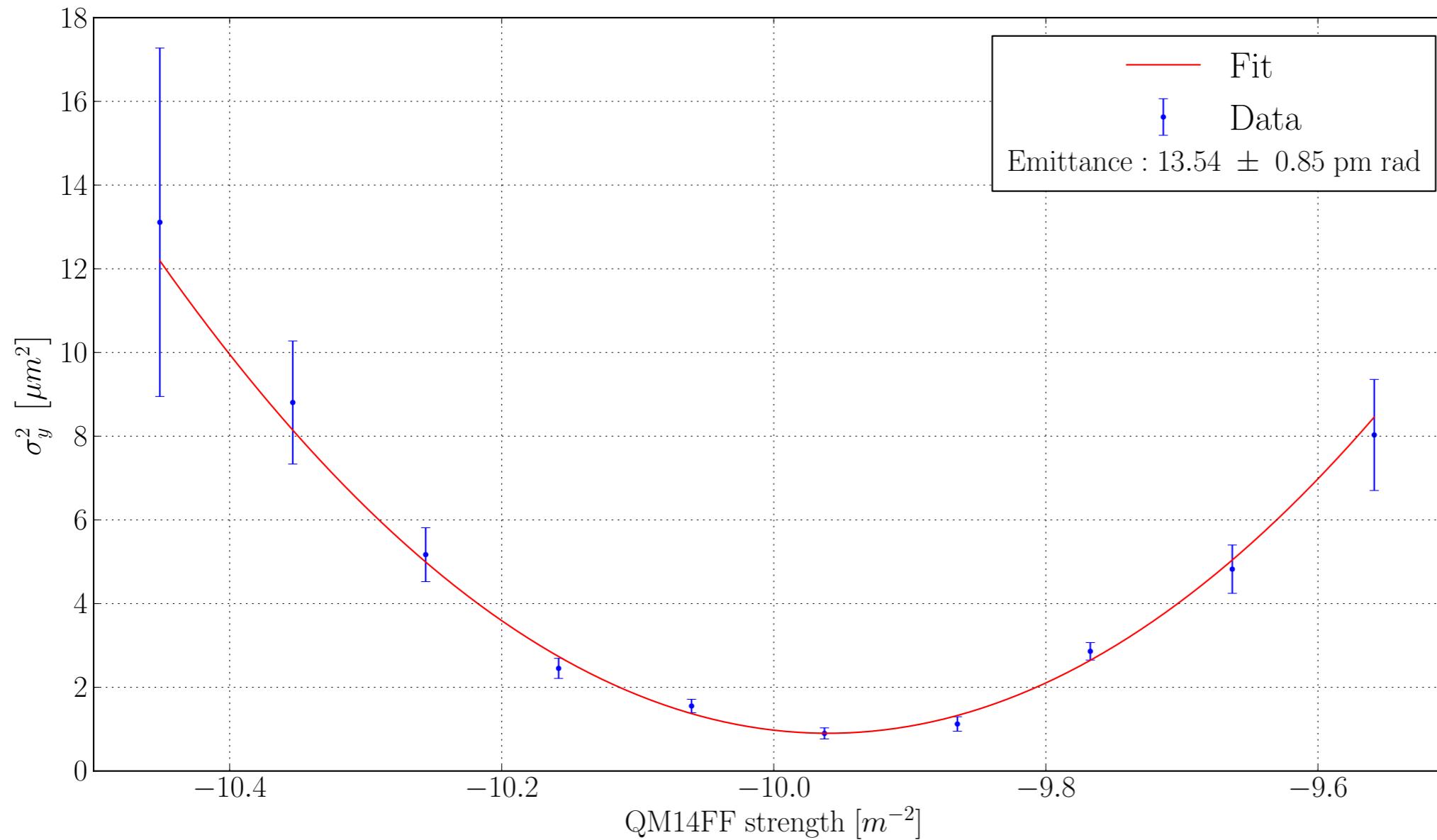
- too small leads to large error
- too big systematically adds more noise

# CURSOR SIZE

91-00-001.fit



# EMITTANCE



# SUMMARY

- No new data taken since spring 2013
- Focus on data analysis
  - Analysis code converted to python for future project
  - Choice of window size
  - emittance calculation
- Plan to publish paper to Journal of Instrumentation